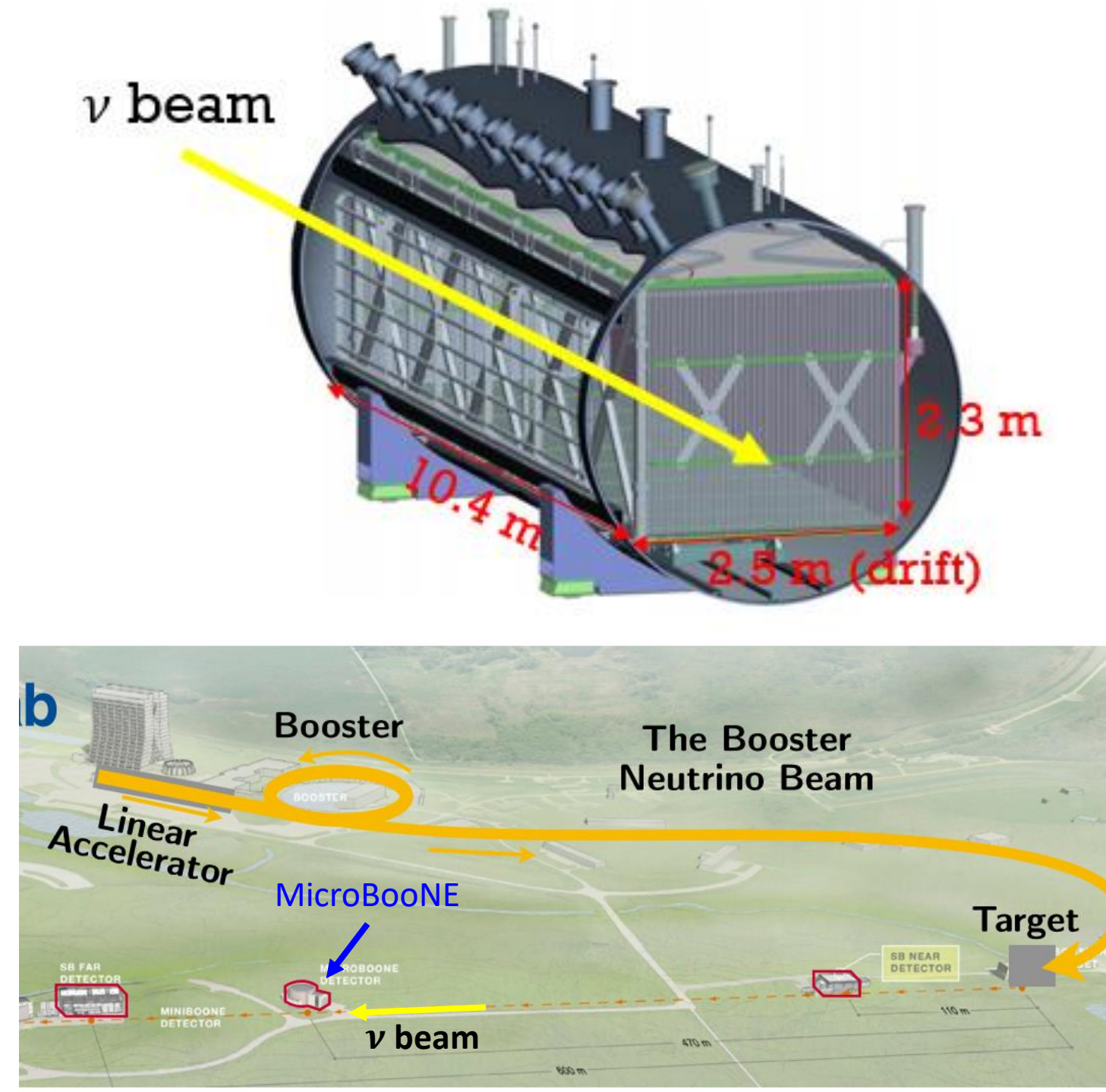


# Extraction of the Inclusive $\nu_\mu$ CC Cross-Section

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## 1. MicroBooNE

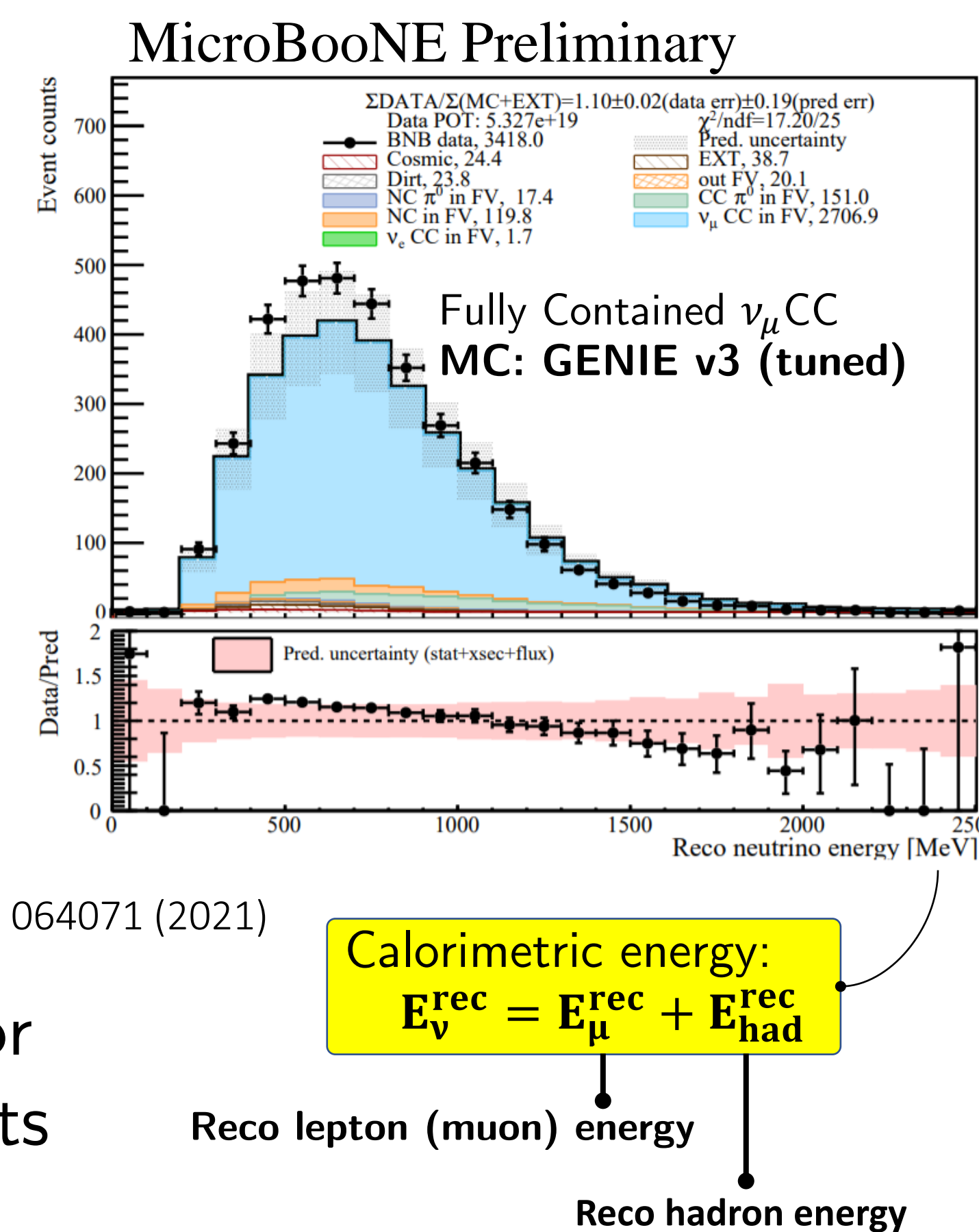


- Accelerator  $\nu$  experiment at Fermilab
  - LArTPC with 85-ton active mass
  - Near-surface operation
- Main physics goals
  - Investigate MiniBooNE low-energy excess
  - Measure  $\nu$ -Ar interaction cross sections

## 2. $\nu_\mu$ CC inclusive selection

	Efficiency	Purity	Cosmic- $\mu$ rejection
Trigger	1	5e-5	1
Generic- $\nu$ detection	80%	65%	7e-6
<b><math>\nu_\mu</math> CC (Fully &amp; Partially Contained)</b>	<b>64%</b>	<b>93%</b>	<b>7e-7</b>

- Achieved excellent cosmic- $\mu$  rejection
  - Wire-Cell reconstruction: JINST 16 (2021) 06, P06043
  - Generic- $\nu$  detection: arXiv:2012.07928; Phys. Rev. Applied 15, 064071 (2021)
- **High-statistics** event selection allows for high-precision cross-section measurements
  - MICROBOONE-NOTE-1095-PUB



## 5. Towards a cross-section extraction

$$M(E_{rec}) = \underbrace{POT}_{\text{Proton-on-target}} \cdot \underbrace{T}_{\text{Neutrino flux}} \cdot \int \underbrace{F(E_\nu)}_{\text{Cross section}} \cdot \underbrace{\sigma(E_\nu)}_{\text{Selection efficiency}} \cdot \underbrace{D(E_\nu, E_{rec})}_{\text{Background}} \cdot dE_\nu + B(E_{rec})$$

- Extract the cross section  $\sigma_{CC}(E_\nu)$  with data unfolding technique
- More dimensions are allowed:  $d\sigma_{CC}/dE_\mu$ ,  $d\sigma_{CC}/d\nu$ ,  $d\sigma_{CC}/dE_\mu d\theta_\mu$

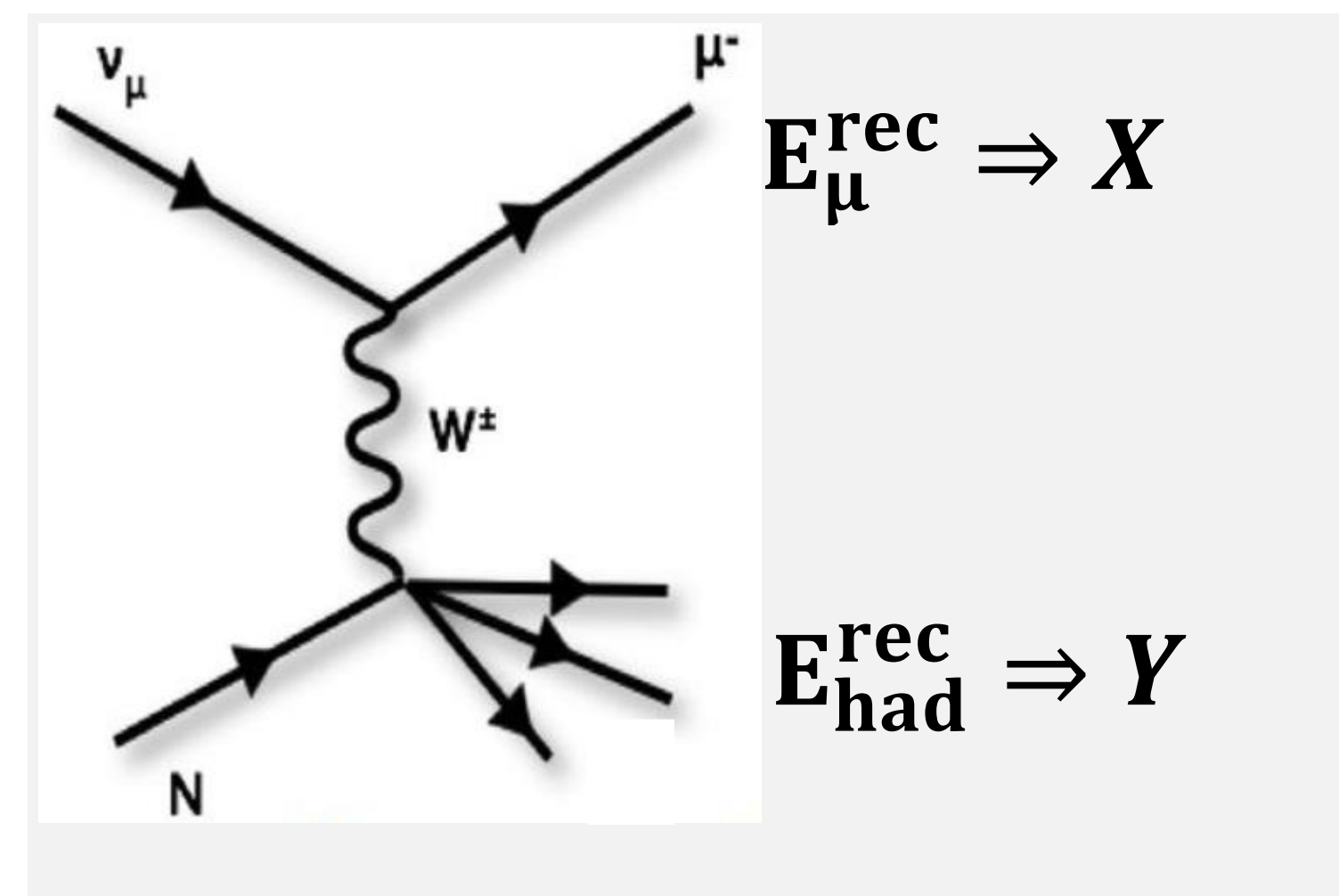
## 3. Model validation: $E_\nu$ to $E_\nu^{rec}$

- **Neutrino energy modeling is crucial for neutrino oscillation measurements**
  - Key challenge: understanding  $\nu$ -Ar cross section as a function of energy

- **A new procedure for validating  $E_\nu^{rec}$  from model prediction/simulation:**

$$E_\nu^{rec} = E_\mu^{rec} + E_{had}^{rec}$$

- Simulated muon kinematics ( $E_\mu^{rec}$ ,  $\cos\theta_\mu^{rec}$ ) are compared with data first
- Hadronic energy ( $E_{had}^{rec}$ ) is further validated given the **constrained** model prediction: constrain muon kinematics to that of data



### Formalism of conditional constraint

$$\mu_{X,Y} = \begin{pmatrix} \mu_X \\ \mu_Y \end{pmatrix}, \quad \Sigma_{X,Y} = \begin{pmatrix} \Sigma_{XX} & \Sigma_{XY} \\ \Sigma_{YX} & \Sigma_{YY} \end{pmatrix}$$

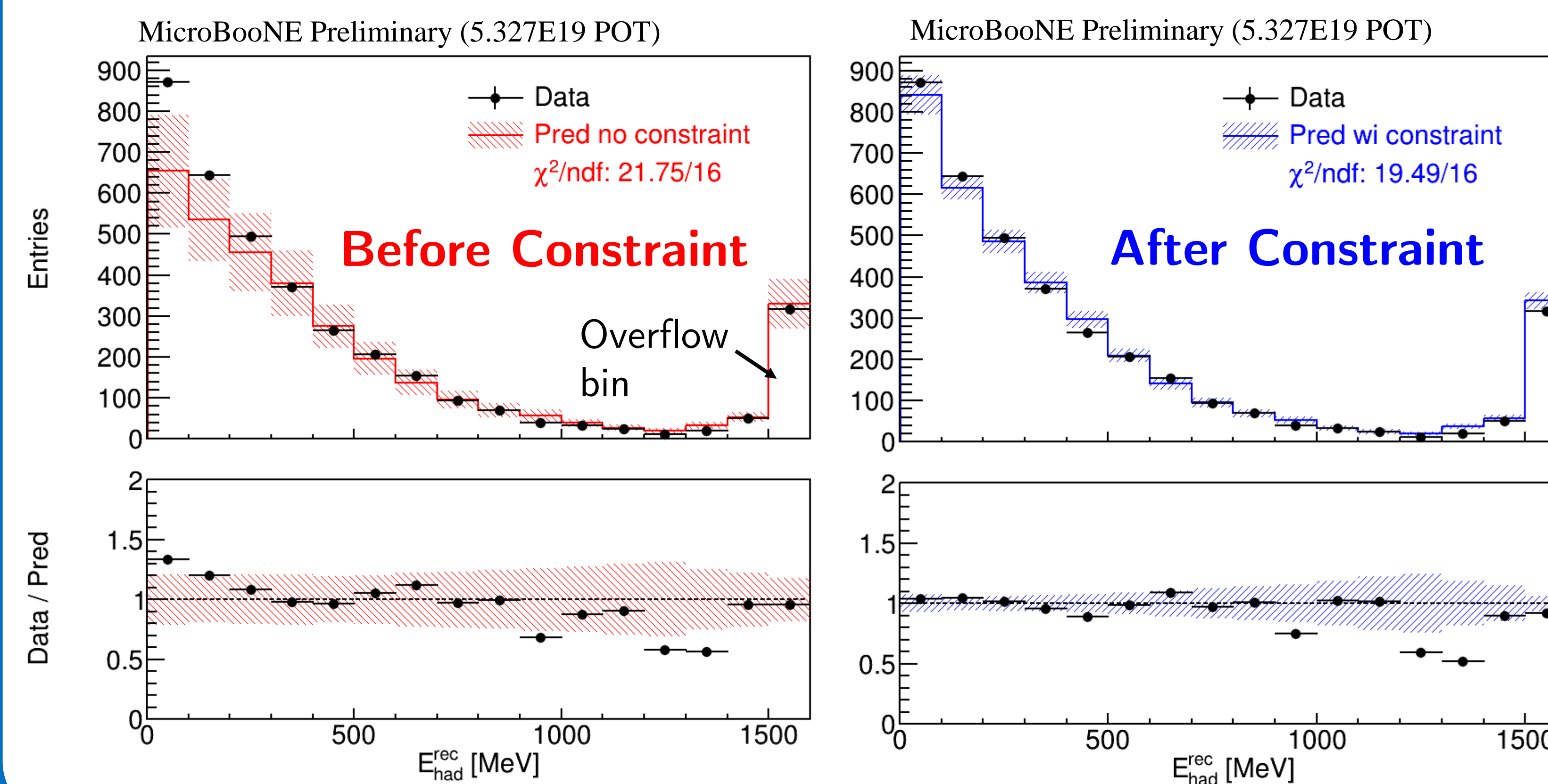
Joint mean                      Joint covariance

$$\mu_{Y|X}^{constrained} = \mu_Y + \Sigma_{YX}\Sigma_{XX}^{-1}(X - \mu_X)$$

$$\Sigma_{Y|X}^{constrained} = \Sigma_{YY} - \Sigma_{YX}\Sigma_{XX}^{-1}\Sigma_{XY}$$

- A data-driven correction for the model prediction of Y given a measurement of X
- **Common systematic uncertainties (e.g., flux) are reduced**  
⇒ **more stringent model validation**

## 4. Validation of hadron energy reconstruction



- **After constraint with  $E_\mu^{rec}$  and  $\cos\theta_\mu^{rec}$ : no more excess at low hadronic energy**
  - Significant reduction in overall uncertainties (20% → 5%)
  - No sign of mis-modeling of the hadron missing energy

MC folding vs. data unfolding (a re-smearing process to extract truth model)

$$M_i = \sum_j R_{ij} S_j \iff \hat{S} = A_C \cdot R^{-1} \cdot M$$

M: measured event distribution  
S: binned true distribution  
 $R_{ij}$ : response matrix (reco bin i and true bin j)  
 $A_C$ : regularization, also applied to models when comparing result to theoretic predictions