

$$T: V \rightarrow W$$

$$\begin{array}{ccc} V & \xrightarrow{T} & W \\ \downarrow C: V \rightarrow [V]_{\alpha} & & \downarrow D: W \rightarrow [W]_{\beta} \end{array}$$

$$[V]_{\alpha} \in F^n \xrightarrow{L_A} [W]_{\beta} \in F^m$$

$$[W]_{\beta} = \underbrace{[L_A]_{\alpha}^{\beta}}_A [V]_{\alpha}$$

if $V = F^n$, $W = F^m$ only need to make sure C, D don't change the matrix (i.e. α, β are the standard ordered bases for F^n and F^m) $\Rightarrow T = L_A$

In general,
$$T = C L_A D^{-1}$$

$$T \neq L_A$$