We have assumed that the mentioned document scanners are flatbed scanners and that the paper is flat. Due to the 'flat' nature of the scanner bed and paper, an affine motion model is sufficient for all cases, but the goal is to pick an 'optimal' motion model.

- (a) Rigid (translation + rotation) motion model is suitable. But, the only possibilities are the document being shifted/rotated on the scanner bed. As the document is same with no stretching or bending, modelling scaling/shearing is not required.
- (b) Rigid and equal scaling in X, Y directions is suitable. As X and Y resolutions for both scanners are same, let's assume the first scanner has a resolution  $p \times p$  and the second scanner's resolution is  $q \times q$ . Now, in addition to translation and rotation discussed in (a), as the scanners have different resolutions, the image of the first scanner has to be scaled by a factor of q/p in both the X direction as well as the Y direction. Again, as the document is same with no stretching or bending, modelling scaling/shearing is not required.
- (c) Rigid and unequal scaling in X, Y directions is suitable. To remove bleeding artifacts in the image of one side of the page, it has to be aligned with the image of the other side and vice versa. This requires us to perform a lateral inversion to the image of the other side. For this, the rigid model is not sufficient. As for a rigid model given by the equation 1; to perform a lateral inversion, the determinant of the matrix A must be non-negative. But it can be calculated that  $\det(A) = 1 \nleq 0$ .

$$\begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix} = \underbrace{\begin{bmatrix} \cos \theta & -\sin \theta & t_x \\ \sin \theta & \cos \theta & t_y \\ 0 & 0 & 1 \end{bmatrix}}_{A} \begin{bmatrix} x_1 - x_c \\ y_1 - y_c \\ 1 \end{bmatrix}$$
 (1)

Instead, we should first laterally invert the image of the other side by using a scaling factor of -1 in the X direction and 1 in the Y direction and then align the images using the rigid model making our system. This is achieved by incorporating a scaling matrix S into our equations as follows:

$$\begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix} = \underbrace{\begin{bmatrix} \cos \theta & -\sin \theta & t_x \\ \sin \theta & \cos \theta & t_y \\ 0 & 0 & 1 \end{bmatrix}}_{\mathbf{A}} \underbrace{\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}}_{\mathbf{C}} \begin{bmatrix} x_1 - x_c \\ y_1 - y_c \\ 1 \end{bmatrix}$$
(2)

This procedure should be repeated to remove bleeding from the image of the other side too. Again, as the document is same with no stretching or bending, modelling scaling/shearing is not required.

If a negative scaling factor is not supported by the alignment system then we will have to use the next best model which is the affine model shown to be sufficient.