

11. Suppose a particle in 1d is subjected to a potential  $a/\cos^2(x/X)$ . Using action-angle variables,
- (a) set up an expression for  $J$ , but do not do the integral. For what  $E$ 's is it possible to use action angle variables? Sketch the potential near the origin.
  - (b) Look at the case of small oscillations,  $x \ll X$ . Get the frequency by elementary means.
  - (c) Do the integral for  $dJ/dE$  for the case of small oscillations, and compare to the answer in (b). You may need the integral

$$\int \frac{dx}{(u^2 - x^2)^{1/2}} = \sin^{-1}(x/u)$$