

HW7 KEY

40 points total, 2 points per problem part unless otherwise noted.

Q1 Power Plants

```
library(tidyverse)
InData <- read.csv("C:/hess/STAT511_FA11/ASCII-comma/CH08/ex8-23.txt",quote=" ' ")
str(InData)

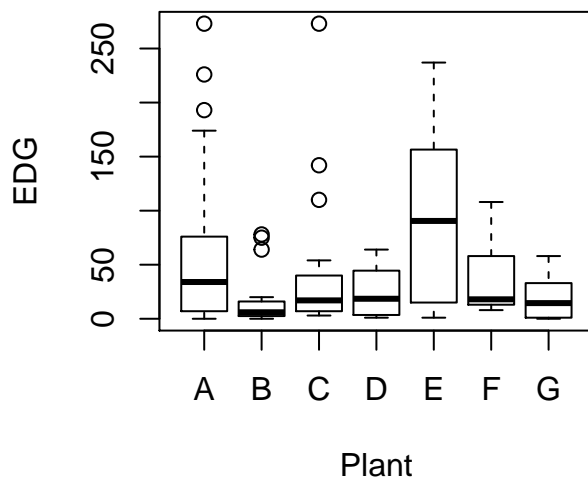
## 'data.frame':  34 obs. of  7 variables:
## $ A: int  28 50 193 55 4 7 174 76 10 0 ...
## $ B: int   2 11 75 6 1 12 4 6 64 3 ...
## $ C: int 142 110 3 273 54 32 3 40 23 30 ...
## $ D: int  64 29 1 3 8 29 4 60 NA NA ...
## $ E: int 139 21 214 67 174 1 9 2 119 237 ...
## $ F: int  18 108 9 8 17 88 28 NA NA NA ...
## $ G: int   0 6 0 16 1 58 13 36 33 19 ...

Reliability <- gather(InData, key = "Plant", value = "EDG")
Reliability$Plant <- as.factor(Reliability$Plant)
str(Reliability)

## 'data.frame':  238 obs. of  2 variables:
## $ Plant: Factor w/ 7 levels "A","B","C","D",...: 1 1 1 1 1 1 1 1 1 1 ...
## $ EDG  : int  28 50 193 55 4 7 174 76 10 0 ...
```

1A. Boxplots

```
boxplot(EDG ~ Plant, data = Reliability)
```



1B. ANOVA (Original Scale)

```
Model1 <- lm(EDG ~ Plant, data = Reliability)
anova(Model1)
```

```
## Analysis of Variance Table
##
## Response: EDG
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Plant      6  58745   9790.9    2.6761 0.01912 *
## Residuals 96 351233   3658.7
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

1C. (4pts) Diagnostics (Original Scale)

Plot of residuals vs fitted values shows megaphone shape. Levene's test p-value = 0.039.

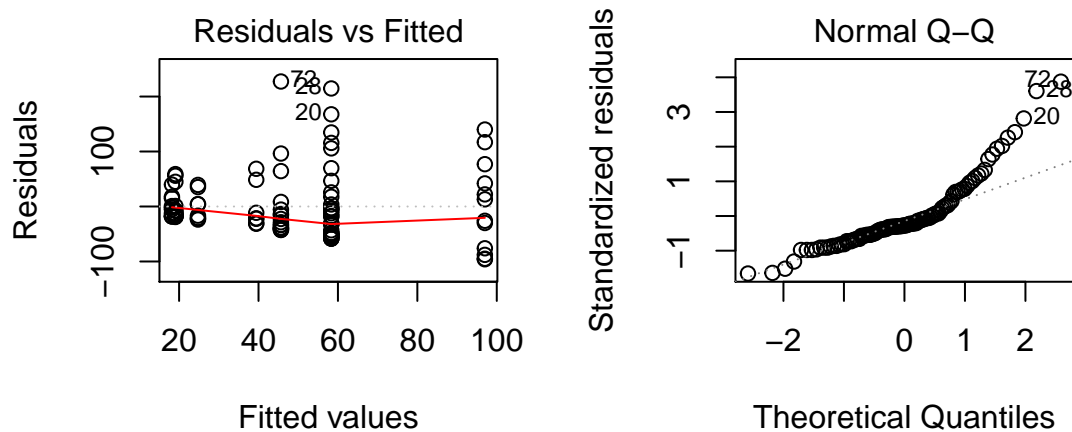
Based on this information, assumption of equal variance is NOT met.

QQplot shows strong curvature. Shapiro-Wilk test p-value < 0.001.

Based on this information, assumption of normality is NOT met.

Note: Plots not required but shown here for convenience.

```
library(car)
par(mfrow=c(1,2))
plot(Model1, which = 1:2)
```



```
leveneTest(EDG ~ Plant, data = Reliability)

## Levene's Test for Homogeneity of Variance (center = median)
##           Df F value    Pr(>F)
## group    6  2.3122 0.03963 *
##          96
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

shapiro.test(Model1$residuals)

##
## Shapiro-Wilk normality test
```

```
##
## data: Model1$residuals
## W = 0.85649, p-value = 1.444e-08

1D. ANOVA (Square Root Transform)

Reliability$sqrtEDG <- sqrt(Reliability$EDG)
Model2 <- lm(sqrtEDG ~ Plant, data = Reliability)
anova(Model2)

## Analysis of Variance Table
##
## Response: sqrtEDG
##          Df Sum Sq Mean Sq F value Pr(>F)
## Plant      6  252.49   42.082   2.6817 0.0189 *
## Residuals 96 1506.46    15.692
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

1E. (4pts) Diagnostics (Square Root Transform)

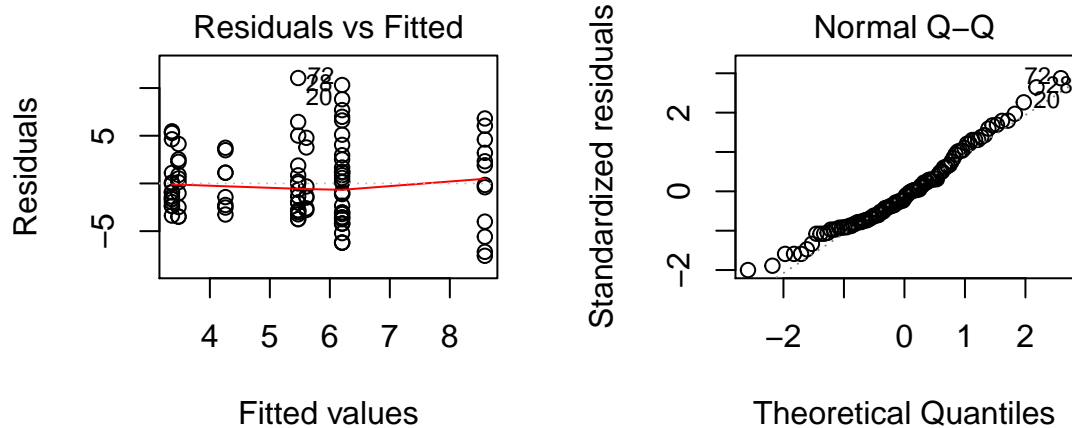
Plot of residuals vs fitted values looks better (but not perfect). Levene's test p-value = 0.1428.
Mixed evidence on equality of variances.

QQplot looks much better, but Shapiro-Wilk test p-value = 0.0164.

Again, mixed evidence on normality.

Note: Plots not required but shown here for convenience.

```
par(mfrow=c(1,2))
plot(Model2, which = 1:2)
```



```
leveneTest(sqrtEDG ~ Plant, data = Reliability)

## Levene's Test for Homogeneity of Variance (center = median)
##          Df F value Pr(>F)
## group    6  1.6464 0.1428
##          96

shapiro.test(Model2$residuals)
```

```
##
## Shapiro-Wilk normality test
##
## data: Model2$residuals
## W = 0.96913, p-value = 0.01645
```

1F. Kruskal-Wallis p-value = 0.051.
Fail to Reject H0 (but just barely!).

```
kruskal.test(EDG ~ Plant, data = Reliability)
```

```
##
## Kruskal-Wallis rank sum test
##
## data: EDG by Plant
## Kruskal-Wallis chi-squared = 12.537, df = 6, p-value = 0.051
```

1G. (4pts) Dunn's comparisons
Comparing other plants to G, only plant E shows evidence of a difference from plant G (at the 0.05 level).

```
library(dunn.test)
dunn.test(x = Reliability$EDG, g = Reliability$Plant)
```

```
## Kruskal-Wallis rank sum test
##
## data: x and group
## Kruskal-Wallis chi-squared = 12.5372, df = 6, p-value = 0.05
```

```
##
##
## Comparison of x by group
## (No adjustment)
## Col Mean-|
## Row Mean |      A      B      C      D      E      F
## -----|-----
## B |      2.286906
##    |      0.0111*
##    |
## C |      0.455880 -1.618775
##    |      0.3242      0.0527
##    |
## D |      0.994053 -0.726924  0.595221
##    |      0.1601      0.2336      0.2758
##    |
## E |     -1.385870 -3.031778 -1.593366 -1.875307
##    |      0.0829      0.0012*      0.0555      0.0304
##    |
## F |     -0.118471 -1.656043 -0.411029 -0.849750  0.875049
##    |      0.4528      0.0489      0.3405      0.1977      0.1908
##    |
## G |      1.596615 -0.329450  1.101424  0.387375  2.428228  1.265278
##    |      0.0552      0.3709      0.1354      0.3492      0.0076*      0.1029
##
## alpha = 0.05
## Reject Ho if p <= alpha/2
```

Q2 Weight Loss

```
library(tidyverse)
InData <- read.csv("C:/hess/STAT511_FA11/ASCII-comma/CH09/ex9-13.txt",quote=" ' ")
str(InData)
```

```
## 'data.frame': 10 obs. of 5 variables:
## $ A1: num 12.4 10.7 11.9 11 12.4 12.3 13 12.5 11.2 13.1
## $ A2: num 9.1 11.5 11.3 9.7 13.2 10.7 10.6 11.3 11.1 11.7
## $ A3: num 8.5 11.6 10.2 10.9 9 9.6 9.9 11.3 10.5 11.2
## $ A4: num 12.7 13.2 11.8 11.9 12.2 11.2 13.7 11.8 12.2 11.7
## $ S : num 8.7 9.3 8.2 8.3 9 9.4 9.2 12.2 8.5 9.9
```

```
WtLoss <- InData %>%
  gather(key = "Trt", value = "Loss") %>%
  mutate(Trt = as_factor(Trt)) %>%
  mutate(Trt = fct_relevel(Trt, "S"))
str(WtLoss)
```

```
## 'data.frame': 50 obs. of 2 variables:
## $ Trt : Factor w/ 5 levels "S","A1","A2",...: 2 2 2 2 2 2 2 2 2 2 ...
## $ Loss: num 12.4 10.7 11.9 11 12.4 12.3 13 12.5 11.2 13.1 ...
```

2A. (4pts) Summary Statistics

```
SumStats <- WtLoss %>%
  group_by(Trt) %>%
  summarise(n = n(),
            mean = mean(Loss),
            sd = sd(Loss),
            se = sd/sqrt(n))
SumStats
```

```
## # A tibble: 5 x 5
##   Trt      n mean    sd    se
##   <fct> <int> <dbl> <dbl> <dbl>
## 1 S      10  9.27  1.16  0.366
## 2 A1     10 12.0   0.829 0.262
## 3 A2     10 11.0   1.12  0.355
## 4 A3     10 10.3   1.03  0.325
## 5 A4     10 12.2   0.756 0.239
```

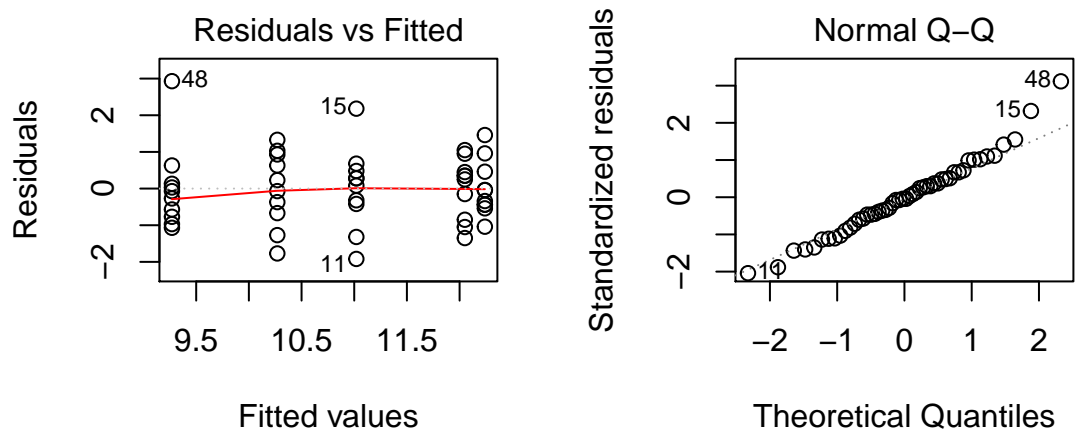
““

2B. ANOVA Note: Plots not required but shown here for convenience.

```
Model <- lm(Loss ~ Trt, data = WtLoss)
anova(Model)
```

```
## Analysis of Variance Table
##
## Response: Loss
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Trt         4  61.618  15.4045   15.681 4.164e-08 ***
## Residuals   45  44.207   0.9824
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
par(mfrow=c(1,2))
plot(Model, which = 1:2)
```



2C. Unadjusted Pairwise Comparisons

```
library(emmeans)
emout <- emmeans(Model, ~ Trt)
pairs(emout, adjust = "none")
```

##	contrast	estimate	SE	df	t.ratio	p.value
##	S - A1	-2.78	0.443	45	-6.272	<.0001
##	S - A2	-1.75	0.443	45	-3.948	0.0003
##	S - A3	-1.00	0.443	45	-2.256	0.0290
##	S - A4	-2.97	0.443	45	-6.700	<.0001
##	A1 - A2	1.03	0.443	45	2.324	0.0247
##	A1 - A3	1.78	0.443	45	4.016	0.0002
##	A1 - A4	-0.19	0.443	45	-0.429	0.6702
##	A2 - A3	0.75	0.443	45	1.692	0.0976
##	A2 - A4	-1.22	0.443	45	-2.752	0.0085
##	A3 - A4	-1.97	0.443	45	-4.444	0.0001

2D. Tukey adjusted Pairwise Comparisons

```
pairs(emout)
```

##	contrast	estimate	SE	df	t.ratio	p.value
##	S - A1	-2.78	0.443	45	-6.272	<.0001
##	S - A2	-1.75	0.443	45	-3.948	0.0024
##	S - A3	-1.00	0.443	45	-2.256	0.1784
##	S - A4	-2.97	0.443	45	-6.700	<.0001
##	A1 - A2	1.03	0.443	45	2.324	0.1563
##	A1 - A3	1.78	0.443	45	4.016	0.0020
##	A1 - A4	-0.19	0.443	45	-0.429	0.9927
##	A2 - A3	0.75	0.443	45	1.692	0.4490
##	A2 - A4	-1.22	0.443	45	-2.752	0.0618
##	A3 - A4	-1.97	0.443	45	-4.444	0.0005
##						

```
## P value adjustment: tukey method for comparing a family of 5 estimates
```

2E. Without adjusting for multiple testing, 8 comparisons have p-values < 0.05.

After Tukey adjustment, 5 comparisons have p-values < 0.05.

2F. HSD value

```
qtukey(0.95, 5, 45)*sqrt(0.9824)*sqrt(1/10)
```

```
## [1] 1.259503
```

2G. CLD display

```
CLD(emout)
```

```
## Trt emmean SE df lower.CL upper.CL .group
## S 9.27 0.313 45 8.64 9.9 1
## A3 10.27 0.313 45 9.64 10.9 12
## A2 11.02 0.313 45 10.39 11.7 23
## A1 12.05 0.313 45 11.42 12.7 3
## A4 12.24 0.313 45 11.61 12.9 3
##
```

```
## Confidence level used: 0.95
```

```
## P value adjustment: tukey method for comparing a family of 5 estimates
```

```
## significance level used: alpha = 0.05
```

2H. (4pts) Dunnett adjusted comparisons

A1, A2, A4 show evidence of greater weight loss than S (at the 0.05 level).

```
emout2 <- emmeans(Model, dunnett ~ Trt)
```

```
emout2$contrasts
```

```
## contrast estimate SE df t.ratio p.value
## A1 - S 2.78 0.443 45 6.272 <.0001
## A2 - S 1.75 0.443 45 3.948 0.0010
## A3 - S 1.00 0.443 45 2.256 0.0961
## A4 - S 2.97 0.443 45 6.700 <.0001
##
```

```
## P value adjustment: dunnettx method for 4 tests
```