SEIR-C: An epidemic model that includes contact tracing

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The SEIR model has been widely used to study the dynamics of pandemics. Here we update the model to include the effects of contact tracing as a means to control the outbreak. We call this new model SEIR-C.

DESCRIPTION OF MODEL

Here we modify the SEIR model to include contact tracing and testing...

Conventions and notation

The populations are divided into those who participate in contact tracing and those who do not. During each phase of the disease progression, there is never a transfer of population from the group that is contact tracing and those who are not. We denote any population, J, that does not contact trace with a bar (\bar{J}) and those who do contact trace with a dot (J).

In this model, anyone who is notified of a potential exposure through contact tracing is quarantined for some average time τ_{iso} . During this time, their R_0 is reduced by a fraction d_r , making them far less likely to be exposed to the virus if they are susceptible, or much less likely to infect others if they are infectious. Testing can also take place. The average probability that someone in the general population is selected for testing is p_t . Later on we will allow for different testing rates for those who have been identified as being potentially exposed through contact tracing (p_t^t) , those who show symptoms while infectious (p_t^i) , and those who develop severe symptoms (p_t^{sev}) . We can also account for tests that return false positives (f_{pos}) and false negatives (f_{neg}) , as well as the time it takes to get the test results (τ_t) As in the basic SEIR model, the average time spent in the exposure phase is τ_{inc} , and the time spend in the infectious phase is τ_{inf} . Instead of a monolithic recovery phase, we consider several different subpopulations. There are those who are asymptomatic, those with mild infections, those with severe infections that lead to hospitalizations, and those who die after being hospitalized.

II. SUSCEPTIBLE

The rate of change equations for the susceptible populations that are not contact tracing (\bar{S}) are given as:

$$\frac{d\bar{S}}{dt} = \bar{S}_{m} \cdot \bar{S},\tag{1}$$

where:

$$\bar{S}_{m} = \begin{bmatrix}
-\gamma' - p_{t} & \frac{(1 - f_{pos})}{\tau_{t}} & \frac{1}{\tau_{iso}} \\
p_{t} & -\frac{1}{\tau_{t}} - d_{r}\gamma' & 0 \\
0 & \frac{f_{pos}}{\tau_{t}} & -d_{r}\gamma'
\end{bmatrix}$$

$$\bar{S} = \begin{bmatrix}
\bar{S}_{g} \\
\bar{S}_{w} \\
\bar{S}_{t}
\end{bmatrix}$$
(2)

$$\bar{S} = \begin{bmatrix} \bar{S}_g \\ \bar{S}_w \\ \bar{S}_t \end{bmatrix} \tag{3}$$

(4)

Here @TODO explain terms.

The rate of change of the susceptible populations that are participating in contact tracing (\hat{S}) are given as:

$$\frac{d\check{S}}{dt} = \check{S}_{m} \cdot \check{S},\tag{5}$$

where:

$$\tilde{\mathbf{S}}_{m} = \begin{bmatrix}
-\gamma' - \gamma_{false}^{c} - p_{t} & \frac{1}{\tau_{iso}} & \frac{(1 - f_{pos})}{\tau_{t}} & \frac{1}{\tau_{iso}} \\
\gamma_{false}^{c} & -p_{t}^{c} - \frac{1}{\tau_{iso}} - d_{r}\gamma' & 0 & 0 \\
p_{t} & p_{t}^{c} & -\frac{1}{\tau_{t}} - d_{r}\gamma' & 0 \\
0 & 0 & \frac{f_{pos}}{\tau_{t}} - \frac{1}{\tau_{iso}} - d_{r}\gamma'
\end{bmatrix},$$
(6)

$$\check{S} = \begin{bmatrix}
\check{S}_g \\
\check{S}_q \\
\check{S}_w \\
\check{S}_n
\end{bmatrix}$$
(7)

III. EXPOSURE

The rate of change equations for the exposed populations that are not contact tracing (\bar{S}) are given as:

$$\frac{d\bar{E}}{dt} = \bar{E}_{m} \cdot \bar{E} + T_{\bar{S}\bar{E}}\bar{S}, \tag{8}$$

where:

$$\bar{E}_{m} = \begin{bmatrix} -p_{t} - \frac{1}{\tau_{inc}} & \frac{(1 - f_{neg})}{\tau_{t}} & \frac{1}{\tau_{iso}} \\ p_{t} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{inc}} & 0 \\ 0 & \frac{f_{neg}}{\tau_{t}} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{inc}} \end{bmatrix}$$
(9)

$$\bar{E} = \begin{bmatrix} \bar{E}_g \\ \bar{E}_w \\ \bar{E}_t \end{bmatrix}$$

$$(10)$$

$$T_{\bar{S}\bar{E}} = \begin{bmatrix} \gamma' & 0 & 0\\ 0 & d_r \gamma' & 0\\ 0 & 0 & d_r \gamma' \end{bmatrix}. \tag{11}$$

For the exposed population participating in contact tracing we have:

$$\frac{d\check{E}}{dt} = \check{E}_{m} \cdot \check{E} + T_{\check{S}\check{E}}\check{S},\tag{12}$$

where:

$$\mathbf{\check{E}}_{m} = \begin{bmatrix}
-\gamma_{false}^{c} - \gamma_{true}^{c} - p_{t} - \frac{1}{\tau_{inc}} & \frac{1}{\tau_{iso}} & \frac{1}{\tau_{iso}} \\
\gamma_{false}^{c} + \gamma_{true}^{c} & -p_{t}^{c} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{inc}} & 0 & 0 \\
p_{t} & p_{t}^{c} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{inc}} & 0 \\
0 & 0 & \frac{(1 - f_{neg})}{\tau_{t}} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{inc}}
\end{bmatrix},$$
(13)

$$\check{E} = \begin{bmatrix}
\check{E}_g \\
\check{E}_q \\
\check{E}_w \\
\check{E}_n
\end{bmatrix},$$
(14)

$$T_{\tilde{S}\tilde{E}} = \begin{bmatrix} \gamma' & 0 & 0 & 0 \\ 0 & d_r \gamma' & 0 & 0 \\ 0 & 0 & d_r \gamma' & 0 \\ 0 & 0 & 0 & d_r \gamma' \end{bmatrix}. \tag{15}$$

IV. INFECTIOUS

In the infectious population, we must consider that a certain percentage of those infected (p_a) will be asymptomatic. Those who display no symptoms will not be as likely to be tested, and will be more difficult to quarantine. The asymptomatic individuals will be split between those who contact trace and those who do not. We denote those who are asymptomatic with a superscript a.

A. Individuals who are infectious and display symptoms

First we consider those who display symptoms, but don't contact trace:

$$\frac{d\bar{I}}{dt} = \bar{I}_{m} \cdot \bar{I} + \frac{(1 - p_{a})}{\tau_{inc}} \mathbb{1} \cdot \bar{E}, \tag{16}$$

where:

$$\bar{\mathbf{I}}_{m} = \begin{bmatrix} -p_{t}^{i} - \frac{1}{\tau_{inf}} & \frac{f_{neg}}{\tau_{t}} & \frac{1}{\tau_{iso}} \\ p_{t}^{i} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{inf}} & 0 \\ 0 & \frac{(1 - f_{neg})}{\tau_{t}} & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{inf}} \end{bmatrix},$$
(17)

$$\bar{I} = \begin{bmatrix} \bar{I}_g \\ \bar{I}_w \\ \bar{I}_t \end{bmatrix}, \tag{18}$$

(19)

and the idenity matrix is represented as 1.

Those who participate in contact tracing, are infectious, and display symptoms:

$$\frac{d\check{I}}{dt} = \check{I}_{m}\check{I} + \frac{(1 - p_{a})}{\tau_{inc}} \mathbb{1} \cdot \check{E}, \tag{20}$$

where:

$$\tilde{\boldsymbol{I}}_{m} = \begin{bmatrix}
-\gamma_{false}^{c} - \gamma_{true}^{c} - p_{t}^{i} - \frac{1}{\tau_{inf}} & \frac{1}{\tau_{iso}} & \frac{1}{\tau_{iso}} & \frac{1}{\tau_{iso}} & \frac{1}{\tau_{iso}} \\
\gamma_{false}^{c} + \gamma_{true}^{c} & -p_{t}^{n} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{inf}} & 0 & 0 & 0 \\
p_{t}^{i} & p_{t}^{n} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{inf}} & 0 & 0 \\
0 & 0 & \frac{(1-f_{neg})}{\tau_{t}} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{inf}} & 0 \\
0 & 0 & 0 & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{inf}}
\end{bmatrix}, (21)$$

$$\check{I} = \begin{bmatrix}
\check{I}_g \\
\check{I}_q \\
\check{I}_w \\
\check{I}_n \\
\check{I}_{n'}
\end{bmatrix},$$
(22)

B. Asymptomatic

For those who are asymptomatic, we first look at the group that does not participate in contact tracing:

$$\frac{dI^a}{dt} = \bar{I}_m^a \cdot \bar{I}^a + \frac{p_a}{\tau_{inc}} \mathbb{1} \cdot \bar{E}, \tag{23}$$

$$\bar{I}_{m}^{a} = \bar{I}_{m}, \tag{24}$$

$$\bar{I}^a = \begin{bmatrix} \bar{I}_g^a \\ \bar{I}_w^a \\ \bar{I}_t^a \end{bmatrix}, \tag{25}$$

Finally, we have those who are asymptomatic but are participating in contact tracing:

$$\frac{d\check{I}^a}{dt} = \check{I}^a_m \cdot \check{I}^a + \frac{p_a}{\tau_{inc}} \mathbb{1} \cdot \check{E}, \tag{26}$$

$$\check{I}_{m}^{a} = \check{I}_{m}, \tag{27}$$

$$\check{I} = \begin{bmatrix}
\check{I}_g^a \\
\check{I}_q^a \\
\check{I}_w^a \\
\check{I}_n^a \\
\check{I}_{n'}^a
\end{bmatrix}$$
(28)

OUTCOMES

This is part of the R section in a traditional SEIR model. We divide this into several transition times as it make take a patient some time to recover after they are infectious (and therefore still test positive). We divide these up into those who are asymptomatic, mild, and severe. Those who are severe have a chance p_h of needing hospitalization or making a recovery R. Those who are hospitalized can recover R or die D. We denote the intermetiate states where someone is in the recovery process O for outcomes.

Asymptomatic

Those who are asymptomatic, but not participating in contact tracing, have a population that changes:

$$\frac{d\bar{A}}{dt} = \bar{A}_{m} \cdot \bar{A} + \frac{1}{\tau_{inf}} \mathbb{1} \cdot \bar{I}^{a}, \tag{29}$$

where:

$$\bar{A}_{m} = \begin{bmatrix}
-p_{t} - \frac{1}{\tau_{a}} & \frac{f_{neg}}{\tau_{t}} & \frac{1}{\tau_{iso}} \\
p_{t} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{a}} & 0 \\
0 & \frac{(1 - f_{neg})}{\tau_{t}} & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{a}}
\end{bmatrix},$$

$$\bar{A} = \begin{bmatrix} \bar{A}_{g} \\ \bar{A}_{w} \\ \bar{A}_{t} \end{bmatrix}.$$
(30)

$$\bar{A} = \begin{bmatrix} \bar{A}_g \\ \bar{A}_w \\ \bar{A}_t \end{bmatrix} . \tag{31}$$

(32)

Those who are participating in contact tracing, but are asymptomatic have the following population change as a function of time:

$$\frac{d\mathring{A}}{dt} = \check{A}_{m} \cdot \check{A} + \frac{1}{\tau_{inf}} \mathbb{1} \cdot \check{I}^{a}, \tag{33}$$

where:

$$\check{\mathbf{A}}_{m} = \begin{bmatrix}
-\gamma_{false}^{c} - \gamma_{true}^{c} - p_{t} - \frac{1}{\tau_{a}} & \frac{1}{\tau_{iso}} & \frac{f_{neg}}{\tau_{t}} & \frac{1}{\tau_{iso}} & \frac{1}{\tau_{iso}} \\
\gamma_{false}^{c} + \gamma_{true}^{c} & -p_{t}^{c} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{a}} & 0 & 0 & 0 \\
p_{t} & p_{t}^{c} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{a}} & 0 & 0 & 0 \\
0 & 0 & \frac{(1-f_{neg})}{\tau_{t}} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{a}} & 0 & 0 \\
0 & 0 & 0 & 0 & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{a}}
\end{bmatrix}, (34)$$

$$\check{A} = \begin{bmatrix}
\check{A}_g \\
\check{A}_q \\
\check{A}_n \\
\check{A}_{n'}
\end{bmatrix}.$$
(35)

(36)

We must track each of these subpopulations. Even though no one in A is still infectious, they can still test positive and thereby notify others that they need to quarantine themselves (including those who they may have infected).

1. Mild

We now deal with the infectious population who develop a mild case (show symptoms), but do not need hospitalization and do not die. These individual recover in a time τ_{mild} , and make up p_{mild} fraction of total infectious cases. Asymptomatic individuals cannot be included in this group. Since we are looking at a subpoulation who aren't asymptomatic, we must account for this. The fraction of nonasymptomatic individuals who develop mild cases is given as:

$$p_m = \frac{p_{mild}}{(1 - p_a)}. (37)$$

For those who develop mild cases and do not participate in contact tracing we have:

$$\frac{d\bar{M}}{dt} = \bar{M}_{m} \cdot \bar{M} + \frac{p_{m}}{\tau_{inf}} \mathbb{1} \cdot \bar{I}, \tag{38}$$

where:

$$\bar{M}_{m} = \begin{bmatrix}
-p_{t} - \frac{1}{\tau_{mild}} & \frac{f_{neg}}{\tau_{t}} & \frac{1}{\tau_{iso}} \\
p_{t} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{mild}} & 0 \\
0 & \frac{(1 - f_{neg})}{\tau_{t}} & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{mild}}
\end{bmatrix},$$

$$\bar{M} = \begin{bmatrix}
\bar{M}_{g} \\
\bar{M}_{w} \\
\bar{M}_{t}
\end{bmatrix}.$$
(39)

$$\bar{M} = \begin{bmatrix} \bar{M}_g \\ \bar{M}_w \\ \bar{M}_t \end{bmatrix} . \tag{40}$$

(41)

Finally, for those who develop mild cases and contact trace:

$$\frac{d\tilde{M}}{dt} = \tilde{M}_{m} \cdot \tilde{M} + \frac{p_{m}}{\tau_{inf}} \mathbb{1} \cdot \tilde{I}, \tag{42}$$

where:

$$\tilde{\boldsymbol{M}}_{m} = \begin{bmatrix}
-\gamma_{false}^{c} - \gamma_{true}^{c} - p_{t} - \frac{1}{\tau_{mild}} & \frac{1}{\tau_{iso}} & \frac{f_{neg}}{\tau_{t}} & \frac{1}{\tau_{iso}} & \frac{1}{\tau_{iso}} \\
\gamma_{false}^{c} + \gamma_{true}^{c} & -p_{t}^{c} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{mild}} & 0 & 0 & 0 \\
p_{t} & p_{t}^{c} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{mild}} & 0 & 0 & 0 \\
0 & 0 & \frac{(1 - f_{neg})}{\tau_{t}} - \frac{1}{\tau_{iso}} - \frac{1}{\tau_{mild}} & 0 & 0 \\
0 & 0 & 0 & 0 & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{mild}}
\end{bmatrix}, (43)$$

$$\check{M} = \begin{bmatrix}
\check{M}_g \\
\check{M}_q \\
\check{M}_w \\
\check{M}_n \\
\check{M}_{n'}
\end{bmatrix} .$$
(44)

(45)

В. Severe

The final group we must consider are those who are severe cases. These represent the following fraction of the symptomatic cases that are severe:

$$p_{sev} = 1 - p_m, \tag{46}$$

and lead to hospitalization some time τ_h after they cease to be infectious. We also assume that anyone in the severe category will be tested at a rate p_t^{sev} regardless of whether they have been notified of a potential contact Those hospitalized will either recover or die. Those who do not participate in contact tracing can be descibed by the following dynamics:

$$\frac{d\bar{X}}{dt} = \bar{X}_{m} \cdot \bar{X} + \frac{p_{sev}}{\tau_{inf}} \mathbb{1} \cdot \bar{I}, \tag{47}$$

where:

$$\bar{\mathbf{X}}_{m} = \begin{bmatrix} -p_{t}^{sev} - \frac{1}{\tau_{h}} & \frac{f_{neg}}{\tau_{t}} & \frac{1}{\tau_{iso}} \\ p_{t}^{sev} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{h}} & 0 \\ 0 & \frac{(1 - f_{neg})}{\tau_{t}} & -\frac{1}{\tau_{iso}} - \frac{1}{\tau_{h}} \end{bmatrix},$$

$$(48)$$

$$\bar{X} = \begin{bmatrix} X_g \\ \bar{X}_w \\ \bar{X}_t \end{bmatrix} . \tag{49}$$

(50)

For those who do participate in contact tracing but develop severe symptoms we have:

$$\frac{d\check{X}}{dt} = \check{X}_{m} \cdot \check{X} + \frac{p_{sev}}{\tau_{inf}} \mathbb{1} \cdot \check{I}, \tag{51}$$

where:

$$\check{\boldsymbol{X}}_{m} = \begin{bmatrix}
-p_{t}^{sev} - \frac{1}{\tau_{h}} & \frac{f_{neg}}{\tau_{t}} & 0 & 0 \\
p_{t}^{sev} & -\frac{1}{\tau_{t}} - \frac{1}{\tau_{h}} & 0 & 0 \\
0 & \frac{(1-f_{neg})}{\tau_{t}} & -\frac{1}{\tau_{h}} & 0 \\
0 & 0 & 0 & -\frac{1}{\tau_{h}}
\end{bmatrix},$$
(52)

$$\check{D} = \begin{bmatrix}
\check{D}_g \\
\check{D}_w \\
\check{D}_n \\
\check{D}_{n'}
\end{bmatrix},$$
(53)

(54)

1. Hospitalized

Those that are hospitalized The population dynamics for those hospitalized who are not contact tracing is given as:

$$\frac{d\bar{H}}{dt} = \bar{H}_{m} \cdot \bar{H} + \frac{1}{\tau_{h}} \mathbb{1} \cdot \bar{X}, \tag{55}$$

where:

$$\bar{\boldsymbol{H}}_{\boldsymbol{m}} = \begin{bmatrix} -p_t^{sev} - \gamma^{sev} & \frac{f_{neg}}{\tau_t} & 0\\ p_t^{sev} & \frac{1}{\tau_t} - \gamma^{sev} & 0\\ 0 & \frac{(1 - f_{neg})}{\tau_t} & -\gamma^{sev} \end{bmatrix},$$
(56)

$$\bar{H} = \begin{bmatrix} \bar{H}_g \\ \bar{H}_w \\ \bar{H}_t \end{bmatrix} . \tag{57}$$

(58)

Those who participate in contact tracing and are hospitalized automatically notify all of their prior contacts regardless if they have been tested. There is no effect if they are notified of a potential contact.

$$\frac{d\check{H}}{dt} = \check{H}_{m} \cdot \check{H} + \frac{1}{\tau_{h}} \mathbb{1} \cdot \check{X}, \tag{59}$$

$$\check{\boldsymbol{H}}_{m} = \begin{bmatrix}
-p_{t}^{sev} - \gamma^{sev} & \frac{f_{neg}}{\tau_{t}} & 0 & 0 \\
p_{t}^{sev} & -\frac{1}{\tau_{t}} - \gamma^{sev} & 0 & 0 \\
0 & \frac{(1 - f_{neg})}{\tau_{t}} & -\gamma^{sev} & 0 \\
0 & 0 & 0 & -\gamma^{sev}
\end{bmatrix},$$
(60)

$$\check{H} = \begin{bmatrix}
\check{H}_g \\
\check{H}_w \\
\check{H}_n \\
\check{H}_{n'}
\end{bmatrix},$$
(61)

(62)

C. Deaths

In this model, only those who are hospitalized have a probability p_d of dying. We will split the population of potential deaths into those who died and were contact tracing and those who died but were not. The two equations

describing the death rate are:

$$\frac{d\bar{D}}{dt} = \frac{p_d}{\tau_d} \mathbb{1} \cdot \bar{H},\tag{63}$$

$$\frac{d\check{D}}{dt} = \frac{p_d}{\tau_d} \mathbb{1} \cdot \check{H}. \tag{64}$$

To find p_d , we must use the case fatality rate, C_{FR} to figure out the percantage of those hospitalized that will die. Since the case fatality rate applies to all infections, the probability of those who are hospitalized dying is:

$$p_d = \frac{C_{FR}}{1 - p_a - p_{mild}}. (65)$$

D. Recovery

Finally, we consider those who recover and are now considered immune. Again we consider those who recover and contact trace and those who abstain. For the non participants we have:

$$\frac{d\bar{R}}{dt} = \frac{(1 - p_d)}{\tau_{sev}} \mathbb{1} \cdot \bar{H} + \frac{1}{\tau_{mild}} \mathbb{1} \cdot \bar{M} + \frac{1}{\tau_a} \mathbb{1} \cdot \bar{A},\tag{66}$$

and for those who do participate in contact tracing the recovery rate is:

$$\frac{d\check{R}}{dt} = \frac{(1 - p_d)}{\tau_{sev}} \mathbb{1} \cdot \check{H} + \frac{1}{\tau_{mild}} \mathbb{1} \cdot \check{M} + \frac{1}{\tau_a} \mathbb{1} \cdot \check{A}, \tag{67}$$

Now for the mega array composed of smaller populations:

$$\gamma_{false}^c = \beta_c(\check{S}_n + \check{E}_n + \check{I}_{n'} + \check{I}_{n'}^a + \check{R}_{n'}) + \frac{(R_c - R_0)}{\tau_c}(\check{I}_n + \check{I}_n^a + \check{R}_n), \tag{68}$$

$$\gamma_{true}^c = \beta_0(\check{I}_n + \check{I}_n^a + \check{R}_n), \tag{69}$$

$$\check{R}_{n'} = \check{A}_{n'} + \check{M}_{n'} + \check{X}_{n'} + \check{H}_{n'}, \tag{70}$$

$$\check{\mathbf{R}}_{n} = \check{A}_{n} + \check{M}_{n} + \check{X}_{n} + \check{H}_{g} + \check{H}_{w} + \check{H}_{n} \tag{71}$$

TABLE I. Parameter List

Parameter	Definition	
Average time parameters		
$ au_{iso}$	Time spent in isolation after a contact or positive test	
$ au_{inc}$	Incubation time. Length of time spent in the exposed phase.	
$ au_{inf}$	Amount of time spent infectious.	
$ au_a$	Amount of time it takes someone asymptomatic to recover after leaving infectious phase	
$ au_{mild}$	Amount of time it takes someone with mild symptoms to recover after leaving infectious phase	
$ au_h$	Average time before someone with severe symptoms enters the hospital.	
$ au_{sev}$	Amount of time it takes someone with severe symptoms to recover after entering the hospital.	
$ au_d$	Amount of time it takes someone to die who is in the hospital.	
$ au_c$	Average time over which to consider notifying those who someone infectious has made contact with.	

$Testing\ parameters$

$ au_t$	Average time it takes to return a test result.
f_{neg}	Fraction of tests that return a false negative.
f_{pos}	Fraction of tests that return a false positive.
p_t	Probability that someone in the general population gets tested (not showing symptoms or isolating)
p_t^c	Probability that someone who is notified of a possible infectious contact event is tested.
p_t^i	Probability that someone in the infectious phase showing symptoms is tested.
p_t^n	The greater of p_c^c , p_t^i , or p_t .
p_t^{sev}	Probability that someone who is showing severe symptoms or is hospitalized is tested.

$Population\ percentages$

Fraction of the population participating in contact tracing. Fraction of the population that is asymptomatic p_c

 p_a

Infectious Rates

Trijectio de Tudece	
R_0	Reproduction rate
eta_0	$=rac{R_0}{ au_{inf}}$
d_r	The fraction that R_0 is reduced by those who are isolating through contact tracing or testing.
d_q	The fraction that R_0 is reduced due to stay-at-home orders.
$\gamma^{'}$	$=\beta_0(\bar{I}_{tot}+d_r\check{I}_{tot})$ The probability someone infectious spreads
R_c	Average number of individuals an infectious person has come in contact with in the past τ_c days.
β_c	Average number of total daily contacts someone infectious has made.
γ^c_{false}	Rate of false notifications of individuals who aren't infected.
γ^c_{true}	Rate of true notifications of individuals who have become infectious (contact tracing works).