
A Cross-Domain Benchmark for Active Learning

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Abstract

Active Learning (AL) deals with identifying the most informative samples for labeling to reduce data annotation costs for supervised learning tasks. AL research suffers from the fact that lifts from literature generalize poorly and are only conducted on a small number of repetitions of experiments. To overcome this obstacles, we propose *ALBench*, the first active learning benchmark which includes tasks in computer vision, natural language processing and tabular learning. Furthermore, by providing an efficient greedy oracle, *ALBench* can be evaluated with 50 runs for each experiment. We will show, that both the cross-domain character and the large amount of repetitions are crucial for sophisticated evaluation of AL research. Concretely, we will show that the superiority of specific methods varies over the different domains, making it important to evaluate Active Learning with a cross-domain benchmark. Additionally, we show, that having a large amount of runs is crucial. With only conducting five runs as often done in the literature, the superiority of specific methods can strongly vary with the specific runs. This effect goes so far, that it may even happen that dedicated methods like *margin-sampling* are not able to outperform the random baseline.

1 Introduction

Deep neural networks (NN) have produced state-of-the-art results on many important supervised learning tasks. Since Deep NNs usually require large amounts of labeled training data, Active Learning (AL) deals with selecting the most informative samples out of a large pool of unlabeled data, so that only these samples need to be labeled. It has been shown that a small labeled set of this nature can be used to train well-performing models. In the last decade, many different algorithms for AL have been proposed and almost every method has reported lifts over all its predecessors,¹ However, real insights into the current state of AL are hard to draw from these works, due to the following reasons: 1. These works do not use a standardized evaluation setting with fixed datasets and baseline approaches. 2. Due to cost reasons, a lot of works do only a small amount of experimental runs, hence it is questionable whether the superiority of a specific approach can be concluded from the conducted experiments. 3. The works are only evaluated in a specific domain, such as computer vision or language processing. However, AL is a general principle of supervised learning, and thus methods should be evaluated in multiple domains to assess their capabilities.

While multiple benchmark suites have been proposed to solve problem 1, to the best of our knowledge, all of them are either limited in the domains they consider or do not do enough runs for conclusive results. Hence, the current state of the art in Active Learning is still not well-understood and principle shortcomings of different algorithms and whether they are present domain-independent, are currently not identified.

¹Out of all considered algorithms for this paper, only BALD [7] did not claim a new SOTA performance in their result section.

36 Here we step in with *ALBench*, an active learning benchmark which covers multiple application do-
37 mains and which reports a large amount of runs per experiment, so that the significance of perfor-
38 mance differences can be estimated. To be more detailed, *ALBench* consists of datasets from
39 computer vision, natural language processing and the tabular domain. We provide our datasets both
40 in raw format (i.e. consisting of text, images etc) or already “embedded” where one can evaluate AL
41 approaches on already learned representations. Furthermore, we provide further synthetic datasets
42 to identify general challenges for AL methods.

43 The evaluation protocol on which we evaluate in *ALBench* uses 50 runs for each experiment. By
44 having such a large amount of runs, we can evaluate the significance of performance gaps and
45 identify the in-fact best performing approaches for different runs. Furthermore, we will show, that
46 the small amounts of runs other works do can in fact lead to misleading results. To be more specific,
47 we show that if only 5 runs are randomly sampled, the performance of specific methods strongly
48 varies. As we will see, the ranking of the different method heavily fluctuates with the specific set of
49 randomly selected runs. This effect goes so far, that for a well-established method such as margin-
50 sampling, the question whether this method is significantly better or worse than the random baselines,
51 will be answered differently depending on the 5 runs which were chosen.

52 To enable a large amount of runs, we propose a *greedy oracle function*, which uses only a small
53 amount of search steps to estimate the optimal solution. While being more time-efficient than es-
54 tablished oracle functions, it can be a large underestimate of the real performance of the optimal
55 solution. However, as our experiments will show, it is still far ahead of all current AL methods and
56 thus is perfectly suitable for having a lower bound on what AL methods could be able to achieve.

57 Our experimental evaluation shows, that there exists no clear SoTa method for Active Learning. The
58 superiority of specific datasets is strongly domain-dependent with the outstanding observation, that
59 the image domain works fundamentally different than the tabular and text domain. Here, the best
60 performing approach in text and tabular data, namely *margin sampling*, is significantly outperformed
61 by *Least Confident*, which does not belong to the top performing approaches in text and tabular.
62 Thus, using the performance of Active Learning approaches on the image domain as a proxy of
63 Active Learning in general, as often done, is questionable. To further understand this performance
64 gaps, we propose *Honeypot* and *Diverging Sin*, two synthetic datasets, which are designed to be
65 challenging for naive clustering or decision-boundary based approaches. Hence, they can be used as
66 a lower bar for assessing a AL approach as sophisticated.

67 To sum up, *ALBench* consists of an experimental framework which includes a fast oracle approxima-
68 tion, multiple application domains, enough repetitions to draw valid conclusions and two synthetic
69 tasks to estimate if a specific method reaches a minimum amount of complexity. By being the first
70 benchmark to proving these things together, we believe that *ALBench* is a major step forward of as-
71 sessing the overall state of Active Learning research, independent of a specific application domain.
72 *ALBench* is publicly available. Our contributions include the following:

Link etc

- 73 1. We show that the small of runs that previous work has conducted is not sufficient for mean-
74 ingful conclusions. This can go so far, that it may not even be possible to access whether
75 margin sampling is better than random.
- 76 2. We propose an efficient and performant oracle which is computed greedily. With that, we
77 overcome one of the major obstacles for sufficient repetitions of AL experiments.
- 78 3. We propose *Honeypot* and *Diverging Sin*, two synthetic datasets designed to hinder active
79 learning by simple decision-boundary or clustering-based approaches. Thus, they provide
80 as a lower bar on the complexity of AL methods.
- 81 4. We propose *IMTSBench*, the first general benchmark providing tasks in the domains of
82 images, text and tabular learning. It further contains synthetic and already encoded data to
83 allow for a sophisticated evaluation of AL methods. Our experiments show, that there is no
84 clear state-of-the art method for active learning over different domains.
85

Sagt man “is
computed
greedily”?
Ist das wirk-
lich NICHT
search based?
Weil eine
greedy-search
ist ja auch
search based

Ich bin mir
nicht ganz
sicher, wie
man Hon-
eypot und
Diverging Sin

Table 1: Comparison of our benchmark with the existing literature. Oracle curves serve as an approximation of the best possible AL algorithm. Including the encoded versions of our datasets we reach 14 datasets, without we have 9. "Semi" indicates whether the paper is employing any form of self- or semi-supervised learning. A "-" for repetitions means that we could not determine how often each experiment is repeated in the respective framework. *ALBench* is the only benchmark which reports over enough runs for meaningful results and considers all 5 domains.

Paper	Sampling	#Data	#Alg	Img	Txt	Tab	Synth	Semi	Oracle	Repetitions
Beck et al. [2]	batch	4	7	✓	-	-	-	-	-	-
Hu et al. [9]	batch	5	13	✓	✓	-	-	-	-	3
Zhou et al. [29]	batch	3	2	✓	✓	-	-	-	✓	5
Zhan et al. [27]	sngl+batch	35	18	-	-	✓	✓	-	✓	10-100
Munjal et al. [19]	batch	2	8	✓	-	-	-	-	-	3
Li et al. [15]	batch	5	13	✓	-	-	-	✓	-	-
Rauch et al. [22]	batch	11	5	-	✓	-	-	-	-	5
Ji et al. [10]	batch	3	8	✓	-	-	-	-	-	-
Lueth et al. [17]	batch	4	5	✓	-	-	-	✓	-	3
Ours	sngl+batch	9(14)	11	✓	✓	✓	✓	✓	✓	50

2 Problem Description

Given two spaces \mathcal{X}, \mathcal{Y} , $n = l + u$ data points with $l \in \mathbb{N}$ labeled examples $\mathcal{L} = \{(x_1, y_1), \dots, (x_l, y_l)\}$, $u \in \mathbb{N}$ unlabeled examples $\mathcal{U} = \{x_{l+1}, \dots, x_n\}$, a model $\hat{y} : \mathcal{X} \rightarrow \mathcal{Y}$, a budget $\mathbb{N} \ni b \leq u$ and an annotator $A : \mathcal{X} \rightarrow \mathcal{Y}$ that can label x . We call $x \in \mathcal{X}$, $y \in \mathcal{Y}$ predictors and labels respectively where (x, y) are drawn from an unknown distribution ρ . Find an acquisition function $\Omega : \mathcal{U}^{(i)}, \mathcal{L}^{(i)} \mapsto x^{(i)} \in \mathcal{U}^{(i)}$ that iteratively selects the next unlabeled point $x^{(i)}$ for labeling

$$\begin{aligned}\mathcal{L}^{(i+1)} &\leftarrow \mathcal{L}^{(i)} \cup \{(x^{(i)}, A(x^{(i)}))\} \\ \mathcal{U}^{(i+1)} &\leftarrow \mathcal{U}^{(i)} \setminus \{x^{(i)}\}\end{aligned}$$

with $\mathcal{U}^{(0)} = \text{seed}(\mathcal{U}, s)$ and $\mathcal{L}^{(0)} = (\mathcal{U}_i^{(0)}, A(\mathcal{U}_i^{(0)}))$ $i \in [1, \dots, s]$, where $\text{seed}(\mathcal{U}, s)$ selects s points per class for the initial labeled set.

So that the average expected loss $\ell : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}$ of a machine learning algorithm fitting $\hat{y}^{(i)}$ on the respective labeled set $\mathcal{L}^{(i)}$ is minimal:

$$\min \frac{1}{B} \sum_{i=0}^B \mathbb{E}_{(x,y) \sim \rho} \ell(y, \hat{y}^{(i)})$$

3 Related Work

While multiple benchmark suites have been proposed for Active Learning, none of them provide experiments for more than two domains. The authors of [2], [19], [15], [10] and [17] even focus exclusively on the image domain. Experiments on the interplay between AL and semi-supervised learning have only been provided by two works so far [15, 17], both of them only for images. An oracle algorithm has so far been proposed by only two works [29, 28]. Both of these algorithms rely on search, while our proposed method can be constructed sequentially. The two closest related works to this benchmark are [10] and [17], who also place a much higher emphasis on the problem of evaluating AL algorithms under many forms of variance than their predecessors (indicated in Tab. 1 by a dashed line). The authors of [10] posed a total of 12 "recommendations" for reliable evaluation of AL algorithms. We largely adapt the proposed recommendations of [10] and extend their work to multiple domains, batch sizes and comparisons. For a complete list of the recommendations and our implementation of them, please refer to App. A. This work also pays attention to the so-called "pitfalls" of AL evaluation proposed in [17]. For a complete list of the pitfalls and our implementation of them, please refer to App. B. To the best of our knowledge, we are the first to extend reliable SOTA (based on [10, 17]) experimentation to a total of 5 data domains.

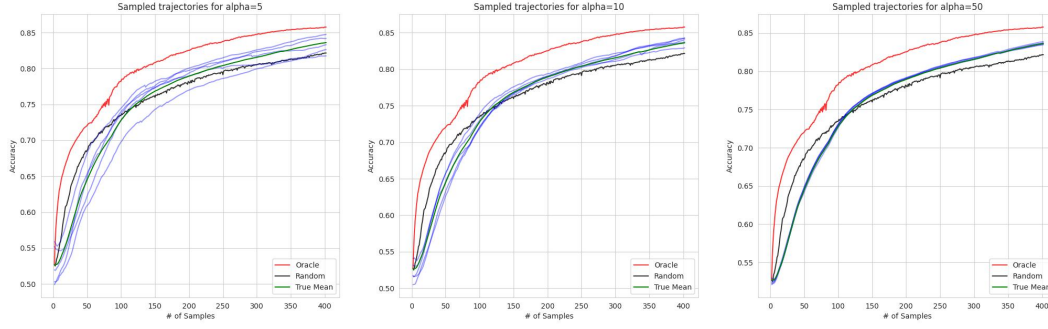


Figure 1: Random draws from a pool of 100 runs for margin sampling on the Splice dataset with different numbers of repetitions ($\alpha = \{5, 10, 50\}$). Green curves are the mean performance of all 100 runs, while the samples are blue. Even with 5 or 10 repetitions, we can observe that single draws for margin sampling display below-random performance (black), while the true mean should be above random.

109 4 Methodology

110 4.1 Why we need 50 restarts

111 To evaluate how many restarts are necessary to obtain conclusive results in an AL experiment, we
 112 computed 100 runs of our top-performing algorithm on one dataset. Our best algorithm is margin
 113 sampling and we chose the Splice dataset for its average size and complexity.
 114 This allows us firstly, to obtain a very strong estimation of the "true" average performance of margin
 115 sampling on this dataset and secondly, to draw subsets from this pool of 100 runs. Setting the size
 116 of our draws to α and sampling uniformly, we can approximate a cross-validation process with α
 117 restarts. Each of these draws can be interpreted as a **reported result in AL literature** where the
 118 authors employed α restarts. Figure 1 shows the "true" mean performance of margin sampling
 119 (green) in relation to random sampling (black) and the oracle performance (red). We display 5
 120 random draws of size α in blue. We can observe that even for a relatively high number of restarts the
 121 variance between the samples is extremely high, resulting in some performance curves being worse
 122 than random and some being significantly better. When setting $\alpha = 50$ we observe all samples to
 123 converge close to the true mean performance. In addition to this motivating example, we carried out
 124 our main evaluation (Tab. 3) multiple times by uniformly sampling 3 random from our 50 available
 125 runs and comparing the results. We found significant differences in the performance of acquisition
 126 functions on individual datasets, as well as permutations in the final ranking. This partly explains
 127 the ongoing difficulties in reproducing results for AL experiments and benchmarks. This details can
 128 be found in App. D. For this benchmark we employ 50 restarts of every experiment.

129 4.2 Seeding vs. Restarts

130 Considering the high computational cost of 50 repetitions, another approach to ensure reproducibil-
 131 ity would be to reduce the amount of variance in the experiment by keeping as many subsystems
 132 (weight initialization, data splits, etc.) as possible fixed with specialized seeding.
 133 We describe a novel seeding strategy in Appendix H that creates 3 separate Random Number Gen-
 134 erators (RNG) based on 3 different seeds. In short, we introduce three different seeds: s_Ω for the
 135 AL algorithm, $s_\mathcal{D}$ for dataset splitting and mini-batch sampling, and s_θ for model initialization and
 136 sampling of dropout masks. Unless stated otherwise, we will keep s_Ω fixed, while $s_\mathcal{D}$ and s_θ are
 137 incremented by 1 between restarts to introduce stochasticity into our framework. While this seeding
 138 strategy is capable of controlling the amount variance in the experiment, previous works have noted
 139 that an actively sampled, labeled set does not generalize well between model architectures or even

different initializations of the same model ([29, 16]), reducing its value in practice and providing a bad approximation of the quality of an AL algorithm. Hence, we opt for letting the subsystems vary (by increasing $s_{\mathcal{D}}$ and s_{θ}) and combine that with a high number of restarts to obtain a good average of the generalization performance of each AL algorithm. Where a high number of restarts is computationally not feasible, we advise to additionally keep either $s_{\mathcal{D}}$ or s_{θ} (or both) fixed.

4.3 Datasets

A detailed description of the preprocessing of each dataset can be found in Appendix K.

Tabular: AL research conducted on tabular data is sparse (only [1] from the considered baseline papers). We, therefore, introduce a set of tabular datasets that we selected according to the following criteria: (i) They should be solvable by medium-sized models in under 1000 samples, (ii) the gap between most AL algorithms and random sampling should be significant (potential for AL is present) and (iii) the gap between the AL algorithms and our oracle should also be significant (research on these datasets can produce further lifts). We use **Splice**, **DNA** and **USPS** from LibSVMTools [20].

Image: We use **FashionMNIST** [25] and **Cifar10** [13], since both are widely used in AL literature.

Text: We use **News Category** [18] and **TopV2** [6]. Text datasets have seen less attention in AL research, but most of the papers that evaluate on text ([9], [29]) use at least one of these datasets.

We would like to point out that these datasets are selected for speed of computation (both in terms of number of features and necessary budget to solve the dataset). However, similar to our argumentation for picking smaller classifiers, we are solely focused on comparing different AL algorithms in this paper and do not aim to develop novel classification models on these datasets. Our assumption is that a well-performing algorithm in our benchmark will also generalize well to larger real-world datasets, because we included multiple different data domains and classifier sizes in our experiments.

Adapting the experimental setting from [8], we offer all our datasets in the un-encoded (normal) setting as well as pre-encoded by a fixed embedding model that was trained by unsupervised contrastive learning. The text datasets are an exception to this, as they are only offered in their encoded form. The pre-encoded datasets enable us to test single-sample algorithms on more complex datasets like Cifar10 and FashionMnist. They also serve the purpose of investigating the interplay between self-supervised learning techniques and AL, as well as alleviating the cold-start problem described in [17] as they require a way smaller seed set. The classification model for every encoded dataset is a single linear layer with softmax activation. The embedding model was trained with the SimCLR [5] algorithm adopting the protocol from [8]. To ensure that enough information from the data is encoded by our embedding model, the quality of embeddings during pretext training was measured after each epoch. We attached a linear classification head to the encoder, fine-tuned it to the data and evaluated this classifier for test accuracy, mirroring our AL setup for embedded datasets. The checkpoint of each encoder model will be provided together with the framework.

Every dataset has a fixed size for the seed set of 1 sample per class, with the only exceptions being un-encoded FashionMnist and Cifar10 with 100 examples per class to alleviate the cold-start problem in these complex domains.

4.4 Batch Sizes

We selected batch sizes for each dataset to accommodate the widest range possible that results in a reasonable runtime for low batch sizes and allows for at least 4 round of data acquisition for high batch sizes. The available batch sizes per dataset can be found in Table 2.

4.5 Realism vs. Variance

We would like to point out that some design choices for this framework prohibit direct transfer of our results to practical applications. This is a conscious choice, as we think that this is a necessary trade-off between realism and experiment variance. We would like to highlight the following design

188 decisions:

189 (i) Creating test and validation splits from the full dataset rather than only the labeled seed set. Fully
 190 fledged test and validation splits are unobtainable in practice, but they provide not only a better
 191 approximation of algorithm performance, but also a better foundation for hyperparameter tuning,
 192 which is bound to reduce variance in the experiment.

193 (ii) Choosing smaller classifiers instead of SOTA models. Since we are not interested in archiving a
 194 new SOTA in any classification problem, we instead opt to use smaller classifiers for the following
 195 reasons: Smaller classifiers generally exhibit more stable training behavior, on average require fewer
 196 sampled datapoints to reach their full-dataset-performance and have faster training times. For every
 197 dataset, the chosen architecture’s hyperparameters are optimized to archive maximum full-dataset
 198 performance. Generally, we use MLPs for tabular, ResNet18 for image and BiLSTMs for text
 199 datasets. Every encoded dataset is classified by a single linear layer with softmax activation. The
 200 used model for each dataset can be found in Tab. 2. For a detailed description and employed
 201 hyperparameters please refer to Appendix K.

202 4.6 Greedy Oracle Algorithm

203 Posing Active Learning as a combinatorial problem, the oracle set \mathcal{O}_b for a given dataset,
 204 model, and training procedure is the set that induces the high-

205 est AUC score for a given bud-
 206 get. However, since this prob-
 207 lem is computationally infeas-
 208 ible for realistic datasets, pre-
 209 vious works have proposed ap-
 210 proximations to this oracle sequence. [29] used simulated annealing to search for the optimal subset
 211 and used the best solution found after a fixed time budget. Even though their reported performance
 212 curves display a significant lift over all other acquisition functions, we found the computational cost
 213 of reproducing this oracle for all our datasets to be prohibitive (The authors reported the search to
 214 take several days per dataset on 8 V100 GPUs). In this paper, we propose a greedy oracle algorithm
 215 that constructs an approximation of the optimal set in an iterative fashion. Our oracle algorithm
 216 evaluates every data point $u_k = \text{unif}(\mathcal{U})$ $k \in [1 \dots \tau]$ in a subsample of unlabeled points by fitting
 217 the classifier \hat{y} on $\mathcal{L}^{(i)} \cup \{u_k\}$ and directly measuring the resulting test performance. The data point
 218 with the best test performance is selected and added to the labeled pool for that iteration. We noticed
 219 that this oracle is over-specializing on the test set, resulting in stagnating or even decreasing perfor-
 220 mance curves in later AL iterations. This can happen, for example, if the oracle picked a labeled
 221 set that enables the classifier to correctly classify a big portion of easy samples in the test set, but
 222 now fails to find the next **single** unlabeled point that would enable the classifier to succeed on one
 223 of the hard samples. This leads to a situation, where no point can immediately incur an increase in
 224 test performance and therefore the selected data point can be considered random. To circumvent this
 225 problem, we use margin sampling [24] as a fallback option for the oracle. Whenever the oracle does
 226 not find an unlabeled point that results in an increase in performance, it defaults to margin sampling
 227 in that iteration. The resulting greedy algorithm constructs an approximation of the optimal labeled
 228 set that consistently outperforms all other algorithms by a significant margin, while requiring rela-
 229 tively low computational cost ($\mathcal{O}(B\tau)$). We fix $\tau = 20$ in this work, as this gave us already a
 230 significant lift and we expect diminishing returns for larger τ . The pseudocode for our oracle can
 231 be found in App. L. Even though our proposed algorithm is more efficient than other approaches,
 232 the computational costs for high budget datasets like Cifar10 and FashionMnist meant that we could
 233 not compute the oracle for all 10000 datapoints. To still provide an oracle for these two datasets, we
 234 select two points per iteration instead of one and stop the oracle computation at a budget of 5000.
 235 The rest of the curve is forecast with a simple linear regression that asymptotically approaches the
 236 upper bound performance of the dataset. A detailed description can be found in App. I.

Table 2: Employed model, chosen budget and available batch sizes for each dataset

	Model	B	1	5	20	50	100	500	1K
Enc. DNA	Linear	40	o	o					
Enc. Splice	Linear	100	o	o	o	o			
TopV2	BiLSTM	200	o	o	o	o			
Splice	MLP	400	o	o	o	o	o		
DNA	MLP	300	o	o	o	o	o		
USPS	MLP	400	o	o	o	o	o		
Enc. Cifar10	Linear	450	o	o	o	o	o		
Enc. FMnist	Linear	500	o	o	o	o	o		
Enc. USPS	Linear	600	o	o	o	o	o		
News	BiLSTM	3K			o	o	o	o	
FMnist	ResNet18	10K						o	o
Cifar100	ResNet18	10K							

240 4.7 Evaluation Protocol

241 Following [29], the quality of an AL algorithm is evaluated by an “anytime protocol” that incorpo-
 242 rates classification performance at every iteration, as opposed to evaluating final performance after
 243 the budget is exhausted. We employ the normalized area under the accuracy curve (AUC):

$$\text{AUC}(\mathcal{D}_{\text{test}}, \hat{y}, B) := \frac{1}{B} \sum_{i=1}^B \text{Acc}(\mathcal{D}_{\text{test}}, \hat{y}^{(i)}) \quad (1)$$

244 The AUC incorporates performance in early stages (low budget) as well as capabilities to push the
 245 classifier in later stages (high budget). AL algorithms have to perform well in both scenarios.

246 Since AUC is still influenced by the budget, we define a set of rules to set this hyperparameter
 247 upfront, so that we are not favoring a subset of algorithms by handcrafting a budget. In this work, we
 248 choose the budget per dataset to be the first point at which one of 2 stopping conditions apply: (i) an
 249 algorithm (except Oracle) manages to reach 99% of the full-dataset-performance (using the smallest
 250 query size) or (ii) the best algorithm (except oracle) did not improve the classifier’s accuracy by at
 251 least 2% in the last 20% of iterations. The first rule follows [10], while the second rule prevents
 252 excessive budgets for cases with diminishing returns in the budget. The resulting budgets can be
 253 found in Tab. 2.

254 As described in Sec. 4.1, we restart each experiment multiple times. Each restart retains the train/test
 255 split (often given by the dataset itself), but creates a new validation split that is sampled (based on
 256 $s_{\mathcal{D}}$) from the entire dataset (not just the seed set $\mathcal{L}^{(0)}$).

257 Apart from plotting standard performance curves and reporting their AUC values per dataset in
 258 App. G, we primarily rely on ranks to aggregate the performance of an acquisition function across
 259 datasets. For each dataset and query size, the AUC values of all acquisition functions are sorted and
 260 assigned a rank based on position, with the best rank being 1. These ranks can safely be averages
 261 across datasets as they are no longer subjected to scaling differences of each dataset. Additionally,
 262 we employ Critical Difference (CD) diagrams (like Fig. 2) for statistical testing. CD diagrams use
 263 the Wilcoxon signed-rank test, which is a variant of the paired T-test, to find significant differences
 264 of ranks between acquisition functions. For these diagrams, each combination of dataset, query
 265 size and run is considered a separate experiment, i.e. the results of Dataset1-QuerySize1-run5
 266 of an acquisition function x is only compared to the results of Dataset1-QuerySize1-run5 of
 267 acquisition function y . Due to the large number of restarts and the wide range of datasets and query
 268 sizes, we can provide very accurate significance tests. For a detailed description of how every CD
 269 diagram is created, please refer to App. F.

270 5 Experiments

271 5.1 Implementation Details

272 At each iteration i the acquisition function Ω picks an unlabeled datapoint based on a fixed set of in-
 273 formation $\{\mathcal{L}^{(i)}, \mathcal{U}^{(i)}, B, |\mathcal{L}^{(i)}| - |\mathcal{L}^{(1)}|, \text{acc}^{(i)}, \text{acc}^{(1)}, \hat{y}^{(i)}, \text{opt}_{\hat{y}}\}$, where $\text{opt}_{\hat{y}}$ is the optimizer used
 274 to fit $\hat{y}^{(i)}$. This set grants full access to the labeled and unlabeled set, as well as all parameters of the
 275 classifier and the optimizer. Additionally, we provide meta-information, like the size of the seed set
 276 through $|\mathcal{L}^{(i)}| - |\mathcal{L}^{(1)}|$, the remaining budget though the addition of B and the classifiers potential
 277 though $\text{acc}^{(1)}$ and $\text{acc}^{(i)}$. We allow acquisition functions to derive information from this set, e.g.
 278 predictions of the classifier $\hat{y}^{(i)}(x)$; $x \in \mathcal{U}^{(i)} \cup \mathcal{L}^{(i)}$, clustering, or even training additional models.
 279 However, the algorithm may not incorporate external information e.g. other datasets, queries to re-
 280 cover additional labels, additional training steps for \hat{y} , or the test/validation set.

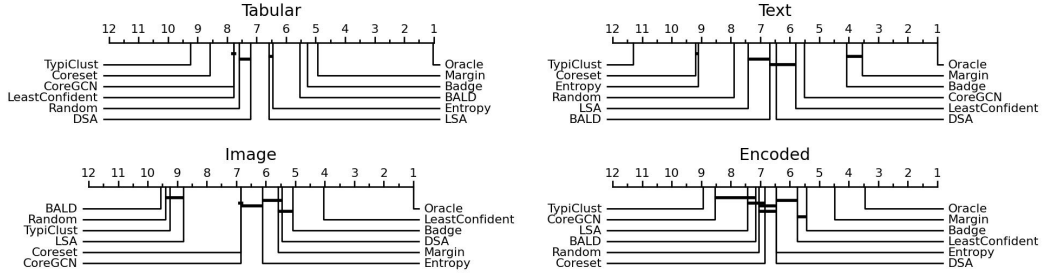
281 For our study we selected acquisition functions with good performances reported by multiple dif-
 282 ferent sources that can work with the set of information stated above. For a list of all acquisition
 283 functions, please refer to Table 3, with detailed descriptions being found in Appendix C.

284 The model \hat{y} can be trained in two ways. Either the parameters of the model are reset to a fixed initial
 285 setting $\hat{y}^{(0)}$ after each AL iteration and the classifier is trained from scratch with the updated labeled

Table 3: Performances for acquisition functions on real-world datasets, aggregated for un-encoded and encoded datasets. Performance is shown as average ranks over restarts (1.0 is the best rank). Algorithms are sorted by aggregated performance on un-encoded datasets.

	Splice	DNA	USPS	Cfr10	FMnist	TopV2	News	Un-enc.	Enc.
Oracle	1.0 ± 0.01	1.0 ± 0.01	1.0 ± 0.0	1.0 ± 0.0	1.0 ± 0.0	1.0 ± 0.01	1.0 ± 0.0	1.0	2.0
Margin	6.6 ± 0.02	4.3 ± 0.01	2.1 ± 0.01	6.3 ± 0.01	4.4 ± 0.0	2.4 ± 0.01	3.7 ± 0.0	4.3	4.2
Badge	5.2 ± 0.01	6.3 ± 0.01	2.9 ± 0.01	5.2 ± 0.01	4.7 ± 0.0	3.3 ± 0.01	3.5 ± 0.0	4.5	5.4
LeastConf	9.2 ± 0.02	10.3 ± 0.02	8.1 ± 0.02	2.1 ± 0.01	4.0 ± 0.0	7.9 ± 0.02	3.0 ± 0.01	6.4	6.5
DSA	7.4 ± 0.02	7.3 ± 0.01	7.5 ± 0.01	5.4 ± 0.01	5.1 ± 0.0	6.0 ± 0.02	7.3 ± 0.01	6.6	6.7
BALD	4.0 ± 0.01	4.7 ± 0.01	5.4 ± 0.01	12.0 ± 0.01	7.6 ± 0.0	7.6 ± 0.02	5.0 ± 0.0	6.6	7.6
CoreGCN	6.9 ± 0.01	4.9 ± 0.01	10.4 ± 0.01	7.6 ± 0.01	6.5 ± 0.01	4.0 ± 0.01	6.8 ± 0.0	6.7	8.2
Entropy	6.6 ± 0.02	3.9 ± 0.01	7.6 ± 0.01	7.6 ± 0.01	4.9 ± 0.01	9.8 ± 0.02	9.6 ± 0.0	7.1	6.5
LSA	6.1 ± 0.01	6.8 ± 0.01	5.3 ± 0.01	7.7 ± 0.01	10.6 ± 0.01	7.5 ± 0.01	7.3 ± 0.01	7.3	7.5
Random	9.0 ± 0.01	9.3 ± 0.01	5.3 ± 0.01	8.4 ± 0.01	11.1 ± 0.0	7.9 ± 0.01	8.0 ± 0.0	8.4	6.9
Coreset	7.1 ± 0.01	9.0 ± 0.01	10.5 ± 0.01	6.8 ± 0.01	7.1 ± 0.0	8.5 ± 0.02	10.8 ± 0.01	8.5	7.2
TypiClust	8.8 ± 0.01	10.2 ± 0.01	12.0 ± 0.02	7.9 ± 0.01	11.0 ± 0.01	12.0 ± 0.02	12.0 ± 0.01	10.5	9.2

Figure 2: Ranks of each acquisition function aggregated by domain. Horizontal bars indicate a **non**-significant rank difference. The significance is tested via a paired-t-test with $\alpha = 0.05$.



set $\mathcal{L}^{(i)}$, or the previous state $\hat{y}^{(i-1)}$ is retained and the classifier is fine-tuned on $\mathcal{L}^{(i)}$ for a reduced number of epochs. In this work, we use the fine-tuning method for un-encoded datasets to save computational time, while we use the from-scratch training for embedded datasets since they have very small classifiers and this approach generally produces better results. Our fine-tuning scheme always trains for at least one epoch and employs an aggressive early stopping with a patience of 2 afterwards.

5.2 Results on Real-world Data

In Table 3 we provide the rank of each acquisition function per dataset and averaged for each (un-)encoded dataset. Please note, that for Tab 3 we are averaging not only over runs, but also over query sizes per dataset. For the results per query size, please refer to App. E.

As stated in contribution C4, our results on real-world data shows significant differences in the performance of the tested algorithms between data domains. Not only do some algorithms overperform on some domains (like least confidence sampling on Images), but the Top-3 of algorithms (except Oracle) does not contain the same three algorithms for any two domains. Most interestingly, the image domain, which received the most attention in benchmarking so far could even be considered an outlier, as this is the only domain where the Top-1 algorithm changes. This highlights the dire need for diverse data domains in AL benchmarking.

6 Synthetic Datasets for AL

AL approaches can be categorized into two types, uncertainty and geometric approaches. Typical members of the first category are variants of uncertainty sampling like entropy-, margin and least-confident-sampling [24] as well as BALD [7]. Typical members of the second category are clustering approaches like Coreset [23], BADGE [1] and TypiClust [8]. Both types of algorithms have principled shortcomings in terms of the utilized information that makes them unsuitable for

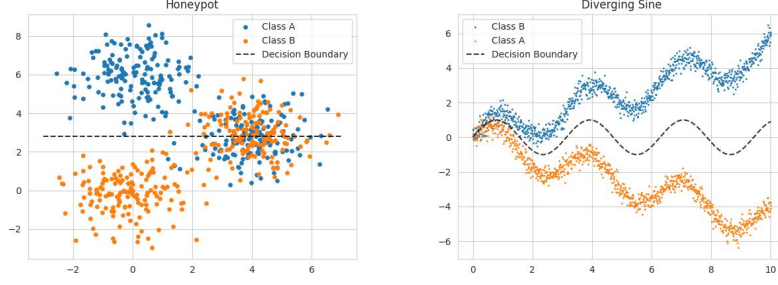
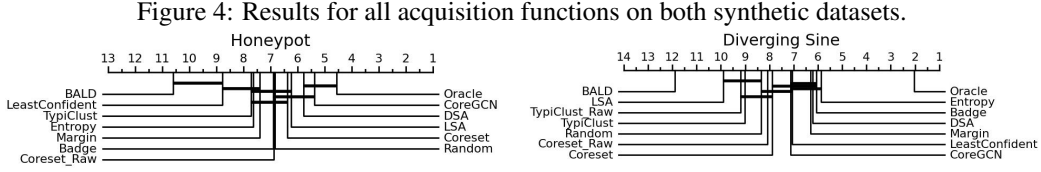


Figure 3: Synthetic "Honeypot" and "Diverging Sine" datasets. The optimal decision boundary is not part of the dataset and serves only as a visual guide.



certain data distributions. To test for these specific shortcomings, we created two synthetic datasets, namely "Honeypot" and "Diverging Sine", that are hard to solve for methods focused on the classifier's decision boundary or data clustering respectively. To avoid algorithms memorizing these datasets they are generated from scratch for each experiment, depending on s_D .

Honeypot creates two easy to distinguish clusters with 150 samples each and one overlapping "honeypot" that represents a noisy region of the dataset with potentially miss-labeled, miss-measured or generally adverse samples. This honeypot contains 150 samples of each class, creating a balance of 50% beneficial samples and 50% adverse samples in the dataset. The honeypot is located on the likely decision boundary of a classifier that is trained on the beneficial samples to maximize its negative impact on purely uncertainty based acquisition functions. Diverging Sine samples the datapoints for each class from two diverging sinusoidal functions that are originating from the same y-intercept. This creates a challenging region on the left hand side, where a lot of datapoints need to be sampled and an easy region on the right hand side, where very few datapoints are enough. The repeating nature of a sin function encourages diversity based acquisition functions to equally sample the entire length, drastically oversampling the right hand side of the dataset. Each class has 500 datapoints. Both datasets have a budget of $B = 60$ and are tested with query sizes 1 and 5.

Results for the Honeypot dataset reveal expected shortcomings of uncertainty sampling algorithms like margin, entropy and least confident sampling as well as BALD. In addition, BADGE is underperforming for this dataset compared to real-world data. Results for Diverging Sine also confirm expected behavior, as clustering algorithms (Coreset, TypiClust) fall behind uncertainty algorithms (Entropy-, Margin-Sampling), with the exception of BADGE.

We provide a very small ablation study on the importance of the embeddings by testing a version of Coreset and TypiClust on this dataset that does not use the embeddings produced by the classification model, but rather clusters the data directly. "Coreset Raw" and "TypiClust Raw" both perform worse than their embedding-based counterpart.

6.1 Results on Synthetic Data

Our results on Honeypot reveal principled shortcomings for the two best algorithms in BADGE and margin sampling. Both are vulnerable to adverse samples or simply measurement noise, which highlights the need for further research in this area.

Finally, the fact that BADGE is able to perform well on Diverging Sine highlights the importance of

341 embeddings for the clustering algorithms, as the so-called gradient embedding from BADGE seems
342 to be able to encode uncertainty information, guiding the selection into the left hand regions of the
343 dataset. We also show that embeddings are generally useful for this dataset, by providing results for
344 "Coreset Raw" and "TypiClust Raw".

345 **7 Conclusion**

346 We strongly advocate to test newly proposed AL algorithms not only on a wide variety of real data
347 domains, but also to pay close attention to the Honeypot and Diverging Sine datasets to reveal princi-
348 pled shortcomings of the algorithm in question. Both tasks can be easily carried out by implementing
349 the new acquisition function into our code base.

350 **Acknowledgement** anonymous

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425 **A AL Recommendations from Ji et al.**

426 TODO

427 **B AL Pitfalls from Lueth et al.**

428 TODO

429 **C Acquisition Functions**

430 **Uncertainty Sampling** tries to find the sample that the classifier is most uncertain about by
431 computing heuristics of the class probabilities. For our benchmark, we use entropy and margin
432 (a.k.a. best-vs-second-best) sampling.

433 **BALD** [12] applies the query-by-committee strategy of model ensembles to a single model by
434 interpreting the classifier’s parameters as distributions and then sample multiple outputs from them
435 via Monte-Carlo dropout.

436 **BADGE** [1] uses gradient embeddings of unlabeled points to select samples where the classifier
437 is expected to change a lot. The higher the magnitude of the gradient the higher the expected
438 improvement in model performance.

439 **Coreset** [23] employs K-Means clustering trying to cover the whole data distribution. Selects
440 the unlabeled sample that is the furthest away from all cluster centers. Clustering is done in a
441 semantically meaningful space by encoding the data with the current classifier \hat{y} . In this work, we
442 use the greedy variant of Coreset.

443 **TypiClust** [8] relies on clustering similar to Coreset, but proposes a new measure called “Typical-
444 ity” to select unlabeled samples. It selects points that are in the densest regions of clusters that do
445 not contain labeled samples yet. Clustering is done in a semantically meaningful space by encoding
446 the data with the current classifier \hat{y} . It has to be pointed out that TypiClust was designed for
447 low-budget scenarios, but we think it is still worthwhile to test and compare this algorithm with
448 higher budgets.

449 **Core-GCN** [3] TODO

450 **DSA/LSA** [11] TODO

451 **Excluded Algorithms**

452 **Learning Loss for AL** [26] Introduces an updated training of the classification model with an
453 auxiliary loss and therefore cannot be compared fairly against classification models without this
454 boosted training regime.

455 **Reinforcement Learning Algorithms**

456

457 **D Difference of Ranks with 3 Repetitions**

458 Table 4 and Table 5 follow the exact same computation of ranks that created the main result (Table
459 3) with the only difference being a reduced number of runs per acquisition function. For each table
460 we uniformly sampled 3 runs from the available 50 per acquisition function.

461 We can observe significant differences between the two tables:

462 **Purple:** A multitude of rank differences of acquisition functions for specific datasets, some as high
463 as 4.7 ranks for TypiClust on the Splice dataset

464 **Olive:** Well separated acquisition functions in Tab. 5 (Margin and BADGE) are almost indistin-
465 guishable in Tab 4

466 **Red:** BALD lost 2 places in the overall ranking and Entropy gained 2

467 Even though the overall ordering of acquisition functions stayed relatively unchanged due to the
468 averaging across many datasets, each individual dataset was subject to drastic permutations. This
469 highlights the need for many repetitions in AL experiments.

Table 4: Ranks of all acquisition functions per dataset. First random draw of 3 runs from the overall pool of 50.

	Splice	DNA	USPS	Cifar10	FMnist	TopV2	News	Unencoded	Encoded
Oracle	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	2.1
Margin	6.0	7.3	2.0	6.7	5.3	2.3	3.3	4.7	4.4
Badge	6.0	7.3	3.0	6.7	5.0	3.3	4.0	5.0	5.3
BALD	3.3	4.7	5.3	12.0	7.0	6.3	4.3	6.1	7.9
CoreGCN	8.7	3.7	10.7	6.3	5.3	4.0	7.7	6.6	9.1
DSA	8.3	6.3	7.7	7.7	4.3	6.7	6.7	6.8	6.1
LeastConf	10.0	12.0	8.0	3.0	4.3	9.3	2.3	7.0	6.7
LSA	5.7	6.7	5.3	6.7	10.7	7.7	7.0	7.1	6.3
Entropy	11.0	3.3	7.3	4.0	6.7	8.3	9.7	7.2	7.0
Random	7.7	8.7	5.3	8.0	11.0	8.0	9.0	8.2	6.3
Coreset	4.7	10.3	10.3	7.7	6.0	9.0	11.0	8.4	7.2
TypiClust	5.7	6.7	12.0	8.3	11.3	12.0	12.0	9.7	9.7

Table 5: Ranks of all acquisition functions per dataset. Second random draw of 3 runs from the overall pool of 50.

	Splice	DNA	USPS	Cifar10	FMnist	TopV2	News	Unencoded	Encoded
Oracle	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	2.4
Margin	6.0	3.3	2.0	5.7	2.0	2.0	4.3	3.6	3.8
Badge	6.0	9.0	3.0	3.0	5.7	3.7	3.3	4.8	4.9
CoreGCN	4.3	6.3	10.3	7.3	5.3	5.7	5.3	6.4	8.1
DSA	8.7	7.3	7.3	6.0	4.3	5.3	6.0	6.4	6.5
BALD	4.7	4.0	4.7	12.0	7.3	6.7	6.7	6.6	7.5
Entropy	6.7	4.7	7.7	5.3	5.0	7.3	9.3	6.6	6.8
LeastConf	7.7	10.0	8.3	3.3	6.0	8.7	3.0	6.7	7.3
LSA	7.7	5.3	6.0	9.0	11.0	9.0	7.3	7.9	7.5
Random	9.3	8.0	5.0	8.7	11.7	8.3	8.7	8.5	7.6
Coreset	6.0	10.7	10.7	8.0	8.3	8.3	11.0	9.0	6.3
TypiClust	10.0	8.3	12.0	8.7	10.3	12.0	12.0	10.5	9.4

470 E AUCs by Query Size

Table 6: AUC values for each dataset that supports query size 1.

	Splice	SpliceEncoded	DNA	DNAEncoded	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	DivergingSin	ThreeClust
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.721+-0.013	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.957+-0.009	0.783+-0.03
Margin	0.769+-0.021	0.678+-0.032	0.806+-0.013	0.642+-0.047	0.858+-0.006	0.426+-0.038	0.653+-0.013	0.68+-0.012	0.861+-0.009	0.941+-0.018	0.704+-0.074
Badge	0.767+-0.02	0.661+-0.026	0.78+-0.014	0.642+-0.046	0.83+-0.008	0.371+-0.035	0.656+-0.013	0.68+-0.009	0.826+-0.024	0.941+-0.017	0.69+-0.083
LeastConfident	0.779+-0.019	0.68+-0.032	0.809+-0.01	0.629+-0.05	0.846+-0.009	0.421+-0.039	0.668+-0.014	0.685+-0.009	0.843+-0.013	0.94+-0.016	0.692+-0.094
DSA	0.766+-0.021	0.691+-0.022	0.803+-0.01	0.646+-0.032	0.829+-0.01	0.431+-0.05	0.663+-0.014	0.679+-0.01	0.844+-0.017	0.941+-0.014	0.731+-0.032
BALD	0.78+-0.014	0.649+-0.04	0.784+-0.01	0.632+-0.042	0.819+-0.01	0.242+-0.046	0.666+-0.014	0.644+-0.018	0.815+-0.024	0.928+-0.014	0.698+-0.043
CoreGCN	0.765+-0.021	0.686+-0.023	0.804+-0.012	0.646+-0.03	0.753+-0.016	0.39+-0.044	0.623+-0.018	0.647+-0.012	0.85+-0.01	0.938+-0.014	0.731+-0.028
Entropy	0.768+-0.022	0.678+-0.035	0.812+-0.013	0.635+-0.045	0.83+-0.011	0.399+-0.035	0.663+-0.013	0.681+-0.011	0.815+-0.021	0.942+-0.017	0.696+-0.083
LSA	0.772+-0.016	0.68+-0.026	0.787+-0.012	0.618+-0.036	0.821+-0.009	0.422+-0.037	0.613+-0.014	0.642+-0.012	0.816+-0.013	0.932+-0.016	0.727+-0.033
Random	0.76+-0.016	0.674+-0.027	0.774+-0.013	0.63+-0.035	0.823+-0.009	0.404+-0.036	0.613+-0.014	0.639+-0.013	0.815+-0.012	0.933+-0.017	0.721+-0.036
Coreset	0.772+-0.016	0.69+-0.017	0.79+-0.012	0.638+-0.041	0.767+-0.016	0.404+-0.046	0.659+-0.011	0.684+-0.009	0.826+-0.022	0.937+-0.014	0.734+-0.031
TypiClust	0.762+-0.016	0.685+-0.025	0.778+-0.01	0.663+-0.028	0.828+-0.007	0.396+-0.046	0.653+-0.013	0.649+-0.007	0.831+-0.011	0.934+-0.018	0.727+-0.033

Table 7: AUC values for each dataset that supports query size 5.

	Splice	SpliceEncoded	DNA	DNAEncoded	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEncoded	TopV2	DivergingSin	ThreeClust
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.721+-0.013	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.957+-0.009	0.783+-0.03
Margin	0.765+-0.021	0.662+-0.032	0.794+-0.011	0.611+-0.05	0.855+-0.006	0.508+-0.02	0.656+-0.014	0.678+-0.009	0.848+-0.013	0.923+-0.019	0.697+-0.055
Badge	0.768+-0.014	0.646+-0.035	0.785+-0.011	0.624+-0.036	0.846+-0.007	0.48+-0.021	0.647+-0.012	0.67+-0.009	0.847+-0.01	0.924+-0.019	0.72+-0.036
LeastConfident	0.763+-0.023	0.643+-0.034	0.798+-0.013	0.585+-0.065	0.831+-0.014	0.478+-0.028	0.67+-0.01	0.681+-0.009	0.819+-0.023	0.921+-0.019	0.675+-0.072
DSA	0.765+-0.023	0.653+-0.029	0.793+-0.009	0.613+-0.034	0.822+-0.01	0.489+-0.024	0.661+-0.013	0.662+-0.012	0.833+-0.02	0.924+-0.018	0.718+-0.034
BALD	0.775+-0.018	0.641+-0.034	0.801+-0.013	0.592+-0.054	0.84+-0.008	0.332+-0.054	0.681+-0.011	0.681+-0.011	0.824+-0.023	0.893+-0.035	0.673+-0.041
CoreGCN	0.759+-0.018	0.662+-0.027	0.79+-0.011	0.62+-0.03	0.755+-0.011	0.45+-0.03	0.604+-0.016	0.609+-0.013	0.837+-0.014	0.922+-0.018	0.723+-0.034
Entropy	0.765+-0.022	0.66+-0.03	0.798+-0.011	0.611+-0.054	0.823+-0.013	0.464+-0.024	0.663+-0.013	0.672+-0.011	0.801+-0.025	0.924+-0.02	0.689+-0.066
LSA	0.769+-0.016	0.654+-0.032	0.781+-0.013	0.61+-0.041	0.82+-0.009	0.484+-0.022	0.617+-0.012	0.641+-0.011	0.816+-0.012	0.915+-0.018	0.718+-0.038
Random	0.758+-0.015	0.655+-0.026	0.771+-0.013	0.623+-0.031	0.82+-0.009	0.476+-0.024	0.616+-0.016	0.637+-0.012	0.812+-0.014	0.921+-0.018	0.713+-0.034
Coreset	0.765+-0.017	0.663+-0.023	0.784+-0.014	0.603+-0.034	0.765+-0.015	0.449+-0.022	0.657+-0.009	0.674+-0.009	0.817+-0.017	0.92+-0.017	0.713+-0.035
TypiClust	0.759+-0.014	0.641+-0.028	0.775+-0.01	0.603+-0.04	0.757+-0.02	0.465+-0.027	0.596+-0.014	0.567+-0.012	0.727+-0.026	0.916+-0.02	0.693+-0.045

Table 8: AUC values for each dataset that supports query size 20.

	Splice	SpliceEncoded	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	News
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.49+-0.003
Margin	0.759+-0.027	0.618+-0.04	0.779+-0.013	0.847+-0.008	0.439+-0.027	0.656+-0.01	0.67+-0.011	0.823+-0.014	0.464+-0.007
Badge	0.767+-0.013	0.619+-0.033	0.776+-0.013	0.845+-0.006	0.44+-0.019	0.647+-0.013	0.665+-0.007	0.827+-0.016	0.463+-0.007
LeastConfident	0.751+-0.02	0.597+-0.05	0.748+-0.025	0.798+-0.027	0.391+-0.024	0.665+-0.013	0.669+-0.011	0.775+-0.035	0.467+-0.008
DSA	0.759+-0.02	0.599+-0.034	0.769+-0.013	0.809+-0.012	0.421+-0.023	0.647+-0.014	0.63+-0.013	0.793+-0.026	0.459+-0.01
BALD	0.768+-0.022	0.57+-0.037	0.784+-0.015	0.822+-0.009	0.298+-0.039	0.675+-0.008	0.673+-0.01	0.789+-0.024	0.468+-0.009
CoreGCN	0.759+-0.018	0.612+-0.039	0.774+-0.012	0.754+-0.016	0.397+-0.026	0.587+-0.015	0.583+-0.015	0.807+-0.018	0.453+-0.006
Entropy	0.759+-0.027	0.618+-0.038	0.773+-0.015	0.803+-0.019	0.372+-0.022	0.656+-0.011	0.65+-0.012	0.773+-0.031	0.451+-0.007
LSA	0.761+-0.014	0.611+-0.039	0.768+-0.015	0.816+-0.009	0.411+-0.022	0.621+-0.01	0.635+-0.011	0.796+-0.016	0.452+-0.007
Random	0.755+-0.014	0.612+-0.039	0.763+-0.012	0.818+-0.009	0.439+-0.019	0.622+-0.013	0.633+-0.012	0.795+-0.016	0.45+-0.006
Coreset	0.759+-0.016	0.601+-0.034	0.764+-0.015	0.757+-0.015	0.39+-0.029	0.647+-0.009	0.651+-0.011	0.784+-0.026	0.435+-0.012
TypiClust	0.751+-0.012	0.551+-0.036	0.76+-0.016	0.643+-0.026	0.411+-0.024	0.488+-0.02	0.449+-0.017	0.652+-0.035	0.406+-0.011

Table 9: AUC values for each dataset that supports query size 50.

	Splice	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	News
Oracle	0.803+-0.012	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.49+-0.003
Margin	0.747+-0.023	0.751+-0.019	0.828+-0.009	0.363+-0.031	0.64+-0.013	0.653+-0.01	0.774+-0.029	0.46+-0.006
Badge	0.758+-0.017	0.754+-0.018	0.831+-0.008	0.376+-0.028	0.632+-0.013	0.649+-0.011	0.781+-0.026	0.462+-0.007
LeastConfident	0.731+-0.025	0.688+-0.041	0.761+-0.037	0.291+-0.03	0.644+-0.013	0.65+-0.011	0.73+-0.049	0.462+-0.009
DSA	0.748+-0.021	0.738+-0.018	0.783+-0.016	0.346+-0.027	0.624+-0.014	0.588+-0.016	0.748+-0.041	0.45+-0.011
BALD	0.76+-0.017	0.756+-0.018	0.796+-0.016	0.241+-0.026	0.65+-0.009	0.645+-0.01	0.746+-0.038	0.455+-0.007
CoreGCN	0.755+-0.016	0.745+-0.018	0.752+-0.019	0.328+-0.027	0.581+-0.015	0.568+-0.018	0.771+-0.025	0.453+-0.007
Entropy	0.747+-0.024	0.748+-0.018	0.778+-0.024	0.275+-0.026	0.633+-0.011	0.625+-0.012	0.734+-0.036	0.442+-0.007
LSA	0.754+-0.013	0.749+-0.019	0.807+-0.01	0.341+-0.029	0.613+-0.012	0.625+-0.01	0.763+-0.025	0.45+-0.006
Random	0.746+-0.012	0.745+-0.015	0.806+-0.008	0.379+-0.028	0.615+-0.014	0.621+-0.01	0.759+-0.026	0.448+-0.006
Coreset	0.751+-0.016	0.733+-0.019	0.74+-0.017	0.325+-0.034	0.624+-0.012	0.608+-0.013	0.731+-0.045	0.432+-0.012
TypiClust	0.749+-0.016	0.736+-0.016	0.586+-0.038	0.348+-0.027	0.451+-0.024	0.375+-0.022	0.614+-0.046	0.397+-0.012

Table 10: AUC values for each dataset that supports query size 100.

	Splice	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	News
Oracle	0.803+-0.012	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.49+-0.003
Margin	0.733+-0.024	0.711+-0.027	0.799+-0.013	0.473+-0.026	0.629+-0.012	0.628+-0.009	0.455+-0.006
Badge	0.743+-0.014	0.714+-0.032	0.804+-0.013	0.472+-0.029	0.623+-0.01	0.621+-0.01	0.456+-0.006
LeastConfident	0.715+-0.033	0.639+-0.05	0.708+-0.034	0.23+-0.034	0.631+-0.013	0.62+-0.012	0.457+-0.008
DSA	0.729+-0.021	0.697+-0.031	0.753+-0.021	0.427+-0.028	0.609+-0.013	0.546+-0.017	0.442+-0.01
BALD	0.744+-0.015	0.718+-0.024	0.765+-0.021	0.285+-0.046	0.632+-0.009	0.609+-0.01	0.444+-0.007
CoreGCN	0.742+-0.015	0.713+-0.025	0.744+-0.019	0.433+-0.032	0.583+-0.013	0.554+-0.015	0.448+-0.007
Entropy	0.733+-0.023	0.713+-0.031	0.743+-0.026	0.395+-0.037	0.618+-0.012	0.59+-0.012	0.432+-0.007
LSA	0.738+-0.017	0.716+-0.027	0.789+-0.011	0.439+-0.03	0.609+-0.013	0.608+-0.01	0.447+-0.006
Random	0.733+-0.013	0.713+-0.023	0.789+-0.012	0.468+-0.024	0.611+-0.01	0.606+-0.01	0.446+-0.005
Coreset	0.735+-0.019	0.698+-0.026	0.721+-0.021	0.396+-0.024	0.608+-0.012	0.562+-0.016	0.426+-0.012
TypiClust	0.733+-0.016	0.704+-0.025	0.592+-0.042	0.427+-0.027	0.501+-0.02	0.338+-0.02	0.383+-0.012

Table 11: AUC values for each dataset that supports query size 500.

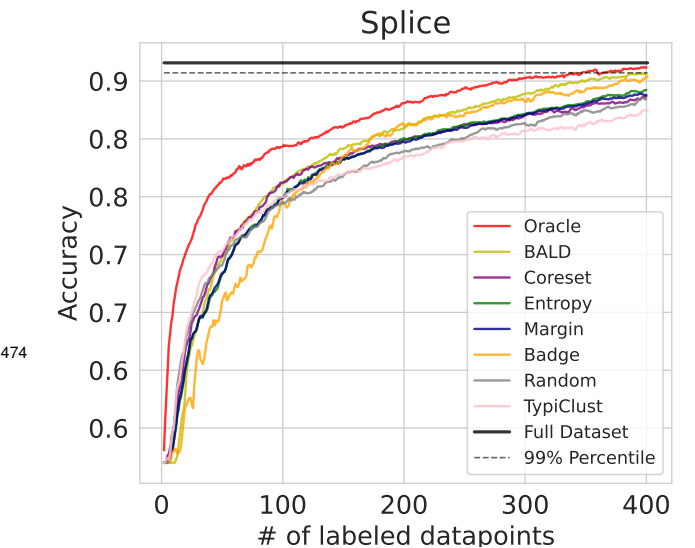
	Cifar10	FashionMnist
Oracle	0.689+-0.001	0.905+-0.001
Margin	0.556+-0.008	0.882+-0.004
Badge	0.56+-0.008	0.883+-0.005
LeastConfident	0.591+-0.01	0.884+-0.005
DSA	0.56+-0.009	0.882+-0.004
BALD	0.478+-0.014	0.878+-0.003
CoreGCN	0.553+-0.01	0.88+-0.007
Entropy	0.553+-0.009	0.882+-0.006
LSA	0.558+-0.01	0.866+-0.005
Random	0.557+-0.01	0.863+-0.005
Coreset	0.553+-0.007	0.878+-0.006
TypiClust	0.557+-0.009	0.864+-0.004

Table 12: AUC values for each dataset that supports query size 1000.

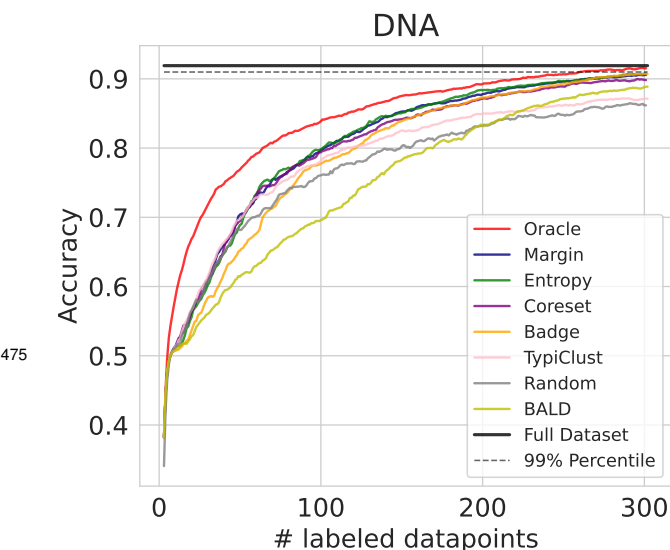
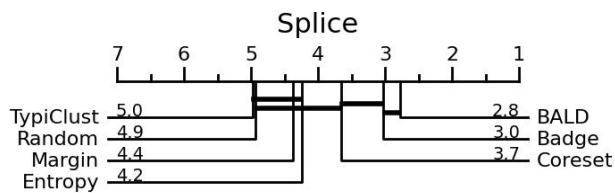
	Cifar10	FashionMnist
Oracle	0.689+-0.001	0.905+-0.001
Margin	0.56+-0.011	0.872+-0.007
Badge	0.562+-0.013	0.871+-0.007
LeastConfident	0.561+-0.012	0.873+-0.006
DSA	0.56+-0.011	0.87+-0.008
BALD	0.535+-0.011	0.866+-0.003
CoreGCN	0.557+-0.011	0.867+-0.012
Entropy	0.557+-0.014	0.871+-0.009
LSA	0.551+-0.012	0.854+-0.009
Random	0.55+-0.01	0.855+-0.006
Coreset	0.562+-0.012	0.869+-0.004
TypiClust	0.552+-0.011	0.854+-0.009

472 **F Critical Difference Diagrams**

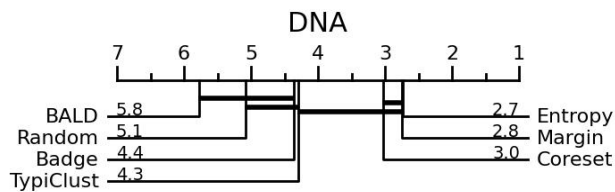
473 **G Individual Results**



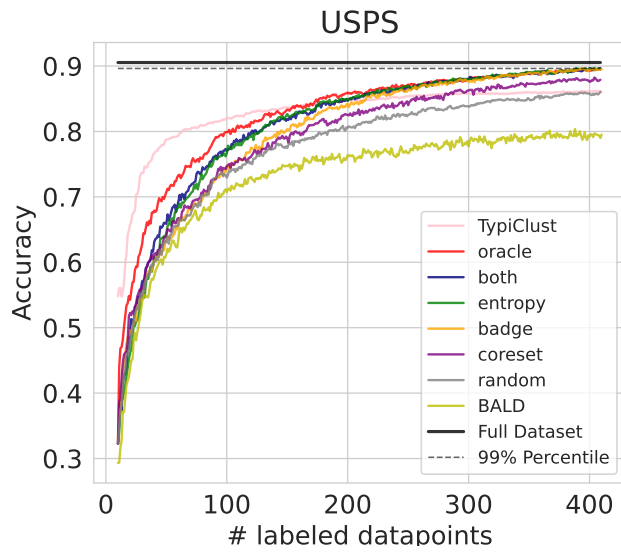
	Splice
Oracle	0.811 ± 0.010
BALD	0.785 ± 0.013
Coreset	0.778 ± 0.014
Entropy	0.774 ± 0.016
Margin	0.773 ± 0.016
Badge	0.770 ± 0.016
Random	0.768 ± 0.014
TypiClust	0.766 ± 0.014



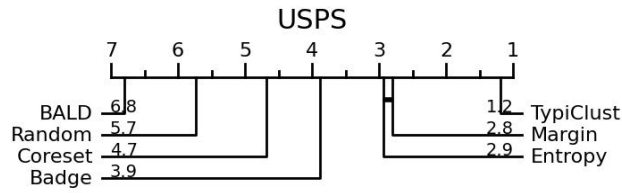
	DNA
Oracle	0.842 ± 0.021
Margin	0.807 ± 0.035
Entropy	0.805 ± 0.038
Coreset	0.796 ± 0.028
Badge	0.789 ± 0.056
TypiClust	0.788 ± 0.036
Random	0.768 ± 0.024
BALD	0.749 ± 0.044



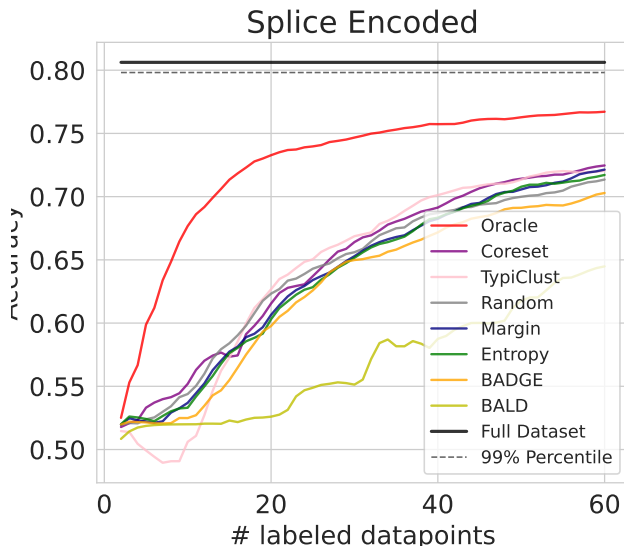
476



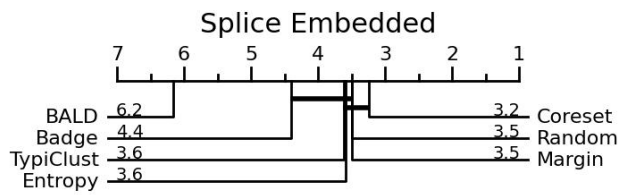
	USPS
TypiClust	0.830 ± 0.007
Oracle	0.823 ± 0.011
Margin	0.809 ± 0.013
Entropy	0.807 ± 0.013
Badge	0.795 ± 0.018
Coreset	0.788 ± 0.017
Random	0.774 ± 0.012
BALD	0.725 ± 0.050

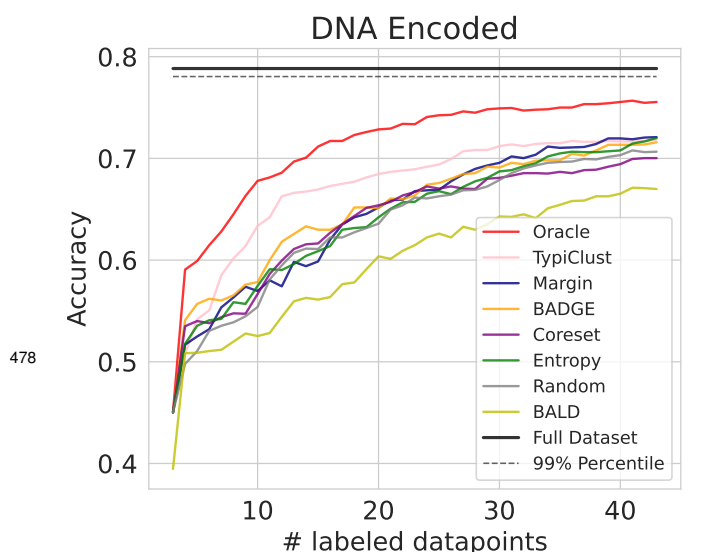


477

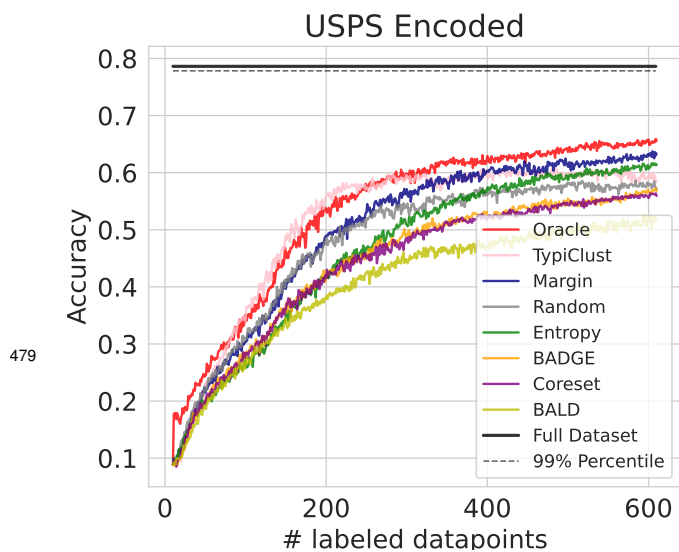
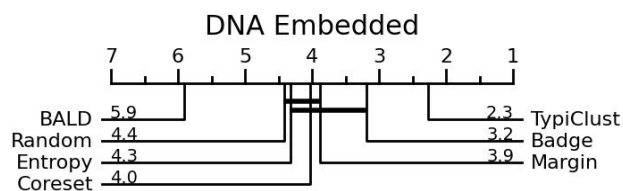


	SpliceEncoded
Oracle	0.728 ± 0.022
Coreset	0.648 ± 0.027
TypiClust	0.645 ± 0.042
Random	0.643 ± 0.036
Entropy	0.636 ± 0.033
Margin	0.636 ± 0.033
Badge	0.627 ± 0.040
BALD	0.565 ± 0.049

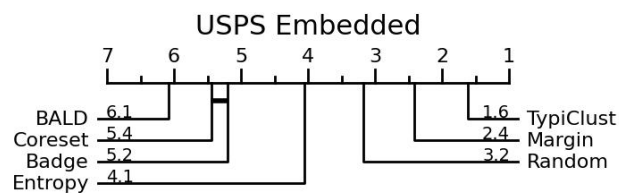


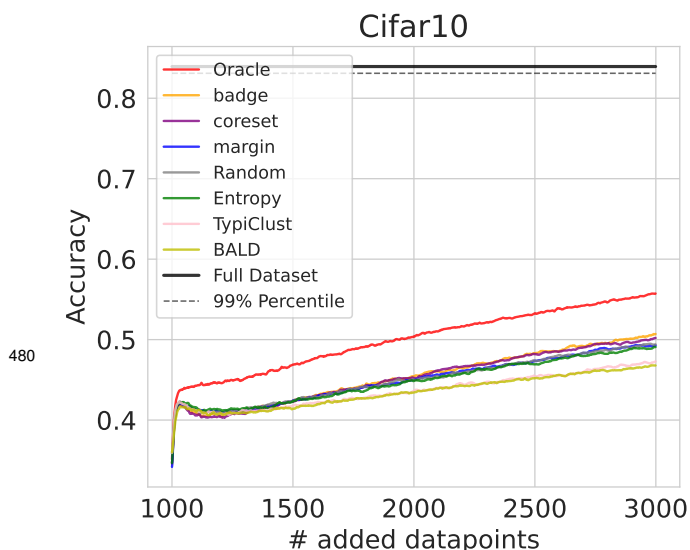


	DNAEncoded
Oracle	0.709 ± 0.023
TypiClust	0.672 ± 0.029
Margin	0.648 ± 0.047
Badge	0.647 ± 0.037
Coreset	0.640 ± 0.041
Entropy	0.629 ± 0.062
Random	0.626 ± 0.035
BALD	0.594 ± 0.039

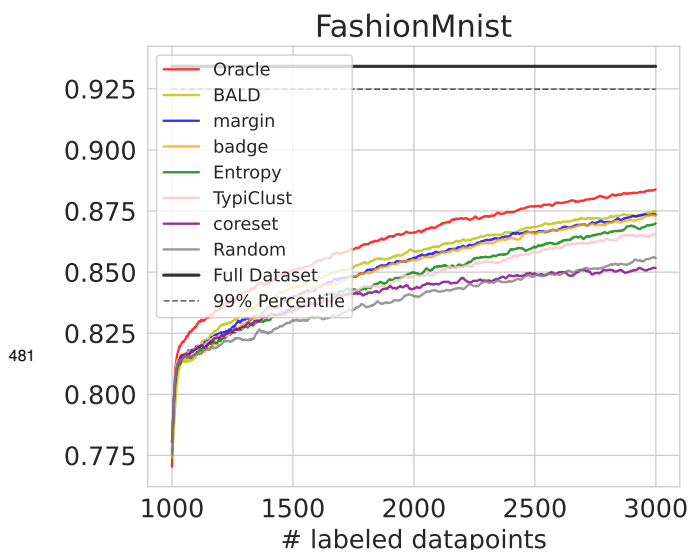
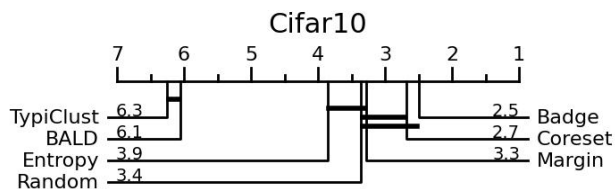


	USPSEncoded
Oracle	0.522 ± 0.021
TypiClust	0.507 ± 0.025
Margin	0.496 ± 0.030
Random	0.468 ± 0.025
Entropy	0.459 ± 0.021
Badge	0.440 ± 0.026
Coreset	0.435 ± 0.027
BALD	0.402 ± 0.052

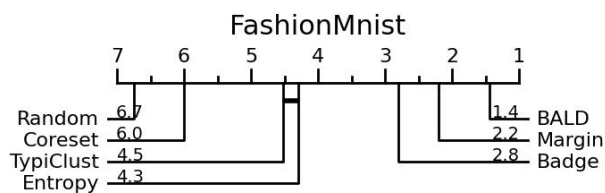


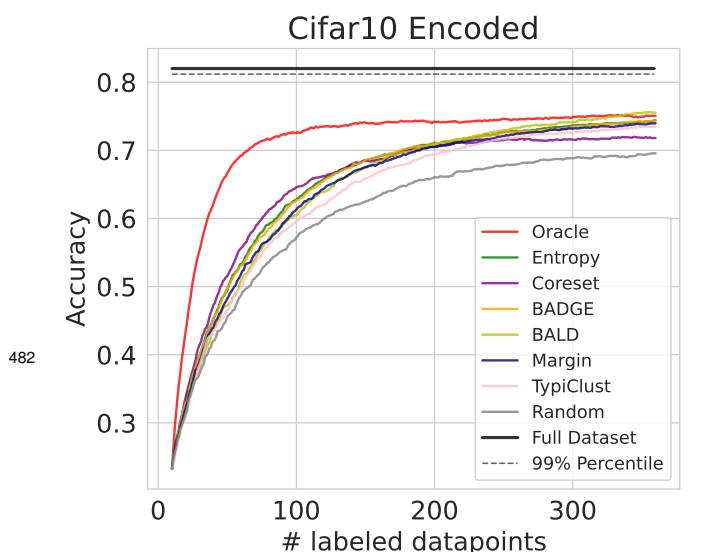


	Cifar10
Oracle	0.500 ± 0.010
Badge	0.453 ± 0.012
Coreset	0.453 ± 0.009
Margin	0.451 ± 0.010
Random	0.450 ± 0.012
Entropy	0.449 ± 0.010
TypiClust	0.436 ± 0.010
BALD	0.436 ± 0.010

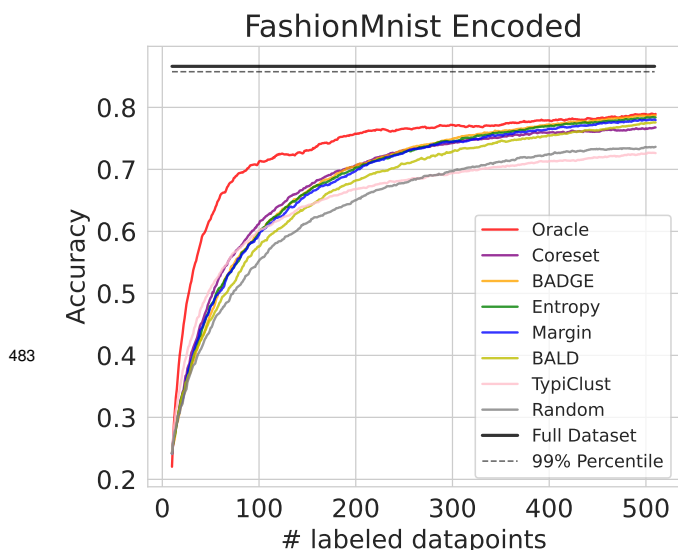
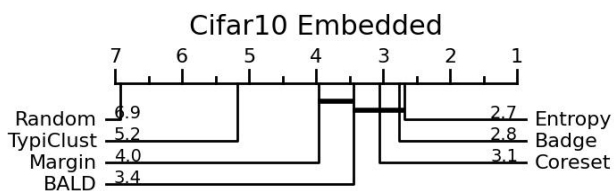


	FashionMnist
Oracle	0.862 ± 0.003
BALD	0.854 ± 0.003
Margin	0.851 ± 0.003
Badge	0.851 ± 0.003
Entropy	0.847 ± 0.004
TypiClust	0.846 ± 0.004
Coreset	0.840 ± 0.004
Random	0.837 ± 0.004

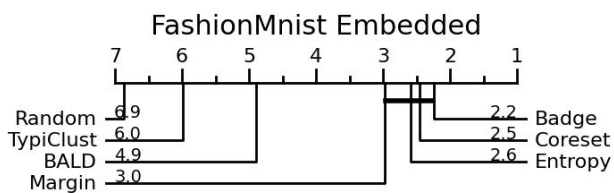




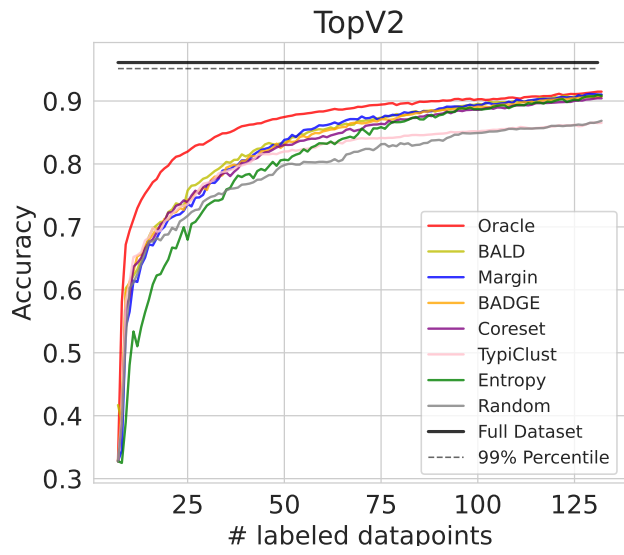
	Cifar10Encoded
Oracle	0.714 ± 0.007
Entropy	0.654 ± 0.013
Coreset	0.653 ± 0.012
Badge	0.653 ± 0.012
BALD	0.650 ± 0.016
Margin	0.647 ± 0.012
TypiClust	0.636 ± 0.009
Random	0.607 ± 0.013



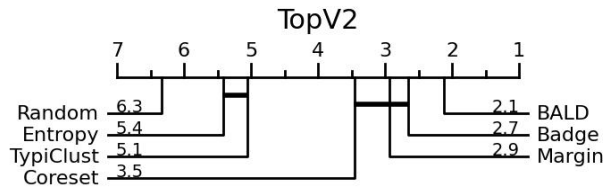
	FashionMnistEncoded
Oracle	0.732 ± 0.006
Coreset	0.686 ± 0.008
Badge	0.685 ± 0.008
Entropy	0.684 ± 0.009
Margin	0.682 ± 0.011
BALD	0.668 ± 0.009
TypiClust	0.652 ± 0.009
Random	0.640 ± 0.011



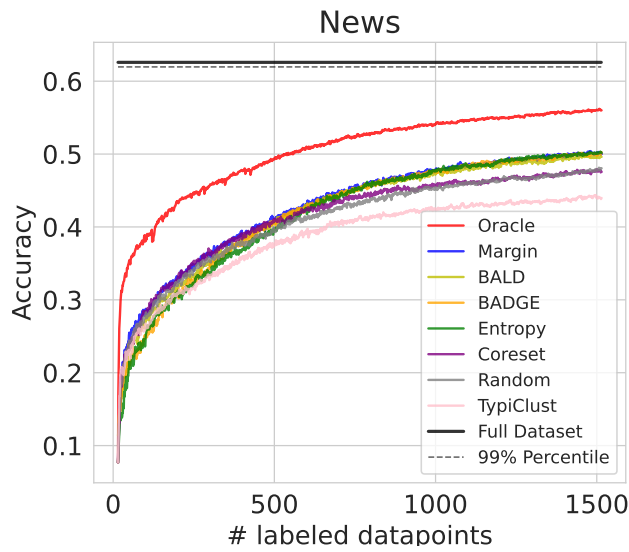
484



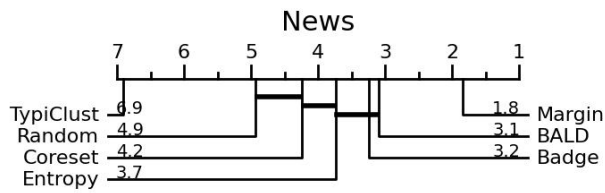
	TopV2
Oracle	0.862 ± 0.006
BALD	0.831 ± 0.013
Badge	0.826 ± 0.015
Coreset	0.823 ± 0.016
Margin	0.822 ± 0.015
TypiClust	0.805 ± 0.015
Entropy	0.801 ± 0.025
Random	0.787 ± 0.015

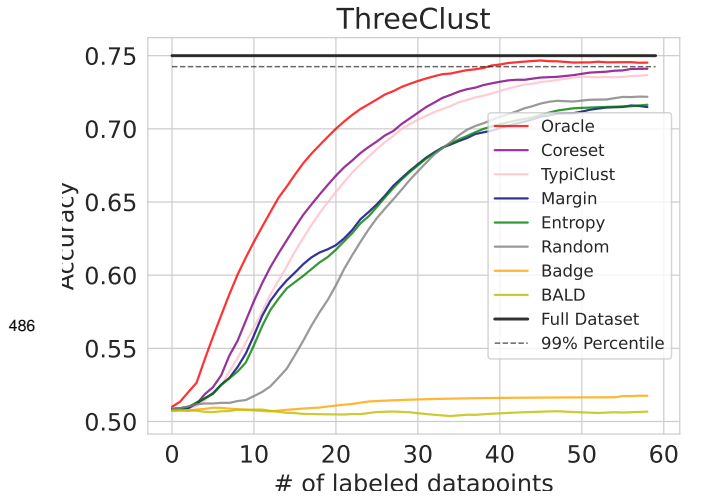


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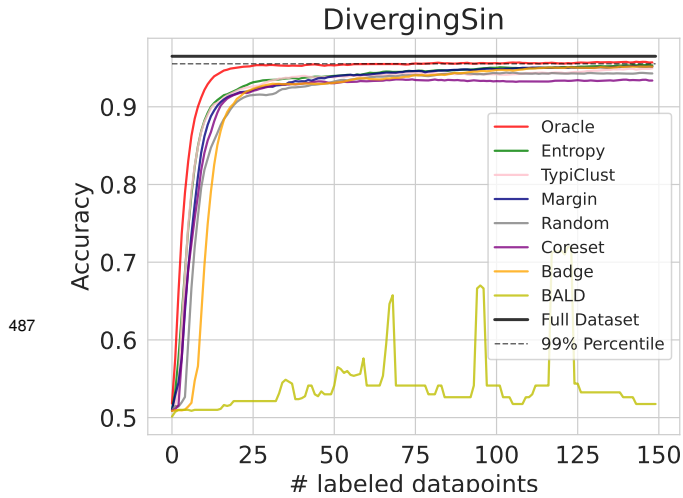
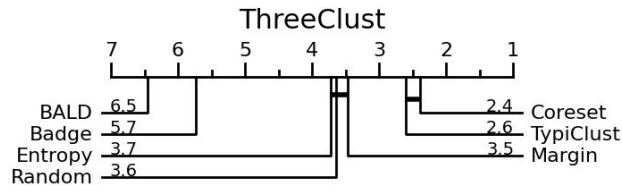


	News
Oracle	0.502 ± 0.005
Margin	0.427 ± 0.007
BALD	0.421 ± 0.008
Badge	0.420 ± 0.011
Entropy	0.416 ± 0.010
Coreset	0.415 ± 0.011
Random	0.409 ± 0.008
TypiClust	0.385 ± 0.010

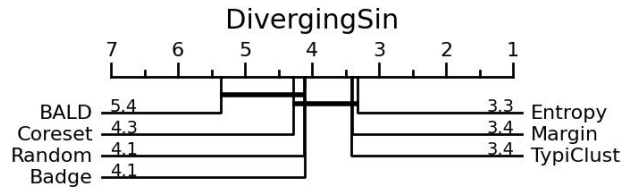




	ThreeClust
Oracle	0.722 ± 0.097
Coreset	0.698 ± 0.058
TypiClust	0.697 ± 0.055
Entropy	0.682 ± 0.098
Random	0.672 ± 0.067
Margin	0.669 ± 0.095
Badge	0.524 ± 0.086
BALD	0.507 ± 0.050



	DivergingSin
Oracle	0.948 ± 0.198
Entropy	0.936 ± 0.202
TypiClust	0.930 ± 0.196
Margin	0.929 ± 0.201
Random	0.919 ± 0.191
Badge	0.914 ± 0.202
Coreset	0.914 ± 0.197
BALD	0.661 ± 0.167



488 H Seeding Strategy

489 We aim to provide an experimental setup that is fully reproducible independent of the dataset, classi-
 490 fication model, or AL algorithm used. For a fair comparison of two AL algorithms, both algorithms
 491 need to receive equal starting conditions in terms of train/validation split, initialization of classifier,

and even the state of minor systems like the optimizer or mini-batch sampler. Even though different implementations might have their own solution to some of these problems, only [10] has described and implemented a fully reproducible pipeline for AL evaluation. The term reproducibility in this work is used as a synonym not only for the reproducibility of an experiment (a final result given a seed), but also the reproducibility of all subsystems independent of each other. The seed for one subsystem should always reproduce the behavior of this subsystem independent of all other subsystems and their seeds. The main obstacle for ensuring reproducibility is the seeding utility in PyTorch, Tensorflow, and other frameworks, whose default choice is a single global seed. Since many subsystems draw random numbers from this seed, all of them influence each other to a point where a single additional draw can completely change the model initialization, data split or the order of training batches. Even though some workarounds exist, e.g. re-setting the seed multiple times, this problem is not limited to the initialization phase, but also extends to the AL iterations and the systems within. We propose an implementation that creates separate Random Number Generators (RNGs) for each of these systems to ensure equal testing conditions even when the AL algorithm, dataset, or classifier changes. We hypothesize that the insufficient setup with global seeds contributes to the ongoing problem of inconsistent results of AL algorithms in different papers.

In summary, we introduce three different seeds: s_Ω for the AL algorithm, $s_\mathcal{D}$ for dataset splitting and mini-batch sampling, and s_θ for model initialization and sampling of dropout masks. Unless stated otherwise, we will keep s_Ω fixed, while $s_\mathcal{D}$ and s_θ are incremented by 1 between restarts to introduce stochasticity into our framework. Some algorithms require a subsample to be drawn from \mathcal{U} in order to reduce the computational cost in each iteration, while others need access to the full unlabeled pool (e.g. for effective clustering). If a subsample is required, it will be drawn from s_Ω and therefore will not influence other systems in the experiments. For each algorithm, we decided if subsampling is required based on our available hardware, but decided against setting a fixed time limit per experiment, since this would introduce unnecessary complexity into the benchmark. An overview of selected hyperparameters per AL algorithm can be found in Appendix J.

Note: Even though we decoupled the subsystems via the described seeds, the subsystems can still influence each other in a practical sense. For example, keeping $s_\mathcal{D}$ fixed does not mean that always the same sequence of samples from \mathcal{U} (if subsamples are drawn) are shown to all acquisition functions. This is practically impossible, as different acquisition functions pick different $x^{(i)}$. However, the hypothetical **tree** of all possible sequences of samples from \mathcal{U} remains the same, granting every acquisition function equal possibilities.

I Oracle Curve Forecasting

TODO

J Hyperparameters per AL Algorithm

Table 13: Selected hyperparameters for all tested acquisition functions. Last column indicates the source of our implementation.

Algorithm	Sample Size	Other	Source
BADGE	100	Dropout Trials: 5	Based on [1, 14]
BALD	100		Based on [4]
Coreset	8000		Own
TypiClust	10000	Min Cluster Size: 5 Max # Clusters: 500	Based on [8]
Margin	8000		Own
Entropy	8000		Own

527 K Hyperparameters and Preprocessing per Dataset

528 For all our datasets we use the pre-defined train/test splits, if given. In the remaining cases, we
 529 define test sets upfront and store them into separate files to keep them fixed across all experiments.
 530 The validation set is split in the experiment run itself and depends on the dataset-seed.
 531 **Tabular:** We use **Splice**, **DNA** and **USPS** from LibSVMTools [20]. All three datasets are normal-
 532 ized between [0, 1].
 533 **Image:** We use **FashionMNIST** [25] and **Cifar10** [13], since both are widely used in AL literature.
 534 Both datasets are normalized according to their standard protocols.
 535 **Text:** We use **News Category** [18] and **TopV2** [6]. For News Category we use the 15 most com-
 536 mon categories as indicated by its Kaggle site. We additionally drop sentences above 80 words to
 537 reduce the padding needed (retaining 99,86% of the data). For TopV2, we are only using the "alarm"
 538 domain. Both datasets are encoded with pre-trained GloVe (Common Crawl 840B Tokens) embed-
 539 dings [21]. Since neither dataset provided a fixed test set, we randomly split 7000 datapoints into a
 540 test set.

Dataset	Seed Set	Budget	Val Split
Splice	1	400	0.2
SpliceEnc.	1	60	0.2
DNA	1	300	0.2
DNAEnc	1	40	0.2
USPS	1	400	0.2
USPSEnc	1	600	0.2
FashionMnist	100	2000	0.04
FashionMnistEnc	1	500	0.04
Cifar10	100	2000	0.04
Cifar10Enc	1	350	0.04
TopV2	1	125	0.25
News	1	1500	0.03

Table 14: Size of the seed set is given by number of labeled sample per class.

Dataset	Classifier	Optimizer	LR	Weight Decay	Dropout	Batch Size
Splice	[24, 12]	NAdam	1.2e-3	5.9e-5	0	43
SpliceEnc.	linear	NAdam	6.2e-4	5.9e-6	0	64
DNA	[24, 12]	NAdam	3.9e-2	3.6e-5	0	64
DNAEnc	linear	NAdam	1.6e-3	4e-4	0	64
USPS	[24, 12]	Adam	8.1e-3	1.5e-6	0	43
USPSEnc	linear	NAdam	7.8e-3	1.9e-6	0	64
FashionMnist	ResNet18	NAdam	1e-3	0	0	64
FashionMnistEnc	linear	Adam	1.6e-3	1e-5	5e-2	64
Cifar10	ResNet18	NAdam	1e-3	0	0	64
Cifar10Enc	linear	NAdam	1.7e-3	2.3e-5	0	64
TopV2	BiLSTM	NAdam	1.5e-3	1.7e-7	5e-2	64
News	BiLSTM	NAdam	1.5e-3	1.7e-7	5e-2	64

Table 15: Classifier architectures and optimized hyperparameters per dataset. Numbers in brackets signify a MLP with corresponding hidden layers.

Algorithm 1 Active Learning Loop**Require:** $\mathcal{L}, \mathcal{U}, \mathcal{D}_{\text{test}}, \text{Train}, \text{Seed}, \hat{y}$ **Require:** Ω

▷ Acquisition Function

▷ Create the initial labeled set

```

1:  $\mathcal{L}^{(1)} \leftarrow \text{Seed}(\mathcal{U})$ 
2:  $\mathcal{U}^{(1)} \leftarrow \mathcal{U}$ 
3: for  $i := 1 \dots B$  do
4:    $\text{acc}^{(i)} \leftarrow \text{Train}(\mathcal{L}^{(i)})$ 
5:    $a^{(i)} \leftarrow \Omega(\mathcal{U}^{(i)})$ 
6:    $\mathcal{L}^{(i+1)} \leftarrow \mathcal{L}^{(i)} \cup \{(\mathcal{U}_a^{(i)}, A(\mathcal{U}_a^{(i)}))\}$ 
7:    $\mathcal{U}^{(i+1)} \leftarrow \mathcal{U}^{(i)} \setminus \{\mathcal{U}_a^{(i)}\}$ 
8: return  $\frac{1}{B} \sum_{i=1}^B \text{acc}^{(i)}$ 

```

Algorithm 2 Retrain**Require:** $\mathcal{L}, \mathcal{D}_{\text{val}}, \mathcal{D}_{\text{test}}$ **Require:** \hat{y}, e_{max}

```

1:  $\text{loss}^* \leftarrow \infty$ 
2: for  $i := 1 \dots e_{\text{max}}$  do
3:    $\hat{y}_{i+1} \leftarrow \hat{y}_i - \eta \nabla_{\hat{y}} \ell(\mathcal{L}, \hat{y})$ 
4:    $\text{loss}_i \leftarrow \ell(\mathcal{D}_{\text{val}}, \hat{y})$ 
5:   if  $\text{loss}_i < \text{loss}^*$  then
6:      $\text{loss}^* \leftarrow \text{loss}_i$ 
7:   else
8:     Break
9: return  $\text{Acc}(\mathcal{D}_{\text{test}}, \hat{y})$ 

```

Algorithm 3 Acquire Oracle Ω **Require:** $\mathcal{U}, \mathcal{L}, A, \mathcal{D}_{\text{test}}, \tau, \hat{y}_{\theta}$ **Require:** $\text{Train}, \text{Margin}, \text{Acc}$

```

1:  $\text{acc}^0 \leftarrow \text{acc}^* \leftarrow \text{Acc}(\mathcal{D}_{\text{test}}, \hat{y}_{\theta})$ 
2: for  $k := 1 \dots \tau$  do
3:    $u_k = \text{unif}(\mathcal{U})$ 
4:    $\mathcal{L}' \leftarrow \mathcal{L}^{(i)} \cup \{(u_k, A(u_k))\}$ 
5:    $\hat{y}'_{\theta} \leftarrow \text{Train}(\mathcal{L}', \hat{y}_{\theta})$ 
6:    $\text{acc}' \leftarrow \text{Acc}(\mathcal{D}_{\text{test}}, \hat{y}'_{\theta})$ 
7:   if  $\text{acc}' > \text{acc}^*$  then
8:      $\text{acc}^* \leftarrow \text{acc}'$ 
9:      $u^* \leftarrow u_k$ 
10: if  $\text{acc}^0 = \text{acc}^*$  then
11:    $u^* \leftarrow \text{Margin}(\mathcal{U}, \hat{y}_{\theta})$ 
return  $u^*$ 

```

542 Alg. 3 replaces the acquisition function Ω in the AL loop (Alg. L line 5).