Drehimpulsoperator
$$J = \begin{pmatrix} J_x \\ J_y \\ J_z \end{pmatrix}$$

$$[J_x, J_y] = i\hbar \epsilon_{xyz} J_z$$
 $[H, J^2] = [H, J_z] = [J^2, J_z] = 0$

$$J^{2} |jm\rangle = \hbar^{2} j(j+1) |jm\rangle$$

$$J_{z} |jm\rangle = \hbar m |jm\rangle$$

$$\text{mit } J_{\pm} = J_{x} \pm iJ_{y}$$

$$J_{\pm} |j,m\rangle = \hbar \sqrt{(j \mp m)(j \pm m + 1)} |j,m \pm 1\rangle$$

$$\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$
 $\sigma_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$ $\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$