# 1 Trend vs. Cycle

#### Trend vs. Cycle

• Trend: growth rate

• Cycle: deviations from the trend

## The role of $\lambda$ in HP filter

- ullet  $\lambda$  captures how much one cares about the smoothness of the trend
- $\lambda \to 0$ : time-varying trend and there is no cycle
- $\lambda \to \infty$ : trend growth is constant

#### Problems with HP filters

- Instability of the HP trend at the margin.
- HP filter cannot separate demand from supply shocks (i.e., a slowdown in trend growth will be identified during a long-lasting recession).
- What is the right  $\lambda$  for HP filter?

#### Kalman filter

- The Kalman filter can easily handle missing data
- Future is a special case of missing data

# 2 Recessions vs. Expansions

#### Recessions

- Periods with contracting economic activity
- Two consecutive quarters of negative real GDP growth

#### Forecasting indicator: the yield curve

- Yield curve slope is historically one of the best predictors for upcoming recessions (especially in the US)
- All recessions were preceded by an inverted (negatively sloped) yield curves; yield curve was rarely inverted without a recession following

## Forecast vs. Nowcast

- Forecast = is a recession going to start during the next 12 months?
- Nowcast = is an economy in a recession right now?
- Good rule of thumb: a recession has started if 3-month change of the 3-month moving average of seasonally adjusted unemployment rate rises above 0.3 pp

## 3 Welfare Costs

#### Lucas calibration

The resulting estimate for costs of economic fluctuations is tiny! Why should anyone care about business cycles?

- observed fluctuations are the ones resulting despite macroeconomic stabilization policies (could have been even larger without stabilization)
- cost of business cycles are not equally distributed over population
- direct costs of unemployment (negative impact on life satisfaction)
- persistent effects of economic fluctuations (recessions lead to a permanent level shift in the trend)

#### 4 Comovement

#### **DFM**

- Summarize the data and extract a signal for the current underlying dynamic in an economy
- Essential toolkit for all CBs
- Useful to monitor incoming data
- Good for nowcasts, but not helpful for medium-term forecasts

### What is the first principal component doing intuitively?

• The first principal component of a dataset corresponds to  $f_t$ , which is an underlying force driving the common variation in the dataset

## Why is the DFM useful for monitoring the business cycle?

 can be updated in realtime, allows us to consider all the data simultaneously instead of just focusing on one individual time series

## Conclusion

- The business cycle affects many aspects of the economy
- Therefore, it can be seen in many time series (e.g. GDP, unemployment, productivity)
- DFM is very useful if you want to have a more timely and broad-based measure of current dynamics

# 5 Computing Swiss GDP

- Estimation
  - annual GDP adds up value added according to firm survey
  - is estimated from production side
  - first estimate published 8 months after the end of reference year (i.e. first estimate for 2021 will be published at the end of August 2022)

- Quarterly GDP is an inter- and extra-polation of annual GDP
  - The preliminary estimate does not typically add up to observed annual GDP
  - Chow-Lin approach
- Interpolation vs. Extrapolation
  - The quarterly series is an interpolation for the years for which there is an annual estimate available (e.g. 2020)
  - It is an extrapolation for the latest quarters
- GDP is continuously revised
  - Indicators are revised
  - Annual estimates are revised
  - Benchmark revisions
  - Quarterization revisions: new indicators, new sa methods
  - Changes in estimated Chow-Lin coefficients

# 6 New Keynesian Model

• NKIS curve

$$c_t \simeq \mathbb{E}_t c_{t+1} - \frac{1}{\sigma} (i_t - \mathbb{E}_t \pi_{t+1} - \rho) + \frac{1 - \rho_z}{\sigma} z_t$$

- IS curve describes current aggregate demand as a function of endogenous variables (future demand, inflation), the interest rate, and an exogenous shock
- Monetary policy rate

$$i_t = MP\left(\pi_t \atop +\right) + v_t$$

- Monetary policy reacts to higher inflation by raising the interest rate
- Monopolistic competition
  - Because each firm produces a differentiated good that is not perfectly substitutable, each firm has some monopoly power
- Profit maximizing price under flex prices

$$P_t^*(i) = \frac{\varepsilon}{\varepsilon - 1} \frac{W_t}{A_t}$$

- Profit-maximizing price is the same for all firms,  $P_t^*(i) = P_t^*$
- Profit-maximizing price does not depend on  $YP^{\varepsilon}$  (but total profits do)
- $-YP^{\varepsilon}$  is a measure for how many units a firm can sell for any given price
- Labor market equilibrium under flex price

$$Y_t = A^{\frac{1+\varphi}{\varphi+\sigma}} \left(\frac{\varepsilon-1}{\varepsilon}\right)^{\frac{1}{\varphi+\sigma}}$$

- Equilibrium production does not depend on prices
- The trilemma of international finance
  - A country cannot simultaneously have an independent monetary policy, a fixed exchange rate, and capital mobility

- Reasoning: arbitrage. If interest rates between two countries differ, but the exchange rate is fixed, capital will flow to the country with higher interest rate
- Profit maximization with sticky prices

$$O_t = \mathbb{E}_t \left[ \sum_{j=0}^{\infty} \omega_j P_{t+j}^* \right] \quad \text{where} \quad \omega_j = \frac{\frac{\theta^j}{R_{i+j}} Y_{t+j} P_{t+j}^{\varepsilon}}{\sum_{j=0}^{\infty} \frac{\theta^J j}{R_{i+j}} Y_{t+j} P_{t+j}^{\varepsilon}} \right]$$

- The optimal price under sticky prices,  $O_t$ , is a weighted average of optimal prices under flexibility
- $-\theta^{j}$ : the probability that the price is still in place in t+j
- $-\frac{1}{R_{t+1}}$ : the present value of the profit that is generated in t+j
- $-\ Y_{t+j}$ : aggregate demand in t+j (i.e. how many units are expected to be sold)
- $Y_{t+j}P_{t+j}^{\varepsilon}$ : it shifts demand for a given price
- Log-linear approximation of the optimal price

$$o_t \simeq \sum_{i=0}^{\infty} \frac{(\beta \theta)^j}{\sum_{k=0}^{\infty} (\beta \theta)^k} \mathbb{E}_t p_{t+j}^*$$

- We did an approximation around steady state
- In steady state  $Y_{t+j}P_{t+j}^{\varepsilon}$  is constant and therefore cancels out
- In steady state,  $i = -\log \beta = \log \frac{1}{\beta} \simeq \frac{1}{\beta} 1$ ,  $\pi = 0$
- Optimal price under sticky prices

$$o_t = (1 - \beta \theta) p_t^* + \beta \theta \mathbb{E}_t o_{t+1}$$

- The optimal price today is a weighted average of today's flexible price and tomorrow's optimal price
- Higher discounting  $(\beta \downarrow)$  and more often firms adjust  $(\theta \downarrow)$ , the larger weight on today's flexible price
- Aggregate price dynamics

$$\pi_t = (1 - \theta)(o_t - p_{t-1})$$

Intuition: inflation is driven by

- how much adjusting firms change prices,  $o_t p_{t-1}$
- how many firms can reset prices,  $1 \theta$
- adjusting firm choose high  $o_t$  if
  - \* they expect high optimal price in the future,  $\mathbb{E}_t o_{t+1}$
  - \* current flex price,  $p^*$ , is high
- Inflation

$$\pi_t = \frac{1 - \theta}{\theta} (1 - \beta \theta) (p_t^* - p_t) + \beta \mathbb{E}_t \pi_{t+1}$$

Inflation is high whenever

- expected inflation is high (comes from adjusting firms choosing high  $o_t$  because they expect high  $\mathbb{E}_t o_{t+1}$ )
- current flex prices are high relative to the price level,  $p_t^* p_t$  (comes from adjusting firms choosing high  $o_t$  because  $p_t^*$  is high)
- When is  $(p_t^* p_t)$  high?

$$\frac{P_t^*}{P_t} = \frac{\varepsilon}{\varepsilon - 1} \frac{1}{A_t} \frac{W_t}{P_t}$$

- $-p_t^*-p_t$  is high, if real wage  $\frac{W_t}{P_t}$  is high (reason: high real wage implies high costs for firms)
- Natural level of output

$$\frac{P_t^*}{P_t} = \left(\frac{Y_t}{Y_t^n}\right)^{\varphi + \sigma}$$

- Whenever the output is above natural level, the optimal flex price is above the price index generating upward pressure on inflation
- NKPK

$$\pi_t = \frac{1 - \theta}{\theta} (1 - \beta \theta)(\varphi + \sigma)(y_t - y_t^n) + \beta \mathbb{E}_t \pi_{t+1}$$

- The output gap is proportional to  $p_t^* p_t$
- $-p_t^*-p_t$  is high, whenever
  - \* production is high,  $\frac{P_t^*}{P_t} = \frac{\varepsilon}{\varepsilon 1} A_t^{-\varphi 1} Y_t^{\varphi + \sigma}$
  - \* the output gap is positive,  $\frac{P_t^*}{P_t} = \left(\frac{Y_t}{Y_t^n}\right)^{\varphi + \sigma}$
  - \* a high production requires a lot of labor, which can only be drawn into the labor market via high real wages
  - \* high production equals a positive output gap
- The natural real interest rate

$$r_t^n = \rho + \sigma \mathbb{E}_t[\Delta y_{t+1}^n] + (1 - \rho_z) z_t$$

- Real natural interest rate is the interest rate if the output gap is closed and inflation is on target in t
- The output gap is expected to remain closed in the next period and inflation to remain on target
- $r_t^n$  increases with growth of natural level of output, also depends on shock  $z_t$

## 7 Pandenomics

#### Drawbacks of SIR model

- Behavior does not depend on probability of getting infected (i.e. the number of contacts is given exogenously)
- There exists no interaction with economic decisions

### Macro-SIR model

- In Macro-SIR model
  - Stronger recession
  - Less deaths
- Why?
  - Individuals take into account the risk of getting infected at workplace or shops
  - The higher the number of new infections, the larger the risk of getting infected, the more cautious are individuals
- The decentralized equilibrium can be improved when containment measures are introduced
  - In decentralized equilibrium, people only take into account the risk of getting infected but they do
    not consider their effect on the overall spread of the disease (i.e. negative externality)
- The optimal policy is to immediately introduce severe containment measures
  - Overall utility increases because of fewer deaths
  - Minimizes deaths at the cost of a larger recession in the beginning
- Limitations
  - Policies to mitigate economic hardships are not considered

- Financial markets are not included
- Sticky prices
  - $\ast$  Sticky prices alleviate the impact of a negative supply shift because the pandemic is not only a demand but also a supply shock
- Vaccine assumed to work perfectly
- Age-dependent health risks are not considered