

Recurrent Event Analysis with **reda** and **reReg**

Recurrent event data arise in situations where the event of interest, such as hospital admissions, infections, or tumor recurrences, can recur in the same individual during follow-up. The standard “time-to-first” event analysis cannot capture the cumulative experience of the recurrent events and could lead to invalid inferences. The R packages **reda** (Wang et al., 2020) and **reReg** (HanChiou and Huang, 2020) provide a collection of visualization tools and statistical methods for exploring and analyzing recurrent event data.

Suppose in a study consists of a random sample of n subjects and $N_i(t)$ be the number of events the i th subject experienced over the interval $[0, t]$. Let D be the failure time of interest that could either be a terminal event (e.g., death) or a non-terminal event (e.g., treatment failure). Let C be the potential censoring time for reasons other than the failure event, the observed data are independent and identically distributed copies $\{N_i(t), Y_i, X_i; t \leq Y_i, i = 1, \dots, n\}$, where $Y_i = \min(D, C)$, $\Delta_i = I(D \leq C)$, X_i is a covariate vector, $I(\cdot)$ is the indicator function, and the recurrent event process $N_i(\cdot)$ is observed up to the composite censoring time Y_i . Suppose we are interested in making inference about the recurrent event process and the failure event in the time interval $[0, \tau]$, where the constant τ is determined with the knowledge that recurrent and failure events could potentially be observed up to time τ . We will illustrate the rehospitalization data (González et al., 2005) from the **frailtypack** package (Rondeau et al., 2019).

In the packages **reda** and **reReg**, recurrent event data are represented using an object of type **Recur** created by the **Recur()** function. The **Recur** object is an S4 class object that bundles together a set of recurrent times, failure time, and censoring status, allowing users an easy first glance of the recurrent event data. The **Recur** object is also used as the formula response for many key functions in **reda** and **reReg**. The following commands can be used to create a **Recur** object corresponding to the rehospitalization data:

```
library(reda); library(reReg)
data(readmission, package = "frailtypack")
with(readmission, Recur(t.stop, id, event, death))
```

Error: Subjects having multiple terminal events:
60, 109, 280.

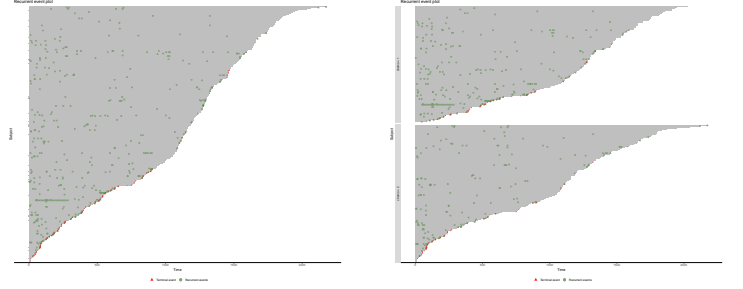
The **Recur()** internally checks whether the specified data fits into the recurrent event data framework and detected a possible issue on the data structure. The **show()** method for **Recur** objects presents recurrent events in intervals, where events happened at end of the recurrent episodes with censoring due to (or not) terminal indicated by a trailing + (or *). The following prints the **Recur** object for the first five subjects.

```
with(readmission[1:14,], Recur(t.stop, id, event, death))
```

```
[1] 1: (0, 24], (24, 457], (457, 1037+]
[2] 2: (0, 489], (489, 1182+]
[3] 3: (0, 15], (15, 783*]
[4] 4: (0, 163], (163, 288], ..., (686, 2048+]
[5] 5: (0, 1134], (1134, 1144+]
```

Another easy way to glance at recurrent event data is by event plots, which can be created by applying the generic function **plot()** to the **Recur** object when the **reReg** package is loaded. Additionally, the **plotEvents()** function from the **reReg** package allows users to stratify the event plots by discrete variables. The following codes produces event plots with and without stratifying by whether the patients receive chemotherapy.

```
df0 <- subset(readmission, !(id %in% c(60, 109, 280)))
obj <- with(df0, Recur(t.stop, id, event, death))
plot(obj, legend = "bottom") ## no stratification
fn <- Recur(t.stop, id, event, death) ~ chemo
plotEvents(fn, data = df0, legend = "bottom") ## by chemo
```



(a) No stratification

(b) Stratified by **chemo**

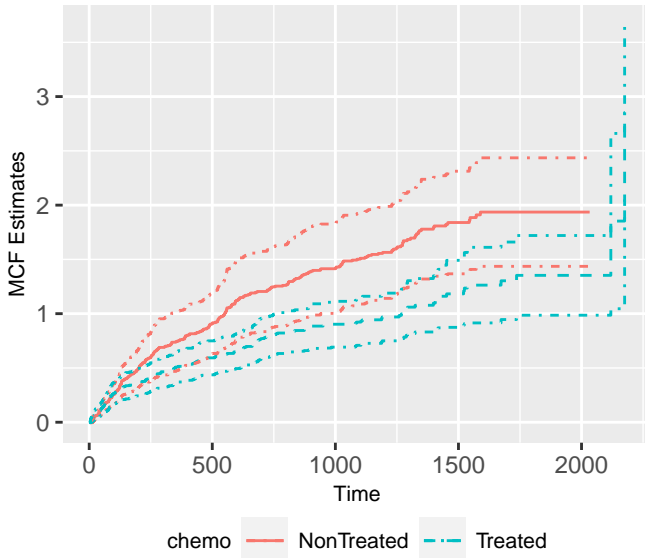
Figure 1: Event plots

The mean cumulative function (MCF) is often the focus in a nonparametric analysis of recurrent data. Let $M_i(t) = \mathbb{E}\{N_i(t)\}$ denote the MCF of $N_i(t)$. The Nelson-Aalen estimator (Nelson, 2003) are widely utilized in exploring the trend of recurrent event data.

$$\hat{M}(t) = \int_0^t \frac{dN(s)}{\delta(s)},$$

where $dN(s) = \sum_{i=1}^k dN_i(s)$, $\delta(s) = \sum_{i=1}^k \delta_i(s)$, $dN_i(s)$ and $\delta_i(s)$ is, respectively, the jump size and at-risk indicator of process i at time s . The MCF can be visualized by plotting the **Recur** object with argument **MCF = TRUE** when the **reReg** package is active. The **reReg** package also offers the **plotMCF()** function for plotting MCF estimates to be stratified by discrete variables. Alternatively, the **mcf()** function from the **reda** package provides a more sophisticated approach to plot MCFs. Some of the unique features the **mcf()** has include the different variance estimations, confidence interval constructions, and predictions. The following example uses the **mcf()** function to visualize MCF estimates stratified by whether the patients receive chemotherapy. The **plot()** method, as well as the **plotEvents()** function, return a **ggplot2** object (Wickham, 2016) so that users may further customize the plot easily.

```
re_mcf <- mcf(fn, data = df0)
plot(re_mcf, conf.int = TRUE, lty = 1:2) +
  ggplot2::theme(legend.position = "bottom")
```



Furthermore, the MCF difference between two groups can be tested with the two-sample pseudo-score tests (Cook et al., 1996) via `mcfDiff.test()` as follows:

```
mcfDiff.test(re_mcf)
```

Two-Sample Pseudo-Score Tests:

	Statistic	Variance	Chisq	DF	Pr(>Chisq)
Constant Weight	47.49	416.71	5.41	1	0.020 *
Linear Weight	36.56	263.59	5.07	1	0.024 *

Signif. codes:

0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Variance Estimator: robust

Both the constant weighted and the linear weighted tests indicate the MCF estimates are statistically different at a significance level of 0.05.

The `reReg()` function from the **reReg** package provides flexible approaches to fit semiparametric regression model to recurrent event data. At the default specification, a joint scale-change model for the recurrent event process and the failure time is fitted. Specifically, the joint model takes the form of

$$\lambda(t) = Z\lambda_0(te^{X^\top\alpha})e^{X^\top\beta}; h(t) = Zh_0(te^{X^\top\alpha})e^{X^\top\beta}, \quad (1)$$

where Z is a latent shared frailty variable to account for association between the two types of outcomes, and (α, β) is the regression coefficient.

Reference

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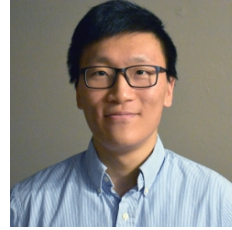
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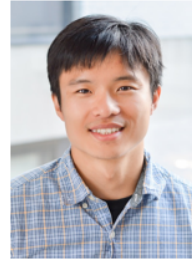
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Wenjie Wang
Research Scientist
Machine Learning, Artificial
Intelligence, and Connected Care
Advanced Analytics and Data Sciences
Eli Lilly and Company
Email: wang_wenjie@lilly.com



Sy Han Chiou
Assistant Professor
Department of Mathematical Sciences
University of Texas at Dallas
Email: schiou@utdallas.edu