

# Deep V-Learning for Pool-Based Active Learning

March 7, 2022

## 1 Introduction

Even though pool-based Active Learning (P-AL) is the more popular setting for Active Learning, it creates significant challenges when reinforcement learning is applied to it. The most prominent one is that both Q-Learning and Policy Gradient Methods require a fixed action space. In the P-AL setting the action space has the same size as the pool of unlabeled images to choose from (or a subsample thereof). Even for simple datasets P-AL methods require a sample size of  $>100$  to work effectively, creating a large action space for the reinforcement learning agent.

### 1.1 Contribution

- First V-Learning Approach for P-AL
- Variable sample sizes to fit every dataset
- (Dataset and model agnostic state space) *Probably not the first*

## 2 Related Work

## 3 Background

### 3.1 V-Learning

V-Learning ([1] p.119) is closely related to Q-Learning. It estimates the value of states rather than the value of all actions given a state (Q-Learning [1] p.131). This requires the environment to provide possible future states  $s_{t+1} \in S_{t+1}$  given any state  $s_t$ . A policy  $\pi_v$  typically chooses the most promising future state  $\operatorname{argmax} V(s_{t+1})$ .

Temporal difference (TD) learning for a neural network parametrized by  $\theta$  gives us a nearly identical update formula compared to Q-Learning

$$\theta \leftarrow \theta + \eta \left( r_t + \gamma \hat{V}_\theta(s_{t+1}) \right) \quad (1)$$

### 3.2 Active Learning as a V-Learning MDP

We change the usual MDP formulation from predecesing literature, which, based on a presented sample of unlabeled samples of size  $k$ , defines a state space  $S := \mathbb{R}^{k \times f}$  with features  $f$  and consequently an action space of  $A := \{1, \dots, k\}$ .

We instead define the state space to be 1-dimensional and use the batch dimension  $b$  for a variable sample size.

$$S := \mathbb{R}^{3+|Z|} := [\text{BvsSB}, \text{Entropy}, \text{F1}, \text{Z}] \quad (2)$$

V-Learning does not define an action space, since the actions are implicit, as defined by the policy  $\pi_v$ . This formulation poses a problem when storing transitions. The starting state  $s_t$  intuitively will be chosen datapoint  $s_{t,a_t}$ , but since we don't want to store the full follow-up state  $s_{t+1} \in \mathbb{R}^{b \times 3 + |Z|}$  we use the average over the batch-dimension. This serves as a proxy of the impact of the implicit action  $a_t$  on the follow-up state  $s_{t+1}$ .

This results in a stored transition  $\phi_t := \{s_{t,a_t}, r_t, \bar{s}_{t+1}, d_t\}$  where  $\bar{s}_{t+1}$  is the average of the follow-up state and  $d_t$  indicates whether a terminal state was reached.

## 4 Methodology

### 4.1 Model and Reinforcement Learning

We use a MLP with a single output neuron  $f_\theta : \mathbb{R}^{3+|Z|} \rightarrow \mathbb{R}$  as agent network. As stated before, the sample of presented datapoints uses the batch dimension for sample size, resulting in  $b$  point-wise predictions of the agent.

For fitting the agent we use a target network  $f_{\theta^-}$  [3], an n-step return ([1] p. 142) with  $n = 3$  and prioritized experience replay [2]

## References

- [1] Andrew G. Barto Richard S. Sutton. *Reinforcement Learning: An Introduction*. MIT Press, Massachusetts, 2 edition, 2020.
- [2] Tom Schaul, John Quan, Ioannis Antonoglou, and David Silver. Prioritized experience replay. *arXiv preprint arXiv:1511.05952*, 2015.
- [3] Hado Van Hasselt, Arthur Guez, and David Silver. Deep reinforcement learning with double q-learning. In *Proceedings of the AAAI conference on artificial intelligence*, volume 30, 2016.