

6.11

$$n_1 = 12, \mu_1 = 36 = \bar{x}, s_1 = 5$$

$$n_2 = 15, \mu_2 = 32 = \bar{y}, s_2 = 7$$

$n < 30$
 σ 未知 \rightarrow 大分配

$$\frac{12+15}{180} = \frac{27}{180}$$

$$1 - \alpha = 90\% = 0.9$$

$$\alpha = 0.1 \quad \frac{\alpha}{2} = 0.05$$

$$(\bar{x} - \bar{y}) \pm t_{\frac{\alpha}{2}} (n_1 + n_2 - 2) \sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}$$

$$= (36 - 32) \pm t_{0.05} (15 + 12 - 2) \sqrt{38.44 \left(\frac{1}{12} + \frac{1}{15} \right)}$$

$\underbrace{\frac{1}{12} + \frac{1}{15}}_{0.15}$

$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$= \frac{(14)7^2 + (11)5^2}{25}$$

$$= \frac{961}{25} = 38.44$$

$$= 4 \pm t_{0.05}(25) \times 2.401$$

$$= 4 \pm 1.708 \times 2.401$$

$$= 4 \pm 4.1 = (-0.1, 8.1)$$