COMPSCI/SFWRENG 2FA3

Discrete Mathematics with Applications II

Winter 2019

Assignment 8

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Revised: March 17, 2019

Assignment 8 consists of two problems. You must write your solutions to the problems using LaTeX.

Please submit Assignment 8 as two files, `Assignment_8_`*`YourMacID`*`.tex` and `Assignment_8_`*`YourMacID`*`.pdf`, to the Assignment 8 folder on Avenue under Assessments/Assignments. *`YourMacID`* must be your personal MacID (written without capitalization). The `Assignment_8_`*`YourMacID`*`.tex` file is a copy of the LaTeX source file for this assignment (`Assignment_8.tex` found on Avenue under Contents/Assignments) with your solution entered after each problem. The `Assignment_8_`*`YourMacID`*`.pdf` is the PDF output produced by executing

```
pdflatex Assignment_8_YourMacID
```

This assignment is due **Sunday, March 24, 2019 before midnight.** You are allow to submit the assignment multiple times, but only the last submission will be marked. **Late submissions and files that are not named exactly as specified above will not be accepted!** It is suggested that you submit your preliminary `Assignment_8_`*`YourMacID`*`.tex` and `Assignment_8_`*`YourMacID`*`.pdf` files well before the deadline so that your mark is not zero if, e.g., your computer fails at 11:50 PM on March 24.

Although you are allowed to receive help from the instructional staff and other students, your submission must be your own work. Copying will be treated as academic dishonesty! If any of the ideas used in your submission were obtained from other students or sources outside of the lectures and tutorials, you must acknowledge where or from whom these ideas were obtained.

Problems

1. **[10 points]** Construct a regular grammar that generates the language matched by the regular expression $0(00 + 11)^*1$.

   Yunbing Weng, wengy12, 03/24/2019

   $S \to 0T1$

   $T \to \epsilon|G|TG$

   $G \to 00|11$

2. **[10 points]** Let $\Sigma = (\mathcal{B}, \mathcal{C}, \mathcal{F}, \mathcal{P}, \tau)$ be a signature of MSFOL where:

   $\mathcal{B} = \{\alpha, \beta\}$.
   $\mathcal{C} = \{a, b\}$ with $\tau(a) = \alpha$ and $\tau(b) = \beta$.
   $\mathcal{F} = \{f\}$ with $\tau(f) = \alpha \times \beta \to \alpha$.
   $\mathcal{P} = \{p\}$ with $\tau(p) = \alpha \to \mathbb{B}$.

   Write a context-free grammar in BNF form that generates the set of Σ-formulas. Assume $\mathcal{V} = \{x, y, z\}$.

   Yunbing Weng, wengy12, 22/03/2019

   $< term >::=< term - \alpha > | < term - \beta >$

   $< term - \alpha >::=< const - \alpha >: \alpha| < func > | < var >: \alpha$

   $< term - \beta >::=< const - \beta >: \beta| < var >: \beta$

   $< func >::= f(< term - \alpha >, < term - \beta >)$

   $< const - \alpha >::= a$

   $< const - \beta >::= b$

   $< var >::= x|y|z$

   $< formula >::=< equality > | < predicate > | < negation > | < implication > | < universalquantification >$

   $< equality >::=< term >=< term >$

   $< predicate >::= p(< term - \alpha >)$

   $< negation >::= \neg < formula >$

   $< implication >::=< formula > \Longrightarrow < formula >$

   $< universalquantification >::=< UQ - \alpha > | < UQ - \beta >$

   $< UQ - \alpha >::= \forall c : \alpha. < formula >$

   $< UQ - \beta >::= \forall c : \beta. < formula >$