#### **STAT 426**

# 1.1 Categorical Response Data

### Categorical response data

- We make the distinction between response (or dependent) variables and explanatory (or independent) variables.
- We concentrate on the response variables that are categorical.
- Explanatory variables can be of any type as in ordinary regression models

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### Categorical response data

#### Categorical variables scales:

- Nominal: Categories do not have a natural order.
- Ordinal: Categories have a natural order.

#### Other levels of measurements:

Interval: There is a numerical distances between any two values.

Example: Blood pressure level.

 Ratio:An interval variable where ratios are valid (presence of absolute zero).

Example: Distance run by an athlete.

Categorical data arise from many applications in the real world, specially in social and biomedical sciences. Let's see some examples:

### Example

Example 1: Level of income A new business is investigating the power income of their potential customers, to agree upon an affordable price on their products. They use a questionnaire with the question: What is your household income?

- Below \$30,001
- \$30,001 \$40,000
- \$40,001 \$50,000
- \$50,001 and above

#### Example

Example 2: Level of education When filling forms for job applications, admission, training, etc., a respondent is usually requested the level of education. Companies use a questionnaire with the question: What is your highest level of education?

- School SAT
- High School
- BSc
- MSc
- PhD

#### Example

Example 3: Level of satisfaction Businesses normally like to rate a customer service rendered in order to improve their service. They use a questionnaire with the question:

Kindly rate your customer service experience with us:

- Very poor
- Poor
- Neutral
- Good
- Very good

#### Example

Example 4: Level of motivation A company wants to improve employee productivity and uses a questionnaire to study what motivates employees to work better. The specific question is: What motivates you to work better? (If Others please specify specify)

- Peer motivation
- Recognition
- Professional growth opportunities
- Friendly work culture
- Others —

#### Example

Example 5: Motives for travelling Travel companies want to improve their marketing strategies and ask their customers the following question: What are your motives for travelling? (If Others please specify)

- Business
- Leisure
- Family
- Study
- Health
- Others ——

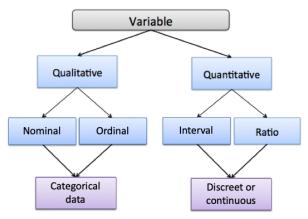
#### Levels of measurements

- A variable's level of measurement determines the statistical methods to be used for its analysis.
- Variables hierarchy: Ratio > Interval > Ordinal > Nominal
- Statistical methods applied to variables at a lower level can be used with variables at a higher level but the contrary is not true.
  Example: An ordinal variable can be analyzed as a nominal
  - variable (ignoring the order) but the opposite does not apply.
- In this class we will discuss the analysis of nominal and ordinal variables.
- The methods can also be applied to interval and ratio variables grouped into a small number of ordered categories.
  - Example: Years of Education: 0-10 years, 10-12 years, > 12 years and so on.

#### Levels of Measurements

It is important to make the distinction between:

- Continuous vs. Discrete variables
- Quantitative vs. Qualitative



# Models for Categorical Responses

- Models in this class resemble regression models with continuous response variables, but responses can have
  - Binomial
  - Multinomial
  - Poisson
- Featured models are:
  - Logistic regression models (logit): Binary responses and assume a binomial distribution.
  - Generalization of the logistic regression: Multi-category responses (nominal and ordinal).
  - Loglinear models: Count data and assume a Poisson distribution.
  - Generalizations to multivariate categorical responses: Represent associations and interactions among variables.
  - Models for repeated categorical responses: Longitudinal data.

# Example (Agresti, Table 2.1)

Myocardial In	farction
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	Fatal Attack	Nonfatal Attack	No Attack
Placebo	18	171	10845
Aspirin	5	99	10933

- Is there a relationship between myocardial infarction and aspirin use?
- If so, of what kind? How strong?
- What kinds of quantities can measure the strength of the relationship?

# Example (Agresti, Table 2.1)

	Myocardial Infarction			
	Fatal Attack	Nonfatal Attack	No Attack	
Placebo	18	171	10845	
Aspirin	5	99	10933	

What kind of statistical models might be appropriate?

- What is random?
- What would be the distributions?
- How would you form estimates? Tests? Confidence intervals?

#### Please review:

- ullet convergence in probability  $( o_p)$
- convergence in distribution  $(\stackrel{d}{\rightarrow})$
- law of large numbers (LLN)
- central limit theorem (CLT)
- consistency and asymptotic normality
- normal approximation to the binomial
- Poisson approximation to the binomial
- normal approximation to the Poisson
- confidence intervals (CIs)
- tests (level, power) and P-values
- marginal and conditional probabilities, densities, and distributions
- Bayes' rule for probabilities