

# Report of assignment 1

## 1. Flowchart

According to the flowchart, I used “if-elif-else” structure to define a method “Print\_values(a, b, c)” with three arguments a, b, c. Either applied random.random() to create random a, b, c or set certain a, b, c and then call for method Print-value(a, b, c), the console windows showed like this:

```
c = 1
```

```
a = 2
```

```
b = 3
```

Print\_values(a, b, c) : when b is the biggest one, the output is to print empty.

```
c = 1
```

```
a = 3
```

```
b = 2
```

```
Print_values(a, b, c)
```

```
3, 2, 1
```

```
c = 1
```

```
a = 3
```

```
b = 1
```

```
Print_values(a, b, c)
```

```
3, 1, 1
```

```
c = 4
```

```
a = 3
```

```
b = 1
```

```
Print_values(a, b, c)
```

```
4, 3, 1
```

```
c = 4
```

```
a = 2
```

```
b = 3
```

```
Print_values(a, b, c)
```

```
4, 3, 2
```

```
a = random.random();
```

```
b = random.random();
```

```
c = random.random();
```

```
Print_values(a, b, c)
```

```
0.2703991133069813, 0.10372005239302096, 0.08213798389241322
```

## 2. Matrix multiplication

### 2.1

For making matrix, I referred this website:

[https://blog.csdn.net/qq\\_43287650/article/details/82860938](https://blog.csdn.net/qq_43287650/article/details/82860938)

In this website, I learned how to use “numpy” to generate all types of matrices or array. Selecting from it, I used “np.random.randint(lower\_lim, upper\_lim, [nrow, ncol])”.

This randint() is a method to fill integer number randomly chosen from number “lower\_lim” to number “upper\_lim” into a matrix with row and column number equating to nrow and ncol respectively.

So M1 (5 rows and 10 columns ) is :

```
M1 = np.random.randint(0, 51, [5, 10])
```

M1

Out[52]:

```
array([[45,  6, 36, 26, 21,  8, 17, 39, 33, 24],
       [12, 17,  4,  6, 33, 34, 24,  0, 16, 27],
       [ 6, 45, 22, 39, 18,  6, 20, 44, 36, 12],
       [47, 13, 32, 41, 12, 32, 14, 25, 29, 13],
       [21, 40, 13, 21, 25, 22, 23,  5, 26, 44]])
```

M2 (10 rows and 5 columns ) is:

```
M2 = np.random.randint(0, 51, [10, 5])
```

M2

Out[54]:

```
array([[16, 25, 37, 30, 44],
       [16, 31, 13,  2, 31],
       [47,  4, 47, 39, 10],
       [16, 20, 41, 43, 15],
       [48,  4, 28, 34, 45],
       [39, 48, 35, 45, 29],
       [46, 10, 10, 27,  6],
       [19,  9, 44,  1,  6],
       [50, 35,  7,  4, 43],
       [22, 44, 10, 24, 11]])
```

### 2.2

I defined a method Matrix\_multip(M1, M2). In this method, get one row and one column for M1, M2 by x, y in for loop respectively, then, multiple each single elements and make a sum to form M3[x,y]. Finally, I did a test by python ‘dot’ function. For specific results like this:

M3

Out[57]:

```
array([[7945., 5175., 7726., 6164., 6112.],
       [6156., 4715., 3835., 4820., 4785.],
       [7392., 5157., 6662., 4703., 5512.],
       [7799., 6062., 8122., 7126., 6498.]])
```

```
M4 = np.dot(M1,M2)
M3 == M4
Out[56]:
array([[ True,  True,  True,  True,  True],
       [ True,  True,  True,  True,  True],
       [ True,  True,  True,  True,  True],
       [ True,  True,  True,  True,  True]])
```

Pascal triangle is showed in figure below (from Baidu):

			1				n=1
		1		1			n=2
	1		2		1		n=3
	1	3		3		1	n=4
	1	4	6		4	1	n=5
1	5	10	10	5		1	n=6
1	6	15	20	15	6	1	n=7

Firstly, a “jc(k)” function is defined to calculate factorial of number k. Then combination number of k is “b = jc(k)/jc(k-a)/jc(a)”. So we can do Pascal\_triangle(k) to show the kth line of pascal triangle. Results like this:

Out[111]: [1]

Out[112]: [1, 1]

Out[113]: [1, 2, 1]

Out[114]: [1, 3, 3, 1]

Out[115]: [1, 4, 6, 4, 1]

Out[116]: [1, 5, 10, 10, 5, 1]

Pascal\_triangle(100)

Out[119]:

```
[1,
 99,
4851,
156849,
3764376,
71523144,
1120529256,
14887031544,
171200862756,
1731030945644,
15579278510796,
126050526132804,
924370524973895,
6186171974825304,
38000770702498296,
215337700647490336,
1130522928399324288,
5519611944537877504,
25144898858450329600,
107196674080761937920,
428786696323047751680,
1613054714739084230656,
5719012170438571720704,
19146258135816089894912,
60629817430084289560576,
181889452290252818350080,
517685364210719585730560,
1399667836569723550564352,
3599145865465002725474304,
8811701946483283423395840,
20560637875127662394998784,
45764000431735766071115776,
97248500917438495384928256,
197443926105102399720914944,
383273503615786966757408768,
711793649572175834674888704,
1265410932572756856170086400,
2154618614921180756379172864,
3515430371713505560356716544,
5498493658321124166161399808,
8247740487481687348753727488,
11868699725888281821365403648,
```

16390109145274292058913243136,  
21726423750712436063073206272,  
27651812046361279063513890816,  
33796659167774902497245659136,  
39674339023040090311067959296,  
44739148260023941546373021696,  
48467410615025938141252943872,  
50445672272782101035857477632,  
50445672272782101035857477632,  
48467410615025946937345966080,  
44739148260023941546373021696,  
39674339023040099107160981504,  
33796659167774898099199148032,  
27651812046361279063513890816,  
21726423750712436063073206272,  
16390109145274294257936498688,  
11868699725888281821365403648,  
8247740487481687348753727488,  
5498493658321125265673027584,  
3515430371713505560356716544,  
2154618614921180756379172864,  
1265410932572757131047993344,  
711793649572175972113842176,  
383273503615786966757408768,  
197443926105102399720914944,  
97248500917438495384928256,  
45764000431735757481181184,  
20560637875127662394998784,  
8811701946483283423395840,  
3599145865465003262345216,  
1399667836569723282128896,  
517685364210719652839424,  
181889452290252851904512,  
60629817430084281171968,  
19146258135816085700608,  
5719012170438571720704,  
1613054714739084492800,  
428786696323047686144,  
107196674080761921536,  
25144898858450333696,  
5519611944537877504,  
1130522928399324288,  
215337700647490368,  
38000770702498296,

```

6186171974825304,
924370524973895,
126050526132804,
15579278510796,
1731030945643,
171200862756,
14887031543,
1120529256,
71523144,
3764376,
156849,
4851,
99,
1]

```

```
Pascal_triangle(200)
```

```
Traceback (most recent call last):
```

```

File "<ipython-input-120-6e8cb372cac1>", line 1, in <module>
    Pascal_triangle(200)

```

```

File "<ipython-input-117-21e9c58fe877>", line 8, in Pascal_triangle
    b = jc(k)/jc(k-a)/jc(a)

```

```
OverflowError: integer division result too large for a float
```

```
Pascal_triangle(200) is too large to print, sorry...
```

#### 4. Least moves

Least moves is :

Divide RMB K by 2, if the reminder is 1, make  $(K - 1)$  replace K, otherwise, make  $K/2$  replace

K. Use i to count the times of doing each operation.

Result is:

```
1, 2, 4, 5
```

```
Least_moves(5)
```

```
Out[128]: 3
```

```
1, 2, 4, 5, 10
```

```
Least_moves(10)
```

```
Out[129]: 4
```

```
1, 2, 3, 6, 12, 24, 48, 49, 98, 99
```

```
Least_moves(99)
```

```
Out[130]: 9
```

## 5. Dynamic programming

In this question, though I made a lot of reference, question was truly settled down.

My idea is:

1. I need to insert "+", "-", and nothing (this is to make N-digital number) into 123456789, therefore, I should firstly make probabilities of (+, -, "") into a list. The list should have a number to the eighth power of 3.

Here, I referred: <https://code-examples.net/zh-CN/q/197e4>. And used "itertools" to get the list.

itertools.product([a,b,c], repeat = N) function can get all the probabilities of arbitrarily place these number, a, b, c, in these N postions.

2. Once I get the list, I should combine each one in the list with 123456789, which means inserting each probability of "+-'" between each single number of 12456789, to make the final expression that we want, of course "= X" should be added in the end. however, before adding "=X", we should judge whether the result of expression match X or not.

Here, I referred: <http://c.biancheng.net/view/4277.html> to use "join()" function to combine and get expression. "join()" can join two string into one.

I referred: [https://blog.csdn.net/weixin\\_43097301/article/details/82933099](https://blog.csdn.net/weixin_43097301/article/details/82933099) to use "eval()" calculate string, which mean making the string expression into real calculation formula and return the result.

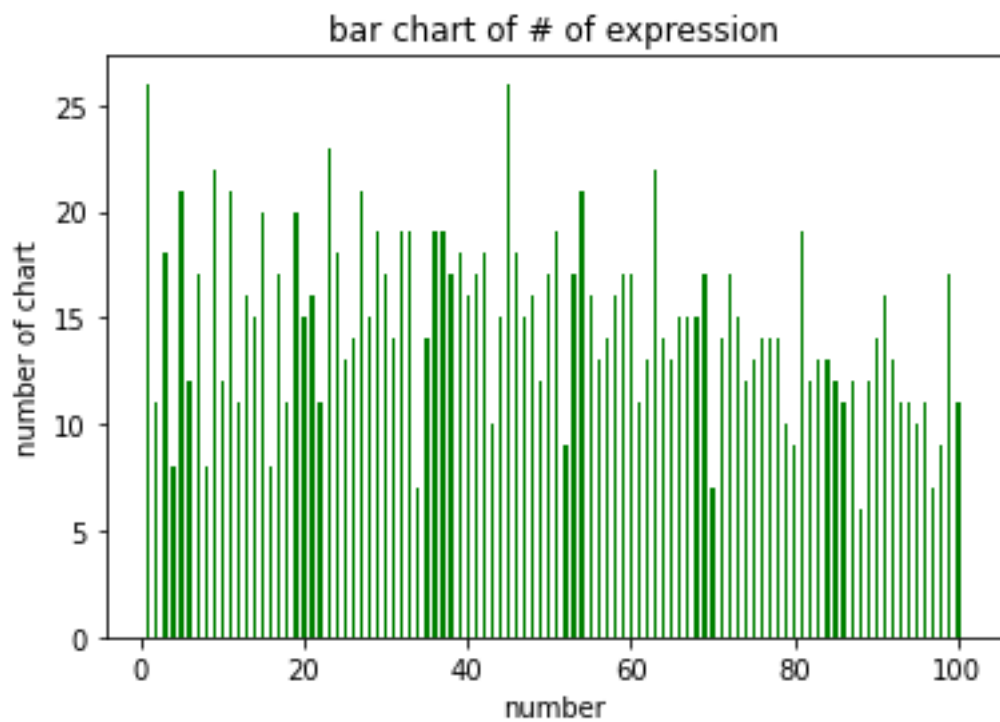
I referred: [https://m.jingyanlib.com/resultpage?id=CsFJGPp1X\\_PdaFvnJN-oLg](https://m.jingyanlib.com/resultpage?id=CsFJGPp1X_PdaFvnJN-oLg) to use "for index, value in enumerate(res)" to ergodic and match result.

From this process, I learned a lot and realized the power and wisdom of python and programmer behind it. More importantly, I started thinking a question by a process of from building concept model to creating math model: figure out problem logically by logically, module by module.

Last is the figure and results:

```
Find_expression(50)
1+2+3+4-56+7+89=50
1+2+3-4+56-7+8-9=50
1+2+34-5-6+7+8+9=50
1+2+34-56+78-9=50
1+2-3+4+56+7-8-9=50
1+2-34+5-6-7+89=50
1-2+3-45+6+78+9=50
1-2+34+5+6+7+8-9=50
1-2+34-5-67+89=50
1-2-3+4+56-7-8+9=50
1-2-3-4-5-6+78-9=50
1-2-34-5-6+7+89=50
1-23+4+5-6+78-9=50
1-23-4-5-6+78+9=50
12+3+4-56+78+9=50
12-3+45+6+7-8-9=50
12-3-4-5+67-8-9=50
Out[137]: 17
```

Figure:



```
Max = max(Total_solutions)
```

```
for index, value in enumerate(Total_solutions):
```

```
    if (value == Max):
```

```
        print(index+1)
```

```
1
```

```
45
```

```
Max
```

```
Out[156]: 26
```

The 1 and 45 have maximal number of expressions.