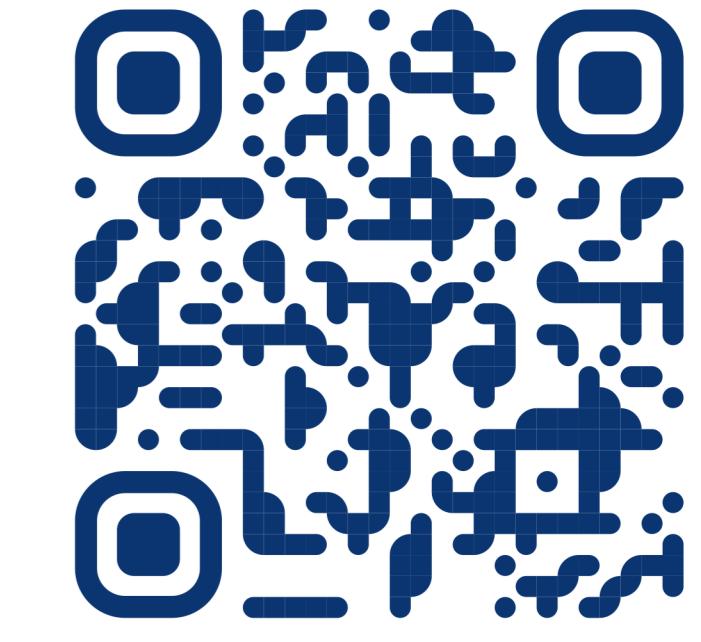


# Deblur e-NeRF: NeRF from Motion-Blurred Events under High-speed or Low-light Conditions

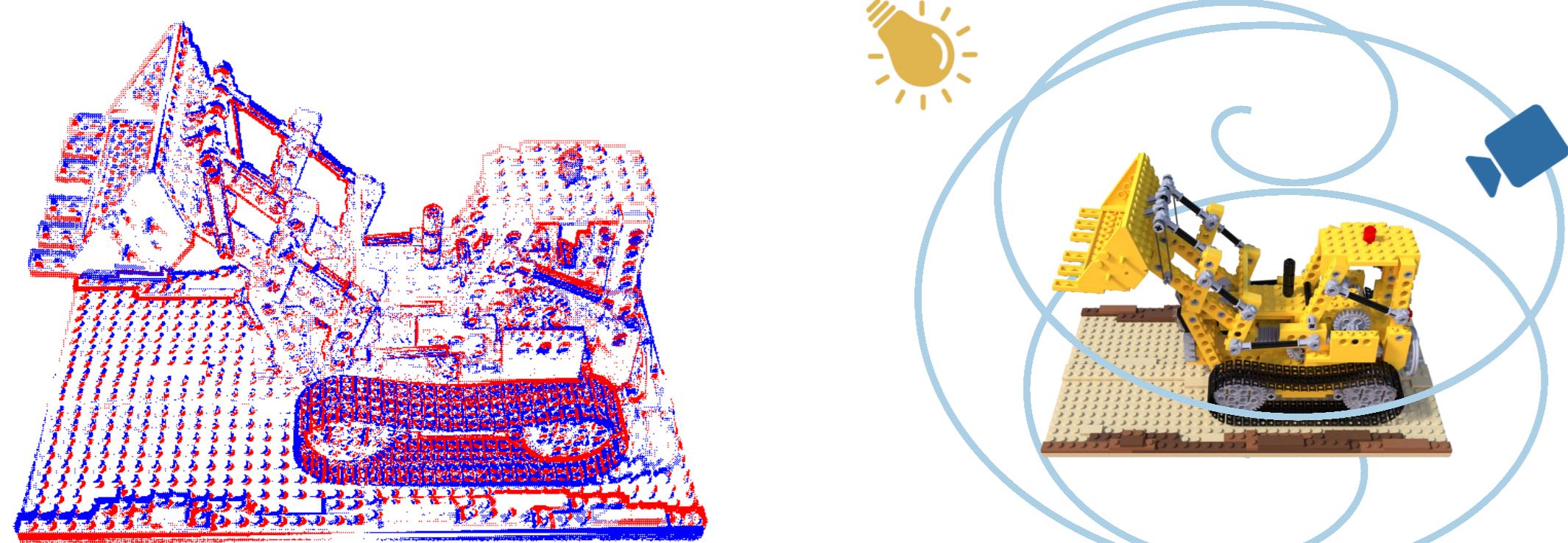
Weng Fei Low

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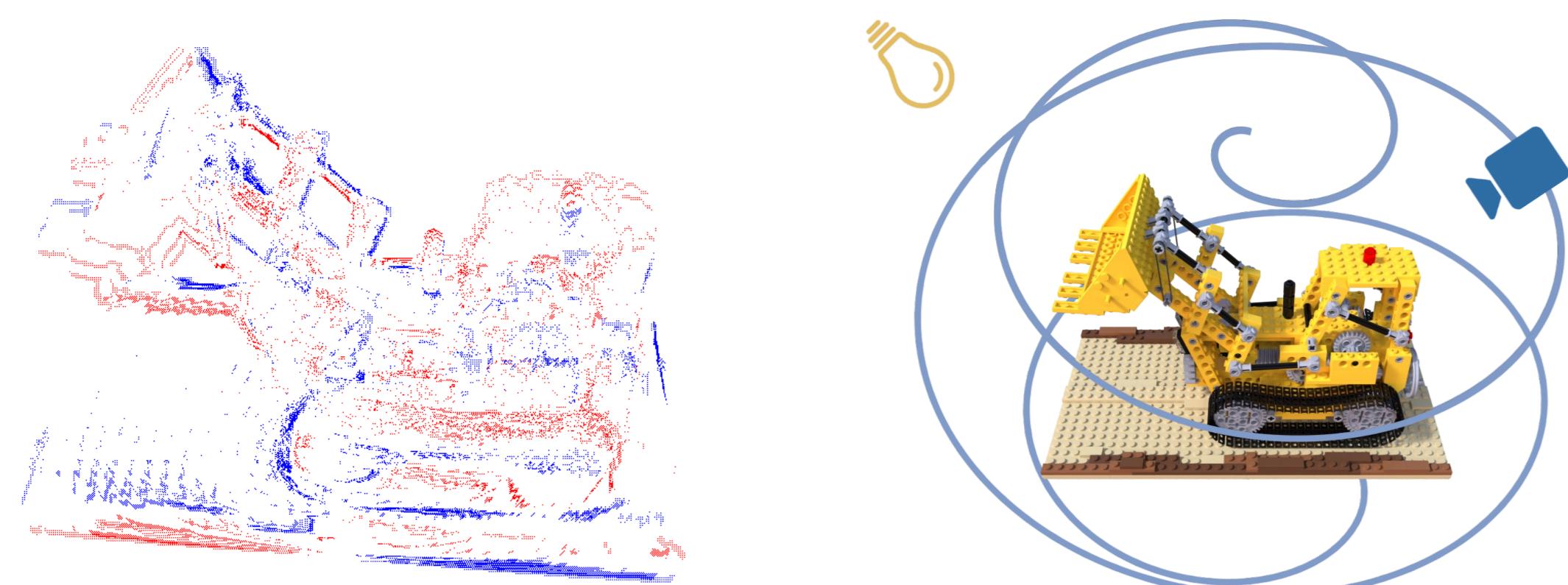


## Motivation

- Event cameras outperform standard cameras under:
  - High speed
  - High dynamic range
  - Low light
 due to their distinctive principle of operation
- However, event cameras also suffer from motion blur, especially under these challenging conditions
- This is due to the limited bandwidth of the event sensor pixel, which is mostly proportional to the light intensity



(a) Minimally motion-blurred events (left), under low speed and bright light (right).

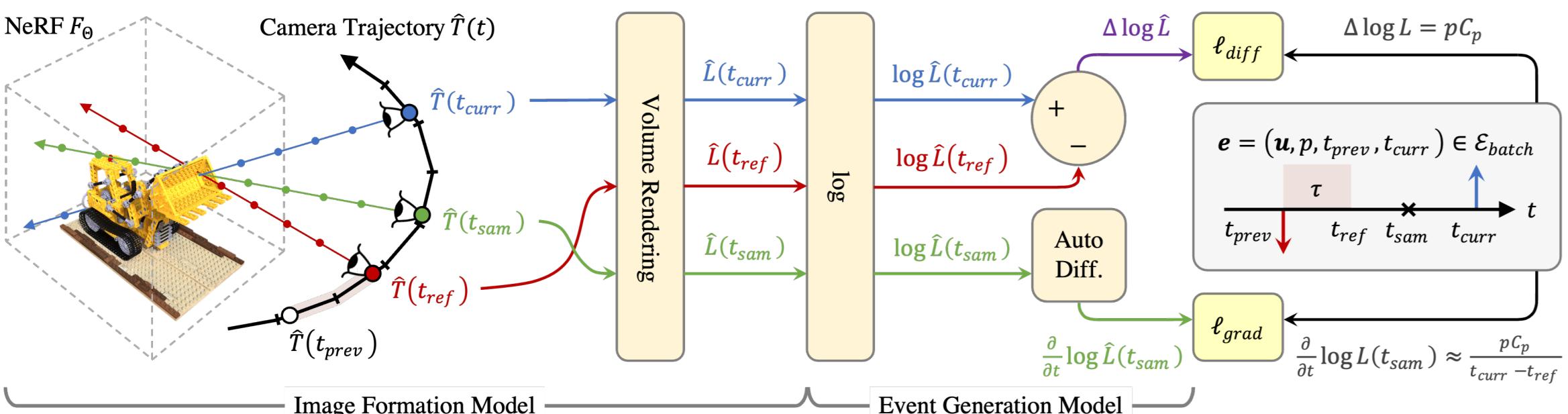


(b) Significantly motion-blurred events (left), under high speed and low light (right).

## Research Question

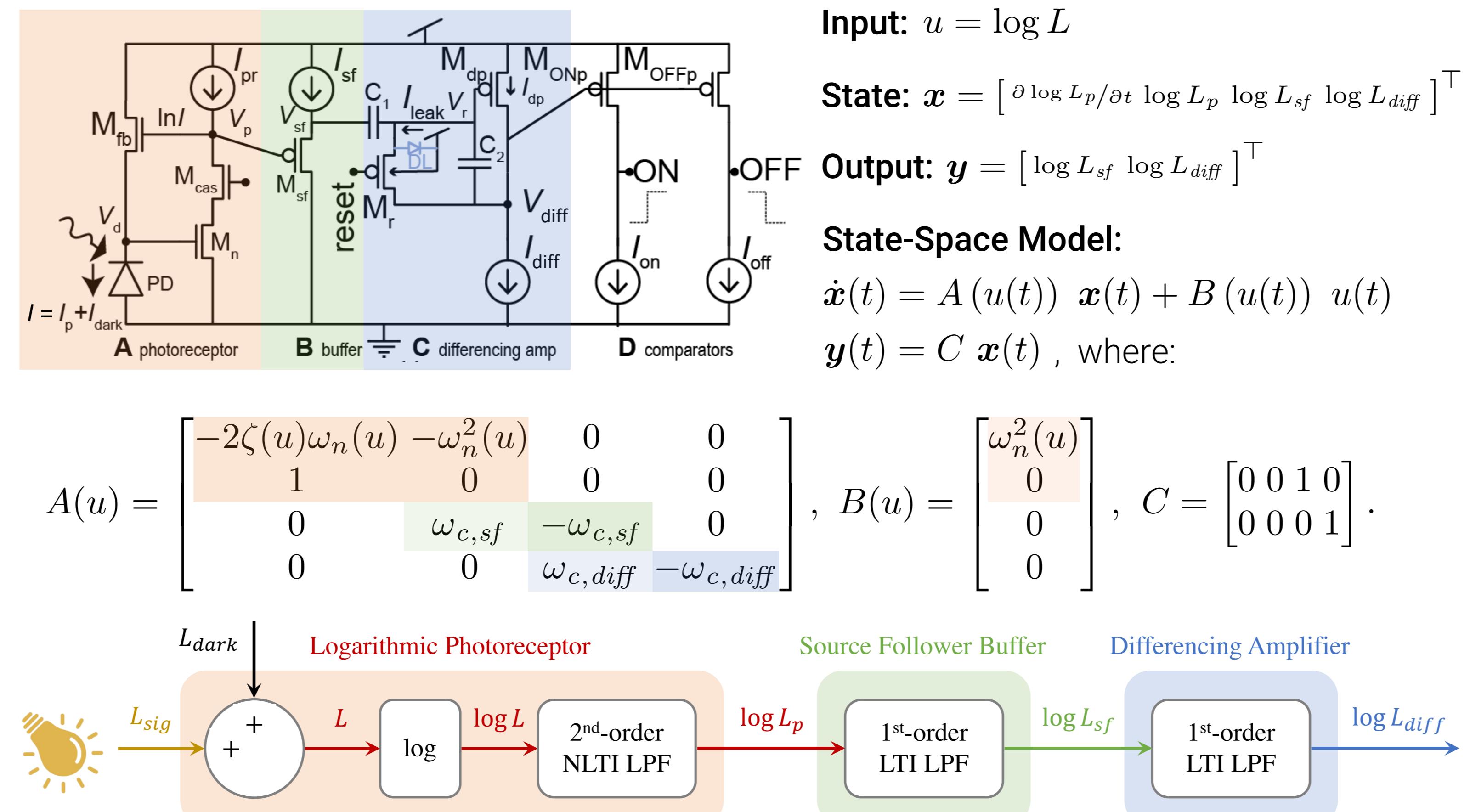
How to reconstruct blur-minimal NeRFs from motion-blurred events, generated under high-speed or low-light conditions?

## Prior Work: Robust e-NeRF



## Proposed Method: Deblur e-NeRF

### Pixel Bandwidth Model



Input:  $u = \log L$

State:  $\mathbf{x} = [\partial \log L_p / \partial t, \log L_p, \log L_{sf}, \log L_{diff}]^\top$

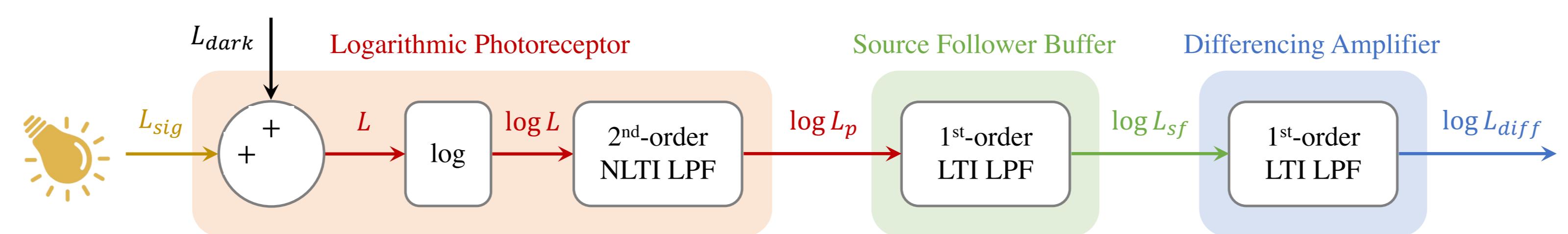
Output:  $\mathbf{y} = [\log L_{sf}, \log L_{diff}]^\top$

State-Space Model:

$$\dot{\mathbf{x}}(t) = A(u(t))\mathbf{x}(t) + B(u(t))u(t)$$

$$\mathbf{y}(t) = C\mathbf{x}(t), \text{ where:}$$

$$A(u) = \begin{bmatrix} -2\zeta(u)\omega_n(u) - \omega_n^2(u) & 0 & 0 \\ 1 & 0 & 0 \\ 0 & \omega_{c,sf} & -\omega_{c,sf} \\ 0 & 0 & \omega_{c,diff} - \omega_{c,diff} \end{bmatrix}, \quad B(u) = \begin{bmatrix} \omega_n^2(u) \\ 0 \\ 0 \\ 0 \end{bmatrix}, \quad C = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}.$$



### Synthesis of Motion-Blurred Effective Log-Radiance

Continuous-Time NLTI System

$$\dot{\mathbf{x}}(t) = A(t)\mathbf{x}(t) + B(t)u(t)$$

$$\mathbf{y}(t) = C\mathbf{x}(t)$$

Continuous-Time LTV System

$$\dot{\mathbf{x}}(t) = A[k]\mathbf{x}(t) + B[k]u(t)$$

$$\mathbf{y}(t) = C\mathbf{x}(t)$$

$$\mathbf{y}[k] \approx \sum_{i=k_0}^k \hat{\mathbf{w}}[i] u[i]$$

Discretize

$$\mathbf{x}[k+1] = A_d[k]\mathbf{x}[k] + B_d[k]u[k] + \tilde{B}_d[k]u[k+1]$$

$$\mathbf{y}[k] = C_d\mathbf{x}[k]$$

Discrete-Time LTV Solution

Discrete-Time LTV System

Importance Sampling:  $T_i \sim \text{Exp}(t_k - t_i; \omega_{c,dom,min}) = \omega_{c,dom,min} e^{-\omega_{c,dom,min}(t_k - t_i)}$

### Threshold-Normalized Total Variation Loss

$$\ell_{tv}(\mathbf{e}) = \left| \frac{\delta \log \hat{L}_{blur}}{\bar{C}} \right|, \text{ where } \bar{C} = \frac{1}{2}(C_{-1} + C_{+1}),$$

$$\delta \log \hat{L}_{blur} := \log \hat{L}_{blur}(\mathbf{u}, t_{end}) - \log \hat{L}_{blur}(\mathbf{u}, t_{start}).$$

### Translated-Gamma Correction

$\hat{L}_{sig,corr} = \mathbf{b} \odot \hat{L}^a - \mathbf{c}$ , where  $a, \mathbf{b}$  and  $\mathbf{c}$  are correction parameters.

## Novel View Synthesis Results

**Table 1:** Upper bound performance without event motion blur

Method	PSNR ↑ SSIM ↑ LPIPS ↓
E2VID + NeRF	19.49 0.847 0.268
Robust e-NeRF	28.48 0.944 0.054
Deblur e-NeRF	<b>29.43</b> <b>0.953</b> <b>0.043</b>

**Table 2:** Quantitative results of the real exps.

Method	08_peanuts_running			11_all_characters		
	PSNR ↑ SSIM ↑ LPIPS ↓					
E2VID + NeRF	14.85	0.690	0.595	13.12	0.695	0.627
Robust e-NeRF	18.00	0.677	0.507	15.91	0.677	0.552
Deblur e-NeRF	<b>18.27</b>	<b>0.695</b>	<b>0.503</b>	<b>16.53</b>	<b>0.710</b>	<b>0.511</b>

**Table 3:** Effect of camera speed. <sup>†</sup>Trained with 1/8× the batch size of baselines.

Method	v = 0.125×			v = 1×			v = 4×		
	PSNR ↑ SSIM ↑ LPIPS ↓								
E2VID + NeRF	18.58	0.849	0.259	18.85	0.839	0.278	17.82	0.804	0.328
Robust e-NeRF	28.31	0.943	0.050	26.11	0.924	0.074	22.18	0.861	0.122
Deblur e-NeRF <sup>†</sup>	<b>28.71</b>	<b>0.948</b>	<b>0.048</b>	<b>28.41</b>	<b>0.947</b>	<b>0.049</b>	<b>27.48</b>	<b>0.939</b>	<b>0.061</b>

**Table 4:** Effect of scene illuminance. <sup>†</sup>Trained with 1/8× the batch size of baselines.

Method	E <sub>sc</sub> = 100 000lux			E <sub>sc</sub> = 1 000lux			E <sub>sc</sub> = 10lux		
	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓
E2VID + NeRF	19.27	0.846	0.268	18.85	0.839	0.278	17.24	0.804	0.354
Robust e-NeRF	27.62	0.942	0.055	26.11	0.924	0.074	22.72	0.870	0.129
Deblur e-NeRF <sup>†</sup>	<b>28.73</b>	<b>0.948</b>	<b>0.047</b>	<b>28.41</b>	<b>0.947</b>	<b>0.049</b>	<b>28.62</b>	<b>0.935</b>	<b>0.059</b>

**Table 5:** Collective effect of camera speed and scene illuminance. <sup>†</sup>Trained with 1/8× the batch size of baselines.

Method	v = 0.125×, E <sub>sc</sub> = 100 000lux			v = 1×, E <sub>sc</sub> = 1 000lux			v = 4×, E <sub>sc</sub> = 10lux			
	Opt. C <sub>p</sub>	Opt. Ω	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	PSNR ↑ SSIM ↑ LPIPS ↓	
E2VID + NeRF	—	—	19.19	0.844	0.281	18.85	0.839	0.278	15.37	0.