

$$\begin{bmatrix} 7 & -3 \\ 0 & 4 \end{bmatrix} \quad \begin{aligned} 7x_1 - 3x_2 &= \lambda x_1 \\ 4x_2 &= \lambda x_2 \end{aligned}$$

$$\lambda_1 = 7, u_1 = [1, 0]$$

$$\lambda_2 = 4, u_2 = \left[\frac{1}{2}, \frac{1}{2}\right]$$

$$\begin{bmatrix} 1 \\ 0 \\ \frac{1}{2} \end{bmatrix}$$

$$(I - 5A)x = -5x.$$

$$-4Ax = -2x.$$

$$-5Ax = -6x.$$

$$A^{-1}x = 2x$$

$$\frac{5}{6}x = A^{-1}x.$$

$$-8 - 20 + 14 + 15$$

$$-8 - 20 + 14 + 2$$

$$(A - 4I)^{-1}x = \lambda x.$$

$$\frac{1}{\lambda}x = (A - 4I)x$$

$$\lambda_1 = -\frac{1}{9} \quad \lambda_2 = -\frac{1}{3}$$

$$\|e\| = \left| \frac{\alpha_2}{\alpha_1} \right| \left| \frac{\lambda_2}{\lambda_1} \right|^k \|u_2\|$$

$$-4, 9.$$

at least a factor of  $10^{-n} \rightarrow x \cdot x \cdot x \cdot \dots / 10^{-(n+1)}$

$$x_k = \frac{1}{\lambda_3^k} \left( \frac{\lambda_3^k}{\lambda_1^k} \alpha_1 u_1 + \frac{\lambda_3^k}{\lambda_2^k} \alpha_2 u_2 + \alpha_3 u_3 \right)$$

$$\|e_k\| = \left| \frac{\alpha_2}{\alpha_3} \right| \left| \frac{\lambda_3^k}{\lambda_2^k} \right| \|u_2\| = \left| \frac{\lambda_3^k}{\lambda_2^k} \right| \|e_0\| = \left| \frac{\lambda_3^k}{\lambda_2^k} \right| \|x_0\|$$

$$x_0 = \alpha_1 u_1 + \alpha_2 u_2 + \alpha_3 u_3$$

$$x_k = A^k x_0 = \lambda_1^k \alpha_1 u_1 + \lambda_2^k \alpha_2 u_2 + \lambda_3^k \alpha_3 u_3$$

$9^k$                        $7^k$                        $6^k$

$$= \lambda_1^k (\alpha_1 \underbrace{u_1}_{\text{circled}}) + \left(\frac{\lambda_2}{\lambda_1}\right)^k \alpha_2 u_2 + \left(\frac{\lambda_3}{\lambda_1}\right)^k \alpha_3 u_3$$

$$Av = 9v.$$

$$v = \begin{bmatrix} 4 \\ 8 \\ 10 \end{bmatrix}$$

$$\left[ \begin{array}{cc|cc} 1 & 2 & 1-k & 2 \\ 2 & 3 & 2 & 3-k \end{array} \right] \quad \begin{array}{l} 3-4k+k^2-4 \\ k^2-4k-1. \end{array}$$

$$\frac{4 \pm \sqrt{16+4}}{2} = 2 \pm \sqrt{5}$$

$$A x_{k+1} = x_k.$$

$$PLU x_{k+1} = x_k.$$

$$\underbrace{LU}_{\mathcal{V}} x_{k+1} = P^T x_k$$



$$L y = P^T x_k$$

$$U x_{k+1} = y$$