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# Towards Comparable Active Learning

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## Abstract

Active Learning has received significant attention in the field of machine learning. Its goal is to select the most informative samples for labeling, thereby reducing data annotation costs. However, it has been brought to attention multiple times that reported lifts from literature generalize poorly and display high variance, leading to an inconclusive landscape in Active Learning research. Based on recent insights for reliable evaluation for Active Learning, this work extends experimentation from the commonly used image domain to a wide spectrum of domains. Additionally, we provide an analysis of how many repetitions an Active Learning experiment needs in order to derive conclusive results and propose that previous benchmarks have not met the necessary number of repetitions. To the best of our knowledge, we propose the first AL benchmark that applies state-of-the-art evaluation on algorithms in 3 major domains: Tabular, Image, and Text as well as synthetic data. We report empirical results for 11 widely used algorithms on 7 real-world and 2 synthetic datasets and aggregate them into domain-specific and overall rankings of AL algorithms.

## 1 Introduction

Deep neural networks (NN) have produced state-of-the-art results on many important supervised learning tasks. Since Deep NNs usually require large amounts of labeled training data, Active Learning (AL) can be used to instead select the most informative samples out of a large pool of unlabeled data, so that only these samples need to be labeled. It has been shown that a small labeled set of this nature can be used to train well-performing models [2, 9, 15, 29].

On top of providing a principled way to label unlabeled datasets, active learning is one of the two major approaches besides semi-supervised learning to make deep learning models more data efficient by requiring only a limited set of manually labeled data. In the last decade, many different algorithms for AL have been proposed. Even though, almost every method has reported lifts over all its predecessors,<sup>1</sup> AL research faces four central difficulties: (i) The experiments are often carried out on different datasets and model architectures, hindering direct comparison, (ii) generalize poorly across different domains, (iii) the reported results can be subject to very high variance across restarts and (iv) are not always compared against important baselines like margin sampling [24]. While multiple benchmark suites have been proposed to solve (i), to the best of our knowledge, we are the first to report results on all 3 data domains of tabular, image and text. Additionally, we provide synthetic datasets to highlight principled shortcoming of existing AL algorithms. Regarding (ii) and (iii), [29] has pointed out severe inconsistencies in results of AL papers in recent years. They conducted a meta analysis of reported results of several different AL algorithms and found that all

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<sup>1</sup>Out of all considered algorithms for this paper, only BALD [7] did not claim a new SOTA performance in their result section.

Code available at: anonymous

Table 1: Comparison of our benchmark with the existing literature. Oracle curves serve as an approximation of the best possible AL algorithm. Including the encoded versions of our datasets we reach 14 datasets. "Semi" indicates whether the paper is employing any form of self- or semi-supervised learning. A "-" for repetitions means that we could not determine how often each experiment is repeated in the respective framework.

Paper	Sampling	#Data	#Alg	Img	Txt	Tab	Synth	Semi	Oracle	Repetitions
Beck et al. [2]	batch	4	7	✓	-	-	-	-	-	-
Hu et al. [9]	batch	5	13	✓	✓	-	-	-	-	3
Zhou et al. [29]	batch	3	2	✓	✓	-	-	-	✓	5
Zhan et al. [27]	sngl+batch	35	18	-	-	✓	✓	-	✓	10-100
Munjal et al. [19]	batch	2	8	✓	-	-	-	-	-	3
Li et al. [15]	batch	5	13	✓	-	-	-	✓	-	-
Rauch et al. [22]	batch	11	5	-	✓	-	-	-	-	5
Ji et al. [10]	batch	3	8	✓	-	-	-	-	-	-
Lueth et al. [17]	batch	4	5	✓	-	-	-	✓	-	3
<b>Ours</b>	sngl+batch	9(14)	11	✓	✓	✓	✓	✓	✓	50

considered algorithms only provided significant lifts in their own original papers, while following literature reported performances no better than uncertainty sampling, or in some cases no better than random sampling for the same algorithm ([29] Appendix A). These outlined issues lead to an inconclusive landscape of AL algorithms, where the vast majority of reported lifts are neither statistically significant, nor prove to be generalizable. This makes it very hard to identify the best AL algorithm, or even identifying state-of-the-art algorithms. In this work we propose an evaluation protocol that was designed to handle the high variance in the performances of AL algorithms as well as being fully controllable regardless of the combination of dataset, model and AL algorithm. We base our work largely on [10], following their guidelines for a reliable evaluation of AL algorithms, while extending the number of evaluated data domains from 1 to 5.

We focus on pool-based AL where a pool of unlabeled samples is fixed at the start of each experiment and one or more samples are chosen sequentially. In addition to the default scenario of selecting a batch of samples every iteration we incorporate the single sample case into our benchmark. Batched algorithms (and benchmarks) do not have a principled advantage over single-sample AL except for speed of computation. The problem of optimizing a portfolio of unlabeled samples in each iteration is more complicated to solve and the algorithms have systematically less information per sample to work with leading to a generally worse performance, that impacts some algorithms more than others. We propose single-sample AL as an important tool to identify the best acquisition function, rather than the best combination of acquisition function and diversity regularization.

Table 1 shows a feature comparison between our proposed benchmark and several existing benchmarks in the literature. We offer our datasets in two versions - normal and encoded. An encoded dataset was pre-encoded by a self-supervised encoder model, providing a different use case for active learning. Our synthetic and text datasets (which use word embeddings in the normal setting) are exempt from this, bringing our total dataset count to 14 across 5 domains (Tabular, Image, Text, Synthetic, Encoded).

## Contributions

- C1 Study on the reproducibility of AL experiments, providing evidence that previous works might have not repeated their experiments often enough to provide reliable results
- C2 Efficient and performant algorithm for an oracle that can be constructed greedily and does not rely on search
- C3 Two novel synthetic datasets named "Honeypot" and "Diverging Sine" that highlight two principled shortcomings AL algorithms. Firstly, a susceptibility to noisy or adverse samples and secondly, the oversampling of easy to distinguish regions of the dataset
- C4 Extending the evaluation of Active Learning algorithms to 5 data domains and revealing significant differences in algorithm performance between them

## 70 2 Problem Description

71 Given two spaces  $\mathcal{X}, \mathcal{Y}$ ,  $n = l + u$  data points with  $l \in \mathbb{N}$  labeled examples  $\mathcal{L} =$   
 72  $\{(x_1, y_1), \dots, (x_l, y_l)\}$ ,  $u \in \mathbb{N}$  unlabeled examples  $\mathcal{U} = \{x_{l+1}, \dots, x_n\}$ , a model  $\hat{y} : \mathcal{X} \rightarrow \mathcal{Y}$ ,  
 73 a budget  $\mathbb{N} \ni b \leq u$  and an annotator  $A : \mathcal{X} \rightarrow \mathcal{Y}$  that can label  $x$ . We call  $x \in \mathcal{X}$ ,  $y \in \mathcal{Y}$   
 74 predictors and labels respectively where  $(x, y)$  are drawn from an unknown distribution  $\rho$ . Find an  
 75 acquisition function  $\Omega : \mathcal{U}^{(i)}, \mathcal{L}^{(i)} \mapsto x^{(i)} \in \mathcal{U}^{(i)}$  that iteratively selects the next unlabeled point  
 76  $x^{(i)}$  for labeling

$$\begin{aligned}\mathcal{L}^{(i+1)} &\leftarrow \mathcal{L}^{(i)} \cup \{(x^{(i)}, A(x^{(i)}))\} \\ \mathcal{U}^{(i+1)} &\leftarrow \mathcal{U}^{(i)} \setminus \{x^{(i)}\}\end{aligned}$$

with  $\mathcal{U}^{(0)} = \text{seed}(\mathcal{U}, s)$  and  $\mathcal{L}^{(0)} = (\mathcal{U}_i^{(0)}, A(\mathcal{U}_i^{(0)}))$   $i \in [1, \dots, s]$ , where  $\text{seed}(\mathcal{U}, s)$  selects  $s$   
 points per class for the initial labeled set.

So that the average expected loss  $\ell : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}$  of a machine learning algorithm fitting  $\hat{y}^{(i)}$  on the  
 respective labeled set  $\mathcal{L}^{(i)}$  is minimal:

$$\min \frac{1}{B} \sum_{i=0}^B \mathbb{E}_{(x,y) \sim \rho} \ell(y, \hat{y}^{(i)})$$

## 77 3 Related Work

78 While multiple benchmark suites have been proposed for Active Learning, none of them provide  
 79 experiments for more than two domains. The authors of [2], [19], [15], [10] and [17] even focus  
 80 exclusively on the image domain. Experiments on the interplay between AL and semi-supervised  
 81 learning have only been provided by two works so far [15, 17], both of them only for images. An  
 82 oracle algorithm has so far been proposed by only two works [29, 28]. Both of these algorithms  
 83 rely on search, while our proposed method can be constructed sequentially. The two closest related  
 84 works to this benchmark are [10] and [17], who also place a much higher emphasis on the problem of  
 85 evaluating AL algorithms under many forms of variance than their predecessors (indicated in Tab. 1  
 86 by a dashed line). The authors of [10] posed a total of 12 "recommendations" for reliable evaluation  
 87 of AL algorithms. We largely adapt the proposed recommendations of [10] and extend their work  
 88 to multiple domains, batch sizes and comparisons. For a complete list of the recommendations  
 89 and our implementation of them, please refer to App. A. This work also pays attention to the  
 90 so-called "pitfalls" of AL evaluation proposed in [17]. For a complete list of the pitfalls and our  
 91 implementation of them, please refer to App. B. To the best of our knowledge, we are the first to  
 92 extend reliable SOTA (based on [10, 17]) experimentation to a total of 5 data domains.

## 93 4 Methodology

### 94 4.1 Why we need 50 restarts

95 To evaluate how many restarts are necessary to obtain conclusive results in an AL experiment, we  
 96 computed 100 runs of our top-performing algorithm on one dataset. Our best algorithm is margin  
 97 sampling and we chose the Splice dataset for its average size and complexity.

98 This allows us firstly, to obtain a very strong estimation of the "true" average performance of margin  
 99 sampling on this dataset and secondly, to draw subsets from this pool of 100 runs. Setting the size  
 100 of our draws to  $\alpha$  and sampling uniformly, we can approximate a cross-validation process with  $\alpha$   
 101 restarts. Each of these draws can be interpreted as a **reported result in AL literature** where the  
 102 authors employed  $\alpha$  restarts. Figure 1 shows the "true" mean performance of margin sampling  
 103 (green) in relation to random sampling (black) and the oracle performance (red). We display 5  
 104 random draws of size  $\alpha$  in blue. We can observe that even for a relatively high number of restarts the  
 105 variance between the samples is extremely high, resulting in some performance curves being worse

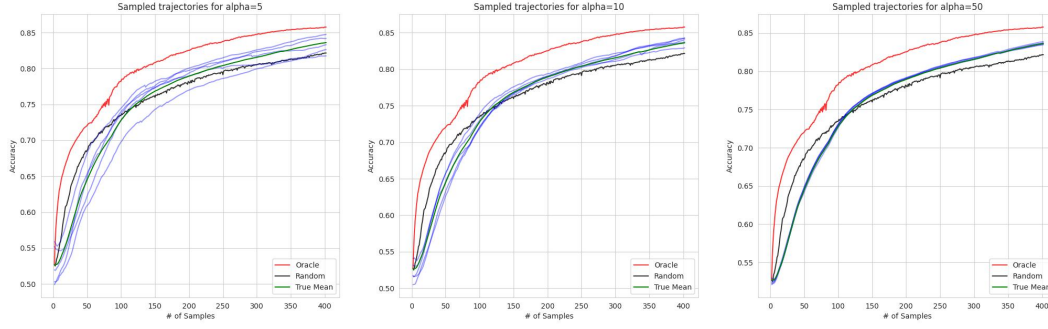


Figure 1: Random draws from a pool of 100 runs for margin sampling on the Splice dataset with different numbers of repetitions ( $\alpha = \{5, 10, 50\}$ ). Green curves are the mean performance of all 100 runs, while the samples are blue. Even with 5 or 10 repetitions, we can observe that single draws for margin sampling display below-random performance (black), while the true mean should be above random.

that random and some being significantly better. When setting  $\alpha = 50$  we observe all samples to converge close to the true mean performance. In addition to this motivating example, we carried out our main evaluation (Tab. 3) multiple times by uniformly sampling 3 random from our 50 available runs and comparing the results. We found significant differences in the performance of acquisition functions on individual datasets, as well as permutations in the final ranking. This partly explains the ongoing difficulties in reproducing results for AL experiments and benchmarks. This details can be found in App. D. For this benchmark we employ 50 restarts of every experiment.

## 4.2 Seeding vs. Restarts

Considering the high computational cost of 50 repetitions, another approach to ensure reproducibility would be to reduce the amount of variance in the experiment by keeping as many subsystems (weight initialization, data splits, etc.) as possible fixed with specialized seeding.

We describe a novel seeding strategy in Appendix H that creates 3 separate Random Number Generators (RNG) based on 3 different seeds. In short, we introduce three different seeds:  $s_\Omega$  for the AL algorithm,  $s_\mathcal{D}$  for dataset splitting and mini-batch sampling, and  $s_\theta$  for model initialization and sampling of dropout masks. Unless stated otherwise, we will keep  $s_\Omega$  fixed, while  $s_\mathcal{D}$  and  $s_\theta$  are incremented by 1 between restarts to introduce stochasticity into our framework. While this seeding strategy is capable of controlling the amount variance in the experiment, previous works have noted that an actively sampled, labeled set does not generalize well between model architectures or even different initializations of the same model ([29, 16]), reducing its value in practice and providing a bad approximation of the quality of an AL algorithm. Hence, we opt for letting the subsystems vary (by increasing  $s_\mathcal{D}$  and  $s_\theta$ ) and combine that with a high number of restarts to obtain a good average of the generalization performance of each AL algorithm.

Where a high number of restarts is computationally not feasible, we advise to additionally keep either  $s_\mathcal{D}$  or  $s_\theta$  (or both) fixed.

## 4.3 Datasets

A detailed description of the preprocessing of each dataset can be found in Appendix K.

**Tabular:** AL research conducted on tabular data is sparse (only [1] from the considered baseline papers). We, therefore, introduce a set of tabular datasets that we selected according to the following criteria: (i) They should be solvable by medium-sized models in under 1000 samples, (ii) the gap between most AL algorithms and random sampling should be significant (potential for AL is present) and (iii) the gap between the AL algorithms and our oracle should also be significant (research on

these datasets can produce further lifts). We use **Splice**, **DNA** and **USPS** from LibSVMTools [20]. **Image:** We use **FashionMNIST** [25] and **Cifar10** [13], since both are widely used in AL literature. **Text:** We use **News Category** [18] and **TopV2** [6]. Text datasets have seen less attention in AL research, but most of the papers that evaluate on text ([9], [29]) use at least one of these datasets.

We would like to point out that these datasets are selected for speed of computation (both in terms of number of features and necessary budget to solve the dataset). However, similar to our argumentation for picking smaller classifiers, we are solely focused on comparing different AL algorithms in this paper and do not aim to develop novel classification models on these datasets. Our assumption is that a well-performing algorithm in our benchmark will also generalize well to larger real-world datasets, because we included multiple different data domains and classifier sizes in our experiments.

Adapting the experimental setting from [8], we offer all our datasets in the un-encoded (normal) setting as well as pre-encoded by a fixed embedding model that was trained by unsupervised contrastive learning. The text datasets are an exception to this, as they are only offered in their encoded form. The pre-encoded datasets enable us to test single-sample algorithms on more complex datasets like Cifar10 and FashionMnist. They also serve the purpose of investigating the interplay between self-supervised learning techniques and AL, as well as alleviating the cold-start problem described in [17] as they require a way smaller seed set. The classification model for every encoded dataset is a single linear layer with softmax activation. The embedding model was trained with the SimCLR [5] algorithm adopting the protocol from [8]. To ensure that enough information from the data is encoded by our embedding model, the quality of embeddings during pretext training was measured after each epoch. We attached a linear classification head to the encoder, fine-tuned it to the data and evaluated this classifier for test accuracy, mirroring our AL setup for embedded datasets. The checkpoint of each encoder model will be provided together with the framework.

Every dataset has a fixed size for the seed set of 1 sample per class, with the only exceptions being un-encoded FashionMnist and Cifar10 with 100 examples per class to alleviate the cold-start problem in these complex domains.

#### 4.4 Batch Sizes

We selected batch sizes for each dataset to accommodate the widest range possible that results in a reasonable runtime for low batch sizes and allows for at least 4 round of data acquisition for high batch sizes. The available batch sizes per dataset can be found in Table 2.

Table 2: Employed model, chosen budget and available batch sizes for each dataset

	Model	B	1	5	20	50	100	500	1K
Enc. DNA	Linear	40	o	o					
Enc. Splice	Linear	100	o	o	o	o			
TopV2	BiLSTM	200	o	o	o	o			
Splice	MLP	400	o	o	o	o	o		
DNA	MLP	300	o	o	o	o	o		
USPS	MLP	400	o	o	o	o	o		
Enc. Cifar10	Linear	450	o	o	o	o	o		
Enc. FMnist	Linear	500	o	o	o	o	o		
Enc. USPS	Linear	600	o	o	o	o	o		
News	BiLSTM	3K			o	o	o	o	
FMnist	ResNet18	10K						o	o
Cifar10	ResNet18	10K						o	o

#### 4.5 Realism vs. Variance

We would like to point out that some design choices for this framework prohibit direct transfer of our results to practical applications. This is a conscious choice, as we think that this is a necessary trade-off between realism and experiment variance. We would like to highlight the following design decisions:

(i) Creating test and validation splits from the full dataset rather than only the labeled seed set. Fully fledged test and validation splits are unobtainable in practice, but they provide not only a better approximation of algorithm performance, but also a better foundation for hyperparameter tuning, which is bound to reduce variance in the experiment.

(ii) Choosing smaller classifiers instead of SOTA models. Since we are not interested in archiving a new SOTA in any classification problem, we instead opt to use smaller classifiers for the following reasons: Smaller classifiers generally exhibit more stable training behavior, on average require fewer sampled datapoints to reach their full-dataset-performance and have faster training times. For every

dataset, the chosen architecture’s hyperparameters are optimized to archive maximum full-dataset performance. Generally, we use MLPs for tabular, ResNet18 for image and BiLSTMs for text datasets. Every encoded dataset is classified by a single linear layer with softmax activation. The used model for each dataset can be found in Tab. 2. For a detailed description and employed hyperparameters please refer to Appendix K.

#### 4.6 Greedy Oracle Algorithm

Posing Active Learning as a combinatorial problem, the oracle set  $\mathcal{O}_b$  for a given dataset, model, and training procedure is the set that induces the highest AUC score for a given budget. However, since this problem is computationally infeasible for realistic datasets, previous works have proposed approximations to this oracle sequence. [29] used simulated annealing to search for the optimal subset and used the best solution found after a fixed time budget. Even though their reported performance curves display a significant lift over all other acquisition functions, we found the computational cost of reproducing this oracle for all our datasets to be prohibitive (The authors reported the search to take several days per dataset on 8 V100 GPUs). In this paper, we propose a greedy oracle algorithm that constructs an approximation of the optimal set in an iterative fashion. Our oracle algorithm evaluates every data point  $u_k = \text{unif}(\mathcal{U})$   $k \in [1 \dots \tau]$  in a subsample of unlabeled points by fitting the classifier  $\hat{y}$  on  $\mathcal{L}^{(i)} \cup \{u_k\}$  and directly measuring the resulting test performance. The data point with the best test performance is selected and added to the labeled pool for that iteration. We noticed that this oracle is over-specializing on the test set, resulting in stagnating or even decreasing performance curves in later AL iterations. This can happen, for example, if the oracle picked a labeled set that enables the classifier to correctly classify a big portion of easy samples in the test set, but now fails to find the next **single** unlabeled point that would enable the classifier to succeed on one of the hard samples. This leads to a situation, where no point can immediately incur an increase in test performance and therefore the selected data point can be considered random. To circumvent this problem, we use margin sampling [24] as a fallback option for the oracle. Whenever the oracle does not find an unlabeled point that results in an increase in performance, it defaults to margin sampling in that iteration. The resulting greedy algorithm constructs an approximation of the optimal labeled set that consistently outperforms all other algorithms by a significant margin, while requiring relatively low computational cost ( $\mathcal{O}(B\tau)$ ). We fix  $\tau = 20$  in this work, as this gave us already a significant lift and we expect diminishing returns for larger  $\tau$ . The pseudocode for our oracle can be found in App. L. Even though our proposed algorithm is more efficient than other approaches, the computational costs for high budget datasets like Cifar10 and FashionMnist meant that we could not compute the oracle for all 10000 datapoints. To still provide an oracle for these two datasets, we select two points per iteration instead of one and stop the oracle computation at a budget of 5000. The rest of the curve is forecast with a simple linear regression that asymptotically approaches the upper bound performance of the dataset. A detailed description can be found in App. I.

#### 4.7 Evaluation Protocol

Following [29], the quality of an AL algorithm is evaluated by an “anytime protocol” that incorporates classification performance at every iteration, as opposed to evaluating final performance after the budget is exhausted. We employ the normalized area under the accuracy curve (AUC):

$$\text{AUC}(\mathcal{D}_{\text{test}}, \hat{y}, B) := \frac{1}{B} \sum_{i=1}^B \text{Acc}(\mathcal{D}_{\text{test}}, \hat{y}^{(i)}) \quad (1)$$

The AUC incorporates performance in early stages (low budget) as well as capabilities to push the classifier in later stages (high budget). AL algorithms have to perform well in both scenarios.

Since AUC is still influenced by the budget, we define a set of rules to set this hyperparameter upfront, so that we are not favoring a subset of algorithms by handcrafting a budget. In this work, we choose the budget per dataset to be the first point at which one of 2 stopping conditions apply: (i) an algorithm (except Oracle) manages to reach 99% of the full-dataset-performance (using the smallest query size) or (ii) the best algorithm (except oracle) did not improve the classifier’s accuracy by at

least 2% in the last 20% of iterations. The first rule follows [10], while the second rule prevents excessive budgets for cases with diminishing returns in the budget. The resulting budgets can be found in Tab. 2.

As described in Sec. 4.1, we restart each experiment multiple times. Each restart retains the train/test split (often given by the dataset itself), but creates a new validation split that is sampled (based on  $s_{\mathcal{D}}$ ) from the entire dataset (not just the seed set  $\mathcal{L}^{(0)}$ ).

Apart from plotting standard performance curves and reporting their AUC values per dataset in App. G, we primarily rely on ranks to aggregate the performance of an acquisition function across datasets. For each dataset and query size, the AUC values of all acquisition functions are sorted and assigned a rank based on position, with the best rank being 1. These ranks can safely be averaged across datasets as they are no longer subjected to scaling differences of each dataset. Additionally, we employ Critical Difference (CD) diagrams (like Fig. 2) for statistical testing. CD diagrams use the Wilcoxon signed-rank test, which is a variant of the paired T-test, to find significant differences of ranks between acquisition functions. For these diagrams, each combination of dataset, query size and run is considered a separate experiment, i.e. the results of Dataset1-QuerySize1-run5 of an acquisition function  $x$  is only compared to the results of Dataset1-QuerySize1-run5 of acquisition function  $y$ . Due to the large number of restarts and the wide range of datasets and query sizes, we can provide very accurate significance tests. For a detailed description of how every CD diagram is created, please refer to App. F.

## 5 Experiments

### 5.1 Implementation Details

At each iteration  $i$  the acquisition function  $\Omega$  picks an unlabeled datapoint based on a fixed set of information  $\{\mathcal{L}^{(i)}, \mathcal{U}^{(i)}, B, |\mathcal{L}^{(i)}| - |\mathcal{L}^{(1)}|, \text{acc}^{(i)}, \text{acc}^{(1)}, \hat{y}^{(i)}, \text{opt}_{\hat{y}}\}$ , where  $\text{opt}_{\hat{y}}$  is the optimizer used to fit  $\hat{y}^{(i)}$ . This set grants full access to the labeled and unlabeled set, as well as all parameters of the classifier and the optimizer. Additionally, we provide meta-information, like the size of the seed set through  $|\mathcal{L}^{(i)}| - |\mathcal{L}^{(1)}|$ , the remaining budget though the addition of  $B$  and the classifiers potential though  $\text{acc}^{(1)}$  and  $\text{acc}^{(i)}$ . We allow acquisition functions to derive information from this set, e.g. predictions of the classifier  $\hat{y}^{(i)}(x)$ ;  $x \in \mathcal{U}^{(i)} \cup \mathcal{L}^{(i)}$ , clustering, or even training additional models. However, the algorithm may not incorporate external information e.g. other datasets, queries to recover additional labels, additional training steps for  $\hat{y}$ , or the test/validation set.

For our study we selected acquisition functions with good performances reported by multiple different sources that can work with the set of information stated above. For a list of all acquisition functions, please refer to Table 3, with detailed descriptions being found in Appendix C.

The model  $\hat{y}$  can be trained in two ways. Either the parameters of the model are reset to a fixed initial setting  $\hat{y}^{(0)}$  after each AL iteration and the classifier is trained from scratch with the updated labeled set  $\mathcal{L}^{(i)}$ , or the previous state  $\hat{y}^{(i-1)}$  is retained and the classifier is fine-tuned on  $\mathcal{L}^{(i)}$  for a reduced number of epochs. In this work, we use the fine-tuning method for un-encoded datasets to save computational time, while we use the from-scratch training for embedded datasets since they have very small classifiers and this approach generally produces better results. Our fine-tuning scheme always trains for at least one epoch and employs an aggressive early stopping with a patience of 2 afterwards.

### 5.2 Results on Real-world Data

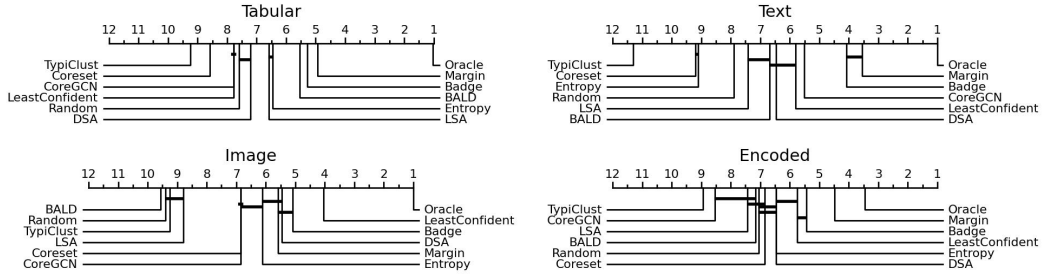
In Table 3 we provide the rank of each acquisition function per dataset and averaged for each (un-)encoded dataset. Please note, that for Tab 3 we are averaging not only over runs, but also over query sizes per dataset. For the results per query size, please refer to App. E.

As stated in contribution C4, our results on real-world data shows significant differences in the performance of the tested algorithms between data domains. Not only do some algorithms overperform on some domains (like least confidence sampling on Images), but the Top-3 of algorithms (except

Table 3: Performances for acquisition functions on real-world datasets, aggregated for un-encoded and encoded datasets. Performance is shown as average ranks over restarts (1.0 is the best rank). Algorithms are sorted by aggregated performance on un-encoded datasets.

	Splice	DNA	USPS	Cfr10	FMnist	TopV2	News	Un-enc.	Enc.
Oracle	1.0 $\pm$ 0.01	1.0 $\pm$ 0.01	1.0 $\pm$ 0.0	1.0 $\pm$ 0.0	1.0 $\pm$ 0.0	1.0 $\pm$ 0.01	1.0 $\pm$ 0.0	1.0	2.0
Margin	6.6 $\pm$ 0.02	4.3 $\pm$ 0.01	2.1 $\pm$ 0.01	6.3 $\pm$ 0.01	4.4 $\pm$ 0.0	2.4 $\pm$ 0.01	3.7 $\pm$ 0.0	4.3	4.2
Badge	5.2 $\pm$ 0.01	6.3 $\pm$ 0.01	2.9 $\pm$ 0.01	5.2 $\pm$ 0.01	4.7 $\pm$ 0.0	3.3 $\pm$ 0.01	3.5 $\pm$ 0.0	4.5	5.4
LeastConf	9.2 $\pm$ 0.02	10.3 $\pm$ 0.02	8.1 $\pm$ 0.02	2.1 $\pm$ 0.01	4.0 $\pm$ 0.0	7.9 $\pm$ 0.02	3.0 $\pm$ 0.01	6.4	6.5
DSA	7.4 $\pm$ 0.02	7.3 $\pm$ 0.01	7.5 $\pm$ 0.01	5.4 $\pm$ 0.01	5.1 $\pm$ 0.0	6.0 $\pm$ 0.02	7.3 $\pm$ 0.01	6.6	6.7
BALD	4.0 $\pm$ 0.01	4.7 $\pm$ 0.01	5.4 $\pm$ 0.01	12.0 $\pm$ 0.01	7.6 $\pm$ 0.0	7.6 $\pm$ 0.02	5.0 $\pm$ 0.0	6.6	7.6
CoreGCN	6.9 $\pm$ 0.01	4.9 $\pm$ 0.01	10.4 $\pm$ 0.01	7.6 $\pm$ 0.01	6.5 $\pm$ 0.01	4.0 $\pm$ 0.01	6.8 $\pm$ 0.0	6.7	8.2
Entropy	6.6 $\pm$ 0.02	3.9 $\pm$ 0.01	7.6 $\pm$ 0.01	7.6 $\pm$ 0.01	4.9 $\pm$ 0.01	9.8 $\pm$ 0.02	9.6 $\pm$ 0.0	7.1	6.5
LSA	6.1 $\pm$ 0.01	6.8 $\pm$ 0.01	5.3 $\pm$ 0.01	7.7 $\pm$ 0.01	10.6 $\pm$ 0.01	7.5 $\pm$ 0.01	7.3 $\pm$ 0.01	7.3	7.5
Random	9.0 $\pm$ 0.01	9.3 $\pm$ 0.01	5.3 $\pm$ 0.01	8.4 $\pm$ 0.01	11.1 $\pm$ 0.0	7.9 $\pm$ 0.01	8.0 $\pm$ 0.0	8.4	6.9
Coreset	7.1 $\pm$ 0.01	9.0 $\pm$ 0.01	10.5 $\pm$ 0.01	6.8 $\pm$ 0.01	7.1 $\pm$ 0.0	8.5 $\pm$ 0.02	10.8 $\pm$ 0.01	8.5	7.2
TypiClust	8.8 $\pm$ 0.01	10.2 $\pm$ 0.01	12.0 $\pm$ 0.02	7.9 $\pm$ 0.01	11.0 $\pm$ 0.01	12.0 $\pm$ 0.02	12.0 $\pm$ 0.01	10.5	9.2

Figure 2: Ranks of each acquisition function aggregated by domain. Horizontal bars indicate a **non**-significant rank difference. The significance is tested via a paired-t-test with  $\alpha = 0.05$ .



Oracle) does not contain the same three algorithms for any two domains. Most interestingly, the image domain, which received the most attention in benchmarking so far could even be considered an outlier, as this is the only domain where the Top-1 algorithm changes. This highlights the dire need for diverse data domains in AL benchmarking.

## 6 Synthetic Datasets for AL

AL approaches can be categorized into two types, uncertainty and geometric approaches. Typical members of the first category are variants of uncertainty sampling like entropy-, margin and least-confident-sampling [24] as well as BALD [7]. Typical members of the second category are clustering approaches like Coreset [23], BADGE [1] and TypiClust [8]. Both types of algorithms have principled shortcomings in terms of the utilized information that makes them unsuitable for certain data distributions. To test for these specific shortcomings, we created two synthetic datasets, namely "Honeypot" and "Diverging Sine", that are hard to solve for methods focused on the classifier's decision boundary or data clustering respectively. To avoid algorithms memorizing these datasets they are generated from scratch for each experiment, depending on  $s_D$ .

Honeypot creates to two easy to distinguish clusters with 150 samples each and one overlapping "honeypot" that represents a noisy region of the dataset with potentially miss-labeled, miss-measured or generally adverse samples. This honeypot contains 150 samples of each class, creating a balance of 50% beneficial samples and 50% adverse samples in the dataset. The honeypot is located on the likely decision boundary of a classifier that is trained on the beneficial samples to maximize its negative impact on purely uncertainty based acquisition functions. Diverging Sine samples the datapoints for each class from two diverging sinusoidal functions that are originating from the same y-intercept. This creates a challenging region on the left hand side, where a lot of datapoints need to be sampled and an easy region on the right hand side, where very few datapoints are enough. The repeating nature of a sin function encourages diversity based acquisition functions to equally sample the entire length, drastically oversampling the right hand side of the dataset. Each



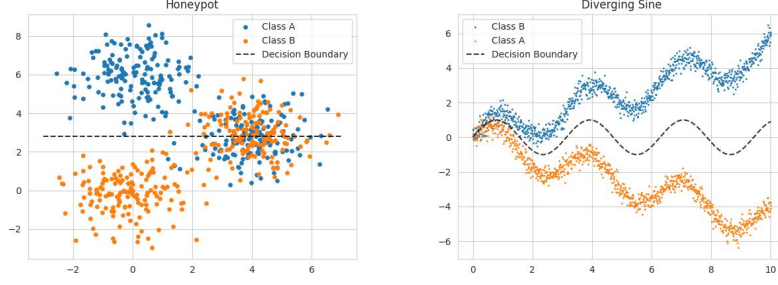
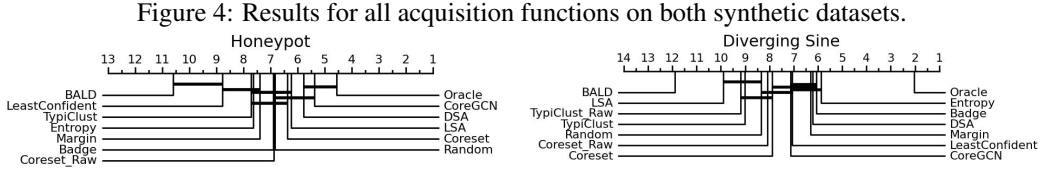


Figure 3: Synthetic "Honeyplot" and "Diverging Sine" datasets. The optimal decision boundary is not part of the dataset and serves only as a visual guide.



class has 500 datapoints. Both datasets have a budget of  $B = 60$  and are tested with query sizes 1 and 5.

Results for the Honeyplot dataset reveal expected shortcomings of uncertainty sampling algorithms like margin, entropy and least confident sampling as well as BALD. In addition, BADGE is underperforming for this dataset compared to real-world data. Results for Diverging Sine also confirm expected behavior, as clustering algorithms (Coreset, TypiClust) fall behind uncertainty algorithms (Entropy-, Margin-Sampling), with the exception of BADGE.

We provide a very small ablation study on the importance of the embeddings by testing a version of Coreset and TypiClust on this dataset that does not use the embeddings produced by the classification model, but rather clusters the data directly. "Coreset Raw" and "TypiClust Raw" both perform worse than their embedding-based counterpart.

## 6.1 Results on Synthetic Data

Our results on Honeyplot reveal principled shortcomings for the two best algorithms in BADGE and margin sampling. Both are vulnerable to adverse samples or simply measurement noise, which highlights the need for further research in this area.

Finally, the fact that BADGE is able to perform well on Diverging Sine highlights the importance of embeddings for the clustering algorithms, as the so-called gradient embedding from BADGE seems to be able to encode uncertainty information, guiding the selection into the left hand regions of the dataset. We also show that embeddings are generally useful for this dataset, by providing results for "Coreset Raw" and "TypiClust Raw".

## 7 Conclusion

We strongly advocate to test newly proposed AL algorithms not only on a wide variety of real data domains, but also to pay close attention to the Honeyplot and Diverging Sine datasets to reveal principled shortcomings of the algorithm in question. Both tasks can be easily carried out by implementing the new acquisition function into our code base.

333 **Acknowledgement** anonymous

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408 **A AL Recommendations from Ji et al.**

409 TODO

410 **B AL Pitfalls from Lueth et al.**

411 TODO

412 **C Acquisition Functions**

413 **Uncertainty Sampling** tries to find the sample that the classifier is most uncertain about by  
414 computing heuristics of the class probabilities. For our benchmark, we use entropy and margin  
415 (a.k.a. best-vs-second-best) sampling.

416 **BALD** [12] applies the query-by-committee strategy of model ensembles to a single model by  
417 interpreting the classifier’s parameters as distributions and then sample multiple outputs from them  
418 via Monte-Carlo dropout.

419 **BADGE** [1] uses gradient embeddings of unlabeled points to select samples where the classifier  
420 is expected to change a lot. The higher the magnitude of the gradient the higher the expected  
421 improvement in model performance.

422 **Coreset** [23] employs K-Means clustering trying to cover the whole data distribution. Selects  
423 the unlabeled sample that is the furthest away from all cluster centers. Clustering is done in a  
424 semantically meaningful space by encoding the data with the current classifier  $\hat{y}$ . In this work, we  
425 use the greedy variant of Coreset.

426 **TypiClust** [8] relies on clustering similar to Coreset, but proposes a new measure called “Typical-  
427 ity” to select unlabeled samples. It selects points that are in the densest regions of clusters that do  
428 not contain labeled samples yet. Clustering is done in a semantically meaningful space by encoding  
429 the data with the current classifier  $\hat{y}$ . It has to be pointed out that TypiClust was designed for  
430 low-budget scenarios, but we think it is still worthwhile to test and compare this algorithm with  
431 higher budgets.

432 **Core-GCN** [3] TODO

433 **DSA/LSA** [11] TODO

434 **Excluded Algorithms**

435 **Learning Loss for AL** [26] Introduces an updated training of the classification model with an  
436 auxiliary loss and therefore cannot be compared fairly against classification models without this  
437 boosted training regime.

438 **Reinforcement Learning Algorithms**

439

440 **D Difference of Ranks with 3 Repetitions**

441 Table 4 and Table 5 follow the exact same computation of ranks that created the main result (Table  
442 3) with the only difference being a reduced number of runs per acquisition function. For each table  
443 we uniformly sampled 3 runs from the available 50 per acquisition function.

444 We can observe significant differences between the two tables:

445 **Purple:** A multitude of rank differences of acquisition functions for specific datasets, some as high  
446 as 4.7 ranks for TypiClust on the Splice dataset

447 **Olive:** Well separated acquisition functions in Tab. 5 (Margin and BADGE) are almost indistin-  
448 guishable in Tab 4

449 **Red:** BALD lost 2 places in the overall ranking and Entropy gained 2

450 Even though the overall ordering of acquisition functions stayed relatively unchanged due to the  
451 averaging across many datasets, each individual dataset was subject to drastic permutations. This  
452 highlights the need for many repetitions in AL experiments.

Table 4: Ranks of all acquisition functions per dataset. First random draw of 3 runs from the overall pool of 50.

	Splice	DNA	USPS	Cifar10	FMnist	TopV2	News	Unencoded	Encoded
Oracle	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	2.1
Margin	6.0	7.3	2.0	6.7	5.3	2.3	3.3	4.7	4.4
Badge	6.0	7.3	3.0	6.7	5.0	3.3	4.0	5.0	5.3
BALD	3.3	4.7	5.3	12.0	7.0	6.3	4.3	6.1	7.9
CoreGCN	8.7	3.7	10.7	6.3	5.3	4.0	7.7	6.6	9.1
DSA	8.3	6.3	7.7	7.7	4.3	6.7	6.7	6.8	6.1
LeastConf	10.0	12.0	8.0	3.0	4.3	9.3	2.3	7.0	6.7
LSA	5.7	6.7	5.3	6.7	10.7	7.7	7.0	7.1	6.3
Entropy	11.0	3.3	7.3	4.0	6.7	8.3	9.7	7.2	7.0
Random	7.7	8.7	5.3	8.0	11.0	8.0	9.0	8.2	6.3
Coreset	4.7	10.3	10.3	7.7	6.0	9.0	11.0	8.4	7.2
TypiClust	5.7	6.7	12.0	8.3	11.3	12.0	12.0	9.7	9.7

Table 5: Ranks of all acquisition functions per dataset. Second random draw of 3 runs from the overall pool of 50.

	Splice	DNA	USPS	Cifar10	FMnist	TopV2	News	Unencoded	Encoded
Oracle	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	2.4
Margin	6.0	3.3	2.0	5.7	2.0	2.0	4.3	3.6	3.8
Badge	6.0	9.0	3.0	3.0	5.7	3.7	3.3	4.8	4.9
CoreGCN	4.3	6.3	10.3	7.3	5.3	5.7	5.3	6.4	8.1
DSA	8.7	7.3	7.3	6.0	4.3	5.3	6.0	6.4	6.5
BALD	4.7	4.0	4.7	12.0	7.3	6.7	6.7	6.6	7.5
Entropy	6.7	4.7	7.7	5.3	5.0	7.3	9.3	6.6	6.8
LeastConf	7.7	10.0	8.3	3.3	6.0	8.7	3.0	6.7	7.3
LSA	7.7	5.3	6.0	9.0	11.0	9.0	7.3	7.9	7.5
Random	9.3	8.0	5.0	8.7	11.7	8.3	8.7	8.5	7.6
Coreset	6.0	10.7	10.7	8.0	8.3	8.3	11.0	9.0	6.3
TypiClust	10.0	8.3	12.0	8.7	10.3	12.0	12.0	10.5	9.4

## 453 E AUCs by Query Size

Table 6: AUC values for each dataset that supports query size 1.

	Splice	SpliceEncoded	DNA	DNAEncoded	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	DivergingSin	ThreeClust
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.721+-0.013	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.957+-0.009	0.783+-0.03
Margin	0.769+-0.021	<b>0.678+-0.032</b>	0.806+-0.013	0.642+-0.047	<b>0.858+-0.006</b>	0.426+-0.038	0.653+-0.013	0.68+-0.012	<b>0.861+-0.009</b>	0.941+-0.018	0.704+-0.074
Badge	0.767+-0.02	0.661+-0.026	0.78+-0.014	0.642+-0.046	0.83+-0.008	0.371+-0.035	0.656+-0.013	0.68+-0.009	0.826+-0.024	0.941+-0.017	0.69+-0.083
LeastConfident	0.779+-0.019	0.68+-0.032	0.809+-0.01	0.629+-0.05	0.846+-0.009	0.421+-0.039	<b>0.668+-0.014</b>	<b>0.685+-0.009</b>	0.843+-0.013	0.94+-0.016	0.692+-0.094
DSA	0.766+-0.021	0.691+-0.022	0.803+-0.01	<b>0.646+-0.032</b>	0.829+-0.01	<b>0.431+-0.05</b>	0.663+-0.014	0.679+-0.01	0.844+-0.017	0.941+-0.014	<b>0.731+-0.032</b>
BALD	<b>0.78+-0.014</b>	0.649+-0.04	0.784+-0.01	0.632+-0.042	0.819+-0.01	0.242+-0.046	0.666+-0.014	0.644+-0.018	0.815+-0.024	0.928+-0.014	0.698+-0.043
CoreGCN	0.765+-0.021	0.686+-0.023	0.804+-0.012	<b>0.646+-0.03</b>	0.753+-0.016	0.39+-0.044	0.623+-0.018	0.647+-0.012	0.85+-0.01	0.938+-0.014	<b>0.731+-0.028</b>
Entropy	0.768+-0.022	<b>0.678+-0.035</b>	<b>0.812+-0.013</b>	0.635+-0.045	0.83+-0.011	0.399+-0.035	0.663+-0.013	0.681+-0.011	0.815+-0.021	<b>0.942+-0.017</b>	0.696+-0.083
LSA	0.772+-0.016	0.68+-0.026	0.787+-0.012	0.618+-0.036	0.821+-0.009	0.422+-0.037	0.613+-0.014	0.642+-0.012	0.816+-0.013	0.932+-0.016	0.727+-0.033
Random	0.76+-0.016	0.674+-0.027	0.774+-0.013	0.63+-0.035	0.823+-0.009	0.404+-0.036	0.613+-0.014	0.639+-0.013	0.815+-0.012	0.933+-0.017	0.721+-0.036
Coreset	0.772+-0.016	0.69+-0.017	0.79+-0.012	0.638+-0.041	0.767+-0.016	0.404+-0.046	0.659+-0.011	0.684+-0.009	0.826+-0.022	0.937+-0.014	0.734+-0.031
TypiClust	0.762+-0.016	0.685+-0.025	0.778+-0.01	0.663+-0.028	0.828+-0.007	0.396+-0.046	0.653+-0.013	0.649+-0.007	0.831+-0.011	0.934+-0.018	0.727+-0.033

Table 7: AUC values for each dataset that supports query size 5.

	Splice	SpliceEncoded	DNA	DNAEncoded	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEncoded	TopV2	DivergingSin	ThreeClust
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.721+-0.013	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.957+-0.009	0.783+-0.03
Margin	0.765+-0.021	0.662+-0.032	0.794+-0.011	0.611+-0.05	0.855+-0.006	0.508+-0.02	0.656+-0.014	0.678+-0.009	0.848+-0.013	0.923+-0.019	0.697+-0.055
Badge	0.768+-0.014	0.646+-0.035	0.785+-0.011	0.624+-0.036	0.846+-0.007	0.48+-0.021	0.647+-0.012	0.674+-0.009	0.847+-0.01	0.924+-0.019	0.72+-0.036
LeastConfident	0.763+-0.023	0.643+-0.034	0.798+-0.013	0.585+-0.065	0.831+-0.014	0.478+-0.028	0.67+-0.01	0.681+-0.009	0.819+-0.023	0.921+-0.019	0.675+-0.072
DSA	0.765+-0.023	0.653+-0.029	0.793+-0.009	0.613+-0.034	0.822+-0.01	0.489+-0.024	0.661+-0.013	0.662+-0.012	0.833+-0.02	0.924+-0.018	0.718+-0.034
BALD	0.775+-0.018	0.641+-0.034	0.801+-0.013	0.592+-0.054	0.84+-0.008	0.332+-0.054	0.681+-0.011	0.681+-0.011	0.824+-0.023	0.893+-0.035	0.673+-0.041
CoreGCN	0.759+-0.018	0.662+-0.027	0.79+-0.011	0.62+-0.03	0.755+-0.011	0.45+-0.03	0.604+-0.016	0.609+-0.013	0.837+-0.014	0.922+-0.018	0.723+-0.034
Entropy	0.765+-0.022	0.66+-0.03	0.798+-0.011	0.611+-0.054	0.823+-0.013	0.464+-0.024	0.663+-0.013	0.672+-0.011	0.801+-0.025	0.924+-0.02	0.689+-0.066
LSA	0.769+-0.016	0.654+-0.032	0.781+-0.013	0.61+-0.041	0.82+-0.009	0.484+-0.022	0.617+-0.012	0.641+-0.011	0.816+-0.012	0.915+-0.018	0.718+-0.038
Random	0.758+-0.015	0.655+-0.026	0.771+-0.013	0.623+-0.031	0.82+-0.009	0.476+-0.024	0.616+-0.016	0.637+-0.012	0.812+-0.014	0.921+-0.018	0.713+-0.034
Coreset	0.765+-0.017	0.663+-0.023	0.784+-0.014	0.603+-0.034	0.765+-0.015	0.449+-0.022	0.657+-0.009	0.674+-0.009	0.817+-0.017	0.92+-0.017	0.713+-0.035
TypiClust	0.759+-0.014	0.641+-0.028	0.775+-0.01	0.603+-0.04	0.757+-0.02	0.465+-0.027	0.596+-0.014	0.567+-0.012	0.727+-0.026	0.916+-0.02	0.693+-0.045

Table 8: AUC values for each dataset that supports query size 20.

	Splice	SpliceEncoded	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	News
Oracle	0.803+-0.012	0.678+-0.021	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.49+-0.003
Margin	0.759+-0.027	0.618+-0.04	0.779+-0.013	0.847+-0.008	0.439+-0.027	0.656+-0.01	0.67+-0.011	0.823+-0.014	0.464+-0.007
Badge	0.767+-0.013	0.619+-0.033	0.776+-0.013	0.845+-0.006	0.44+-0.019	0.647+-0.013	0.665+-0.007	0.827+-0.016	0.463+-0.007
LeastConfident	0.751+-0.02	0.597+-0.05	0.748+-0.025	0.798+-0.027	0.391+-0.024	0.665+-0.013	0.669+-0.011	0.775+-0.035	0.467+-0.008
DSA	0.759+-0.02	0.599+-0.034	0.769+-0.013	0.809+-0.012	0.421+-0.023	0.647+-0.014	0.63+-0.013	0.793+-0.026	0.459+-0.01
BALD	0.768+-0.022	0.57+-0.037	0.784+-0.015	0.822+-0.009	0.298+-0.039	0.675+-0.008	0.673+-0.01	0.789+-0.024	0.468+-0.009
CoreGCN	0.759+-0.018	0.612+-0.039	0.774+-0.012	0.754+-0.016	0.397+-0.026	0.587+-0.015	0.583+-0.015	0.807+-0.018	0.453+-0.006
Entropy	0.759+-0.027	0.618+-0.038	0.773+-0.015	0.803+-0.019	0.372+-0.022	0.656+-0.011	0.65+-0.012	0.773+-0.031	0.451+-0.007
LSA	0.761+-0.014	0.611+-0.039	0.768+-0.015	0.816+-0.009	0.411+-0.022	0.621+-0.01	0.635+-0.011	0.796+-0.016	0.452+-0.007
Random	0.755+-0.014	0.612+-0.039	0.763+-0.012	0.818+-0.009	0.439+-0.019	0.622+-0.013	0.633+-0.012	0.795+-0.016	0.45+-0.006
Coreset	0.759+-0.016	0.601+-0.034	0.764+-0.015	0.757+-0.015	0.39+-0.029	0.647+-0.009	0.651+-0.011	0.784+-0.026	0.435+-0.012
TypiClust	0.751+-0.012	0.551+-0.036	0.76+-0.016	0.643+-0.026	0.411+-0.024	0.488+-0.02	0.449+-0.017	0.652+-0.035	0.406+-0.011

Table 9: AUC values for each dataset that supports query size 50.

	Splice	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	TopV2	News
Oracle	0.803+-0.012	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.884+-0.006	0.49+-0.003
Margin	0.747+-0.023	0.751+-0.019	0.828+-0.009	0.363+-0.031	0.64+-0.013	0.653+-0.01	0.774+-0.029	0.46+-0.006
Badge	0.758+-0.017	0.754+-0.018	0.831+-0.008	0.376+-0.028	0.632+-0.013	0.649+-0.011	0.781+-0.026	0.462+-0.007
LeastConfident	0.731+-0.025	0.688+-0.041	0.761+-0.037	0.291+-0.03	0.644+-0.013	0.65+-0.011	0.73+-0.049	0.462+-0.009
DSA	0.748+-0.021	0.738+-0.018	0.783+-0.016	0.346+-0.027	0.624+-0.014	0.588+-0.016	0.748+-0.041	0.45+-0.011
BALD	0.76+-0.017	0.756+-0.018	0.796+-0.016	0.241+-0.026	0.65+-0.009	0.645+-0.01	0.746+-0.038	0.455+-0.007
CoreGCN	0.755+-0.016	0.745+-0.018	0.752+-0.019	0.328+-0.027	0.581+-0.015	0.568+-0.018	0.771+-0.025	0.453+-0.007
Entropy	0.747+-0.024	0.748+-0.018	0.778+-0.024	0.275+-0.026	0.633+-0.011	0.625+-0.012	0.734+-0.036	0.442+-0.007
LSA	0.754+-0.013	0.749+-0.019	0.807+-0.01	0.341+-0.029	0.613+-0.012	0.625+-0.01	0.763+-0.025	0.45+-0.006
Random	0.746+-0.012	0.745+-0.015	0.806+-0.008	0.379+-0.028	0.615+-0.014	0.621+-0.01	0.759+-0.026	0.448+-0.006
Coreset	0.751+-0.016	0.733+-0.019	0.74+-0.017	0.325+-0.034	0.624+-0.012	0.608+-0.013	0.731+-0.045	0.432+-0.012
TypiClust	0.749+-0.016	0.736+-0.016	0.586+-0.038	0.348+-0.027	0.451+-0.024	0.375+-0.022	0.614+-0.046	0.397+-0.012

Table 10: AUC values for each dataset that supports query size 100.

	Splice	DNA	USPS	USPSEncoded	Cifar10Encoded	FashionMnistEnc	News
Oracle	0.803+-0.012	0.825+-0.009	0.866+-0.004	0.436+-0.057	0.749+-0.009	0.755+-0.005	0.49+-0.003
Margin	0.733+-0.024	0.711+-0.027	0.799+-0.013	0.473+-0.026	0.629+-0.012	0.628+-0.009	0.455+-0.006
Badge	0.743+-0.014	0.714+-0.032	0.804+-0.013	0.472+-0.029	0.623+-0.01	0.621+-0.01	0.456+-0.006
LeastConfident	0.715+-0.033	0.639+-0.05	0.708+-0.034	0.23+-0.034	0.631+-0.013	0.62+-0.012	0.457+-0.008
DSA	0.729+-0.021	0.697+-0.031	0.753+-0.021	0.427+-0.028	0.609+-0.013	0.546+-0.017	0.442+-0.01
BALD	0.744+-0.015	0.718+-0.024	0.765+-0.021	0.285+-0.046	0.632+-0.009	0.609+-0.01	0.444+-0.007
CoreGCN	0.742+-0.015	0.713+-0.025	0.744+-0.019	0.433+-0.032	0.583+-0.013	0.554+-0.015	0.448+-0.007
Entropy	0.733+-0.023	0.713+-0.031	0.743+-0.026	0.395+-0.037	0.618+-0.012	0.59+-0.012	0.432+-0.007
LSA	0.738+-0.017	0.716+-0.027	0.789+-0.011	0.439+-0.03	0.609+-0.013	0.608+-0.01	0.447+-0.006
Random	0.733+-0.013	0.713+-0.023	0.789+-0.012	0.468+-0.024	0.611+-0.01	0.606+-0.01	0.446+-0.005
Coreset	0.735+-0.019	0.698+-0.026	0.721+-0.021	0.396+-0.024	0.608+-0.012	0.562+-0.016	0.426+-0.012
TypiClust	0.733+-0.016	0.704+-0.025	0.592+-0.042	0.427+-0.027	0.501+-0.02	0.338+-0.02	0.383+-0.012

Table 11: AUC values for each dataset that supports query size 500.

	Cifar10	FashionMnist
Oracle	0.689+-0.001	0.905+-0.001
Margin	0.556+-0.008	0.882+-0.004
Badge	0.56+-0.008	0.883+-0.005
LeastConfident	0.591+-0.01	0.884+-0.005
DSA	0.56+-0.009	0.882+-0.004
BALD	0.478+-0.014	0.878+-0.003
CoreGCN	0.553+-0.01	0.88+-0.007
Entropy	0.553+-0.009	0.882+-0.006
LSA	0.558+-0.01	0.866+-0.005
Random	0.557+-0.01	0.863+-0.005
Coreset	0.553+-0.007	0.878+-0.006
TypiClust	0.557+-0.009	0.864+-0.004

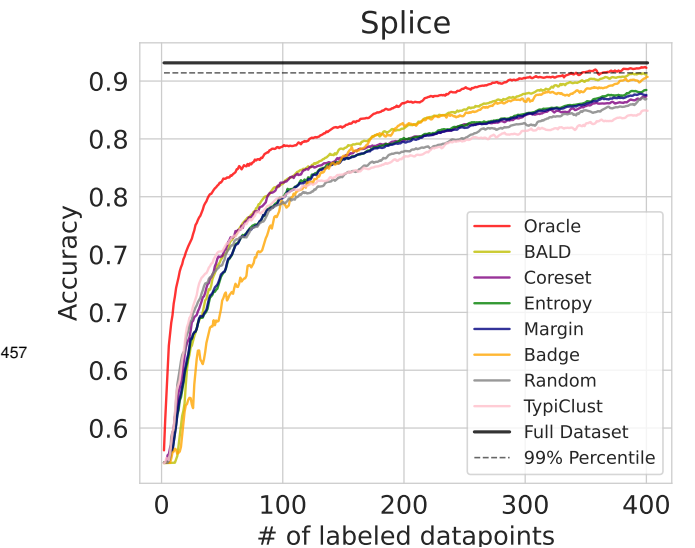
Table 12: AUC values for each dataset that supports query size 1000.

	Cifar10	FashionMnist
Oracle	0.689+-0.001	0.905+-0.001
Margin	0.56+-0.011	0.872+-0.007
Badge	0.562+-0.013	0.871+-0.007
LeastConfident	0.561+-0.012	0.873+-0.006
DSA	0.56+-0.011	0.87+-0.008
BALD	0.535+-0.011	0.866+-0.003
CoreGCN	0.557+-0.011	0.867+-0.012
Entropy	0.557+-0.014	0.871+-0.009
LSA	0.551+-0.012	0.854+-0.009
Random	0.55+-0.01	0.855+-0.006
Coreset	0.562+-0.012	0.869+-0.004
TypiClust	0.552+-0.011	0.854+-0.009

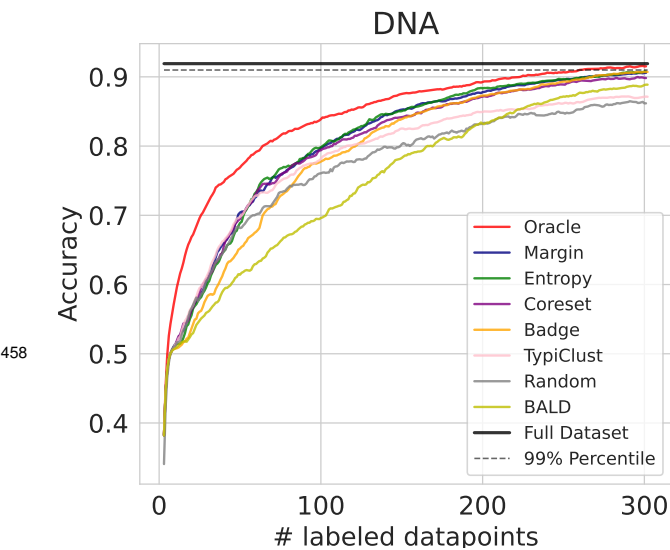
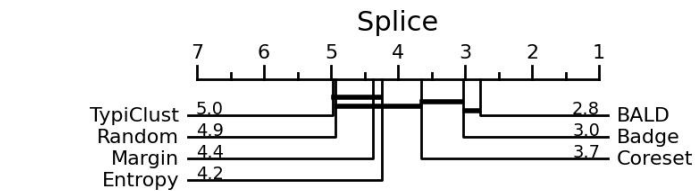


455 **F Critical Difference Diagrams**

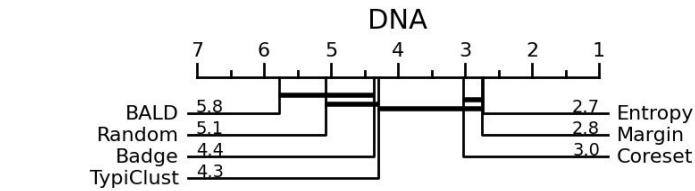
456 **G Individual Results**



	Splice
Oracle	$0.811 \pm 0.010$
BALD	$0.785 \pm 0.013$
Coreset	$0.778 \pm 0.014$
Entropy	$0.774 \pm 0.016$
Margin	$0.773 \pm 0.016$
Badge	$0.770 \pm 0.016$
Random	$0.768 \pm 0.014$
TypiClust	$0.766 \pm 0.014$

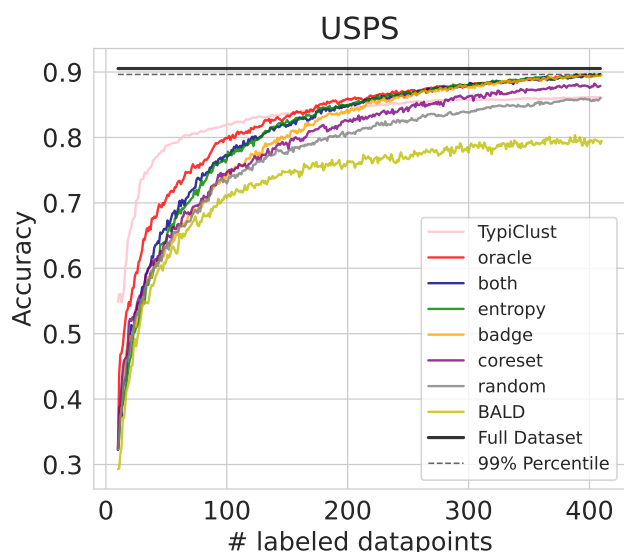


	DNA
Oracle	$0.842 \pm 0.021$
Margin	$0.807 \pm 0.035$
Entropy	$0.805 \pm 0.038$
Coreset	$0.796 \pm 0.028$
Badge	$0.789 \pm 0.056$
TypiClust	$0.788 \pm 0.036$
Random	$0.768 \pm 0.024$
BALD	$0.749 \pm 0.044$

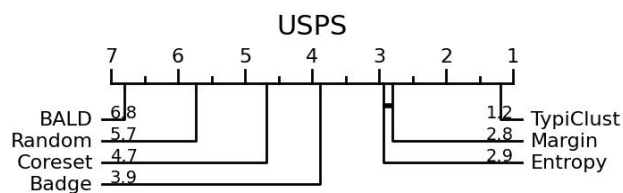




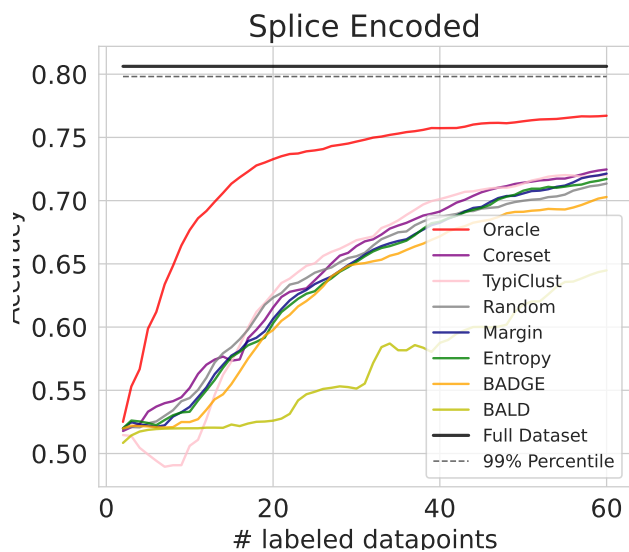
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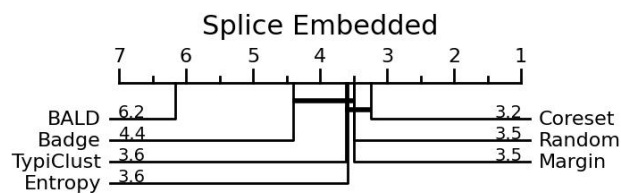
	USPS
TypiClust	$0.830 \pm 0.007$
Oracle	$0.823 \pm 0.011$
Margin	$0.809 \pm 0.013$
Entropy	$0.807 \pm 0.013$
Badge	$0.795 \pm 0.018$
Coreset	$0.788 \pm 0.017$
Random	$0.774 \pm 0.012$
BALD	$0.725 \pm 0.050$



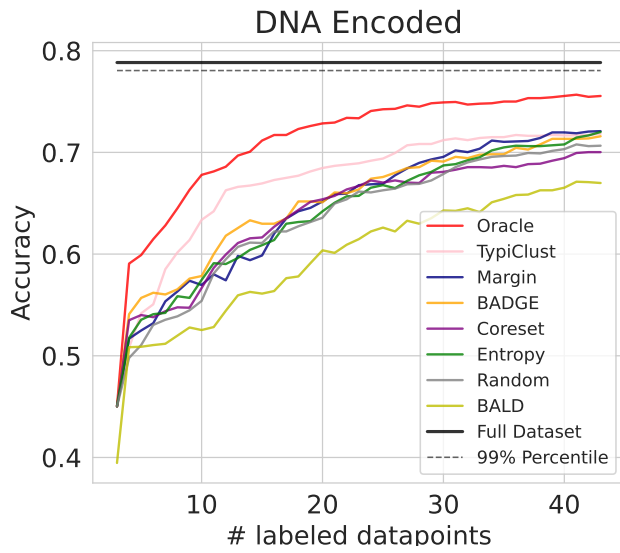
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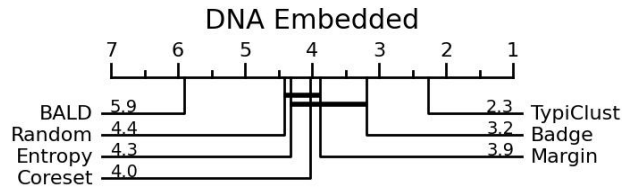
	SpliceEncoded
Oracle	$0.728 \pm 0.022$
Coreset	$0.648 \pm 0.027$
TypiClust	$0.645 \pm 0.042$
Random	$0.643 \pm 0.036$
Entropy	$0.636 \pm 0.033$
Margin	$0.636 \pm 0.033$
Badge	$0.627 \pm 0.040$
BALD	$0.565 \pm 0.049$



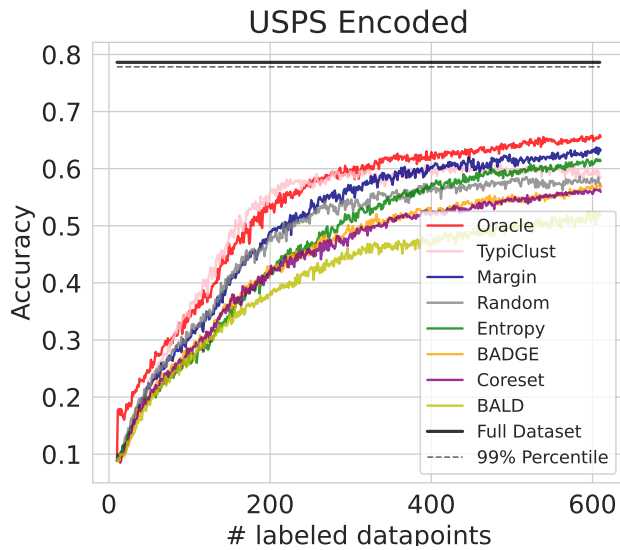
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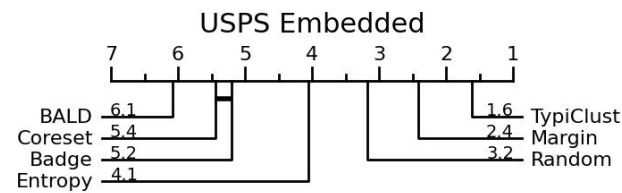
	DNAEncoded
Oracle	$0.709 \pm 0.023$
TypiClust	$0.672 \pm 0.029$
Margin	$0.648 \pm 0.047$
Badge	$0.647 \pm 0.037$
Coreset	$0.640 \pm 0.041$
Entropy	$0.629 \pm 0.062$
Random	$0.626 \pm 0.035$
BALD	$0.594 \pm 0.039$

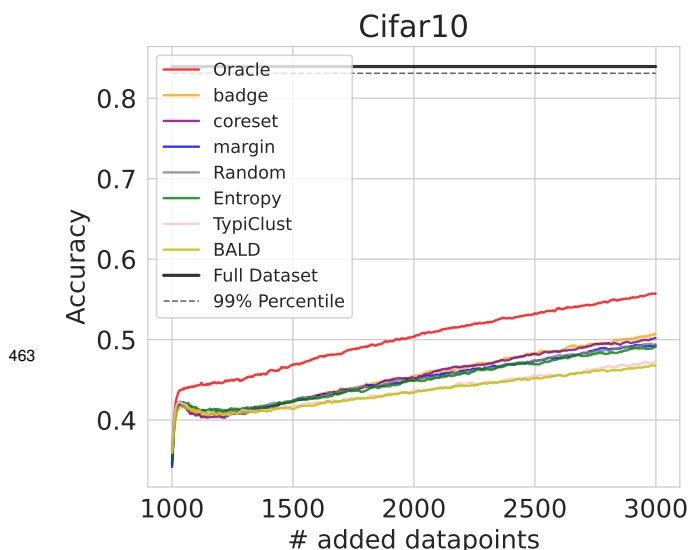


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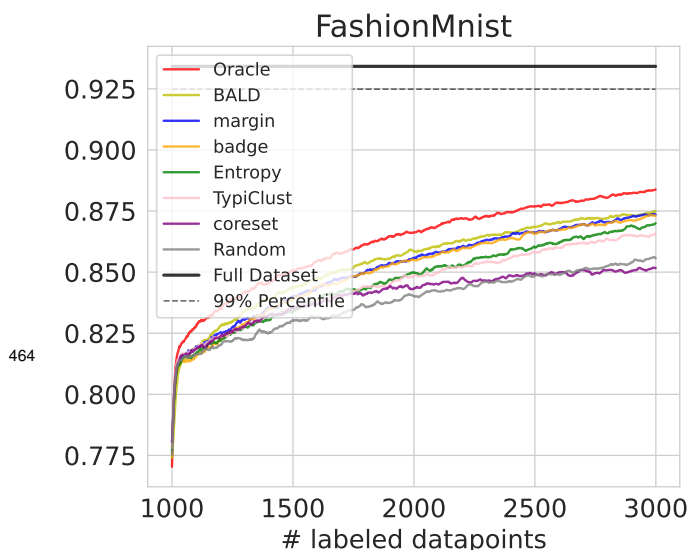
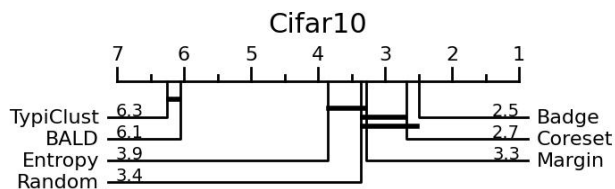


	USPSEncoded
Oracle	$0.522 \pm 0.021$
TypiClust	$0.507 \pm 0.025$
Margin	$0.496 \pm 0.030$
Random	$0.468 \pm 0.025$
Entropy	$0.459 \pm 0.021$
Badge	$0.440 \pm 0.026$
Coreset	$0.435 \pm 0.027$
BALD	$0.402 \pm 0.052$

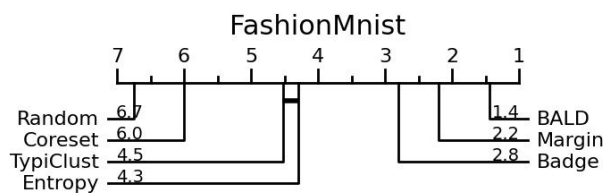


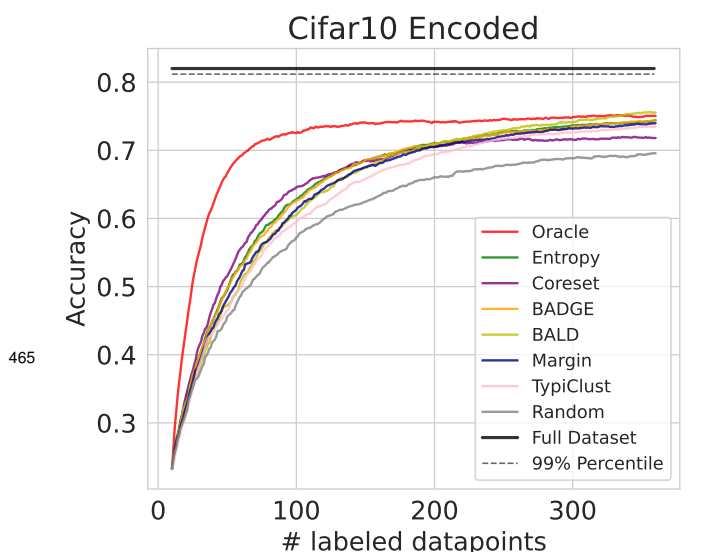


	Cifar10
Oracle	$0.500 \pm 0.010$
Badge	$0.453 \pm 0.012$
Coreset	$0.453 \pm 0.009$
Margin	$0.451 \pm 0.010$
Random	$0.450 \pm 0.012$
Entropy	$0.449 \pm 0.010$
TypiClust	$0.436 \pm 0.010$
BALD	$0.436 \pm 0.010$

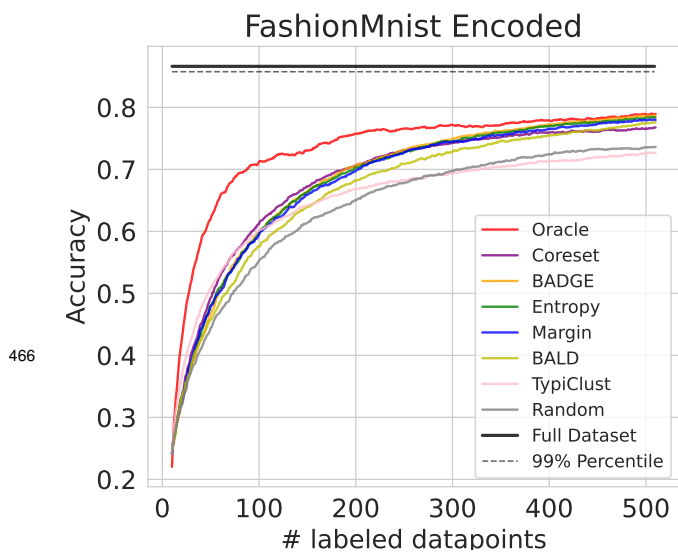
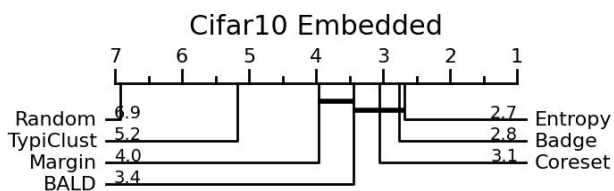


	FashionMnist
Oracle	$0.862 \pm 0.003$
BALD	$0.854 \pm 0.003$
Margin	$0.851 \pm 0.003$
Badge	$0.851 \pm 0.003$
Entropy	$0.847 \pm 0.004$
TypiClust	$0.846 \pm 0.004$
Coreset	$0.840 \pm 0.004$
Random	$0.837 \pm 0.004$

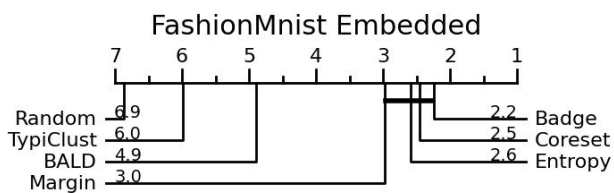


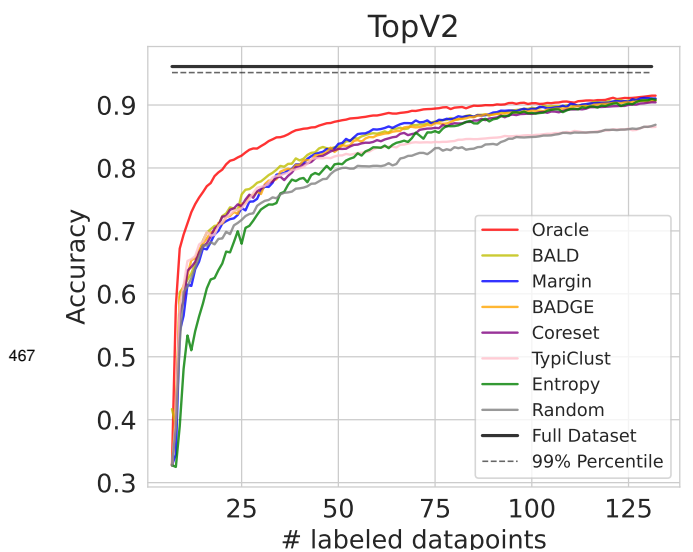


	Cifar10Encoded
Oracle	$0.714 \pm 0.007$
Entropy	$0.654 \pm 0.013$
Coreset	$0.653 \pm 0.012$
Badge	$0.653 \pm 0.012$
BALD	$0.650 \pm 0.016$
Margin	$0.647 \pm 0.012$
TypiClust	$0.636 \pm 0.009$
Random	$0.607 \pm 0.013$

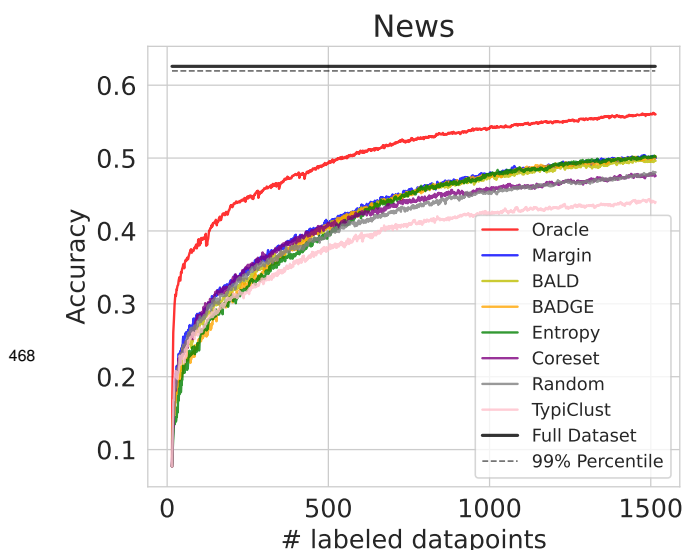
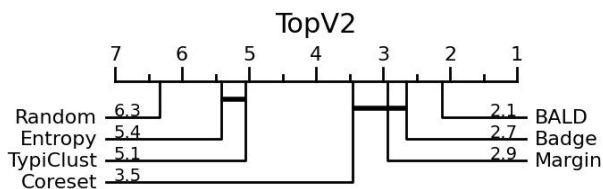


	FashionMnistEncoded
Oracle	$0.732 \pm 0.006$
Coreset	$0.686 \pm 0.008$
Badge	$0.685 \pm 0.008$
Entropy	$0.684 \pm 0.009$
Margin	$0.682 \pm 0.011$
BALD	$0.668 \pm 0.009$
TypiClust	$0.652 \pm 0.009$
Random	$0.640 \pm 0.011$

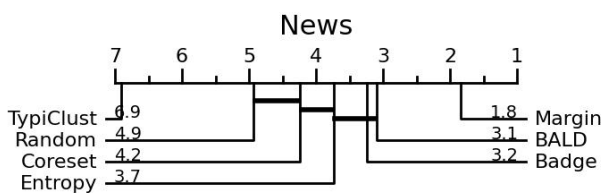


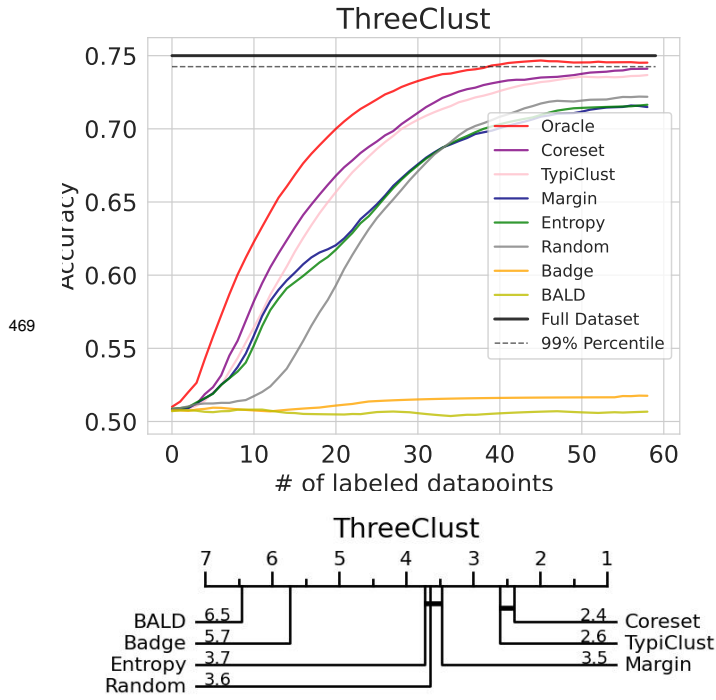


	TopV2
Oracle	$0.862 \pm 0.006$
BALD	$0.831 \pm 0.013$
Badge	$0.826 \pm 0.015$
Coreset	$0.823 \pm 0.016$
Margin	$0.822 \pm 0.015$
TypiClust	$0.805 \pm 0.015$
Entropy	$0.801 \pm 0.025$
Random	$0.787 \pm 0.015$

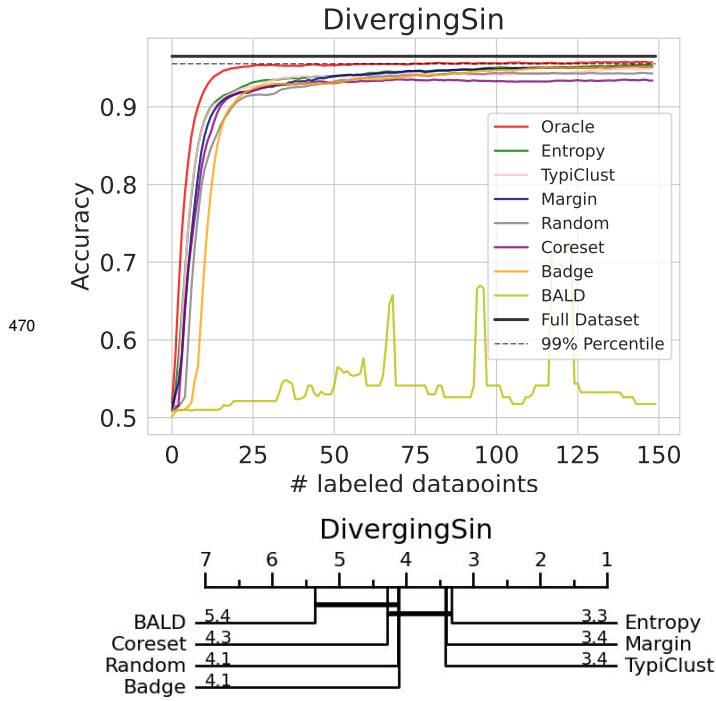


	News
Oracle	$0.502 \pm 0.005$
Margin	$0.427 \pm 0.007$
BALD	$0.421 \pm 0.008$
Badge	$0.420 \pm 0.011$
Entropy	$0.416 \pm 0.010$
Coreset	$0.415 \pm 0.011$
Random	$0.409 \pm 0.008$
TypiClust	$0.385 \pm 0.010$





	ThreeClust
Oracle	$0.722 \pm 0.097$
Coreset	$0.698 \pm 0.058$
TypiClust	$0.697 \pm 0.055$
Entropy	$0.682 \pm 0.098$
Random	$0.672 \pm 0.067$
Margin	$0.669 \pm 0.095$
Badge	$0.524 \pm 0.086$
BALD	$0.507 \pm 0.050$



	DivergingSin
Oracle	$0.948 \pm 0.198$
Entropy	$0.936 \pm 0.202$
TypiClust	$0.930 \pm 0.196$
Margin	$0.929 \pm 0.201$
Random	$0.919 \pm 0.191$
Badge	$0.914 \pm 0.202$
Coreset	$0.914 \pm 0.197$
BALD	$0.661 \pm 0.167$

## 471 H Seeding Strategy

472 We aim to provide an experimental setup that is fully reproducible independent of the dataset, classi-  
 473 fication model, or AL algorithm used. For a fair comparison of two AL algorithms, both algorithms  
 474 need to receive equal starting conditions in terms of train/validation split, initialization of classifier,

and even the state of minor systems like the optimizer or mini-batch sampler. Even though different implementations might have their own solution to some of these problems, only [10] has described and implemented a fully reproducible pipeline for AL evaluation. The term reproducibility in this work is used as a synonym not only for the reproducibility of an experiment (a final result given a seed), but also the reproducibility of all subsystems independent of each other. The seed for one subsystem should always reproduce the behavior of this subsystem independent of all other subsystems and their seeds. The main obstacle for ensuring reproducibility is the seeding utility in PyTorch, Tensorflow, and other frameworks, whose default choice is a single global seed. Since many subsystems draw random numbers from this seed, all of them influence each other to a point where a single additional draw can completely change the model initialization, data split or the order of training batches. Even though some workarounds exist, e.g. re-setting the seed multiple times, this problem is not limited to the initialization phase, but also extends to the AL iterations and the systems within. We propose an implementation that creates separate Random Number Generators (RNGs) for each of these systems to ensure equal testing conditions even when the AL algorithm, dataset, or classifier changes. We hypothesize that the insufficient setup with global seeds contributes to the ongoing problem of inconsistent results of AL algorithms in different papers.

In summary, we introduce three different seeds:  $s_\Omega$  for the AL algorithm,  $s_\mathcal{D}$  for dataset splitting and mini-batch sampling, and  $s_\theta$  for model initialization and sampling of dropout masks. Unless stated otherwise, we will keep  $s_\Omega$  fixed, while  $s_\mathcal{D}$  and  $s_\theta$  are incremented by 1 between restarts to introduce stochasticity into our framework. Some algorithms require a subsample to be drawn from  $\mathcal{U}$  in order to reduce the computational cost in each iteration, while others need access to the full unlabeled pool (e.g. for effective clustering). If a subsample is required, it will be drawn from  $s_\Omega$  and therefore will not influence other systems in the experiments. For each algorithm, we decided if subsampling is required based on our available hardware, but decided against setting a fixed time limit per experiment, since this would introduce unnecessary complexity into the benchmark. An overview of selected hyperparameters per AL algorithm can be found in Appendix J.

**Note:** Even though we decoupled the subsystems via the described seeds, the subsystems can still influence each other in a practical sense. For example, keeping  $s_\mathcal{D}$  fixed does not mean that always the same sequence of samples from  $\mathcal{U}$  (if subsamples are drawn) are shown to all acquisition functions. This is practically impossible, as different acquisition functions pick different  $x^{(i)}$ . However, the hypothetical **tree** of all possible sequences of samples from  $\mathcal{U}$  remains the same, granting every acquisition function equal possibilities.

## I Oracle Curve Forecasting

TODO

## J Hyperparameters per AL Algorithm

Table 13: Selected hyperparameters for all tested acquisition functions. Last column indicates the source of our implementation.

Algorithm	Sample Size	Other	Source
BADGE	100	Dropout Trials: 5  Min Cluster Size: 5 Max # Clusters: 500	Based on [1, 14]
BALD	100		Based on [4]
Coreset	8000		Own
TypiClust	10000		Based on [8]
Margin	8000		Own
Entropy	8000		Own

## 510 K Hyperparameters and Preprocessing per Dataset

511 For all our datasets we use the pre-defined train/test splits, if given. In the remaining cases, we  
 512 define test sets upfront and store them into separate files to keep them fixed across all experiments.  
 513 The validation set is split in the experiment run itself and depends on the dataset-seed.  
 514 **Tabular:** We use **Splice**, **DNA** and **USPS** from LibSVMTools [20]. All three datasets are normal-  
 515 ized between [0, 1].  
 516 **Image:** We use **FashionMNIST** [25] and **Cifar10** [13], since both are widely used in AL literature.  
 517 Both datasets are normalized according to their standard protocols.  
 518 **Text:** We use **News Category** [18] and **TopV2** [6]. For News Category we use the 15 most com-  
 519 mon categories as indicated by its Kaggle site. We additionally drop sentences above 80 words to  
 520 reduce the padding needed (retaining 99,86% of the data). For TopV2, we are only using the "alarm"  
 521 domain. Both datasets are encoded with pre-trained GloVe (Common Crawl 840B Tokens) embed-  
 522 dings [21]. Since neither dataset provided a fixed test set, we randomly split 7000 datapoints into a  
 523 test set.

Dataset	Seed Set	Budget	Val Split
Splice	1	400	0.2
SpliceEnc.	1	60	0.2
DNA	1	300	0.2
DNAEnc	1	40	0.2
USPS	1	400	0.2
USPSEnc	1	600	0.2
FashionMnist	100	2000	0.04
FashionMnistEnc	1	500	0.04
Cifar10	100	2000	0.04
Cifar10Enc	1	350	0.04
TopV2	1	125	0.25
News	1	1500	0.03

Table 14: Size of the seed set is given by number of labeled sample per class.

Dataset	Classifier	Optimizer	LR	Weight Decay	Dropout	Batch Size
Splice	[24, 12]	NAdam	1.2e-3	5.9e-5	0	43
SpliceEnc.	linear	NAdam	6.2e-4	5.9e-6	0	64
DNA	[24, 12]	NAdam	3.9e-2	3.6e-5	0	64
DNAEnc	linear	NAdam	1.6e-3	4e-4	0	64
USPS	[24, 12]	Adam	8.1e-3	1.5e-6	0	43
USPSEnc	linear	NAdam	7.8e-3	1.9e-6	0	64
FashionMnist	ResNet18	NAdam	1e-3	0	0	64
FashionMnistEnc	linear	Adam	1.6e-3	1e-5	5e-2	64
Cifar10	ResNet18	NAdam	1e-3	0	0	64
Cifar10Enc	linear	NAdam	1.7e-3	2.3e-5	0	64
TopV2	BiLSTM	NAdam	1.5e-3	1.7e-7	5e-2	64
News	BiLSTM	NAdam	1.5e-3	1.7e-7	5e-2	64

Table 15: Classifier architectures and optimized hyperparameters per dataset. Numbers in brackets signify a MLP with corresponding hidden layers.



**Algorithm 1** Active Learning Loop**Require:**  $\mathcal{L}, \mathcal{U}, \mathcal{D}_{\text{test}}, \text{Train}, \text{Seed}, \hat{y}$ **Require:**  $\Omega$ 

▷ Acquisition Function

▷ Create the initial labeled set

```

1:  $\mathcal{L}^{(1)} \leftarrow \text{Seed}(\mathcal{U})$ 
2:  $\mathcal{U}^{(1)} \leftarrow \mathcal{U}$ 
3: for  $i := 1 \dots B$  do
4:    $\text{acc}^{(i)} \leftarrow \text{Train}(\mathcal{L}^{(i)})$ 
5:    $a^{(i)} \leftarrow \Omega(\mathcal{U}^{(i)})$ 
6:    $\mathcal{L}^{(i+1)} \leftarrow \mathcal{L}^{(i)} \cup \{(\mathcal{U}_a^{(i)}, A(\mathcal{U}_a^{(i)}))\}$ 
7:    $\mathcal{U}^{(i+1)} \leftarrow \mathcal{U}^{(i)} \setminus \{\mathcal{U}_a^{(i)}\}$ 
8: return  $\frac{1}{B} \sum_{i=1}^B \text{acc}^{(i)}$ 

```

**Algorithm 2** Retrain**Require:**  $\mathcal{L}, \mathcal{D}_{\text{val}}, \mathcal{D}_{\text{test}}$ **Require:**  $\hat{y}, e_{\text{max}}$ 

```

1:  $\text{loss}^* \leftarrow \infty$ 
2: for  $i := 1 \dots e_{\text{max}}$  do
3:    $\hat{y}_{i+1} \leftarrow \hat{y}_i - \eta \nabla_{\hat{y}} \ell(\mathcal{L}, \hat{y})$ 
4:    $\text{loss}_i \leftarrow \ell(\mathcal{D}_{\text{val}}, \hat{y})$ 
5:   if  $\text{loss}_i < \text{loss}^*$  then
6:      $\text{loss}^* \leftarrow \text{loss}_i$ 
7:   else
8:     Break
9: return  $\text{Acc}(\mathcal{D}_{\text{test}}, \hat{y})$ 

```

**Algorithm 3** Acquire Oracle  $\Omega$ **Require:**  $\mathcal{U}, \mathcal{L}, A, \mathcal{D}_{\text{test}}, \tau, \hat{y}_{\theta}$ **Require:**  $\text{Train}, \text{Margin}, \text{Acc}$ 

```

1:  $\text{acc}^0 \leftarrow \text{acc}^* \leftarrow \text{Acc}(\mathcal{D}_{\text{test}}, \hat{y}_{\theta})$ 
2: for  $k := 1 \dots \tau$  do
3:    $u_k = \text{unif}(\mathcal{U})$ 
4:    $\mathcal{L}' \leftarrow \mathcal{L}^{(i)} \cup \{(u_k, A(u_k))\}$ 
5:    $\hat{y}'_{\theta} \leftarrow \text{Train}(\mathcal{L}', \hat{y}_{\theta})$ 
6:    $\text{acc}' \leftarrow \text{Acc}(\mathcal{D}_{\text{test}}, \hat{y}'_{\theta})$ 
7:   if  $\text{acc}' > \text{acc}^*$  then
8:      $\text{acc}^* \leftarrow \text{acc}'$ 
9:      $u^* \leftarrow u_k$ 
10: if  $\text{acc}^0 = \text{acc}^*$  then
11:    $u^* \leftarrow \text{Margin}(\mathcal{U}, \hat{y}_{\theta})$ 
return  $u^*$ 

```

525 Alg. 3 replaces the acquisition function  $\Omega$  in the AL loop (Alg. L line 5).