

Harmonische Störung $V(t) = V e^{i\omega t} + V^\dagger e^{-i\omega t}$

$$\begin{aligned}
 P(i \rightarrow n) &= \left| \left(\frac{-i}{\hbar} \right) \langle n | \int_{t_0}^t V_I(t') dt' | i \rangle \right|^2 \\
 &= \frac{4}{\hbar^2} \left[\frac{|V_{ni}|^2}{(\omega_{ni} + \omega)^2} \sin^2 \left(\frac{(\omega_{ni} + \omega)t}{2} \right) + \frac{|V_{ni}^\dagger|^2}{(\omega_{ni} - \omega)^2} \sin^2 \left(\frac{(\omega_{ni} - \omega)t}{2} \right) \right] \\
 &= \frac{2\pi t}{\hbar^2} |V_{ni}|^2 \delta(\omega_{ni} + \omega) + \frac{2\pi t}{\hbar^2} |V_{ni}^\dagger|^2 \delta(\omega_{ni} - \omega)
 \end{aligned}$$

$ w_{i \rightarrow n} = \underbrace{\frac{2\pi}{\hbar} V_{ni} ^2 \delta(E_n - E_i + \hbar\omega)}_{\text{Emission}} + \underbrace{\frac{2\pi}{\hbar} V_{ni}^\dagger ^2 \delta(E_n - E_i - \hbar\omega)}_{\text{Absorption}} $

