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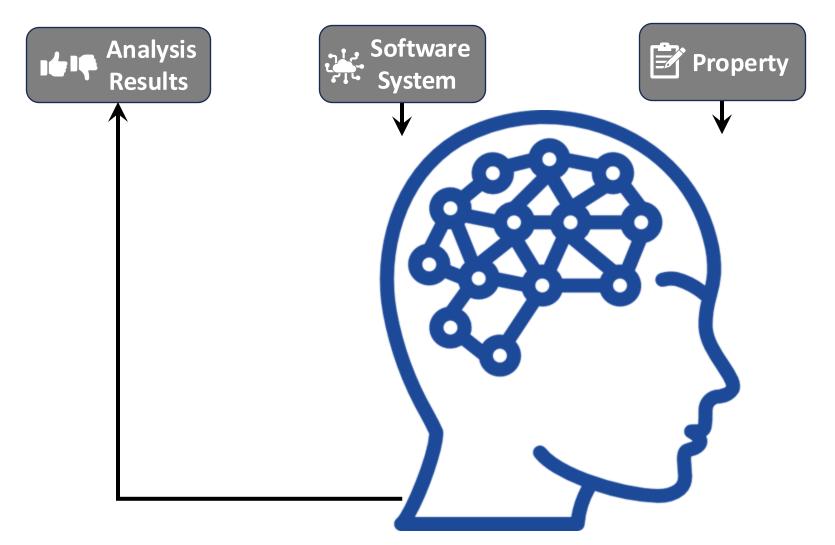
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### Direction 1: Software Verification

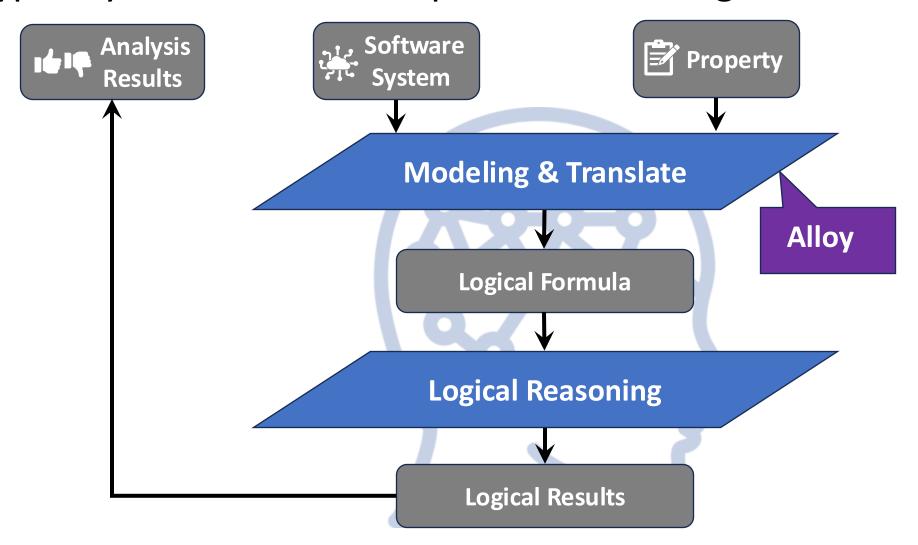
Systematically and logically analyze software systems with properties





### Direction 1: Software Verification

Typically models software problems into logical formulas



#### Overview

#### **Alloy Language:**

build models, requirements, specifications, software design

- 1) Lightweight: small and easy to use, and capable of expressing common properties naturally
- 2) Precise: having a simple and uniform mathematical semantics

#### **Alloy Analyzer:**

fully automated software model analysis

#### Why we need Alloy?

#### **Alloy Language:**

- Provides precise description of artifacts
- Good Documentation
- Provides higher level of abstraction
- Helps describe properties that we cannot (easily) express in source code

#### **Alloy Analyzer:**

- Enables machine reasoning
- Helps eliminate/reduce ambiguities, inconsistencies, and incompleteness

#### Why we need Alloy?

#### "Everybody likes a winner"

- Ambiguous?
- Incomplete?

#### Precise meaning?

- all p: Person | some w: Winner | p.likes(w)
- all p: Person | all w: Winner | p.likes(w)

### A lot of Applications over the past two decades

- 1. Network and Web Security Modeling and Analysis
- 2. Formal modeling and analysis of a flash filesystem in Alloy
- 3. Efficient re-resolution of specifications for evolving software architectures
- 4. Specification of a distributed spanning tree
- 5. Declarative testing for distributed programs
- 6. Analyzing the Fundamental Liveness Property of the Chord Protocol

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### Alloy in General

Alloy is general enough that it can model

- any (finite) domain of individuals and
- any relations between them

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#### **Atoms and Relations**

An atom is a primitive entity that is

- indivisible: it cannot be broken down into smaller parts
- immutable: it does not change over time
- uninterpreted: it does not have any built-in property (the way numbers do for example)

A relation is a structure that relates atoms

It is a set of tuples of the same type

#### **Atoms** and **Relations**: Example

#### FriendBook

Ted -> ted@gmail.com Ryan -> ryan@hotmail.com

#### WorkBook

Pilard -> pilard@uiowa.edu Ryan -> ryan@uiowa.edu

Unary relations: a set of names, a set of addresses and a set of books

```
Name = { (N0), (N1), (N2)}
Addr = { (D0), (D1)}
Book = { (B0), (B1)}
Tuples
```

A binary relation from names to addresses

```
address = { (N0,D0), (N1,D1) }
```

A ternary relation from books to name to addresses

```
addr = { (B0,N0,D0), (B0,N1,D1), (B1,N1,D2) }
```

**Everything in Alloy is** built from relations

### Main components of an Alloy Model

- 1. Signatures and Fields
- 2. Predicates
- 3. Facts
- 4. Commands and scopes

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#### Signatures and Fields

- 1. Signatures: introduces a set of atoms Unary relation
- 2. Fields: declares relations

#### Example:

1. Introduces three sets named A, B, C, respectively

```
sig A {} sig B {} sig C {}
```

2. Declare Binary Relation:

```
sig A { f1: B } // f1 is a field, a binary relation of type A x B
```

3. Ternary Relation:

```
sig A { f2: B -> C } // f2 is a field, a ternary relation of type A x B x C
```

Cardinality Constraints: constrain the sizes of sets

```
- some e //e is non-empty
           - no e //e is empty
           - lone e //e has at most one tuple
           - one e //e has exactly one tuple
Example:
one sig List {
                     // Declare one single linked-list
 header: lone Node
                     // with ?
sig Node {
 next: lone Node // each node has?
```

Cardinality Constraints: constrain the sizes of sets

```
- some e //e is non-empty
           - no e //e is empty
           - lone e //e has at most one tuple
           - one e //e has exactly one tuple
Example:
                      // Declare one single linked-list
one sig List {
 header: lone Node
                     // with at most one header node
sig Node {
 next: lone Node
                    // each node has at most one next node
```

### Main components of Alloy Model

- 1. Signatures and Fields
- 2. Predicates
- 3. Facts
- 4. Commands and scopes

#### Facts and Predicates

Alloy models can be refined further by adding formulas expressing additional constraints over signatures and relations

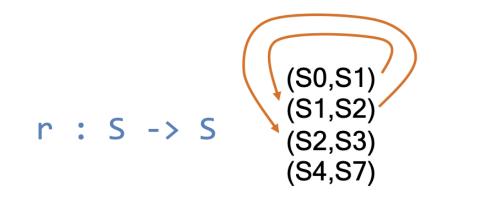
- Facts: the constraints that Alloy model must satisfy
- Predicates: optional constraints that Alloy model can satisfy

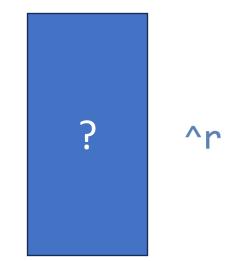
Facts and Predicates Relational Operators

> _	arrow (cross product)
~ _	transpose
_ • _	dot join
_[_]	box join
^ _	transitive closure
* _	reflexive-transitive closure
_ <: _	domain restriction
_ :> _	image restriction
_ ++ _	override

Relational Operators: transitive closure

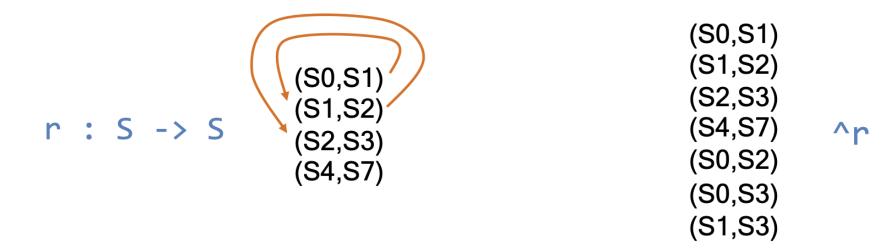
Given a binary relation r (x->y), the **transitive closure** of r, denoted  $^{r}$ , includes all elements x and y such that x can reach y by following one or more steps of r.





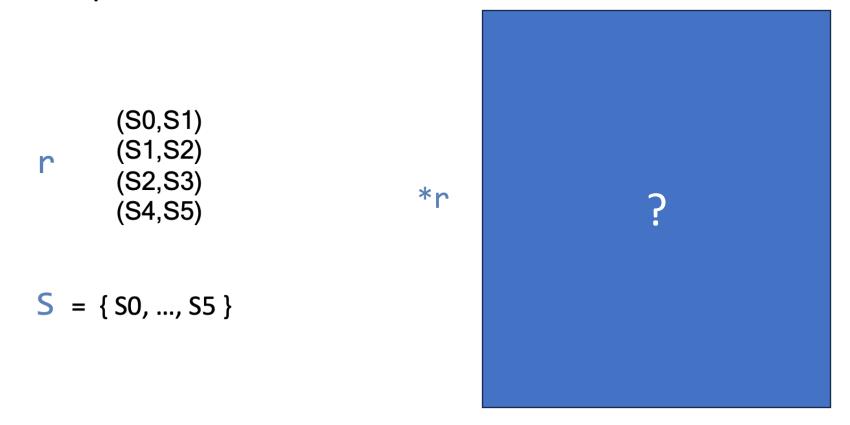
Relational Operators: transitive closure

Given a binary relation r, the **transitive closure** of r, denoted **^r**, includes all elements x and y such that x can reach y by following **one or more steps** of r.



Relational Operators: reflexive-transitive closure

**reflexive-transitive closure** of a relation \*r is the transitive closure plus **reflexive connections**.



Relational Operators: reflexive-transitive closure

reflexive-transitive closure of a relation \*r is the transitive closure plus reflexive connections.

Relational Operators: dot join

What is the join of theses two tuples?

```
    (a<sub>1</sub>,...,a<sub>m</sub>) and (b<sub>1</sub>,...,b<sub>n</sub>)
    If a<sub>m</sub> ≠ b<sub>1</sub> then the join is undefined
    If a<sub>m</sub> = b<sub>1</sub> then it is: (a<sub>1</sub>,...,a<sub>m-1</sub>,b<sub>2</sub>,...,b<sub>n</sub>)
```

#### **Example**

```
- (a,b).(a,c,d) undefined
- (a,b).(b,c,d) = (a,c,d)
```

What about (a).(a)?
 Not defined!

t<sub>1</sub>.t<sub>2</sub> is not defined if t<sub>1</sub> and t<sub>2</sub> are **both** unary tuples

### **Relational Operators**

```
Example:
one sig List {
  header: lone Node
}
sig Node {
  next: lone Node
}
```

```
// All nodes are reachable from the header node
fact Reachable {
  ?
}
```

#### **Relational Operators**

```
Example:
one sig List {
 header: lone Node
}
sig Node {
 next: lone Node
}
```

```
// All nodes are reachable from the header node
fact Reachable {
  Node = List.header.*next
}
```

#### Facts and Predicates

#### **Logical Operators**

(Boolean) negation

conjunction

disjunction

implication

#### **Set Operators**

### Main components of Alloy Model

- 1. Signatures and Fields
- 2. Predicates
- 3. Facts
- 4. Commands and scopes

#### Run Commands and Scopes

To analyze a model, you add a run command and instruct Alloy Analyzer to execute a predicate

- the run command
   tells the tool to search for an instance that satisfy all facts and the predicate
- you may also give a scope to signatures
   bounds the size of instances that will be considered

#### **Example:**

```
one sig List {
  header: lone Node
}
sig Node {
  next: lone Node
}
```

```
Predicate Reachable {
  Node = List.header.*next
}
```

run Reachable for exactly 3 Node

#### Overview

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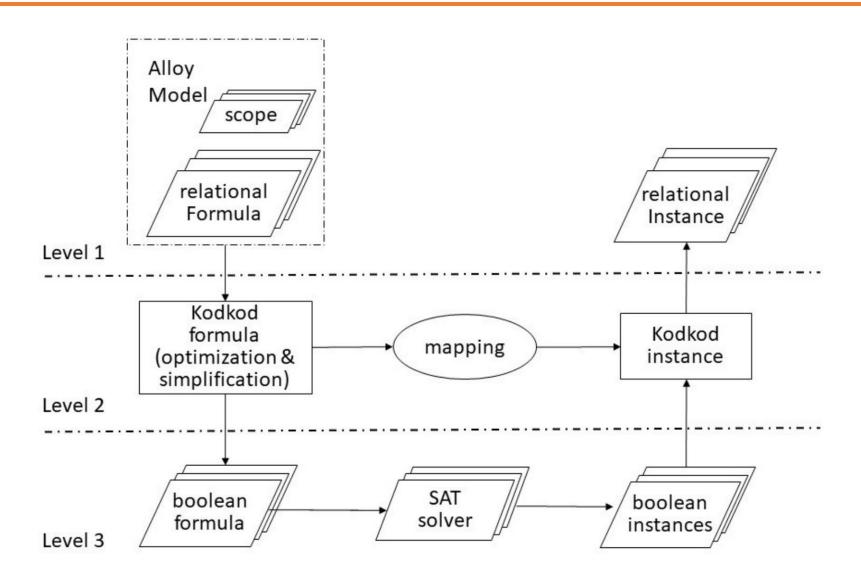
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# Alloy Analyzer



# Alloy Analyzer

Let's implement an Alloy model!

#### Research Topics

### Improve analysis using ML

- Incremental analysis
- SAT optimizations
- Symmetry breaking

#### Solve new ML applications using Alloy

- Can you model ML-related problems from your domain?
- ML applications:
  - verify a certain property of Neural network models
  - Synthesis NN model with Alloy
  - Generate test cases for testing NN models