

Urban area analysis using Statistics for SAR Imagery report

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1 Data select

The urban_area image in this report is select from Fig.3.4, in which we choose subimage of 100 pixels * 100 pixels in urban area and show as Figure 1. In this experiment, we only select raw intensity HH bands as our objective. So the codes is very simple and understandable.

```
> #The road of raw intensity HH bands#
> imagepath <- "/home/a421-2/wenzheng/Report-Statistics-SAR-master
/Data/Images/ESAR/"
> HH_Complex <- myread.ENVI(paste(imagepath,
                                   "ESAR97HH.DAT", sep = ""),
                             paste(imagepath, "ESAR97HH.hdr", sep = ""))
> HH_Intensity <- (Mod(HH_Complex))^2
> #The area of selected#
> urban_area <- HH_Intensity[1100:1199,1100:1199]
> vexample <- data.frame(HH=as.vector(urban_area))

> plot(imagematrix(equalize(urban_area)))
> imagematrixPNG(name = "./urban_area.png", imagematrix(equalize(urban_area)))

> vexample <- data.frame(HH=as.vector(urban_area))

> summary(vexample)
HH
Min.      :      3
1st Qu.:  16028
Median :  51070
Mean    : 193548
3rd Qu.: 181281
```

Max. :11946965

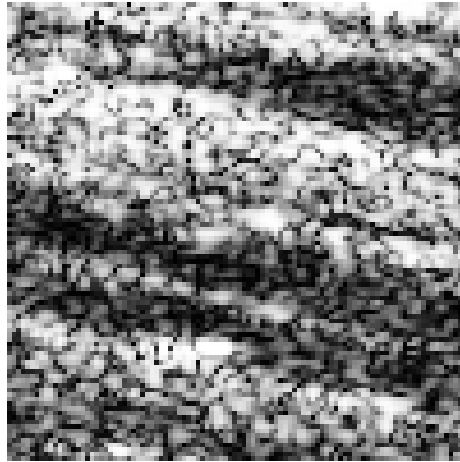


Figure 1: selected area

2 Analysis of Histogram

Consider the real part of the HH band of Figure 2 and Figure 3 whose histogram is the top leftmost. assume it is stored in the |HH.Complex| variable. These data are clearly not uniformly distributed.

We will randomly sample (fixing the pseudorandom number generator and the seed for reproducibility) one hundred observations, and then proceed to build its empirical function.

```
>binwidth_complete <- 2*IQR(vexample$HH)*length(vexample$HH)^(-1/3)

>ggplot(data=vexample, aes(x=HH)) +
  geom_histogram(aes(y=..density..),
    binwidth = binwidth_complete) +
  xlab(" Intensities") +
  ylab(" Proportions") +
  ggtitle(" Complete Histogram") +
  theme_few()
>ggsave(filename = "./HistogramExample.pdf")

> binwidth_complete
[1] 15340.79
```

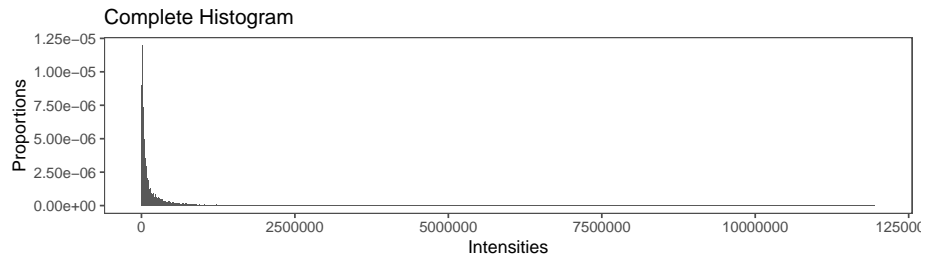


Figure 2: HistogramExample

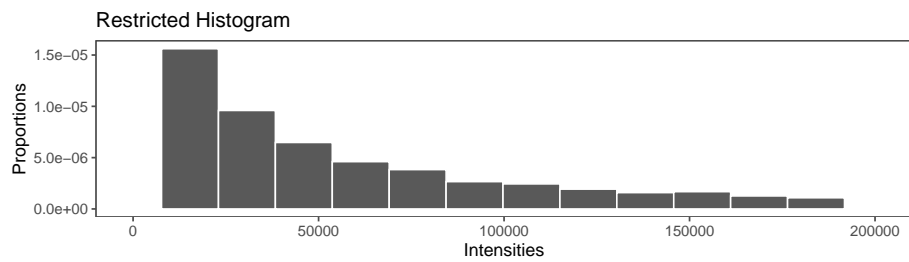


Figure 3: HistogramRestrictedExample

3 The result of estimation

The maximum likelihood estimation is used to evaluate the experimental data. Here we use only one function to achieve this function, and eventually we get a result value.

```
## Estimation
require(maxLik)

GI0.Estimator.mlm2 <- function(z, L) {
  m1 <- mean(z)
  m2 <- mean(z^2)
  m212 <- m2/m1^2

  a <- -2 - (L+1) / (L * m212)
  g <- m1 * (2 + (L+1) / (L * m212))

  return(list("alpha"=a, "gamma"=g))
}
```

```

}

estim.urban_area <- GI0.Estimator.mlm2(urban_area, 1)

LogLikelihoodLknown <- function(params) {

    p_alpha <- -abs(params[1])
    p_gamma <- abs(params[2])
    p_L <- abs(params[3])

    n <- length(z)

    return(
n*(lgamma(p_L-p_alpha) - p_alpha*log(p_gamma) - lgamma(-p_alpha)) +
      (p_alpha-p_L)*sum(log(p_gamma + z*p_L))
    )
}

estim.exampleML <- maxNR(LogLikelihoodLknown,
start=c(estim.urban_area$alpha, estim.urban_area$gamma,1),
activePar=c(TRUE,TRUE,FALSE))$estimate[1:2]

values:
binwidth_complete : 15340.7948389499
estim.exampleME : num [1:2] -42741 143335
mean : 1
N : 15
sigma2 : 1

> GI0.Estimator.mlm2
function(z, L) {
m1 <- mean(z)
m2 <- mean(z^2)
m212 <- m2/m1^2

a <- -2 - (L+1) / (L * m212)
g <- m1 * (2 + (L+1) / (L * m212))

return(list("alpha"=a, "gamma"=g))
}
<bytecode: 0x5566609e2b40>
> estim.urban_area
$alpha
[1] -2.279272

```

```
$gamma  
[1] 441148  
  
> estim.exampleML  
[1] -42740.89 143335.12
```

results all above