

SAPTHAGIRI NPS UNIVERSITY
BE 1st Semester 2024-25
Third Internal Assessment Test

Course Code: 24BEPHY102
Course: Linear Algebra and Calculus
Time: 90mins

Semester: I
SRN:
Max Marks : 50

PART –A

Answer any Ten of the following

2x10=20

1. Define symmetric functions with examples.
2. If $u = 3x^2y + 6xy^2 + 7$ find $\frac{\partial u}{\partial x}$ and $\frac{\partial u}{\partial y}$.
3. If $f(x, y) = x^2y + 3xy^2$, find $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$.
4. State Euler's theorem for homogeneous function of two variables.
5. Write the total derivative formula for the function $u = f(x, y)$ where, $x = x(t)$ and $y = y(t)$.
6. If $z = u^2 + v^2$, $u = at$ and $v = 2at$. Find $\frac{dz}{dt}$.
7. Write the formula for Jacobian $J \left[\frac{u,v,w}{x,y,z} \right]$.
8. If $u = x + y$, $v = x - y$, find $J \left[\frac{u,v}{x,y} \right]$.
9. Evaluate $\int_{y=0}^2 \int_{x=0}^1 xy \, dx \, dy$.
10. Evaluate $\int_0^1 \int_1^2 (x + 3) \, dx \, dy$.
11. Find the value of $\int_0^1 \int_0^x (2x + y) \, dy \, dx$.
12. Evaluate $\int_2^1 \int_0^1 (y + 4) \, dy \, dx$.

PART –B

Answer any Four of the following

5 x 4 =20

1. If $u = e^{ax-by} \sin(ax + by)$, show that $b \frac{\partial u}{\partial x} - a \frac{\partial u}{\partial y} = 2abu$.
2. If $u = \sin^{-1} \left(\frac{x^2+y^2}{x+y} \right)$, show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \tan u$.
3. If $u = x^2 + y^2 + z^2$, $v = xy + yz + zx$, $w = x + y + z$, find $\frac{\partial(u,v,w)}{\partial(x,y,z)}$.
4. Evaluate $\int_0^1 \int_0^x (x^2 + y^2) \, dy \, dx$.
5. Evaluate $\int_1^2 \int_0^{2-y} xy \, dx \, dy$.

PART – C

Answer any One of the following

10 x 1=10

1. If $u = \log \left(\frac{x^2+y^2}{x+y} \right)$, show that $xu_x + yu_y = 1$.
2. If $u = x + 3y^2 - z^3$, $v = 4x^2yz$, $w = 2z^2 - xy$ find $\frac{\partial(u,v,w)}{\partial(x,y,z)}$ at $(1, -1, 0)$.