## Pillow Example: BIBD treating blocks as random

We return to the Pillow Data (from ExpDesign3) an experiment run in a balanced incomplete block design (BIBD). This time we treat blocks as random. Comparing to our original analysis (treating blocks as fixed) we see that the results are different.

```
library(lme4)
library(lmerTest)
library(pbkrtest)
library(emmeans)
library(multcompView)
Pillow <- read.csv("C:/hess/STAT512/RNotes/ExpDesign3/ED3_PillowBIBD.csv")
str(Pillow)
## 'data.frame':
                   36 obs. of 3 variables:
   $ blk
             : int 1 1 1 2 2 2 3 3 3 4 ...
   $ pillow : Factor w/ 9 levels "A","B","C","D",..: 1 2 3 4 5 6 7 8 9 1 ...
## $ firmness: int 59 26 38 85 92 69 74 52 27 62 ...
#Important: Need to define blk as.factor!!!!
Pillow$blk<-as.factor(Pillow$blk)</pre>
Model <- lmer (firmness ~ pillow + (1|blk), data = Pillow)
summary(Model)
## Linear mixed model fit by REML t-tests use Satterthwaite approximations
    to degrees of freedom [lmerMod]
## Formula: firmness ~ pillow + (1 | blk)
     Data: Pillow
##
##
## REML criterion at convergence: 185.4
##
## Scaled residuals:
               1Q Median
## -1.5281 -0.7596 -0.0081 0.5565
                                  1.3103
##
## Random effects:
## Groups
            Name
                        Variance Std.Dev.
## blk
             (Intercept) 2.041
                                  1.429
                         33.381
                                  5.778
## Residual
## Number of obs: 36, groups: blk, 12
## Fixed effects:
                                       df t value Pr(>|t|)
              Estimate Std. Error
## (Intercept)
               59.286
                            2.969
                                   26.866 19.969 < 2e-16 ***
## pillowB
               -36.425
                            4.167
                                   24.185 -8.741 5.95e-09 ***
               -20.435
                                   24.185 -4.904 5.20e-05 ***
## pillowC
                            4.167
## pillowD
                17.624
                            4.167
                                   24.185
                                            4.229 0.000291 ***
## pillowE
                30.081
                            4.167
                                   24.185
                                            7.219 1.77e-07 ***
## pillowF
                10.372
                            4.167
                                   24.185
                                            2.489 0.020072 *
## pillowG
                15.359
                            4.167
                                   24.185
                                            3.686 0.001150 **
                                   24.185 -1.954 0.062335 .
## pillowH
                -8.143
                            4.167
## pillowI
               -25.753
                            4.167 24.185 -6.180 2.12e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Correlation of Fixed Effects:
          (Intr) pillwB pillwC pillwD pillwE pillwF pillwG pillwH
## pillowB -0.702
## pillowC -0.702 0.500
## pillowD -0.702 0.500 0.500
## pillowE -0.702 0.500 0.500 0.500
## pillowF -0.702 0.500
                         0.500
                               0.500
                                      0.500
## pillowG -0.702 0.500
                         0.500
                                0.500
                                      0.500 0.500
## pillowH -0.702 0.500 0.500 0.500 0.500 0.500 0.500
## pillowI -0.702 0.500 0.500 0.500 0.500 0.500 0.500 0.500
anova(Model, ddf="Kenward-Roger")
## Analysis of Variance Table of type III with Kenward-Roger
## approximation for degrees of freedom
         Sum Sq Mean Sq NumDF DenDF F.value
                                               Pr(>F)
## pillow 13422 1677.8
                            8 24.859 50.261 1.889e-13 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
emout <- emmeans(Model, pairwise ~ pillow)</pre>
emout
## $emmeans
                              df lower.CL upper.CL
  pillow
            emmean
                         SE
##
   Α
          59.28555 3.152629 26.9 52.81577 65.75533
##
  В
          22.86030 3.152629 26.9 16.39052 29.33008
  C
          38.85078 3.152629 26.9 32.38100 45.32056
          76.90929 3.152629 26.9 70.43951 83.37908
## D
##
  Ε
          89.36702 3.152629 26.9 82.89724 95.83680
  F
          69.65789 3.152629 26.9 63.18811 76.12768
##
##
  G
          74.64446 3.152629 26.9 68.17468 81.11424
## H
          51.14250 3.152629 26.9 44.67272 57.61228
##
          33.53219 3.152629 26.9 27.06241 40.00197
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
##
## $contrasts
##
   contrast
                             SE
                                   df t.ratio p.value
              estimate
   A - B
             36.425249 4.460253 24.86
##
                                      8.167 <.0001
##
   A - C
             20.434770 4.460253 24.86
                                       4.582 0.0030
  A - D
            -17.623742 4.460253 24.86 -3.951
                                              0.0139
  A - E
            -30.081469 4.460253 24.86 -6.744
##
                                              <.0001
##
   A - F
            -10.372341 4.460253 24.86
                                      -2.326 0.3651
##
   A - G
            -15.358903 4.460253 24.86 -3.444 0.0443
##
   A - H
             8.143056 4.460253 24.86
                                       1.826 0.6660
##
   A - I
             25.753359 4.460253 24.86
                                       5.774 0.0002
##
  B - C
            -15.990480 4.460253 24.86 -3.585 0.0323
##
  B - D
            -54.048991 4.460253 24.86 -12.118 <.0001
  B - F.
            -66.506719 4.460253 24.86 -14.911
##
                                              <.0001
## B - F
            -46.797590 4.460253 24.86 -10.492
##
  B - G
            -51.784153 4.460253 24.86 -11.610
                                              <.0001
##
  В - Н
            -28.282194 4.460253 24.86 -6.341
## B - I
            -10.671890 4.460253 24.86 -2.393 0.3302
```

```
C - D
            -38.058511 4.460253 24.86 -8.533 <.0001
##
   C - E
            -50.516239 4.460253 24.86 -11.326
                                               <.0001
##
   C - F
            -30.807111 4.460253 24.86
                                       -6.907
                                               <.0001
   C - G
##
            -35.793673 4.460253 24.86
                                       -8.025
                                               <.0001
   C - H
            -12.291714 4.460253 24.86
                                       -2.756
                                               0.1792
##
   C - I
              5.318590 4.460253 24.86
                                        1.192 0.9508
   D - E
            -12.457728 4.460253 24.86
                                       -2.793 0.1674
   D - F
              7.251401 4.460253 24.86
##
                                        1.626 0.7823
##
   D - G
              2.264838 4.460253 24.86
                                        0.508 0.9998
##
   D - H
             25.766797 4.460253 24.86
                                        5.777 0.0002
   D - I
             43.377101 4.460253 24.86
                                        9.725 < .0001
   E - F
##
             19.709129 4.460253 24.86
                                        4.419 0.0045
##
   E - G
             14.722566 4.460253 24.86
                                        3.301 0.0604
##
   E - H
                                        8.570 < .0001
             38.224525 4.460253 24.86
##
   E - I
             55.834829 4.460253 24.86 12.518 <.0001
   F - G
##
             -4.986562 4.460253 24.86
                                       -1.118 0.9657
##
   F - H
             18.515397 4.460253 24.86
                                        4.151 0.0086
                                        8.099 <.0001
##
   F - I
             36.125700 4.460253 24.86
##
   G - H
             23.501959 4.460253 24.86
                                        5.269 0.0005
## G - I
             41.112263 4.460253 24.86
                                        9.217 <.0001
## H - I
             17.610304 4.460253 24.86
                                       3.948 0.0140
##
## P value adjustment: tukey method for comparing a family of 9 estimates
cld(emout$emmeans)
```

```
SE
   pillow
                               df lower.CL upper.CL .group
##
   В
          22.86030 3.152629 26.9 16.39052 29.33008 1
##
   Ι
          33.53219 3.152629 26.9 27.06241 40.00197 12
##
  C
          38.85078 3.152629 26.9 32.38100 45.32056
## H
          51.14250 3.152629 26.9 44.67272 57.61228
                                                       34
          59.28555 3.152629 26.9 52.81577 65.75533
##
  Α
                                                        45
## F
          69.65789 3.152629 26.9 63.18811 76.12768
                                                         56
          74.64446 3.152629 26.9 68.17468 81.11424
                                                          67
## G
## D
          76.90929 3.152629 26.9 70.43951 83.37908
                                                          67
##
          89.36702 3.152629 26.9 82.89724 95.83680
                                                          7
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## P value adjustment: tukey method for comparing a family of 9 estimates
## significance level used: alpha = 0.05
```