

Jacobians.

$$\begin{aligned} \begin{bmatrix} V \\ W \end{bmatrix} &= g(q) \dot{q} \quad \left\{ \begin{array}{l} dx = \frac{\partial(L_1 c_1 + L_2 c_{12})}{\partial \theta_1} + \frac{\partial(L_1 c_1 + L_2 c_{12})}{\partial \theta_2} \\ dy = (-L_1 s_1 - L_2 s_{12}) d\theta_1 + (-L_1 s_{12}) d\theta_2 \end{array} \right. \\ x &= L_1 c_1 + L_2 c_{12} \quad \left\{ \begin{array}{l} dx = (-L_1 s_1 - L_2 s_{12}) d\theta_1 + (-L_1 s_{12}) d\theta_2 \\ dy = (L_1 c_1 + L_2 c_{12}) d\theta_1 + (L_2 c_{12}) d\theta_2 \end{array} \right. \\ y &= L_1 s_1 + L_2 s_{12} \quad \left| \begin{array}{c} dx = -L_1 s_{12} \\ dy = L_1 c_1 + L_2 c_{12} \end{array} \right| \left| \begin{array}{c} d\theta_1 \\ d\theta_2 \end{array} \right| \end{aligned}$$

$$\begin{vmatrix} dx \\ dy \end{vmatrix} = \begin{vmatrix} -2S(30) - 2S(30+50) & -2C(30+50) \\ 2C(30) + 2C(30+50) & 2C(30+50) \end{vmatrix} \begin{bmatrix} S \\ C \end{bmatrix}$$

$$\begin{vmatrix} dx \\ dy \end{vmatrix} = \begin{vmatrix} -2,96 & -1,96 \\ 2,08 & 0,35 \end{vmatrix} = \begin{vmatrix} -18,72 \\ 11,1 \end{vmatrix} \text{ N}$$

junta

$$J_i = \begin{bmatrix} \vec{z}_{i-1} \times (0_m - \vec{0}_{i-1}) \\ z_{i-1} \end{bmatrix} \quad J_i = \begin{bmatrix} z_{i-1} \\ 0 \end{bmatrix}$$

Rotacional Prismatico.

$$J = [J_1 \ J_2]$$

$$J = \begin{bmatrix} z_{0x}(\theta_2 - \theta_0) & z_{1x}(\theta_2 - \theta_1) \\ z_0 & z_1 \end{bmatrix}$$

link. a α d θ

0-1 a₁ 0 0 θ₁

1-2 a₂ 0 0 θ₂

$${}^0 A_1 = \begin{bmatrix} a_1 & -a_1 & 0 & a_1 c_1 \\ s_1 & c_1 & 0 & a_1 s_1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0 A_{12} = \begin{bmatrix} c_{12} & -s_{12} & 0 & a_2 c_{12} + a_1 c_1 \\ s_{12} & c_{12} & 0 & a_2 s_{12} + a_1 s_1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$Z_0 = R_0^0 K = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad D_2 = d_0^2 = \begin{bmatrix} a_2 c_{12} + a_1 c_1 \\ a_2 s_{12} + a_1 s_1 \end{bmatrix} \quad Z_1 = R_0^1 K = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$D_1 = d_0^1 = \begin{bmatrix} a_1 c_1 \\ a_1 s_1 \\ 0 \end{bmatrix} \quad D_0 = d_0^0 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$J = \begin{bmatrix} 0 & (a_2 c_{12} + a_1 c_1) & 0 \\ 0 & a_2 s_{12} + a_1 s_1 & 0 \\ 1 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$J = \left(\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \times \begin{bmatrix} 2,08 \\ 2,96 \\ 0 \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \right)$$

Exercício 2

Rank: $a_1 = 2$ e $a_2 = 2$, d. $\theta_1 = 90^\circ$

D-2 $a_3 = 2$ d. $\theta_2 = 30^\circ$ d. $\theta_1 = 90^\circ$

D-3 $a_3 = 2$ d. $\theta_3 = (-60)^\circ$

$${}^0A_1 = \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 0 \end{bmatrix}, \quad {}^0A_2 = \begin{bmatrix} -0,86 & 0,5 & 0 & -1,73 \\ 0 & 0 & 1 & 0 \\ -0,5 & 0,86 & 0 & 3 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \quad {}^0A_3 = \begin{bmatrix} -0,86 & -0,5 & 0 & -3,46 \\ 0 & 0 & 1 & 0 \\ -0,5 & 0,86 & 0 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$J = \begin{bmatrix} z_0 \times (\theta_3 - \theta_0) & z_1 \times (\theta_3 - \theta_1) & z_2 \times (\theta_3 - \theta_2) \\ z_1 & z_1 & z_2 \end{bmatrix}$$

$$Z_0 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad Z_1 = R_0^0 K = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad D_0 = d_0^0 = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \theta_3 = d_0^3 = \begin{bmatrix} -3,46 \\ 0 \\ 6 \end{bmatrix}$$

$$Z_2 = R_0^2 K = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad D_1 = d_0^1 = \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix}$$

$$\theta_2 = d_0^2 = \begin{bmatrix} -1,73 \\ 0 \\ 3 \end{bmatrix}$$

Jandaia

$$J = \begin{bmatrix} 0 & -3,46 & 0 \\ 0 & 0 & -0 \\ 1 & 2 & 0 \end{bmatrix} \times \begin{bmatrix} 0 & -3,46 & 0 \\ 1 & 0 & -0 \\ 0 & 2 & 0 \end{bmatrix} \times \begin{bmatrix} 0 & -3,46 & 1,87 \\ 1 & 0 & -0 \\ 0 & 2 & 3 \end{bmatrix}$$

$$\begin{array}{c} 0 \\ 0 \\ 1 \end{array} \quad \begin{array}{c} 0 \\ 1 \\ 0 \end{array} \quad \begin{array}{c} 0 \\ 0 \\ 0 \end{array}$$

$$\begin{bmatrix} v \\ w \end{bmatrix} = \begin{bmatrix} 0 & 0 & -1 \\ -3,46 & 0 & 0 \\ 0 & 3,46 & 1,73 \\ 0 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 4 \\ 3 \\ 1 \end{bmatrix} = \begin{bmatrix} -1 & 7\sqrt{2} \\ -13,84 + V_1 \\ 12,11 + V_2 \\ 0 + W_1 \\ 4 + W_2 \\ 4 + W_2 \end{bmatrix}$$

Resolución 2 (Ficha 8)

H₁²

$$H_1^2 = H_0^1 \cdot H_1^2$$

$$H_2^3 = H_0^1 \cdot H_1^2 \cdot H_2^3$$

Tutoriales Probótica 2º Parte.

Calculo do jacobiano.

$$J = [J_1 \ J_2 \ J_3 \ J_4 \ J_5 \ J_6]$$

$$J = \begin{bmatrix} 20 \times (0_6 - 0_0) & \dots & 25 \times (0_6 - 0_0) \\ 2_0 & 2_5 \end{bmatrix}$$

Tablas de Denavit-Hartenberg
substitucion ϕ

$$2_0 = 0_{03}$$

$$2_1 = 0_1$$

$$2_2 = 0_2$$

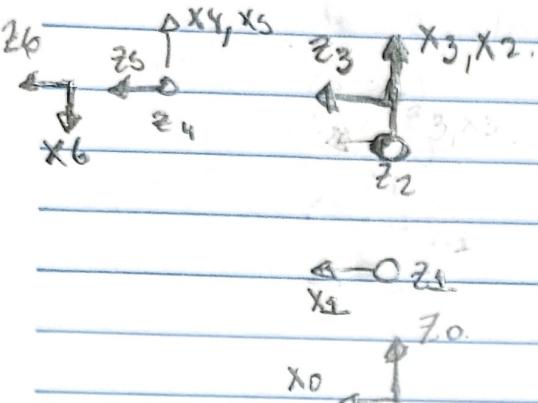
$$J = \begin{bmatrix} & & & & & \end{bmatrix}$$

a) sepa probiamo para.

$$\theta_1 = \dots$$

$$\theta_2 = \dots$$

b)



Dennavit - Hartenberg

link a num d ang

$$0-1 \quad 0$$

$$1-2 \quad \alpha_2$$

$$2-3 \quad \alpha_3$$

$$3-4$$

$$4-5$$

$$5-6$$

$$\dot{\theta}(t) = 10, 8t - 2, 16t^2$$

$$\theta(t) = C_0 + C_1 t + C_2 t^2 + C_3 t^3$$

$$\theta(t_0) = 30 = C_0 + C_1(0) + C_2(0)^2 + C_3(0)^3$$

$$\text{obs: } t_0 = 0 \quad [C_0 = 30]$$

$$\theta(t) = 75 = C_0 + C_1(s) + C_2(s)^2 + C_3(s)^3$$

$$t_f = 5 \quad 75 = 30 + 5C_1 + 25C_2 + 125C_3$$

$$5C_1 + 25C_2 + 125C_3 = 45$$

$$\dot{\theta}(t) = C_1 + 2C_2 t + 3C_3 t^2$$

$$\dot{\theta}(t) = 0 = C_1 + 2C_2(0) + 3C_3(0)^2$$

$$[C_1 = 0]$$

$$\ddot{\theta}(t) \leq 0 = C_2 + 2C_3 t + 3C_3 s^2$$

$$10C_2 + 75C_3 = 0$$

$$\begin{cases} 25C_2 + 125C_3 = 45 & | \times 5 \\ 10C_2 + 75C_3 = 0 & | \times 10 \end{cases} \Rightarrow \begin{cases} 125C_2 + 625C_3 = 225 \\ 100C_2 + 750C_3 = 0 \end{cases} \Rightarrow \begin{cases} 25C_2 = 225 \\ 100C_2 = 750 \end{cases} \Rightarrow \begin{cases} C_2 = 9 \\ C_2 = 7.5 \end{cases}$$

$$C_2 = 9$$

$$C_3 = -0.75$$

Exercício

$$\theta(t) = C_0 + C_1 t + C_2 t^2 + C_3 t^3$$

$$\theta(t_0) = 75 = C_0 + C_1(0) + C_2(0)^2 + C_3(0)^3$$

$$C_0 = 75$$

$$\dot{\theta}(t) = C_1 + 2C_2 t + 3C_3 t^2$$

$$\dot{\theta}(t) = 0 = C_1 + 2C_2(0) + 3C_3(0)^2$$

$$[C_1 = 0]$$

$$\theta(t_f) = 105 = C_0 + C_1(3) + C_2(3)^2 + C_3(3)^3$$

$$3C_1 + 9C_2 + 27C_3 = 30$$

$$\dot{\theta}(t) = 0 = C_1 + 2C_2(3) + 3(3)(3)^2$$

$$6C_2 + 27C_3 = 0$$

$$9C_2 + 27C_3 = 0 \Rightarrow C_2 = 10$$

$$6C_2 + 27C_3 = 0 \Rightarrow C_3 = -2.22$$

$$\theta(t) = 75 + 10t^2 - 2.22t^3$$

$$\theta(t) = 20t - 6.66t^2$$

Exercício 3

$$\theta(t) = C_0 + C_1 t + C_2 t^2 + C_3 t^3 + C_4 t^4 + C_5 t^5$$

cond. Iniciais $t_i=0 \quad t_f=5$

$$\theta(t_i) = 30 \quad \theta(t_f) = 75$$

$$\ddot{\theta}(t_i) = 3^\circ/\text{s} \quad \ddot{\theta}(t_f) = 5^\circ/\text{s}$$

$$\theta(t_i) = 30 = C_0 + C_1(0) + C_2(0)^2 + C_3(0)^3 + C_4(0)^4 + C_5(0)^5$$

$$t_i=0 \quad [C_0 = 30]$$

$$\dot{\theta}(t_i) = 0 = C_1 + 2C_2(0) + 3(C_3(0)^2 + 4(C_4(0)^3 + 5C_5(0)^4$$

$$[C_1 = 0]$$

$$\ddot{\theta}(t_i) = 3 = 2C_2 + 6C_3(0) + 12C_4(0)^2 + 20C_5(0)^3$$

$$2C_2 = 3$$

$$(C_2 = 1,5)$$

$$\theta(t_i) = 30 + 0(5) + 2,5(5)^2 + C_3(5)^3 + C_4(5)^4 + C_5(5)^5$$

$$75 = 30 + 62,5 + 125(C_3 + 625(C_4 + 3125(C_5$$

$$125C_3 + 625C_4 + 3125C_5 = 17,5$$

$$\dot{\theta}(t_i) = 0 = 0 + 2(2,5)(5) + 3C_3(5)^2 + 4C_4(5)^3 + 5C_5(5)^4$$

$$150C_3 + 500C_4 + 3125C_5 = -25$$

$$\ddot{\theta}(t_i) = -5 = 2(2,5) + 6C_3(5) + 12C_4(5)^2 + 20C_5(5)$$

$$30(C_3 + 300C_4 + 2500C_5) = -10$$

$$150C_3 + 625C_4 + 3125C_5 = -17,5 \quad C_3 = 1,6$$

$$75(C_3 + 500C_4 + 3125C_5) = -25 \quad C_4 = -0,58$$

$$30(C_3 + 300C_4 + 2500C_5) = -10 \quad C_5 = 0,0464$$

$$\theta(t) = 30 + 2,5t^2 + 1,6t^3 - 0,58t^4 + 0,0464t^5$$

$$\dot{\theta}(t) = 5t + 4,8t^2 - 2,32t^3 + 0,232t^4$$

$$\ddot{\theta}(t) = 5 + 9,6t - 6,9t^2 + 0,928t^3$$

(9) antropomórfico QRR

$$\theta(t) = C_0 + C_1 t + C_2 t^2 + C_3 t^3 + C_4 t^4 + C_5 t^5$$

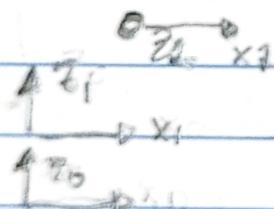
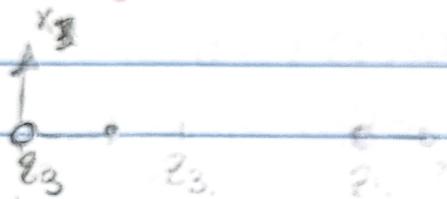
junta 1: $\theta(t) = 3,06 t^2 - 0,2915 t^3$

junta 2: $\phi(t) = 2,6239 t^3 - 0,5623 t^4 + 0,0321 t^5$

junta 3: $\theta(t) = 0,2915 t^3 - 0,0625 t^4 + 0,0036 t^5$

Linha de Perseção.

①



Motoman MH-SF

	a	α	d	θ	orient
0-1	88	-30	330	50	
1-2	310	+180	0	$(\theta_2) - 30$	
2-3	40	-90	0	$\theta_3 = 80$	
3-4	0	30	-306	$\theta_4 = 90$	
4-5	0	-90	0	$\theta_5 = 0$	
5-6	0	0	-80	$\theta_6 = 20$	

$$J = [J_1 \dots J_6]$$

$$J = \begin{bmatrix} Z_0 \times (\alpha_6 - \alpha_0) & Z_5 \times (\alpha_6 - \alpha_5) \\ Z_0 & \dots & Z_5 \end{bmatrix}$$

$$Z_0 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$Z_3 = \begin{bmatrix} -0,11 \\ -0,13 \\ -0,98 \end{bmatrix}$$

$$O_0 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$O_3 = \begin{bmatrix} 31 \\ 0 \\ 0 \end{bmatrix}$$

$$Z_1 = \begin{bmatrix} -0,767 \\ 0,64 \\ 0 \end{bmatrix}$$

$$Z_4 = \begin{bmatrix} -0,63 \\ -0,75 \\ 0,17 \end{bmatrix}$$

$$O_1 = \begin{bmatrix} 56,56 \\ 67,41 \\ 330 \end{bmatrix}$$

$$Z_2 = \begin{bmatrix} 0,76 \\ -0,64 \\ 0 \end{bmatrix}$$

$$Z_5 = \begin{bmatrix} -0,11 \\ -0,13 \\ -0,98 \end{bmatrix}$$

$$O_2 = \begin{bmatrix} 56,56 \\ 67,41 \\ 640 \end{bmatrix}$$

III

2 DOF

$\text{Ref}(x, a) \text{ Trans}(0, 0, d)$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \text{ca} & -\text{sa} & -\text{dca} \\ 0 & \text{sa} & \text{ca} & \text{dca} \\ 0 & 0 & 0 & 1 \end{bmatrix} \rightarrow \text{derivada é o jacobiano.}$$

$$px=0 \Rightarrow \dot{p}_x=0$$

$$py = -\text{dca} \Rightarrow \dot{p}_y = \frac{\partial l}{\partial d}(-\text{dca}) + \frac{\partial l}{\partial a}(-\text{dca}) = -5\text{a}^2\text{d} - \text{dca}^2\text{a} \Rightarrow \textcircled{1}$$

$$pz = \text{dca} \Rightarrow \dot{p}_z = \frac{\partial l}{\partial d}(\text{dca}) + \frac{\partial l}{\partial a}(\text{dca}) \Rightarrow \text{cadd} - \text{dsaaa}$$

$$\textcircled{2} \quad \begin{array}{c|c|c|c|c} p_x & -\text{sa} & -\text{dca} & 2\text{d} \\ \hline \dot{p}_x & \text{ca} & -\text{dca} & 2\text{a} \\ \hline \dot{p}_y & & & \\ \hline \dot{p}_z & & & \end{array}$$

θ_x	θ_y	θ_z	θ_1	θ_2	θ_3
9	6	10			

8,4	5,9	9,8
7,8	5,8	9,6

3	5	8
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