```
function [J, grad] = linearRegCostFunction(X, y, theta, lambda)
    %LINEARREGCOSTFUNCTION Compute cost and gradient for regularized
linear
    %regression with multiple variables
    % [J, grad] = LINEARREGCOSTFUNCTION(X, y, theta, lambda) computes
the
    % cost of using theta as the parameter for linear regression to fit the
    % data points in X and y. Returns the cost in J and the gradient in grad
    % Initialize some useful values
    m = length(y); % number of training examples
    % You need to return the following variables correctly
    J = 0;
    grad = zeros(size(theta));
    % ======= YOUR CODE HERE ===
    % Instructions: Compute the cost and gradient of regularized linear
              regression for a particular choice of theta.
    %
    %
    %
              You should set J to the cost and grad to the gradient.
    %
    H = X*theta;
    J = sum((H - y).^2) / (2 * m) + lambda*sum(theta(2:end).^2) / (2 * m);
    grad = X'*(H - y) / m + lambda*[0;theta(2:end)] / m;
    grad = grad(:);
    end
function [error_train, error_val] = ...
      learningCurve(X, y, Xval, yval, lambda)
    %LEARNINGCURVE Generates the train and cross validation set errors
needed
    %to plot a learning curve
    % [error_train, error_val] = ...
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%
      LEARNINGCURVE(X, y, Xval, yval, lambda) returns the train and
%
      cross validation set errors for a learning curve. In particular,
     it returns two vectors of the same length - error_train and
%
%
      error_val. Then, error_train(i) contains the training error for
     i examples (and similarly for error_val(i)).
%
%
% In this function, you will compute the train and test errors for
% dataset sizes from 1 up to m. In practice, when working with larger
% datasets, you might want to do this in larger intervals.
%
% Number of training examples
m = size(X, 1);
% You need to return these values correctly
error_train = zeros(m, 1);
error_val = zeros(m, 1);
% ======= YOUR CODE HERE ===
% Instructions: Fill in this function to return training errors in
%
          error_train and the cross validation errors in error_val.
%
          The vector numex_vec contains the number of training
          examples to use for each calculation of training error and
%
%
          cross validation error, i.e, error_train(i) and
          error_val(i) should give you the errors
%
%
          obtained after training on i examples.
%
% Note: You should evaluate the training error on the first i training
      examples (i.e., X(1:i, :) and y(1:i)).
%
%
%
      For the cross-validation error, you should instead evaluate on
%
      the _entire_ cross validation set (Xval and yval).
%
% Note: If you are using your cost function (linearRegCostFunction)
      to compute the training and cross validation error, you should
%
      call the function with the lambda argument set to 0.
%
%
      Do note that you will still need to use lambda when running
%
      the training to obtain the theta parameters.
%
% Hint: You can loop over the examples with the following:
%
%
     for i = 1:m
%
        % Compute train/cross validation errors using training examples
%
        % X(1:i, :) and y(1:i), storing the result in
        % error_train(i) and error_val(i)
%
%
```

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%
    %
         end
    % ------ Sample Solution ------
    val_size = size(Xval,1);
    for i = 1 : m,
        [theta] = trainLinearReg([ones(i, 1) X(1:i, :)], y(1:i), lambda);
        [error_train(i), grad] = linearRegCostFunction([ones(i, 1) X(1:i, :)],
y(1:i), theta, 0);
        [error_val(i), grad] = linearRegCostFunction([ones(val_size , 1) Xval],
yval, theta, 0);
    end
    % ------
    end
function [X_poly] = polyFeatures(X, p)
    %POLYFEATURES Maps X (1D vector) into the p-th power
    % [X_poly] = POLYFEATURES(X, p) takes a data matrix X (size m x 1) and
    % maps each example into its polynomial features where
    % X_{poly}(i, :) = [X(i) X(i).^2 X(i).^3 ... X(i).^p];
    %
    % You need to return the following variables correctly.
    X_{poly} = zeros(numel(X), p);
    % ======= YOUR CODE HERE ===
    % Instructions: Given a vector X, return a matrix X_poly where the p-th
             column of X contains the values of X to the p-th power.
    %
    %
    %
    for i = 1 : p,
        X_{poly}(:,i) = X^i;
    function [lambda_vec, error_train, error_val] = ...
      validationCurve(X, y, Xval, yval)
    %VALIDATIONCURVE Generate the train and validation errors needed to
    %plot a validation curve that we can use to select lambda
    % [lambda_vec, error_train, error_val] = ...
         VALIDATIONCURVE(X, y, Xval, yval) returns the train
         and validation errors (in error_train, error_val)
    %
         for different values of lambda. You are given the training set (X,
         y) and validation set (Xval, yval).
    %
```

```
%
% Selected values of lambda (you should not change this)
lambda_vec = [0 0.001 0.003 0.01 0.03 0.1 0.3 1 3 10]';
% You need to return these variables correctly.
error_train = zeros(length(lambda_vec), 1);
error_val = zeros(length(lambda_vec), 1);
% ======== YOUR CODE HERE ===
% Instructions: Fill in this function to return training errors in
%
          error_train and the validation errors in error_val. The
%
          vector lambda_vec contains the different lambda parameters
          to use for each calculation of the errors, i.e,
%
%
          error_train(i), and error_val(i) should give
          you the errors obtained after training with
%
%
          lambda = lambda_vec(i)
%
% Note: You can loop over lambda_vec with the following:
%
     for i = 1:length(lambda_vec)
        lambda = lambda_vec(i);
%
%
        % Compute train / val errors when training linear
        % regression with regularization parameter lambda
%
        % You should store the result in error_train(i)
%
%
        % and error val(i)
%
        ....
%
      end
%
%
for i = 1: length(lambda_vec),
     lambda = lambda_vec(i);
     [theta] = trainLinearReg(X, y, lambda);
     [error_train(i), grad] = linearRegCostFunction(X, y, theta, 0);
     [error_val(i), grad] = linearRegCostFunction(Xval, yval, theta, 0);
end
end
```