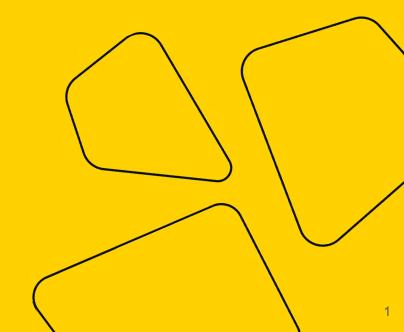
Machine Learning Lecture 1: intro to ML

Radoslav Neychev MIPT, 2021





Outline



- Introduction to Machine Learning, motivation
- 2. ML thesaurus and notation
- 3. Maximum Likelihood Estimation
- 4. Machine Learning problems overview (selection):
 - a. Classification
 - o. Regression
 - c. Dimensionality reduction
- 5. Naïve Bayes classifier
- 6. k Nearest Neighbours (kNN)

Motivation, historical overview and current state of ML and Al

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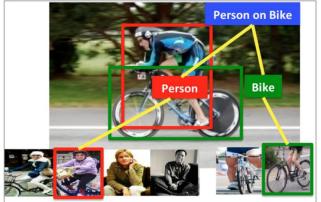
Machine Learning applications





- Object detection
- Action classification
- Image captioning
-





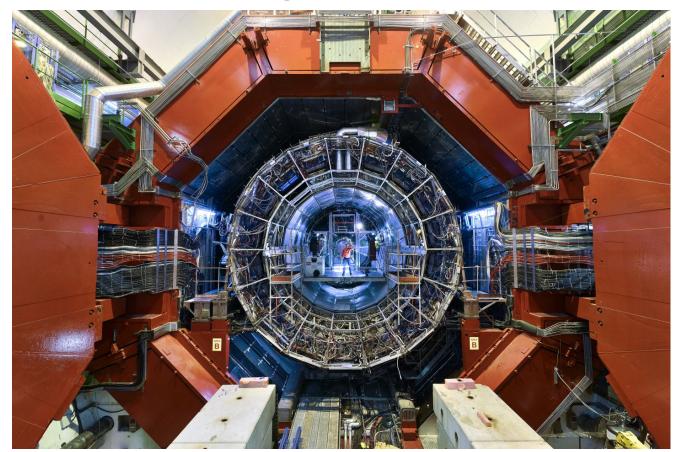
Machine Learning applications





Machine Learning applications



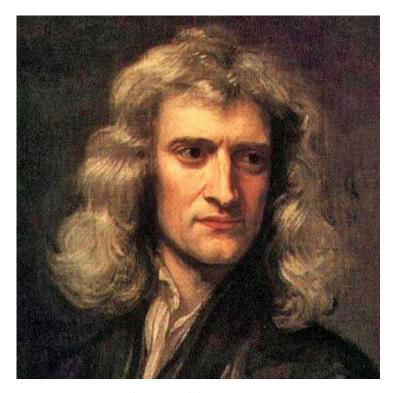




Data Knowledge

Long before the ML





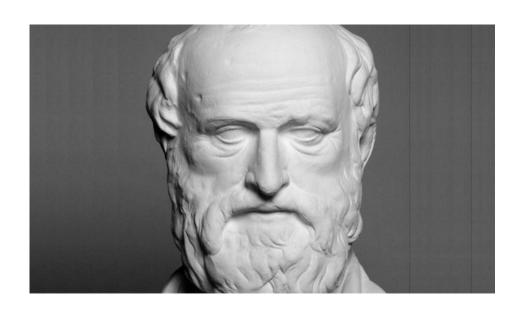
Isaac Newton



Johannes Kepler

Long before the ML





Eratosthenes

girafe





Denote the **dataset**.

| \langle | | | Statistics | Python | | Native | Target | Target |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|----------|
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
| | John | 22 | 5 | 4 | Brown | English | 5 | TRUE |
| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| · · | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| J | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |



Observation (or datum, or data point) is one piece of information.

| , | | • | | . , | · | | | |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|----------|
| \langle | | | Statistics | Python | | Native | Target | Target |
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
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| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| X | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |
| | | | | | | | | |

In many cases the observations are supposed to be *i.i.d.*

- independent
- identically distributed



Feature (or predictor) represents some special property.

| \langle | | | Statistics | Python | | Native | Target | Target |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|----------|
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
| | John | 22 | 5 | 4 | Brown | English | 5 | TRUE |
| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| X | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |



| | , | | | | | | | |
|---|---------|-----|------------|--------|-----------|-----------|--------|----------|
| / | | | Statistics | Python | | Native | Target | Target |
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
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| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
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| | , | | | | | | | |
|---|---------|-----|------------|--------|-----------|-----------|--------|----------|
| / | | | Statistics | Python | | Native | Target | Target |
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
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| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
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| \langle | | | Statistics | Python | | Native | Target | Target |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|----------|
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
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| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
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| | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |



| , | | | | | | | | |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|----------|
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| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
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| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |



And even the name is a **feature**

| | <mark>/</mark> | | | | | | | |
|---|----------------|-----|------------|--------|-----------|-----------|--------|----------|
| / | | | Statistics | Python | | Native | Target | Target |
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
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| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |



The **design matrix** contains all the features and observations.

| , | , | | | | | | | |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|----------|
| \langle | | | Statistics | Python | | Native | Target | Target |
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
| | John | 22 | 5 | 4 | Brown | English | 5 | TRUE |
| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| X | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |

Features can even be multidimensional, we will discuss it later in this course.



Target represents the information we are interested in.

| | | | | | | | I | |
|---|---------|-----|------------|--------|-----------|-----------|--------|----------|
| / | | | Statistics | Python | | Native | Target | Target |
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
| | John | 22 | 5 | 4 | Brown | English | 5 | TRUE |
| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| Y | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |

Target can be either a **number** (real, integer, etc.) – for **regression** problem



Target represents the information we are interested in.

| / | | | | | | | | |
|---|---------|-----|------------|--------|-----------|-----------|--------|----------|
| | | | Statistics | Python | | Native | Target | Target |
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
| | John | 22 | 5 | 4 | Brown | English | 5 | TRUE |
| / | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |

Or a **label** – for **classification** problem



Target represents the information we are interested in.

| / | | | | | | | | |
|---|---------|-----|------------|--------|-----------|-----------|--------|----------|
| / | | | Statistics | Python | | Native | Target | Target |
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (passed) |
| | John | 22 | 5 | 4 | Brown | English | 5 | TRUE |
| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | TRUE |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | TRUE |
| | Michael | 27 | 3 | 4 | Green | French | 5 | TRUE |
| | Some | | | | | | | |
| Y | student | 23 | 3 | 3 | NA | Esperanto | 2 | FALSE |

Mark can be treated as a label too (due to finite number of labels: 1 to 5). We will discuss it later.



Further we will work with the numerical target (mark)

| Name | Age | Statistics (mark) | Python (mark) | Eye color | Native language | Target (mark) |
|---------|-----|----------------------|------------------|-----------|--------------------|------------------|
| John | 22 | , | , | Brown | English | 5 |
| Aahna | 17 | 4 | 5 | Brown | Hindi | 4 |
| Emily | 25 | 5 | 5 | Blue | Chinese | 5 |
| Michael | 27 | 3 | 4 | Green | French | 5 |
| Some | | | | | | |
| student | 23 | 3 | 3 | NA | Esperanto | 2 |



The **prediction** contains values we predicted using some **model**.

| \langle | | | Statistics | Python | | Native | Target | Predicted |
|-----------|---------|-----|------------|--------|-----------|-----------|--------|-----------|
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (mark) |
| | John | 22 | 5 | 4 | Brown | English | 5 | 4.5 |
| 1 | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 4.5 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 5 |
| | Michael | 27 | 3 | 4 | Green | French | 5 | 3.5 |
| | Some | | | | | | | |
| | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3 |

One could notice that prediction just averages of Statistics and Python marks. So our **model** can be represented as follows:



The **prediction** contains values we predicted using some **model**.

| | | | Statistics | Python | _ | Native | Target | Predicted |
|---|---------|-----|------------|--------|-----------|-----------|--------|-----------|
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (mark) |
| | John | 22 | 5 | 4 | Brown | English | 5 | 4.5 |
| | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 4.5 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 5 |
| _ | Michael | 27 | 3 | 4 | Green | French | 5 | 3.5 |
| | Some | | | | | | | |
| 1 | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3 |

Different models can provide different predictions:



The **prediction** contains values we predicted using some **model**.

| | Name | Age | Statistics (mark) | Python (mark) | Eye color | | Target (mark) | Predicted (mark) |
|---|---------|-----|----------------------|------------------|-----------|-----------|------------------|---------------------|
| | John | 22 | 5 | 4 | Brown | English | 5 | 1 |
| | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 5 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 2 |
| | Michael | 27 | 3 | 4 | Green | French | 5 | 4 |
| | Some | | | | | | | |
| 1 | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3 |

Different models can provide different predictions:

$$\operatorname{mark}_{ML} = \operatorname{random}(\operatorname{integer from} [1; 5])$$



The **prediction** contains values we predicted using some **model**.

| | | | I | | | I | I | |
|---|---------|-----|------------|--------|-----------|-----------|--------|-----------|
| | | | Statistics | Python | | Native | Target | Predicted |
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (mark) |
| | John | 22 | 5 | 4 | Brown | English | 5 | 1 |
| / | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 5 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 2 |
| | Michael | 27 | 3 | 4 | Green | French | 5 | 4 |
| | Some | | | | | | | |
| | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3 |

Different models can provide different predictions.

Usually some hypothesis lies beneath the model choice.



Loss function measures the error rate of our model.

| Square deviation | Target (mark) | Predicted (mark) |
|---------------------|------------------|---------------------|
| 16 | 5 | 1 |
| 1 | 4 | 5 |
| 9 | 5 | 2 |
| 1 | 5 | 4 |
| 1 | 2 | 3 |

• **Mean Squared Error** (where **y** is vector of targets):

$$MSE(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{N} ||\mathbf{y} - \hat{\mathbf{y}}||_2^2 = \frac{1}{N} \sum_{i} (y_i - \hat{y}_i)^2$$



Loss function measures the error rate of our model.

| Absolute deviation | Target (mark) | Predicted (mark) |
|-----------------------|------------------|---------------------|
| 4 | 5 | 1 |
| 1 | 4 | 5 |
| 3 | 5 | 2 |
| 1 | 5 | 4 |
| 1 | | 7 |
| | 2 | 3 |

• **Mean Absolute Error** (where **y** is vector of targets):

$$MAE(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{N} ||\mathbf{y} - \hat{\mathbf{y}}||_1 = \frac{1}{N} \sum_{i} |y_i - \hat{y}_i|$$



To learn something, our **model** needs some degrees of freedom:

| | Name | Age | Statistics (mark) | Python (mark) | Eye color | | Target (mark) | Predicted (mark) |
|---|---------|-----|----------------------|------------------|-----------|-----------|------------------|---------------------|
| | John | 22 | 5 | 4 | Brown | English | 5 | 4.5 |
| | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 4.5 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 5 |
| | Michael | 27 | 3 | 4 | Green | French | 5 | 3.5 |
| | Some | | | | | | | |
| 1 | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3 |

$$\operatorname{mark}_{ML} = w_1 \cdot \operatorname{mark}_{Statistics} + w_2 \cdot \operatorname{mark}_{Python}$$



To learn something, our **model** needs some degrees of freedom:

| | | | Statistics | Python | | Native | Target | Predicted |
|---|---------|-----|------------|--------|-----------|-----------|--------|-----------|
| \ | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (mark) |
| | John | 22 | 5 | 4 | Brown | English | 5 | 4.447 |
| | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 4.734 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 5.101 |
| | Michael | 27 | 3 | 4 | Green | French | 5 | 3.714 |
| | Some | | | | | | | |
| 1 | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3.060 |

$$\operatorname{mark}_{ML} = w_1 \cdot \operatorname{mark}_{Statistics} + w_2 \cdot \operatorname{mark}_{Python}$$



To learn something, our **model** needs some degrees of freedom:

| | | | Statistics | Python | | Native | Target | Predicted |
|---|---------|-----|------------|--------|-----------|-----------|--------|-----------|
| | Name | Age | (mark) | (mark) | Eye color | language | (mark) | (mark) |
| | John | 22 | 5 | 4 | Brown | English | 5 | 1 |
| | Aahna | 17 | 4 | 5 | Brown | Hindi | 4 | 5 |
| | Emily | 25 | 5 | 5 | Blue | Chinese | 5 | 2 |
| | Michael | 27 | 3 | 4 | Green | French | 5 | 4 |
| | Some | | | | | | | |
| 1 | student | 23 | 3 | 3 | NA | Esperanto | 2 | 3 |

$$\operatorname{mark}_{ML} = \operatorname{random}(\operatorname{integer from} [1; 5])$$



Last term we should learn for now is **hyperparameter**.

Hyperparameter should be fixed before our model starts to work with the data.

We will discuss it later with kNN as an example.



Recap:

- Dataset
- Observation (datum)
- Feature
- Design matrix
- Target
- Prediction
- Model
- Loss function
- Parameter
- Hyperparameter

Maximum Likelihood Estimation

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Likelihood



Denote dataset generated by distribution with parameter heta

Likelihood function:

$$L(\theta|X,Y) = P(X,Y|\theta)$$

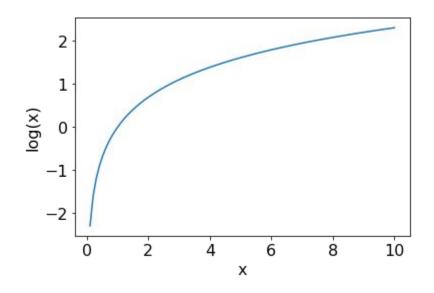
$$L(\theta|X,Y) \longrightarrow \max_{\theta}$$

samples should be i.i.d.

$$L(\theta|X,Y) = P(X,Y|\theta) = \prod_{i} P(x_i, y_i|\theta)$$

Maximum Likelihood Estimation





Likelihood



Denote dataset generated by distribution with parameter $oldsymbol{ heta}$

Likelihood function:

$$L(\theta|X,Y) = P(X,Y|\theta)$$

$$L(\theta|X,Y) \longrightarrow \max_{\theta} \ \ \text{samples should be i.i.d.}$$

$$L(\theta|X,Y) = P(X,Y|\theta) = \prod_{i} P(x_i,y_i|\theta)$$

equivalent to

$$\log L(\theta|X,Y) = \sum_{i} \log P(x_i, y_i|\theta) \longrightarrow \max_{\theta}$$

Machine Learning problems overview

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Supervised learning problem statement

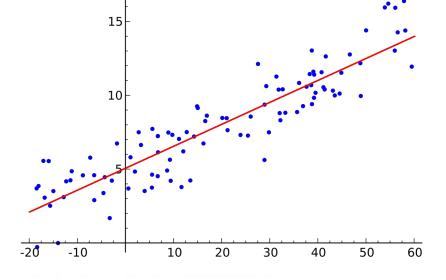


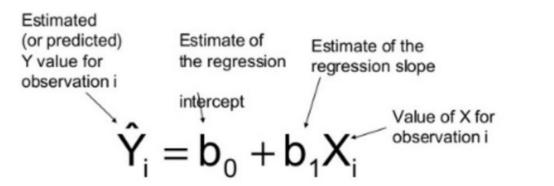
Let's denote:

- Training set $\mathcal{L} = \{\mathbf{x}_i, y_i\}_{i=1}^n$, where
 - $\circ (\mathbf{x} \in \mathbb{R}^p, y \in \mathbb{R})$ for regression
 - $\mathbf{x}_i \in \mathbb{R}^p$, $y_i \in \{+1, -1\}$ for binary classification
- ullet Model $f(\mathbf{X})$ predicts some value for every object
- ullet Loss function $Q(\mathbf{x},y,f)$ that should be minimized



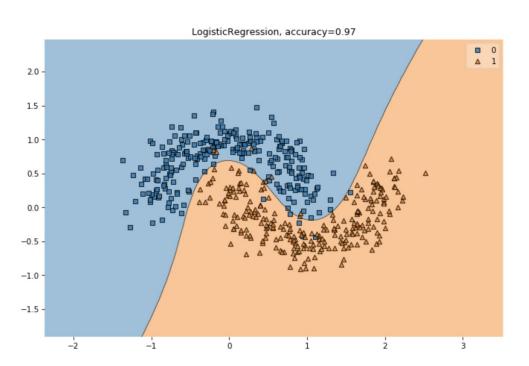
• Regression problem





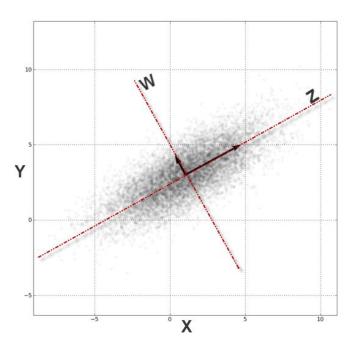


- Regression problem
- Classification problem





- Regression problem
- Classification problem
- Dimensionality reduction



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Let's denote:

- ullet Training set $\mathcal{L} = \{\mathbf{x}_i, y_i\}_{i=1}^n$, where
 - $oldsymbol{arphi}_i \in \mathbb{R}^{p}$, $y_i \in \{C_1, \dots, C_k\}$ for k-class classification

Bayes' theorem



$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

or, in our case

$$P(y_i = C_k | \mathbf{x}_i) = \frac{P(\mathbf{x}_i | y_i = C_k) P(y_i = C_k)}{P(\mathbf{x}_i)}$$



Let's denote:

- Training set $\mathcal{L} = \{\mathbf{x}_i, y_i\}_{i=1}^n$, where
 - \circ $\mathbf{x}_i \in \mathbb{R}^p$, $y_i \in \{C_1, \dots, C_K\}$ for K-class classification

$$P(y_i = C_k | \mathbf{x}_i) = \frac{P(\mathbf{x}_i | y_i = C_k) P(y_i = C_k)}{P(\mathbf{x}_i)}$$

Naïve assumption: features are **independent**



$$P(y_i = C_k | \mathbf{x}_i) = \frac{P(\mathbf{x}_i | y_i = C_k) P(y_i = C_k)}{P(\mathbf{x}_i)}$$

Naïve assumption: features are independent:

$$P(\mathbf{x}_i|y_i = C_k) = \prod_{l=1}^{r} P(x_i^l|y_i = C_k)$$



$$P(y_i = C_k | \mathbf{x}_i) = \frac{P(\mathbf{x}_i | y_i = C_k) P(y_i = C_k)}{P(\mathbf{x}_i)}$$

Optimal class label:

$$C^* = \arg\max_k P(y_i = C_k | \mathbf{x_i})$$

To find maximum we even do not need the denominator

But we need it to get probabilities

kNN – k Nearest Neighbors

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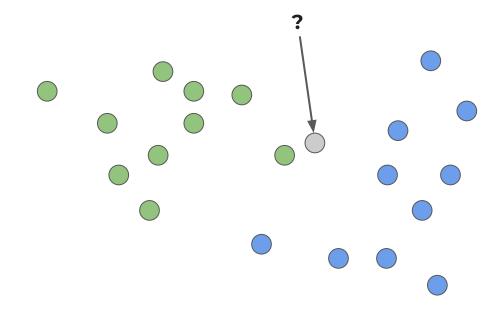


kNN - k Nearest Neighbours



kNN - k Nearest Neighbours





k Nearest Neighbors Method



Given a new observation:

- 1. Calculate the distance to each of the samples in the dataset.
- 2. Select samples from the dataset with the minimal distance to them.
- 3. The label of the new observation will be the most frequent label among those nearest neighbors.

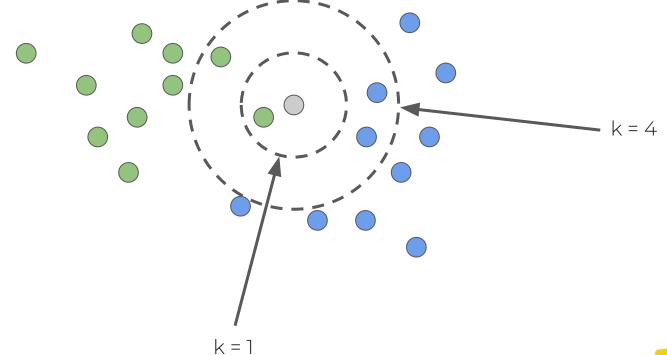
How to make it better?



• The number of neighbors k (it is a **hyperparameter**)

kNN - k Nearest Neighbours



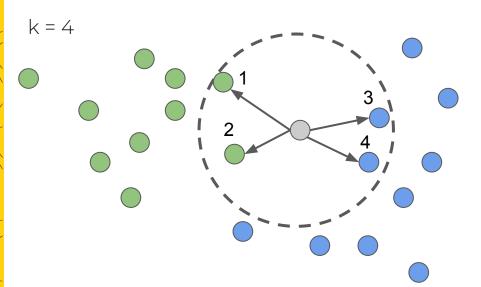


How to make it better?

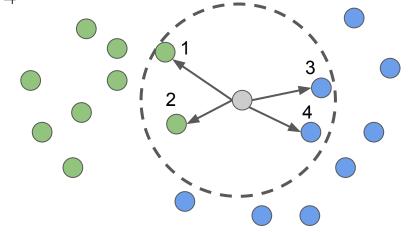


- The number of neighbors k (it is a **hyperparameter**)
- The distance measure between samples
 - a. Hamming
 - b. Euclidean
 - c. cosine
 - d. Minkowski distances
 - e. etc.
- Weighted neighbours







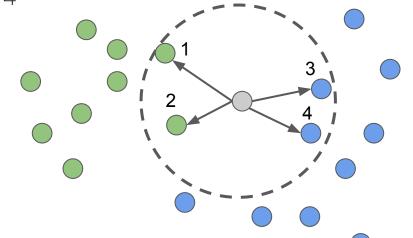


 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$



$$k = 4$$



 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$

or on the distance itself

$$w(\mathbf{x}_{(i)}) = w(d(\mathbf{x}, \mathbf{x}_{(i)}))$$



Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$

ullet or on the distance itself $w(\mathbf{x}_{(i)}) = w(d(\mathbf{x}, \mathbf{x}_{(i)}))$

$$p_{\text{green}} = \frac{w(\mathbf{x}_1) + w(\mathbf{x}_2)}{w(\mathbf{x}_1) + w(\mathbf{x}_2) + w(\mathbf{x}_3) + w(\mathbf{x}_4)}$$



 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$

 $oldsymbol{w}$ or on the distance itself $w(\mathbf{x}_{(i)}) = w(d(\mathbf{x}, \mathbf{x}_{(i)}))$

$$p_{\text{blue}} = \frac{w(\mathbf{x}_3) + w(\mathbf{x}_4)}{w(\mathbf{x}_1) + w(\mathbf{x}_2) + w(\mathbf{x}_3) + w(\mathbf{x}_4)}$$

Outro



- Remember the i.i.d. property
- Usually the first dimension corresponds to the batch size, the second (and so on) to the features/time/...
- Even the naïve assumptions may be suitable in some cases
- Simple models provide great baselines

Revise



- Introduction to Machine Learning, motivation
- 2. ML thesaurus and notation
- 3. Maximum Likelihood Estimation
- 4. Machine Learning problems overview (selection):
 - a. Classification
 - b. Regression
 - c. Dimensionality reduction
- 5. Naïve Bayes classifier
- 6. k Nearest Neighbours (kNN)

A&Q

Thanks for attention!





Model validation and evaluation





Supervised learning problem statement



Let's denote:

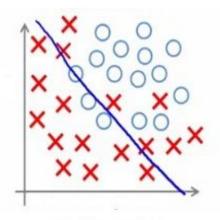
- ullet Training set $\mathcal{L} = \{\mathbf{x}_i, y_i\}_{i=1}^n$, where
 - \circ ($\mathbf{x} \in \mathbb{R}^p$, $y \in \mathbb{R}$) for regression
 - $\mathbf{x}_i \in \mathbb{R}^p$, $y_i \in \{+1, -1\}$ for binary classification

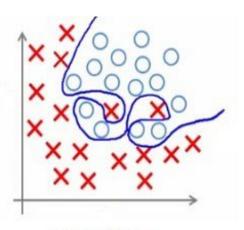
Model $f(\mathbf{x})$ predicts some value for every object

Loss function $Q(\mathbf{x},y,f)$ that should be minimized

Overfitting vs. underfitting







Under-fitting

Appropriate-fitting

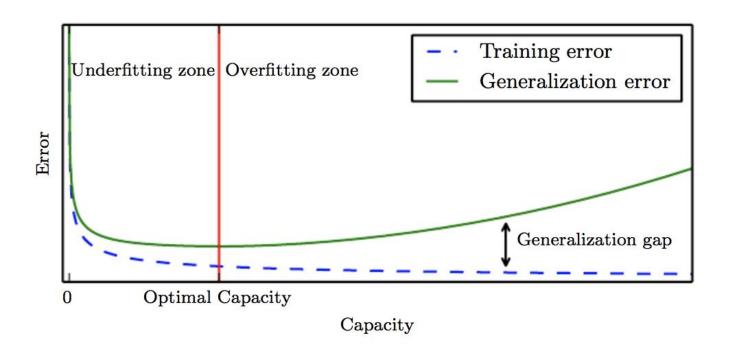
Over-fitting

(too simple to explain the variance)

(forcefitting -- too good to be true)

Overfitting vs. underfitting





Overfitting vs. underfitting



- We can control overfitting / underfitting by altering model's capacity (ability to fit a wide variety of functions):
- select appropriate hypothesis space
- learning algorithm's effective capacity may be less than the representational capacity of the model family



Dataset

Training

Testing

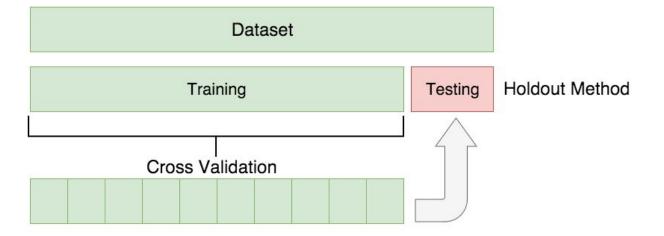
Holdout Method



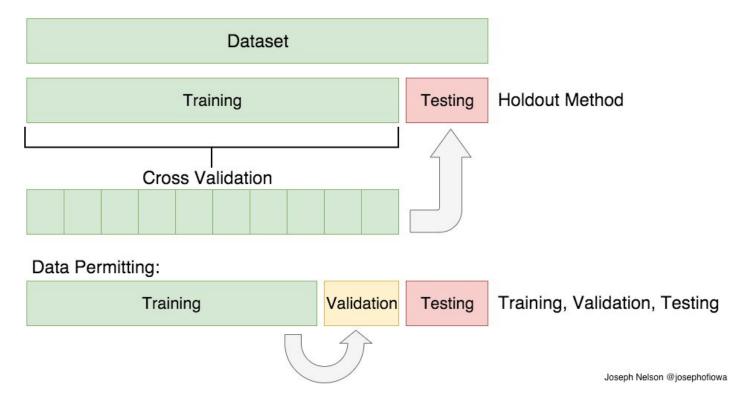


Is it good enough?









Cross-validation



