Homework 1

Due 11:59 PM on Monday October 7, 2019

In this assignment, you will come up with and implement two dynamic programming algorithms. **Key instructions:**

- 1. Collaboration: You are **required** to work in groups of 2 students on each assignment. Please indicate the name of your collaborator at the top of each assignment (in comments for each piece of code you submit) and cite any references you used (including articles, books, code, websites, and personal communications). If you're not sure whether to cite a source, err on the side of caution and cite it. You may submit just one copy of the solution for the group. Remember not to plagiarize: all solutions must be written by members of the group. If you are the odd person out we will have you join an existing group of 2.
- 2. Please only use **python2** for the assignment (allowing multiple versions makes grading substantially harder for a huge class)
- 3. Please do NOT use any additional imports, only write your code where you see TODO: YOUR CODE HERE, and change your return value accordingly.
- 4. You will need to submit your diffing.py and respacing.py on CMS. Please be careful not to swap them by accident!
- 5. Reminder on Late Policy: Each student has a total of one slip day that may be used without penalty for homework. We will also drop your lowest homework score. An assignment can be at most one day late without penalty via slip days.

1 Diffing with costs

1.1 Problem statement

We saw in lecture that 'diffing' two strings can be accomplished with dynamic programming: Lecture 2 - P10. In this problem we will solve a more general version. We would like to align two strings, s and t, in a way to produce a *minimum-cost* alignment.

To produce an alignment on two strings s and t, we insert the special character '-' some number of times into each string to produce align_s and align_t so that:

- align_s and align_t have the same length, and
- There is no i such that align_s[i] and align_t[i] are both '-'.

The cost of an alignment is given by a cost function, which we will call cost. The cost of an alignment is the sum over all i of cost(align_s[i], align_t[i]). The cost of aligning a letter with itself is always 0.

For example, given this cost table:

Letter from
$$s$$
a b c -
a 0 1 5 3
b 5 0 5 3
c 3 4 0 3
- 2 2 1 \cdot

The minimum-cost alignment between string s = 'acb' and t = 'baa' is given by:

align_s: -acb
align_t: ba-a

With a total cost of 5, which is lower than any other alignment.

This problem arises, for example, in DNA sequencing; given two strands of DNA, there are many sequences of mutations (insertions, deletions, etc.) which would have transformed one to the other; we would like to find the most probable. We know that certain mutations are more likely than other, and these probabilities are reflected in the cost table (the pair with higher likelihood has a lower cost).

1.2 TODO

In diffing.py:

fill_cell . You should fill in fill_cell(table, i, j, s, t, cost), which will be called once per cell. table is the table as filled in so far; use its get method to find these values. Your function should not mutate the table directly, but rather return a DiffingTableCell. cost is a function which encodes a cost function: it takes two characters and returns their cost. Each call to fill_cell should call it no more than four times. fill_cell should run in O(1) time.

cell_ordering. You should fill in **cell_ordering(n,m)**, which will be called once. n and m are the lengths of the strings s and t. **cell_ordering** should return a list of two-tuples; these are the coordinates of cells in the order you would like fill_cell to be called. No cell should be repeated, but you do not need to use all cells.

diff_from_table . You should fill in diff_from_table(s,t, table). s is the string being respaced, and table is the table that is already filled in. diff_from_table should run in O(n+m) time, and make no calls to cost.

Once you have finished implementing these 3 functions, you can do a quick sanity check by running the main given at the bottom of diffing.py which puts all the pieces together with our dynamic programming framework. See if the result is coherent with the example we gave you in this document.

Test harness To help you concentrate more on the actual algorithms part, we have also provided you a test harness test_diffing.py that runs tests on your diffing.py implementation using diffing_tests.txt as the input testfile. It is hence your responsibility to make sure your code works before submission. However, the test harness and the test cases we gave you are non-exhaustive, meaning passing these tests alone does not necessarily guarantee a perfect score.

2 Respacing

2.1 Problem statement

The respacing problem is to put spaces back into a string that has lost them, given a dictionary. For example, given the string "itwasthebestoftimes" and an English dictionary, we would like to reconstruct the original sentence: "it was the best of times".

2.2 TODO

In respacing.py:

fill_cell . You should fill in fill_cell(T, i, j, string, is_word), which will be called once per cell. T is the table as filled in so far; use its get method to find these values. Your function should not mutate T directly, but rather return a RespaceTableCell. is_word is a function which encodes a dictionary: given a string, it returns true or false, according to whether the string is a word. Each call to fill_cell should call it no more than once. fill_cell should run in O(N) time.

cell_ordering . You should fill in **cell_ordering(N)**, which will be called once. *N* is the length of the string to be respaced. **cell_ordering** should return a list of two-tuples; these are the coordinates of cells in the order you would like **fill_cell** to be called. No cell should be repeated, but you do not need to use all cells.

respace_from_table . You should fill in respace_from_table(s, table). s is the string being respaced, and table is the table that is already filled in. respace_from_table should run in $O(N^2)$ time, and make no calls to is_word.

Just like the first problem, an example for putting these all together with our dynamic programming framework is given in the main at the bottom of respacing.py.

Test harness Also we have also provided you a **non-exhaustive** test harness test_respace.py that runs tests on your respacing.py implementation using respace_tests.txt as the input testfile. Passing these tests alone does not necessarily guarantee a perfect score.

3 Dynamic Programming Framework

We have provided the skeleton code for you, in dynamic_programming.py, diffing.py, and respacing.py. It is designed to let you just think about the algorithm and worry less about the software engineering stuff, while also ensuring that the algorithm you design is in fact a dynamic program. You will write some code to fill in a dynamic programming table, and then to compute the final answer from this table.

The table for respacing is $(N+1) \times (N+1)$, where N is the length of the word to be respaced. Each cell may contain a single boolean and a single integer.

The table for diffing is $(|s|+1) \times (|t|+1)$, where s and t are the strings to be diffed and |s| stands for the length of string s. Each cell may contain a single integer and two characters (a character is a length-1 string).

4 Testing and logistics

4.1 Outside resources

We are asking you to come up with new algorithms using dynamic programming. We expect that finding an appropriate optimal substructure will be the bulk of the work – the code is fairly short once you have found one. You should NOT use or seek any resources that describe how to solve these problems, even in pseudocode.

4.2 Testing

In addition to the provided tests, we encourage you to write additional ones because in real-life software development, you will eventually have to learn to write tests like this yourself and I recommend reading up on Richard's slides from last year if you want to know more.

4.3 Python etc.

You can assume that all strings (words in respacing, input to respacing, and strings in diffing) consist of lowercase letters a,b,c,...z, have length at least 1, and are not None.

Please use python2.

Please do not use any additional imports.

You will need to submit your diffing.py and respacing.py on CMS. Please be careful not to swap them by accident!