Highway Exmaple #2: Best Subsets Selection

We return to the Highway data but this time consider best subsets selection. For this data from Weisberg, the response variable (Y) is accident rate (per million vehicle miles) and there are 13 potential predictors (X's).

We consider AIC selection using the MuMIn package and Cp selection using the leaps package.

```
highway <- read.csv("C:/hess/STAT512/RNotes/MultReg3/MR3 Highway.csv")
str(highway)
  'data.frame':
                   39 obs. of 15 variables:
                1 2 3 4 5 6 7 8 9 10 ...
   $ nr : int
##
   $ rate: num 4.58 2.86 3.02 2.29 1.61 6.87 3.85 6.12 3.29 5.88 ...
   $ len: num 4.99 16.11 9.75 10.65 20.01 ...
   $ adt : int
                69 73 49 61 28 30 46 25 43 23 ...
##
   $ trks: int
                8 8 10 13 12 6 8 9 12 7 ...
##
   $ slim: int 55 60 60 65 70 55 55 55 50 50 ...
##
   $ lwid: int 12 12 12 12 12 12 12 12 12 12 ...
##
   $ shld: int 10 10 10 10 10 10 8 10 4 5 ...
   $ itg : num
                1.2 1.43 1.54 0.94 0.65 0.34 0.47 0.38 0.95 0.12 ...
##
   $ sigs: num 0 0 0 0 0 1.84 0.7 0.38 1.39 1.21 ...
   $ acpt: num 4.6 4.4 4.7 3.8 2.2 24.8 11 18.5 7.5 8.2 ...
   $ lane: int 8 4 4 6 4 4 4 4 4 4 ...
   $ fai : int
                1 1 1 1 1 0 0 0 0 0 ...
   $ pa : int 0 0 0 0 0 1 1 1 1 1 ...
   $ ma
        : int 0000000000...
highway <- highway[,-1]
FullModel <- lm(rate ~ . , data = highway)
```

Best Subset Selection based on AIC using MuMIn package

To use dredge(), you supply the "full" model (the "largest" or most complicated model you want to consider). MuMIn handles factors and produces a nice summary table. For continuous predictors, the partial regression coefficients are shown. For categorical predictors (factors), a + in the summary table would indicate that predictor was included in the model. By default, dredge() will rank models by AICc. That choice is completely reasonable, but I use AIC here to compare to other methods. Note: Watch out for the head() function here. It rescales the model weights to sum to 1 for just the models shown.

```
library(MuMIn)
options(na.action = "na.fail")
AllSubsets <- dredge(FullModel, rank = "AIC", extra = c("R^2"))
## Fixed term is "(Intercept)"
head(AllSubsets)
## Global model call: lm(formula = rate ~ ., data = highway)
## ---
## Model selection table
        (Intrc)
                           fai
                                             len
                                                                    shld
                  acpt
                                  lane
                                                              рa
## 3362
         9.944 0.06428
                                        -0.07405
                                                         -0.7744
## 7458 10.570 0.06277
                                       -0.06345
                                                         -0.7432
## 3874 10.940 0.06033
                                        -0.07014
                                                         -0.9016 0.05678
```

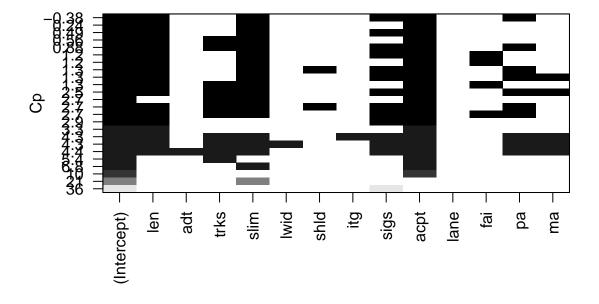
```
## 3490 10.540 0.06993
                                       -0.07105 -0.3785 -0.9725
## 3378
         9.933 0.06676
                               0.05202 -0.07231
                                                        -0.7622
## 3366
        10.060 0.06721 0.2162
                                       -0.07203
                                                        -0.6935
##
                                  R^2 df logLik
                                                    AIC delta weight
         sigs
                  slim
                           trks
## 3362 0.7974 -0.1051
                                0.7450
                                        7 -54.942 123.9
                                                         0.00 0.301
## 7458 0.7013 -0.1031 -0.08852 0.7521
                                       8 -54.396 124.8
                                                         0.91 0.191
## 3874 0.8163 -0.1293
                                        8 -54.734 125.5
                                0.7478
                                                         1.58
## 3490 0.7622 -0.1136
                                0.7477
                                        8 -54.734 125.5
                                                         1.58
                                                               0.136
## 3378 0.7421 -0.1085
                                0.7459
                                        8 -54.873 125.7
                                                         1.86
                                                               0.119
                                0.7458 8 -54.886 125.8 1.89 0.117
## 3366 0.7763 -0.1095
## Models ranked by AIC(x)
```

Best Subset Selection based on Cp using leap package

By Default method="exhaustive" which is best subsets. BIC and Adjusted R2 options are also available, but not aic? Stepwise regression options also available.

Leaps will accept factors, but does not handle them in a convenient way.

```
library(leaps)
Compare <- regsubsets(rate ~ ., data = highway, nbest = 3)
plot(Compare, scale = "Cp")</pre>
```



```
## Subset selection object
## Call: regsubsets.formula(rate ~ ., data = highway, nbest = 3)
```

summary(Compare)

```
## 13 Variables (and intercept)
##
        Forced in Forced out
## len
            FALSE
                       FALSE
## adt
            FALSE.
                       FALSE
## trks
            FALSE
                       FALSE
## slim
            FALSE
                       FALSE
## lwid
            FALSE
                       FALSE
## shld
            FALSE
                       FALSE
## itg
            FALSE
                       FALSE
            FALSE
                       FALSE
## sigs
## acpt
            FALSE
                       FALSE
            FALSE
                       FALSE
## lane
## fai
            FALSE
                       FALSE
##
            FALSE
                       FALSE
  рa
## ma
            FALSE
                       FALSE
## 3 subsets of each size up to 8
## Selection Algorithm: exhaustive
##
            len adt trks slim lwid shld itg sigs acpt lane fai pa ma
##
     (2)""""
##
     (3)
##
  1
     (1)
## 2
      (2)
      (3
## 2
      (1)
## 3
      (2
## 3
      (3
         )
      (1
      (2
## 4
      (3
      ( 1
## 5
      (2
## 5
      (3
## 6
      (1
      (2
##
          )
      (3
##
      (1)
## 7
      (2)
## 7
      (3
          )
## 8
      (1
         )
     (2)
```

8

(3) "*" "*"