A Cross-Domain Benchmark for Active Learning

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Abstract

Active Learning (AL) deals with identifying the most informative samples for labeling to reduce data annotation costs for supervised learning tasks. AL research suffers from the fact that lifts from literature generalize poorly and that only a small number of repetitions of experiments are conducted. To overcome this obstacles, we propose ALBench, the first active learning benchmark which includes tasks in computer vision, natural language processing and tabular learning. Furthermore, by providing an efficient greedy oracle, ALBench can be evaluated with 50 runs for each experiment. We will show, that both the cross-domain character and the large amount of repetitions are crucial for sophisticated evaluation of AL research. Concretely, we will show that the superiority of specific methods varies over the different domains, making it important to evaluate Active Learning with a cross-domain benchmark. Additionally, we show, that having a large amount of runs is crucial. With only conducting five runs as often done in the literature, the superiority of specific methods can strongly vary with the specific runs. This effect goes so far, that it may even happen that dedicated methods like margin-sampling are not able to outperform the random baseline.

1 Introduction

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Deep neural networks (NN) have produced state-of-the-art results on many important supervised learning tasks. Since Deep NNs usually require large amounts of labeled training data, Active Learning (AL) deals with selecting the most informative samples out of a large pool of unlabeled data, so that only these samples need to be labeled. It has been shown that a small labeled set of this nature can be used to train well-performing models In the last decade, many different algorithms for AL have been proposed and almost every method has reported lifts over all its predecessors, ¹ However, real insights into the current state of AL are hard to draw from these works, due to the following reasons: 1. These works do not use a standardized evaluation setting with fixed datasets and baseline approaches. 2. Due to cost reasons, a lot of works do only a small amount of experimental runs, hence it is questionable wether the superiority of a specific approach can be concluded from the conducted experiments. 3. The works are only evaluated in a specific domain, such as computer vision or language processing. However, AL is a general principle of supervised learning, and thus methods should be evaluated in multiple domains to assess their capabilities.

While multiple benchmark suites have been proposed to solve problem 1, to the best of our knowledge, all of them are either limited in the domains they consider or do not do enough runs for conclusive results Hence, the current state of the art in Active Learning is still not well-understood and principled shortcomings of different algorithms and wether they are domain-independent, are currently not identified.

¹Out of all considered algorithms for this paper, only BALD [7] did not claim a new SOTA performance in their result section.

Here we step in with *ALBench*, an active learning benchmark which covers multiple application domains and reports a large amount of runs per experiment, so that the significance of performance differences can can be estimated. Specifically, *ALBench* consists of datasets from computer vision, natural language processing and the tabular domain. We provide our datasets both in raw format as well as "embedded" by a fixed embedding model, enabling evaluation of AL methods in this semi-supervised setting. Furthermore, we propose two novel synthetic datasets to highlight general challenges for AL methods.

The applied evaluation protocol in ALBench uses 50 runs for each experiment. By having such a 43 large amount of runs, we can evaluate the significance of performance gaps and identify the best 44 performing approaches for each dataset as well as whole domains. Furthermore, we show that 45 the small amount of runs other works do in fact produce to misleading results. To be more spe-46 cific, we show that if only 3 restarts are employed for each experiment, the performance of specific methods strongly varies. As we will see, even the ranking of the different methods averaged 48 over many datasets fluctuates with the specific set of runs. This effect is so strong, that even for a 49 well-established method such as margin-sampling, it's performance can be significantly better and 50 significantly worse than random for the same dataset, depending on the seed. 51

To enable the computation of an oracle performance for a protocol with large amounts of restarts we propose a *greedy oracle function* which uses only a small amount of search steps to estimate the optimal solution. While being more time-efficient than established oracle functions, it possibly underestimates the real upper bound performance. However, as our experiments will show, it is still outperforming all current AL methods by at least 5% and thus is suitable as an upper bound.

Our experimental evaluation shows, that there exists no clear SOTA method for Active Learning. 57 The superiority of methods is strongly dataset- and domain-dependent with the outstanding observation, that the image domain works fundamentally different than the tabular and text domain. Here, 59 the best performing approach for text and tabular data, namely margin sampling, is significantly out-60 performed by least confident sampling, which does not belong to the top performing approaches in 61 any other domain. Thus, using the performance of Active Learning approaches on the image domain as a proxy of Active Learning in general, as it is often done [2, 19, 15, 10, 17], is questionable. To 63 further analyze performance of common methods, we propose *Honeypot* and *Diverging Sin*, two 64 synthetic datasets, designed to be challenging for naive decision-boundary- and clustering-based 65 approaches respectively. Hence, they provide insights in principled shortcomings of AL methods. 66

To sum up, *ALBench* is an experimental framework which includes an efficient oracle approximation, multiple application domains, enough repetitions to draw valid conclusions and two synthetic tasks to highlight shortcomings of AL methods. By being the first benchmark to proving these things in one code-base, we believe that *ALBench* is a major step forward of assessing the overall state of Active Learning research, independent of specific application domains. *ALBench* is publicly available under *anonymous*.

Our contributions include the following:

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- 1. We show that the small of repetitions that previous works have employed is not sufficient for meaningful conclusions. Sometimes even making it impossible to assess if a performance is above or below random.
- 2. We propose an efficient and performant oracle which is constructed iteratively in a greedy fashion, overcoming major computational hurdles.
- 3. We propose *IMTSBench*, the first general benchmark providing tasks in the domains of images, text and tabular learning. It further contains synthetic and pre-encoded data to allow for a sophisticated evaluation of AL methods. Our experiments show, that there is no clear state-of-the art method for active learning across different domains.
- 4. We propose *Honeypot* and *Diverging Sin*, two synthetic datasets designed to hinder active learning by naive decision-boundary- or clustering-based approaches respectively. Thus, they provide an important tool to identify shortcomings of existing AL methods.

Table 1: Comparison of our benchmark with the existing literature. Oracle curves serve as an approximation of the best possible AL algorithm. Including the encoded versions of our datasets we reach 14 datasets, without we have 9. "Semi" indicates whether the paper is employing any form of self- or semi-supervised learning. A "-" for repetitions means that we could not determine how often each experiment is repeated in the respective framework. *ALBench* is the only benchmark which reports over enough runs for meaningful results and considers all 5 domains.

Paper	Sampling	#Data	#Alg	Img	Txt	Tab	Synth	Semi	Oracle	Repetitions
Beck et al. [2]	batch	4	7	√	-	-	-	-	-	-
Hu et al. [9]	batch	5	13	✓	\checkmark	-	-	-	-	3
Zhou et al. [29]	batch	3	2	✓	\checkmark	-	-	-	✓	5
Zhan et al. [27]	sngl+batch	35	18	-	-	\checkmark	\checkmark	-	✓	10-100
Munjal et al. [19]	batch	2	8	✓	-	-	-	-	-	3
Li et al. [15]	batch	5	13	✓	-	-	-	\checkmark	-	-
Rauch et al. [22]	batch	11	5	-	\checkmark	-	-	-	-	5
Ji et al. [10]	batch -	3	8							
Lueth et al. [17]	batch	4	5	✓	-	-	-	\checkmark	-	3
Ours	sngl+batch	9(14)	11	✓	\checkmark	\checkmark	\checkmark	\checkmark	✓	50

36 2 Problem Description

Given two spaces \mathcal{X}, \mathcal{Y} , n = l + u data points with $l \in \mathbb{N}$ labeled examples $\mathcal{L} = \{(x_1, y_1), \ldots, (x_l, y_l)\}$, $u \in \mathbb{N}$ unlabeled examples $\mathcal{U} = \{x_{l+1}, \ldots, x_n\}$, a model $\hat{y} : \mathcal{X} \to \mathcal{Y}$, a budget $\mathbb{N} \ni b \le u$ and an annotator $A : \mathcal{X} \to \mathcal{Y}$ that can label x. We call $x \in \mathcal{X}, y \in \mathcal{Y}$ predictors and labels respectively where (x, y) are drawn from an unknown distribution ρ . Find an acquisition function $\Omega : \mathcal{U}^{(i)}, \mathcal{L}^{(i)} \mapsto x^{(i)} \in \mathcal{U}^{(i)}$ that iteratively selects the next unlabeled point $x^{(i)}$ for labeling

$$\mathcal{L}^{(i+1)} \leftarrow \mathcal{L}^{(i)} \cup \{ \left(x^{(i)}, A(x^{(i)}) \right) \}$$
$$\mathcal{U}^{(i+1)} \leftarrow \mathcal{U}^{(i)} \setminus \left\{ x^{(i)} \right\}$$

with $\mathcal{U}^{(0)} = \operatorname{seed}(\mathcal{U}, s)$ and $\mathcal{L}^{(0)} = \left(\mathcal{U}_i^{(0)}, A(\mathcal{U}_i^{(0)})\right)$ $i \in [1, \dots, s]$, where $\operatorname{seed}(\mathcal{U}, s)$ selects s points per class for the initial labeled set.

So that the average expected loss $\ell: \mathcal{Y} \times \mathcal{Y} \to \mathbb{R}$ of a machine learning algorithm fitting $\hat{y}^{(i)}$ on the respective labeled set $\mathcal{L}^{(i)}$ is minimal:

$$\min \quad \frac{1}{B} \sum_{i=0}^{B} \mathbb{E}_{(x,y) \sim \rho} \ell(y, \hat{y}^{(i)})$$

93 Related Work

While multiple benchmark suites have been proposed for Active Learning, none of them provide experiments for more than two domains. The authors of [2], [19], [15], [10] and [17] even focus exclusively on the image domain. Especially the tabular domain is underrepresented in preceding benchmarks, as only [28] provides experiments for it. Experiments on the interplay between AL and semi-supervised learning are similarly under-researched, as only two works exist [15, 17], both of them only using images. An oracle algorithm has been proposed by two works [29, 28]. Both of these algorithms rely on search and are computationally very expensive, while our proposed method efficiently can be constructed sequentially. The two closest related works to this benchmark are [10] and [17], who also place a much higher emphasis on the problem of evaluating AL algorithms under many forms of variance than their predecessors (indicated in Tab. 1 by a dashed line). The authors of [10] posed a total of 12 "recommendations" for reliable evaluation of AL algorithms. We largely adapt the proposed recommendations of [10] and extend their work to multiple domains, batch sizes and comparisons. For a complete list of the recommendations and our implementation of them, please refer to App. A. This work also pays attention to the so-called "pitfalls" of AL evaluation proposed in [17]. For a complete list of the pitfalls and our implementation of them, please refer to

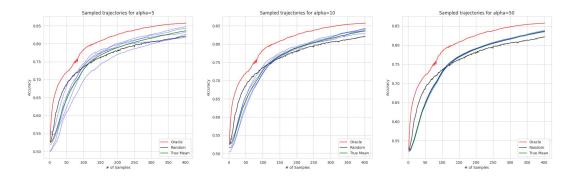


Figure 1: Random draws from a pool of 100 runs for margin sampling on the Splice dataset with different numbers of repetitions ($\alpha = \{5, 10, 50\}$). Green curves are the mean performance of all 100 runs, while the samples are blue. Even with 5 or 10 repetitions, we can observe that single draws for margin sampling display below-random performance (black), while the true mean should be above random.

App. B. To the best of our knowledge, we are the first to extend reliable SOTA (based on [10, 17]) experimentation to a total of 5 data domains and a high number of restarts per experiment.

4 Few Repetitions are not Sufficient for Meaningful Results

To evaluate how many restarts are necessary to obtain conclusive results in an AL experiment, we 112 computed 100 runs of our top-performing algorithm on one dataset. Our best algorithm is margin 113 sampling and we chose the Splice dataset for its average size and complexity. 114 This allows us firstly, to obtain a very strong estimation of the "true" average performance of margin 115 sampling on this dataset and secondly, to draw subsets from this pool of 100 runs. Setting the size 116 of our draws to α and sampling uniformly, we can approximate a cross-validation process with α 117 restarts. Each of these draws can be interpreted as a reported result in AL literature where the 118 authors employed α restarts. Figure 1 shows the "true" mean performance of margin sampling 119 (green) in relation to random sampling (black) and the oracle performance (red). We display 5 120 random draws of size α in blue. We can observe that even for a relatively high number of restarts the 121 variance between the samples is extremely high, resulting in some performance curves being worse 122 that random and some being significantly better. When setting $\alpha = 50$ we observe all samples to 123 converge close to the true mean performance. In addition to this motivating example, we carried 124 out our main evaluation (Tab. 3) multiple times by uniformly sampling 3 random from our available 125 runs and comparing the results. We found significant differences in the performance of acquisition 126 functions on individual datasets, as well as permutations in the final ranking. This partly explains 127 the ongoing difficulties in reproducing results for AL experiments and benchmarks. The details can 128 be found in App. D. For this benchmark we employ 50 restarts of every experiment. 129

4.1 Seeding vs. Restarts

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Considering the high computational cost of 50 repetitions, another approach to ensure consistency between experiments would be to reduce the amount of variance in the experiment by keeping as many subsystems (weight initialization, data splits, etc.) as possible fixed with specialized seeding. We describe a novel seeding strategy in Appendix H that creates 3 separate Random Number Generators (RNG) based on 3 different seeds. In short, we introduce three different seeds: s_{Ω} for the AL algorithm, $s_{\mathcal{D}}$ for dataset splitting and mini-batch sampling, and s_{θ} for model initialization and sampling of dropout masks. Unless stated otherwise, we will keep s_{Ω} fixed, while $s_{\mathcal{D}}$ and s_{θ} are incremented by 1 between restarts to introduce stochasticity into our framework. While this seeding strategy is capable of controlling the amount variance in the experiment, previous works have noted

that an actively sampled, labeled set does not generalize well between model architectures or even different initializations of the same model ([29, 16]), providing a bad approximation of the quality of an AL algorithm (i.e. measured performances for an algorithm might not even transfer to a different model initialization). Hence, we opt for letting the subsystems vary (by increasing s_D and s_θ) and combine that with a high number of restarts to obtain a good average of the generalization performance of each AL algorithm.

Where a high number of restarts is computationally not feasible, we advise to additionally keep

5 ALBench: A Cross-Domain Active Learning Benchmark

either $s_{\mathcal{D}}$ or s_{θ} (or both) fixed.

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A detailed description of the preprocessing of each dataset can be found in Appendix K.

Tabular: AL research conducted on tabular data is sparse (only [1] from the considered baseline 150 papers). We, therefore, introduce a set of tabular datasets that we selected according to the following 151 criteria: (i) They should be solvable by medium-sized models in under 1000 samples, (ii) the gap be-152 tween most AL algorithms and random sampling should be significant (potential for AL is present) 153 and (iii) the gap between the AL algorithms and our oracle should also be significant (research on 154 these datasets can produce further lifts). We use **Splice**, **DNA** and **USPS** from LibSVMTools [20]. 155 **Image:** We use **FashionMNIST** [25] and **Cifar10** [13], since both are widely used in AL literature. 156 Text: We use News Category [18] and TopV2 [6]. Text datasets have seen less attention in AL 157 research, but most of the papers that evaluate on text ([9], [29]) use at least one of these datasets. 158 159

We would like to point out that these datasets are selected for speed of computation (both in terms of the required classifier and the necessary budget to solve the dataset). However, similar to our argumentation for picking smaller classifiers, we are solely focused on comparing different AL algorithms in this paper and do not aim to develop novel classification models on these datasets. Our assumption is that a well-performing algorithm in our benchmark will also generalize well to larger real-world datasets, because we included multiple different data domains and classifier sizes in our experiments.

Adapting the semi-supervised setting from [8], we offer all our datasets un-encoded (normal) as well 166 as pre-encoded by a fixed embedding model that was trained by unsupervised contrastive learning. 167 The text datasets are an exception to this, as they are only offered in their encoded form. Pre-encoded 168 datasets enable us to test small query sizes on more complex datasets like Cifar10 and FashionM-169 nist. They also serve the purpose of investigating the interplay between self-supervised learning 170 techniques and AL, as well as alleviating the cold-start problem described in [17] as they require a 171 way smaller seed set. The classification model for every encoded dataset is a single linear layer with 172 softmax activation. The embedding model was trained with the SimCLR [5] algorithm adopting the 173 protocol from [8]. To ensure that enough information from the data is encoded by our embedding 174 model, the quality of embeddings during pretext training was measured after each epoch. To this 175 end, we attached a linear classification head to the encoder, fine-tuned it to the data and evaluated 176 this classifier for test accuracy. The checkpoint of each encoder model will be provided together 177 with the framework. 178

Every dataset has a fixed size for the seed set of 1 sample per class, with the only exceptions being un-encoded FashionMnist and Cifar10 with 100 examples per class to alleviate the cold-start problem in these complex domains.

5.1 Batch Sizes

We selected batch sizes for each dataset to accommodate the widest range possible that results in a reasonable runtime for low batch sizes and allows for at least 4 round of data acquisition for high batch sizes. The available batch sizes per dataset can be found in Table 2.

5.2 Realism vs. Variance

Table 2: Employed model, chosen budget and available batch sizes for each dataset

We would like to point out that some design choices for this framework prohibit direct trans-fer of our results to practical ap-plications. This is a conscious choice, as we think that this is a necessary trade-off between re-alism and experiment variance. We would like to highlight the following design decisions:

	Model	В	1	5	20	50	100	500	1K
Enc. DNA	Linear	40	0	0					
Enc. Splice	Linear	100	0	0	О	О			
TopV2	BiLSTM	200	0	0	О	О			
Splice	MLP	400	0	0	0	0	О		
DNA	MLP	300	0	0	0	0	О		
USPS	MLP	400	0	0	О	О	О		
Enc. Cifar10	Linear	450	0	0	О	О	О		
Enc. FMnist	Linear	500	0	О	О	О	О		
Enc. USPS	Linear	600	0	0	0	0	О		
News	BiLSTM	3K			О	О	О	О	
FMnist	ResNet18	10K						o	О
Cifar10	ResNet18	10K						o	o

(i) Creating test and validation splits from the full dataset rather than only the labeled seed set. Fully fledged test and validation splits are unobtainable in practice, but they not only provide a better approximation of the algorithms generalization performance, but also a better foundation for hyper-parameter tuning, which is bound to reduce variance in the experiment.

(ii) Choosing smaller classifiers instead of SOTA models. Since we are not interested in archiving a new SOTA in any classification problem, we instead opt to use smaller classifiers for the following reasons: Smaller classifiers generally exhibit more stable training behavior, on average require fewer sampled datapoints to reach their full-dataset-performance and have faster training times. For every dataset, the chosen architecture's hyperparameters are optimized to archive maximum full-dataset performance. Generally, we use MLPs for tabular, RestNet18 for image and BiLSTMs for text datasets. Every encoded dataset is classified by a single linear layer with softmax activation. The used model for each dataset can be found in Tab. 2. For a detailed description and employed hyperparameters please refer to Appendix K.

5.3 Evaluation Protocol

Following [29], the quality of an AL algorithm is evaluated by an "anytime protocol" that incorporates classification performance at every iteration, as opposed to evaluating final performance after the budget is exhausted. We employ the normalized area under the accuracy curve (AUC):

$$AUC(\mathcal{D}_{test}, \hat{y}, B) := \frac{1}{B} \sum_{i=1}^{B} Acc(\mathcal{D}_{test}, \hat{y}^{(i)})$$
(1)

The AUC incorporates performance in early stages (low budget) as well as capabilities to push the classifier in later stages (high budget). AL algorithms have to perform well in both scenarios.

Since AUC is still influenced by the budget, we define a set of rules to set this hyperparameter upfront, so that we are not favoring a subset of algorithms by handcrafting a budget. In this work, we choose the budget per dataset to be the first point at which one of 2 stopping conditions apply: (i) an algorithm (except Oracle) manages to reach 99% of the full-dataset-performance (using the smallest query size) or (ii) the best algorithm (except oracle) did not improve the classifier's accuracy by at least 2% in the last 20% of iterations. The first rule follows [10], while the second rule prevents excessive budgets for cases with diminishing returns in the budget. The resulting budgets can be found in Tab. 2.

As described in Sec. 4, we restart each experiment multiple times. Each restart retains the train/test split (often given by the dataset itself), but creates a new validation split that is sampled (based on $s_{\mathcal{D}}$) from the entire dataset (not just the seed set $\mathcal{L}^{(0)}$).

Apart from plotting standard performance curves and reporting their AUC values per dataset in App. G, we primarily rely on ranks to aggregate the performance of an acquisition function across datasets. For each dataset and query size, the AUC values of all acquisition functions are sorted and assigned a rank based on position, with the best rank being 1. These ranks can safely be averages across datasets as they are no longer subjected to scaling differences of each dataset. Additionally, we employ Critical Difference (CD) diagrams (like Fig. 2) for statistical testing. CD diagrams use the Wilcoxon signed-rank test, which is a variant of the paired T-test, to find significant differences of ranks between acquisition functions. For these diagrams, each combination of dataset, query

size and run is considered a separate experiment, i.e. the results of Dataset1-QuerySize1-run5
of an acquisition function x is only compared to the results of Dataset1-QuerySize1-run5 of
acquisition function y. Due to the large number of restarts and the wide range of datasets and query
sizes, we can provide very accurate significance tests. For a detailed description of how every CD
diagram is created, please refer to App. F.

240 6 A Greedy Oracle Algorithm

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A oracle method for AL tries to find the oracle set \mathcal{O}_b for a given dataset, model, and training procedure that induces the highest AUC score for a given budget. However, since this combinatorial problem is computationally infeasible for realistic datasets, previous works have proposed approximations to this oracle sequence. [29] used simulated annealing to search for the optimal subset and used the best solution found after a fixed time budget. Even though their reported performance curves display a significant lift over all other acquisition functions, we found the computational cost of reproducing this oracle for all our datasets to be prohibitive (The authors reported the search to take several days per dataset on 8 V100 GPUs). In this paper, we propose a greedy oracle algorithm that constructs an approximation of the optimal set in an iterative fashion. Our oracle algorithm evaluates every data point $u_k = \text{unif}(\mathcal{U})$ $k \in [1 \dots \tau]$ in a subsample of unlabeled points by recovering the label, fitting the classifier \hat{y} on $\mathcal{L}^{(i)} \cup \{u_k\}$ and directly measuring the resulting test performance. The data point that incurs the largest lift in test performance is selected and added to the labeled pool for that iteration. Due to the algorithms greedy nature (just considering the next point to pick), our oracle frequently encounters situations where every point in u_k would incur a negative lift (worsening the test performance). This can happen, for example, if the oracle picked a labeled set that enables the classifier to correctly classify a big portion of easy samples in the test set, but now fails to find the next single unlabeled point that would enable the classifier to succeed on one of the hard samples. This leads to a situation, where no point can immediately incur an increase in test performance and therefore the selected data point can be considered random. To circumvent this problem, we use our best-performing acquisition function (margin sampling [24]) as a fallback option for the oracle. Whenever the oracle does not find an unlabeled point that results in an increase in performance, it defaults to margin sampling in that iteration. The resulting greedy algorithm constructs an approximation of the optimal labeled set that consistently outperforms all other algorithms by a significant margin, while requiring relatively low computational cost $(\mathcal{O}(B\tau))$. We fix $\tau=20$ in this work, as this gave us an average lift of 5% over the best performing acquisition function per dataset (which is significant for AL settings) and we expect diminishing returns for larger τ . The pseudocode for our oracle can be found in App. L. Even though our proposed algorithm is more efficient than other approaches, the computational costs for high budget datasets like Cifar10 and FashionMnist meant that we could not compute the oracle for all 10000 datapoints. To still provide an oracle for these two datasets, we select two points per iteration instead of one and stop the oracle computation at a budget of 2000. The rest of the curve is forecast with a simple linear regression that asymptotically approaches the upper bound performance of the dataset. A detailed description can be found in App. I.

[Thorben]
Ich habe die
Erklärung für
den Fallback
im Oracle
neu gemacht.
Ist das
verständlich?

Da wir den Fallback haben, sollten wir das Oracle vielleicht einfach als Erweiterung von Margin-Sampling verkaufen?

7 Experiments

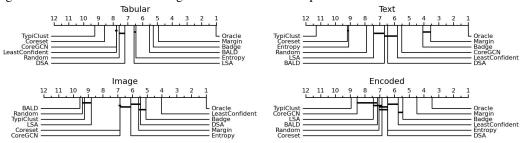
7.1 Implementation Details

At each iteration i the acquisition function Ω picks an unlabeled datapoint based on a fixed set of information $\{\mathcal{L}^{(i)}, \mathcal{U}^{(i)}, B, |\mathcal{L}^{(i)}| - |\mathcal{L}^{(1)}|, \operatorname{acc}^{(i)}, \operatorname{acc}^{(1)}, \hat{y}^{(i)}, \operatorname{opt}_{\hat{y}}\}$, where $\operatorname{opt}_{\hat{y}}$ is the optimizer used to fit $\hat{y}^{(i)}$. This set grants full access to the labeled and unlabeled set, as well as all parameters of the classifier and the optimizer. Additionally, we provide meta-information, like the size of the seed set through $|\mathcal{L}^{(i)}| - |\mathcal{L}^{(1)}|$, the remaining budget though the addition of B and the classifiers potential though $\operatorname{acc}^{(1)}$ and $\operatorname{acc}^{(i)}$. We allow acquisition functions to derive information from this set, e.g. predictions of the classifier $\hat{y}^{(i)}(x)$; $x \in \mathcal{U}^{(i)} \cup \mathcal{L}^{(i)}$, clustering, or even training additional models.

Table 3: Performances for acquisition functions on real-world datasets, aggregated for un-encoded and encoded datasets. Performance is shown as average ranks over restarts (1.0 is the best rank). Algorithms are sorted by aggregated performance on un-encoded datasets.

	Splice	DNA	USPS	Cfr10	FMnist	TopV2	News	Un-enc.	Enc.
Oracle	1.0 ± 0.01	1.0 ± 0.01	1.0 ± 0.0	1.0 ± 0.0	1.0 ± 0.0	1.0 ± 0.01	1.0 ± 0.0	1.0	2.0
Margin	6.6 ± 0.02	4.3 ± 0.01	2.1 ± 0.01	6.3 ± 0.01	4.4 ± 0.0	2.4 ± 0.01	3.7 ± 0.0	4.3	4.2
Badge	5.2 ± 0.01	6.3 ± 0.01	2.9 ± 0.01	5.2 ± 0.01	4.7 ± 0.0	3.3 ± 0.01	3.5 ± 0.0	4.5	5.4
LeastConf	9.2 ± 0.02	10.3 ± 0.02	8.1 ± 0.02	2.1 ± 0.01	4.0 ± 0.0	7.9 ± 0.02	3.0 ± 0.01	6.4	6.5
DSA	7.4 ± 0.02	7.3 ± 0.01	7.5 ± 0.01	5.4 ± 0.01	5.1 ± 0.0	6.0 ± 0.02	7.3 ± 0.01	6.6	6.7
BALD	4.0 ± 0.01	4.7 ± 0.01	5.4 ± 0.01	12.0 ± 0.01	7.6 ± 0.0	7.6 ± 0.02	5.0 ± 0.0	6.6	7.6
CoreGCN	6.9 ± 0.01	4.9 ± 0.01	10.4 ± 0.01	7.6 ± 0.01	6.5 ± 0.01	4.0 ± 0.01	6.8 ± 0.0	6.7	8.2
Entropy	6.6 ± 0.02	3.9 ± 0.01	7.6 ± 0.01	7.6 ± 0.01	4.9 ± 0.01	9.8 ± 0.02	9.6 ± 0.0	7.1	6.5
LSA	6.1 ± 0.01	6.8 ± 0.01	5.3 ± 0.01	7.7 ± 0.01	10.6 ± 0.01	7.5 ± 0.01	7.3 ± 0.01	7.3	7.5
Random	9.0 ± 0.01	9.3 ± 0.01	5.3 ± 0.01	8.4 ± 0.01	11.1 ± 0.0	7.9 ± 0.01	8.0 ± 0.0	8.4	6.9
Coreset	7.1 ± 0.01	9.0 ± 0.01	10.5 ± 0.01	6.8 ± 0.01	7.1 ± 0.0	8.5 ± 0.02	10.8 ± 0.01	8.5	7.2
TypiClust	8.8 ± 0.01	10.2 ± 0.01	12.0 ± 0.02	7.9 ± 0.01	11.0 ± 0.01	12.0 ± 0.02	12.0 ± 0.01	10.5	9.2

Figure 2: Ranks of each acquisition function aggregated by domain. Horizontal bars indicate a **non**-significant rank difference. The significance is tested via a paired-t-test with $\alpha = 0.05$.



However, the algorithm may not incorporate external information e.g. other datasets, queries to recover additional labels, additional training steps for \hat{y} , or the test/validation set.

For our study we selected acquisition functions with good performances reported by multiple different sources that can work with the set of information stated above. For a list of all acquisition functions, please refer to Table 3, with detailed descriptions being found in Appendix C.

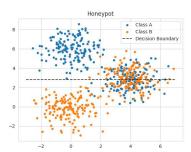
The model \hat{y} can be trained in two ways. Either the parameters of the model are reset to a fixed initial setting $\hat{y}^{(0)}$ after each AL iteration and the classifier is trained from scratch with the updated labeled set $\mathcal{L}^{(i)}$, or the previous state $\hat{y}^{(i-1)}$ is retained and the classifier is fine-tuned on $\mathcal{L}^{(i)}$ for a reduced number of epochs. In this work, we use the fine-tuning method for un-encoded datasets to save computational time, while we use the from-scratch training for embedded datasets since they have very small classifiers and this approach generally produces better results. Our fine-tuning scheme always trains for at least one epoch and employs an aggressive early stopping with a patience of 2 afterwards.

7.2 Results on Real-world Data

need for diverse data domains in AL benchmarking.

In Table 3 we provide the rank of each acquisition function per dataset and averaged for each (un)encoded dataset. Please note, that for Tab 3 we are averaging not only over runs, but also over query sizes per dataset. For the results per query size, please refer to App. E.

As stated in contribution C4, our results on real-world data shows significant differences in the performance of the tested algorithms between data domains. Not only do some algorithms overperform on some domains (like least confidence sampling on Images), but the Top-3 of algorithms (except Oracle) does not contain the same three algorithms for any two domains. Most interestingly, the image domain, which received the most attention in benchmarking so far could even be considered an outlier, as this is the only domain where the Top-1 algorithm changes. This highlights the dire



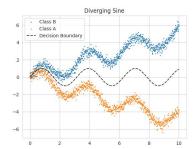


Figure 3: Synthetic "Honeypot" and "Diverging Sine" datasets. The optimal decision boundary is not part of the dataset and serves only as a visual guide.

8 Honeypot and Diverging Sine

AL approaches can be categorized into two types, uncertainty and geometric approaches. Typical members of the first category are variants of uncertainty sampling like entropy-, margin and least-confident-sampling [24] as well as BALD [7]. Typical members of the second category are clustering approaches like Coreset [23], BADGE [1] and TypiClust [8]. Both types of algorithms have principled shortcomings in terms of the utilized information that makes them unsuitable for certain data distributions. To test for these specific shortcomings, we created two synthetic datasets, namely "Honeypot" and "Diverging Sine", that are hard to solve for methods focused on the classifier's decision boundary or data clustering respectively. To avoid algorithms memorizing these datasets they are generated from scratch for each experiment, depending on $s_{\mathcal{D}}$.

Honeypot creates to two easy to distinguish clusters with 150 samples each and one overlapping "honeypot" that represents a noisy region of the dataset with potentially miss-labeled, miss-measured or generally adverse samples. This honeypot contains 150 samples of each class, creating a balance of 50% beneficial samples and 50% adverse samples in the dataset. The honeypot is located on the likely decision boundary of a classifier that is trained on the beneficial samples to maximize its negative impact on purely uncertainty based acquisition functions. Diverging Sine samples the datapoints for each class from two diverging sinusoidal functions that are originating from the same y-intercept. This creates a challenging region one the left hand side, where a lot of datapoints need to be sampled and an easy region on the right hand side, where very few datapoints are enough. The repeating nature of a sin function encourages diversity based acquisition functions to equally sample the entire length, drastically oversampling the right hand side of the dataset. Each class has 500 datapoints. Both datasets have a budget of B=60 and are tested with query sizes 1 and 5.

Results for the Honeypot dataset reveal expected shortcomings of uncertainty sampling algorithms like margin, entropy and least confident sampling as well as BALD. In addition, BADGE is underperforming for this dataset compared to real-world data. Results for Diverging Sine also confirm expected behavior, as clustering algorithms (Coreset, TypiClust) fall behind uncertainty algorithms (Entropy-, Margin-Sampling), with the exception of BADGE.

We provide a very small ablation study on the importance of the embeddings by testing a version of
Coreset and TypiClust on this dataset that does not use the embeddings produced by the classification model, but rather clusters the data directly. "Coreset Raw" and "TypiClust Raw" both perform
worse than their embedding-based counterpart.

8.1 Results

Our results on Honeypot reveal principled shortcomings for the two best algorithms in BADGE and margin sampling. Both are vulnerable to adverse samples or simply measurement noise, which highlights the need for further research in this area.

Finally, the fact that BADGE is able to perform well on Diverging Sine highlights the importance of

Figure 4: Results for all acquisition functions on both synthetic datasets.



embeddings for the clustering algorithms, as the so-called gradient embedding from BADGE seems to be able to encode uncertainty information, guiding the selection into the left hand regions of the dataset. We also show that embeddings are generally useful for this dataset, by providing results for "Coreset Raw" and "TypiClust Raw".

9 Conclusion

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We strongly advocate to test newly proposed AL algorithms not only on a wide variety of real data domains, but also to pay close attention to the Honeypot and Diverging Sine datasets to reveal principled shortcomings of the algorithm in question. Both tasks can be easily carried out by implementing the new acquisition function into our code base.

354 Acknowledgement anonymous

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429 A AL Recommendations from Ji et al.

430 TODO

B AL Pitfalls from Lueth et al.

432 TODO

433 C Acquistion Functions

Uncertainty Sampling tries to find the sample that the classifier is most uncertain about by computing heuristics of the class probabilities. For our benchmark, we use entropy and margin (a.k.a. best-vs-second-best) sampling.

BALD [12] applies the query-by-committee strategy of model ensembles to a single model by interpreting the classifier's parameters as distributions and then sample multiple outputs from them via Monte-Carlo dropout.

BADGE [1] uses gradient embeddings of unlabeled points to select samples where the classifier is expected to change a lot. The higher the magnitude of the gradient the higher the expected improvement in model performance.

Coreset [23] employs K-Means clustering trying to cover the whole data distribution. Selects the unlabeled sample that is the furthest away from all cluster centers. Clustering is done in a semantically meaningful space by encoding the data with the current classifier \hat{y} . In this work, we use the greedy variant of Coreset.

TypiClust [8] relies on clustering similar to Coreset, but proposes a new measure called "Typicality" to select unlabeled samples. It selects points that are in the densest regions of clusters that do not contain labeled samples yet. Clustering is done in a semantically meaningful space by encoding the data with the current classifier \hat{y} . It has to be pointed out that TypiClust was designed for low-budget scenarios, but we think it is still worthwhile to test and compare this algorithm with higher budgets.

453 Core-GCN [3] TODO
 454 DSA/LSA [11] TODO

455 Excluded Algorithms

Learning Loss for AL [26] Introduces an updated training of the classification model with an auxiliary loss and therefore cannot be compared fairly against classification models without this boosted training regime.

459 Reinforcement Learning Algorithms

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D Difference of Ranks with 3 Repetitions

Table 4 and Table 5 follow the exact same computation of ranks that created the main result (Table 3) with the only difference being a reduced number of runs per acquisition function. For each table we sampled 3 runs uniformly at random from the available 50 per acquisition function.

We can observe significant differences between the two tables:

Purple: A multitude of rank differences of acquisition functions for specific datasets, some as high as 4.7 ranks for TypiClust on the Splice dataset

Olive: Well separated acquisition functions in Tab. 5 (Margin and BADGE) are almost indistinguishable in Tab 4

470 Red: BALD lost 2 places in the overall ranking and Entropy gained 2

Even though the overall ordering of acquisition functions stayed relatively unchanged due to the averaging across many datasets, each individual dataset was subject to drastic permutations. This highlights the need for many repetitions in AL experiments.

Table 4: Ranks of all acquisition functions per dataset. First random draw of 3 runs from the overall pool of 50.

	Splice	DNA	USPS	Cifar10	FMnist	TopV2	News	Unencoded	Encoded
Oracle	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	2.1
Margin	6.0	7.3	2.0	6.7	5.3	2.3	3.3	4.7	4.4
Badge	6.0	7.3	3.0	6.7	5.0	3.3	4.0	5.0	5.3
BALD	3.3	4.7	5.3	12.0	7.0	6.3	4.3	6.1	7.9
CoreGCN	8.7	3.7	10.7	6.3	5.3	4.0	7.7	6.6	9.1
DSA	8.3	6.3	7.7	7.7	4.3	6.7	6.7	6.8	6.1
LeastConf	10.0	12.0	8.0	3.0	4.3	9.3	2.3	7.0	6.7
LSA	5.7	6.7	5.3	6.7	10.7	7.7	7.0	7.1	6.3
Entropy	11.0	3.3	7.3	4.0	6.7	8.3	9.7	7.2	7.0
Random	7.7	8.7	5.3	8.0	11.0	8.0	9.0	8.2	6.3
Coreset	4.7	10.3	10.3	7.7	6.0	9.0	11.0	8.4	7.2
TypiClust	5.7	6.7	12.0	8.3	11.3	12.0	12.0	9.7	9.7

Table 5: Ranks of all acquisition functions per dataset. Second random draw of 3 runs from the overall pool of 50.

	Splice	DNA	USPS	Cifar10	FMnist	TopV2	News	Unencoded	Encoded
Oracle	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	2.4
Margin	6.0	3.3	2.0	5.7	2.0	2.0	4.3	3.6	3.8
Badge	6.0	9.0	3.0	3.0	5.7	3.7	3.3	4.8	4.9
CoreGCN	4.3	6.3	10.3	7.3	5.3	5.7	5.3	6.4	8.1
DSA	8.7	7.3	7.3	6.0	4.3	5.3	6.0	6.4	6.5
BALD	4.7	4.0	4.7	12.0	7.3	6.7	6.7	6.6	7.5
Entropy	6.7	4.7	7.7	5.3	5.0	7.3	9.3	6.6	6.8
LeastConf	7.7	10.0	8.3	3.3	6.0	8.7	3.0	6.7	7.3
LSA	7.7	5.3	6.0	9.0	11.0	9.0	7.3	7.9	7.5
Random	9.3	8.0	5.0	8.7	11.7	8.3	8.7	8.5	7.6
Coreset	6.0	10.7	10.7	8.0	8.3	8.3	11.0	9.0	6.3
TypiClust	10.0	8.3	12.0	8.7	10.3	12.0	12.0	10.5	9.4

474 E AUCs by Query Size

Table 6: AUC values for each dataset that supports query size 1.

	Splice	Callage Canadad	DNA	DNAEncoded	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	Diameter-Circ	ThereClass
		SpliceEncoded								DivergingSin	ThreeClust
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.721+-0.013	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.957+-0.009	0.783+-0.03
Margin	0.769+-0.021	0.678+-0.032	0.806 + -0.013	0.642+-0.047	0.858+-0.006	0.426+-0.038	0.653+-0.013	0.68+-0.012	0.861 + -0.009	0.941 + -0.018	0.704+-0.074
Badge	0.767+-0.02	0.661 + -0.026	0.78 + -0.014	0.642+-0.046	0.83 + -0.008	0.371+-0.035	0.656+-0.013	0.68+-0.009	0.826 + -0.024	0.941+-0.017	0.69 + -0.083
LeastConfident	0.779+-0.019	0.68+-0.032	0.809 + -0.01	0.629 + -0.05	0.846 + -0.009	0.421+-0.039	0.668+-0.014	0.685+-0.009	0.843 + -0.013	0.94 + -0.016	0.692+-0.094
DSA	0.766+-0.021	0.691+-0.022	0.803 + -0.01	0.646+-0.032	0.829 + -0.01	0.431 + -0.05	0.663+-0.014	0.679 + -0.01	0.844+-0.017	0.941+-0.014	0.731 + -0.032
BALD	0.78+-0.014	0.649+-0.04	0.784 + -0.01	0.632 + -0.042	0.819 + -0.01	0.242+-0.046	0.666+-0.014	0.644 + -0.018	0.815 + -0.024	0.928+-0.014	0.698+-0.043
CoreGCN	0.765+-0.021	0.686+-0.023	0.804 + -0.012	0.646+-0.03	0.753 + -0.016	0.39+-0.044	0.623+-0.018	0.647+-0.012	0.85 + -0.01	0.938+-0.014	0.731 + -0.028
Entropy	0.768+-0.022	0.678+-0.035	0.812+-0.013	0.635+-0.045	0.83 + -0.011	0.399+-0.035	0.663+-0.013	0.681+-0.011	0.815+-0.021	0.942+-0.017	0.696+-0.083
LSA	0.772+-0.016	0.68+-0.026	0.787+-0.012	0.618+-0.036	0.821 + -0.009	0.422 + -0.037	0.613+-0.014	0.642+-0.012	0.816+-0.013	0.932+-0.016	0.727+-0.033
Random	0.76+-0.016	0.674+-0.027	0.774 + -0.013	0.63 + -0.035	0.823 + -0.009	0.404+-0.036	0.613+-0.014	0.639+-0.013	0.815+-0.012	0.933+-0.017	0.721+-0.036
Coreset	0.772+-0.016	0.69 + -0.017	0.79 + -0.012	0.638+-0.041	0.767+-0.016	0.404+-0.046	0.659+-0.011	0.684+-0.009	0.826+-0.022	0.937+-0.014	0.73 + -0.031
TypiClust	0.762+-0.016	0.685 + -0.025	0.778 + -0.01	0.663 + -0.028	0.828 + -0.007	0.396+-0.046	0.653+-0.013	0.649 + -0.007	0.831 + -0.011	0.934 + -0.018	0.727+-0.033

Table 7: AUC values for each dataset that supports query size 5.

	Splice	SpliceEncoded	DNA	DNAEncoded	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEncoded	TopV2	DivergingSin	ThreeClust
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.721+-0.013	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.957+-0.009	0.783+-0.03
Margin	0.765+-0.021	0.662+-0.032	0.794 + -0.011	0.611+-0.05	0.855 + -0.006	0.508 + -0.02	0.656+-0.014	0.678+-0.009	0.848 + -0.013	0.923+-0.019	0.697+-0.055
Badge	0.768+-0.014	0.646+-0.035	0.785 + -0.011	0.624+-0.036	0.846 + -0.007	0.48 + -0.021	0.647+-0.012	0.67+-0.009	0.847 + -0.01	0.924+-0.019	0.72 + -0.036
LeastConfident	0.763+-0.023	0.643+-0.034	0.798 + -0.013	0.585+-0.065	0.831 + -0.014	0.478 + -0.028	0.67 + -0.01	0.681+-0.009	0.819+-0.023	0.921+-0.019	0.675 + -0.072
DSA	0.765+-0.023	0.653+-0.029	0.793 + -0.009	0.613+-0.034	0.822 + -0.01	0.489 + -0.024	0.661+-0.013	0.662+-0.012	0.833 + -0.02	0.924+-0.018	0.718 + -0.033
BALD	0.775+-0.018	0.641+-0.034	0.801 + -0.013	0.592+-0.054	0.84 + -0.008	0.332+-0.054	0.681+-0.011	0.681+-0.013	0.824+-0.023	0.893+-0.035	0.673 + -0.041
CoreGCN	0.759+-0.018	0.662+-0.027	0.79 + -0.011	0.62 + -0.03	0.755 + -0.011	0.45 + -0.03	0.604+-0.016	0.609+-0.013	0.837 + -0.014	0.922+-0.018	0.723 + -0.034
Entropy	0.765+-0.022	0.66 + -0.03	0.798 + -0.011	0.611+-0.054	0.823+-0.013	0.464+-0.024	0.663+-0.013	0.672+-0.011	0.801 + -0.025	0.924+-0.02	0.689+-0.066
LSA	0.769+-0.016	0.654+-0.032	0.781 + -0.013	0.61 + -0.041	0.82 + -0.009	0.484 + -0.022	0.617+-0.012	0.641+-0.011	0.816+-0.012	0.915+-0.018	0.718 + -0.038
Random	0.758+-0.015	0.655+-0.026	0.771 + -0.013	0.623+-0.031	0.82 + -0.009	0.476 + -0.024	0.616+-0.016	0.637+-0.012	0.812 + -0.014	0.921+-0.018	0.713 + -0.034
Coreset	0.765+-0.017	0.663+-0.023	0.784 + -0.014	0.603+-0.034	0.765+-0.015	0.449+-0.022	0.657+-0.009	0.674+-0.009	0.817 + -0.017	0.92+-0.017	0.713 + -0.035
TypiClust	0.759+-0.014	0.641+-0.028	0.775 + -0.01	0.603 + -0.04	0.757 + -0.02	0.465 + -0.027	0.596+-0.014	0.567+-0.012	0.727+-0.026	0.916+-0.02	0.693+-0.045

Table 8: AUC values for each dataset that supports query size 20.

	Splice	SpliceEncoded	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	News
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.49+-0.003
Margin	0.759+-0.027	0.618 + -0.04	0.779 + -0.013	0.847 + -0.008	0.439 + -0.027	0.656 + -0.01	0.67 + -0.011	0.823 + -0.014	0.464 + -0.007
Badge	0.767+-0.013	0.619 + -0.033	0.776 + -0.013	0.845 + -0.006	0.44 + -0.019	0.647 + -0.013	0.665 + -0.007	0.827 + -0.016	0.463 + -0.007
LeastConfident	0.751+-0.02	0.597+-0.05	0.748 + -0.025	0.798 + -0.027	0.391+-0.024	0.665 + -0.013	0.669+-0.011	0.775 + -0.035	0.467 + -0.008
DSA	0.759+-0.02	0.599+-0.034	0.769+-0.013	0.809 + -0.012	0.421 + -0.023	0.647 + -0.014	0.63 + -0.013	0.793 + -0.026	0.459+-0.01
BALD	0.768+-0.022	0.57 + -0.037	0.784 + -0.015	0.822 + -0.009	0.298 + -0.039	0.675 + -0.008	0.673 + -0.01	0.789 + -0.024	0.468 + -0.009
CoreGCN	0.759+-0.018	0.612 + -0.039	0.774 + -0.012	0.754 + -0.016	0.397 + -0.026	0.587 + -0.015	0.583 + -0.015	0.807 + -0.018	0.453 + -0.006
Entropy	0.759+-0.027	0.618 + -0.038	0.773 + -0.015	0.803 + -0.019	0.372 + -0.022	0.656+-0.011	0.65+-0.012	0.773 + -0.031	0.451 + -0.007
LSA	0.761+-0.014	0.611+-0.039	0.768+-0.015	0.816 + -0.009	0.411+-0.022	0.621+-0.01	0.635+-0.011	0.796 + -0.016	0.452 + -0.007
Random	0.755+-0.014	0.612 + -0.039	0.763 + -0.012	0.818 + -0.009	0.439 + -0.019	0.622 + -0.013	0.633 + -0.012	0.795 + -0.016	0.45 + -0.006
Coreset	0.759+-0.016	0.601 + -0.034	0.764 + -0.015	0.757 + -0.015	0.39 + -0.029	0.647 + -0.009	0.651 + -0.011	0.784 + -0.026	0.435 + -0.012
TypiClust	0.751+-0.012	0.551+-0.036	0.76 + -0.016	0.643 + -0.026	0.411 + -0.024	0.488 + -0.02	0.449 + -0.017	0.652 + -0.035	0.406+-0.011

Table 9: AUC values for each dataset that supports query size 50.

	Splice	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	News
Oracle	0.803+-0.012	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.49+-0.003
Margin	0.747+-0.023	0.751 + -0.019	0.828 + -0.009	0.363 + -0.031	0.64+-0.013	0.653+-0.01	0.774+-0.029	0.46 + -0.006
Badge	0.758+-0.017	0.754 + -0.018	0.831 + -0.008	0.376 + -0.028	0.632+-0.013	0.649+-0.011	0.781 + -0.026	0.462 + -0.007
LeastConfident	0.731+-0.025	0.688 + -0.041	0.761 + -0.037	0.291 + -0.03	0.644+-0.013	0.65+-0.011	0.73 + -0.049	0.462 + -0.009
DSA	0.748+-0.021	0.738 + -0.018	0.783 + -0.016	0.346 + -0.027	0.624+-0.014	0.588+-0.016	0.748 + -0.041	0.45 + -0.011
BALD	0.76+-0.017	0.756 + -0.018	0.796 + -0.016	0.241 + -0.026	0.65 + -0.009	0.645 + -0.01	0.746 + -0.038	0.455 + -0.007
CoreGCN	0.755+-0.016	0.745 + -0.018	0.752 + -0.019	0.328 + -0.027	0.581 + -0.015	0.568+-0.018	0.771 + -0.025	0.453 + -0.007
Entropy	0.747+-0.024	0.748 + -0.018	0.778 + -0.024	0.275 + -0.026	0.633 + -0.011	0.625 + -0.012	0.734+-0.036	0.442 + -0.007
LSA	0.754+-0.013	0.749 + -0.019	0.807 + -0.01	0.341 + -0.029	0.613 + -0.012	0.625 + -0.01	0.763 + -0.025	0.45 + -0.006
Random	0.746+-0.012	0.745 + -0.015	0.806 + -0.008	0.379 + -0.028	0.615 + -0.014	0.621 + -0.01	0.759 + -0.026	0.448 + -0.006
Coreset	0.751+-0.016	0.733 + -0.019	0.74 + -0.017	0.325 + -0.034	0.624+-0.012	0.608+-0.013	0.731 + -0.045	0.432 + -0.012
TypiClust	0.749+-0.016	0.736+-0.016	0.586+-0.038	0.348+-0.027	0.451+-0.024	0.375+-0.022	0.614+-0.046	0.397+-0.012

Table 10: AUC values for each dataset that supports query size 100.

	Splice	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	News
Oracle	0.803+-0.012	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.49+-0.003
Margin	0.733+-0.024	0.711 + -0.027	0.799+-0.013	0.473 + -0.026	0.629+-0.012	0.628 + -0.009	0.455 + -0.006
Badge	0.743+-0.014	0.714 + -0.032	0.804 + -0.013	0.472 + -0.029	0.623 + -0.01	0.621+-0.01	0.456 + -0.006
LeastConfident	0.715+-0.033	0.639 + -0.05	0.708 + -0.034	0.23 + -0.034	0.631 + -0.013	0.62 + -0.012	0.457 + -0.008
DSA	0.729+-0.021	0.697 + -0.031	0.753 + -0.021	0.427 + -0.028	0.609+-0.013	0.546+-0.017	0.442 + -0.01
BALD	0.744+-0.015	0.718 + -0.024	0.765 + -0.021	0.285 + -0.046	0.632 + -0.009	0.609+-0.01	0.444 + -0.007
CoreGCN	0.742+-0.015	0.713 + -0.025	0.744 + -0.019	0.433 + -0.032	0.583+-0.013	0.554+-0.015	0.448 + -0.007
Entropy	0.733+-0.023	0.713 + -0.031	0.743 + -0.026	0.395 + -0.037	0.618+-0.012	0.59+-0.012	0.432 + -0.007
LSA	0.738+-0.017	0.716 + -0.027	0.789 + -0.011	0.439 + -0.03	0.609+-0.013	0.608 + -0.01	0.447 + -0.006
Random	0.733+-0.013	0.713 + -0.023	0.789 + -0.012	0.468 + -0.024	0.611 + -0.01	0.606 + -0.01	0.446 + -0.005
Coreset	0.735+-0.019	0.698 + -0.026	0.721 + -0.021	0.396 + -0.024	0.608 + -0.012	0.562+-0.016	0.426 + -0.012
TypiClust	0.733+-0.016	0.704+-0.025	0.592+-0.042	0.427 + -0.027	0.501 + -0.02	0.338+-0.02	0.383+-0.012

Table 11: AUC values for each dataset that supports query size 500.

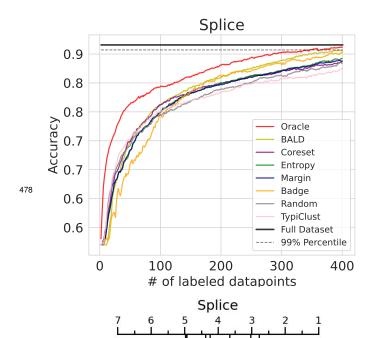
Table 12: AUC values for each dataset that supports query size 1000.

ports query size 50	00.		ports query size 1000.				
	Cifar10	FashionMnist		Cifar10	FashionMnist		
Oracle	0.689+-0.001	0.905+-0.001	Oracle	0.689+-0.001	0.905+-0.001		
Margin	0.556+-0.008	0.882 + -0.004	Margin	0.56+-0.011	0.872 + -0.007		
Badge	0.56+-0.008	0.883 + -0.005	Badge	0.562+-0.013	0.871 + -0.007		
LeastConfident	0.591+-0.01	0.884 + -0.005	LeastConfident	0.561+-0.012	0.873 + -0.006		
DSA	0.56+-0.009	0.882 + -0.004	DSA	0.56+-0.011	0.87 + -0.008		
BALD	0.478+-0.014	0.878 + -0.003	BALD	0.535+-0.011	0.866 + -0.003		
CoreGCN	0.553+-0.01	0.88 + -0.007	CoreGCN	0.557+-0.011	0.867 + -0.012		
Entropy	0.553+-0.009	0.882 + -0.006	Entropy	0.557+-0.014	0.871 + -0.009		
LSA	0.558+-0.01	0.866 + -0.005	LSA	0.551+-0.012	0.854 + -0.009		
Random	0.557+-0.01	0.863 + -0.005	Random	0.55+-0.01	0.855 + -0.006		
Coreset	0.553+-0.007	0.878 + -0.006	Coreset	0.562+-0.012	0.869 + -0.004		
TypiClust	0.557+-0.009	0.864+-0.004	TypiClust	0.552+-0.011	0.854+-0.009		

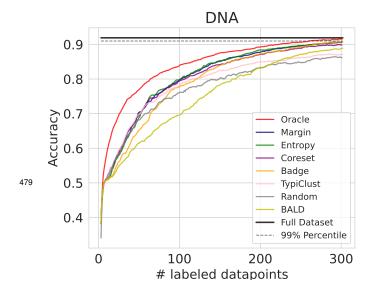
476 F Critical Difference Diagrams

477 G Individual Results

TypiClust 5.0
Random 4.9
Margin 4.4
Entropy 4.2



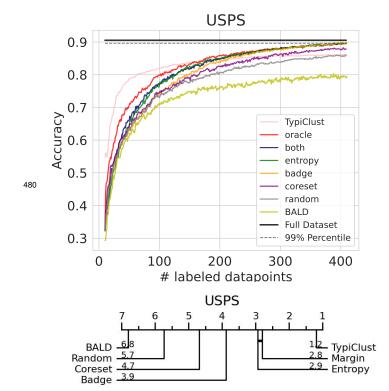
	Splice
Oracle	0.811 ± 0.010
BALD	0.785 ± 0.013
Coreset	0.778 ± 0.014
Entropy	0.774 ± 0.016
Margin	0.773 ± 0.016
Badge	0.770 ± 0.016
Random	0.768 ± 0.014
TypiClust	0.766 ± 0.014



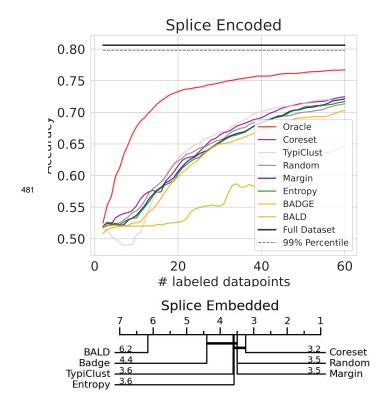
	DNA
Oracle	0.842 ± 0.021
Margin	0.807 ± 0.035
Entropy	0.805 ± 0.038
Coreset	0.796 ± 0.028
Badge	0.789 ± 0.056
TypiClust	0.788 ± 0.036
Random	0.768 ± 0.024
BALD	0.749 ± 0.044

				DNA				
	7 	6 I	5 - 1	4 l	3	2 l	1	
BALD Random Badge TvpiClust	5.8 5.1 4.4 4.3						2.7 Entropy 2.8 Margin 3.0 Coreset	

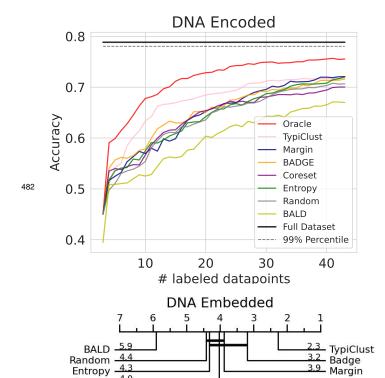
2.8 BALD 3.0 Badge 3.7 Coreset



	USPS
TypiClust	0.830 ± 0.007
Oracle	0.823 ± 0.011
Margin	0.809 ± 0.013
Entropy	0.807 ± 0.013
Badge	0.795 ± 0.018
Coreset	0.788 ± 0.017
Random	0.774 ± 0.012
BALD	0.725 ± 0.050

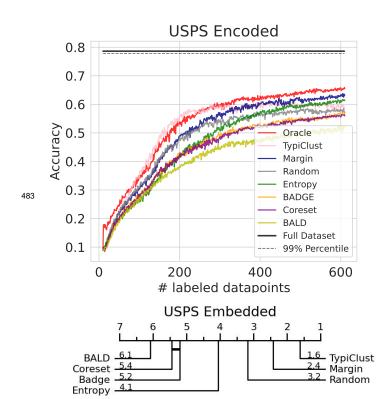


	SpliceEncoded
Oracle	0.728 ± 0.022
Coreset	0.648 ± 0.027
TypiClust	0.645 ± 0.042
Random	0.643 ± 0.036
Entropy	0.636 ± 0.033
Margin	0.636 ± 0.033
Badge	0.627 ± 0.040
BALD	0.565 ± 0.049

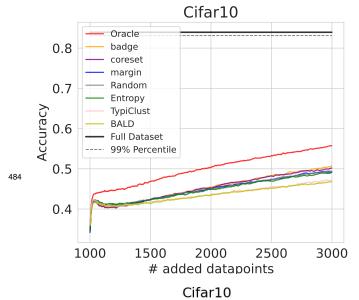


Entropy 4.3 Coreset 4.0

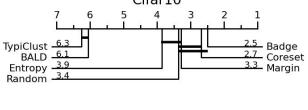
	DNAEncoded
Oracle	0.709 ± 0.023
TypiClust	0.672 ± 0.029
Margin	0.648 ± 0.047
Badge	0.647 ± 0.037
Coreset	0.640 ± 0.041
Entropy	0.629 ± 0.062
Random	0.626 ± 0.035
BALD	0.594 ± 0.039

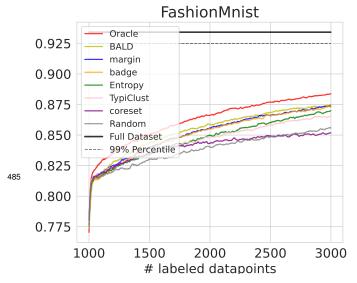


	USPSEncoded
Oracle	0.522 ± 0.021
TypiClust	0.507 ± 0.025
Margin	0.496 ± 0.030
Random	0.468 ± 0.025
Entropy	0.459 ± 0.021
Badge	0.440 ± 0.026
Coreset	0.435 ± 0.027
BALD	0.402 ± 0.052



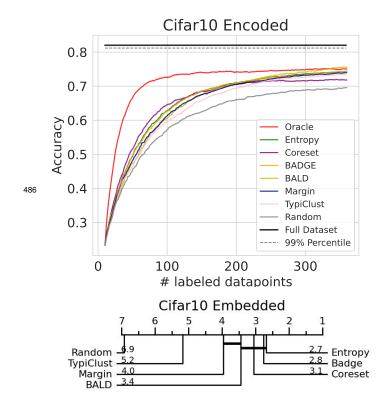
	Cifar10
Oracle	0.500 ± 0.010
Badge	0.453 ± 0.012
Coreset	0.453 ± 0.009
Margin	0.451 ± 0.010
Random	0.450 ± 0.012
Entropy	0.449 ± 0.010
TypiClust	0.436 ± 0.010
BALD	0.436 ± 0.010



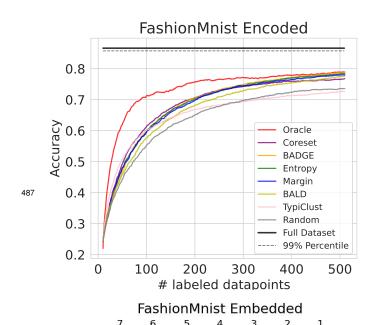


	FashionMnist
Oracle	0.862 ± 0.003
BALD	0.854 ± 0.003
Margin	0.851 ± 0.003
Badge	0.851 ± 0.003
Entropy	0.847 ± 0.004
TypiClust	0.846 ± 0.004
Coreset	0.840 ± 0.004
Random	0.837 ± 0.004

			Fas	hior	ιMr	nist		
	7	6	5	. 4		3	2	1
Random Coreset TypiClust Entropy	6.0			<u> </u>				1.4 BALD 2.2 Margin 2.8 Badge



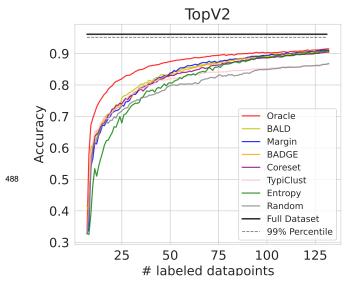
	Cifar10Encoded
Oracle	0.714 ± 0.007
Entropy	0.654 ± 0.013
Coreset	0.653 ± 0.012
Badge	0.653 ± 0.012
BALD	0.650 ± 0.016
Margin	0.647 ± 0.012
TypiClust	0.636 ± 0.009
Random	0.607 ± 0.013



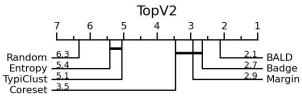
Random 69 TypiClust 6.0 BALD 4.9 Margin 3.0

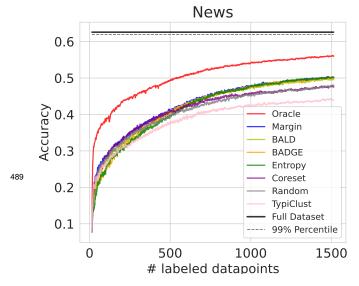
	FashionMnistEncoded
Oracle	0.732 ± 0.006
Coreset	0.686 ± 0.008
Badge	0.685 ± 0.008
Entropy	0.684 ± 0.009
Margin	0.682 ± 0.011
BALD	0.668 ± 0.009
TypiClust	0.652 ± 0.009
Random	0.640 ± 0.011

2.2 Badge 2.5 Coreset 2.6 Entropy



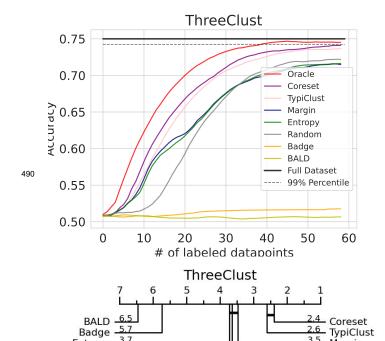
	TopV2
Oracle	0.862 ± 0.006
BALD	0.831 ± 0.013
Badge	0.826 ± 0.015
Coreset	0.823 ± 0.016
Margin	0.822 ± 0.015
TypiClust	0.805 ± 0.015
Entropy	0.801 ± 0.025
Random	0.787 ± 0.015



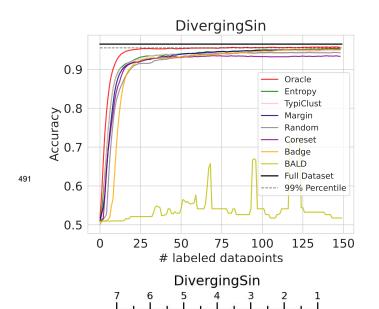


	News
Oracle	0.502 ± 0.005
Margin	0.427 ± 0.007
BALD	0.421 ± 0.008
Badge	0.420 ± 0.011
Entropy	0.416 ± 0.010
Coreset	0.415 ± 0.011
Random	0.409 ± 0.008
TypiClust	0.385 ± 0.010

						Ν	ew	IS				
TypiClust Random Coreset Entropy	4.2	<u></u>	6 I	ř	5	1	4		3	-	2 1	1 1.8 1.8 Margin



	ThreeClust
Oracle	0.722 ± 0.097
Coreset	0.698 ± 0.058
TypiClust	0.697 ± 0.055
Entropy	0.682 ± 0.098
Random	0.672 ± 0.067
Margin	0.669 ± 0.095
Badge	0.524 ± 0.086
BALD	0.507 ± 0.050
	!



DivergingSin
0.948 ± 0.198
0.936 ± 0.202
0.930 ± 0.196
0.929 ± 0.201
0.919 ± 0.191
0.914 ± 0.202
0.914 ± 0.197
0.661 ± 0.167

Seeding Strategy

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BALD 5.4

Coreset 4.3 Random 4.1 Badge

Entropy Random

We aim to provide an experimental setup that is fully reproducible independent of the dataset, classi-493 fication model, or AL algorithm used. For a fair comparison of two AL algorithms, both algorithms 494 495

3.3 Entropy 3.4 Margin 3.4 TypiClust

3.5 Margin

need to receive equal starting conditions in terms of train/validation split, initialization of classifier,

implementations might have their own solution to some of these problems, only [10] has described 497 498 and implemented a fully reproducible pipeline for AL evaluation. The term reproducibility in this work is used as a synonym not only for the reproducibility of an experiment (a final result given a 499 seed), but also the reproducibility of all subsystems independent of each other. The seed for one sub-500 system should always reproduce the behavior of this subsystem independent of all other subsystems 501 and their seeds. The main obstacle for ensuring reproducibility is the seeding utility in PyTorch, 502 Tensorflow, and other frameworks, whose default choice is a single global seed. Since many subsys-503 tems draw random numbers from this seed, all of them influence each other to a point where a single 504 additional draw can completely change the model initialization, data split or the order of training 505 batches. Even though some workarounds exist, e.g. re-setting the seed multiple times, this problem 506 is not limited to the initialization phase, but also extends to the AL iterations and the systems within. 507 We propose an implementation that creates separate Random Number Generators (RNGs) for each 508 of these systems to ensure equal testing conditions even when the AL algorithm, dataset, or classi-509 fier changes. We hypothesize that the insufficient setup with global seeds contributes to the ongoing 510 problem of inconsistent results of AL algorithms in different papers. 511 In summary, we introduce three different seeds: s_{Ω} for the AL algorithm, $s_{\mathcal{D}}$ for dataset splitting 512 and mini-batch sampling, and s_{θ} for model initialization and sampling of dropout masks. Unless 513 stated otherwise, we will keep s_{Ω} fixed, while $s_{\mathcal{D}}$ and s_{θ} are incremented by 1 between restarts to 514 introduce stochasticity into our framework. Some algorithms require a subsample to be drawn from 515 \mathcal{U} in order to reduce the computational cost in each iteration, while others need access to the full 516 unlabeled pool (e.g. for effective clustering). If a subsample is required, it will be drawn from $s_{\rm O}$ 517 and therefore will not influence other systems in the experiments. For each algorithm, we decided 518 if subsampling is required based on our available hardware, but decided against setting a fixed time 519 limit per experiment, since this would introduce unnecessary complexity into the benchmark. An 520 overview of selected hyperparameters per AL algorithm can be found in Appendix J. 521 522

and even the state of minor systems like the optimizer or mini-batch sampler. Even though different

Note: Even though we decoupled the subsystems via the described seeds, the subsystems can still influence each other in a practical sense. For example, keeping $s_{\mathcal{D}}$ fixed does not mean that always the same sequence of samples from \mathcal{U} (if subsamples are drawn) are shown to all acquisition functions. This is practically impossible, as different acquisition functions pick different $x^{(i)}$. However, the hypothetical **tree** of all possible sequences of samples from \mathcal{U} remains the same, granting every acquisition function equal possibilities.

528 I Oracle Curve Forecasting

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J Hyperparameters per AL Algorithm

Table 13: Selected hyperparameters for all tested acquisition functions. Last column indicates the source of our implementation.

Algorithm	Sample Size	Other	Source
BADGE	100		Based on [1, 14]
BALD	100	Dropout Trials: 5	Based on [4]
Coreset	8000	_	Own
TypiClust	10000	Min Cluster Size: 5	Based on [8]
		Max # Clusters: 500	
Margin	8000		Own
Entropy	8000		Own

K Hyperparameters and Preprocessing per Dataset

- For all our datasets we use the pre-defined train/test splits, if given. In the remaining cases, we
- define test sets upfront and store them into separate files to keep them fixed across all experiments.
- The validation set is split in the experiment run itself and depends on the dataset-seed.
- Tabular: We use **Splice**, **DNA** and **USPS** from LibSVMTools [20]. All three datasets are normalized between [0, 1].
- Image: We use FashionMNIST [25] and Cifar10 [13], since both are widely used in AL literature.
- Both datasets are normalized according to their standard protocols.
- Text: We use News Category [18] and TopV2 [6]. For News Category we use the 15 most com-
- mon categories as indicated by its Kaggle site. We additionally drop sentences above 80 words to
- reduce the padding needed (retaining 99,86% of the data). For TopV2, we are only using the "alarm"
- domain. Both datasets are encoded with pre-trained GloVe (Common Crawl 840B Tokens) embed-
- dings [21]. Since neither dataset provided a fixed test set, we randomly split 7000 datapoints into a
- 544 test set.

Dataset	Seed Set	Budget	Val Split
Splice	1	400	0.2
SpliceEnc.	1	60	0.2
DNA	1	300	0.2
DNAEnc	1	40	0.2
USPS	1	400	0.2
USPSEnc	1	600	0.2
FashionMnist	100	2000	0.04
FashionMnistEnc	1	500	0.04
Cifar10	100	2000	0.04
Cifar10Enc	1	350	0.04
TopV2	1	125	0.25
News	1	1500	0.03

Table 14: Size of the seed set is given by number of labeled sample per class.

Dataset	Classifier	Optimizer	LR	Weight Decay	Dropout	Batch Size
Splice	[24, 12]	NAdam	1.2e-3	5.9e-5	0	43
SpliceEnc.	linear	NAdam	6.2e-4	5.9e-6	0	64
DNA	[24, 12]	NAdam	3.9e-2	3.6e-5	0	64
DNAEnc	linear	NAdam	1.6e-3	4e-4	0	64
USPS	[24, 12]	Adam	8.1e-3	1.5e-6	0	43
USPSEnc	linear	NAdam	7.8e-3	1.9e-6	0	64
FashionMnist	ResNet18	NAdam	1e-3	0	0	64
FashionMnistEnc	linear	Adam	1.6e-3	1e-5	5e-2	64
Cifar10	ResNet18	NAdam	1e-3	0	0	64
Cifar10Enc	linear	NAdam	1.7e-3	2.3e-5	0	64
TopV2	BiLSTM	NAdam	1.5e-3	1.7e-7	5e-2	64
News	BiLSTM	NAdam	1.5e-3	1.7e-7	5e-2	64

Table 15: Classifier architectures and optimized hyperparameters per dataset. Numbers in brackets signify a MLP with corresponding hidden layers.

545 L AL Pseudocode

Algorithm 2 Retrain

```
Require: \mathcal{L}, \mathcal{D}_{val}, \mathcal{D}_{test}
Require: \hat{y}, e_{\text{max}}
  1: loss^* \leftarrow \infty
  2: for i := 1 \dots e^{\max} do

\hat{y}_{i+1} \leftarrow \hat{y}_i - \eta \nabla_{\hat{y}} \ell(\mathcal{L}, \hat{y}) \\
loss_i \leftarrow \ell(\mathcal{D}^{\text{val}}, \hat{y})

  3:
  4:
                 if loss_i < loss^* then
  5:
                         loss^* \leftarrow loss_i
  6:
  7:
                 else
  8:
                         Break
  9: return Acc(\mathcal{D}^{test}, \hat{y})
```

Algorithm 3 Acquire Oracle Ω

```
Require: \mathcal{U}, \mathcal{L}, A, \mathcal{D}_{test}, \tau, \hat{y}_{\theta}
Require: Train, Margin, Acc
   1: \operatorname{acc}^0 \leftarrow \operatorname{acc}^* \leftarrow \operatorname{Acc}(\mathcal{D}_{\operatorname{test}}, \hat{y}_{\theta})
2: \operatorname{for} k := 1 \dots \tau \operatorname{do}
                      u_k = \operatorname{unif}(\mathcal{U})
                      \mathcal{L}' \leftarrow \mathcal{L}^{(i)} \cup \{(u_k, A(u_k))\}\hat{y}'_{\theta} \leftarrow \operatorname{Train}(\mathcal{L}', \hat{y}_{\theta})
   4:
   5:
                      \operatorname{acc}' \leftarrow \operatorname{Acc}(\mathcal{D}_{\operatorname{test}}, \hat{y}'_{\theta})
   6:
                      if acc' > acc^* then
   7:
                                 acc^* \leftarrow acc'
   8:
   9:
                                 u^* \leftarrow u_k
10: if acc^0 = acc^* then
           u^* \leftarrow \operatorname{Margin}(\mathcal{U}, \hat{y}_{\theta}) return u^*
```

Alg. 3 replaces the acquisition function Ω in the AL loop (Alg. L line 5).