**Numerical Simulation of Velocity-stress Equation in 3D Based on Staggered-Grid Finite Difference**



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**年 级 2018级博士研究生**

**Abstract**：

Staggered-grid finite difference has double precision while keeping computational and memory constant. In this paper, the staggered-grid finite difference is used to discretize the elastic wave equation. Then CPU and GPU are used to realize the numerical simulation of the elastic wave equation, and we compare the accuracy of CPU and GPU. Due to the large number of variables of speed and stress, the 3D implementation will consume a lot of memory. Therefore, it is necessary to implement the PML absorption boundary by optimizing the memory. By establishing a random medium model, we apply this velocity model to the elastic wave forward modeling.

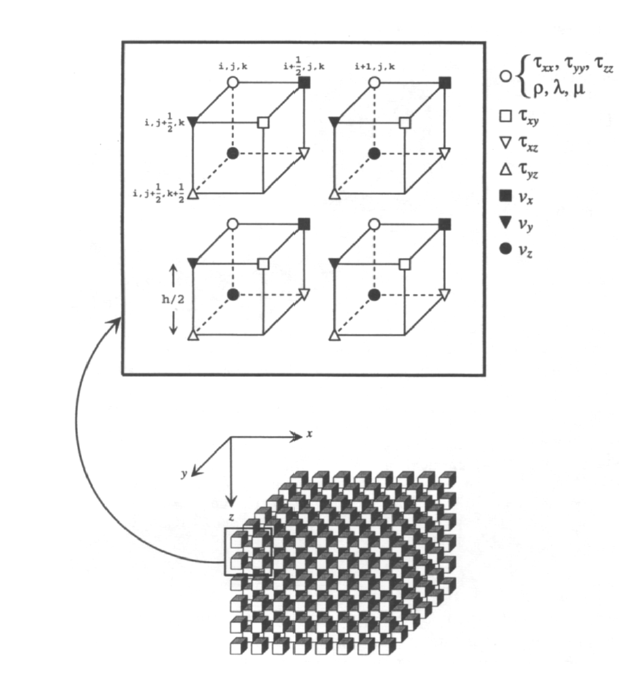
**Keywords：**Velocity-stress Equation, 3D, Staggered-Grid, Finite Difference, GPU

**Algorithm implementation：**

1. Velocity-stress Equation:

(1)

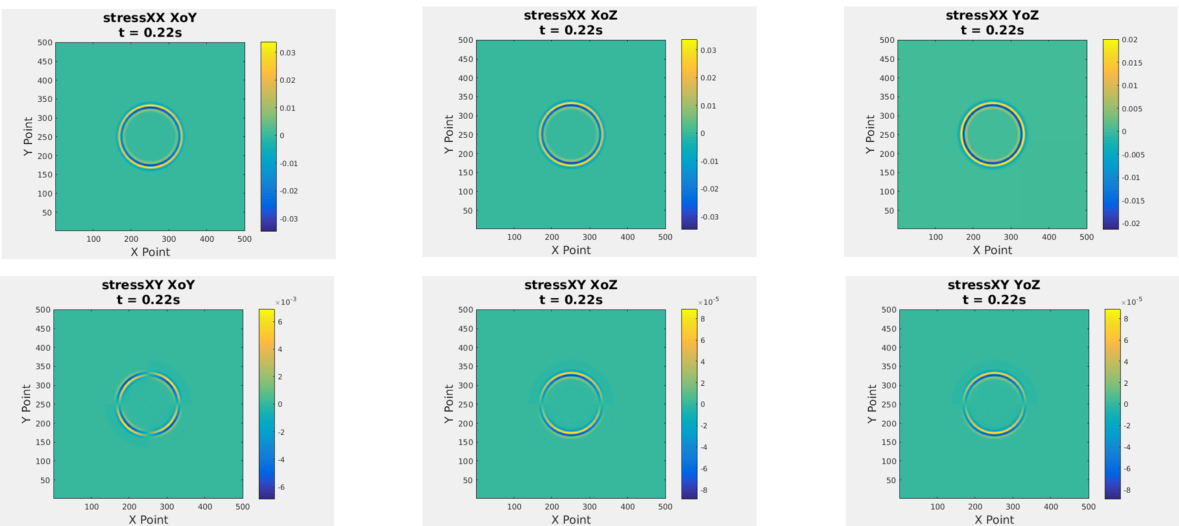
(2)

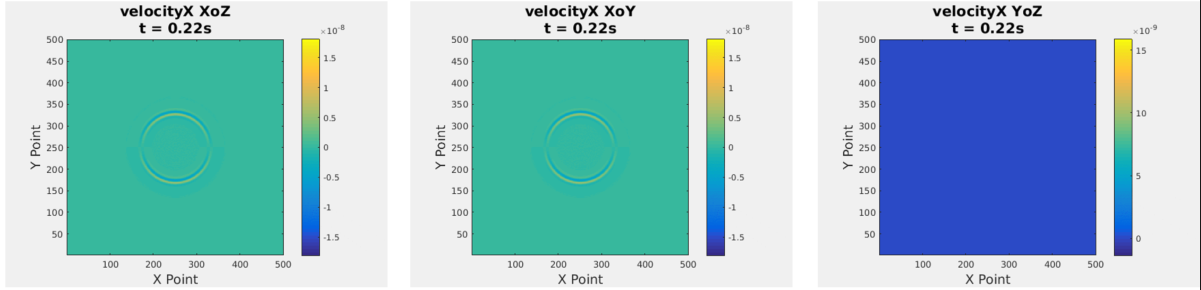


1. Staggered-Grid Finite Difference:

As is shown in the picture, all variables are distributed on the grid points. Then we can obtain the following finite difference equation from the above equation.

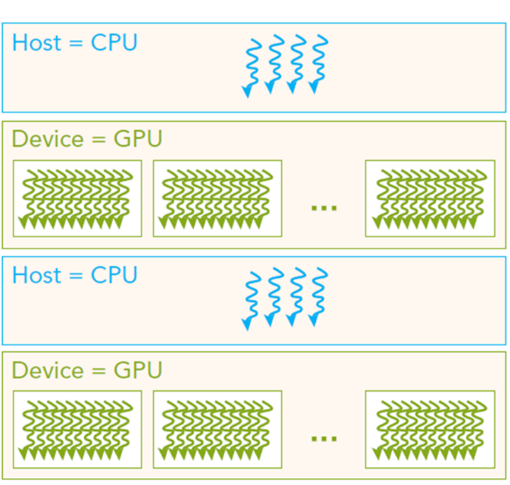
Firstly, we use C++ codes to implement the staggered-grid finite difference equation, and we get the snapshot in the following pictures.

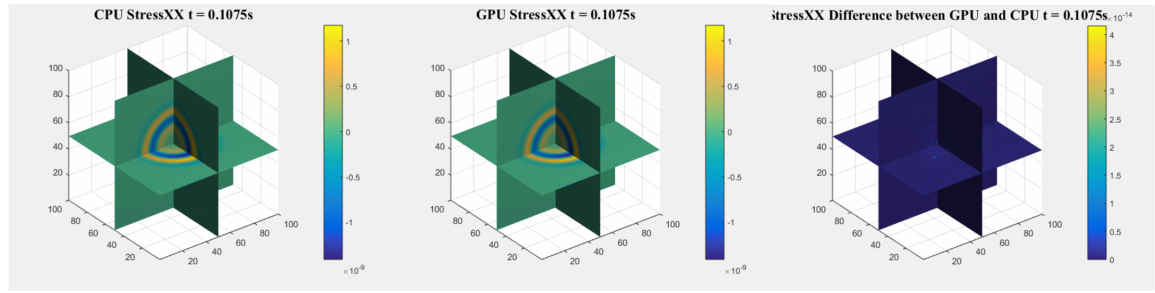




1. Implement of CPU and GPU

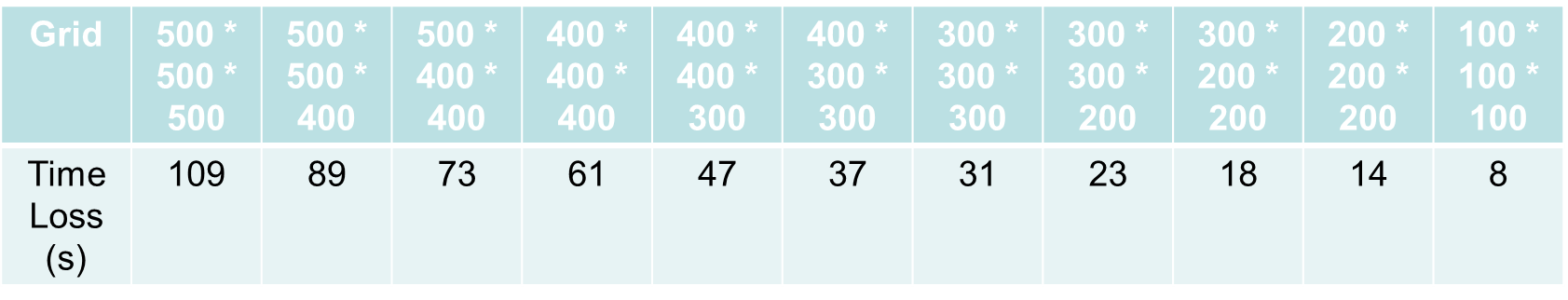
CUDA is a set of parallel programming framework provided by NVIDIA. We can transfer the CPU data to the GPU, accelerate it in parallel in the GPU, and then retransmit the data back to CPU. CUDA C is a C-like language. NVIDIA has already mapped it to hardware. We don't need to think too much about hardware details when programming. More attention is paid to the algorithm logic of parallel programs.





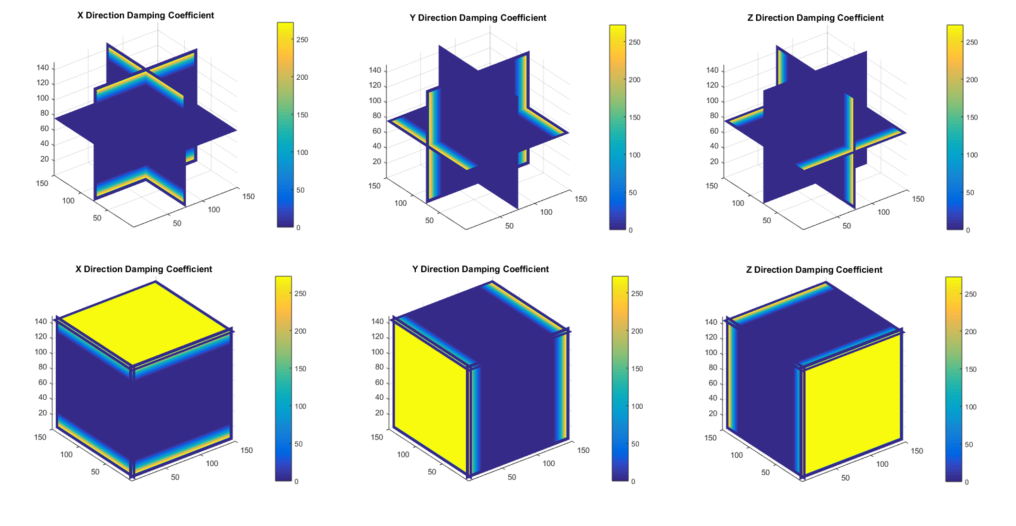
As is shown in the above picture, the difference between GPU and CPU is small enough to omit.

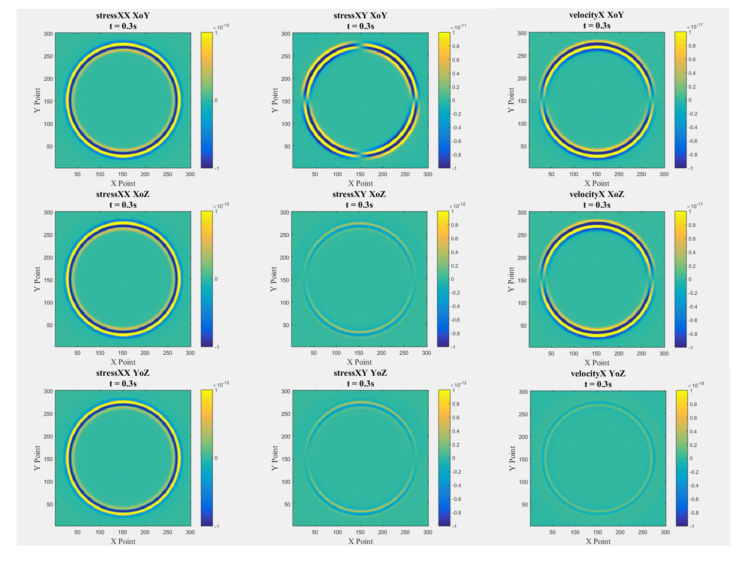
When we calculate a grid model 500\*500\*500, the time loss is about 7 hours on the CPU and about 100 seconds on the GPU. As the time loss on CPU is very big, we didn’t calculate so many models. We calculate several modes on GPU, and the time loss is in the following table.

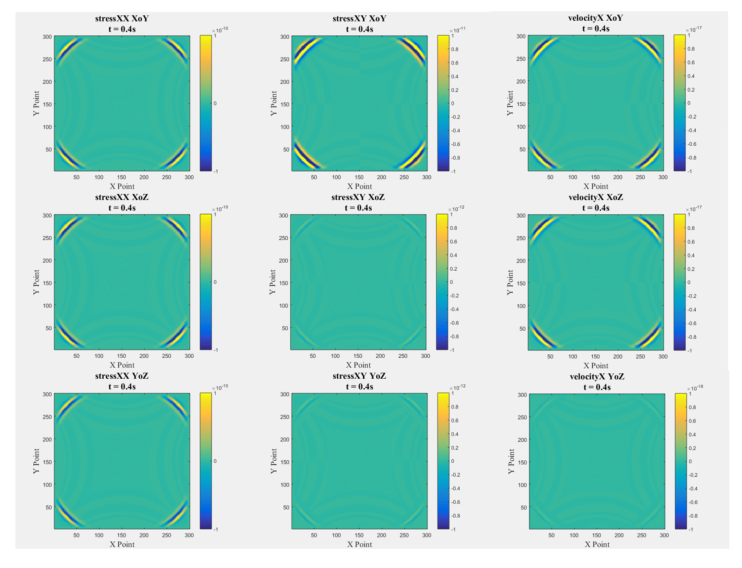


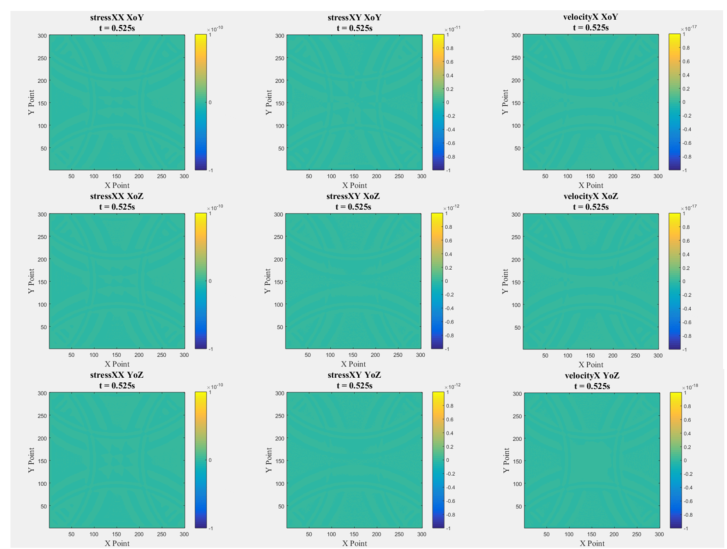
It’s obvious that the GPU performs much well than CPU.

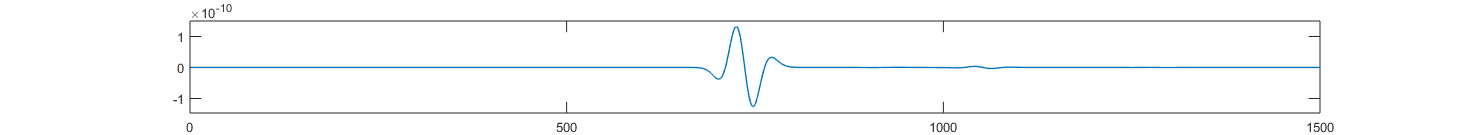
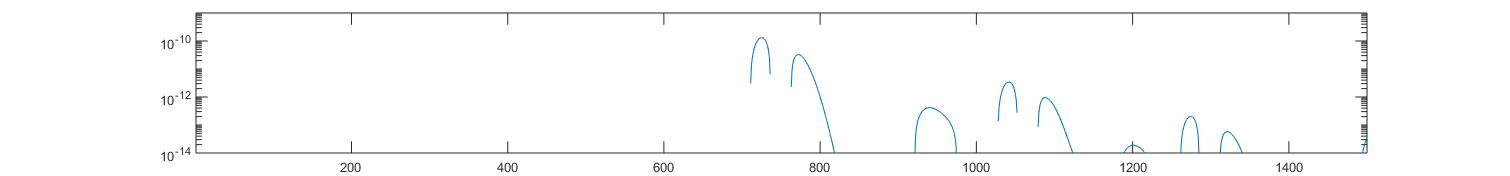
1. PML



If we do not add artificial absorption boundaries, we will generate pseudo-reflected waves.







1. Random Medium

We establish a velocity model based on random medium theory. Then, we use the velocity model for numerical simulation of elastic equations. The algorithm flow chart is show below:

Autocorrelation Function

Power Spectral Function

Generate Random Sequence

Power Spectral Function

Suppress

Random Error

Random Disturbance

Mean and

Variance

Autocorrelation Function

Normalization

Random Medium

Disturbance

Background Model Parameters

Random Medium Model

FFT

IFFT

