Short-term Finance, Long-term Effects*

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Abstract

We study the effect of short-term finance on firm growth and its aggregate implications in emerging economies. In theory, short-term finance promotes firm growth by enabling entrepreneurs to allocate their net worth more efficiently away from unproductive cash and towards productive capital. Importantly, these effects are persistent only if firms face intertemporal distortions in the form of exit risk or a tax on net worth. The quantitative model fitted to Moroccan data replicates qualitatively and quantitatively the observational impacts of a loan guarantee program (LGP) designed to relax short-term financial constraints. Fitting the model to the data also reveals that intertemporal distortions are large and that the costs of participating in the LGP are high. This implies that there are potentially large gains from increasing the guaranteed ratio and decreasing the participation costs. These two policies generate substantial growth and welfare gains, with the former generating relatively higher growth and the latter motivating relatively more participation.

Keywords: SME financing; financial frictions; liquidity constraints; developing economy; JEL Classification: O11, O16, E22, E44, G28, G38

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1 Introduction

The lack of access to external credit for Small and Medium Enterprises (SMEs) is one of the major development bottlenecks in MENAP (Middle East, North Africa, Afghanistan, and Pakistan) countries. For instance, Blancher et al. (2019) find that closing the SME financial inclusion gap in those countries would increase annual growth by up to 1%. The first purpose of this paper is to study the ability of loan guarantee programs (LGP) targeted at SMEs to improve their access to credit, the extent to which it actually promotes development, and through which channels, using a model calibrated to Moroccan firm-level data on an ongoing LGP.

The second purpose of this paper is to understand the effect of short-term external finance on firm growth and the aggregate economy in emerging countries. Financial frictions hinder the ability of firms to use inputs efficiently, affect firm growth, and, therefore, lower economic development, especially in emerging economies. Extensive literature addresses how the scarcity of long-term external finance leads to under-leveraged small and young enterprises and hinders economic development.¹ However, little attention has been paid to the scarcity of short-term external finance in emerging countries. This paper fills that gap.

The role of short-term external finance is different from long-term external finance. Long-term external finance promotes firm growth since it directly enlarges entrepreneurs' total asset scale, given their net worth. Short-term external finance, as we show in a simple dynamic model, promotes firm growth by enabling a more efficient allocation of the entrepreneurs' existing net worth. Since entrepreneurs in emerging economies tend to hoard a substantial amount of cash to meet their working capital needs, short-term external finance promotes firm growth by allowing entrepreneurs to allocate their net worth more efficiently away from unproductive cash and towards productive capital. Importantly, these effects are persistent only if firms face intertemporal distortions in the form of exit risk or a tax on net worth. These distortions, by discouraging net worth accumulation, prevent firms from outgrowing their financial constraints through savings and self-financing. Therefore, in the presence of intertemporal distortions, better access to external finance has both short-term and long-term impacts.

To evaluate the equilibrium growth and welfare gains of expanding credit guarantee programs, we calibrate and estimate a quantitative model using a loan guarantee program (LGP) designed to relax short-term external financial constraints in Morocco. Our dataset combines Moroccan firm-level data from Orbis with the national-level loan guarantee data from Tamwilcom.²

¹See Cooley and Quadrini (2001), Albuquerque and Hopenhayn (2004), Clementi and Hopenhayn (2006), DeMarzo and Fishman (2007), Buera, Kaboski, and Shin (2011a), and Arellano, Bai, and Zhang (2012), among others.

²Tamwilcom is a public financial institution under the supervision of the Central Bank of Morocco, Bank Al-Maghrib. Therefore, the national loan guarantee data covers every firm that has ever been guaranteed in Morocco.

The model includes, for quantitative purposes, a uniformly distributed LGP participation cost and a size-dependent collateral constraint. The participation cost prevents small firms from entering the program as only firms with a high enough growth potential self-select into the program. In contrast, the large firms do not self-select into the program since they do not need the guarantee. These assumptions are important quantitatively to fit the endogenous selection of firms into the program and the observed hump-shaped participation rate in firm size.

There are two main takeaways from the model's calibration. First, a high participation cost, equivalent to one-third of the average net worth, is needed to fit the low LGP participation rate of 3.8%. This implies that only large constrained, or small fortunate firms can access the guarantee. This large number reflects a lack of access of small firms to the guarantee program due to geographical barriers or to the fact that many small firms do not have a relationship with the banking system. Making access to the LGP easier is, therefore, one channel through which the program can be expanded. Second, intertemporal distortions are large. These large distortions imply that credit guarantees have a strong impact on firms both in the short and long run.

We empirically validate the findings from our model by using our Moroccan data. The empirical results show that, relative to their peers, (i) guaranteed firms expand their production scale homogeneously by increasing sales, capital input, and labor input by about 10% relative to their matched peers and (ii) they decrease their cash-to-asset ratio. Importantly, the results are persistent, which is consistent with the presence of intertemporal distortions. We do not interpret these results as causal, as we cannot rule out self-selection: firms that are more productive can endogeneously self-select into the program. However, our quantitative model, which accounts for self-selection, is able to replicate the empirically estimated impact of the guarantee: the model-simulated data yields estimation results that are similar to the empirical model.

We then examine two policies aimed at expanding the LGP: a higher guaranteed ratio and a lower participation cost. We show that the gains from enlarging the loan guarantee programs by reducing both frictions are substantial. Increasing the guaranteed ratio from 60% to 80%, as in Indonesia, more than doubles the participation rate, decreases the cash ratio by 1.2 percentage points, and achieves an output growth of 0.09% and a welfare gain of 0.25%. Decreasing participation costs achieves less extra growth and welfare, but increases the participation rate further without substantially increasing the guaranteed portfolio. Interestingly, increasing the guaranteed ratio also has a positive effect on participation, as it increases the gains from participating in the program. This is especially true for small firms, which are more likely to be constrained while productive.

This paper relates to the large theoretical literature on firms' financial frictions and their aggregate implications, such as Cooley and Quadrini (2001), Albuquerque and Hopenhayn (2004),

Quadrini (2004), Clementi and Hopenhayn (2006), DeMarzo and Fishman (2007), Huynh and Petrunia (2010), Arellano, Bai, and Zhang (2012), Moll (2014), Midrigan and Xu (2014), Gopinath et al. (2017), Jo and Senga (2019), Buera, Kaboski, and Shin (2021) and others. We contribute to this literature first by focusing on short-term finance. We show that short-term external finance promotes firm growth by allowing entrepreneurs to allocate their net worth more efficiently towards productive capital stock and away from unproductive cash holdings. Second, we contribute to a better understanding of the aggregate impact of external finance. The literature has shown that the gains from access to external finance are elusive. In particular, when productivity shocks are persistent, firms typically grow out of their collateral constraints through savings and self-financing (Moll, 2014; Buera, Kaboski, and Shin, 2021). We show that intertemporal distortions, that is, distortions in the consumption/saving choices of entrepreneurs, are an overlooked and crucial factor that amplifies the aggregate effect of external finance by hindering firms' self-financing abilities. This intertemporal friction interacts with the external finance frictions to determine the long-run scale of firms. We estimate these distortions and show that they are important in Morocco. We also show, by performing counterfactual exercises, that they contribute substantially to the aggregate effect of the LGPs.³

In our model, credit guarantees are modeled explicitly. Firms face a credit constraint that is micro-founded in the spirit of Hart and Moore (1994) and Kiyotaki and Moore (1997). The renegotiation-proof debt contract generates a debt limit equal to the creditors' outside value. This outside option depends on the liquidation value of the firm. Credit guarantees affect the firms' credit constraints by increasing the creditors' outside value. We assume that the firms' participation constraint is always satisfied, which we check ex-post in our quantitative analysis. In other studies, the credit policy is typically modeled as a technology that reduces or annihilates the enforceability constraint of the loan (Jo and Senga, 2019; Buera, Kaboski, and Shin, 2011b, 2021). We acknowledge here that credit guarantees do not improve the firms' credit access through better enforceability of the loan but rather by affecting the banks' incentives to provide loans. Another strand of the literature has shown that when markets are prone to adverse selection (Stiglitz and Weiss, 1981), credit guarantees improve aggregate outcomes (Smith and Stutzer, 1989; Gale, 1990; Philippon and Skreta, 2012). Other papers, some of which were motivated by the Covid-19 crisis, focus on emergency credit guarantee programs that are put in place to limit firms' defaults and debt overhang (Philippon and Schnabl, 2013; Eleney, Landvoigt, and Van Nieuwerburgh, 2022; Glode and Opp, 2023; Martin, Mayordomo, and Vanasco, 2023).

This paper also contributes to the empirical literature on credit guarantee schemes. A credit

³Intertemporal distortions are often in the background of theoretical papers studying firms' financial frictions in the form of an exit probability or a tax, but their role is not made explicit or quantified. See for instance Arellano, Bai, and Zhang (2012), Jo and Senga (2019), Cooley and Quadrini (2001).

guarantee scheme is one of the most common policy tools to facilitate SMEs' access to finance. Gudger (1998) and Green (2003) provide an overview of credit guarantee programs' typology, design, implementation, and general evaluation worldwide. Beck, Klapper, and Mendoza (2010) survey 76 partial credit guarantee schemes across 46 developed and developing countries. Saadani, Arvai, and Rocha (2011) focus on the Middle East and North Africa (MENA) and review credit guarantee programs in 10 countries in the MENA region. Some empirical contributions study the impact of guarantee programs using microdata, including Paravisini (2008), Oh et al. (2009), Lelarge, Sraer, and Thesmar (2010), Bach (2013), Banerjee and Duflo (2014), Brown and Earle (2017), Mullins and Toro (2018), Bhue, Prabhala, and Tantri (2019), Wilcox and Yasuda (2019), Barrot et al. (2019) and Bachas, Kim, and Yannelis (2021). Our paper contributes to the literature by presenting new empirical findings on the usage of cash and the profile of growth post-guarantee. Our evidence is not causal but is used to validate our model.

The rest of the paper is organized as follows. Section 2 lays down the full model. Section 3 presents the mechanism and implications of short-term financial constraints in a simple special case. Section 4 calibrates the full model to Moroccan firm-level data and a Moroccan loan guarantee program. Section 5 documents some empirical findings and validates the quantitative analysis. Finally, Section 6 performs policy experiments.

2 The Model

We consider an economy with heterogeneous entrepreneurs facing collateral and working capital constraints, intertemporal distortions, and access to short-term loan guarantees with fixed participation costs. Time is discrete. There is a unit mass of entrepreneurs indexed by $i \in [0,1]$. Each entrepreneur owns a firm that is subject to idiosyncratic productivity shock. We do not distinguish entrepreneurs and firms. Firms decide how much investment to undertake, how much labor to hire, how much debt to issue, how much cash to hold, and how many dividends to pay. They face three frictions: first, external financial friction in the form of a collateral constraint and a working capital constraint; second, intertemporal distortions in the form of an exogenous exit risk and a tax on net worth; third, imperfect selection into the guarantee program in the form of a stochastic participation cost. A capital good producer and a unit mass of other households complete this general equilibrium model.

2.1 Technology and Production

Technology Each firm i produces with capital $k_{i,t}$, and labor $l_{i,t}$ using the production function $y_{i,t} = z_{i,t}F(k_{i,t},l_{i,t}) + (1-\delta)q_tk_{it}$, where $z_{i,t}$ is the firm's idiosyncratic stochastic productivity, which follows an exogenous Markov process $\log(z_{i,t}) = \rho_z \log(z_{i,t-1}) + \sigma_z \varepsilon_{i,t}$, with $\varepsilon_{i,t}$ a standard normal i.i.d. process, δ is the capital depreciation rate and q_t is the price of capital. The input combination $F(k_{i,t},l_{i,t})$ features decreasing returns to scale.

Working Capital Constraint At the beginning of each period, before the realization of their productivity shocks, firms pay in advance for their working capital: they are required to pay their current period wage bill $w_t l_{i,t}$ before production. They can finance this working capital through both internal and external funds: they can use their cash holdings $c_{i,t}$ or short-term borrowing $b_{i,t} \leq \bar{b}_{i,t}$. Therefore, the working capital constraint is $w_t l_{i,t} \leq c_{i,t} + \bar{b}_{i,t}$.

2.2 Credit Market

Firms can access competitive financial intermediaries, who receive deposits from all households (including cash from entrepreneurs) and provide short-term loans to firms. The competitive financial intermediaries make zero net profit with the same market deposit interest rate and loan interest rate of r_t . Contracts are imperfectly enforceable, as entrepreneurs can walk away without completing production. This gives rise to a short-term borrowing constraint.

The short-term borrowing $b_{i,t} \leq \bar{b}_{i,t}$ of the firm i is subject to a collateral constraint. Since entrepreneurs can easily transfer their liquid assets (cash holdings), financial intermediaries only consider their illiquid assets (fixed capital) as collateral. As in Hart and Moore (1994) and Kiyotaki and Moore (1997), we assume that the firm's creditors impose a repudiation-proof debt limit on the firm. This debt limit is equal to the liquidation value of the firm, which is the outside option of the creditors.⁴ Since the liquidation of the firm's fixed capital would incur fixed costs and proportional re-structuring costs, the collateral constraint could, therefore, be nonlinear in the firm's capital stock (Gopinath et al., 2017). We write the liquidation value as $\Theta(k_{i,t})$, which will be specified later. Without guarantees, the debt limit $\bar{b}_{i,t}$ is equal to the liquidation value $\Theta(k_{i,t})$.

We are assuming here that the firm participation constraint is always satisfied and firms do not default in equilibrium. In the event of default, the firm does not pay back its debt but loses its capital stock. For default to be ruled out, it is enough that the depreciated value of capital $(1 - \delta)k_{it}$ is higher than the total value of debt repayments. We assume this condition is satisfied throughout, but check the ex-post to ensure it is indeed the case in the quantitative analysis.

⁴As in Kiyotaki and Moore (1997), we consider a situation where firms can negotiate the debt down to the liquidation value of the firm's capital because the value of the project is zero without the cooperation of the firm owner.

2.3 Loan Guarantee

We now introduce the loan guarantee programs. For the sake of fitting the Moroccan credit market and LGP, we make the following assumptions. First, a certain fraction of credit is non-bank third-party credit, which the government can hardly guarantee. Therefore, we assume that there are two types of intermediaries: banks, which can benefit from the LGP, and non-bank creditors, which cannot. We denote bank loans by b_{it}^b and the non-bank loans by b_{it}^{nb} . In case of liquidation, banks are entitled to a fraction $s \in [0,1]$ of the firm's collateral in case of default, while non-bank creditors are entitled to a fraction 1-s. This fraction s represents the relative bargaining power of bank and non-bank creditors in appropriating the liquidation value once the firm has defaulted. This means that the firm could renegotiate its formal debt b_{it}^b down to $s\Theta(k_{it})$ with the banks and its informal debt b_{it}^{nb} down to $(1-s)\Theta(k_{it})$ with its informal creditors. Banks and non-bank creditors thus each impose a separate renegotiation-proof debt limit: $b_{it}^b \leq s\Theta(k_{it})$ and $b_{it}^{nb} \leq (1-s)\Theta(k_{it})$. This implies that in practice, a proportion s of a firm's loans comes from formal banks, and a proportion s occurs from non-bank creditors.

Second, the LGP does not restrict large firms from applying.⁶ With a fixed commission fee, unconstrained large firms would self-select not to participate.

Third, a firm's selection into LGP does not perfectly reflect its profitability. Therefore, we assume that firms participating in the LGP incur a uniformly distributed random fixed participation cost $\xi \in [0, \bar{\xi}]$, which is paid in units of labor. This fixed cost accounts for all the explicit and implicit barriers to accessing the guarantees, which can be pecuniary, geographical, or cognitive. In practice, this cost can reflect an unequal access to the guarantee. Moreover, as we will see, because of this cost, only firms that are profitable enough will select into the guarantee. The model can then account for endogenous self-selection.⁷

Finally, upon successfully getting the guaranteed loan, a fraction x of the bank loans $b_{i,t}^b$ is guaranteed, and the firm pays a commission fee μ on top of the interest rate for the guaranteed part of the loan to the government. If the guaranteed firm defaults, the government would repay the guaranteed proportion x of the loan to the banks.

The LGP multiplier If the firm obtain the guarantee, then the bank's outside option increases by the amount $xb_{i,t}^b$, which means that the renegotiation-proof debt limit on bank loans becomes $b_{i,t}^b \leq s\Theta(k_{i,t}) + xb_{i,t}^b$. This generates a financial multiplier effect: for each unit of additional bank

⁵For instance, a large fraction of credit in Morocco is composed of trade credit.

⁶In fact, the Moroccan LGP does impose a limit on firm size, but this limit is not binding in practice as very few large firms apply to guarantee. In alternative specifications, we impose a cap on firm size in the LGP. The quantitative results are almost equivalent to the baseline model.

⁷A random fixed cost setup is widely used in the lumpy investment literature, i.e., Khan and Thomas (2008), Fang (2021), and Fang (2023). It is also introduced in Chen, Deng, and Fang (2022) for patent collateral participation.

loan, the firm increases its liquidation value by x. The effective constraint, which takes into account this multiplier effect, is then: $b_{i,t}^b \leq s\chi\Theta(k_{i,t})$, where $\chi=\frac{1}{1-x}$ is the LGP multiplier. The LGP multiplier is greater than one and can be very large. For instance, if the government guarantees 60% of the bank loan, then $\chi=\frac{100\%}{100\%-60\%}=2.5$.

Effective constraint on total borrowing Let $F = \{A, N\}$ indicate whether a firm decides to pay the fixed participation cost and participate in the LGP. When F = N, the firm does not pay the participation cost and can only borrow up to its original collateral constraint. When F = A, the firm pays the participation cost and relaxes its borrowing constraint. In that case, the firm can borrow up to χ times more in the form of bank loans. Therefore, the effective constraint on total borrowing $b_{i,t} = b_{i,t}^b + b_{i,t}^{nb}$ that the firm faces depends on F:

$$b_{i,t} \le \begin{cases} (1 + (\chi - 1)s)\Theta(k_{i,t}) & if F = A \\ \Theta(k_{i,t}) & if F = N \end{cases}$$

2.4 Recursive Problem for Firms

The individual state variables of a firm are its idiosyncratic productivity $z_{i,t}$ and its beginning-of-period net worth $n_{i,t-1}$. Firm decisions are divided into three sub-periods. In the first sub-period, the firm learns about the participation cost for the next period and decides whether to participate in the LGP. In the second sub-period, the firm makes production and working capital decisions. In the third sub-period, it makes consumption and saving decisions.

Production Decisions It is useful first to consider the production decisions, which happen in the second sub-period, before the participation decisions in the first sub-period. In the second sub-period, after having drawn its participation cost ξ_t^i and decided whether to participate $(F_t^i = A)$ or not $(F_t^i = N)$ in the LGP, the firm maximizes its total net revenue given its productivity, its beginning-of-period net worth, and its LGP participation decision F_t^i . The firm decides how much capital $q_t k_{i,t}$ to invest, how much cash $c_{i,t}$ to hold, and how much labor $w_t l_{i,t}$ to hire. Given the working capital and collateral constraints, the firm maximizes its net revenue

$$\pi^*(z_{i,t}, n_{i,t-1}, F_{i,t}) = \max_{k_i^t, c_i^t, l_i^t, b_i^t} \left\{ z_{i,t} F(k_{i,t}, l_{i,t}) - w_t l_{i,t} + (1 - \delta) q_t k_{i,t} + (1 + r_t) c_{i,t} - r_t b_{i,t} - \mu \tilde{b}_{i,t} \right\}$$
(1)

subject to the constraints

$$n_{i,t-1} = q_t k_{i,t} + c_{i,t} (2)$$

$$w_t l_{i,t} \le c_{i,t} + \mathbb{1}_{F_{i,t}=A} \cdot (1 + (\chi - 1)s)\Theta(k_{i,t}) + (1 - \mathbb{1}_{F_{i,t}=A}) \cdot \Theta(k_{i,t})$$
(3)

$$b_{i,t} = w_t l_{i,t} - c_{i,t} \tag{4}$$

$$\tilde{b}_{i,t} \equiv \mathbb{1}_{F_{i,t}=A} \cdot \chi s\Theta(k_{i,t}) \tag{5}$$

where $\tilde{b}_{i,t}$ is the guaranteed proportion of loans that pays a commission fee μ .

Participation Decision Now that we understand how net revenues are affected by participation in the LGP, we can characterize the participation decision $F_{i,t}$. In the first sub-period, the chooses to participate ($F_{i,t} = A$) whenever $\xi_t^i < \xi^*(z_{i,t}, n_{i,t-1})$, where $\xi^*(z_{i,t}, n_{i,t-1})$ is a threshold participation cost:

$$\xi^*(z_{i,t}, n_{i,t-1}) = \frac{\pi^*(z_{i,t}, n_{i,t-1}, A) - \pi^*(z_{i,t}, n_{i,t-1}, N)}{w_t}$$
(6)

A firm with state $(z_{i,t}, n_{i,t-1})$ which draws a fixed cost higher than $\xi^*(z_{i,t}, n_{i,t-1})$ will not participate $(F_{i,t} = N)$ in the loan guarantee program. Otherwise, it pays the fixed cost and joins the program.

Intertemporal Decisions and Intertemporal Distortions Finally, in the third sub-period, the entrepreneur makes saving and consumption decisions. The entrepreneur faces two intertemporal distortions that are relevant to their consumption/saving choices. The first is due to the high exit risk that firms face in emerging countries. We assume an exogenous survival rate $\epsilon \leq 1$. Exiting firms are replaced with the same measure of entrants with an initial low net worth \underline{n}_0 . The second is the "erosion" of the firm's net worth, which we represent through a tax on net worth $\tau \geq 0$. This erosion could come from effective taxes, but also red tape, corruption, and expropriation risk and captures the entrepreneur's potential losses on their net worth in developing countries. Both the exit risk and net worth erosion work as intertemporal distortions. We will use our Moroccan firm-level data to discipline these distortions and quantify their economic effects.

The entrepreneur makes consumption/saving decisions to maximize her value function $v(z_{i,t}, n_{i,t-1}, F_{i,t})$ given her end-of-period total net revenue $\pi^*(z_{i,t}, n_{i,t-1}, F_{i,t})$ and her participation cost ξ_t^i . We write the entrepreneur's optimization recursively:

$$v(z_{i,t}, n_{i,t-1}, F_{i,t}, \xi_t^i) = \max_{d_{i,t}, n_t^i} \left\{ \frac{d_{i,t}^{1-\eta}}{1-\eta} + \beta \epsilon E_t [\tilde{v}(z_{i,t+1}, n_{i,t})] \right\}$$
(7)

where β is the stochastic discount factor of the entrepreneur.

The net worth follows the accumulation rule:

$$n_{i,t} = (1 - \tau) \left\{ \pi^*(z_{i,t}, n_{i,t-1}, F_{i,t}) - d_{i,t} - w_t \xi_{i,t} \right\}$$
(8)

 $^{^8}$ The initial net worth \underline{n}_0 of all new entrants equals the post-restructuring net worth of exiting firms. We assume that financial institutions owned by all households conduct the restructuring, so such restructuring costs return to households' total income.

Finally, $\tilde{v}(z_{i,t+1}, n_{i,t})$ is the ex-ante value of the firm before drawing the new participation cost in period t+1. Therefore, $\tilde{v}(z_{i,t+1}, n_{i,t}) \equiv \frac{\xi^*(z_{i,t+1}, n_{i,t})}{\xi} v(z_{i,t+1}, n_{i,t}, A) + (1 - \frac{\xi^*(z_{i,t+1}, n_{i,t})}{\xi}) v(z_{i,t+1}, n_{i,t}, N)$, because $\xi^*(z_{i,t}, n_{i,t})$ is bounded between 0 and ξ .

2.5 Other Households and the Capital Good Producer

The general equilibrium model is completed by introducing a unit mass of identical households that consume and supply labor and the capital goods producer who supplies investment goods.

Other Households There is a unit measure continuum of identical non-entrepreneur households with preferences over consumption C_t and labor supply L_t whose expected utility is:

$$E_0 \sum_{t=0}^{\infty} \beta^t \left(\frac{C_t^{1-\eta}}{1-\eta} - \theta \frac{L_t^{1+\omega}}{1+\omega} \right)$$

subject to the budget constraint $C_t + \frac{1}{1+r_t}B_t \leq B_{t-1} + w_tL_t + \Pi_t$, where β is the discount factor of households, θ is the disutility of working, r_t is the interest rate, B_t is a one-period bond, and w_t is the wage. Π_t summarizes all the profits from financial institutions and all the government gains or losses in the loan guarantee program that are transferred to other households. Households choose consumption, labor, and bonds, which supply two Euler equations that determine both the wage and the real interest rate:

$$w_t = -\frac{U_l(C_t, L_t)}{U_c(C_t, L_t)} = \theta L_t^{\omega} C_t^{\eta}$$
(9)

$$\frac{1}{1+r_t} = \beta \frac{U_c(C_{t+1}, L_{t+1})}{U_c(C_t, L_t)} = \beta \left(\frac{C_t}{C_{t+1}}\right)^{\eta}$$
(10)

Capital Good Producer There is a representative capital good producer who produces new aggregate capital using the technology $\Phi(I_t/K_t)K_t$, where I_t are units of the final good used to produce capital, $K_t = \int k_{jt} dj$ is the aggregate capital stock at the beginning of the period, $\Phi(I_t/K_t) = \frac{\delta/\phi}{1-1/\phi} \left(\frac{I_t}{K_t}\right)^{1-1/\phi} - \frac{\delta}{\phi-1}$, and δ is the steady-state investment rate. Profit maximization pins down the relative price of capital as $q_t = \frac{1}{\Phi'(I_t/K_t)} = \frac{I_t/K_t}{\delta}^{1/\phi}$.

2.6 Equilibrium Definition

We now characterize and define the equilibrium of the model. We focus on the stationary equilibrium, given current government policies.

Definition 1 (Stationary Equilibrium) A stationary equilibrium for this economy is defined by a set of policy functions $\{v(z, n, F, \xi), \xi^*(z, n), k(z, n, F), c(z, n, F), l(z, n, F), \pi(z, n, F), d(z, n, F, \xi)\}$, a set of quantities $\{C, L, Y, K\}$, a set of prices $\{w, r, q\}$, and a distribution $\mu'(z, n, F, \xi)$ that solves the firms' problem, capital good producer's problem, household's problem, and market clearing of labor and final goods such that:

- (i). [Firm Optimization] Taking the aggregate prices $\{w, r, q\}$ as given, $\{v(z, n, F, \xi), \xi^*(z, n), k(z, n, F), c(z, n, F), \pi(z, n, F), d(z, n, F, \xi)\}$ solve the firms' static participation and production choices and the dynamic consumption/saving choice.
- (ii). [Household and Capital Good Producer Optimization] Taking the aggregate prices $\{w, r, q\}$ as given, C and L solve the household's utility maximization problem and I and K solve the capital producer's maximization problem.
- (iii). [Market Clearing] Given the aggregate prices $\{w, r, q\}$ as given, the labor market clears $L = \int l(z, n, F) d\mu'(z, n, F, \xi)$, and the final goods market clears $Y = C + D + I + \Delta$, where $D = \int d(z, n, F, \xi) d\mu'(z, n, F, \xi)$ is the sum of entrepreneurs' dividend and $\Delta = \int \tau n(z, n, F, \xi) d\mu'(z, n, F, \xi)$ is the sum of the net worth erosion across all firms.
 - (iv). The quantities $\{C, L, Y, K\}$, prices $\{w, r, q\}$, and distribution $\mu'(z, n, F, \xi)$ are constant.

3 The Mechanism and Predictions

Before we turn to the quantitative and empirical analyses, we consider a simple, special case of the model in partial equilibrium to illustrate the main mechanisms that could qualitatively guide our empirical analysis and discuss their aggregate implications.

The mechanism generates three predictions. First, we show how, in the joint presence of collateral and working capital constraints, getting access to the loan guarantee program alleviates cash needs, allocates resources to productive capital, and achieves higher sales in the short run. Second, we show that while the loan guarantee always benefits firms in the short run, the guarantee affects the firm's long-run scale only in the presence of intertemporal distortions. Third, selection into the program is endogenous: when the participation cost prevents the participation of small and unproductive firms, it also lowers the participation of large firms due to sufficient self-financing. As a result, we should observe a hump-shaped participation rate in the loan guarantee program over firm size.

3.1 A Special Case

We consider a special case of the full model defined as follows:

Definition 2 (A Special Case) In the special case, we make the following assumptions:

(i). The technology is Leontief, and productivity is constant:

$$y_t = Z[\min(k_t, a^{-1}l_t)]^{\alpha} \tag{11}$$

where Z is the firm's constant total productivity, a^{-1} measures the relative labor productivity of the firm, and α is the curvature of the production function.

- (ii). The collateral constraint is linear: $\Theta(k_t) = \theta k$. Note that in a conventional calibration, labor share relative to capital share is $a \approx 2$, and $\theta < 1$, so we assume that $a > \theta$.
- (iii). The loan guarantee does not incur fees: $\mu = 0$, the participation cost is zero: $\xi = 0$, and all credits are formal loans: s = 1.
- (iv). The wage, the price of capital, and the interest rate are constant as the economy is in a partial equilibrium: $w_t = q_t = 1$ and $1 + r_t = 1/\beta$.

In what follows, we discuss the effects of short-term finance in the form of LGPs on the firm's optimal choices of capital and cash and on firm growth. The LGP helps the firm scale up its pledgeable share of capital (θ) from θ_{low} (F = N) to θ_{high} (F = A) where the additional share ($\theta_{high} - \theta_{low}$) is guaranteed by the government. We compare the trajectories of a firm in two worlds, one in which it obtains access to the guarantee and one in which it does not.

Define $\psi_t = Z[\min(k_t, a^{-1}l_t)]^{\alpha} - q_tk_t - w_tl_t + (1 - \delta)k_t$ as the equilibrium profits. With the Leontieff assumption, $l_t = ak_t$ always holds. Then, since $w_t = q_t = 1$, $\psi_t = \psi(k_t) = Zk_t^{\alpha} - (a + \delta)k_t$. We consolidate the firm's problem, represented by Equation (1) and Equation (7). The following maximization can summarize the firm's choice:

$$v(n_{t-1}) = \max_{k_t, c_t, d_t, n_t} \left\{ \frac{d_t^{1-\eta}}{1-\eta} + \beta \epsilon v(n_t) \right\}$$
 (12)

subject to the constraints

$$(1 - \tau)[\psi(k_t) + (1 + r_t)c_t] - d_t - n_t \ge 0 \tag{13}$$

$$n_{t-1} \ge k_t + c_t \tag{14}$$

$$c_t + \theta k_t \ge ak_t \tag{15}$$

$$c_t \ge 0 \tag{16}$$

3.2 Short-run Growth and Resource Reallocation from Cash to Capital

In the first step, we analyze how scaling up the firm's pledgeable share from θ_{low} to θ_{high} affects the static production and financing choices of the firm's decisions given its net worth n_t .

Denote by η_t the shadow price of the budget constraint (13), and $\gamma_t \eta_t (1-\tau)$, $\lambda_t \eta_t (1-\tau)$ and $\zeta_t \eta_t (1-\tau)$ the shadow prices of, respectively, the net worth allocation constraint (14), the working capital constraint (15) and the non-negative cash constraint (16). The shadow prices are normalized by $[\eta_t (1-\tau)]^{-1}$ for convenience. From the first-order conditions of the objective equation (12) concerning capital and cash holdings, we can derive the relationship between the marginal benefit of capital (MBK) and marginal benefit of cash holding (MBC) through the three shadow prices. The full derivation is in Appendix B.1.1. Below we describe the relationship between MBK and MBC.

$$\gamma_t = MBK_t = MBC_t + \zeta_t \tag{17}$$

where the marginal benefit of capital (MBK) and marginal benefit of cash holding (MBC) are

$$MBK_t = \underbrace{\psi'(k_t)}_{ ext{Physical Return of Assets}} + \underbrace{\lambda_t(\theta - a)}_{ ext{Shadow Return of Finance}}$$
 $MBC_t = \underbrace{1 + r_t}_{ ext{Physical Return of Assets}} + \underbrace{\lambda_t}_{ ext{Shadow Return of Finance}}$

with $\psi'(k_t) = Z\alpha k_t^{\alpha-1} - (a+\delta)$. Both capital and cash have a physical return on assets and a shadow return on finance. These physical and shadow returns may differ. First, capital has a large physical return $\psi'(k_t)$ for a sufficiently small firm, while cash has a low physical return. Second, capital has a negative shadow return of finance $(\lambda_t(\theta-a))^9$. Increasing the capital stock increases the demand for labor and, hence, the need for working capital, thus increasing the tightness of the collateral constraint. However, cash provides a positive shadow return of finance $(\lambda_t > 0)$ because increasing cash reduces the need for external working capital funds, thus relaxing the tightness of collateral constraint.

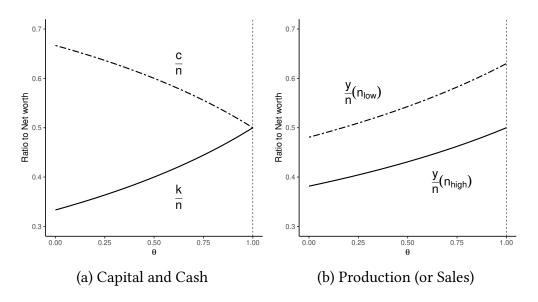
The optimal choice of a constrained firm whose demand for cash is positive ($\zeta_t = 0$), that is, a sufficiently small firm, would be to build cash holdings up to achieve a shadow benefit of relaxing the collateral constraint such that $MBK_t = MBC_t$. This yields an optimal shadow return of finance from cash $\lambda_t^* = \frac{\psi'(k_t) - r_t}{1 + a - \theta}$. This shadow return is proportional to the return of capital $\psi'(k_t)$, which is

⁹Since *a* measures the input share of labor relative to capital, which is usually assumed to be around 2, without loss of generality, $a > \theta$ always holds. As a result, $(\lambda_t(\theta - a)) < 0$ always holds.

higher for smaller firms, as $\psi(\cdot)$ decreases in k, and k is constrained by n. Combining the binding collateral and working capital constraints ($ak_t = c_t + \theta k_t$) and the budget constraint ($c_t + k_t = n_t$), the constrained firm's choices of capital and cash are proportional to net worth:

$$k_t^* = k(\theta, n_t) = \frac{1}{1 + a - \theta} n_t, \quad c_t^* = c(\theta, n_t) = \frac{a - \theta}{1 + a - \theta} n_t.$$
 (18)

Figure 1: Relationship between Optimal Choices and heta



Note: This plot shows the entrepreneur's optimal capital, cash, and production choices as a function of θ . The numerical calibration of the parameters corresponds to an annual frequency: the annual depreciation in the capital is set to $\delta=0.1$, returns to scale are set to $\alpha=2/3$, the labor to capital share is set to a=2, and $n_{low}=1$ and $n_{high}=2$ stand for small and large entrepreneurs.

Using the production function (11) along with the optimal capital and cash equations (18), we can determine how the capital, cash, and output choices are affected by θ , which is summarized in Proposition 1 below. Figure 1 illustrates these properties in Proposition 1 visually.

Proposition 1 Suppose that the economy is described by the special case laid down in Definition 2. LGPs that increase the firm's collateral θ increase the shadow benefit of relaxing the collateral constraint and, therefore,

- (i). increase the firm's optimal choice of capital $\left(\frac{\partial k}{\partial \theta} > 0\right)$.
- (ii). decrease the firm's optimal choice of cash holdings $\left(\frac{\partial c}{\partial \theta} < 0\right)$.
- (iii). increase the firm's optimal sales $\left(\frac{\partial y}{\partial \theta} > 0\right)$.

Proof. (i), (ii), and (iii) are derived directly from Equation (18).

3.3 Long-run Scales of the Firms with Intertemporal Distortions

In the second step, we analyze how increasing the firm's collateral ability from θ_{low} to θ_{high} affects the long-run scale of the firm. We now consider the firm's intertemporal choices and derive the first-order conditions of the firm's objective (12) with respect to dividends, future net worth, and cash. The full derivation is in Appendix B.1.1. The derived Euler equation is as follows:

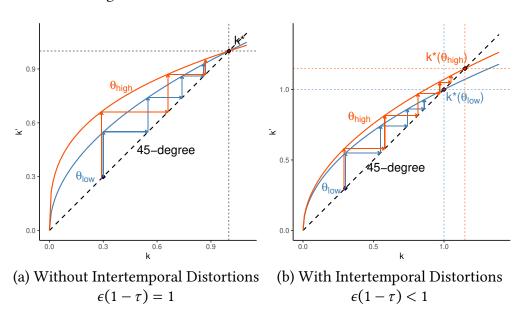
$$1 = \beta \epsilon (1 - \tau) \left(\frac{d_{t+1}}{d_t} \right)^{-\eta} ((1 + r_{t+1}) + \lambda_{t+1})$$
 (19)

where $\epsilon(1-\tau) < 1$ is the total intertemporal distortion resulting from both the exit risk and the net worth erosion and distorts the entrepreneur's net worth accumulation. If the firm survives long enough, the shadow price of the constraint admits a long-term value that we denote by λ^{LT} . It is defined by the Euler equation (19) where $d_t = d_{t+1} = d^{LT}$:

$$\lambda^{LT} = \frac{1}{\beta \epsilon (1 - \tau)} - (1 + r^{LT}) \tag{20}$$

where $\beta(1 + r^{LT}) = 1$ if the economy is in a steady state.

Figure 2: Dynamics of Firm's Long-term Growth



Note: Given the erosion conditions, this plot shows the entrepreneur's growth dynamics. The numerical calibration of the parameters is conventional to an annual model: $\delta=0.1$ stands for annual depreciation in the capital, $\alpha=2/3$ stands for decreasing return to scale, a=2 stands for labor share in production, $n_{low}=1$ and $n_{high}=2$ stand for smaller and larger entrepreneurs.

As a result, the long-term shadow price of cash is positive ($\lambda^{LT}>0$) in the long run only if $\epsilon(1-\tau)<1$, that is, if entrepreneurs face intertemporal distortions. Therefore, a key implication is that the firm's long-run scale is affected by financial constraints only in the presence of intertemporal distortions. Otherwise, the financial constraints are irrelevant ($\lambda^{LT}=0$) in the long run, so financial constraints only affect the speed at which the firm converges to that long-term scale. The following proposition summarizes how the financial constraints affect the firm's long-run scale.

Proposition 2 Suppose that the economy is described by the special case defined in Definition 2.

(i) The financial constraints remain relevant in the long run (i.e., $\lambda^{LT}>0$) if and only if the intertemporal distortions are non-negligible: $\epsilon(1-\tau)<1$. In that case

$$\lambda^{LT} = \frac{1}{\beta} \left(\frac{1}{\epsilon (1 - \tau)} - 1 \right) > 0 \tag{21}$$

(ii) In the long run, the gap between long-term capital k^{LT} and the undistorted capital stock k^{opt} is affected by the long-term shadow value of the financial constraint λ^{LT} following

$$\psi'(k^{LT}) - \psi'(k^*) = (1 + a - \theta)\lambda^{LT} > 0$$
(22)

where λ^{LT} is defined in equation (21), and $\psi'(k^*) = 1/\beta - (1-\delta)$.

Proof. See Appendix B.1.2.

The first point of Proposition 2 restates the above discussion. The second point describes in more detail how the distortion in long-term capital accumulation depends on the interaction between the intertemporal distortions (through λ^{LT}) and the collateral constraint (through θ). The expression (22) shows clearly that the intertemporal distortions and the collateral constraint reinforce their respective impact on capital accumulation in the long run. An increase in θ increases the stock of capital for firms that are below their long-run scale compared to a firm that does not benefit from an increased θ . This increase is temporary without intertemporal distortions as the long-run scale is unchanged. In the presence of intertemporal distortions, a firm that benefits from an increased θ converges to a larger scale.

3.4 Endogenous Selection into the Guarantee Program

In the final step, we analyze how increasing the firm's collateral from θ_{low} to θ_{high} and the participation cost affects the participation of firms in the guarantee program and discuss the potential

aggregate implications.

We still consider the same special case above, except that the participation cost is now strictly positive $\xi > 0$. In this case, we examine which type of firm self-selects into the loan guarantee program. A firm decides to ask for the guarantee only if $\psi(k(\theta_{high}, n_t)) - \psi(k(\theta_{low}, n_t)) > \xi$, which we can approximate as follows:

$$\psi'(k(\theta_{low}, n_t)) \cdot n_t > \frac{\xi}{\Lambda \theta} \tag{23}$$

where we used $k(\theta_{high}, n_t) - k(\theta_{low}, n_t) \simeq n_t \Delta \theta$ with $\Delta \theta \equiv \theta_{high} - \theta_{low}$. Importantly, considering the participation cost ξ and the guarantee increment $\Delta \theta$, essentially two factors decide whether a firm joins the loan guarantee program: marginal productivity $\psi'(\cdot)$ and net worth n_t .

Proposition 3 Suppose that the economy is described by the special case defined in Definition 2, but now the participation cost is positive: $\xi > 0$.

- (i) Given net worth n_t , more productive firms (with high marginal productivity $\psi'(\cdot)$) would be more likely to self-select into the program.
- (ii) Given marginal productivity $\psi'(\cdot)$, firms with a high net worth n_t would be more likely to self-select into the program.
- (iii) Neither very large firms ($\psi'(\cdot) \to 0$) nor very small firms ($n \to 0$) will self-select into the program. The participation rate would be hump-shaped in firm size.

Proof. (i), (ii), and (iii) are derived directly from Equation (23).

The first and second points of Proposition 3 indicates that the self-selection into the guarantee program benefits the aggregate as resources are allocated to firms with a higher growth potential or with a higher total output. The third point shows that the limited guarantee resources are not allocated to firms which cannot afford it or firms which do not need it at all.

However, there is still a group of firms that are inefficiently constrained. These high-potential firms with high $\psi'(\cdot)$ but a low net worth n_t may have low incentives to ask for a guarantee. In that case, the firm is limited in its capacity to increase its scale, which limits the incentives to pay the participation cost ξ . As a result, some small but productive firms may still not ask for a guarantee if the participation cost is high. Lower participation costs ξ or an increase in the guaranteed ratio $\Delta\theta$ could potentially motivate these firms to participate.

3.5 Remarks on the Mechanisms and Predictions

This simple special case suggests that lowering participation costs or increasing the guaranteed ratio could push productive but small firms to participate in the LGPs and achieve a higher scale.

We will test these policy suggestions in the fully parameterized quantitative model in Section 4 below. This simple model also provides three predictions on how LGPs should affect firm static production and financing choices in the short run and in the long run. First, firms with LGPs lower their unproductive cash holdings and increase their productive capital stock. Second, firms with LGPs achieve a persistent increase in their production scale if they face non-negligible intertemporal distortions. Third, the participation rate in the LGPs is hump-shaped over firm size because small firms and firms with lower marginal productivity self-select out of the loan guarantee program. We will confront these predictions to the data in Section 5 below.

4 Quantitative Analysis

We now assess quantitatively how short-term finance shapes firm financing and growth. We parameterize the model to our Moroccan firm-level data and LGP program, using information on guaranteed and non-guaranteed firms. The key parameters that capture financial frictions are set to match some cross-sectional and dynamic patterns observed in the data. We then find that the model can quantitatively account for the observed growth effect of LGPs in Morocco.

4.1 Institutional Background and Data

Our analysis merges loan-level data from Tamwilcom, a Moroccan government institution that provides SME-related loan guarantees, with firm-level data from Orbis.

Collateral Requirements and Loan Guarantees in Morocco Collateral requirements for loans are exceptionally high in Morocco. Approximately 84% of the loans in Morocco require collateral, as reported by World Bank (2013). Most collaterals are asset-based. To reduce potential inefficiency caused by such high collateral requirements, Tamwilcom, as a public financial institution under the supervision of the Central Bank of Morocco, *Bank Al-Maghrib*, cooperates with four leading banks which jointly cover an extensive credit network to provide loan guarantee programs to SMEs.¹⁰ Firms that apply for bank loans at these four leading banks and which do not have insufficient collateral but still eligible for guarantees are transferred to Tamwilcom for further assessment. Once approved, the bank grants credit to qualified borrowers, and Tamwilcom underwrites a share of the loan.

Firms in Morocco are severely financially constrained. They have almost no access to long-

¹⁰Tamwilcom (formerly *Caisse Centrale de Garanties*) has a long history as a credit institution dating back to 1949. Since its reform in 2012, Tamwilcom has focused on SME-related loan guarantees (Tamwilcom, 2013-2018). Our study focuses on the post-reform period from 2012 to 2018.

term formal bank loans (< 1% of total corporate credit) and very limited access to short-term formal bank loans (\approx 20% of total corporate credit). To fulfill their liquidity needs, they rely heavily on non-bank loans (\approx 80% of total corporate credit), such as trade credit. Meanwhile, they also stockpile cash holdings, equivalent to about 42% of total corporate credit and more than 200% of bank credit¹¹. To alleviate such severe financial frictions, the Moroccan government started to provide extensive LGPs for short-term loans to SMEs in 2012. This loan guarantee program is the ideal setup to evaluate the impact of short-term external finance.

Products of the Loan Guarantee Program Among the range of products Tamwilcom offers, we focus on two main products catering to the firm's working capital needs: Damane Exploitation and Damane Express. Damane Exploitation targets medium-sized firms requesting a short-term loan of up to 18 months. Access to Damane Exploitation is subject to a firm size threshold, but this size threshold does not appear to be binding in the data. The loan size varies substantially, ranging from 180 million dirhams to as small as 1 million dirhams. Tamwilcom guarantees 60% of the loan and requires a commission fee of 0.5% of the loan amount. Damane Express is a product that targets working capital loans and is designed explicitly for small firms. It deals with loans below 1 million dirhams and provides a guarantee coverage of up to 70%. The commission fee is 0.5% for loans up to 12 months and 1.5% for those beyond 12 months.

Since both programs are designed to alleviate credit constraints of firms ranging from small to medium and jointly cover almost all SMEs in Morocco, we will pool both programs together as one in our analysis. In practice, firms self-select into different programs based on the size of their liquidity needs, which is implied by the smooth sales distribution for firms guaranteed under both products, as shown in Figure 3 in Appendix A.3.

Tamwilcom Loan-level Data The Tamwilcom loan-level database is a unique confidential database. It covers loans guaranteed by Tamwilcom through the short-term loan guarantee programs and provides information on 43,195 loans associated with 23,017 firms guaranteed by Tamwilcom from 2009 to 2019. The database includes firm identifiers (name, national ID, address, creation date) and loan characteristics (loan approval date, maturity, loan amount, guarantee amount, commission, and maturity). The total number of guaranteed loans amounts to 87 billion dirhams, which constitutes about 3.2% of the total short-term loans to SMEs in Morocco.¹⁴

Orbis Firm-level Data The Orbis firm-level database is a commercial database by Bureau van Dijk (BvD) that is widely used in economics research (Kalemli-Ozcan et al., 2015). For Morocco,

¹¹All calculations are based on firm-level data in Orbis.

 $^{^{12}}$ The size threshold is 175 million dirhams (\approx 18 million US dollars). Approximately 92% of firms in the program have sales of less than 100 million dirhams. Damane Exploitation was renamed Damane Atassyir in 2019.

¹³Damane Express is also associated with a much-simplified process and a fast approval period of 48 hours.

¹⁴We exclude canceled guarantees and only consider the first guarantee in case of renewal.

BvD collects firm-level balance sheet data from Morocco's business register, the Office of Industrial and Commercial Property (OMPIC), and standardizes it to its global format. OMPIC maintains the central trade register of all firms under the supervision of the Moroccan government. It is the most comprehensive source of firm data in Morocco. Consequently, the data's coverage and quality of Orbis are well-suited for our analysis. Orbis covers firms throughout the period of our loan-level data from Tamwilcom.

We pair the Tamwilcom guarantee dataset with the Orbis balance sheet dataset to construct our final data sample. Details for the pairing procedure are in Appendix A.1. The targeted moments are computed using the sample of guaranteed and non-guaranteed firms.

4.2 Quantitative Specifications

We specify the model's functional forms in the quantitative analysis. First, we assume that the production function is the conventional Cobb-Douglas form:

$$F(k,l) = k^{\alpha}l^{\nu}, \quad \alpha + \nu < 1$$

Second, we follow Gopinath et al. (2017) to model the size-dependent collateral constraint:

$$b_{i,t} \le \bar{b_{i,t}} \equiv \Theta(k_{i,t}) = \theta_0 k_{i,t} + \theta_1 \Psi(k_{i,t}) = \left[\theta_0 + \theta_1 \frac{\Psi(k_{i,t})}{k_{i,t}}\right] k_{i,t}$$
(24)

where $\Psi(k) = exp(\gamma k) - 1$ is an increasing and convex function of capital and θ_0 and θ_1 are parameters characterizing the borrowing constraint. In this micro-foundation, the $\Psi(\cdot)$ function denotes an increasing and convex cost firms incur from disrupting their productive capacity. In contrast to Gopinath et al. (2017), we introduce the elasticity γ to change the convexity of the size-dependent component of the collateral constraint to provide additional freedom to match the moments in the Moroccan firm-level data.

4.3 Parameterization

We group parameters into two categories. The first category includes preference and technology parameters that are difficult to identify using our data. We fix these parameters using values that are standard in existing work. The second category includes parameters that determine the process for productivity, financial frictions, and LGPs. We pin down these parameters by requiring that the model fits the salient features of the Moroccan data.

Fixed Parameters Table 1 lists the parameters that are calibrated from the literature. The

Table 1: FIXED PARAMETERS

Parameter	Description	Value
Firms		
α	Capital coefficient	0.21
ν	Labor coefficient	0.64
δ	Capital depreciation	0.10
ϕ	Capital adjustment cost	4.0
Households		
β	Discount factor	0.96
η	Elasticity of intertemporal substitution	1
θ	Leisure preference	2
ω	Inverse Frisch	0.5

Table 2: FITTED PARAMETERS

Parameter	Description	Value
Output Dynamics		
$ ho_z$	Persistence of TFP shock	0.90
σ_z	Volatility of TFP shock	0.06
\underline{n}_0	Net worth of entrants	0.08
ϵ	Survival rate	0.91
au	Net worth erosion	0.02
Financial Frictions		
s	Share of formal bank loans	0.20
$ heta_{ m o}$	Collateral constraint (size-irrelevant)	0.01
$ heta_1$	Collateral constraint (size-dependent)	0.26
γ	Collateral constraint (size-dependent)	1.35
Loan guarantee program	_	
μ	Guaranteed loan commission fee	0.005
χ	Multiplier of LGP on loans	2.5
$rac{\chi}{ar{\xi}}$	Upper bound of LGP fixed cost	0.35

frequency of the model is a year, so we set the discount factor $\beta=0.96$ to match an annual interest rate of 4%. We assume log utility, which implies a unit elasticity of intertemporal substitution ($\eta=1$). We set the Frisch elasticity of labor supply to 2, within the range of macro elasticities identified by Chetty et al. (2011), which implies an inverse Frisch $\omega=0.5$. We then set leisure preference $\theta=2$ to match the fact that households spend a third of their time working. On the firm side, we set the capital coefficient $\alpha=0.21$ and the labor coefficient $\nu=0.64$ to match a labor share of two-thirds and return to scale of 85%. Capital depreciates at a rate of $\delta=0.10$ annually, and the capital adjustment cost is set to $\phi=4.0$, which generates an average aggregate nonresidential fixed investment rate as in Bachmann, Caballero, and Engel (2013).

Fitted Parameters The second category of parameters, listed in Table 2, are jointly pinned down by the requirement that the model accounts for the firm-level facts in Morocco to match

Table 3: Target Moments

Moments	Data	Model
Output Dynamics		
1-year autocorrelation of output	0.89	0.89
3-year autocorrelation of output	0.69	0.71
5-year autocorrelation of output	0.53	0.56
Size ratio of entrant relative to average	17%	16.4%
Annual exit rate of firms	9.0%	9.0%
Financial Frictions		
Mean debt/asset ratio (non-guaranteed)	51%	39%
Mean debt/asset ratio (guaranteed)	64%	64%
Mean cash/asset ratio (non-guaranteed)	22%	21%
Mean cash/asset ratio (guaranteed)	9%	6%
Guaranteed loan/current liability ratio	22%	22%
Loan guarantee program		
Guaranteed loan commission fee	0.5%	0.5%
Percentage of loan guaranteed	60%	60%
Percentage of firms participating LGP	3.4%	3.4%

Note: This table reports the moments from both the Orbis firm-level database and the Tamwilcom loan-level database. Moments of *productivity* and *entry/exit* are from all the Moroccan firms in the Orbis firm-level database. The output level of a firm is measured by its sales. The size ratio of the entrant relative to the average is calculated using total assets. The exit rate is calculated for Moroccan firms from 2006 to 2017. Moments of *financial frictions* are calculated from both the sample of the Orbis firm-level database and the sample of the Tamwilcom guarantee-level database. The debt/asset ratio only includes current liability because, for SMEs in Morocco, the long-term debt is less than 1% of their total credit.

the moments in Table 3. First, the four parameters related to output dynamics: persistence of TFP shock ρ_z , volatility of TFP shock σ_z , the net worth of entrants \underline{n}_0 , and survival rate ϵ jointly match the three moments of productivity persistence, the relative size ratio of entrants to an average firm, and the annual exit rate of firms in the data. Second, the loan guarantee parameters: commission fee μ , multiplier of LGP on loans χ , and share of guaranteed loans s explicitly match the three corresponding moments of the commission fee, percentage of loan guaranteed, and guaranteed loan to current liability ratio in the data.

Then, we parameterize the other three financial friction parameters: the size-irrelevant collateral parameter θ_0 , the size-dependent collateral parameter θ_1 , and the net worth erosion parameter τ to jointly match the five moments of LGP participating rate, cash asset ratios, and debt asset ratios. The collateral constraint parameters and net worth erosion then jointly pin down the cash asset ratios and debt asset ratios of both the guaranteed and non-guaranteed firms. These four moments reflect that guaranteed firms have, on average, a 13 percentage point lower cash ratio and a 13 percentage point higher debt ratio.

The fitted exit rate $(1 - \epsilon)$ and net worth erosion τ yield a high intertemporal distortion $(1 - \epsilon) + \tau = 0.11$. Note that the exit rate $(1 - \epsilon)$ is probably overestimated, as part of the firms that exit the dataset, in fact, fail to update their registration in the trade registry. However, as the average cash and debt ratios are determined mostly by the saving behavior of firms, the total level of intertemporal distortions is strongly disciplined by these variables. Therefore, the overestimation of the exit rate is compensated by the underestimation of the net worth erosion.¹⁵

Finally, the upper bound of the LGP participation cost $\bar{\xi}$ mostly uniquely pins down the percentage of firms participating in LGP of 3.8%. The value of that upper bound implies an average cost of 0.175. This represents one-third of the average net worth. This number is large, implying that the barriers to participation remain important so that only large constrained firms or small lucky firms would have the chance to self-select into the program. This large number reflects an imperfect penetration of the guarantee program among small firms due to geographical barriers or the fact that many small firms do not have a relationship with the banking system. In 2023, many firms still did not have checking or deposit accounts (27% against 11% in the rest of the world, according to the World Bank Enterprise Survey) and did not interact with the banking system, which could increase the informational barriers. Many firms also cannot provide reliable financial information (only 24% of firms produce an annual financial statement reviewed by external auditors, compared to 46% in the rest of the world, according to the same source), which prevents them from submitting relevant information to banks. Administrative and cognitive costs related to the application procedure are also far from negligible. As an illustration, after 2018, when the guarantee allocation procedure was automated, the number of applications increased dramatically. Policies that lower the fixed cost by simplifying the application procedure, advertising the LGP, or diversifying the application channels are, therefore, one potential important margin to expand guarantee programs, which we discuss in the policy section.

4.4 Model Implications

With the calibrated model, we show how the loan guarantee program affects the firm's static choice between capital and cash, the participation rate in the loan guarantee program, and the firm's long-term scale. We find that the quantitative model reproduces the mechanisms from the special case in Section 3.

Short-term Growth and Resource Reallocation We first show the effects of short-term finance on the reallocation of resources from cash to capital. Figure 3 plots the optimal capital,

 $^{^{15}}$ We later check that our parametrization is consistent with the estimated long-term effect of the guarantees. Besides, as we show below, a higher exit rate reduces the aggregate impact of the guarantee for a given total intertemporal distortion. Fitting ϵ in this way thus generates conservative parameters.

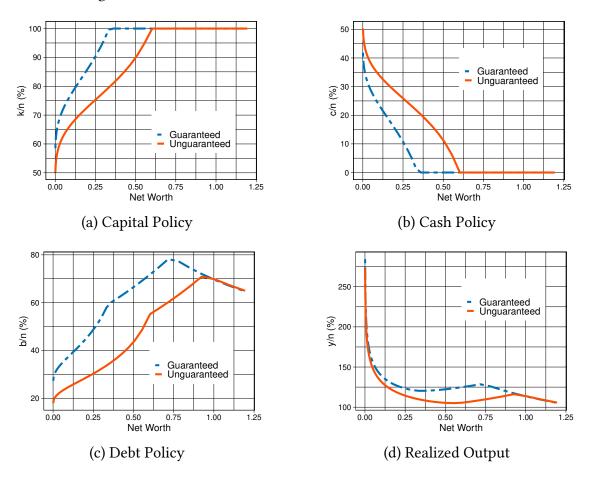


Figure 3: Reallocation of Resources from Cash to Capital

Notes: This figure shows the capital, cash, debt, and output policies as a function of net worth for firms with median productivity. The blue line stands for guaranteed firms, and the red line stands for unguaranteed firms. Net worth is truncated at 1.25 because the measure of firms larger than 1.25 is tiny, and the decision rules are monotone in net worth beyond 1.25.

cash, and debt policies and the realized output of guaranteed and unguaranteed firms. First, we compare the optimal policies among the dimension of net worth, focusing on unguaranteed firms. Due to their limited access to short-term external finance, smaller firms borrow less, hoard more cash, and accumulate less capital. When firms grow, their short-term financial constraints are relaxed, so they start borrowing more and lowering their cash holdings. Finally, if firms grow further, they become unconstrained.

Second, in Figure 3, we compare the policies and realized output of guaranteed firms versus unguaranteed firms. Generally, guaranteed firms with access to the guarantee accumulate more productive capital, lower their unproductive cash holdings, borrow more external debt, and produce more output per net worth. The changes are most significant for median-sized firms. The

policies converge when firms become large and unconstrained. These effects on the reallocation of resources from cash to capital and its consequences are consistent with our empirical findings in Section 5.1 and our analytical findings in Section 3.2.

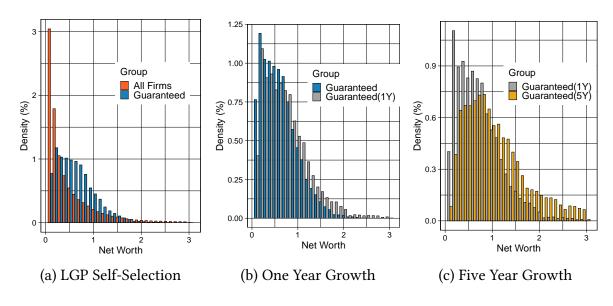


Figure 4: Distribution of Firm Long-term Scale

Notes: This figure shows the net worth distributions of all firms, of guaranteed firms upon their self-selection into the loan guarantee program, of guaranteed firms after one-year growth without exiting, and of guaranteed firms after five years, conditional on not exiting. It helps to distinguish the selection effect and growth effect. The mean net worth of the distributions are 0.51, 0.72, 0.85, and 1.27, respectively.

Firms Long-Term Scale We then show the effects of short-term finance on the long-term scale of firms. Figure 4 plots the distributions of all firms and guaranteed firms alone. More specifically, the distribution of guaranteed firms is shown in three stages. The first stage is the distribution of firms that self-select into the loan guarantee program before accessing the additional credit line. Given the random fixed participation cost, medium firms are more likely to be able to pay the fixed cost and enter the program, which is consistent with our data in Section 5.1. The difference between the distributions of *Guaranteed* and *All Firms* shows the selection effect of the loan guarantee program.

The second stage is the distribution of these guaranteed firms in the first stage after one year of growth without exiting. The additional credit line from the loan guarantee program helps them accumulate more net worth, so the distribution shifts to the right. Finally, we show the third stage, the distribution of the guaranteed firms after five years of guarantee without exiting. These firms grow significantly larger with a distribution shifting to the right. These effects on the long-term scale of firms are consistent with our empirical findings in Section 5.1 and our

analytical findings in Section 3.3.

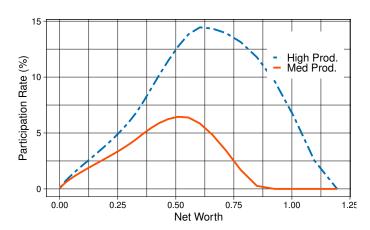


Figure 5: Participation In the Guarantee Program

Notes: This figure shows the proportion of firms participating in the LGP as a function of net worth for two different productivity levels. The blue line stands for the higher-productivity firms, and the red line stands for the lower-productivity firms (in this plot, the median productivity). Net worth is truncated at 1.25 because the measure of firms above 1.25 is tiny, and the decision rules are monotone beyond 1.25.

Participation In the Guarantee Program Figure 5 shows the participation probability for firms with two different productivity levels as a function of net worth. First, the participation rate is hump-shaped over the net worth dimension. The smallest firms hardly participate in the LGP programs since they can hardly support the fixed cost of participation, while the largest firms also hardly participate because they are much less financially constrained. As a result, the median-sized firms are the most engaged in the LGP. Second, high-productivity firms have a higher participation rate than low-productivity peers with the same net worth since these firms gain more from participating in the LGP and are more able to pay for the participation costs with their higher profits. These effects on the participation rate in the LGP are consistent with our empirical findings in Section 5.2 and our analytical findings in Section 3.4.

5 Model Validation with Firm-level Data

In this section, we empirically validate the findings illustrated in our quantitative model using Moroccan firm-level data. Specifically, we document empirical evidence on a guaranteed firm's enlarged production scale and reduced cash holdings.

Our empirical strategy combines nearest-neighbor matching with a difference-in-difference (DID) approach. The matching procedure is to find statistical twins for a guaranteed firm based

on a series of time-varying and observable variables. Details on the matching procedure are in Appendix A.1 and the summary statistics of the firm-level data are in Appendix A.3. The DID method controls for unobservable group-specific time effects, where the "group" refers to the guaranteed firm and its matched unguaranteed firms.

It is important to note that we do not interpret these results as causal evidence. Because we cannot fully control for time-varying unobservable drivers of selection into the program (like the firm productivity), the differences in outcome variables between guaranteed and matched firms cannot be fully interpreted as causal evidence. Our results are instead compared with the model, which accounts for selection since only firms that are productive enough enter the program (see Proposition 3). This will constitute our model validation.

5.1 Estimation Results on Short-term Growth and Long-Term Scale

We first try to validate the short-term growth and resource reallocation, as shown in Figure 3 and firms' long-term scale, as shown in Figure 4 through regressions. Our regression follows Brown and Earle (2017)'s matched DID setup:

$$\Delta Y_{igs} = \delta D_{it} + \lambda_{gs} + \epsilon_{igs}, \tag{25}$$

where i indexes the firm, g is the group (the guaranteed firm and its matched unguaranteed firms), t is the guarantee year, and s = t + 1, t + 2, t + 3 refers to three post-guarantee years. The dependent variable ΔY_{igs} is the change in the selected outcome variable in the post-guarantee period compared to the year before obtaining the guarantee. It has the form $\Delta Y_{igs} = Y_{igs} - Y_{igt-1}$, where year t-1 is considered as the base year and s = t+1, t+2, t+3 refers to three post-guarantee years. We cannot estimate t+5 as in the model due to short data length. All Y variables are in logs so that the dependent variable can be read as a growth rate. D_{it} is a dummy variable indicating whether firm i has been granted a guarantee in year t. λ_{gs} are the group-year fixed effects, which control for the group-specific trend. We also include city-year fixed effects to control local credit demand and financial conditions. Standard errors are clustered at the city level.

We first examine whether the guarantee is associated with an expansion in production scale, measured in sales growth, total asset growth, cost of employee growth, and fixed asset growth. Columns (1) to (3) of Table 4 report the estimation results for sales growth. Firm sales growth

¹⁶Firm-level fixed effects are not included since our dependent variable has differenced out any individual fixed effects relevant to the outcome. We do not include fixed effects for sector, year, and size because we use group fixed effects. A group consists of one guaranteed firm and five matched unguaranteed firms from the same sector, year, and size category. Therefore, the group fixed effects account for fixed effects across these three dimensions. Further details are provided in in Appendix A.1.

under a Tamwilcom guarantee increases by 13.5% in the first year, compared to the pre-guarantee period, relative to non-guaranteed firms. The impact is close to 12.5% in the third year after obtaining the guaranteed loan. This large and significant effect on sales indicates that the guarantee goes together with a firm's expansion in production. Columns (4) to (6) of Table 4 report the significant and positive association of the guarantee with total asset growth. This shows that the firm simultaneously increases its net worth. All in all, access to the loan guarantee coincides with a persistent increase in firm scale.

Table 4: Effects on Firm Sales and Total Assets

	Sa	ales Grow	th	Total Asset Growth		
	(1) t+1	(2) t+2	(3) t+3	(4) t+1	(5) t+2	(6) t+3
Guaranteed	0.135***	0.101***	0.125***	0.092***	0.092***	0.166***
	(0.010)	(0.021)	(0.020)	(0.011)	(0.021)	(0.014)
N	18503	10610	5585	18959	11018	5952
adj. R^2	0.332	0.315	0.357	0.299	0.264	0.268
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of ("Guaranteed") treatment from the DID regression (25). Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variable "Sales Growth" is the log difference between sales in year t+1, t+2 or t+3, and sales in year t-1. The dependent variable "Total Assets Growth" is the log difference between total assets in year t+1, t+2 or t+3, and total assets in year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the city level. Significance level: t+10.10, t+11, t+12, t+13, t+13, and total assets in year t+13, t+14, t+15, t+15, t+15, and total assets in year t+15, t+15, t+15, and total assets in year t+15, and total assets in year t+15, and total assets in year t+16, and the year t+16,

We then examine how guaranteed firms change their production inputs in Table 5. We use the variable "cost of employee growth" to detect changes in a firm's hiring since we do not have good coverage for the number of employees in the Orbis database. As Table 5 shows, labor costs increase by 11.5% in the year following the granting of a guarantee relative to non-guaranteed firms and remain 10.6% and 10.5% higher in the two following years. Along with the increase in the wage bill, guaranteed firms also experience increases in fixed tangible assets after the treatment, according to Table 5. This variable is a good proxy for investment in productive assets (Amamou, Gereben, and Wolski, 2020). It shows that guaranteed firms allocate more resources to long-term productive assets, consistent with an expansion in productive capacities.

We then explore changes in the firm's balance sheet, including current liabilities and cash, summarized in Table 6. There is a persistent 12-17% increase in current liabilities in guaranteed firms relative to control firms. This arises naturally from the buildup of current liabilities from newly granted working capital loans. Conversely, we observe stagnation and decline (though

Table 5: Effects on Firm Production Inputs

	Cost of	Employee	Growth	Fixed Asset Growth			
	(1) t+1	(2) t+2	(3) t+3	(4) t+1	(5) t+2	(6) t+3	
Guaranteed	0.115***	0.106***	0.105***	0.116**	0.230***	0.241**	
	(0.015)	(0.023)	(0.025)	(0.037)	(0.062)	(0.079)	
N	17852	10422	5416	18344	10624	5760	
adj. R^2	0.252	0.223	0.239	0.183	0.174	0.236	
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes	
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes	

Note: This table reports the coefficients of ("Guaranteed") treatment from the DID regression (25). Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variable "Cost of Employee Growth" is the log difference between labor costs in year t+1, t+2 or t+3, and labor costs in year t-1. The dependent variable "Fixed Asset Growth" is the log difference between fixed tangible assets in year t+1, t+2 or t+3, and fixed tangible assets in year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t-1. Group-year and city-year fixed effects are included. Standard errors are clustered at the city level. Significance level: t+10 or t+11, t+12 or t+13, and t+14 or t+15. Significance level: t+15 or t+15

Table 6: Effects on Firm Balance Sheet

	Curren	t Liability	Growth	Cash Growth		
	(1) t+1	(2) t+2	(3) t+3	(4) t+1	(5) t+2	(6) t+3
Guaranteed	0.131***	0.122***	0.167***	-0.061	-0.210***	0.088
	(0.014)	(0.015)	(0.025)	(0.069)	(0.054)	(0.070)
N	19299	11171	5969	18761	10683	5814
adj. R^2	0.252	0.276	0.243	0.321	0.304	0.291
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of ("Guaranteed") treatment from the DID regression (25). Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variable "Current Liability Growth" is the log difference between current liabilities in year t+1, t+2 or t+3, and current liabilities in year t-1. The dependent variable, "Cash Growth," is the log difference between cash and cash equivalents in years t+1, t+2 or t+3, and cash and cash equivalents in years t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the city level. Significance level: t+10 of t+11 of t+12 or t+13 or t+13 or t+14 or t+15 or t+1

only significant for the period t+2) in cash for guaranteed firms. The decrease in cash holdings is significantly negative in t+2 and not significant in the other two years. Combined with the guaranteed firms' sharp increase in total assets documented in Table 4, this result implies that cash holdings decrease relative to the production scale. To further validate our mechanism, we test for cash ratio changes in Table 7. The results are consistent with our predictions.

Table 7: Effects on Firm Cash Ratio

	Cash Ratio Growth					
	(1) t+1 (2) t+2 (3) t+3					
Guaranteed	-0.004^{+}	-0.010*	-0.008*			
	(0.002)	(0.004)	(0.004)			
\overline{N}	18766	10716	5818			
adj. R^2	0.215	0.161	0.126			
Group × Year FE	Yes	Yes	Yes			
City × Year FE	Yes	Yes	Yes			

Note: This table reports the coefficients of ("Guaranteed") treatment from the DID regression (25). Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variable, "Cash Ratio Growth," is the difference between cash ratio in years t+1, t+2 or t+3, and cash and cash ratio in years t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the city level. Significance level: t0 on t0, t0 on t0, t0 on t0. t0 on t0. t0 on t0. t0 on t0. t0 on t0 on t0. t0 on t0. t0 on t0

Robustness Checks We also perform a series of robustness checks, which are reported in Appendix A.5. We check for (1) changing the number of pre-treatment years in matching, (2) correcting the data attrition bias, (3) emphasizing cash in matching, and (4) including propensity score in Mahalanobis distance. The estimation results remain mostly unchanged.

5.2 Participation in the Loan Guarantee Program

We finally examine the propensity of firms to participate in the loan guarantee program. Figure 6 represents the percentage of Orbis firms that have been identified as benefiting from a guarantee, which proxies for the participation rate. The participation rate is hump-shaped, as both small and very large companies have a low rate compared to medium and large firms. This hump-shaped distribution is maintained when looking at the participation rate by total asset quantile bins. More details are in Appendix A.4.

It is important to note that these results are biased by the size-dependent probability of Tamwilcom firms being paired with Orbis firms, as this probability increases in firm size. In particular, the probability of a small firm being paired may be underestimated. However, the probability of a small firm being paired is 1.7 times lower than that of a medium firm (30% versus 52%). This cannot explain the strong difference in the estimated participation rate. Moreover, this concern is valid only if we have a lot of false negatives in our dataset, that is, if many firms identified as not having a guarantee do, in fact, have a guarantee. While this risk cannot be ruled

out altogether, it is minimized by our thorough pairing procedure described in Appendix A.1. In fact, the most likely reason for a failed pairing is that a guaranteed firm is not in the Orbis dataset. In that case, the participation rates by firm size will not be significantly underestimated.

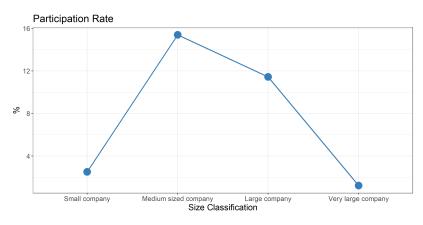


Figure 6: Participation Rate by Size

Notes: This figure shows the participation rate of our Orbis firm sample in Morocco by size. The size classification defines very large companies as those with an operating revenue larger than 100 million euros, total assets larger than 200 million euros, and more than 1000 employees. Large companies have an operating revenue larger than 10 million euros, total assets larger than 20 million euros, and more than 150 employees. Medium-sized companies have an operating revenue larger than 1 million euros, total assets larger than 2 million euros, and more than 15 employees. All the remaining companies are defined as small. The participation rate is calculated as the ratio of guaranteed firms to the total number of firms existing in Orbis.

5.3 Quantitative Model Validation with Regressions

Our empirical estimates from Tables 4 to 7 cannot be interpreted causally because unobservable time-dependent variables, like productivity, may drive selection. We, however, can use these estimates as "untargeted moments" to validate our model. To do so, we simulate a panel of five million firm-year observations and conduct the same empirical procedure of nearest neighbor matching and DID. We refer to these results as "Matched-DID". We also show how "Naive OLS" regressions would overestimate the effects of short-term loan guarantees since relatively larger and higher growth SME firms are more likely to self-select into loan guarantee programs.

We show the results in Table 8. In the table, "Matched-DID (Data)" is taken from our empirical analysis above, and "Matched-DID (Model)" is obtained by applying exactly the same method to our model-simulated data. "Naive OLS (Model)" runs the following OLS regression: $\Delta Y_{is} = \delta D_{it} + \gamma_z' Z_{is-1} + \gamma_i + \gamma_s + \epsilon_{is}$, where i is the firm, t is the guarantee year, and s is the year ahead of the guarantee year. The dependent variable ΔY_{it} is the same as in the Matched-DiD. Similarly, D_{it}

Table 8: QUANTITATIVE MODEL VALIDATION WITH EMPIRICAL ANALYSIS

Effects of	Mate	ched-DID (l	Data)	Matc	hed-DID (N	lodel)	Nai	ve OLS (Mo	del)
Credit Guarantee	t+1	t+2	t+3	t+1	t+2	t+3	t+1	t+2	t+3
$\Delta log(Sales)$	0.135***	0.101***	0.125***	0.187***	0.163***	0.150***	0.524***	0.511***	0.461***
	(0.010)	(0.021)	(0.020)	(0.013)	(0.016)	(0.018)	(0.007)	(0.010)	(0.012)
$\Delta log(TotalAsset)$	0.092***	0.092***	0.166***	0.143***	0.147***	0.139***	0.257***	0.238***	0.215***
	(0.011)	(0.021)	(0.014)	(0.010)	(0.013)	(0.014)	(0.006)	(0.008)	(0.009)
$\Delta log(CurrentLiability)$	0.131***	0.122***	0.167***	0.191***	0.196***	0.187***	0.391***	0.371***	0.341***
	(0.014)	(0.015)	(0.025)	(0.012)	(0.016)	(0.019)	(0.008)	(0.011)	(0.013)
$\Delta log(Cash)$	-0.061	-0.210***	0.088	-0.451***	-0.445***	-0.632***	-1.772***	-1.787***	-1.545***
	(0.069)	(0.054)	(0.070)	(0.051)	(0.063)	(0.077)	(0.049)	(0.061)	(0.065)

Note: "Matched-DID (Data)" is taken from our empirical analysis above, and "Matched-DID (Model)" is obtained by applying exactly the same method to our model simulated data. "Naive OLS (Model)" runs the following OLS regression: $\Delta Y_{is} = \delta D_{it} + \gamma_z' Z_{is-1} + \gamma_i + \gamma_s + \epsilon_{is}$, where i is the firm, t is the guarantee year, and s is the year ahead of the guarantee year. The dependent variable ΔY_{it} is the same as in the Matched-DiD. Similarly, D_{it} is a dummy variable indicating whether firm i has been granted a guarantee in year t, and $gamma_j$ and γ_t are the firm and year fixed effects, respectively. Z_{js-1} is the group of control variables that are used in the matching process for the regression (25). Significance level: p < 0.10, p < 0.05, p < 0.01, p

is a dummy variable indicating whether firm i has been granted a guarantee in year t, and γ_j and γ_t are the firm and year fixed effects, respectively. Z_{js-1} is the group of control variables that are used in the matching process for the regression (25).

Our model matches the empirical analysis results well both in the magnitude and significance levels for sales, total assets, and current liabilities. Although the model over-predicts the effects on cash growth relative to our empirical findings, the directions are mainly consistent. In contrast, the effects of credit guarantee are highly overestimated in the naive OLS regression.

6 Policy Counterfactuals and Aggregate Implications

We finally conduct two groups of policy counterfactuals to demonstrate the aggregate implications of liquidity constraints. More specifically, we show how expanding the short-term loan guarantee program could further reduce liquidity constraints and promote firm growth in Morocco. The loan guarantee program can be expanded mainly along two dimensions, as our analysis suggested in Section 3.4: the fixed participation cost and the guaranteed ratio. We show below in this Section how much firm growth we can achieve by further relaxing these restrictions in four counterfactuals. We focus on both the aggregate output expansion and the coverage and "inclusiveness" of the loan guarantee program.

6.1 Policy Counterfactuals

We show four counterfactuals with realistic alternative participation costs and guaranteed ratios that stand for LGP expansions.

Participation Cost Reduction (PCR) First, in the original benchmark, the upper bound of the participation cost ($\bar{\xi}_{bm} = 0.35$) gives us a participation rate of 3.4%. More importantly, the fixed cost is an overhead cost that is relatively expensive for smaller entrepreneurs, as our analytical analysis suggested in Section 3.4. We explore two counterfactuals below ($PCR \downarrow_{by\frac{1}{3}}$ and $PCR \downarrow_{by\frac{2}{3}}$), where we cut the upper bound of the participation cost to two-thirds ($\bar{\xi}_{PCR} \downarrow_{by\frac{1}{3}} = 0.233$) and to one-third ($\bar{\xi}_{PCR} \downarrow_{by\frac{1}{3}} = 0.117$). These could be understood in the real world as the government requiring fewer financial documents, simplifying the evaluation procedures, directly assisting the application, and subsidizing applications to the LGP.

Guaranteed Ratio Increment (GRI) Second, in the original benchmark, the guaranteed ratio is 60%, which gives a bank loan multiplier of $\chi_{bm} = \frac{100\%}{100\%-60\%} = 2.5$. This is lower than guaranteed ratios in many other countries. For instance, in Kazakhstan, it is equal to 70%; in India, it is equal to 75%; in Indonesia and Japan, it is equal to 80% according to Yoshino and Taghizadeh-Hesary (2019). We explore two counterfactuals below ($GRI\uparrow_{by\,10\%}$ and $GRI\uparrow_{by\,20\%}$), where the guaranteed ratio goes up to 70% and 80%. Correspondingly, the new multipliers are $\chi_{GRI\uparrow_{by\,10\%}} = \frac{100\%}{100\%-70\%} = 3.33$ and $\chi_{GRI\uparrow_{by\,20\%}} = \frac{100\%}{100\%-80\%} = 5.00$. Participating firms have thus more relaxed financial constraints. Moreover, the increased guaranteed ratio could potentially incentivize more firms to participate.

6.2 Firm-level and Aggregate Implications

Implications for Firm Decisions Figure 7 shows the effects of LGP expansions on firm decisions. We mainly focus on how the expansions of LGP affect the choices of capital, cash, output, and participation in the LGP as a function of firm size. First, regarding capital and cash choices, the PCR has no effect conditional on participation. In contrast, the GRI would benefit smaller guaranteed firms more, as shown in plot (a). Second, the same patterns also hold in terms of output, as shown in plot (b).

Third, both types of policies affect the participation rate. Plot (c) shows the changes in the participation rate of the PCR. Lowering the fixed participation cost would increase the participation rate across all firm sizes. Median-sized firms benefit the most and increase their participation even more. Plot (d), on the other hand, shows the changes in participation rate following a GRI. Since an increased guaranteed ratio changes the capital policy and the output, which benefits the smaller firms more, the participation rate increments are skewed towards smaller firms. These

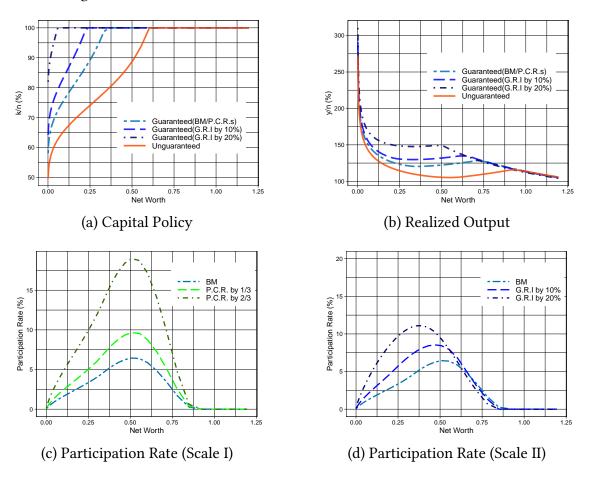


Figure 7: Effects on Firm Financing, Output, and Participation

Notes: This figure shows the capital and output policy, as well as the participation rate, as a function of net worth for firms with the median productivity level. In plot (a) of the capital policy, the k/n ratio will essentially decrease as the net worth grows over a certain scale. However, we do not show these patterns since we focus on small and median-sized firms.

distributional results show that although all counterfactuals benefit firm financing in general, the effects are quite different across firms of different sizes.

Aggregate Implications Table 9 shows the effects of LGP expansions on aggregate financing, economic growth, and welfare. All four counterfactuals improve aggregate TFP, output, and consumption. Participation cost reductions significantly change firm financing patterns. The participation rate increases from 3.4% to 5.1% and 10.1%, and the ratio of guaranteed credit in the economy increases from 1.3% to 2.0% and 3.8%, respectively. The fixed participation cost changes do not substantially affect the guaranteed firm cash and debt ratios. However, more firms are guaranteed, so the average credit ratio increases, and the average cash ratio decreases. Given that most firms that benefit from these policies are small and medium firms, the changes in ag-

Table 9: Aggregate Implication of LGP Expansion

Model Outcomes (%)	Benchmark	$PCR\downarrow_{by\frac{1}{3}}$	$PCR\downarrow_{by\frac{2}{3}}$	GRI↑ _{by 10%}	GRI↑ _{by 20%}
Penal A: Firm Financing					
LGP participation rate	3.4	5.1	10.1	5.0	7.6
Guaranteed credit/total credit	1.3	2.0	3.8	3.1	8.0
Mean cash/asset ratio (guaranteed)	6.0	6.0	6.0	2.9	0.1
Mean cash/asset ratio (all firms)	20.0	19.8	19.3	19.6	18.8
Mean debt/asset ratio (guaranteed)	64.3	64.2	64.0	72.1	85.8
Mean debt/asset ratio (all firms)	40.0	40.3	41.3	40.8	42.7
Penal B: Aggregate Outcomes					
Δ Total Credit	n.a.	0.28	1.25	0.60	1.63
Δ Aggregate TFP	n.a.	0.04	0.14	0.08	0.25
Δ Total Output	n.a.	0.01	0.10	0.05	0.09
Δ Total Consumption	n.a.	0.06	0.29	0.15	0.47
Δ Welfare	n.a.	0.04	0.15	0.08	0.25

Note: This table reports the counterfactual results. The results are reported in two groups: (1) firm financing, which shows how the counterfactual changes the financing patterns of firms in the model, and (2) economic outcomes, which show how the counterfactual changes the aggregate economic conditions. The Benchmark stands for our benchmark calibration of both the fixed participation cost and the guaranteed ratio ($\xi_{bm} = 0.26$, $\chi_{bm} = 2.5$). Each of the four counterfactuals changes only one parameter, reflecting participation cost reduction or guaranteed ratio increment.

gregate outcomes are not substantial at first glance. Nonetheless, we find that reducing the fixed participation cost increases aggregate TFP, total output, consumption, and welfare. Considering the small changes in total credit, the gains are substantial.

Increasing the guaranteed ratio also significantly changes firm financing patterns. The participation rate increases from 3.4% to 5.0% and 7.6%, and the ratio of guaranteed credit in the economy increases from 1.3% to 3.1% and 8.0%, respectively. Contrary to the PCR counterfactuals, guaranteed firms substantially decrease their cash ratio and increase their debt ratio. This reduces the average cash ratio and significantly increases the debt ratio. Finally, we also find that increasing the guaranteed ratio significantly increases aggregate TFP, total output, consumption, and welfare. As for PCR, considering the small changes in total credit, the gains are substantial.

It is worth noticing that two counterfactuals $PCR\downarrow_{by\frac{1}{3}}$ and $GRI\uparrow_{by\,10\%}$ almost increase participation by the same amount, but they have different aggregate outcomes. Because $GRI\uparrow_{by\,10\%}$ affects credit access over the whole distribution of firms, and not only self-selection into the program, total credit increases more, as well as output and welfare. In that sense, a guaranteed ratio increment kills two birds with one stone: it can both increase participation and total output. However, participation cost reduction is more "cost-effective" if the objective is to increase participation without significantly increasing the guaranteed portfolio.

Unfortunately, we cannot directly discuss the exact cost-benefit analysis of such loan guarantee program expansions since we do not know exactly the direct and indirect costs of such expansions in the data, that is, how much direct organization costs the government pays to reduce the participation cost or how much indirect costs the government pays to increase the guaranteed ratio. We leave these to future work due to data limitations.

6.3 The Essential Role of Intertemporal Distortions

Finally, we examine quantitatively how intertemporal distortions determine the aggregate impact of relaxing liquidity constraints. In Section 3.3, we show in Proposition 2 that the long-term growth depends on the interaction between the intertemporal distortions and the collateral constraint. Without intertemporal distortions, the effect of short-term LGPs is temporary as the long-run scale is unchanged. Below, we show how the aggregate long-term economic impacts of a guaranteed ratio increment, demonstrated with the counterfactual of guaranteed ratio increment by 20% above, change under variations of both intertemporal distortions.

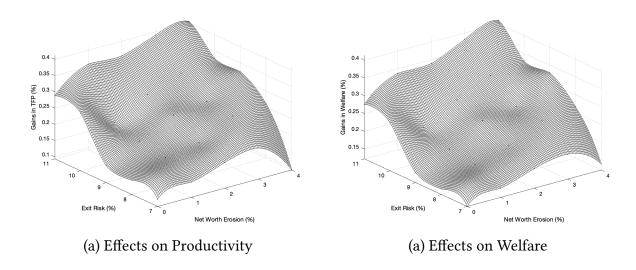


Figure 8: The Role of Intertemporal Distortions

Notes: This figure shows how the intertemporal distortions affect the aggregate impact of a higher guarantee ratio. We consider alternative net worth erosion τ and exit risk $1-\epsilon$ around the benchmark specification ($\tau=2\%, 1-\epsilon=9\%$). The impact on TFP and welfare is more than halved if both intertemporal distortions are reduced by 2%. This arises from a smaller-scale effect, as discussed earlier. In other counterfactuals, with higher net worth erosion and exit risk, the effect of the policy on output, TFP, and welfare is higher than in the benchmark because of the more severe intertemporal distortions.

First, both intertemporal distortions determine the effects of the LGP expansion. Figure 8

shows how the intertemporal distortions affect the aggregate impact of a higher guarantee ratio. We consider alternative net worth erosion τ and exit risk $(1 - \epsilon)$ around the benchmark specification ($\tau = 2\%, 1 - \epsilon = 9\%$). The impact on TFP and welfare is lower if either intertemporal distortion is reduced. This arises from a smaller scale effect, as discussed earlier. In other counterfactuals, with higher net worth erosion and exit risk, the effect of the policy on output, TFP, and welfare is higher than in the benchmark because of the more severe intertemporal distortions.

Table 10: Effect under alternative intertemporal distortions

Model Outcomes	Benchmark $(\tau = 0.02, \epsilon = 0.91)$	Lower τ $(\tau = 0, \epsilon = 0.91)$	Higher ϵ ($\tau = 0.02, \epsilon = 0.93$)	
Changes in Aggregate TFP (%)	0.25	0.14	0.17	
Changes in Total Welfare (%)	0.25	0.15	0.18	

Note: This table reports the effects of policy GRI $\uparrow_{\text{by }20\%}$ with different assumptions on τ and ϵ to illustrate the differences between the roles of net worth erosion and exit risk.

Second, net worth erosion matters more than exit risk. Table 10 shows the aggregate impact of a 20% higher guarantee ratio under two alternative assumptions on τ and ϵ from Figure 10. We first consider a lower τ ($\tau=0$ as opposed to $\tau=0.02$ in the benchmark) while ϵ is unchanged. The impact on output and welfare dropped by about 45% (0.25% to 0.14%). This arises from a smaller scale effect, as discussed above. In another counterfactual, we consider a higher ϵ ($\epsilon=0.93$ as opposed to $\epsilon=0.91$ in the benchmark) while τ remains unchanged. The effect of the policy on TFP and welfare dropped by about 30% (0.25% to 0.18%). Even though the lower τ and higher ϵ counterfactuals generate the same reduction in intertemporal distortion $(1-\tau)\epsilon$, the effects of the policy are stronger in the high ϵ counterfactual than in the low τ counterfactual. With a higher ϵ , firms exit less frequently, which gives them time to reach their long-run scale. This reinforces the long-term scale channel as opposed to the case with a lower τ . However, the effect of the policy remains lower than in the benchmark because of the milder intertemporal distortions. LGP effects are thus particularly strong when intertemporal distortions come from net worth erosion as opposed to when they come from firm exit risk.

7 Conclusion

In this paper, we study the effect of short-term finance and how relaxing liquidity constraints affects firm growth and the aggregate economy.

We first build a heterogeneous firm model in which firms face collateral and working capital constraints and show the theoretical predictions. In the model, constrained firms preserve many

resources in unproductive cash instead of productive capital to finance short-run working capital. A loan guarantee program mitigates credit constraints by inducing firms to reduce their cash holdings and expand their production scale. Additionally, a loan guarantee program generates a permanent increase in production scale due to intertemporal distortions.

We then take the model to a unique firm-level dataset of a credit guarantee program in Morocco. The model matches Moroccan firm-level moments well and replicates the patterns of our empirical findings: we show that firms with guaranteed loans expand their production scale homogeneously and persistently with increased labor and capital inputs and decreased cash ratios, which is consistent both qualitatively and quantitatively with the model. We then conduct counterfactual analyses to relax the severity of the short-term financial constraints. The gains from relaxing the severity of the short-term financial constraints by expanding the loan guarantee programs are substantial in terms of firm growth and welfare.

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Online Appendix to "Short-term Finance, Long-term Effects"

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A Empirical Appendix

A.1 Sample Construction and Statistics

Sample Cleaning We clean the Orbis firm-level data following the standard procedure as in Kalemli-Ozcan et al. (2015): (i) the data series deflated by the Moroccan national GDP deflator from the World Bank (2007 base); (ii) the entire series of company data is dropped if total assets, sales, tangible fixed asset are negative in any year; (iii) values of zero are dropped for all financial variables; (iv) the series are winsorized by year at 1% following Amamou, Gereben, and Wolski (2020); (v) as a final step, firms that are in the finance and insurance, public administration and utilities sectors are excluded since firms are not eligible for Tamwilcom guarantees.

Merge Databases We pair the Tamwilcom guarantee dataset and the Orbis balance-sheet dataset in four rounds. In the first round, considering that the firm's registered ID with the chamber of commerce is not unique across regions, a unique combination of two variables of national ID and date of firm creation is applied to conduct the first pairing round. This yields good pairing results owing to the good coverage of both variables. In the second round, we use the firm's national ID and name as a unique combination. As a first step, redundant elements in firm names are trimmed away, such as STE, SARL, and Société. With more compact firm names, the Levenshtein distance between the names of two firms is calculated to locate the closest match. A string distance of up to two generally indicates a good match. The third pairing round relies on combining the firm name and address. Paired results from this step only yield a small number of matches. The final round is based on the firm's name and the date of firm creation; the pairing rate is also low.

Table 1: Summary Statistics of Tamwilcom-Guaranteed Firms: Whole Sample vs. Merged Sample

-						
Statistics	Guarante	eed Amount	Guarant	eed Loan	Sales	
Sample	ple Whole Merged		Whole Merged		Whole	Merged
Mean	545	663	967	1,162	14,610	15,949
Std	1,336	1,467	3,401	3,598	28,120	28,314
Min	2	4	3	5	3	3
25%	35	42	50	60	775	1,148
Median	105	140	150	200	3,219	4,462
75%	400	560	550	800	14,176	17,039
Max	10,000	10,000	190,000	190,000	163,235	163,235

Notes: This table reports summary statistics of three variables (sales, guaranteed loan, and guaranteed amount) from the Tamwilcom sample and the merged sample between the Tamwilcom database and Orbis. All variables are in thousands of Moroccan Dirhams.

Sample Statistics After linking the Tamwilcom database to Orbis, we can identify 11,344 out of 23,017 guaranteed firms in the Orbis database, implying a rate of the successful pairing of 49.3%. Further participation of identified and unidentified guaranteed firms in Orbis shows that the two groups have similar characteristics. As shown in Table 1, loan amount, guaranteed amount, and sales reported by Tamwilcom are comparable for the two groups. One expected difference is that firm size is slightly higher for the subset of guaranteed firms that have been merged with Orbis data. This is because small firms usually report less complete information, making it less likely to be identified in Orbis.

Although we could successfully pair about half of the firms in our confidential loan-level data, a substantial portion of the successfully paired firms do not have key financial variables. Unfortunately, in our final matched sample, only 2.2% of the Tamwilcom-guaranteed firms are included. The rate is admittedly low but is consistent with other studies using Orbis data, especially considering Morocco as an African country. Even studies focusing on the EU and the US, which have much better data coverage, also suffer from low pairing rates. For instance, Gereben et al. (2019) report a rate of only 3.6% using data from Central and Eastern Europe. Fortunately, the sample size is still sufficiently large for our analysis. Our main concern about the pairing rate is the attrition of small firms in the final sample. To correct this bias, we follow Amamou, Gereben, and Wolski (2020) and use the technique of inverse probability weight (henceforth IPW) to recover the shares of firms of different sizes in the original treated population as a robustness check.

Potential Concerns We have two main concerns about our sample construction. The first is that some unidentified treated firms could be mistaken as untreated control firms and are matched with other treated firms later in the procedure. This would bias the estimation downward. However, this concern is marginally relevant due to the low treatment rate. Suppose the total number of firms in Orbis is taken as a representation of the whole business world in Morocco. In that case, there are approximately 1.58 million firms, of which only 23,017 have been treated. The resulting treatment rate is only 1.5%, indicating a very small possibility of a treated firm being matched with another unpaired treated firm.

The second is survivor bias. It mainly results from the fact that only businesses that actively report their balance sheet to the local trade register's office for the last five years are maintained in Orbis' online version. To reduce this bias, we complement the main online version with Orbis historical vintages, which have records of firms exiting the market.

¹Only 7505 firms have sales data for the year in which they are granted the guarantee. The number drops even further when a panel of at least three consecutive years is required for the matching process later.

A.2 Matching Procedure

Mahalanobis Distance Matching The matching, implemented under the assumption of "selection on observables," consists of finding statistical twins (control firms) for a guaranteed firm based on a series of time-varying and observable variables relevant to selection into the program. We use the Mahalanobis distance matching (MDM) method to construct a control sample in which a treated firm is matched with the five nearest "neighbors."²

Variable Choices Following Caliendo and Kopeinig (2008)'s recommendation, we choose the matching variables based on the existing literature and the institutional setting. As a result, total assets, sales, current liabilities, cash and cash equivalents, and firm age are used to measure the statistical distance between observations. Total assets and sales are selected as matching criteria since they are essential to balance sheet items, which reflect the firm's size and overall performance. Current liabilities, namely short-term debt, shed light on the firm's ability to rely on bank credit and the amount of existing indebtedness and risks associated with external credit. Cash and cash equivalents contain short-term investments and funds that can be used to pay current invoices and represent the firm's liquidity situation. The financial variables are log-transformed.

Matching Choices The matching is based on the firm's three-year history before receiving the credit guarantee. Firms with insufficient data coverage are inevitably excluded from the matching procedure. We apply exact matching on the sector, year, and firm size classification. We further divide the firms into 20 quantiles based on their sales and impose exact matching on their quantile bin. The purpose is to maximize the similarities between matched firms while maintaining a decent sample size. In robustness tests, we extend the three-year pre-treatment period to four and five. Our results are robust for both tests.

We conduct a new round of matching for each outcome variable in Section 5.1. In each round, we impose two requirements to ensure sample quality. First, we restrict the sample used for matching only to firms with data points for that outcome variable in that year. If a firm's data is missing for this variable in that period, this observation is dropped automatically. This ensures we match firms with data for the specified outcome variable to be tested in the regression. Second, we drop out outliers for that outcome variable before conducting matching. An observation is considered an outlier if that log change is huge (we use ten as the cutoff). A guaranteed firm is matched with a maximum of five closest control firms based on their Mahalanobis distances. Matched observations of treated firms are assigned a weight of one, whereas those of control firms are allocated a weight based on their distance from the corresponding treated firm.

²The Mahalanobis distance is a matrix that measures the multivariate proximity between two observations based on selected variables.

Caliper A caliper is implemented to ensure the common support assumption. A caliper refers to the maximum distance allowed between a treated firm and its controls. Any control firm beyond this caliper is dropped. This is to ensure that all control firms in the final sample are similar enough to the treated firm that it is matched with. The choice of the caliper is derived from the 0.9-quantile of the distribution of distances between observations in nearest neighbor pairwise matching with replacement, multiplied by 1.5. The choice is based on Jann (2017), Huber, Lechner, and Wunsch (2013), Huber, Lechner, and Steinmayr (2015) after considering the variance-bias trade-off: choosing a large caliper includes more control observations, thus decreasing variance; however, the bias increases if a non-comparable and distant control is included.

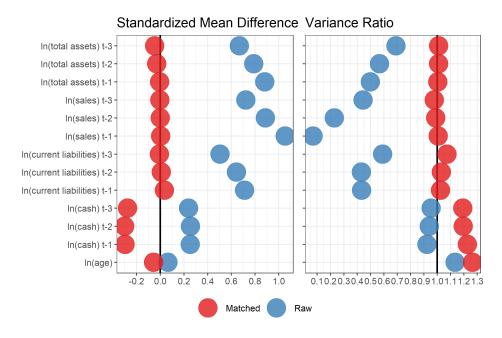
Weighing The analysis unit is firm-year, based on a similar procedure in Brown and Earle (2017). Matched observations of treated firms are assigned a weight of one, whereas those of control firms are allocated a weight based on their distance from the corresponding treated firm. We first calculate the kernel weight of each matched control observation based on its distance from the treated firm, using the Epanechnikov kernel function with the same bandwidth used in the matching. Subsequently, the weight of each control observation is rescaled as the share of its kernel weight in the sum of kernel weights of all controls matched with the same treated firm. This weight rescaling intends to up-weight those control firms close to treated firms and downweight those that are far away. For treated firms, only the firm-year observation of the guarantee receipt year is kept. This is to avoid the situation where a treated observation is matched with another observation from a treated firm in a year in which it does not receive a guarantee. For control firms, multiple firm-year observations that belong to the same firm are maintained in the pool of potential controls for matching, provided that the firm's data covers a three-year history of selected financial variables. The matching is performed with a replacement, which implies that one firm-year observation of an untreated firm can be selected more than once.

Matching Outcomes All matched samples have similar characteristics. For ease of discussion on matching outcomes, we hereby use the matched sample where the outcome of interest is sales growth between year t+1 and year t-1 as a representative sample. We obtain a final matched sample of 506 guaranteed firms and 1937 control firms, among which 60% have been matched only once, and 26% are used twice. The maximum number of times a control firm has been matched is eight. There are only eight firms in this situation. Since most untreated firms are matched only once, we expect the estimation results to be similar to a matching procedure without replacement. This is confirmed later by a robustness check.

Balancedness Tests Figure 1 represents the standardized mean difference (SMD) and variance ratios between the treated and control groups in the raw and matched sample.³ The SMD mea-

³See Table 2 for the statistics represented in Figure 1.

Figure 1: Standardized Mean Difference and Variance Ratio in Raw and Matched Sample



Notes: This figure is a visualization of Table 2. The standardized mean differences ("Std-Dif") and variance ratios ("Ratio") of the raw sample and matched sample are reported by the Stata *kmatch* package as in Jann (2017). All financial variables are log-transformed.

sures the mean difference of a given variable between two groups, normalized by the standard deviation of that variable. Variance ratio refers to the ratio between the variances of a variable across two groups. A value of zero for the SMD and a value of one for the variance ratio indicate a good balance in the sample. As shown in the Figure, the matching procedure substantially improves the overall balancedness for most variables, except for cash. Guaranteed firms have a lower cash holding level on average compared to their matched control firms, which also appears in Figure 2.

As a second balancedness test suggested by Caliendo and Kopeinig (2008), we evaluate the probability of obtaining a guarantee through a logit model based on the variables used in the matching. Ideally, a drop in R^2 indicates a good balance in the sample. We observe that the pseudo R^2 of the logit model falls from 0.11 with the raw sample to 0.01 with the matched sample. This confirms the loss of the predictive power of the selected variables after matching. It confirms that the matching procedure has eliminated differences in the pre-treatment observable characteristics between the two groups and that the treatment status is "randomized" in the matched sample conditional on the selected variables.

Trend Inspection Figure 2 illustrates the weighted average of the log value of the four variables used in the matching procedure. It confirms the parallel pre-treatment trend between the

Table 2: Standardized Mean Difference and Variance Ratio: Raw and Matched Sample

Sample		Raw			Matched	
Mean	Treated	Untreated	StdDif	Treated	Untreated	StdDif
$ln(total assets)_{t-1}$	15.60	14.01	0.88	16.61	16.62	-0.01
$ln(sales)_{t-1}$	15.62	11.23	1.06	16.71	16.70	0.003
$ln(current\ liabilities)_{t-1}$	15.09	13.42	0.71	16.16	16.08	0.03
$ln(cash)_{t-1}$	11.35	10.76	0.25	12.21	12.90	-0.30
$ln(total\ assets)_{t-2}$	15.40	13.94	0.79	16.50	16.55	-0.03
$ln(sales)_{t-2}$	15.13	11.19	0.89	16.66	16.66	-0.001
$ln(current\ liabilities)_{t-2}$	14.88	13.28	0.64	16.06	16.04	0.01
$ln(cash)_{t-2}$	11.35	10.77	0.26	12.13	12.81	-0.30
$ln(total\ assets)_{t-3}$	15.12	13.82	0.67	16.39	16.48	-0.05
$ln(sales)_{t-3}$	14.39	10.78	0.72	16.60	16.61	-0.004
$ln(current\ liabilities)_{t-3}$	14.48	12.96	0.50	15.97	15.99	-0.01
$ln(cash)_{t-3}$	11.31	10.78	0.24	12.13	12.74	-0.28
ln(age)	5.18	5.15	0.07	5.43	5.45	-0.06
Variances	Treated	Untreated	Ratio	Treated	Untreated	Ratio
$ln(total assets)_{t-1}$	2.17	4.35	0.50	1.65	1.64	1.01
$\ln(\text{sales})_{t-1}$	2.26	32.33	0.07	1.35	1.34	1.01
$ln(current\ liabilities)_{t-1}$	3.32	7.66	0.43	1.96	1.91	1.03
$ln(cash)_{t-1}$	5.14	5.56	0.92	4.57	3.72	1.23
$ln(total\ assets)_{t-2}$	2.46	4.34	0.57	1.73	1.71	1.01
$ln(sales)_{t-2}$	7.32	31.99	0.23	1.37	1.38	0.99
$ln(current\ liabilities)_{t-2}$	3.72	8.60	0.43	2.01	1.95	1.03
$ln(cash)_{t-2}$	4.95	5.27	0.94	4.55	3.81	1.20
$ln(total\ assets)_{t-3}$	3.09	4.47	0.69	1.79	1.77	1.01
$ln(sales)_{t-3}$	15.34	34.52	0.44	1.37	1.41	0.98
$ln(current\ liabilities)_{t-3}$	6.67	11.31	0.59	2.08	1.94	1.07
$ln(cash)_{t-3}$	4.78	5.00	0.96	4.51	3.78	1.19
ln(age)	0.23	0.20	1.13	0.22	0.18	1.27

Notes: This table reports the standardized mean differences ("StdDif") and variance ratios ("Ratio") of the raw sample and the matched sample, reported by Stata *kmatch* package (see Jann (2017)). All variables are log-transformed.

treated and control firms and provides preliminary evidence on the dynamic impact of working capital loan guarantees on a firm's growth. As shown in Figure 2, guaranteed firms experience growth in sales, total assets, current liabilities, and a decline in cash. This will be confirmed later in the regressions. Overall, standard balancedness tests indicate a good balance in the sample.

As for the level of financial variables before treatment, they are similar, except for cash. Guaranteed firms have a lower level of cash holding on average compared to their matched control

firms. This is likely linked to the firm's short-term credit demand. Firms that apply for a guarantee have insufficient cash to cover their liquidity needs. To address this issue, we conduct two robustness tests of a matching procedure focused only on cash-related variables. We show that the results are consistent. This is detailed in A.5.

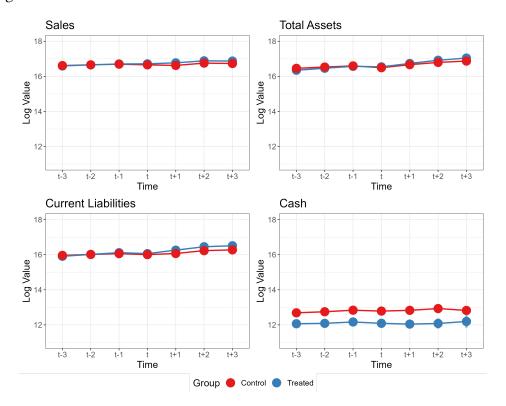
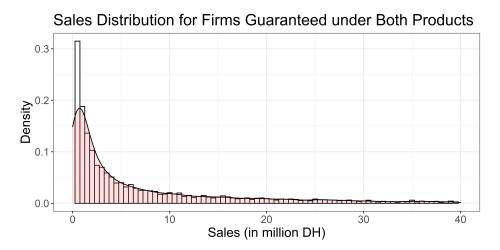


Figure 2: Trend Inspection of Four Financial Variables Used in Matching

Notes: This figure depicts the weighted average of the log values of sales, total assets, current liabilities, and cash in years t-3 to t+3 of treated and control firms in the final matched sample. Confidence intervals are at the 95% level.

A.3 Supplementary on Summary Statistics

Figure 3: Sales Distribution of Guaranteed Firms



Notes: This figure presents the sales distribution (density) of firms guaranteed under Damane Exploitation and Damane Express. The sales number is from the Tamwilcom database.

Table 3: Summary Statistics: Guaranteed Firms VS. Non-Guaranteed Firms

Statistic	N	Mean	St. Dev.	Pctl(25)	Median	Pctl(75)				
Guaranteed firms (treated sample)										
Sales Growth	3,178	0.152	1.836	-0.108	0.073	0.290				
Total Assets Growth	3,184	0.177	1.728	-0.015	0.148	0.367				
Costs of Employees Growth	3,091	0.204	0.597	-0.017	0.130	0.331				
Fixed Assets Growth	3,184	0.099	2.308	-0.323	-0.053	0.340				
Current Liabilities Growth	3,184	0.189	1.537	-0.091	0.123	0.388				
Cash Growth	3,124	0.058	1.984	-0.942	0.066	1.038				
Non-guaranteed firms (cont	rol sampl	e)								
Sales Growth	15,921	0.086	2.214	-0.126	0.034	0.224				
Total Assets Growth	15,932	0.095	1.804	-0.048	0.087	0.265				
Costs of Employees Growth	15,338	0.138	0.573	-0.038	0.089	0.258				
Fixed Assets Growth	15,932	-0.043	2.374	-0.377	-0.096	0.182				
Current Liabilities Growth	15,951	0.094	1.558	-0.137	0.045	0.290				
Cash Growth	15,674	0.104	1.608	-0.624	0.076	0.860				

Notes: The summary statistics are based on the matched sample of treated firms and control firms. The growth rate of financial variables is the first difference between logged variables.

Table 4: Distribution Statistics of Firm Characteristics

Assets Quantile	Assets	Sales/Assets	Debt/Assets	Cash/Assets
Orbis Sample				
1	77	1.21	0.24	0.59
2	338	1.24	0.53	0.25
3	1, 102	1.02	0.61	0.15
4	3,509	0.89	0.65	0.10
5	41, 965	0.68	0.65	0.06
Guaranteed Sample				
1	770	1.69	0.56	0.18
2	2,462	1.31	0.62	0.08
3	5, 422	1.21	0.65	0.06
4	12,866	1.12	0.66	0.05
5	54, 923	0.91	0.68	0.03
Non-Guaranteed Sample (Control)				
1	2,897	2.02	0.60	0.12
2	8,704	1.54	0.64	0.08
3	16,971	1.32	0.64	0.06
4	33, 254	1.08	0.63	0.06
5	111, 372	0.72	0.60	0.04
Non-Guaranteed Sample (Whole)				
1	73	1.20	0.23	0.60
2	309	1.25	0.52	0.26
3	996	1.01	0.61	0.16
4	3, 166	0.87	0.65	0.11
5	40, 929	0.65	0.65	0.06

Notes: This table reports the means of indicated financial variables and ratios based on five quantile groups of total assets. The unit of total assets is a thousand. Observations with ratios of current liabilities/total assets and cash/total assets greater than one or less than 0 are dropped. The Orbis sample comprises all firms in Morocco. The guaranteed sample refers to the whole sample of guaranteed firms. The non-guaranteed sample (whole) comprises all firms that do not possess a credit guarantee. The non-guaranteed sample (control) refers to those non-guaranteed firms selected during the empirical analysis's matching process.

A.4 Supplementary on Participation Rate

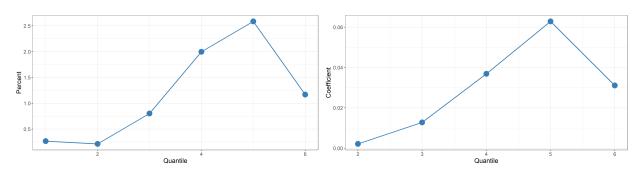
Table 5: Participation Rate by Size

Size	Participation Rate (%)				
Small company	2.51				
Medium-sized company	15.40				
Large company	11.44				
Very large company	1.22				

Table 6: Probability of Successful Pairing between Tamwilcom and Orbis by Size

Size	Probability (%)
Small company	30.37
Medium-sized company	52.54
Large company	74.41
Very large company	79.03

Figure 4: Distribution of Participation Rate



- (a) Distribution by Total Assets Quantile Bin
- (b) Coefficient of Quantile Regression

Notes: The cut points of total assets quantile bins are set at 0.1, 0.5, 0.75, 0.9, 0.99. In Figure 4 (a), the participation rate is calculated as the ratio of the number of guaranteed firms to the total number of firms in each bin. In Figure 4 (b), the coefficient is from the following regression: Participation_{it} = $\sum_{q=1}^{6} \beta_q$ Quantile $\text{Bin}_q + \delta_j + \delta_t$, where *i* indexes individual firms, *j* indexes sector, and *t* indexes year. Participation_{it} is a dummy variable of one if the firm is guaranteed and zero otherwise. Quantile Bin_q is a dummy variable of one of the firm's total assets located in quantile q ($q \in [1, 6]$), and zero otherwise. δ_j and δ_t refer to sector and year fixed effects. Observations in quantile one are dropped automatically by Stata due to collinearity. Coefficients of β_q are reported in Figure 4 (b).

A.5 Robustness Checks

A.5.1 Number of Pre-treatment Years in Matching

The first robustness test corresponds to concerns regarding the number of pre-treatment years used for matching. Existing literature suggests that we should rely on at least three years' pre-treatment performance for matching, which is our main estimation. In this robustness check, we extend the number of years to four and five. Table 7 reports the estimated results when we match four years' data. As a result of the stricter matching requirement, the number of treated firms that have at least one matched control firm drops to 345. Most results in year t+1 remain robust and significant on a similar level, consistent with our baseline results. When we increase the number of years used for matching to five, we only have 213 guaranteed firms that enter the final sample. The estimated results for the year t+1 in Table 8 are mostly significant except for the coefficient on cash. This is also in line with the baseline.

Table 7: Results of Year t + 1 from Matching on Four Pre-Treatment Years' Data

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.130***	0.094**	0.129***	0.090	0.090***	0.146*
	(0.029)	(0.029)	(0.031)	(0.106)	(0.025)	(0.069)
N adj. R^2 Group × Year FE City × Year FE	13432	13723	13952	13531	12636	13460
	0.216	0.236	0.213	0.338	0.228	0.213
	Yes	Yes	Yes	Yes	Yes	Yes
	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we match on four pre-treatment years' data. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+1 t+1

Table 8: Results of Year t+1 from Matching on Five Pre-Treatment Years' Data

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.169*** (0.039)	0.137*** (0.032)	0.130*** (0.036)	0.015 (0.133)	0.081** (0.029)	0.273*** (0.075)
N	8664	8805	8902	8752	8343	8641
adj. R^2	0.265	0.236	0.133	0.361	0.223	0.229
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we match five pre-treatment years' data. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t0.010, t0.010, t0.010, t0.01010.

A.5.2 Data Attrition Bias

The second robustness test is to correct the bias from the data attrition issue. The main concern arises from the loss of observations of small firms during matching. Considering that small firms often report minimal financial data, it could lead to their exclusion in the matching process due to missing data points. In order to correct this bias, we use inverse probability weighting (ipw) (Amamou, Gereben, and Wolski, 2020) to increase the weight of underrepresented SMEs and decrease the weight of those who are over-represented. As a first step, we calculate the number of small, medium, and large firms in the sample of Tamwilcom-guaranteed firms that can be merged with Orbis. As discussed earlier, this sample shares similar statistical properties with the sample of all Tamwilcom-guaranteed firms. The reason for choosing this merged sample rather than the full sample is that we can use the size information provided by Orbis. We assume that information on firm size composition in this merged sample can reflect that of the full sample. As a second step, we count the number of firms of different sizes in the processed sample after matching and divide the number of small, medium, and large firms in the processed sample by the number in the original sample before matching. The inverse of the proportion is then used as a weight to re-scale the representation of different-sized firms in the final sample. As Table 9 shows, estimation results are similar to the main ones, with the exception of total and fixed assets.

Table 9: Results of Year t+1 with Inverse Probability Weight

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.129** (0.046)	0.039 (0.037)	0.109** (0.041)	-0.224 (0.176)	0.131** (0.040)	0.003 (0.103)
N	17199	17344	17520	17017	16571	17117
adj. R^2	0.201	0.222	0.193	0.323	0.319	0.201
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

A.5.3 Emphasizing Cash in Matching

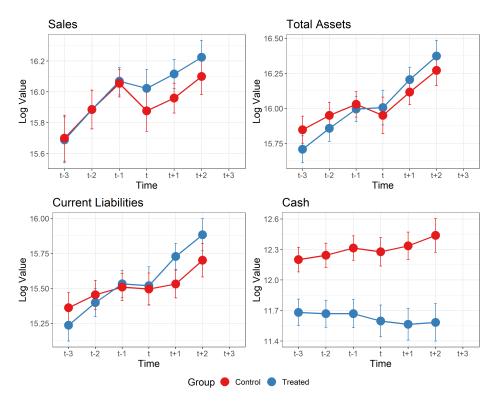
The third set of checks intends to test the robustness of the main results when we emphasize matching on cash-related variables to reduce the difference in the cash level of treated and control firms after matching in Figure 2. As a first test, we use one-to-one nearest-neighbor matching to ensure that only the closest control firm is selected. This is to see if the difference in the gap comes from any chosen control firm that is not similar enough to its matched neighbor. As shown in Figure 5, the gap remains large and is very similar to the five-to-one nearest neighbor matching. In view of this, we rule out the possibility that remote control firms contribute to the difference in cash. As a further test, we only include logged cash and the ratio of cash to total assets in the matching process. This setup "forces" a good matching result on cash by not including other variables so that the measurement of Mahalanobis distance is only based on cashrelated variables. In addition, we divide the variable of logged cash into 20 quantile intervals and apply exact matching on the interval. Figure 6 shows that this procedure manages to substantially improve the matching performance on cash. Furthermore, total assets are balanced as well due to the incorporation of the ratio of cash to total assets. However, we observe a gap in sales. To reduce this gap, we modified the setup to match on cash ratio and logged sales. As Figure 7 indicates, the good balancedness in cash, total assets, and current liabilities are preserved while the difference in sales is decreased. Estimation results for both matchings are reported in Table 10 and Table 11. They are consistent with the main results.

Table 10: Results of Year t+1 from Matching on Logged Cash and Cash Ratio

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.217** (0.080)	0.162** (0.052)	0.203*** (0.050)	-0.067 (0.114)	0.088** (0.032)	0.256* (0.114)
N adj. R^2 Group × Year FE	6109 0.233 Yes	6435 0.231 Yes	6604 0.101 Yes	6144 0.325 Yes	4963 0.359 Yes	6209 0.215 Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we only include logged cash and the ratio of cash to total assets from three pre-treatment years for matching. In addition, we divide the log cash variable into 20 quantile intervals and apply exact matching on the interval. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+10 t+10

Figure 5: Robustness: Trend Inspection from Matching with One Nearest Neighbor



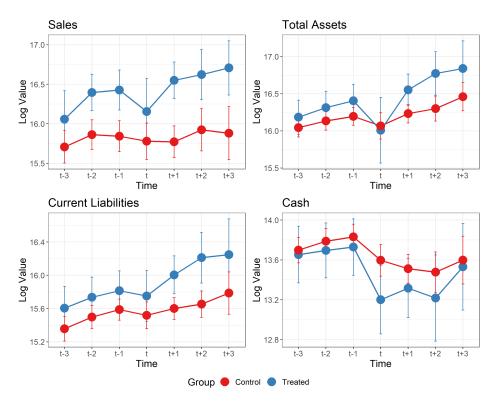
Notes: This figure depicts the weighted average of the log values of sales, total assets, current liabilities, and cash in year t-3 to t+2 of treated and control firms from the robustness test, where we match only one nearest control firm for a treated firm. The confidence interval is at 95% level.

Figure 6: Robustness: Trend Inspection from Matching on Log Cash and Cash Ratio



Notes: This figure depicts the weighted average of the log values of sales, total assets, current liabilities, and cash in year t-3 to t+2 of treated and control firms from the robustness test, where we only include logged cash and the ratio of cash to total assets from three pre-treatment years for matching. In this robustness test, we also divide the log cash variable into 20 quantile intervals and apply exact matching on this interval. The confidence interval is at 95% level.

Figure 7: Robustness: Trend Inspection from Matching on Log Sales and Cash Ratio



Notes: This figure depicts the log values of sales, total assets, current liabilities, and cash in year t-3 to t+2 of both treated and control firms from the robustness test, where we only include logged sales and the ratio of cash to total assets from three pre-treatment years for matching. In this robustness test, we also divide the log cash variable into 20 quantile intervals and apply exact matching on this interval. The confidence interval is at 95% level.

Table 11: Results of Year t+1 from Matching on Logged Sales and Cash Ratio

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.202** (0.071)	0.136** (0.052)	0.205*** (0.050)	-0.091 (0.115)	0.096** (0.031)	0.243* (0.104)
N	6478	6750	6873	6496	5335	6595
adj. R^2	0.324	0.215	0.137	0.297	0.364	0.196
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we only include logged sales and the ratio of cash to total assets from three pre-treatment years for matching. In addition, we divide the log cash variable into 20 quantile intervals and apply exact matching on the interval. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+10 t+1

A.5.4 Propensity Score in Mahalanobis Distance

In the fourth set of checks, we include propensity score as one variable in calculating Mahalanobis distance. We exploit the predictive power of a logit model, where the dependent variable is a dummy of one if a firm is guaranteed in a certain year, and independent variables are the same as those selected for calculating Mahalanobis distance. Table 12 reports the estimation results, which are similar to our main results. We conduct another robustness test where we increase the number of nearest neighbors matched with guaranteed firms to ten. We find that the results are not sensitive to the number of controls chosen for the treated firm, as shown in Table 13. We also apply the matching procedure without replacement and confirm that estimation results remain similar, as shown in Table 14.

Table 12: Results of Year t+1 with Propensity Score in Multivariate Matching

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.139***	0.093***	0.143***	-0.054	0.107***	0.113^{+}
	(0.025)	(0.024)	(0.027)	(0.091)	(0.021)	(0.061)
N	18268	18464	18841	18141	17418	17976
adj. R^2	0.190	0.204	0.213	0.313	0.241	0.199
Group \times Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we include propensity score as one variable in calculating Mahalanobis distance. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variable in the logit model is a dummy of one if a firm is guaranteed in a certain year, and the independent variables are the same ones selected for calculating Mahalanobis distance in the main setup. Outcome variables are the log difference of six main variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+10 the property of the property o

Table 13: Results of Year t + 1 from Matching on 10 Nearest Neighbors

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.136*** (0.023)	0.084*** (0.022)	0.131*** (0.025)	0.135 (0.101)	0.098*** (0.023)	0.163* (0.064)
N	23583	24054	24569	23644	22796	23410
adj. R^2	0.253	0.253	0.249	0.348	0.278	0.246
Group \times Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we match up to 10 nearest control firms for a treated firm. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+10 on t+10 of t+11 of t+12 of t+12 of t+13 of t+1

Table 14: Results of Year t + 1 from Matching without Replacement

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	0.147***	0.105***	0.146***	-0.198*	0.086**	0.109+
	(0.030)	(0.024)	(0.028)	(0.084)	(0.028)	(0.063)
N	16165	16631	16682	16131	14681	16226
adj. R^2	0.297	0.207	0.261	0.328	0.267	0.234
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
$City \times Year\ FE$	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we apply the matching procedure without replacement. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+1 t+1

A.5.5 Placebo Test Assuming Treatment Occurred Three Years Earlier

We conduct a falsification test assuming the treatment occurred three years earlier than it actually took place. Table 15 reports the estimation results. As it shows, most coefficients are not significant, which confirms the robustness of the main results.

Table 15: Results of Year t + 1 from Placebo Test

	(1)	(2)	(3)	(4)	(5)	(6)
	Sales	Total Assets	Current Liabilities	Cash	Costs of Employees	Fixed Assets
Guaranteed	-0.013 (0.117)	0.098 (0.089)	-0.006 (0.057)	-0.022 (0.100)	0.104** (0.039)	0.091 (0.126)
N	17833	17859	17874	17575	17219	17859
adj. R^2	0.069	0.037	0.032	0.102	0.083	0.029
Group × Year FE	Yes	Yes	Yes	Yes	Yes	Yes
City × Year FE	Yes	Yes	Yes	Yes	Yes	Yes

Note: This table reports the coefficients of treatment ("Guaranteed") from DID regression in the robustness test, where we assume the treatment occurred three years earlier. Each outcome variable in each year is based on a different matched sample where we drop firms without data for that outcome variable in that year before matching and excluding outliers. The dependent variables are the log difference of six main outcome variables (sales, total assets, labor costs, fixed assets, cash, and current liabilities) in year t+1 from year t-1. "Guaranteed" indicates that a firm receives a Tamwilcom guarantee in year t. Group-year and city-year fixed effects are included. Standard errors are clustered at the group-year level. Significance level: t+10 t

B Theoretical Appendix

B.1 Proofs in the Analytical Model

B.1.1 The entrepreneur's program in the special case

The first-order conditions of the Lagrangian problem associated with objective (12) are the following:

$$/d_t : d_t^{-\eta} - \eta_t \tag{1}$$

$$/n_t : \beta \epsilon v'(n_t) - \eta_t \qquad = 0 \tag{2}$$

$$/k_t : -\gamma_t + [\psi'(k_t) + 1 - \delta] + \lambda_t(\theta - a) = 0$$
 (3)

$$/c_t: -\gamma_t + (1+r_t) + \lambda_t + \zeta_t \qquad = 0 \tag{4}$$

where η_t is the shadow price of the budget constraint (13), and γ_t , λ_t and ζ_t the shadow prices of, respectively, the net worth allocation constraint (14), the working capital constraint (15) and the non-negative cash constraint (16), normalized by $[\eta_t(1-\tau)]^{-1}$. The envelope theorem yields

$$v'(n_{t-1}) - \gamma_t \eta_t (1 - \tau) = 0 \tag{5}$$

We use the first-order conditions to derive the equations (17) and (19) in the paper. FOC equation (3) and equation (4) yield the relationship between MBK and MBC equation (17) immediately. Considering a sufficiently small SME which needs positive cash holdings ($\zeta = 0$), FOC equation (2), combined with equation (5) evaluated in t + 1, together with equation (4) evaluated in t + 1, and finally replace both η_t and η_{t+1} using equation (1), yield equation (19).

B.1.2 Proof of Proposition 2

Point (i) derives immediately from the long-term Euler equation (21) and from the stationarity of household consumption that implies $\beta(1 + r_{t+1}) = 1$.

To establish the point (ii), we use the expression for λ_t^* , where we replace λ_t^* with its long-term value λ^{LT} . We obtain an implicit definition of the long-run capital stock k^{LT} :

$$\lambda^{LT} = \frac{\psi'(k^{LT}) + 1 - \delta - (1 + r_t)}{1 + a - \theta}$$

we then replace $1 + r_t$ with $1/\beta$. Then, we define the optimal capital stock as k^{opt} . Noting that,

 k^{opt} is determined by $\psi'(k^{opt}) + 1 - \delta = (1 + r_t)$, we replace $1 - \delta - (1 + r_t)$ with $-\psi'(k^{opt})$. This yields point (ii).

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