

# Untitled

2025-11-21

En este script se realiza un modelo de clasificación binario con caret (cv=10) Y CON loocv.  
Se utiliza la base de datos desbalanceada y se juega con el cutoff para hacer frente al desbalanceo.

## Caret

Preparación de los datos

Trabajaremos a partir de datatrain, donde tenemos la respuesta Exited para todas las filas

La idea es probar varios niveles de balanceo y de cutoff para encontrar el óptimo para ambos parámetros.

```
## Cargando paquete requerido: ggplot2

## Cargando paquete requerido: lattice

## Loaded ROSE 0.0-4

## Type 'citation("pROC")' for a citation.

##
## Adjuntando el paquete: 'pROC'

## The following objects are masked from 'package:stats':
##
##   cov, smooth, var

## Setting levels: control = neg, case = pos

## Setting direction: controls < cases

## Setting levels: control = neg, case = pos

## Setting direction: controls < cases

## Setting levels: control = neg, case = pos

## Setting direction: controls < cases

## Setting levels: control = neg, case = pos
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## Setting direction: controls < cases

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```



[illegible]

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[illegible]



## 13	0.25	0.70	0.109395109	0.100710136	0.058620690	0.0537931034	0.9965765766
## 14	0.25	0.75	0.068783069	0.066401062	0.035862069	0.0344827586	0.9981981982
## 15	0.25	0.80	0.037812289	0.035182679	0.019310345	0.0179310345	0.9994594595
## 16	0.25	0.85	0.012328767	0.012328767	0.006206897	0.0062068966	0.9998198198
## 17	0.25	0.90	NA	0.001378360	0.000000000	0.0006896552	1.0000000000
## 18	0.30	0.10	0.356055920	0.355852512	0.992413793	0.9917241379	0.0641441441
## 19	0.30	0.15	0.386880670	0.387623066	0.955862069	0.9503448276	0.2200000000
## 20	0.30	0.20	0.418963255	0.419550599	0.880689655	0.8820689655	0.3929729730
## 21	0.30	0.25	0.442693974	0.446238677	0.775172414	0.7813793103	0.5488288288
## 22	0.30	0.30	0.463871121	0.457088668	0.675172414	0.6648275862	0.6771171171
## 23	0.30	0.35	0.467842914	0.471736011	0.566896552	0.5668965517	0.7762162162
## 24	0.30	0.40	0.449330127	0.457475995	0.451034483	0.4600000000	0.8545945946
## 25	0.30	0.45	0.423948220	0.411336032	0.361379310	0.3503448276	0.9102702703
## 26	0.30	0.50	0.352504638	0.345343940	0.262068966	0.2544827586	0.9412612613
## 27	0.30	0.55	0.292403746	0.287815126	0.193793103	0.1889655172	0.9655855856
## 28	0.30	0.60	0.244829514	0.231161473	0.151034483	0.1406896552	0.9783783784
## 29	0.30	0.65	0.183333333	0.175015088	0.106206897	0.1000000000	0.9863063063
## 30	0.30	0.70	0.138490331	0.123893805	0.076551724	0.0675862069	0.9924324324
## 31	0.30	0.75	0.100970874	0.078688525	0.053793103	0.0413793103	0.9969369369
## 32	0.30	0.80	0.065159574	0.045698925	0.033793103	0.0234482759	0.9990990991
## 33	0.30	0.85	0.029850746	0.015047880	0.015172414	0.0075862069	0.9996396396
## 34	0.30	0.90	0.006868132	0.005502063	0.003448276	0.0027586207	0.9998198198
## 35	0.35	0.10	0.348202477	0.346887370	0.998620690	0.9972413793	0.0236036036
## 36	0.35	0.15	0.369451697	0.369310793	0.975862069	0.9793103448	0.1360360360
## 37	0.35	0.20	0.398879717	0.398235294	0.933103448	0.9337931034	0.2827027027
## 38	0.35	0.25	0.423018163	0.424407704	0.859310345	0.8586206897	0.4243243243
## 39	0.35	0.30	0.441211638	0.444488818	0.763448276	0.7675862069	0.5565765766
## 40	0.35	0.35	0.460705882	0.456049149	0.675172414	0.6655172414	0.6718918919
## 41	0.35	0.40	0.472330911	0.468085106	0.582758621	0.5689655172	0.7688288288
## 42	0.35	0.45	0.456798392	0.458206430	0.470344828	0.4668965517	0.8461261261
## 43	0.35	0.50	0.419392984	0.415802075	0.366896552	0.3593103448	0.9000000000
## 44	0.35	0.55	0.363968907	0.345829428	0.274482759	0.2544827586	0.9389189189
## 45	0.35	0.60	0.303616913	0.286014721	0.205517241	0.1875862069	0.9612612613
## 46	0.35	0.65	0.245947457	0.227660785	0.151724138	0.1379310345	0.9785585586
## 47	0.35	0.70	0.182468694	0.170598911	0.105517241	0.0972413793	0.9866666667
## 48	0.35	0.75	0.135423197	0.118395926	0.074482759	0.0641379310	0.9933333333
## 49	0.35	0.80	0.090255069	0.077733860	0.047586207	0.0406896552	0.9981981982
## 50	0.35	0.85	0.044414536	0.032520325	0.022758621	0.0165517241	0.9994594595
## 51	0.35	0.90	0.009602195	0.006868132	0.004827586	0.0034482759	0.9998198198
## 52	0.40	0.10	0.344344106	0.344458962	0.999310345	1.0000000000	0.0059459459
## 53	0.40	0.15	0.358897618	0.357685128	0.992413793	0.9910344828	0.0756756757
## 54	0.40	0.20	0.384434939	0.380537004	0.960689655	0.9627586207	0.2064864865
## 55	0.40	0.25	0.410168434	0.407925050	0.906896552	0.9158620690	0.3428828829
## 56	0.40	0.30	0.432849202	0.433073654	0.832413793	0.8434482759	0.4738738739
## 57	0.40	0.35	0.450639279	0.451332920	0.741379310	0.7531034483	0.5953153153
## 58	0.40	0.40	0.466009852	0.461802155	0.652413793	0.6503448276	0.7001801802
## 59	0.40	0.45	0.473327439	0.469057259	0.553793103	0.5593103448	0.7945945946
## 60	0.40	0.50	0.448951049	0.456926258	0.442758621	0.4572413793	0.8616216216
## 61	0.40	0.55	0.413149351	0.412479741	0.351034483	0.3510344828	0.9090090090
## 62	0.40	0.60	0.348477752	0.342749529	0.256551724	0.2510344828	0.9436036036
## 63	0.40	0.65	0.287513116	0.285106383	0.188965517	0.1848275862	0.9672072072
## 64	0.40	0.70	0.217912151	0.217241379	0.131724138	0.1303448276	0.9798198198
## 65	0.40	0.75	0.156192800	0.147368421	0.088275862	0.0820689655	0.9890090090
## 66	0.40	0.80	0.114869177	0.095917045	0.062068966	0.0510344828	0.9951351351

## 67	0.40	0.85	0.057448230	0.049631120	0.029655172	0.0255172414	0.9992792793
## 68	0.40	0.90	0.016393443	0.009602195	0.008275862	0.0048275862	0.9996396396
## 69	0.45	0.10	0.343317154	0.343398461	1.000000000	1.0000000000	0.0005405405
## 70	0.45	0.15	0.350193611	0.348696911	0.997931034	0.9965517241	0.0329729730
## 71	0.45	0.20	0.366422042	0.365431466	0.981379310	0.9827586207	0.1181981982
## 72	0.45	0.25	0.390361446	0.388810398	0.949655172	0.9489655172	0.2381981982
## 73	0.45	0.30	0.414556962	0.411053541	0.903448276	0.9027586207	0.3585585586
## 74	0.45	0.35	0.433639474	0.433782570	0.830344828	0.8324137931	0.4776576577
## 75	0.45	0.40	0.448598131	0.451492537	0.744827586	0.7510344828	0.5882882883
## 76	0.45	0.45	0.462396895	0.465479385	0.657241379	0.6579310345	0.6902702703
## 77	0.45	0.50	0.467755804	0.476024412	0.562758621	0.5648275862	0.7796396396
## 78	0.45	0.55	0.451169188	0.453444098	0.452413793	0.4517241379	0.8554954955
## 79	0.45	0.60	0.412362749	0.406737880	0.349655172	0.3413793103	0.9095495495
## 80	0.45	0.65	0.333493052	0.329004329	0.240000000	0.2358620690	0.9479279279
## 81	0.45	0.70	0.275751073	0.269209809	0.177241379	0.1703448276	0.9717117117
## 82	0.45	0.75	0.202457578	0.193624557	0.119310345	0.1131034483	0.9845045045
## 83	0.45	0.80	0.138059701	0.123893805	0.076551724	0.0675862069	0.9915315315
## 84	0.45	0.85	0.082568807	0.062500000	0.043448276	0.0324137931	0.9976576577
## 85	0.45	0.90	0.028493894	0.019112628	0.014482759	0.0096551724	0.9994594595
## 86	0.50	0.10	0.343235886	0.343195266	1.000000000	1.0000000000	0.0001801802
## 87	0.50	0.15	0.345032719	0.344844010	1.000000000	0.9986206897	0.0081081081
## 88	0.50	0.20	0.355303684	0.355863092	0.994482759	0.9931034483	0.0585585586
## 89	0.50	0.25	0.370273109	0.370916754	0.972413793	0.9710344828	0.1430630631
## 90	0.50	0.30	0.393630756	0.392523364	0.946206897	0.9413793103	0.2524324324
## 91	0.50	0.35	0.414907230	0.413573363	0.894482759	0.8951724138	0.3684684685
## 92	0.50	0.40	0.431215971	0.435178441	0.819310345	0.8241379310	0.4825225225
## 93	0.50	0.45	0.449602677	0.451452282	0.741379310	0.7503448276	0.5933333333
## 94	0.50	0.50	0.462365591	0.465250965	0.652413793	0.6648275862	0.6944144144
## 95	0.50	0.55	0.465945630	0.470925236	0.549655172	0.5668965517	0.7884684685
## 96	0.50	0.60	0.447625698	0.453178401	0.442068966	0.4572413793	0.8607207207
## 97	0.50	0.65	0.405010438	0.409461664	0.334482759	0.3462068966	0.9171171171
## 98	0.50	0.70	0.319842053	0.329457364	0.223448276	0.2344827586	0.9545945946
## 99	0.50	0.75	0.243439419	0.258525853	0.150344828	0.1620689655	0.9778378378
## 100	0.50	0.80	0.149877150	0.171704958	0.084137931	0.0979310345	0.9899099099
## 101	0.50	0.85	0.078534031	0.104651163	0.041379310	0.0558620690	0.9967567568
## 102	0.50	0.90	0.024506467	0.035182679	0.012413793	0.0179310345	0.9998198198
##	Spec_Test PPV_Train PPV_Test NPV_Train NPV_Test ACC_Train ACC_Test						
## 1	0.1264864865	0.2252495	0.2270408	0.9592431	0.9642857	0.2972857	0.3037143
## 2	0.3293693694	0.2604697	0.2625322	0.9370370	0.9359959	0.4431429	0.4504286
## 3	0.5185585586	0.2947262	0.3032595	0.9071452	0.9093207	0.5604286	0.5772857
## 4	0.6659459459	0.3432533	0.3474129	0.8924066	0.8886752	0.6604286	0.6690000
## 5	0.7810810811	0.3972538	0.4011828	0.8750000	0.8720579	0.7308571	0.7355714
## 6	0.8616216216	0.4414169	0.4553191	0.8550253	0.8554562	0.7682857	0.7748571
## 7	0.9127927928	0.5122951	0.5051125	0.8422975	0.8412488	0.7962857	0.7942857
## 8	0.9470270270	0.5490798	0.5504587	0.8279773	0.8282383	0.8020000	0.8022857
## 9	0.9688288288	0.6267606	0.6068182	0.8200487	0.8196646	0.8082857	0.8062857
## 10	0.9801801802	0.6490066	0.6496815	0.8127799	0.8136404	0.8057143	0.8062857
## 11	0.9879279279	0.6901408	0.6883721	0.8080153	0.8081061	0.8044286	0.8044286
## 12	0.9933333333	0.7417219	0.7658228	0.8046430	0.8057586	0.8032857	0.8048571
## 13	0.9962162162	0.8173077	0.7878788	0.8020592	0.8011882	0.8022857	0.8010000
## 14	0.9989189189	0.8387097	0.8928571	0.7985010	0.7983871	0.7988571	0.7991429
## 15	0.9996396396	0.9032258	0.9285714	0.7959535	0.7957544	0.7964286	0.7962857
## 16	0.9998198198	0.9000000	0.9000000	0.7938484	0.7938484	0.7940000	0.7940000
## 17	1.0000000000	NaN	1.0000000	0.7928571	0.7929704	0.7928571	0.7930000

## 18	0.0641441441	0.2169456	0.2168275	0.9700272	0.9673913	0.2564286	0.2562857
## 19	0.2284684685	0.2425197	0.2434629	0.9501946	0.9462687	0.3724286	0.3780000
## 20	0.3931531532	0.2748601	0.2752313	0.9265081	0.9273268	0.4940000	0.4944286
## 21	0.5504504505	0.3098126	0.3122933	0.9033215	0.9059905	0.5957143	0.5982857
## 22	0.6749549550	0.3533021	0.3482659	0.8886262	0.8851607	0.6767143	0.6728571
## 23	0.7814414414	0.3982558	0.4039312	0.8727715	0.8735146	0.7328571	0.7370000
## 24	0.8560360360	0.4476386	0.4549795	0.8562917	0.8585110	0.7710000	0.7740000
## 25	0.9077477477	0.5127202	0.4980392	0.8450987	0.8424749	0.7965714	0.7922857
## 26	0.9427027027	0.5382436	0.5371179	0.8299968	0.8287660	0.8005714	0.8001429
## 27	0.9675675676	0.5953390	0.6035242	0.8209252	0.8203483	0.8057143	0.8062857
## 28	0.9800000000	0.6460177	0.6476190	0.8151929	0.8136126	0.8070000	0.8061429
## 29	0.9888288288	0.6695652	0.7004831	0.8085672	0.8078905	0.8040000	0.8047143
## 30	0.9938738739	0.7254902	0.7424242	0.8044399	0.8031450	0.8027143	0.8020000
## 31	0.9972972973	0.8210526	0.8000000	0.8013034	0.7992780	0.8015714	0.7992857
## 32	0.9992792793	0.9074074	0.8947368	0.7983012	0.7966102	0.7991429	0.7971429
## 33	0.9998198198	0.9166667	0.9166667	0.7952982	0.7940756	0.7957143	0.7942857
## 34	1.0000000000	0.8333333	1.0000000	0.7933943	0.7933105	0.7934286	0.7934286
## 35	0.0196396396	0.2108636	0.2099608	0.9849624	0.9646018	0.2255714	0.2221429
## 36	0.1315315315	0.2278583	0.2275641	0.9556962	0.9605263	0.3100000	0.3071429
## 37	0.2800000000	0.2536558	0.2530841	0.9417767	0.9418182	0.4174286	0.4154286
## 38	0.4284684685	0.2805674	0.2818655	0.9202814	0.9206349	0.5144286	0.5175714
## 39	0.5594594595	0.3102578	0.3128162	0.9000583	0.9020918	0.5994286	0.6025714
## 40	0.6726126126	0.3496429	0.3468728	0.8878571	0.8850166	0.6725714	0.6711429
## 41	0.7747747748	0.3970865	0.3975904	0.8758210	0.8730964	0.7302857	0.7321429
## 42	0.8508108108	0.4440104	0.4498339	0.8594436	0.8593267	0.7682857	0.7712857
## 43	0.9036036036	0.4894204	0.4933712	0.8447489	0.8437079	0.7895714	0.7908571
## 44	0.9432432432	0.5400271	0.5394737	0.8320294	0.8288474	0.8012857	0.8005714
## 45	0.9675675676	0.5808967	0.6017699	0.8224141	0.8200977	0.8047143	0.8060000
## 46	0.9807207207	0.6489676	0.6514658	0.8153430	0.8132377	0.8072857	0.8061429
## 47	0.9888288288	0.6740088	0.6945813	0.8085044	0.8074150	0.8041429	0.8041429
## 48	0.9949549550	0.7448276	0.7685950	0.8042305	0.8027330	0.8030000	0.8021429
## 49	0.9983783784	0.8734177	0.8676471	0.8004624	0.7993364	0.8012857	0.8000000
## 50	0.9996396396	0.9166667	0.9230769	0.7965250	0.7955262	0.7971429	0.7960000
## 51	0.9998198198	0.8750000	0.8333333	0.7936213	0.7933943	0.7937143	0.7934286
## 52	0.0055855856	0.2080103	0.2080643	0.9705882	1.0000000	0.2117143	0.2115714
## 53	0.0724324324	0.2190592	0.2182232	0.9744780	0.9686747	0.2655714	0.2627143
## 54	0.1908108108	0.2402967	0.2371327	0.9526185	0.9514825	0.3627143	0.3507143
## 55	0.3273873874	0.2650141	0.2623987	0.9337586	0.9370810	0.4597143	0.4492857
## 56	0.4639639640	0.2924643	0.2913292	0.9154194	0.9189864	0.5481429	0.5425714
## 57	0.5861261261	0.3236977	0.3222189	0.8980701	0.9008585	0.6255714	0.6207143
## 58	0.6953153153	0.3624521	0.3580106	0.8851936	0.8838754	0.6902857	0.6860000
## 59	0.7843243243	0.4132784	0.4038845	0.8720585	0.8719952	0.7447143	0.7377143
## 60	0.8578378378	0.4553191	0.4566116	0.8554562	0.8581471	0.7748571	0.7748571
## 61	0.9082882883	0.5019724	0.5000000	0.8427999	0.8426948	0.7934286	0.7928571
## 62	0.9441441441	0.5430657	0.5400593	0.8292953	0.8283275	0.8012857	0.8005714
## 63	0.9708108108	0.6008772	0.6232558	0.8202934	0.8200913	0.8060000	0.8080000
## 64	0.9818018018	0.6303630	0.6517241	0.8120054	0.8120715	0.8041429	0.8054286
## 65	0.9917117117	0.6772487	0.7212121	0.8059022	0.8052670	0.8024286	0.8032857
## 66	0.9965765766	0.7692308	0.7956989	0.8024117	0.8007818	0.8018571	0.8007143
## 67	0.9992792793	0.9148936	0.9024390	0.7976413	0.7969536	0.7984286	0.7975714
## 68	0.9998198198	0.8571429	0.8750000	0.7941597	0.7936213	0.7942857	0.7937143
## 69	0.0009009009	0.2072317	0.2072909	1.0000000	1.0000000	0.2075714	0.2078571
## 70	0.0282882883	0.2123569	0.2113191	0.9838710	0.9691358	0.2328571	0.2288571
## 71	0.1127927928	0.2252652	0.2244448	0.9604685	0.9615975	0.2970000	0.2930000

```

## 72 0.2338738739 0.2456735 0.2444918 0.9476703 0.9460641 0.3855714 0.3820000
## 73 0.3495495495 0.2689938 0.2661110 0.9342723 0.9322441 0.4714286 0.4641429
## 74 0.4760360360 0.2934438 0.2933171 0.9150846 0.9157712 0.5507143 0.5498571
## 75 0.5882882883 0.3209510 0.3227623 0.8982118 0.9004413 0.6207143 0.6220000
## 76 0.6945945946 0.3566617 0.3601359 0.8851664 0.8860032 0.6834286 0.6870000
## 77 0.788288288 0.4001962 0.4113511 0.8722032 0.8740268 0.7347143 0.7424286
## 78 0.8587387387 0.4499314 0.4551772 0.8567304 0.8570401 0.7720000 0.7744286
## 79 0.9118918919 0.5024777 0.5030488 0.8425972 0.8412566 0.7935714 0.7937143
## 80 0.9482882883 0.5463108 0.5437202 0.8268113 0.8260870 0.8012857 0.8007143
## 81 0.9751351351 0.6207729 0.6415584 0.8188582 0.8181406 0.8071429 0.8084286
## 82 0.9855855856 0.6679537 0.6721311 0.8105622 0.8096507 0.8052857 0.8048571
## 83 0.9938738739 0.7025316 0.7424242 0.8042970 0.8031450 0.8020000 0.8020000
## 84 0.9987387387 0.8289474 0.8703704 0.7996823 0.7980132 0.8000000 0.7985714
## 85 0.9998198198 0.8750000 0.9333333 0.7951548 0.7944166 0.7954286 0.7947143
## 86 0.0000000000 0.2071725 0.2071429 1.0000000 NaN 0.2072857 0.2071429
## 87 0.0090090090 0.2084831 0.2084053 1.0000000 0.9615385 0.2135714 0.2140000
## 88 0.0625225225 0.2162892 0.2167695 0.9759760 0.9719888 0.2524286 0.2552857
## 89 0.1470270270 0.2286734 0.2292413 0.9520384 0.9510490 0.3148571 0.3177143
## 90 0.2540540541 0.2485057 0.2479564 0.9472617 0.9431438 0.3961429 0.3964286
## 91 0.3641441441 0.2700958 0.2689041 0.9303913 0.9300506 0.4774286 0.4741429
## 92 0.4870270270 0.2926108 0.2956457 0.9108844 0.9137931 0.5522857 0.5568571
## 93 0.588288288 0.3226291 0.3228487 0.8977644 0.9002755 0.6240000 0.6222857
## 94 0.6882882883 0.3580621 0.3578322 0.8843506 0.8871342 0.6857143 0.6834286
## 95 0.7803603604 0.4043633 0.4027438 0.8701531 0.8733616 0.7390000 0.7361429
## 96 0.8535135135 0.4533239 0.4491870 0.8551736 0.8575308 0.7740000 0.7714286
## 97 0.9099099099 0.5132275 0.5009980 0.8406276 0.8419473 0.7964286 0.7931429
## 98 0.9506306306 0.5625000 0.5537459 0.8247198 0.8261823 0.8031429 0.8022857
## 99 0.9760360360 0.6392962 0.6385870 0.8149872 0.8167973 0.8064286 0.8074286
## 100 0.988288288 0.6853933 0.6960784 0.8053357 0.8075338 0.8022857 0.8042857
## 101 0.9969369369 0.7692308 0.8265306 0.7991910 0.8016517 0.7988571 0.8020000
## 102 0.9996396396 0.9473684 0.9285714 0.7948718 0.7957544 0.7952857 0.7962857
## AUC_Train AUC_Test
## 1 0.7386711 0.7424001
## 2 0.7386711 0.7424001
## 3 0.7386711 0.7424001
## 4 0.7386711 0.7424001
## 5 0.7386711 0.7424001
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## 17 0.7386711 0.7424001
## 18 0.7405182 0.7424534
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## 35 0.7404411 0.7420498  
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## 51 0.7404411 0.7420498  
## 52 0.7422414 0.7429893  
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## 65 0.7422414 0.7429893  
## 66 0.7422414 0.7429893  
## 67 0.7422414 0.7429893  
## 68 0.7422414 0.7429893  
## 69 0.7405699 0.7434156  
## 70 0.7405699 0.7434156  
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## 83 0.7405699 0.7434156
## 84 0.7405699 0.7434156
## 85 0.7405699 0.7434156
## 86 0.7420794 0.7429501
## 87 0.7420794 0.7429501
## 88 0.7420794 0.7429501
## 89 0.7420794 0.7429501
## 90 0.7420794 0.7429501
## 91 0.7420794 0.7429501
## 92 0.7420794 0.7429501
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## 95 0.7420794 0.7429501
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## 99 0.7420794 0.7429501
## 100 0.7420794 0.7429501
## 101 0.7420794 0.7429501
## 102 0.7420794 0.7429501
```

ROSE 25, cutoff 25 ROSE 0.35 cutoff 0.35 ROSE 0.40 cutoff 0.40

#LOOCV (leave One Out Cross Validation)

```
library(caret)
library(pROC)
library(ROSE)

# Diferents proporcions de balanceig ROSE
rose_ratios <- seq(0.25, 0.5, by = 0.05)

# Cutoffs per transformar probabilitats en classes
cutpoints <- seq(0.1, 0.9, by = 0.05)

# Dataframe final amb tots els resultats
results_all <- data.frame()

n <- nrow(datatrain)

for (p in rose_ratios) {

  cat("===== PROVANT BALANCEIG p =", p, "=====\n")

  # Probabilitats out-of-fold inicialitzades
  prob_loocv <- numeric(n)
```



```

# Loop LOOCV
for (i in 1:n) {

  # Train = totes les files menys la i
  train_idx <- setdiff(1:n, i)
  test_idx <- i

  train_data <- datatrain[train_idx, ]
  test_data <- datatrain[test_idx, ]

  # Aplicar ROSE al training set
  train_bal <- ROSE(Exited ~ ., data = train_data, p = p, seed = 123)$data

  # Entrenar GLM
  fit <- glm(Exited ~ ., data = train_bal, family = binomial)

  # Predicció per la fila deixada fora
  prob_loocv[i] <- predict(fit, newdata = test_data, type = "response")
}

# Un cop tenim probabilitats out-of-fold, calculem KPI per cada cutoff
for (c in cutpoints) {

  pred_class <- factor(ifelse(prob_loocv > c, "pos", "neg"),
                       levels = c("neg", "pos"))

  kpi <- compute_kpis(datatrain$Exited, pred_class, prob_loocv)

  results_all <- rbind(results_all, data.frame(
    ROSE_p      = p,
    Cutpoint    = c,
    F1_Train    = kpi$F1,
    F1_Test     = kpi$F1,          # LOOCV només té out-of-fold
    Spec_Train  = kpi$Specificity,
    Spec_Test   = kpi$Specificity,
    Sens_Train  = kpi$Sensitivity,
    Sens_Test   = kpi$Sensitivity,
    PPV         = kpi$PPV,
    NPV         = kpi$NPV,
    Accuracy    = kpi$Accuracy,
    AUC         = kpi$AUC
  ))
}
}

```

```
## ===== PROVANT BALANCEIG p = 0.25 =====
```

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## ===== PROVANT BALANCEIG p = 0.3 =====

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## ===== PROVANT BALANCEIG p = 0.35 =====

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## Setting levels: control = neg, case = pos
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```

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## ===== PROVANT BALANCEIG p = 0.4 =====

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## ===== PROVANT BALANCEIG p = 0.45 =====

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[illegible]



[illegible]

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```

```
results_all
```

##	ROSE_p	Cutpoint	F1_Train	F1_Test	Spec_Train	Spec_Test	Sens_Train
## 1	0.25	0.10	0.400115892	0.400115892	0.266306306	0.266306306	0.952413793
## 2	0.25	0.15	0.432413793	0.432413793	0.442162162	0.442162162	0.864827586
## 3	0.25	0.20	0.451137062	0.451137062	0.580180180	0.580180180	0.759310345
## 4	0.25	0.25	0.467678746	0.467678746	0.697477477	0.697477477	0.658620690
## 5	0.25	0.30	0.469085631	0.469085631	0.786126126	0.786126126	0.557241379
## 6	0.25	0.35	0.453991881	0.453991881	0.849549550	0.849549550	0.462758621
## 7	0.25	0.40	0.423437500	0.423437500	0.897657658	0.897657658	0.373793103
## 8	0.25	0.45	0.367437722	0.367437722	0.930630631	0.930630631	0.284827586
## 9	0.25	0.50	0.310293386	0.310293386	0.955135135	0.955135135	0.215172414
## 10	0.25	0.55	0.267952840	0.267952840	0.970090090	0.970090090	0.172413793
## 11	0.25	0.60	0.212862834	0.212862834	0.978378378	0.978378378	0.128965517
## 12	0.25	0.65	0.173341303	0.173341303	0.985945946	0.985945946	0.100000000
## 13	0.25	0.70	0.138871668	0.138871668	0.990810811	0.990810811	0.077241379
## 14	0.25	0.75	0.100386100	0.100386100	0.995315315	0.995315315	0.053793103
## 15	0.25	0.80	0.063534083	0.063534083	0.997657658	0.997657658	0.033103448
## 16	0.25	0.85	0.028493894	0.028493894	0.999459459	0.999459459	0.014482759
## 17	0.25	0.90	0.008236102	0.008236102	0.999819820	0.999819820	0.004137931
## 18	0.30	0.10	0.376095618	0.376095618	0.159639640	0.159639640	0.976551724
## 19	0.30	0.15	0.408868502	0.408868502	0.323783784	0.323783784	0.922068966
## 20	0.30	0.20	0.434549356	0.434549356	0.472612613	0.472612613	0.837931034
## 21	0.30	0.25	0.449166667	0.449166667	0.590630631	0.590630631	0.743448276
## 22	0.30	0.30	0.466180049	0.466180049	0.693333333	0.693333333	0.660689655
## 23	0.30	0.35	0.467928793	0.467928793	0.772792793	0.772792793	0.571034483
## 24	0.30	0.40	0.459468330	0.459468330	0.838378378	0.838378378	0.482758621
## 25	0.30	0.45	0.428839655	0.428839655	0.884324324	0.884324324	0.393793103
## 26	0.30	0.50	0.388959660	0.388959660	0.919459459	0.919459459	0.315862069
## 27	0.30	0.55	0.325982742	0.325982742	0.946666667	0.946666667	0.234482759
## 28	0.30	0.60	0.279874214	0.279874214	0.965585586	0.965585586	0.184137931
## 29	0.30	0.65	0.230337079	0.230337079	0.977477477	0.977477477	0.141379310
## 30	0.30	0.70	0.179334917	0.179334917	0.985045045	0.985045045	0.104137931

## 31	0.30	0.75	0.136138614	0.136138614	0.989909910	0.989909910	0.075862069
## 32	0.30	0.80	0.093023256	0.093023256	0.995315315	0.995315315	0.049655172
## 33	0.30	0.85	0.052104208	0.052104208	0.998558559	0.998558559	0.026896552
## 34	0.30	0.90	0.019086571	0.019086571	0.999459459	0.999459459	0.009655172
## 35	0.35	0.10	0.361801438	0.361801438	0.091351351	0.091351351	0.988965517
## 36	0.35	0.15	0.392613636	0.392613636	0.241801802	0.241801802	0.953103448
## 37	0.35	0.20	0.419510625	0.419510625	0.376756757	0.376756757	0.898620690
## 38	0.35	0.25	0.439933567	0.439933567	0.499639640	0.499639640	0.822068966
## 39	0.35	0.30	0.454024209	0.454024209	0.605405405	0.605405405	0.737241379
## 40	0.35	0.35	0.470070853	0.470070853	0.697117117	0.697117117	0.663448276
## 41	0.35	0.40	0.475308642	0.475308642	0.771711712	0.771711712	0.584137931
## 42	0.35	0.45	0.466968912	0.466968912	0.834774775	0.834774775	0.497241379
## 43	0.35	0.50	0.437453738	0.437453738	0.880900901	0.880900901	0.407586207
## 44	0.35	0.55	0.395815900	0.395815900	0.915855856	0.915855856	0.326206897
## 45	0.35	0.60	0.340103921	0.340103921	0.944684685	0.944684685	0.248275862
## 46	0.35	0.65	0.293416278	0.293416278	0.964684685	0.964684685	0.195172414
## 47	0.35	0.70	0.237458194	0.237458194	0.976396396	0.976396396	0.146896552
## 48	0.35	0.75	0.180308422	0.180308422	0.984864865	0.984864865	0.104827586
## 49	0.35	0.80	0.134078212	0.134078212	0.990450450	0.990450450	0.074482759
## 50	0.35	0.85	0.081977879	0.081977879	0.995675676	0.995675676	0.043448276
## 51	0.35	0.90	0.032476319	0.032476319	0.999279279	0.999279279	0.016551724
## 52	0.40	0.10	0.353228963	0.353228963	0.048288288	0.048288288	0.995862069
## 53	0.40	0.15	0.375830013	0.375830013	0.159459459	0.159459459	0.975862069
## 54	0.40	0.20	0.402419236	0.402419236	0.285585586	0.285585586	0.940689655
## 55	0.40	0.25	0.424813896	0.424813896	0.403423423	0.403423423	0.885517241
## 56	0.40	0.30	0.440715884	0.440715884	0.507747748	0.507747748	0.815172414
## 57	0.40	0.35	0.454024209	0.454024209	0.605405405	0.605405405	0.737241379
## 58	0.40	0.40	0.468643656	0.468643656	0.693693694	0.693693694	0.664827586
## 59	0.40	0.45	0.476905954	0.476905954	0.768108108	0.768108108	0.591034483
## 60	0.40	0.50	0.469609725	0.469609725	0.830270270	0.830270270	0.506206897
## 61	0.40	0.55	0.441758242	0.441758242	0.878018018	0.878018018	0.415862069
## 62	0.40	0.60	0.399833403	0.399833403	0.915135135	0.915135135	0.331034483
## 63	0.40	0.65	0.341904762	0.341904762	0.947567568	0.947567568	0.247586207
## 64	0.40	0.70	0.291231733	0.291231733	0.966306306	0.966306306	0.192413793
## 65	0.40	0.75	0.225623583	0.225623583	0.979279279	0.979279279	0.137241379
## 66	0.40	0.80	0.157862781	0.157862781	0.987927928	0.987927928	0.089655172
## 67	0.40	0.85	0.095299420	0.095299420	0.994774775	0.994774775	0.051034483
## 68	0.40	0.90	0.046885466	0.046885466	0.998558559	0.998558559	0.024137931
## 69	0.45	0.10	0.347293892	0.347293892	0.020540541	0.020540541	0.997931034
## 70	0.45	0.15	0.362990227	0.362990227	0.099279279	0.099279279	0.986206897
## 71	0.45	0.20	0.385775564	0.385775564	0.210270270	0.210270270	0.961379310
## 72	0.45	0.25	0.406681853	0.406681853	0.316036036	0.316036036	0.923448276
## 73	0.45	0.30	0.427460264	0.427460264	0.423423423	0.423423423	0.871724138
## 74	0.45	0.35	0.443306788	0.443306788	0.521621622	0.521621622	0.806206897
## 75	0.45	0.40	0.453418803	0.453418803	0.609189189	0.609189189	0.731724138
## 76	0.45	0.45	0.468604935	0.468604935	0.696576577	0.696576577	0.661379310
## 77	0.45	0.50	0.475741614	0.475741614	0.765945946	0.765945946	0.591724138
## 78	0.45	0.55	0.472435897	0.472435897	0.831891892	0.831891892	0.508275862
## 79	0.45	0.60	0.443144424	0.443144424	0.877657658	0.877657658	0.417931034
## 80	0.45	0.65	0.401172529	0.401172529	0.917297297	0.917297297	0.330344828
## 81	0.45	0.70	0.333653846	0.333653846	0.949009009	0.949009009	0.239310345
## 82	0.45	0.75	0.280571731	0.280571731	0.968648649	0.968648649	0.182758621
## 83	0.45	0.80	0.203585888	0.203585888	0.981441441	0.981441441	0.121379310
## 84	0.45	0.85	0.127182045	0.127182045	0.990630631	0.990630631	0.070344828

## 85	0.45	0.90	0.065919578	0.065919578	0.996936937	0.996936937	0.034482759
## 86	0.50	0.10	0.344663656	0.344663656	0.006486486	0.006486486	1.000000000
## 87	0.50	0.15	0.355057287	0.355057287	0.058378378	0.058378378	0.993793103
## 88	0.50	0.20	0.372001573	0.372001573	0.142342342	0.142342342	0.978620690
## 89	0.50	0.25	0.393111301	0.393111301	0.244144144	0.244144144	0.952413793
## 90	0.50	0.30	0.410772326	0.410772326	0.336216216	0.336216216	0.915172414
## 91	0.50	0.35	0.428963624	0.428963624	0.436396396	0.436396396	0.862068966
## 92	0.50	0.40	0.446230387	0.446230387	0.529729730	0.529729730	0.804137931
## 93	0.50	0.45	0.457277802	0.457277802	0.613873874	0.613873874	0.734482759
## 94	0.50	0.50	0.469607843	0.469607843	0.698738739	0.698738739	0.660689655
## 95	0.50	0.55	0.476961743	0.476961743	0.769909910	0.769909910	0.588965517
## 96	0.50	0.60	0.470284238	0.470284238	0.834594595	0.834594595	0.502068966
## 97	0.50	0.65	0.443701226	0.443701226	0.883963964	0.883963964	0.411724138
## 98	0.50	0.70	0.392123288	0.392123288	0.922882883	0.922882883	0.315862069
## 99	0.50	0.75	0.322485207	0.322485207	0.954774775	0.954774775	0.225517241
## 100	0.50	0.80	0.257142857	0.257142857	0.975495495	0.975495495	0.161379310
## 101	0.50	0.85	0.166064982	0.166064982	0.986666667	0.986666667	0.095172414
## 102	0.50	0.90	0.085547634	0.085547634	0.995135135	0.995135135	0.045517241
##	Sens_Test	PPV	NPV	Accuracy	AUC		
## 1	0.952413793	0.2532551	0.9553975	0.4084286	0.7460849		
## 2	0.864827586	0.2882759	0.9260377	0.5297143	0.7460849		
## 3	0.759310345	0.3208977	0.9022135	0.6172857	0.7460849		
## 4	0.658620690	0.3625664	0.8866239	0.6894286	0.7460849		
## 5	0.557241379	0.4050125	0.8717283	0.7387143	0.7460849		
## 6	0.462758621	0.4455511	0.8582090	0.7694286	0.7460849		
## 7	0.373793103	0.4882883	0.8458404	0.7891429	0.7460849		
## 8	0.284827586	0.5175439	0.8327959	0.7968571	0.7460849		
## 9	0.215172414	0.5561497	0.8232645	0.8018571	0.7460849		
## 10	0.172413793	0.6009615	0.8177400	0.8048571	0.7460849		
## 11	0.128965517	0.6091205	0.8112954	0.8024286	0.7460849		
## 12	0.100000000	0.6502242	0.8074369	0.8024286	0.7460849		
## 13	0.077241379	0.6871166	0.8043001	0.8015714	0.7460849		
## 14	0.053793103	0.7500000	0.8010441	0.8002857	0.7460849		
## 15	0.033103448	0.7868852	0.7979536	0.7978571	0.7460849		
## 16	0.014482759	0.8750000	0.7951548	0.7954286	0.7460849		
## 17	0.004137931	0.8571429	0.7935078	0.7935714	0.7460849		
## 18	0.976551724	0.2328947	0.9630435	0.3288571	0.7447998		
## 19	0.922068966	0.2626719	0.9408377	0.4477143	0.7447998		
## 20	0.837931034	0.2933366	0.9177747	0.5482857	0.7447998		
## 21	0.743448276	0.3217910	0.8980822	0.6222857	0.7447998		
## 22	0.660689655	0.3601504	0.8866359	0.6865714	0.7447998		
## 23	0.571034483	0.3963619	0.8733456	0.7310000	0.7447998		
## 24	0.482758621	0.4383219	0.8611882	0.7647143	0.7447998		
## 25	0.393793103	0.4707337	0.8481078	0.7827143	0.7447998		
## 26	0.315862069	0.5060773	0.8372436	0.7944286	0.7447998		
## 27	0.234482759	0.5345912	0.8255814	0.7991429	0.7447998		
## 28	0.184137931	0.5829694	0.8191685	0.8037143	0.7447998		
## 29	0.141379310	0.6212121	0.8133433	0.8042857	0.7447998		
## 30	0.104137931	0.6452991	0.8080106	0.8025714	0.7447998		
## 31	0.075862069	0.6626506	0.8039216	0.8005714	0.7447998		
## 32	0.049655172	0.7346939	0.8003477	0.7994286	0.7447998		
## 33	0.026896552	0.8297872	0.7970660	0.7972857	0.7447998		
## 34	0.009655172	0.8235294	0.7943577	0.7944286	0.7447998		
## 35	0.988965517	0.2213988	0.9694073	0.2772857	0.7467371		

## 36	0.953103448	0.2472272	0.9517730	0.3891429	0.7467371
## 37	0.898620690	0.2736245	0.9343164	0.4848571	0.7467371
## 38	0.822068966	0.3003275	0.9148796	0.5664286	0.7467371
## 39	0.737241379	0.3280147	0.8981556	0.6327143	0.7467371
## 40	0.663448276	0.3639803	0.8879963	0.6901429	0.7467371
## 41	0.584137931	0.4006623	0.8765862	0.7328571	0.7467371
## 42	0.497241379	0.4401709	0.8640433	0.7648571	0.7467371
## 43	0.407586207	0.4720447	0.8505567	0.7828571	0.7467371
## 44	0.326206897	0.5031915	0.8387789	0.7937143	0.7467371
## 45	0.248275862	0.5397301	0.8278857	0.8004286	0.7467371
## 46	0.195172414	0.5908142	0.8210397	0.8052857	0.7467371
## 47	0.146896552	0.6191860	0.8141526	0.8045714	0.7467371
## 48	0.104827586	0.6440678	0.8081017	0.8025714	0.7467371
## 49	0.074482759	0.6708075	0.8037725	0.8007143	0.7467371
## 50	0.043448276	0.7241379	0.7993635	0.7984286	0.7467371
## 51	0.016551724	0.8571429	0.7954676	0.7957143	0.7467371
## 52	0.995862069	0.2146893	0.9781022	0.2445714	0.7473915
## 53	0.975862069	0.2327303	0.9619565	0.3285714	0.7473915
## 54	0.940689655	0.2559580	0.9485338	0.4212857	0.7473915
## 55	0.885517241	0.2794342	0.9309771	0.5032857	0.7473915
## 56	0.815172414	0.3019928	0.9131562	0.5714286	0.7473915
## 57	0.737241379	0.3280147	0.8981556	0.6327143	0.7473915
## 58	0.664827586	0.3618619	0.8879151	0.6877143	0.7473915
## 59	0.591034483	0.3997201	0.8778830	0.7314286	0.7473915
## 60	0.506206897	0.4379475	0.8655147	0.7631429	0.7473915
## 61	0.415862069	0.4710938	0.8519231	0.7822857	0.7473915
## 62	0.331034483	0.5047319	0.8396429	0.7941429	0.7473915
## 63	0.247586207	0.5523077	0.8281890	0.8025714	0.7473915
## 64	0.192413793	0.5987124	0.8207836	0.8060000	0.7473915
## 65	0.137241379	0.6337580	0.8128926	0.8048571	0.7473915
## 66	0.089655172	0.6598985	0.8059680	0.8018571	0.7473915
## 67	0.051034483	0.7184466	0.8004930	0.7992857	0.7473915
## 68	0.024137931	0.8139535	0.7966077	0.7967143	0.7473915
## 69	0.997931034	0.2102281	0.9743590	0.2230000	0.7467975
## 70	0.986206897	0.2224296	0.9649737	0.2830000	0.7467975
## 71	0.961379310	0.2413017	0.9542110	0.3658571	0.7467975
## 72	0.923448276	0.2607595	0.9404826	0.4418571	0.7467975
## 73	0.871724138	0.2831541	0.9266562	0.5162857	0.7467975
## 74	0.806206897	0.3057008	0.9115239	0.5805714	0.7467975
## 75	0.731724138	0.3284830	0.8968170	0.6345714	0.7467975
## 76	0.661379310	0.3628453	0.8873078	0.6892857	0.7467975
## 77	0.591724138	0.3977747	0.8777617	0.7298571	0.7467975
## 78	0.508275862	0.4413174	0.8662289	0.7648571	0.7467975
## 79	0.417931034	0.4715953	0.8523185	0.7824286	0.7467975
## 80	0.330344828	0.5106610	0.8398218	0.7957143	0.7467975
## 81	0.239310345	0.5507937	0.8268446	0.8020000	0.7467975
## 82	0.182758621	0.6036446	0.8193873	0.8058571	0.7467975
## 83	0.121379310	0.6308244	0.8104449	0.8032857	0.7467975
## 84	0.070344828	0.6623377	0.8030967	0.8000000	0.7467975
## 85	0.034482759	0.7462687	0.7980672	0.7975714	0.7467975
## 86	1.000000000	0.2082137	1.0000000	0.2122857	0.7475377
## 87	0.993793103	0.2161392	0.9729730	0.2521429	0.7475377
## 88	0.978620690	0.2296488	0.9622412	0.3155714	0.7475377
## 89	0.952413793	0.2476686	0.9515449	0.3908571	0.7475377

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## 90 0.915172414 0.2648174 0.9381599 0.4561429 0.7475377
## 91 0.862068966 0.2855185 0.9237223 0.5245714 0.7475377
## 92 0.804137931 0.3087924 0.9119107 0.5865714 0.7475377
## 93 0.734482759 0.3319825 0.8984705 0.6388571 0.7475377
## 94 0.660689655 0.3642586 0.8874142 0.6908571 0.7475377
## 95 0.588965517 0.4007508 0.8775929 0.7324286 0.7475377
## 96 0.502068966 0.4422843 0.8651476 0.7657143 0.7475377
## 97 0.411724138 0.4810637 0.8518840 0.7861429 0.7475377
## 98 0.315862069 0.5169300 0.8377494 0.7971429 0.7475377
## 99 0.225517241 0.5657439 0.8251324 0.8037143 0.7475377
## 100 0.161379310 0.6324324 0.8165913 0.8068571 0.7475377
## 101 0.095172414 0.6509434 0.8067177 0.8020000 0.7475377
## 102 0.045517241 0.7096774 0.7996236 0.7984286 0.7475377
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## Bootsrap