

Exercise #4 – blackboard scribble

Declare/Assign: 1 Compare: 1	Return: 1 Add/Subtract: X	Call func: 2 + WCET(func) Other: 0
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Case 1: $z == 0$

$$\text{WCET}(\text{Calc}(0)) = \{\text{Declare}, R\} + \{\text{Compare}, z == 0\} + \{\text{Assign}, R\} + \{\text{Return}, R\} = 1 + 1 + 1 + 1 = 4$$

Case 2: $z == 1$

$$\text{WCET}(\text{Calc}(1)) = \{\text{Declare}, R\} + \{\text{Compare}, z == 0\} + \{\text{Compare}, z == 1\} + \{\text{Assign}, R\} + \{\text{Return}, R\} = 1 + 1 + 1 + 1 + 1 = 5$$

```
int Calc(int z){
    int R;
    if (z == 0) R = 1;
    else if (z == 1) R = 1;
    else R = Calc(z-1) + Calc(z-2);
    return R;
}
```

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Case 3: $z > 1$ (let x be cost for add & sub)

$$\begin{aligned} \text{WCET}(\text{Calc}(z > 1)) &= \{ \text{Declare}^1, R \} + \{ \text{Compare}^1, z \leq 0 \} + \{ \text{Compare}^1, z == 1 \} + \\ &\{ \text{Subtract}^x, z-1 \} + \{ \text{Call}^2, \text{Calc}(z-1) \} + \text{WCET}(\text{Calc}(z-1)) + \\ &\{ \text{Subtract}^x, z-2 \} + \{ \text{Call}^2, \text{Calc}(z-2) \} + \text{WCET}(\text{Calc}(z-2)) + \\ &\{ \text{Add}^x, \text{Calc}(z-1) + \text{Calc}(z-2) \} + \{ \text{Assign}^1, R \} + \{ \text{Return}^1, R \} = \end{aligned}$$

$$1 + 1 + 1 + x + 2 + \text{WCET}(\text{Calc}(z-1)) +$$

$$x + 2 + \text{WCET}(\text{Calc}(z-2)) + x + 1 + 1 =$$

$$9 + 3x + \text{WCET}(\text{Calc}(z-1)) + \text{WCET}(\text{Calc}(z-2))$$

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$$w_{CET}(\text{Calc}(2)) =$$

$$9 + 3x + w_{CET}(\text{Calc}(1)) + w_{CET}(\text{Calc}(0))$$

$$w_{CET}(\text{Calc}(3)) = 9 + 3x + w_{CET}(\text{Calc}(2)) + w_{CET}(\text{Calc}(1))$$

$$2 \cdot (9 + 3x) + 2 \cdot w_{CET}(\text{Calc}(1)) + 1 \cdot w_{CET}(\text{Calc}(0))$$

$$w_{CET}(\text{Calc}(4)) = 9 + 3x + w_{CET}(\text{Calc}(3)) + w_{CET}(\text{Calc}(2))$$

$$4 \cdot (9 + 3x) + 3 \cdot w_{CET}(\text{Calc}(1)) + 2 \cdot w_{CET}(\text{Calc}(0))$$

$$w_{CET}(\text{Calc}(5)) = 9 + 3x + w_{CET}(\text{Calc}(4)) + w_{CET}(\text{Calc}(3))$$

$$7 \cdot (9 + 3x) + 5 \cdot w_{CET}(\text{Calc}(1)) + 3 \cdot w_{CET}(\text{Calc}(0)) =$$

$$= 63 + 21x + 5 \cdot 5 + 3 \cdot 4 = 63 + 21x + 25 + 12 = \boxed{100 + 21x}$$

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b) Derive WCET for main() (let $x=4$)

$$\text{WCET}(\text{main}()) = \{\text{Declare, ans}\} + \{\text{Call, Calc}(5)\} + \text{WCET}(\text{Calc}(5)) + \{\text{Assign, ans}\} =$$

$$1 + 2 + \text{WCET}(\text{Calc}(5)) + 1 = 4 + \text{WCET}(\text{Calc}(5)) =$$

$$4 + 100 + 21x = 104 + 21x \Rightarrow \{x=4\} = 104 + 84 = 188$$

c) Check deadline for main()

$$\text{WCET}(\text{main}()) = 188 > \text{Deadline} = 180 \Rightarrow \text{Fail!}$$

```
int main() {
    int ans;
    ans = Calc(5);
}
```

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d) Derive WCET of `main()` in terms of X

According to subproblem b):

$$\text{WCET}(\text{main}()) = 104 + 21X$$

e) Find maximum cost X

$$\text{WCET}(\text{main}()) = 104 + 21X \leq 180 \Rightarrow 21X \leq 76$$

$$\text{That is: } X \leq \frac{76}{21} \approx 3,6$$

If only integer values of X : Select $X=3$
in order to meet deadline