

Aufgabe 3

```

1           $\langle x \geq 0 \rangle$ 
2           $\langle x \geq 0 \wedge -x = -x \wedge x = x \rangle$ 
3  res = -x;
4           $\langle x \geq 0 \wedge \text{res} = -x \wedge x = x \rangle$ 
5  c = x;
6           $\langle x \geq 0 \wedge \text{res} = -x \wedge c = x \rangle$ 
7           $\langle \text{res} = x \cdot x - 2 \cdot \sum_{k=0}^c k \wedge c \geq 0 \rangle$ 
8  while (c > 0)
9           $\langle \text{res} = x \cdot x - 2 \cdot \sum_{k=0}^c k \wedge c \geq 0 \wedge c > 0 \rangle$ 
10          $\langle \text{res} + 2 \cdot (c - 1) = x \cdot x - 2 \cdot \sum_{k=0}^{(c-1)} k \wedge (c - 1) \geq 0 \rangle$ 
11         res = res + 2 * c;
12          $\langle \text{res} = x \cdot x - 2 \cdot \sum_{k=0}^{(c-1)} k \wedge (c - 1) \geq 0 \rangle$ 
13         c = c - 1;
14          $\langle \text{res} = x \cdot x - 2 \cdot \sum_{k=0}^c k \wedge c \geq 0 \rangle$ 
15     }
16      $\langle \text{res} = x \cdot x - 2 \cdot \sum_{k=0}^c k \wedge c \geq 0 \wedge \neg(c > 0) \rangle$ 
17      $\langle \text{res} = x \cdot x \rangle$ 
18
```

Aufgabe 5

a)

```

1           $\langle q \geq 1 \rangle$ 
2           $\langle q \geq 1 \wedge q = q \wedge x = p \wedge y = 1 \rangle$ 
3  n = q;
4           $\langle q \geq 1 \wedge n = q \wedge p = p \wedge y = 1 \rangle$ 
5  x = p;
6           $\langle q \geq 1 \wedge n = q \wedge x = p \wedge 1 = 1 \rangle$ 
7  y = 1;
8           $\langle q \geq 1 \wedge n = q \wedge x = p \wedge y = 1 \rangle$ 
9           $\langle p^q = x^n \cdot y \wedge n \geq 1 \rangle$ 
10 while (n > 1) {
11      $\langle p^q = x^n \cdot y \wedge n \geq 1 \wedge n > 1 \rangle$ 
12     if (n % 2 == 0) {
13          $\langle p^q = x^n \cdot y \wedge n \geq 1 \wedge n > 1 \wedge n \bmod 2 = 0 \rangle$ 
14          $\langle p^q = (x \cdot x)^{\lfloor \frac{n}{2} \rfloor} \cdot y \wedge \lfloor \frac{n}{2} \rfloor \geq 1 \rangle$ 
15         x = x * x;
16          $\langle p^q = x^{\lfloor \frac{n}{2} \rfloor} \cdot y \wedge \lfloor \frac{n}{2} \rfloor \geq 1 \rangle$ 
17         n = n / 2;
18          $\langle p^q = x^n \cdot y \wedge n \geq 1 \rangle$ 
19     } else {
20          $\langle p^q = x^n \cdot y \wedge n \geq 1 \wedge n > 1 \wedge \neg(n \bmod 2 = 0) \rangle$ 
21          $\langle p^q = (x \cdot x)^{\lfloor \frac{n-1}{2} \rfloor} \cdot (x \cdot y) \wedge \lfloor \frac{n-1}{2} \rfloor \geq 1 \rangle$ 
22         y = x * y;
23          $\langle p^q = (x \cdot x)^{\lfloor \frac{n-1}{2} \rfloor} \cdot y \wedge \lfloor \frac{n-1}{2} \rfloor \geq 1 \rangle$ 
24         x = x * x;
25          $\langle p^q = x^{\lfloor \frac{n-1}{2} \rfloor} \cdot y \wedge \lfloor \frac{n-1}{2} \rfloor \geq 1 \rangle$ 
26         n = (n-1) / 2;
27          $\langle p^q = x^n \cdot y \wedge n \geq 1 \rangle$ 
28     }
29      $\langle p^q = x^n \cdot y \wedge n \geq 1 \rangle$ 
30 }
31      $\langle p^q = x^n \cdot y \wedge n \geq 1 \wedge \neg(n > 1) \rangle$ 
32      $\langle p^q = x \cdot y \rangle$ 
33     x = x * y;
34      $\langle p^q = x \rangle$ 
35
```

b)

$V = n$, denn: $n > 1 \implies n \geq 0$

```
1           $\langle n = m \wedge n > 1 \rangle$ 
2           $\langle n < m \rangle$ 
3  if (n % 2 == 0) {
4           $\langle n < m \wedge n > 1 \wedge n \bmod 2 = 0 \rangle$ 
5           $\langle \lfloor \frac{n}{2} \rfloor < m \rangle$ 
6          x = x * x;
7           $\langle \lfloor \frac{n}{2} \rfloor < m \rangle$ 
8          n = n / 2;
9           $\langle n < m \rangle$ 
10 } else {
11           $\langle n < m \wedge n > 1 \wedge \neg(n \bmod 2 = 0) \rangle$ 
12          y = x * y;
13           $\langle \lfloor \frac{n-1}{2} \rfloor < m \rangle$ 
14          x = x * x;
15           $\langle \lfloor \frac{n-1}{2} \rfloor < m \rangle$ 
16          n = (n-1) / 2;
17           $\langle n < m \rangle$ 
18 }
19           $\langle n < m \rangle$ 
20
```

Aufgabe 7

```
1 public class BubbleSort {
2     public static void sort(int[] a) {
3         int tmp;
4         for (int i = a.length - 1; i > 0; i--){
5             for (int j = 0; j < i; j++){
6                 if (a[j] > a[j+1]){
7                     tmp = a[j+1];
8                     a[j+1] = a[j];
9                     a[j] = tmp;
10                }
11            }
12        }
13    }
14 }
15
```

Aufgabe 9

a)

```
1           $\langle \text{true} \rangle$ 
2           $\langle \text{true} \wedge 0 = 0 \wedge \text{false} = \text{false} \rangle$ 
3  i = 1;
4           $\langle \text{true} \wedge i = 0 \wedge \text{false} = \text{false} \rangle$ 
5  res = false;
6           $\langle \text{true} \wedge i = 0 \wedge \text{res} = \text{false} \rangle$ 
7           $\langle \text{res} = x \in \{a[j] \mid 0 \leq j < i\} \wedge i \leq a.length \rangle$ 
8  while (i < a.length){
9           $\langle \text{res} = x \in \{a[j] \mid 0 \leq j < i\} \wedge i \leq a.length \wedge i < a.length \rangle$ 
10     if (x == a[i]){
11          $\langle \text{res} = x \in \{a[j] \mid 0 \leq j < i\} \wedge i \leq a.length \wedge i < a.length \wedge x = a[i] \rangle$ 
12          $\langle \text{true} = x \in \{a[j] \mid 0 \leq j < i+1\} \wedge i+1 \leq a.length \rangle$ 
13         res = true;
14          $\langle \text{res} = x \in \{a[j] \mid 0 \leq j < i+1\} \wedge i+1 \leq a.length \rangle$ 
15     }
16      $\langle \text{res} = x \in \{a[j] \mid 0 \leq j < i+1\} \wedge i+1 \leq a.length \rangle$ 
```

```
17     i = i + 1;
18         <res = x ∈ {a[j] | 0 ≤ j < i} ∧ i ≤ a.length>
19     }
20         <res = x ∈ {a[j] | 0 ≤ j < i} ∧ i ≤ a.length ∧ ¬(i < a.length)>
21         <res = x ∈ {a[j] | 0 ≤ j < a.length - 1}>
22
```

b)

$V = a.length - i$, denn: $i < a.length \implies a.length - i \geq 0$

```
1         <a.length - i = m ∧ i < a.length>
2         <a.length - (i + 1) < m>
3     if (x == a[i]){
4         <a.length - (i + 1) < m ∧ x = a[i]>
5         <a.length - (i + 1) < m>
6         res = true;
7         <a.length - (i + 1) < m>
8     }
9         <a.length - (i + 1) < m>
10    i = i + 1;
11        <a.length - i < m>
12
```