

# Predicting recreational water quality advisories: a comparison of statistical methods

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## Abstract

Epidemiological studies indicate that fecal indicator bacteria (FIB) in beach water is associated with illnesses among people who have contact with the water. In order to mitigate public health impacts, many beaches are posted with an advisory when the concentration of FIB exceeds a beach action value. The most commonly used method of measuring FIB concentration takes 18–24 hours before returning a result. In order to avoid the 24h lag, it has become common to "nowcast" the FIB concentration using statistical regressions on environmental surrogate variables. Most commonly, nowcast models are estimated using ordinary least squares regression, but other regression methods from the statistical and machine learning literature are sometimes used. This study compares several regression methods across several beaches in Wisconsin to identify which consistently produces the most accurate predictions. A random forest model is identified as the most accurate, followed by the adaptive lasso.

*Keywords:* Regression model; Performance evaluation; Beach health; Water quality

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## 1. Introduction

Fecal indicator bacteria (FIB) in beach water are often used to indicate contamination by pathogens harmful to human health (Cabelli et al., 1979; Wade et al., 2006, 2008; Fleisher et al., 2010). The United States Environmental Protection Agency (USEPA) has established through epidemiological studies that FIB concentration is associated with human health outcomes (Cabelli, 1983; Dufour, 1984; USEPA, 1986). Accordingly, the states have established regulatory standards for water quality. The state of Wisconsin says that a beach should be posted with a swimmer’s advisory when the concentration of *Escherichia coli* (an FIB) exceeds 235 colony forming units (CFU) / 100 mL (USEPA, 2012; Wisconsin Department of Natural Resources, 2012). The beach action value (BAV) of 235 CFU / 100 mL was recommended by the USEPA as the “do not exceed” threshold in order to limit gastrointestinal illnesses among those coming into contact with beach water to 36 cases per 1000 people (USEPA, 2012). The standard method of measuring FIB concentration is by counting CFU in a sample after 18 – 24 hours of incubation (National Environmental Methods Index, 2013). Because of the lag induced by the incubation time, the most up-to-date measurement of FIB concentration is approximately one day old. The model that estimates the current FIB concentration as equal to the most up-to-date measurement is the so-called “persistence model” (USEPA, 2007). Previous research has shown that the concentration of FIB in beach water can vary substantially during the 18 – 24 h incubation period, with the result that the persistence model often provides incorrect information for posting warnings (Whitman et al., 2004; Whitman and Nevers, 2008). Thus, at beaches managed using the persistence model, the public is sometimes exposed to health risks or unnecessarily deprived of recreation opportunities.

In order to have more immediate knowledge of the FIB concentration, it is now common to use regression models that “nowcast” the FIB concentration based on environmental surrogate variables, e.g. turbidity or 24 h rainfall total (Brandt et al., 2006; Olyphant and Whitman, 2004). Ordinary least squares (OLS) regression is the most popular regression method for FIB nowcast models (Nevers and Whitman, 2005; Francy and Darner, 2007; de Brauwere et al., 2014). However, OLS is well-known for drawbacks like overfitting, difficulty of variable selection, and the inflexibility of its linear modeling structure (Ge and Frick, 2007). In order to avoid the pitfalls of OLS, several other regression methods have been used in nowcast models of FIB concentration. They include partial least squares (PLS) (Hou et al., 2006; Brooks et al., 2013), logistic regression (Waschbusch et al., 2004; Jin and Englande Jr., 2006), decision trees (Stidson et al., 2012), random forests (Parkhurst et al., 2005; Jones et al., 2012), and artificial neural networks (Kashefipour et al., 2005; He and He, 2008). A thorough review of the regression methods in use by nowcast models for FIB concentration is available in de Brauwere et al. (2014).

Of particular interest is the one known example of a study that compared predictive models of FIB concentration using several different regression methods. That assessment of seven models for FIB concentration at Santa Monica Beach in California identified classification trees (CT), artificial neural networks (ANN), and binary logistic regression (BLR) with threshold adjustment as the three best methods based on sensitivity, specificity, and total proportion of correct predictions (Thoe et al., 2014). The current study evaluates a different suite of regression methods, though there is overlap. Both studies include partial least squares (PLS) regression, multiple linear regression (MLR), and BLR. In neither study are these among the best performers,

though BLR-T, which includes a threshold adjustment was a top performer in Thoe et al. (2014). All of the methods in the current study use threshold adjustment, which seems to improve predictive performance by identifying exceedances of the BAV more often without unduly increasing the number of false positives. Variable selection for the MLR and BLR models of Thoe et al. (2014) was by stepwise selection; variable selection for the comparable models in the current study was by the genetic algorithm. Models using CT and ANN are not considered in the current study, though we do consider random forest models that consist of thousands of regression trees. We also consider MLR models using the adaptive lasso for variable selection and coefficient estimation.

The literature suggests that many regression methods have been successfully used for nowcast modeling, but most of the available results are specific to a single site. In addition, each study seems to use different standards to manipulate data and summarize performance. Thus, while there are published results indicating that several regression methods outperform OLS for an FIB nowcast model, the existing literature does not compare different methods across a range of sites. In this study, fourteen regression methods are evaluated in nowcast models at seven Wisconsin Great Lakes beaches. The results are compared to identify the methods that most accurately predict instances when a swimmer’s advisory should be posted. This study is designed to compare several regression methods across a range of conditions in order to identify which methods consistently make the best predictions. Accuracy of the predictions is evaluated by comparison to counts made from the traditional FIB analysis method. That is, the FIB count from a cultured sample of beach water is considered the gold standard for evaluation of the predictive nowcast methods.

The performance criteria for comparing models should reflect a study’s aims and the interests of end users (Jakeman et al., 2013; Bennett et al., 2013). Accordingly, the performance criteria in the current study were chosen to answer which method most consistently distinguished between exceedances and nonexceedances of the BAV across the range of sites. Area under the receiver operating characteristic (ROC) curve was used to measure a model’s ability to separate exceedances from nonexceedances; methods were ranked at each site in order to facilitate comparison across sites. A secondary consideration (because it doesn’t directly address the goal of sorting predictions into exceedances and nonexceedances) is how well the predictions matched the measured FIB concentrations. Predictive error sum of squares was used to assess prediction accuracy in this sense, and once again the methods were ranked at each site in order to facilitate a comparison across sites.

Sensitivity, specificity, and total proportion of correct predictions are familiar metrics for evaluating the predictive performance of models for FIB concentration (Thoe et al., 2014). Since calculating these metrics requires a specific choice of decision threshold, we propose a method for setting the threshold and evaluate the sensitivity, specificity, and total proportion correct under this choice of threshold.

## **2. Data**

The seven beach sites analyzed in this study are located within two regions of Wisconsin (Figure 1). Three of the sites are on Chequamegon Bay in Lake Superior and the remaining five are in Manitowoc County along Lake Michigan. The data used in

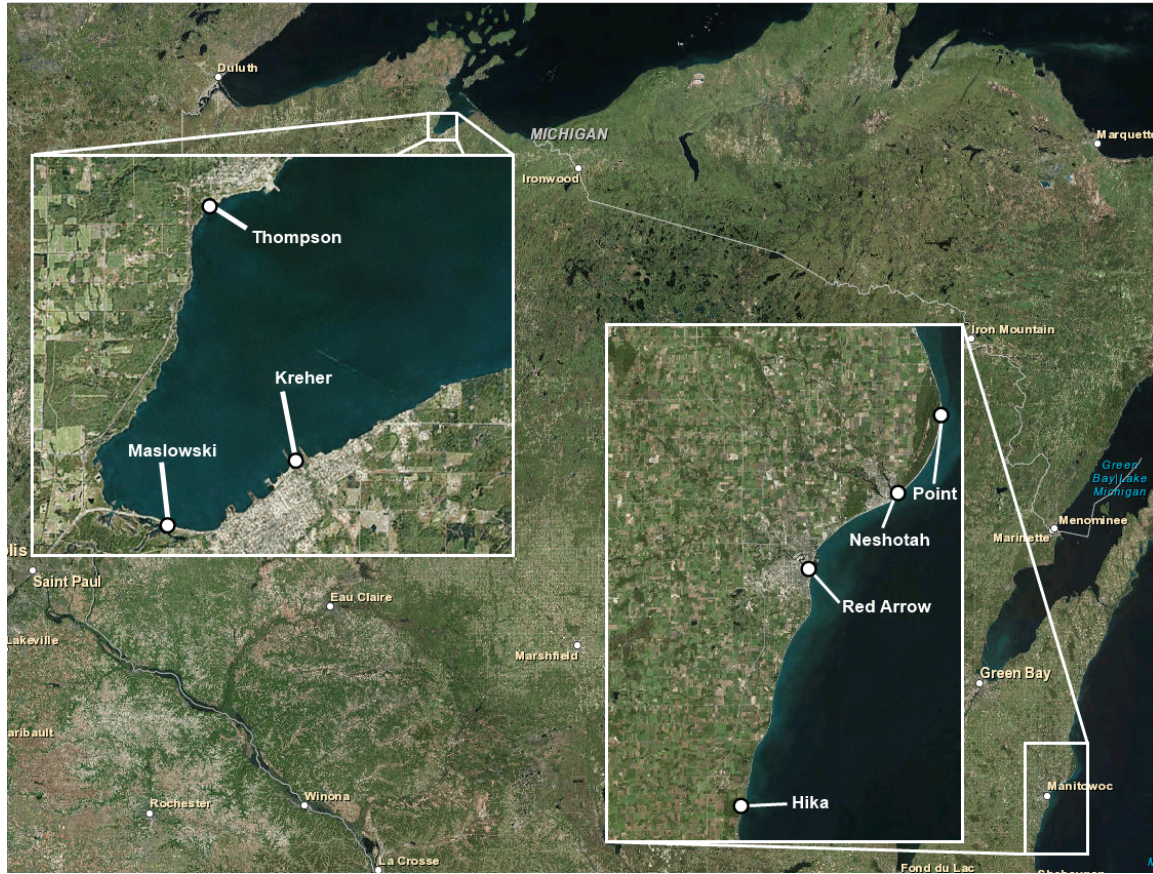


Figure 1: Map showing the location of the seven Wisconsin beaches for which models were analyzed in this work.

the study are the daily FIB concentration and several environmental surrogate variables at each beach during the summer beach seasons of 2010-2013. The surrogates that were used in the predictive models came from a variety of sources. Some were manually measured at the beach sites, some were measured remotely by automated instruments, and the remainder were generated by hydrodynamic and atmospheric models. Examples of data derived from models are wind vectors and lake current vectors. A listing of the surrogates used for predicting the FIB concentration at each beach site is in the Appendix.

## *2.1. Site descriptions*

### *2.1.1. Chequamegon Bay sites*

Chequamegon Bay is approximately 19 km long and ranges from 3 to 10 km in width, with a maximum depth of 11 m. Water quality at the three Chequamegon Bay/Lake Superior beaches is influenced by nearby streams, as well as by urban runoff from Ashland and Washburn, Wisconsin. Thompson Beach is within the city of Washburn, on the north side of the bay. There are two flowing artesian wells that drain to the beach and Thompson Creek, about 300 m from the beach, is the nearest stream. Maslowski Beach is on the west side of Ashland, on the south side of the Chequamegon Bay. Two flowing artesian wells are near the swim area, and Fish Creek (1.5 km west of the beach) and Whittlesley Creek (3 km northwest) are the nearest streams. Kreher Beach is in Ashland, 4 km northeast of Maslowski beach and 1 km west of Bay City Creek. All of the listed streams are influenced by areas of agricultural and forested land use, with Bay City Creek also influenced by urban land use (Francy et al., 2013). Contributions from Fish Creek are dynamic due to a wetland at the creek’s outlet that is influenced by the lake level.

### *2.1.2. Manitowoc County sites*

Red Arrow Beach is within the city of Manitowoc. It has numerous potential influences on water quality, including the mouth of the Manitowoc River 2 km north and urban runoff draining to the beach through storm sewer outlets. The Manitowoc River is dominated by agricultural land use, but there is some urban influence from the city of Manitowoc. The Manitowoc sewage treatment plant sits at the mouth

of the Manitowoc River. Neshotah Beach is in the city of Two Rivers. Small storm sewers drain to the north and to the south directly adjacent to the beach boundaries, and the mouth of the Twin River is 1 km south of the beach. The Twin River drains an agricultural watershed. Point Beach State Park is approximately 18 km north of Manitowoc, about 4 km north of the mouth of Molash Creek whose watershed encompasses a mix of agricultural land use and wetland area. The mouth of Twin River is 10 km south and the mouth of the Kewaunee River is 26 km north of Point Beach State Park. The Kewaunee River is also dominated by agricultural land use. FIB concentration was measured at three beaches within Point Beach State Park, with the samples being considered in the models as three independent observations. Hika Beach is south of the city of Manitowoc near the village of Cleveland. Large floating mats of *Cladophora* algae are common. Centerville Creek, a small stream dominated by agricultural land use, drains to the lake adjacent to the beach.

## 2.2. Data sources

Field data collection and sample analysis followed methods described in Francy et al. (2013). Concentration of *E. coli* was measured at each beach 2–4 times per week for 12–14 weeks between Memorial Day and Labor Day from 2010 through 2013 (during the study period, Memorial Day fell between May 26 and May 31 and Labor Day fell between September 2 and September 6.) Samples were collected from the center of the length of the beach, 30 cm below the water surface where total water depth was 60 cm. All samples were quantified by use of the Colilert QuantiTray/2000 method, and are reported as the most probable number (MPN) of *E. coli* colony forming units (CFU) and were read after 24 hours of incubation (National Environmental Methods



Index, 2013).

Environmental surrogate variables came from online data and manual measurements. Online data were compiled using the publicly available web service Environmental Data Discovery and Transformation (EnDDaT). EnDDaT collects data from public web services provided by federal agencies, aligns the observation times, and performs common transformations (USGS, 2014a). For this study, three data sources were accessed through EnDDaT: The U.S. Geological survey National Water Information System (NWIS) (USGS, 2014b), the National Weather Service North Central River Forecasting Center (National Oceanic and Atmospheric Administration, 2012), and the Great Lakes Costal Forecasting System (Schwab and Bedford, 1999). Surrogates acquired through these sources included: river discharge, precipitation, lake current vectors, wave height, wave direction, lake level, water temperature, air temperature, wind vector, and percent cloud cover.

Most surrogates from online sources were available in hourly increments with the exception of NWIS data which were available in 15 minute increments. In order to make best use of the online data for daily predictions, summary statistics were calculated over several time windows for use as potential surrogates. The statistics by which EnDDaT summarizes measurements during a window period are the mean, minimum, maximum, range, sum, and standard deviation. The use of 1, 2, 6, 12, 24, 48, 72, and 120 hour time windows for calculating the summary statistics followed research showing that selecting from windowed and lagged versions of high-frequency surrogates can improve the predictive accuracy of regression models (Cyterski et al., 2012). The choice of which summary statistics to compute for each environmen-

tal surrogate variable was guided by scientific judgement about how the surrogate could affect the FIB concentration. Some examples of this judgement are listed here. Variability in water temperature may affect the survival and growth of FIB so the standard deviation of water temperature measurements during each window was used as an explanatory variable. The magnitude of recent rain events may determine how much FIB washes into a lake from sources on land, so the sum of rainfall measurements during the window was included as an explanatory variable. Another example: UV light breaks down FIB colonies in the water but this action is inhibited when clouds obscure the sun, so the mean cloud cover measurements during the window was included as an explanatory variable.

Manually collected data were measurements from a specific location and point in time that had the benefit of being measured when and where the FIB samples were collected. However, these surrogates were measured only once per day and at greater expense than the online data because the data had to be collected by field personnel. Scientists from the University of Wisconsin-Oshkosh, Northland College, and Bayfield County collected the data as prescribed by the USEPA’s Great Lakes Beach Sanitary Survey (USEPA, 2008). Among the manually measured data were turbidity, wave height, number of birds present, number of people present, amount of algae floating in the swim area and on the beach, specific conductance, water and air temperature, wind direction, and wind speed. Every beach dataset included turbidity, but other manually collected surrogates occasionally had to be dropped from some of the datasets because of missing values or questionable reliability.

### *2.3. Data transformations*

The response for the continuous regression models was the base-10 logarithm of the FIB concentration. For the binary regression models, the response is an indicator of whether the concentration exceeds the BAV. Transformations were applied to some of the surrogates during pre-processing: the beach water turbidity and the discharge of tributaries near each beach were log-transformed, and rainfall totals were all square root transformed. These transformations were based on the performance of previous studies and were applied to all datasets (Ge and Frick, 2007; Frick et al., 2008).

## **3. Methods**

All of the computations for this study were carried out in the R statistical software environment (R Core Team, 2014). Scripts and details of the how the modeling methods were implemented are in the online supplement. The genetic algorithm, partial least squares, and gradient boosted modeling algorithms are also available as modules in Virtual Beach, a freely-available software package for predicting exceedances of recreational water quality limits (Cyterski et al., 2013). An implementation of the adaptive lasso is also an anticipated addition to Virtual Beach.

### *3.1. Definitions*

For each site, let  $\mathbf{y} = (y_1, \dots, y_n)$  be the vector of  $\log_{10}$  FIB concentration measurements, let  $n$  be the number of observations, and let  $p$  be the number of explanatory variables. The BAV of 235 CFU / 100 mL is represented symbolically in equations

by  $\delta$ . Define an exceedance as an observed FIB concentration that exceeds the BAV. Conversely, a nonexceedance is an observed FIB concentration that does not exceed the BAV.

Predictions are the result of applying a model to data that was not used to estimate the model. The predicted  $\log_{10}$  FIB concentration is denoted by a tilde (e.g.,  $\tilde{y}_i$ ). On the other hand, applying the model to the same data as was used to estimate the model produces fitted values, which are denoted by a hat (e.g.,  $\hat{y}_j$ ). We define a predicted exceedance as when a model predicts that the FIB concentration exceeds the BAV. This is not the same as  $\tilde{y}_i > \delta$  because predictions are compared to a decision threshold  $\hat{\delta}$  rather than to the BAV  $\delta$ . The decision threshold  $\hat{\delta}$  is a parameter that can be adjusted to tune the predictive performance. For instance, increasing the decision threshold reduces the number of false positives but increases the number of false negatives. Setting the decision threshold is an important detail that is discussed in Section 5.4.

### *3.2. Listing of statistical techniques*

Fourteen different regression modeling methods were considered. The (Table 1). Each method uses one of five modeling algorithms: the gradient boosting machine (GBM), the adaptive Lasso (AL), the genetic algorithm (GA), partial least squares (PLS), or sparse PLS (SPLS). Each method is applied to either continuous or binary regression and to either variable selection and model estimation, or variable selection only.

### 3.2.1. Continuous vs. binary regression

The goal of predicting exceedances of the water quality standard is approached in two ways: one is to predict the bacterial concentration and then compare the prediction to a threshold, which is referred to as continuous modeling. The other is referred to as binary modeling, in which we predict the state of the binary indicator  $z_i$ :

$$z_i = \begin{cases} 0 & \text{if } y_i < \delta \\ 1 & \text{otherwise} \end{cases}$$

where  $y_i$  is the FIB concentration and  $\delta$  is the BAV. The indicator is coded as zero when the concentration is below the BAV and one when the concentration exceeds the BAV. All of the binary modeling methods herein use logistic regression (Hosmer Jr and Lemeshow, 2004). Binary regression methods are indicated with a (b).

### 3.2.2. Weighting of observations in binary regression

The concentration of FIB in the water at a single beach on a single day can be subject to a large degree of spatiotemporal heterogeneity (Whitman and Nevers, 2004). Thus, when the concentration in a sample is observed to fall near the BAV, there is considerable uncertainty as to whether an independent sample from the same date and location would or would not exceed the BAV. A weighting scheme for the binary regression methods was designed to reflect this ambiguity by giving more weight to observations far from the BAV. In the weighting scheme, observations were given weights  $w_i$  for  $i = 1, \dots, n$ , where

$$w_i = (y_i - \delta) / \hat{\text{sd}}(y)$$

$$\hat{\text{sd}}(y) = \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2 / n}$$

$$\bar{y} = \sum_{i=1}^n y_i / n.$$

That is, the weights are equal to the number of standard deviations that the observed concentration lies from the BAV. All the methods that were implemented with this weighting scheme were separately implemented without any weighting of the observations. The methods using the weighting scheme are indicated by (w).

### *3.2.3. Selection-only methods*

Modeling methods indicated by an (s) were applied only to select surrogates for a regression model. Once the surrogates were selected, the regression model using the selected surrogates was estimated using ordinary least squares for the continuous methods, or ordinary logistic regression for the binary methods.

### *3.2.4. Listing of modeling algorithms*

*GBM.* A GBM model is a so-called random forest model - a collection of many regression trees, each fit to a randomly drawn subsample of the training data (Friedman, 2001). Prediction is done by averaging the outputs of the trees. Two GBM-based algorithms were studied - we refer to them as GBM-OOB and GBM-CV. The difference between the two is in how the optimal number of trees is determined - GBM-CV

selects the number of trees in a model using leave-one-out cross validation (CV), while GBM-OOB uses the so-called out-of-bag error estimate, where the predictive error of each tree is estimated by its predictive error over the observations that were left out when fitting the tree. In contrast, the predictive error of CV is estimated from observations that are left out from the training data altogether, and are therefore not used in the fitting of any trees. The CV method is much slower (it has to construct as many random forests as there are observations, while the OOB method only requires computing a single random forest). However, GBM-CV should more accurately estimate the prediction error.

*Adaptive Lasso.* The least absolute shrinkage and selection operator (Lasso) is a penalized regression method that simultaneously selects relevant variables and estimates their coefficients (Tibshirani, 1996). The AL is a refinement of the Lasso that possesses the so-called “oracle” properties of asymptotically selecting exactly the correct variables and estimating them as accurately as would be possible if their identities were known in advance (Zou, 2006). To use the AL for prediction requires selecting a tuning parameter. In this study, the AL tuning parameter  $\lambda$  was selected to minimize the corrected Akaike Information Criterion ( $AIC_c$ ) (Akaike, 1973; Hurvich et al., 1998). The  $AIC_c$  for the continuous regression models is

$$AIC_c = \sum_{i=1}^n \frac{(y_i - \hat{y}_i)^2}{\hat{\sigma}^2} + 2df + \frac{2df(df + 1)}{n - df - 1}. \quad (1)$$

where  $\hat{\sigma}^2$  is the variance estimate from the model that used all of the surrogates,  $n$  is

the sample size,  $y_i$  and  $\hat{y}_i$  are respectively the observed and fitted value of the  $i$ th FIB measurement, and  $df$  is the number of surrogates in the model. For binary regression models, the  $AIC_c$  is

$$AIC_c = \sum_{i=1}^n 2 \left\{ z_i \log\left(\frac{z_i}{\hat{z}_i}\right) + (1 - z_i) \log\left(\frac{1 - z_i}{1 - \hat{z}_i}\right) \right\} + 2df + \frac{2df(df + 1)}{n - df - 1} \quad (2)$$

where  $z_i$  and  $\hat{z}_i$  are respectively the observed and fitted value of the  $i$ th BAV exceedance indicator.

*Genetic algorithm.* The GA was used to select surrogates for either an MLR or a BLR model. By analogy to natural selection, so-called chromosomes in the GA represent regression models (Fogel, 1998). A surrogate is included in the model if the corresponding element of the chromosome is one, but not otherwise. Chromosomes are produced in successive generations, where the first generation is produced randomly and subsequent generations are produced by combining chromosomes from the current generation, with additional random drift. The chance that a chromosome in the current generation produces offspring in the next generation is an increasing function of its fitness. The fitness of each chromosome is calculated by the  $AIC_c$  (1), (2).

*PLS.* Partial least squares (PLS) regression is a tool for building regression models with many explanatory variables (Wold et al., 2001). PLS works by decomposing the explanatory variables into mutually orthogonal components, with the components



then used as the covariates in a regression model. This is similar to principal components regression (PCR), but the way PLS components are chosen ensures that they are aligned with the response, whereas PCR is sometimes criticised for decomposing the explanatory variables into components that are unrelated to the response. To use PLS, one must decide how many components to use in the model. Following (Brooks et al., 2013), we use the PRESS statistic to select the number of components.

*SPLS.* Sparse PLS (SPLS) combines the orthogonal decompositions of PLS with the sparsity of Lasso-type variable selection (Chun and Keles, 2010). To do so, SPLS uses two tuning parameters: one that controls the number of orthogonal components and one that controls the Lasso-type penalty. The optimal parameters are those that minimize the mean squared prediction error (MSEP) over a two-dimensional grid search. The MSEP is estimated by 10-fold cross-validation.

### *3.3. Cross Validation*

Our assessment of the modeling methods was based on their performance in predicting exceedances of the BAV. Two types of cross validation were used to measure the performance in prediction: leave-one-out (LOO) and leave-one-year-out (LOYO). In LOO CV, one day's observation was held out for validation while the rest of the data was used to train a model. At Point Beach State Park, where FIB concentration was measured at three locations each day, all three daily observations were left out of the LOO CV models together. The model was used to predict the result of the held out observation(s), and the process - including estimating a new predictive model - was repeated for each date with available data. On the other hand, each cycle of

Abbreviation	Algorithm	Binary	Weighted	Selection Only
GBM-OOB	Gradient boosting out-of-bag tree estimate			
GBM-CV	Gradient boosting cross-validation tree estimate			
AL	Adaptive Lasso			
AL (s)	Adaptive Lasso			X
AL (b)	Adaptive Lasso	X		
AL (b,w)	Adaptive Lasso	X	X	
AL (s,b)	Adaptive Lasso	X		X
AL (s,b,w)	Adaptive Lasso	X	X	X
MLR	Genetic algorithm			
BLR (b)	Genetic algorithm	X		
BLR (b,w)	Genetic algorithm	X	X	
PLS	Patrial least squares			
SPLS	Sparse partial least squares			
SPLS (s)	Sparse partial least squares			X

Table 1: Comprehensive list of the modeling methods analyzed in this study. Listed for each method are the method’s abbreviation, the algorithm used by the method, and indicators of whether the method uses binary regression, observation weighting, and/or variable selection separately from estimation. The two methods GBM-CV and GBM-OOB differ in how the number of GBM trees are selected, as described in the main text.

LOYO CV held out an entire year’s worth of data for validation instead of a single observation. It was intended to approximate the performance of the modeling method under a typical use case: a new model is estimated before the start of each annual beach season and then used for predicting exceedances during the season. The LOYO models in this study were estimated using all the available data except for the held out year, even that from future years. So for instance the 2012 models were estimated using the 2010-2011 and 2013 data.

Some methods also used CV internally to select tuning parameters. In those cases the internal CV was conducted by subdividing the model data, and never looking at the held-out observation(s). This process was independent of the CV to assess predictive performance.

### *3.4. Comparing methods, and quantifying uncertainty in the ranks*

Results were compiled into one table for each site where each observation corresponds to a row in the table. For example, a few rows from the results table at Hika are presented in Table 2. The results table has a column for the observed  $\log_{10}$  FIB concentration and, for each method, columns for the predicted concentration by LOO CV and by LOYO CV. From the table, performance of the modeling methods was summarized by calculating the area under the receiver operating characteristic (ROC) curve (AUROC) and the predictive error sum of squares (PRESS).

The ROC curve is an assessment of how well predictions are separated into exceedances and nonexceedances (Hanley and McNeil, 1982). Every possible value of the decision threshold  $\hat{\delta}$  corresponds to a point on the ROC curve, with coordinates

Row	$\log_{10}$ FIB	PLS (LOO)	PLS (LOYO)	...	SPLS (LOO)	SPLS (LOYO)
1	2.54	2.35	2.22	...	2.29	2.55
2	2.59	1.87	1.79	...	1.91	1.23
$\vdots$	$\vdots$	$\vdots$	$\vdots$	...	$\vdots$	$\vdots$
166	1.57	1.93	2.06	...	1.83	2.07
167	3.38	1.84	2.01	...	1.80	1.71

Table 2: An example of how the results for a site (Hika Beach) were compiled into a results table. The summary statistics used to compare predictive performance (area under the ROC curve and predictive error sum of squares) were calculated from the table. Confidence intervals for the summary statistics were computed via the bootstrap by resampling (with replacement) the rows of the results tables.

$(1 - \text{specificity}(\hat{\delta}), \text{sensitivity}(\hat{\delta}))$ . Specificity is the fraction of decision threshold non-exceedances that have been correctly predicted. Sensitivity is the fraction of decision threshold exceedances that have been correctly predicted. Specificity and sensitivity are mathematically defined as

$$\text{specificity}(\hat{\delta}) = \sum_{i=1}^n I(\tilde{y}_i \leq \hat{\delta}) I(y_i \leq \delta) / \sum_{j=1}^n I(y_j \leq \delta)$$

$$\text{sensitivity}(\hat{\delta}) = \sum_{i=1}^n I(\tilde{y}_i > \hat{\delta}) I(y_i > \delta) / \sum_{j=1}^n I(y_j > \delta).$$

where  $I(A)$  is the indicator function that takes value one if  $A$  is true and zero if  $A$  is false.

The AUROC averages the model's performance over the range of possible thresholds. A model which perfectly separates exceedances from non-exceedances in prediction would have an AUROC of one, while a model that predicts exceedances no better than a coin flip would have an expected AUROC of 0.5.

While AUROC quantifies how well a model sorts exceedances and non-exceedances, PRESS measures how accurately a model’s predictions match the observed FIB concentration. The PRESS can only be computed for continuous regression methods. Recalling that the  $i$ th observed  $\log_{10}$  FIB concentration is denoted  $y_i$  and that the corresponding prediction is denoted  $\tilde{y}_i$  for  $i = 1, \dots, n$  where  $n$  is the total number of predictions, the PRESS is given by

$$\text{PRESS} = \sum_{i=1}^n (\tilde{y}_i - y_i)^2.$$

To identify which modeling methods had the best performance across all sites, the methods at each site were ranked from worst to best according to AUROC and PRESS (the ranks were taken worst to best so that larger numbers represent better performance). The mean rank of each method was then taken across the sites as a measurement of how each of our modeling methods performed relative to the others. Uncertainty in the rankings was quantified by the bootstrap: since PRESS and AUROC are functions of the results tables, the bootstrap procedure was carried out by resampling the rows of each results table and recalculating the ranks for each bootstrap sample. We used 1,000 bootstrap samples of each results table in the analysis that follows.

### *3.5. Classifying responses under a specific decision threshold*

While AUROC measures how well exceedances and nonexcedances are sorted among the predictions, AUROC is an average accuracy over all possible thresholds. In order

to provide the assessment most relevant for operational use, the LOYO CV results were analyzed to count how many correct and incorrect predictions would be seen with a specific choice of decision threshold. Using the LOYO CV results simulates the common scenario that a model is estimated at the beginning of each beach season and used to make predictions during that season, with a new model incorporating the new season of data estimated the following year into the new model’s training data.

Intuitively, the decision threshold should adapt to the conditions that are observed in the beach’s training data. If, for instance, exceedances were rare in the training data, then we expect few exceedances in the future, and should set the decision threshold high to reflect this expectation. On the other hand, if the bacterial concentration often exceeds the BAV, then the decision threshold should be set lower in order to properly flag more of those exceedances. This intuition was encoded into how the decision threshold was set for the LOYO models. Specifically, the decision threshold  $\hat{\delta}$  was set to the  $q^{th}$  quantile of the fitted values of non-exceedances in the training set, where  $q$  is the proportion of training set observations that are non-exceedances.

## 4. Results and discussion

### 4.1. AUROC

The mean LOO and LOYO ranks were computed for all of the methods as determined by AUROC (Figure 2). The three top-ranked methods were GBM-CV, GBM-OOB, and AL. In order to facilitate a pairwise comparison between modeling methods, the frequency that the mean AUROC rank of GBM-OOB, GBM-CV, or AL exceeded

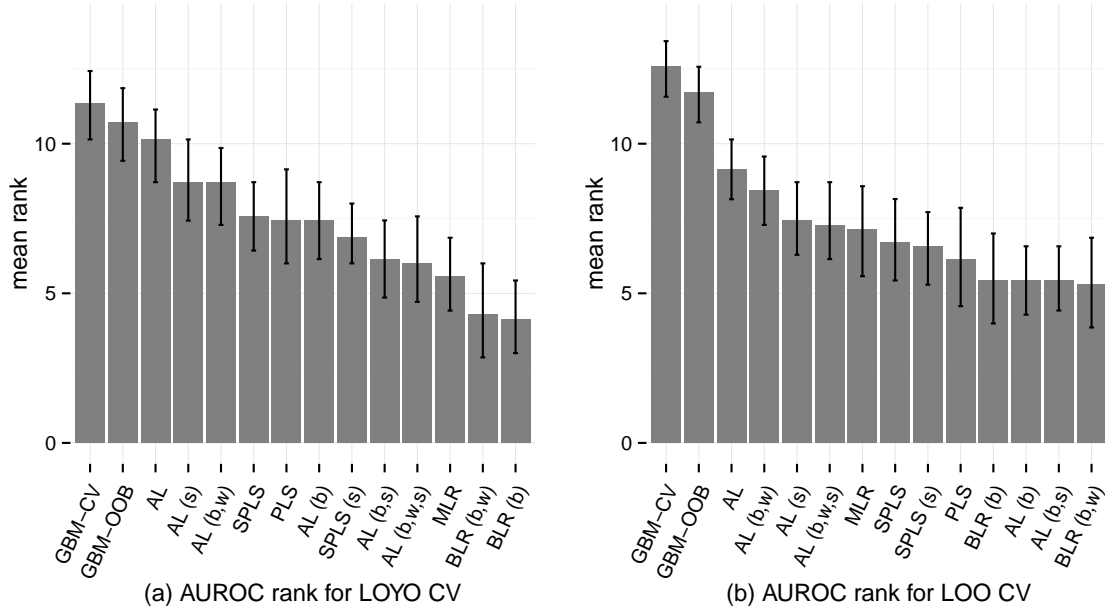


Figure 2: Mean ranking of the methods across all sites by area under the receiver operating characteristic curve (AUROC). Higher is better, with a value of 14 indicating that the method had the greatest AUROC at every site. The error bars are 90% confidence intervals computed by the bootstrap. At left are the AUROC rankings from the leave-one-year-out cross validation (a), at right are the AUROC rankings from the leave-one-out cross validation (b).

each of the other modeling methods for the leave-one-year-out and the leave-one-out analyses were also computed (Table 3).

#### 4.2. PRESS

The PRESS statistic is of interest because a good model should accurately predict the bacterial concentration, but for assessing regression models for FIB concentration, AUROC is more important than PRESS because it directly measures the models' abilities to distinguish exceedances from nonexceedances. That said, we expect the two statistics to usually agree on which modeling methods perform best.

Leave-one-year-out cross-validation:

	GBM- OOB	AL	AL (s)	AL (b,w)	SPLS	PLS	AL (b)	SPLS (s)	AL (b,s)	AL (b,w,s)	MLR	BLR (b,w)	BLR (b)
GBM-CV	0.86	0.87	0.98	0.99	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
GBM-OOB		0.69	0.92	0.95	1.00	0.99	0.99	1.00	1.00	1.00	1.00	1.00	1.00
AL			0.96	0.87	1.00	0.97	0.98	1.00	1.00	1.00	1.00	1.00	1.00

Leave-one-out cross-validation:

	GBM- OOB	AL	AL (b,w)	AL (s)	AL (b,w,s)	MLR	SPLS	SPLS (s)	PLS	BLR (b)	AL (b)	AL (b,s)	BLR (b,w)
GBM-CV	0.96	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
GBM-OOB		1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
AL			0.72	0.99	0.93	0.96	0.98	1.00	0.99	1.00	1.00	1.00	1.00

Table 3: Under leave-one-year-out (top) and leave-one-out (bottom) cross validation, frequency of the mean AUROC rank of GBM-OOB, GBM-CV, or AL (in the rows) exceeding that of the other methods (in the columns).

The top three methods under both LOO and LOYO analysis as determined by PRESS were GBM-CV, GBM-OOB, and AL (Figure 3). Again, to facilitate a pairwise comparison between modeling methods, the frequency that the mean PRESS rank of GBM-OOB, GBM-CV, or AL exceeded each of the other modeling methods for the leave-one-year-out and the leave-one-out analyses were computed (Table 4).

#### 4.3. Narrowing the focus

By AUROC and PRESS, and for LOO and LOYO analyses, the three highest-ranked modeling methods were GBM-CV, GBM-OOB, and AL. The fourth-ranked method was not consistent across the different analyses. By the LOO CV analysis, AL was ranked better than the fourth-ranked method by AUROC, AL (b,w), on 72% of bootstraps and better than the fourth-ranked method by PRESS, SPLS (s), on 73% of bootstraps. And by the LOYO CV analysis, AL was ranked better than the fourth-ranked method by AUROC, AL (s), on 96% of bootstraps and better than the fourth-ranked method by PRESS, SPLS, on 52% of bootstraps. Therefore, we consider only the GBM methods and AL for the following analyses because they consistently outperform the other methods.



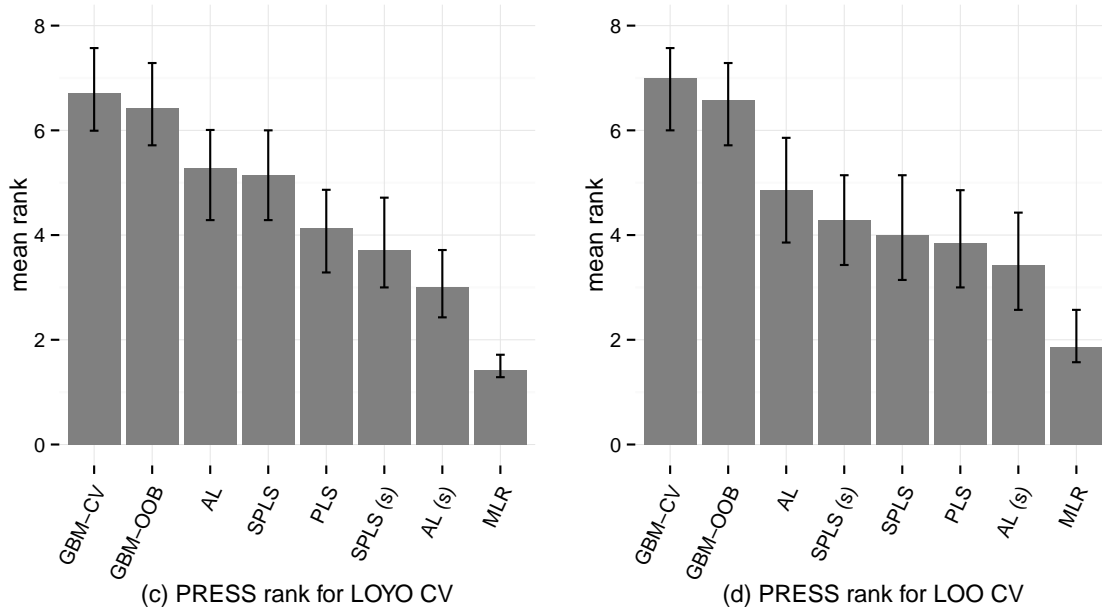


Figure 3: Mean ranking of the methods across all sites by predictive error sum of squares (PRESS). Higher is better, with a value of 8 indicating that the method had the minimum PRESS at every site. The error bars are 90% confidence intervals computed by the bootstrap. At left are the PRESS rankings from the leave-one-year-out cross validation (a), at right are the PRESS rankings from the leave-one-out cross validation (b).

#### Leave-one-year-out cross-validation:

	GBM-OOB	AL	SPLS	PLS	SPLS (s)	AL (s)	MLR
GBM-CV	0.58	0.96	0.97	1.00	1.00	1.00	1.00
GBM-OOB		0.94	0.96	1.00	1.00	1.00	1.00
AL			0.52	0.88	0.94	0.99	1.00

#### Leave-one-out cross-validation:

	GBM-OOB	AL	SPLS (s)	SPLS	PLS	AL (s)	MLR
GBM-CV	0.66	0.99	1.00	1.00	1.00	1.00	1.00
GBM-OOB		0.97	1.00	1.00	1.00	1.00	1.00
AL			0.73	0.80	0.85	0.93	1.00

Table 4: Under leave-one-year-out (top) or leave-one-out (bottom) cross validation, frequency of the mean PRESS rank of GBM-CV, GBM-OOB, or AL (in the rows) exceeding that of the other methods (in the columns).

#### *4.4. Performance with a specific threshold*

The AUROC results are abstract because the AUROC is computed by averaging over all possible decision thresholds. More concrete results can be reported if we set a decision threshold for each model, which we do in the manner described in Section 4.5. In Figure 4, we present the counts on a per-beach basis of four categories of decisions: true negatives (correct predictions of nonexceedances), false positives (incorrect predictions of exceedances) true positives (correct predictions of exceedances), and false negatives (incorrect predictions of nonexceedances). In most cases, the counts were similar between the three methods, with GBM-OOB and GBM-CV commonly resulting in a few more correct decisions than AL. There are, however, exceptions where AL results had more correct decisions (e.g., Hika and Red Arrow).

The specificity, sensitivity, and overall proportion correct for these models are reported in Table 5. The mean specificity and percentage of correct predictions was greatest under the GBM-CV method, at 80% and 76%, respectively. However, mean sensitivity was greatest for the AL method, at 56%, compared to 51% for both of the GBM methods.

#### *4.5. Variable selection*

One difference between the AL and GBM algorithms is that AL does variable selection while GBM-OOB uses all of the available surrogates. In Figure 5, the number of surrogates selected by the AL is compared to the total number of available surrogates.

At most of the sites, AL uses only a small fraction of the available surrogates, but at Point Beach, AL uses almost all of the available surrogates. This is due to the

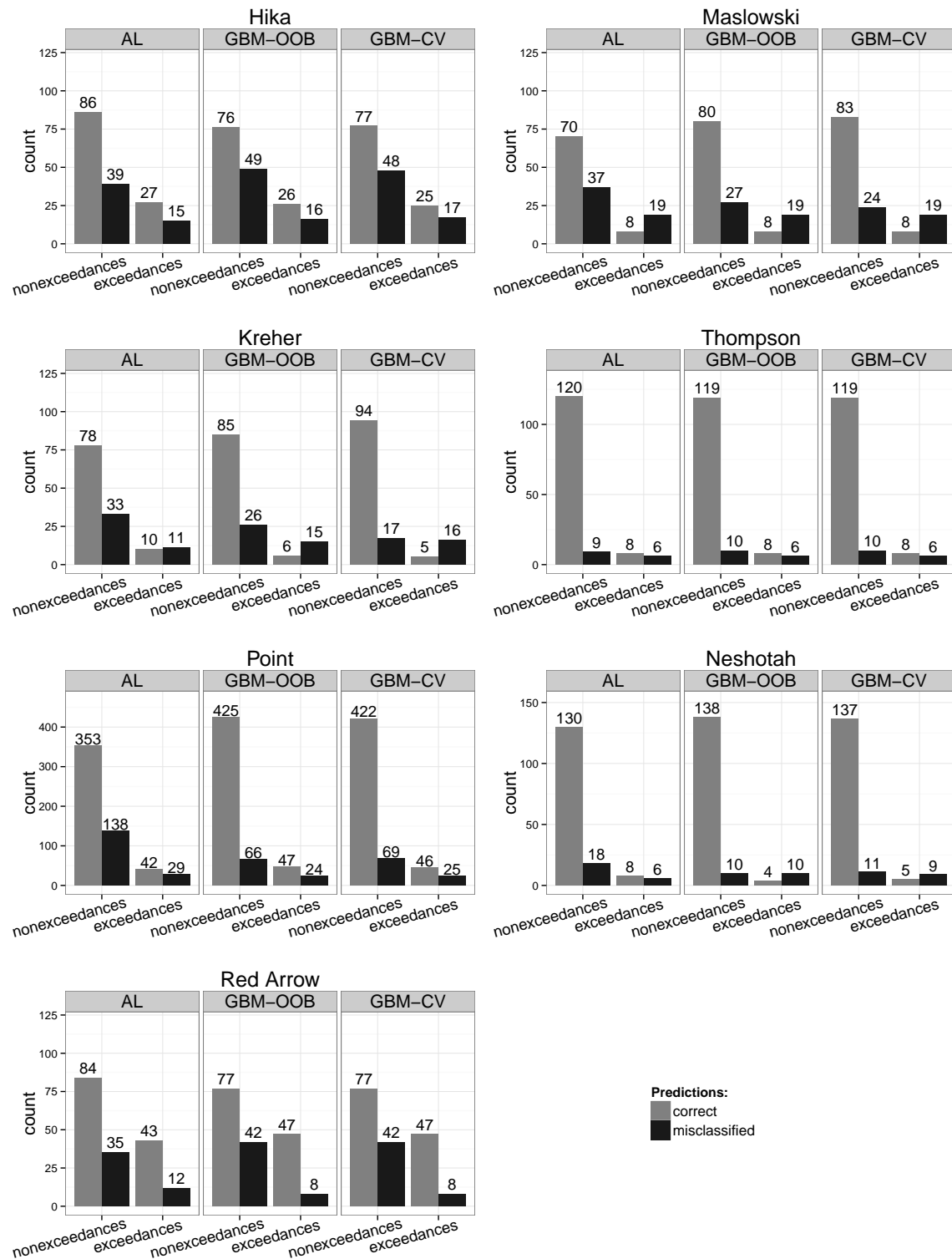


Figure 4: At each site, the number of predictions from AL, GBM-OOB, and GBM-CV that fell into four categories, from left: true negatives, false positives, true positive, and false negatives.

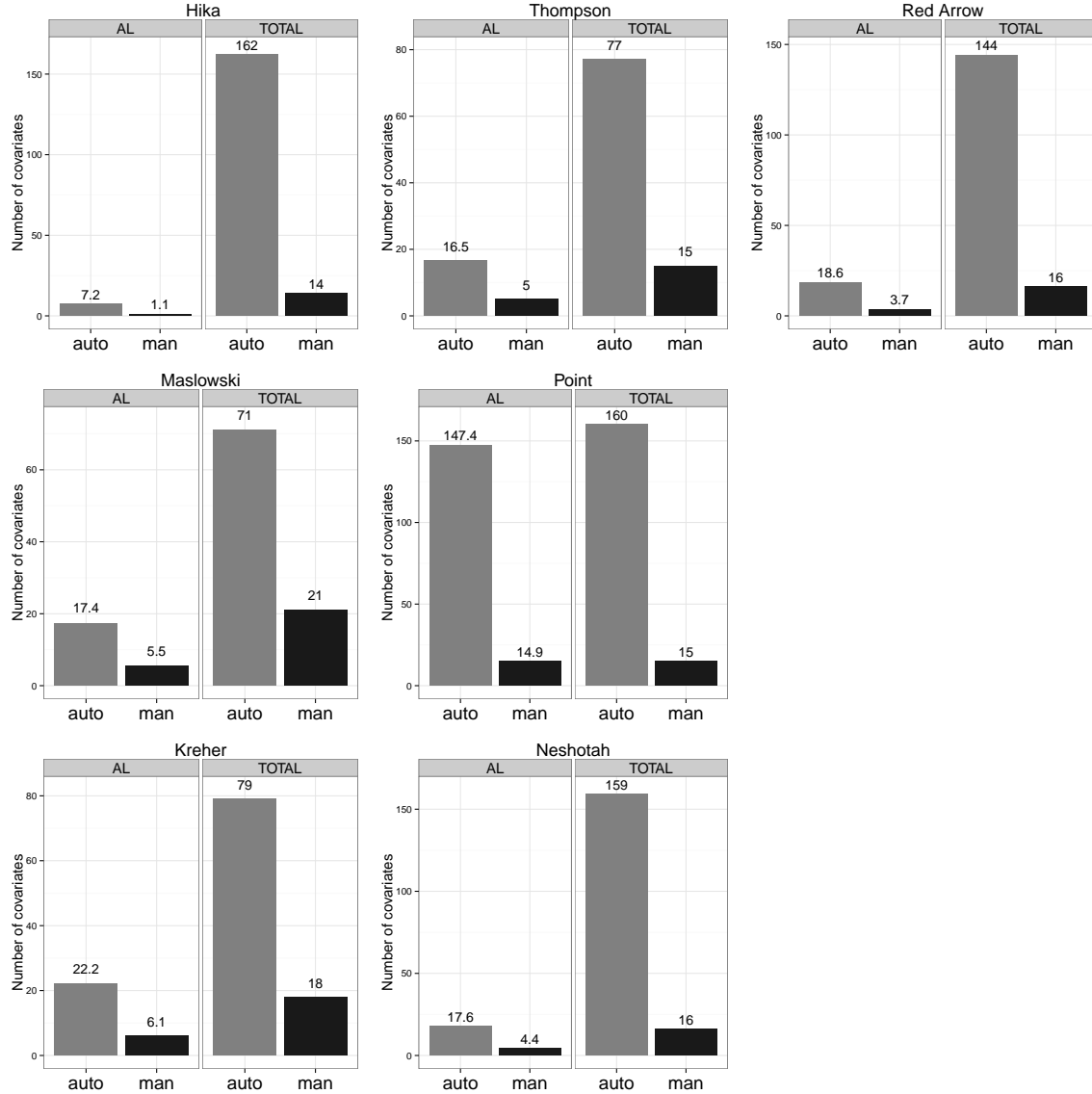


Figure 5: At each site, the mean number of surrogates that were selected for the AL model, and the total number of surrogates, all of which were used in the gradient boosting machine with an out-of-bag estimate of the optimal tree count (GBM-OOB) models. For both AL and GBM-OOB, the surrogate counts are broken down by whether the data values were collected automatically from web services or manually at the beach.

Site	AL			GBM-OOB			GBM-CV		
	specificity	sensitivity	correct	specificity	sensitivity	correct	specificity	sensitivity	correct
Hika	69	64	68	61	62	61	62	60	61
Maslowski	65	30	58	75	30	66	78	30	68
Kreher	70	48	67	77	29	69	85	24	75
Thompson	93	57	90	92	57	89	92	57	89
Point	72	59	70	87	66	84	86	65	83
Neshotah	88	57	85	93	29	88	93	36	88
Red Arrow	71	78	73	65	86	71	65	86	71
Mean	75	56	73	78	51	73	80	51	76

Table 5: Performance of the predictive models at each of the sites in this study are summarized in terms of specificity, sensitivity, and overall proportion of correct decisions. The models summarized here were estimated using the adaptive lasso (AL), gradient boosted modeling with out-of-bag estimate for the tree number (GBM-OOB), and GBM with cross-validation estimate for the tree number (GBM-CV). The entries are multiplied by 100 to be percentages rather than proportions. The "Mean" row reports the average of the seven site rows.

variable selection criterion we used ( $AIC_c$ ) which is intended to minimize predictive error. As the amount of data increases, we accumulate enough information to discern an effect even of surrogates that are only slightly correlated with the response. As our dataset grows, then, we should expect more surrogates to be selected for an AL model, and Point has far more observations than the other sites.

Where it is important to minimize the number of environmental surrogate variables in a model, the selection criterion used here ( $AIC_c$ ) may not be ideal. In that case it may be advantageous to use a criterion that is more conservative about including surrogates, such as the Bayesian information criterion (BIC), for which the penalty term  $2df + 2df(df + 1)/(n - df - 1)$  in (1) or (2) would be replaced by  $n \times df$ , which grows with the sample size  $n$ . The BIC does not exhibit the property of the AIC (or  $AIC_c$ ) where more surrogates are included in the model as the number of observations increases. However, the BIC is derived from the standpoint of identifying the most probable model, rather than minimizing the predictive error. It is therefore likely that an AL model using the BIC for variable selection will have slightly worse predictive

performance than one using the  $AIC_c$ .

## 5. Conclusions

The GBM-CV, GBM-OOB, and AL methods showed the best results by both PRESS and AUROC, under LOO and LOYO cross validation. Though GBM-CV was a bit more accurate than GBM-OOB in all the settings, the small improvement in accuracy may not outweigh the large additional cost in computational time to fit the model. However, the additional computational cost is incurred only once when the model is estimated - given a new observation of beach data, both the GBM-CV and GBM-OOB models produce predictions nigh-instantaneously. Where predictive accuracy is the most important consideration and no difficulty is anticipated in acquiring the data, it is hard to argue against using a GBM-type model.

The predictive performance of the AL models was somewhat worse than that of the GBM models, but by including a variable selection step, the AL models reduce the number of surrogates that must be measured in order to make daily predictions. A model that requires fewer surrogates is less expensive and more robust (since each new environmental surrogate variable increases the chance of missing data). This is particularly important for manually-collected surrogates because collecting data by hand takes more time and is more costly than accessing publicly available data from a web service. Across all of the sites, the ratio of manually-collected to automatically collected surrogates in the AL models seems to mirror the ratio among all available surrogates, indicating that neither the manually- nor automatically-collected surrogates are consistently more important to predicting the FIB concentration. Some

surrogates tended to appear at every site in the AL models (and other models that include a variable selection step). The manually-collected surrogates that were consistently selected for the models were the (log) turbidity in the beach water, and wave height at the beach.

Another advantage of the AL over GBM-type models is interpretability. As a linear regression method, fitting an AL model means estimating a set of coefficients, which can be interpreted as the marginal effect of a change in the corresponding surrogate. On the other hand, GBM produces black-box models that typically make more accurate predictions but are difficult to interpret. One common way to interpret a random forest model (such as from the GBM algorithm) is to observe the proportion of splits in the underlying trees that involve a particular surrogate. The split proportion is a measurement of that surrogate’s importance to the model but gives no indication of how the surrogate affects the bacterial concentration.

## **6. Acknowledgments**

The authors note with gratitude the contributions made by these organizations and their people. Beach water samples and the manual surrogates were collected by scientists from the University of Wisconsin-Oshkosh, Northland College, and Bayfield County. The collection effort was coordinated by the Wisconsin Department of Natural Resources. The predictive models for this study were generated using facilities and software (HTCondor) provided by the University of Wisconsin-Madison’s Center for High Throughput Computing. The remotely sensed surrogates were measured and made available by the National Weather Service’s North Central River Forecasting

Center and Great Lakes Coastal Forecasting System, and the USGS' National Water Information Service. The Environmental Data Discovery and Transformation tool that was used to access the remotely sensed surrogates was created by the USGS' Center for Integrated Data Analytics.

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