

# Linear Analysis Result: truss1

unit: [N], [mm]

## Member Information:

EID	i	j	E [MPa]	I [mm^4]	A [mm^2]	L [mm]	$\theta$
1	1	2	2.00e+05	None	10000.0	5000.0	0
2	3	4	2.00e+05	None	10000.0	5000.0	0
3	1	3	2.00e+05	None	10000.0	9999.78	$0.33\pi$
4	2	4	2.00e+05	None	10000.0	9999.78	$0.33\pi$
5	2	3	2.00e+05	None	10000.0	8660.0	$0.5\pi$

EID	c	s	cs	c^2	s^2	AE/L	12EI/L^3	6EI/L^2	4EI/L	2EI/L
1	1.0	0.0	0.0	1.0	0.0	4.00e+05	None	None	None	None
2	1.0	0.0	0.0	1.0	0.0	4.00e+05	None	None	None	None
3	0.5	0.87	0.43	0.25	0.75	2.00e+05	None	None	None	None
4	0.5	0.87	0.43	0.25	0.75	2.00e+05	None	None	None	None
5	0.0	1.0	0.0	0.0	1.0	2.31e+05	None	None	None	None

## Member Local Stiffness:

$$[K1] = \begin{vmatrix} 4.00e+05 & 0.00e+00 & -4.00e+05 & -0.00e+00 \\ 0.00e+00 & 0.00e+00 & -0.00e+00 & -0.00e+00 \\ -4.00e+05 & -0.00e+00 & 4.00e+05 & 0.00e+00 \\ -0.00e+00 & -0.00e+00 & 0.00e+00 & 0.00e+00 \end{vmatrix}$$

$$[K2] = \begin{vmatrix} 4.00e+05 & 0.00e+00 & -4.00e+05 & -0.00e+00 \\ 0.00e+00 & 0.00e+00 & -0.00e+00 & -0.00e+00 \\ -4.00e+05 & -0.00e+00 & 4.00e+05 & 0.00e+00 \\ -0.00e+00 & -0.00e+00 & 0.00e+00 & 0.00e+00 \end{vmatrix}$$

$$[K3] = \begin{vmatrix} 5.00e+04 & 8.66e+04 & -5.00e+04 & -8.66e+04 \\ 8.66e+04 & 1.50e+05 & -8.66e+04 & -1.50e+05 \\ -5.00e+04 & -8.66e+04 & 5.00e+04 & 8.66e+04 \\ -8.66e+04 & -1.50e+05 & 8.66e+04 & 1.50e+05 \end{vmatrix}$$

$$\begin{aligned}
& \begin{vmatrix} -8.66e+04 & -1.50e+05 & 8.66e+04 & 1.50e+05 \end{vmatrix} \\
& \begin{vmatrix} 5.00e+04 & 8.66e+04 & -5.00e+04 & -8.66e+04 \\ 8.66e+04 & 1.50e+05 & -8.66e+04 & -1.50e+05 \\ -5.00e+04 & -8.66e+04 & 5.00e+04 & 8.66e+04 \\ -8.66e+04 & -1.50e+05 & 8.66e+04 & 1.50e+05 \end{vmatrix} \\
[K4] = & \\
& \begin{vmatrix} 8.66e-28 & 1.41e-11 & -8.66e-28 & -1.41e-11 \\ 1.41e-11 & 2.31e+05 & -1.41e-11 & -2.31e+05 \\ -8.66e-28 & -1.41e-11 & 8.66e-28 & 1.41e-11 \\ -1.41e-11 & -2.31e+05 & 1.41e-11 & 2.31e+05 \end{vmatrix} \\
[K5] = &
\end{aligned}$$

Structure Global Stiffness:

$$[K] = \begin{vmatrix} 4.50e+05 & 8.66e+04 & -4.00e+05 & 0.00e+00 & -5.00e+04 & -8.66e+04 & 0.00e+00 & 0.00e+00 \\ 8.66e+04 & 1.50e+05 & 0.00e+00 & 0.00e+00 & -8.66e+04 & -1.50e+05 & 0.00e+00 & 0.00e+00 \\ -4.00e+05 & 0.00e+00 & 4.50e+05 & 8.66e+04 & -8.66e-28 & -1.41e-11 & -5.00e+04 & -8.66e+04 \\ 0.00e+00 & 0.00e+00 & 8.66e+04 & 3.81e+05 & -1.41e-11 & -2.31e+05 & -8.66e+04 & -1.50e+05 \\ -5.00e+04 & -8.66e+04 & -8.66e-28 & -1.41e-11 & 4.50e+05 & 8.66e+04 & -4.00e+05 & 0.00e+00 \\ -8.66e+04 & -1.50e+05 & -1.41e-11 & -2.31e+05 & 8.66e+04 & 3.81e+05 & 0.00e+00 & 0.00e+00 \\ 0.00e+00 & 0.00e+00 & -5.00e+04 & -8.66e+04 & -4.00e+05 & 0.00e+00 & 4.50e+05 & 8.66e+04 \\ 0.00e+00 & 0.00e+00 & -8.66e+04 & -1.50e+05 & 0.00e+00 & 0.00e+00 & 8.66e+04 & 1.50e+05 \end{vmatrix}$$

Nodal Displacement & Nodal Load:

$$\begin{aligned}
& \begin{vmatrix} 0 \\ 0 \\ u2 \\ 0 \\ u3 \\ v3 \\ u4 \\ v4 \end{vmatrix} \quad \{R\} = \begin{vmatrix} Fx,1 \\ Fy,1 \\ 0 \\ Fy,2 \\ 0 \\ 0 \\ 282840.0 \\ -282840.0 \end{vmatrix}
\end{aligned}$$

Member Local P:

		0.00e+00				0.00e+00	
		0.00e+00				0.00e+00	
{P1} =		0.00e+00		{P2} =		0.00e+00	
		0.00e+00				0.00e+00	

		0.00e+00				0.00e+00	
		0.00e+00				0.00e+00	
{P3} =		0.00e+00		{P4} =		0.00e+00	
		0.00e+00				0.00e+00	

		0.00e+00	
		0.00e+00	
{P5} =		0.00e+00	
		0.00e+00	

### Structure Global P:

		0.00e+00	
		0.00e+00	
		0.00e+00	
		0.00e+00	
{P} =		0.00e+00	
		0.00e+00	
		0.00e+00	
		0.00e+00	

Nodal Displacement {rf}:

$$\{R_f\} = [K_{ff}]\{r_f\} + \{P_f\}$$

$$\{rf\} = [Kff]^{(-1)} \times (\{Rf\} - \{Pf\})$$

$$[Kff] = \begin{vmatrix} 4.50e+05 & -8.66e-28 & -1.41e-11 & -5.00e+04 & -8.66e+04 \\ -8.66e-28 & 4.50e+05 & 8.66e+04 & -4.00e+05 & 0.00e+00 \\ -1.41e-11 & 8.66e+04 & 3.81e+05 & 0.00e+00 & 0.00e+00 \\ -5.00e+04 & -4.00e+05 & 0.00e+00 & 4.50e+05 & 8.66e+04 \\ -8.66e+04 & 0.00e+00 & 0.00e+00 & 8.66e+04 & 1.50e+05 \end{vmatrix}$$

$$\{Rf\} = \begin{vmatrix} 0.00e+00 \\ 0.00e+00 \\ 0.00e+00 \\ 2.83e+05 \\ -2.83e+05 \end{vmatrix}$$

$$\{Pf\} = \begin{vmatrix} 0.00e+00 \\ 0.00e+00 \\ 0.00e+00 \\ 0.00e+00 \\ 0.00e+00 \end{vmatrix}$$

$$\Rightarrow \{rf\} = \begin{vmatrix} u2 \\ u3 \\ v3 \\ u4 \\ v4 \end{vmatrix} = \begin{vmatrix} -4.08e-01 \\ 1.47e+01 \\ -3.35e+00 \\ 1.58e+01 \\ -1.13e+01 \end{vmatrix}$$

Reaction Force {Rs}:

$$\{Rs\} = [Ksf]\{rf\} + \{Ps\}$$

$$[Ksf] = \begin{vmatrix} -4.00e+05 & -5.00e+04 & -8.66e+04 & 0.00e+00 & 0.00e+00 \\ 0.00e+00 & -8.66e+04 & -1.50e+05 & 0.00e+00 & 0.00e+00 \\ 8.66e+04 & -1.41e-11 & -2.31e+05 & -8.66e+04 & -1.50e+05 \\ 0.00e+00 & 0.00e+00 & 0.00e+00 & 0.00e+00 & 0.00e+00 \end{vmatrix}$$

$$\{P_s\} = \begin{bmatrix} 0.00e+00 \\ 0.00e+00 \end{bmatrix}$$

$$\Rightarrow \{R_s\} = \begin{bmatrix} F_{x,1} \\ F_{y,1} \\ F_{y,2} \end{bmatrix} = \begin{bmatrix} -2.83e+05 \\ -7.73e+05 \\ 1.06e+06 \end{bmatrix}$$

Member Force:

Truss: member1

$$S1 = (AE/L) \times \langle -c, -s, c, s \rangle \{r1\} = -1.63e+05$$

Truss: member2

$$S2 = (AE/L) \times \langle -c, -s, c, s \rangle \{r2\} = 4.46e+05$$

Truss: member3

$$S3 = (AE/L) \times \langle -c, -s, c, s \rangle \{r3\} = 8.92e+05$$

Truss: member4

$$S4 = (AE/L) \times \langle -c, -s, c, s \rangle \{r4\} = -3.27e+05$$

Truss: member5

$$S5 = (AE/L) \times \langle -c, -s, c, s \rangle \{r5\} = -7.73e+05$$