Problem set 7

2024-11-04

For this problem set we want you to predict the election. You will enter you predictions to this form. You you will report a prediction of the number of electoral votes for Harris and an interval. You will do the same for the popular vote. We will give prizes for those that report the shortest interval but with the true result inside the interval.

1. Read in the data provided here:

```
url <- "https://projects.fivethirtyeight.com/polls/data/president_polls.csv"</pre>
```

Examine the data frame paying particular attention to the poll_id question_id, population, and candidate. Note that some polls have more than one question based on different population types.

```
library(tidyverse)
```

```
-- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
            1.1.4
v dplyr
                       v readr
                                    2.1.5
v forcats
            1.0.0
                       v stringr
                                    1.5.1
v ggplot2
            3.5.1
                       v tibble
                                    3.2.1
v lubridate 1.9.3
                       v tidyr
                                    1.3.1
v purrr
            1.0.2
-- Conflicts -----
                                               ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag()
                   masks stats::lag()
i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become
```

library(rvest)

```
Attaching package: 'rvest'
The following object is masked from 'package:readr':
    guess_encoding
raw dat <- read csv(url)
Rows: 18095 Columns: 52
-- Column specification -----
Delimiter: ","
chr (25): pollster, sponsors, display name, pollster_rating_name, methodolog...
dbl (16): poll_id, pollster_id, pollster_rating_id, numeric_grade, pollscore...
num (1): sponsor ids
lgl (10): endorsed_candidate_id, endorsed_candidate_name, endorsed_candidate...
i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
raw_dat|>select('poll_id', 'question_id', 'candidate_name', 'population')
# A tibble: 18,095 x 4
   poll_id question_id candidate_name population
     <dbl>
                 <dbl> <chr>
                                       <chr>>
     89372
                216453 Kamala Harris
 1
                                      lv
 2
     89372
                216453 Donald Trump
                                       lv
 3
     89372
                216453 Jill Stein
                                       lv
                216453 Cornel West
 4
     89372
 5
     89372
                216453 Chase Oliver
                                      lv
 6
                216454 Kamala Harris lv
     89372
 7
     89372
                216454 Donald Trump
                                      lv
 8
     89373
                216464 Kamala Harris lv
 9
     89373
                216464 Donald Trump
                                       lv
10
     89373
                216464 Jill Stein
                                       lv
# i 18,085 more rows
```

2. Polls are based on either likely voters (lv), registered voters (rv), all voters (a), or voters (v). Polls based on 'voters' are exit polls. We want to remove these because exit polls are too old or might be biased due to differences in the likelihood of early voter by party. We prefer likely voter (lv) polls because they are more predictive. Registered voter polls

are more predictive than all voter (a) polls. Remove the exit poll (v) polls and then redefine population to be a factor ordered from best to worse predictive power: (lv, rv, a). You should also remove hypothetical polls and make the date columns into date objects. Name the resulting data frame dat.

```
# A tibble: 5,611 x 52
  poll_id pollster_id pollster
                                   sponsor_ids sponsors display_name
                                         <dbl> <chr>
     <dbl>
                 <dbl> <chr>
                                                         <chr>
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
 1
 2
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
3
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
4
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
5
                                            NA <NA>
     89372
                  1528 AtlasIntel
                                                         AtlasIntel
 6
                  1528 AtlasIntel
                                            NA <NA>
     89372
                                                         AtlasIntel
7
                  1528 AtlasIntel
                                            NA <NA>
     89372
                                                         AtlasIntel
8
     89373
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
9
     89373
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
10
     89373
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
# i 5,601 more rows
# i 46 more variables: pollster_rating_id <dbl>, pollster_rating_name <chr>,
    numeric_grade <dbl>, pollscore <dbl>, methodology <chr>,
    transparency score <dbl>, state <chr>, start_date <date>, end_date <date>,
    sponsor_candidate_id <dbl>, sponsor_candidate <chr>,
    sponsor_candidate_party <chr>, endorsed_candidate_id <lgl>,
    endorsed_candidate_name <lgl>, endorsed_candidate_party <lgl>, ...
```

3. Some polls asked more than one questions. So if you filter to one poll ID in our dataset, you might see more than one question ID associated with the same poll. The most common reason for this is that they asked a head-to-head question (Harris versus Trump) and, in the same poll, a question about all candidates. We want to prioritize the head-to-head questions.

Add a column that tells us, for each question, how many candidates where mentioned in that question.

Add a new column **n** to **dat** that provides the number of candidates mentioned for each question. For example the relevant column of your final table will looks something like this:

poll_id	question_id	candidate	n
1	1	Harris	2
1	1	Trump	2
1	2	Harris	3
1	2	Trump	3
1	2	Stein	3

```
dat <- dat |>
  group_by(question_id) |>
  mutate(n=n()) |>
  ungroup()
dat
```

```
# A tibble: 5,611 x 53
   poll_id pollster_id pollster
                                   sponsor_ids sponsors display_name
     <dbl>
                 <dbl> <chr>
                                         <dbl> <chr>
                                                         <chr>
     89372
                  1528 AtlasIntel
                                            NA <NA>
 1
                                                         AtlasIntel
2
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
 3
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
 4
                                            NA <NA>
     89372
                  1528 AtlasIntel
                                                         AtlasIntel
 5
                                            NA <NA>
     89372
                  1528 AtlasIntel
                                                         AtlasIntel
6
     89372
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
7
                  1528 AtlasIntel
     89372
                                            NA <NA>
                                                         AtlasIntel
8
     89373
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
9
     89373
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
10
     89373
                  1528 AtlasIntel
                                            NA <NA>
                                                         AtlasIntel
# i 5,601 more rows
# i 47 more variables: pollster_rating_id <dbl>, pollster_rating_name <chr>,
    numeric grade <dbl>, pollscore <dbl>, methodology <chr>,
    transparency_score <dbl>, state <chr>, start_date <date>, end_date <date>,
#
    sponsor_candidate_id <dbl>, sponsor_candidate <chr>,
#
    sponsor_candidate_party <chr>, endorsed_candidate_id <lgl>,
    endorsed_candidate_name <lgl>, endorsed_candidate_party <lgl>, ...
```

4. We are going to focus on the Harris versus Trump comparison. Redefine dat to only include the rows providing information for Harris and Trump. Then pivot the dataset so that the percentages for Harris and Trump are in their own columns. Note that for pivot to work you will have to remove some columns. To avoid this keep only the columns you are pivoting and along with poll_id, question_id, state, pollster, start_date, end_date, numeric_grade, sample_size. Once you accomplish the pivot, add a column called spread with the difference between Harris and Trump.

Note that the values stored in **spread** are estimates of the popular vote difference that we will use to predict for the competition:

spread = % of the popular vote for Harris - % of the popular vote for Trump

However, for the calculations in the rest of problem set to be consistent with the sampling model we have been discussing in class, save **spread** as a proportion, not a percentage. But remember to turn it back to a percentage when submitting your entry to the competition.

A tibble: 2,189 x 13

```
poll id question id state
                                            start date end date
                                 pollster
                                                                   numeric grade
     <dbl>
                 <dbl> <chr>
                                 <chr>
                                            <date>
                                                        <date>
                                                                           <dbl>
     89372
 1
                216453 <NA>
                                 AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
2
     89372
                216454 <NA>
                                 AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
 3
     89373
                216464 Arizona AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
4
     89373
                216465 Arizona AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
5
                216466 Georgia AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
     89374
                                                                             2.7
6
     89374
                216467 Georgia AtlasIntel 2024-11-03 2024-11-04
7
                216468 Michigan AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
     89375
8
                216469 Michigan AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
     89375
9
     89378
                216474 Nevada
                                 AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
10
     89378
                216475 Nevada
                                 AtlasIntel 2024-11-03 2024-11-04
                                                                             2.7
```

- # i 2,179 more rows
- # i 6 more variables: sample_size <dbl>, n <int>, population <fct>,
- # Harris <dbl>, Trump <dbl>, spread <dbl>
 - 5. Note that some polls have multiple questions. We want to keep only one question per poll. We will keep likely voter (lv) polls when available, and prefer register voter (rv) over all voter polls (a). If more than one question was asked in one poll, take the most targeted question (smallest n). Save the resulting tabledat. Note that now each after you do this each row will represents exactly one poll/question, so can remove n, poll_id and question_id.

```
dat <- dat |>
  arrange(population, n)|>
  group_by(poll_id)|>
  slice(1)|>
  ungroup()|>
  select(-n,-poll_id,-question_id)
dat
```

```
# A tibble: 1,516 x 10
  state
           pollster
                      start_date end_date
                                             numeric_grade sample_size population
   <chr>
           <chr>>
                                  <date>
                                                                  <dbl> <fct>
                      <date>
                                                     <dbl>
1 <NA>
           McLaughlin 2021-05-12 2021-05-18
                                                       0.5
                                                                   1000 lv
2 <NA>
           Echelon I~ 2021-06-18 2021-06-22
                                                       2.7
                                                                   1001 rv
3 <NA>
           McLaughlin 2021-06-16 2021-06-20
                                                       0.5
                                                                   1000 lv
4 <NA>
           McLaughlin 2021-07-29 2021-08-03
                                                       0.5
                                                                   1000 lv
5 <NA>
           McLaughlin 2021-09-09 2021-09-14
                                                       0.5
                                                                   1000 lv
6 <NA>
           Rasmussen 2021-09-21 2021-09-22
                                                       2.1
                                                                   1000 lv
                                                       1.3
7 Florida Victory I~ 2021-09-16 2021-09-18
                                                                    450 lv
                                                       0.5
8 <NA>
           McLaughlin 2021-10-14 2021-10-18
                                                                   1000 lv
9 <NA>
           Redfield ~ 2021-11-15 2021-11-15
                                                       1.8
                                                                   1500 rv
10 <NA>
           McLaughlin 2021-11-11 2021-11-16
                                                       0.5
                                                                   1000 lv
# i 1,506 more rows
# i 3 more variables: Harris <dbl>, Trump <dbl>, spread <dbl>
```

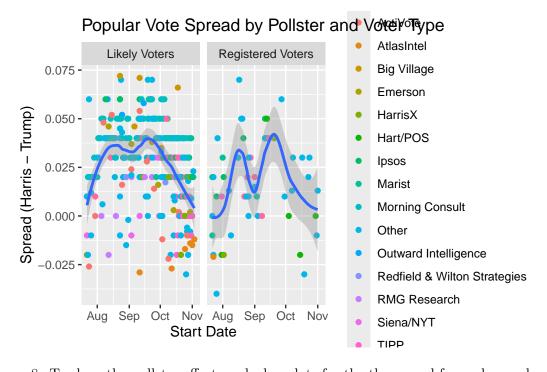
6. Separate dat into two data frames: one with popular vote polls and one with state level polls. Call them popular_vote and polls respectively.

```
popular_vote <- filter(dat, is.na(state))
polls <- filter(dat,!is.na(state))</pre>
```

7. For the popular vote, plot the spread reported by each poll against start date for polls starting after July 21, 2024. Rename all the pollsters with less than 5 polls during this period as Other. Use color to denote pollster. Make separate plots for likely voters and registered voters. Do not use all voter polls (a). Use geom_smooth with method loess to show a curve going through the points. You can change how adaptive the curve is to that through the span argument.

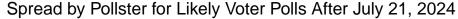
```
popular_vote |>
  filter(start_date > make_date(2024, 7, 21) & population != "a") |>
  group_by(pollster)|>
  mutate(poll_count = n())|>
  ungroup()|>
```

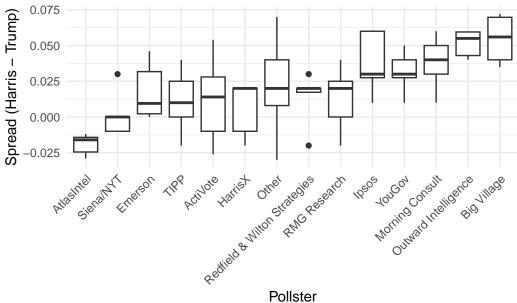
`geom_smooth()` using formula = 'y ~ x'



8. To show the pollster effect, make boxplots for the the spread for each popular vote poll. Include only likely voter polls starting after July 21, 2024. Rename all the pollsters with less than 5 polls during that time period as Other.

```
popular_vote |>
  filter(start_date > make_date(2024, 7, 21) & population == "lv") |>
  group_by(pollster) |>
  mutate(poll_count = n()) |>
  ungroup() |>
```





9. Compute a prediction and an interval for the competition and submit here Include the code you used to create your confidence interval for the popular vote here:

```
tmp <- popular_vote|>
  filter(start_date >= make_date(2024, 10, 04) & population == 'lv' &
          !is.na(numeric_grade))|>
  group_by(pollster)|>
  summarize(spread = mean (spread))|>
  ungroup()|>
  summarize(avg =mean(spread), sd = sd(spread), n= n())

tmp
```

95% Prediction Interval: 0.007237021 0.02294744

I choose October 1, 2024 as the start date as it gives approximately a month of polling data, which should be recent enough to capture the current status. I will keep only likely voter (lv) polls as Likely voter polls focus on respondents who are more likely to actually cast a ballot on Election Day. I also filter NA quality grade (numeric_grade) to make sure that only polls with a defined quality grade are considered. For each pollster, I calculates the average spread across their polls, which helps to reduce bias if a particular pollster conducted multiple polls. Then I calculated the standard deviation of the spread across pollsters and n, the number of pollsters included in the calculation. With this statistics, I calculate the 95% prediction interval for the average spread. The estimated 95% confidence interval for the average spread, ranging from 0.7% to 2.3%

We now move on to predicting the electoral votes.

10. To obtain the number of electoral votes for each state we will visit this website:

```
url <- "https://state.1keydata.com/state-electoral-votes.php"
```

We can use the **rvest** package to download and extract the relevant table:

```
library(rvest)
h <- read_html(url) |>
  html_table()

ev <- h[[4]]</pre>
```

Wrangle the data in ev to only have two columns state and electoral_votes. Make sure the electoral vote column is numeric. Add the electoral votes for Maine CD-1 (1), Maine CD-2 (1), Nebraska CD-2 (1), and District of Columbia (3) by hand.

```
ev <- ev |>
  mutate(state = ev$X2, electoral_votes = ev$X3) |>
  select(state, electoral_votes) |>
  slice(-1) |>
  mutate(electoral_votes = as.numeric(electoral_votes),
    electoral_votes = case_when(
      state == "Maine" ~ electoral_votes - 2,
      state == "Nebraska" ~ electoral_votes - 1,
      TRUE ~ electoral_votes
 ))
new_rows <- data.frame(</pre>
  state = c("Maine CD-1", "Maine CD-2", "Nebraska CD-2", "District of Columbia"),
  electoral_votes = c(1, 1, 1, 3)
ev <- rbind(ev, new_rows)</pre>
# A tibble: 54 x 2
                  electoral_votes
   state
   <chr>
                             <dbl>
 1 California
                                54
 2 Texas
                                40
 3 Florida
                                30
 4 New York
                                28
 5 Illinois
                                19
 6 Pennsylvania
                                19
 7 Ohio
                                17
 8 Georgia
                                16
 9 North Carolina
                                16
10 Michigan
                                15
# i 44 more rows
```

11. The presidential race in some states is a forgone conclusion. Because their is practically no uncertainty in who will win, polls are not taken. We will therefore assume that the party that won in 2020 will win again in 2024 if no polls are being collected for a state.

Download the following sheet:

```
library(gsheet)
sheet_url <- "https://docs.google.com/spreadsheets/d/1D-edaVHTnZNhVU840EPUhz3Cgd7m39Urx7HM8Peraw_res_2020 <- gsheet2tbl(sheet_url)</pre>
```

Tidy the raw_res_2020 dataset so that you have two columns state and party, with D and R in the party column to indicate who won in 2020. Add Maine CD-1 (D), Maine CD-2 (R), Nebraska CD-2 (D), and District of Columbia (D) by hand. Save the result to res_2020. Hint use the janitor row_to_names function.

```
library(janitor)
Attaching package: 'janitor'
The following objects are masked from 'package:stats':
    chisq.test, fisher.test
res 2020 \leftarrow raw res 2020[,c(1,4)] |>
  row_to_names(row_number = 1)|>
  filter(!State %in% c("Nationwide", 'Region', 'Midwest', 'Northeast',
                        'South', 'West', 'Washington D.C.', NA) ) |>
  select(state = State, party = P.S.) |>
  mutate(party = str_sub(party, 1, 1))
extra_entries <- data.frame(</pre>
  state = c("Maine CD-1", "Maine CD-2", "Nebraska CD-2", "District of Columbia"),
  party = c("D", "R", "D", "D")
res_2020 <- bind_rows(res_2020, extra_entries)</pre>
res_2020
# A tibble: 54 x 2
   state
               party
               <chr>
   <chr>
 1 Alabama
               R
 2 Alaska
               R
 3 Arizona
               R
 4 Arkansas
               R
 5 California D
 6 Colorado
               D
 7 Connecticut D
 8 Delaware
```

```
9 Florida R
10 Georgia R
# i 44 more rows
```

12. Decide on a period that you will use to compute your prediction. We will use spread as the outcome. Make sure the outcomes is saved as a proportion not percentage. Create a results data frame with columns state, avg, sd, n and electoral_votes, with one row per state.

Some ideas and recommendations:

- If a state has enough polls, consider a short period, such as a week. For states with few polls you might need to increase the interval to increase the number of polls.
- Decide which polls to prioritize based on the population and numeric_grade columns.
- You might want to weigh them differently, in which you might also consider using sample size.
- If you use fewer than 5 polls to calculate an average, your estimate of the standard deviation (SD) may be unreliable. With only one poll, you wont be able to estimate the SD at all. In these cases, consider using the SD from similar states to avoid unusual or inaccurate estimates.

```
short_period_start <- as.Date("2024-10-21") #two weeks
long_period_start <- as.Date("2024-09-01") #a month</pre>
poll_threshold <- 10</pre>
results <- polls |>
  filter(start_date >= long_period_start) |>
  group_by(state)|>
  mutate(
    poll_count_short = sum(start_date >= short_period_start),# Count polls in short period
    use_short_period = poll_count_short >= poll_threshold, # Decide if we use short period
  filter_start_date = as.Date(ifelse(use_short_period, short_period_start,
                                      long_period_start))
  ) |>
  filter(start_date >= filter_start_date) |>
  ungroup()
results <- results|>
  group_by(state)|>
  summarise(
    avg = sum(spread * sample_size, na.rm = TRUE) / sum(sample_size,
          na.rm = TRUE), # Weighted average based on the `population` and `numeric_grade` co
```

```
# A tibble: 45 x 5
  state
                                n electoral_votes
                 avg
                         \operatorname{sd}
  <chr>
              <dbl> <dbl> <int>
                                           <dbl>
1 Alaska
             -0.0915 0.0285
                                                3
2 Arizona
             -0.0240 0.0222
                               24
                                               11
3 California 0.265 0.0332
                                               54
                                6
4 Colorado 0.128 0.0260
                                6
                                               10
5 Delaware 0.17
                     0.0285
                                1
                                               3
6 Florida
           -0.0541 0.0268
                               34
                                               30
7 Georgia
             -0.0139 0.0114
                               18
                                               16
8 Illinois
             0.172 0.0285
                                2
                                               19
9 Indiana
             -0.165 0.0285
                                3
                                               11
10 Iowa
             -0.0771 0.0285
                                4
                                                6
# i 35 more rows
```

13. Note you will not have polls for all states. Assume that lack of polls implies the state is not in play. Use the res_2020 data frame to compute the electoral votes Harris is practically guaranteed to have.

```
harris_start <- res_2020|>
  filter(party == "D" & !state %in% unique(polls$state)) |>
  left_join(ev, by = "state")|>
  summarise(harris_start = sum(electoral_votes, na.rm = TRUE)) %>% # Sum electoral votes
  pull(harris_start)
harris_start
```

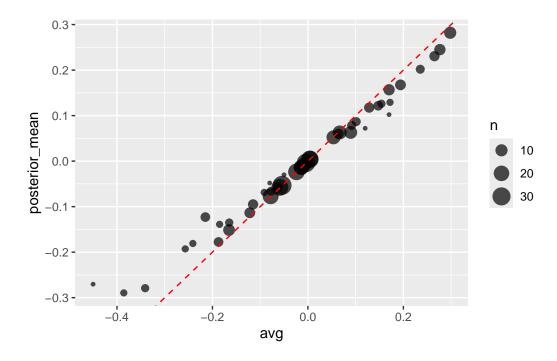
[1] 14

14. Use a Bayesian approach to compute posterior means and standard deviations for each state in results. Plot the posterior mean versus the observed average with the size of the point proportional to the number of polls.

```
theta <- 0
tau <- 0.035
sigma <- results$sd/sqrt(results$n)
x_bar <- results$avg
B <- sigma^2 / (sigma^2 + tau^2)

results <- results %>%
  mutate(
   posterior_mean = B*theta + (1 - B)*x_bar,
   posterior_se = sqrt(1/(1/sigma^2 + 1/tau^2))
)

ggplot(results, aes(x = avg, y = posterior_mean, size = n)) +
   geom_point(alpha = 0.7) +
   geom_abline(slope = 1, intercept = 0, linetype = "dashed", color = "red")
```



```
labs(
    x = "Observed Average Spread",
    y = "Posterior Mean Spread",
    title = "Posterior Mean vs Observed Average Spread by State",
    size = "Number of Polls"
) +
theme_minimal()
```

NULL

Before seeing polling data, we don't think any candidate has the advantage, and a difference of up to 7% either way in 5% significance level is possible, so I set theta <- 0 and tau <- 0.035

15. Compute a prediction and an interval for Harris' electoral votes and submit to the competition here. Include the code you used to create your estimate and interval below.

```
total_votes_harris <- harris_start</pre>
theta \leftarrow 0
tau <- 0.035
bias sd <- 0.03
harris_EV <- replicate(1000, {</pre>
  results |> mutate(sigma = sqrt(sd^2/n + bias_sd^2),
                     B = sigma<sup>2</sup>/(sigma<sup>2</sup> + tau<sup>2</sup>),
                     posterior_mean_2 = B*theta + (1 - B)*avg,
                     posterior_se_2 = sqrt(1/(1/sigma^2 + 1/tau^2)),
                     result = rnorm(length(posterior_mean_2),
                                      posterior_mean_2, posterior_se_2),
                     harris = ifelse(result > 0, electoral_votes, 0)) |> # Harris wins if post
    summarize(harris = sum(harris,na.rm=TRUE)+ harris_start) |>
    pull(harris)
})
predicted_votes_harris <- mean(harris_EV)</pre>
# Calculate a confidence interval
lower_bound <- quantile(harris_EV, 0.025)</pre>
upper_bound <- quantile(harris_EV, 0.975)</pre>
```

```
# Display results
cat("Expected Electoral Votes for Harris:", predicted_votes_harris, "\n")
```

Expected Electoral Votes for Harris: 267.648

```
cat("95% Prediction Interval:", lower_bound, "to", upper_bound, "\n")
```

95% Prediction Interval: 229 to 316

First, I got total_votes_harris, which initializes the electoral vote count for Harris with votes she is practically guaranteed to have. The priors are the same as Q14, as how I explained in Q14. Here I add general bias 0.03 as it is very likely there is a general bias that affects most pollsters in the same way, making the observed data correlated. I assume the average of polls favors Democrats by 3% based on historical data. Then I simulate Electoral Votes using Bayesian to simulate the number of electoral votes Harris is likely to receive from competitive states with 1000 times. For each run, I got posterior mean and sd. I generate a predicted spread for each state using the posterior distribution and assign electoral votes to Harris if the simulated spread (result) is positive. For each simulation, I calculate Harris's total electoral votes by adding her guaranteed votes from safe states and predicted wins in competitive states. Then taking the avg of simulation I got predicted_votes_harris and its 95% CI. Harris has an predicted electoral vote around 269, and the 95% confidence interval of electoral votes includes 269, showing much uncertainty that Harris will win.