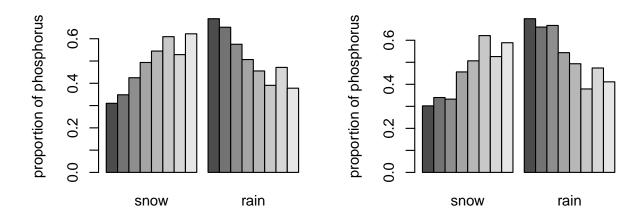
# Analysis of loadings

## Wesley Brooks



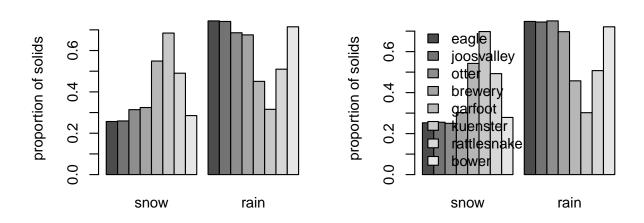


Figure 1 – Cumulative storm loadings at the four creeks.

## 1 Goal

Stream health is threatened by high sediment and phosphorus loads, which are carried into the streams by runoff from the surrounding landscape. It has been shown previously[1] that the phosphorus and sediment loads in Wisconsin are not evenly

distributed in time - rather, most of the annual loading arrives during two pulses: one in early spring, associated with the melting of the winter snowpack, and the other in midsummer, at the same time as the most intense summer thunderstorms.

In this study, we define loading "events" that can span multiple days of continuous runoff. Our goal is to then characterize the events that produce the greatest loading, in order to inform management practices that aim to improve stream health by reducing sediment and phosphorus loads. Our ultimate goal is a mathematical model of stream loading based on some easily-interpretable covariates. Ideally, we will arrive at a global model for all the sites in the study. The alternative are a collection of local models that seem to describe only the specific sites at which they are calibrated.

## 2 Data

**Description** The data in this report comes from eight Wisconsin streams that were monitored (with some gaps in data collection) between 1989 and 2009. The streams and the period during which each was monitored are in Table ??, except that the phosphorus loading was not measured at Brewery Creek from October 1999 onward.

$\mathbf{Stream}$	Events	Years
Eagle	429	1991-1994, 2003-2007
Joos Valley	473	1990-1994, 2002-2007
Otter	424	1990-1997, 2000-2002
Brewery	670	1985, 1990-1998, 2000-2001
Garfoot	527	1985, 1990-1993, 1995-1998
Kuenster	218	1992-1995
Rattlesnake	170	1991-1994
Bower	373	1990-1994, 2006-2009

Each entry in our data set represents one loading event. Events are defined based on the hydrograph - an event begins when the flow rises from a base level toward a peak, and ends when the flow falls back to its new base level. A computer program called Rainmaker was used to separate the total stream flow into base flow and storm flow components. The hydrograph separation is done by analyzing the beginning and ending base flows and the peak storm flow for each event. The storm flow input that drives each event can come from rainfall, from melting snow, or from some combination of the two.

Two kinds of load are measured for each event - the sediment load and the phosphorus load. The load from each event can be divided into two components: the base flow component and the storm flow component. The two components refer, respectively, to the load carried by the stream's base flow and that carried by the additional storm flow pulse. Rainmaker separates the two components based on the hydrograph.

Not all of the data can be collected for each event. For instance, rainfall is measured only when the ground is free of snow, because snow interferes with the rain gauges. And the amount of snowmelt is estimated by multiplying the snow's water content by the change in snow depth during a warm snap, which is inaccurate when additional snow falls during the event. Broadly, there is one set of measurements that are made during rainfall-driven events and a different set of measurements that are made during snowmelt-driven events. Because of this, the two types of event are modeled separately. Furthermore, compared to the data about events that are rainfall-driven, the data about events that are snowmelt-driven is of lower quality. That's because: the accuracy of the stream gauge is reduced by ice on the stream, the winter rainfall, snow depth, and water content are not measured locally (snow data tends (or is it always?) to come from the nearest large airport.) It would be surprising if the accuracy of models for snowmelt-driven loading were comparable to that of models for rainfall-driven loading.

All else being equal, a stream that drains a larger area should have a greater flow, and should carry a greater load of sediment and phosphorus. For this reason, the sediment and phosphorus loads were divided by the drainage area to get the sediment and phosphorus yields. The yields will be the output from our models.

We augmented the data with some antecedent values that we thought could possibly affect the loadings produced during an event. These were the base flow one day before the event, the two-day antecedent mean temperature, the maximum temperature over the two days before the event, and the range between the two-day antecedent max and min temperatures.

Some of the data were measured at a gauge station on each stream - these were the stream gauge, local rainfall (including intensity and duration), and the concentrations of sediment and phosphorus (the concentrations were multiplied by the stream flow to get the loadings.) Other data such as rainfall, snowfall, snow depth, snow water content, and air temperature were measured by the National Weather Service (NWS) at a permanent weather station. We downloaded these data from a database maintained by the NWS. Finally we have some metadata that describes our data at the watershed level: the drainage area, the average stream slope, and the land use composition.

Some of the variables in the analysis were generated from the measurements rather than being measured directly. For instance, the sediment yield (tons per square mile) and phospohrus yield (pounds per square mile) were calculated by dividing each event's sediment and phosphorus loads (tons and pounds, respectively) by the area of the watershed in which the event occured (areas are measured in square miles). the yield was used instead of the load because yields are comparable between watersheds of different sizes. Similarly, in order to compare differently-sized streams, each event's antecedent baseflow was transformed into an antecedent baseflow quantile. This quantile is the proportion of the events in the same stream with a smaller antecedent baseflow.

Exploratory Analysis The first task was to determine how loads are distributed between snowmelt-driven and rainfall-driven events. The total loads from each kind of event are tabulated in Table ??. Figure 1 presents the same information as the tables, while Figure 2 also compares the load from indivudual snowmelt- and rainfall-driven events. In general, more of the load of both phosphorus and sediment is from rainfall-driven events, but at Garfoot and Kuenster more of the both kinds of load came from snowmelt-driven events. At all sites except Garfoot and Kuenster, snowmelt-driven events contributed a larger proportion of phosphorus loading than of sediment loading (and at Garfoot and Kuenster, difference between the proportion was small.) At most sites the difference between the proportion of sediment load produced by snowmelt-driven events and the proportion of phosphorus load produced by snowmelt-driven events was less than ten percentage points, but at Bower the difference was about 34 percentage points. This suggests that melting snow carries proportionally more phosphorus than does rainfall-runoff, which might be the case if the the phosphorus is from animal poop that accumulates on fallen snow, while the sediment comes from dirt that is mainly trapped under the snowpack.

**Rainfall-driven events** We investigated dividing the snow-free seasons into early and late subseasons, separating the two on May 15th of each year. If vegetation serves to hold the soil together, and to increase both evapotranspiration and infiltration, then erosion may be more common early in the spring before most of the summer's vegetation appears. If so, the relationship between rainfall and the stream's loading might change during the summer.

The investigation was done by making linear models to describe the sediment and phosphorus loading during the two subseasons and comparing them to a single model fit to the entire snow-free period. Because the split makes the model more flexible, it will certainly improve the model's fit - the question is whether that improvement is enough to justify making the model more complex. At all four streams, the model improvement was statistically significant but too small to matter (the split models explained about 1%-2% more of the loads). We will not use the split in the rest of the analysis.

Snowmelt-driven events Since sediment and phosphorus are carried into streams by runoff, it makes intuitive sense that the amount of loading during an event should depend on the amount of runoff during that event. In the case of rainfall-driven loading events, it is straightforward to use rain gauges to measure the amount of water entering the stream system. In the case of snowmelt-driven loading events, though, it is not easy to measure how much water melts out of the snowpack, especially when there is also additional snow falling at the same time. There is a subset of events for which we are able to estimate the amount of melting water: Those are the events when we have a measurement of the snow's water content and of the snow depth both before and after the event, and no additional snow falls during the event.

	Sediment		Phosphorus	
	snowmelt-driven	rainfall-driven	snowmelt-driven	rainfall-driven
Eagle	26%	74%	31%	69%
Joos	26%	74%	35%	65%
Otter	31%	69%	42%	58%
Brewery	32%	68%	49%	51%
Garfoot	55%	45%	54%	46%
Kuenster	68%	32%	61%	39%
Rattlesnake	49%	51%	53%	47%
Bower	29%	71%	62%	38%

Table 1 – Proportion of total loading contributed by each type of event

Major events Over the course of the monitoring period, the majority of the total load (both of sediment and of phosphorus) was carried during just a few major events. Just 10% of the events carried between 73.1% (at Otter) and 97.1% (at Bower) of the total sediment load; the same events produced between 64.6% (at Otter) and 88% (at Joos) of the total phosphorus load.

	sediment	phosphorus
eagle	89%	84%
joosvalley	93%	88%
otter	73%	65%
brewery	90%	86%
garfoot	74%	68%
kuenster	94%	82%
rattlesnake	93%	82%
bower	97%	83%

Table 2 – Percentage of loading that comes from the biggest ten percent of events at each site.

## 3 Analysis

### 3.1 Variable selection

In order to make a model of the load carried by the stream, we need to select the predictor variables that have explanatory power. We used stepwise regression with the Bayesian Information Criterion (BIC) to screen the potential predictor variables. We begin the selection with an intercept-only model, and at each step we add or remove one variable. The variable that is added or removed is the one whose addition or removal will do the most to reduce the BIC. If no such variable is found, then selection is considered complete.

**Rainfall-driven events** The predictors that survived the screening at each stream are listed in Table 7. The variables are listed in the order of their importance to the model.

In each case, the two most important predictors are the theisen rainfall and the antecedent baseflow. Using just those two predictors results in an  $R^2$  greater than 0.7 in most models (see Tables 3 and 4.) Since the antecedent baseflow is considered an indicator of how much water is in the watershed before each event, we conclude that the amount of sediment and phosphorus washed into a stream by each event is mainly a function of the quantity of water moving through the system. At Brewery Creek, the intensity of rainfall is a more important predictor than the total quantity of rain.

The performance of the global (aggregate) model is quite good: with just two predictors (sediment: theisen, antecedent\_qbase\_quantile) the  $R^2$  is 0.68 and 0.61, respectively. In the case of sediment, the next-most-important predictor is the stream slope. Including it in the model pushes the  $R^2$  to 0.61.

Snowmelt-driven events We had less success modeling the loading produced by the snowmelt-driven events. The predictors that survived the screening process were different from stream to stream and those variables that did survive at most sites weren't always selected in the same order (like they were for the rainfall-driven events). What's more, the models for snowmelt-driven events were less accurate than for rainfall-driven events, ranging in  $R^2$  from 0.24 to 0.53, with most in the 0.45 range.

At most sites, the most important predictor was a temperature measurement, either the maximum or the mean temperature during the loading event. The antecedent baseflow also appears to be important at most sites. It seems likely that, as in the case of rainfall-driven events, the loading is driven by the quantity of water that moves through the watershed during the event.

## 4 Conclusions

We have an accurate global model that describes the loading that will result from a rainstorm, based just on the base flow before the storm and on the amount of rain that falls during the storm. Antecedent base flow is a measurement of how much water is in the watershed before a storm and any new water comes as rainfall, so it seems that the sediment and phosphorus loads are driven mainly by the quantity of water moving through the watershed. The stream slope also seems to be important; that could be because steeper slopes give surface water less time to infiltrate and therefore increase the intensity of a rainfall event.

We have not yet found an accurate way to model the amount of load during a snowmelt-driven event but we have seen that the air temperature (which drives snowmelt), the antecedent base flow, and the amount of additional precipitation are important predictors for those events.

Most of the annual loading seems to be produced by a few major events. If the goal is to reduce the impact of sediment and phosphorus loading on stream health, then something must be done to mitigate the impact of those major events. Figures ?? and ?? make it look like the majority of the ranfall-driven loading comes from storms that drop at least two inches of rain. Mitigating the effect of large storms will probably require slowing the water's movement through the watershed for instance, by impounding runoff before it can flow into the creeks. A further analysis should look at the frequency of big storms in order to get an idea of how quickly impounded water must be dealt with in order to be ready for the next event.

### References

 M.E. Danz, S.R. Corsi, D.J. Graczyk, and R.T. Bannerman. Characterization of suspended solids and total phosphorus loadings from small watersheds in wisconsin. Scientific Investigations Report 2010-5039, United States Geological Survey, 2010.

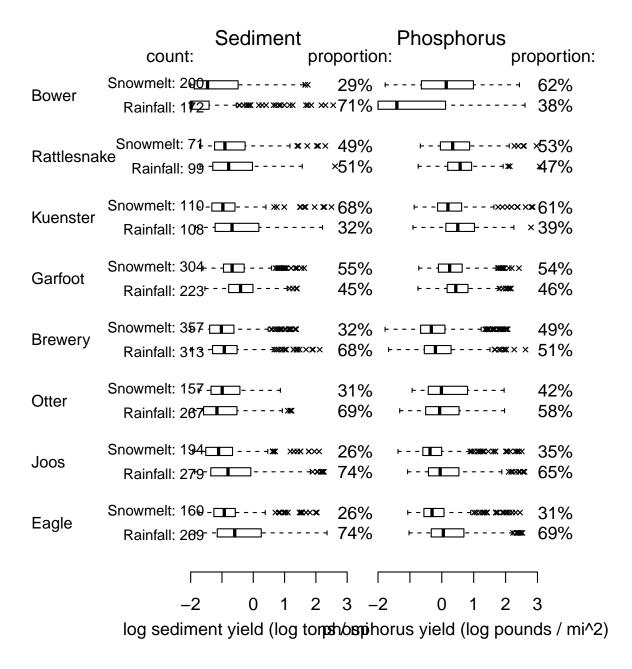


FIGURE 2 – Boxplots showing the sediment and phosphorus load produced by individual events at all four streams.





```
Sediment
                R^2
                      Model terms
              0.481
                      theisen
              0.763
                      theisen + antecedent_qbase_quantile
              0.775
                      theisen + antecedent_qbase_quantile + p30max
Eagle
               0.78
                      theisen + antecedent_qbase_quantile + p30max + duration
              0.785
                      theisen + antecedent_qbase_quantile + p30max + duration + tmin
              0.788
                      theisen + antecedent_qbase_quantile + p30max + duration + tmin + p15max
              0.483
                      theisen
                      the isen + antecedent\_qbase\_quantile
              0.711
              0.733
Joos
                      theisen + antecedent_qbase_quantile + p15max
              0.739
                      theisen + antecedent_qbase_quantile + p15max + ap_3day
                      theisen
              0.447
                      the isen \,+\, antecedent\_qbase\_quantile
              0.782
Otter
              0.792
                      theisen + antecedent\_qbase\_quantile + ap\_1day
                      theisen + antecedent_qbase_quantile + ap_1day + antecedent_tmean
              0.798
              0.484
                      theisen
              0.717
                      theisen + antecedent_qbase_quantile
                      theisen + antecedent_qbase_quantile + p10max
Brewery
              0.734
               0.74
                      theisen + antecedent_qbase_quantile + p10max + antecedent_tmax
              0.448
                      theisen
              0.674
                      the isen + antecedent\_qbase\_quantile
Garfoot
              0.682
                      theisen + antecedent_qbase_quantile + ap_3day
              0.697
                      theisen + antecedent_qbase_quantile + ap_3day + nws_prec
              0.411
Kuenster
              0.768
                      theisen + antecedent_qbase_quantile
              0.485
                      antecedent_qbase_quantile
              0.761
                      antecedent\_qbase\_quantile + theisen
Rattlesnake
               0.78
                      antecedent\_qbase\_quantile + the isen + ap\_5 day
               0.36
                      antecedent_qbase_quantile
              0.741
                      antecedent\_qbase\_quantile + theisen
Bower
              0.748
                      antecedent_qbase_quantile + theisen + ap_5day
              0.399
                      theisen
               0.68
                      theisen + antecedent_qbase_quantile
              0.698
                      theisen + antecedent\_qbase\_quantile + slope
              0.703
                      theisen + antecedent_qbase_quantile + slope + p30max
              0.712
                      theisen + antecedent_qbase_quantile + slope + p30max + ei
Aggregate
              0.717
                      theisen + antecedent_qbase_quantile + slope + p30max + ei + p15max
              0.719
                      theisen + antecedent_qbase_quantile + slope + p30max + ei + p15max + num_events
              0.723
                      theisen + antecedent_qbase_quantile + slope + p30max + ei + p15max + num_events + tmin
                      the isen + antecedent\_qbase\_quantile + slope + p30max + ei + p15max + num\_events + tmin + p5max
              0.724
```

Table 3 – Results of variable selection for a model of sediment yield (tons/mi<sup>2</sup>) from rainfall-driven events

Phosphorus	$\mathbb{R}^2$	Model terms
	0.542	theisen
Eagle	0.759	theisen $+$ antecedent_qbase_quantile
	0.77	theisen $+$ antecedent_qbase_quantile $+$ p30max
Lagio	0.776	theisen + antecedent_qbase_quantile + p30max + tmin
	0.78	theisen $+$ antecedent_qbase_quantile $+$ p30max $+$ tmin $+$ p15max
	0.525	theisen
	0.525 $0.735$	theisen + antecedent_qbase_quantile
	0.733 $0.748$	theisen + antecedent_qbase_quantile + p15max
Joos	0.757	theisen + antecedent_qbase_quantile + p15max + ap_3day
	0.762	theisen + antecedent_qbase_quantile + p15max + ap_3day + antecedent_tmax
	002	theben   ancested and a special   appealing   ancested and a special
	0.43	theisen
_	0.789	theisen + antecedent_qbase_quantile
Otter	0.797	theisen + antecedent_qbase_quantile + cos_julian
	0.802	theisen $+$ antecedent_qbase_quantile $+$ cos_julian $+$ ap_1day
	0.596	theisen
D	0.756	theisen + antecedent_qbase_quantile
Brewery	0.767	theisen + antecedent_qbase_quantile + ap_3day
	0.541	theisen
	0.669	theisen + antecedent_qbase_quantile
Garfoot	0.7	theisen + antecedent_qbase_quantile + nws_prec
	0.713	theisen + antecedent_qbase_quantile + nws_prec + ap_5day
	0.439	theisen
Kuenster	0.756	theisen $+$ antecedent_qbase_quantile
Ruenstei	0.789	theisen $+$ antecedent_qbase_quantile $+$ ap_3day
	0.372	theisen
	0.613	theisen + antecedent_qbase_quantile
Rattlesnake	0.67	theisen + antecedent_qbase_quantile + ap_5day
	0.00	
	0.53	antecedent_qbase_quantile
	0.761	antecedent_qbase_quantile + nws_prec
D.	0.791	antecedent_qbase_quantile + nws_prec + theisen
Bower	0.816	antecedent_qbase_quantile + nws_prec + theisen + tmin
	0.825	antecedent_qbase_quantile + nws_prec + theisen + tmin + tmean
	0.83	antecedent_qbase_quantile $+$ nws_prec $+$ theisen $+$ tmin $+$ tmean $+$ ap_5day
	0.382	theisen
	0.609	theisen $+$ antecedent_qbase_quantile
	0.612	theisen $+$ antecedent_qbase_quantile $+$ tmin
	0.621	theisen + antecedent_qbase_quantile + tmin + tmax
Aggregate	0.627	theisen + antecedent_qbase_quantile + tmin + tmax + p15max
	0.636	theisen + antecedent_qbase_quantile + tmin + tmax + p15max + ei
	0.638	theisen + antecedent_qbase_quantile + tmin + tmax + p15max + ei + slope
	0.64	theisen $+$ antecedent_qbase_quantile $+$ tmin $+$ tmax $+$ p15max $+$ ei $+$ slope $+$ p30max

Table 4 – Results of variable selection for a model of phosphorus yield (pounds/mi<sup>2</sup>) from rainfall-driven events

Sediment	$\mathbb{R}^2$	Model terms
	0.296	tmax
Eagle	0.383	$tmax + antecedent\_qbase\_quantile$
	0.228	tmax
	0.259	$tmax + nws\_prec$
Joos	0.368	$tmax + nws\_prec + num\_days$
	0.487	$tmax + nws\_prec + num\_days + antecedent\_qbase\_quantile$
	0.278	tmax
	0.299	tmax + antecedent_qbase_quantile
Otter	0.556	$tmax + antecedent\_qbase\_quantile + total\_water$
	0.606	$tmax + antecedent\_qbase\_quantile + total\_water + sin\_julian$
	0.323	antecedent_qbase_quantile
Duomoni	0.472	antecedent_qbase_quantile + num_days
Brewery	0.48	$antecedent\_qbase\_quantile + num\_days + tmax$
	0.277	num_days
	0.448	num_days + antecedent_qbase_quantile
Garfoot	0.589	num_days + antecedent_qbase_quantile + total_water
Garioot	0.629	$num\_days + antecedent\_qbase\_quantile + total\_water + nws\_snow$
	0.646	$num\_days + antecedent\_qbase\_quantile + total\_water + nws\_snow + nws\_prec$
	0.467	$\mathrm{melt\_water}$
Kuenster	0.573	$melt\_water + num\_days$
Kuenster	0.695	$melt\_water + num\_days + sin\_julian$
	0.185	num_days
Rattlesnake	0.193	$num_days + antecedent_tmax$
nattiesiiake	0.193	$num\_days + antecedent\_tmax + cos\_julian$
	0.46	total_water
	0.504	$total\_water + nws\_snow$
	0.562	$total\_water + nws\_snow + antecedent\_tmean$
Bower	0.633	$total\_water + nws\_snow + antecedent\_tmean + num\_days$
	0.687	$total\_water + nws\_snow + antecedent\_tmean + num\_days + nws\_prec$
	0.726	$total\_water + nws\_snow + antecedent\_tmean + num\_days + nws\_prec + antecedent\_qbase\_quantile$
	0.138	tmax
	0.218	$tmax + antecedent\_qbase\_quantile$
	0.311	$tmax + antecedent\_qbase\_quantile + num\_days$
Aggregate	0.37	tmax + antecedent_qbase_quantile + num_days + nws_prec
00 -0	0.39	tmax + antecedent_qbase_quantile + num_days + nws_prec + slope
	0.416	tmax + antecedent_qbase_quantile + num_days + nws_prec + slope + nws_snow
	0.425	$tmax + antecedent\_qbase\_quantile + num\_days + nws\_prec + slope + nws\_snow + sin\_julian$

Table 5 – Results of variable selection for a model of sediment yield (tons/mi<sup>2</sup>) from snowmelt-driven events.

Phosphorus	$R^2$	Model terms
Forlo	0.338	tmax
Eagle	0.41	tmax + antecedent_qbase_quantile
	0.237	tmax
	0.281	$tmax + nws\_prec$
Joos	0.328	tmax + nws_prec + antecedent_qbase_quantile
	0.48	tmax + nws_prec + antecedent_qbase_quantile + num_days
	0.32	tmax
	0.37	tmax + antecedent_qbase_quantile
Otter	0.616	$tmax + antecedent\_qbase\_quantile + total\_water$
	0.658	$tmax + antecedent\_qbase\_quantile + total\_water + sin\_julian$
	0.16	num_days
	0.256	num_days + sin_julian
Brewery	0.345	num_days + sin_julian + antecedent_qbase_quantile
Ç .	0.357	$num\_days + sin\_julian + antecedent\_qbase\_quantile + tmax$
	0.996	num dana
	0.236 $0.391$	num_days num_days + total_water
	0.391 $0.449$	num_days + total_water + sin_julian
Garfoot	0.489	num_days + total_water + sin_julian + antecedent_qbase_quantile
	0.53	num_days + total_water + sin_julian + antecedent_qbase_quantile + nws_snow
	0.564	$num\_days + total\_water + sin\_julian + antecedent\_qbase\_quantile + nws\_snow + melt\_water$
	0.553	total_water
	0.668	total_water + nws_snow
	0.704	total_water + nws_snow + sin_julian
Kuenster	0.77	total_water + nws_snow + sin_julian + num_days
	0.81	$total\_water + nws\_snow + sin\_julian + num\_days + tmin$
	0.868	$total\_water + nws\_snow + sin\_julian + num\_days + tmin + tmean$
	0.239	num_days
	0.255	num_days + antecedent_tmax
Rattlesnake	0.251	$num\_days + antecedent\_tmax + cos\_julian$
	0.394	total_water
	$0.568 \\ 0.672$	total_water + antecedent_qbase_quantile total_water + antecedent_qbase_quantile + num_days
Bower	0.756	total_water + antecedent_qbase_quantile + num_days + antecedent_tmean
	0.778	total_water + antecedent_qbase_quantile + num_days + antecedent_tmean + nws_snow
	0.100	
	0.166	tmax
	0.258 $0.34$	tmax + antecedent_qbase_quantile tmax + antecedent_qbase_quantile + num_days
Aggregate	0.397	tmax + antecedent_qbase_quantile + num_days + nws_prec  tmax + antecedent_qbase_quantile + num_days + nws_prec
00 0	0.411	tmax + antecedent_qbase_quantile + num_days + nws_prec + sin_julian
	0.431	$tmax + antecedent\_qbase\_quantile + num\_days + nws\_prec + sin\_julian + nws\_snow$

 $TABLE\ 6-Results\ of\ variable\ selection\ for\ a\ model\ of\ phosphorus\ yield\ (pounds/mi^2)\ from\ snowmelt-driven\ events.$ 

#### Solids

Eagle: theisen, antecedent\_qbase\_quantile, p30max, duration, tmin, p15max

Joos: theisen, antecedent\_qbase\_quantile, p15max, ap\_3day

Otter: theisen, antecedent\_qbase\_quantile, ap\_1day, antecedent\_tmean theisen, antecedent\_qbase\_quantile, p10max, antecedent\_tmax

Garfoot: theisen, antecedent\_qbase\_quantile, ap\_3day, nws\_prec

Kuenster: theisen, antecedent\_qbase\_quantile

Rattlesnake: antecedent\_qbase\_quantile, theisen, ap\_5day
Bower: antecedent\_qbase\_quantile, theisen, ap\_5day

Aggregate: theisen, antecedent\_qbase\_quantile, slope, p30max, ei, p15max, num\_events, tmin, p5max

#### Phosphorus

Eagle: theisen, antecedent\_qbase\_quantile, p30max, tmin, p15max

Joos: theisen, antecedent\_gbase\_quantile, p15max, ap\_3day, antecedent\_tmax

Otter: theisen, antecedent\_qbase\_quantile, cos\_julian, ap\_1day

Brewery: theisen, antecedent\_qbase\_quantile, ap\_3day

Garfoot: theisen, antecedent\_qbase\_quantile, nws\_prec, ap\_5day

Kuenster: theisen, antecedent\_qbase\_quantile, ap\_3day Rattlenake: theisen, antecedent\_qbase\_quantile, ap\_5day

Bower: antecedent\_qbase\_quantile, nws\_prec, theisen, tmin, tmean, ap\_5day
Aggregate: theisen, antecedent\_qbase\_quantile, tmin, tmax, p15max, ei, slope, p30max

TABLE 7 – The most important variables in the models for rainfall-driven loading. The variables are ordered by their importance to the model of the yield.

#### **Solids**

Eagle: tmax, antecedent\_qbase\_quantile

Joos: tmax, nws\_prec, num\_days, antecedent\_qbase\_quantile
Otter: tmax, antecedent\_qbase\_quantile, total\_water, sin\_julian

Brewery: antecedent\_gbase\_quantile, num\_days, tmax

Garfoot: num\_days, antecedent\_qbase\_quantile, total\_water, nws\_snow, nws\_prec

 $\begin{tabular}{lll} Kuenster: & melt\_water, num\_days, sin\_julian \\ Rattlesnake: & num\_days, antecedent\_tmax, cos\_julian \\ \end{tabular}$ 

Bower: total\_water, nws\_snow, antecedent\_tmean, num\_days, nws\_prec, antecedent\_qbase\_quantile

Aggregate: tmax, antecedent\_qbase\_quantile, num\_days, nws\_prec, slope, nws\_snow, sin\_julian

### Phosphorus

Eagle: tmax, antecedent\_qbase\_quantile

Joos: tmax, nws\_prec, antecedent\_qbase\_quantile, num\_days
Otter: tmax, antecedent\_qbase\_quantile, total\_water, sin\_julian
Brewery: num\_days, sin\_julian, antecedent\_qbase\_quantile, tmax

 $Garfoot: \qquad \quad num\_days, \ total\_water, \ sin\_julian, \ antecedent\_qbase\_quantile, \ nws\_snow, \ melt\_water$ 

Kuenster: total\_water, nws\_snow, sin\_julian, num\_days, tmin, tmean

 $Rattlesnake: \quad num\_days, \ antecedent\_tmax, \ cos\_julian$ 

 $\begin{tabular}{ll} Bower: & total\_water, antecedent\_qbase\_quantile, num\_days, antecedent\_tmean, nws\_snow \\ Aggregate: & tmax, antecedent\_qbase\_quantile, num\_days, nws\_prec, sin\_julian, nws\_snow \\ \end{tabular}$ 

TABLE 8 – The most important variables in the models for snowmelt-driven loading. The variables are ordered by their importance to the model of the yield.

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-2.3514	0.0341	-68.98	0.0000
theisen	0.6776	0.0149	45.56	0.0000
antecedent_qbase_quantile	1.6064	0.0423	37.99	0.0000
slope	0.0049	0.0005	10.07	0.0000

TABLE 9 – Summary table for of model for log(sediment yield) during the rainfall period.

	Estimate	Std. Error	t value	$\Pr(> t )$
(Intercept)	-1.1976	0.0310	-38.63	0.0000
theisen	0.6858	0.0177	38.72	0.0000
$antecedent\_qbase\_quantile$	1.4592	0.0472	30.89	0.0000

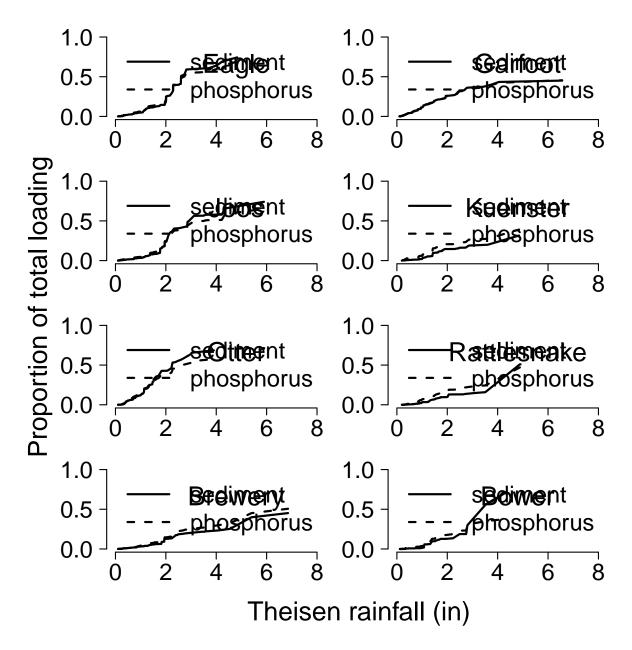
Table 10 – Summary table for of model for log(phosphorus yield) during the rainfall period.

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-2.3158	0.0641	-36.14	0.0000
$\operatorname{tmax}$	0.0115	0.0014	8.01	0.0000
antecedent_qbase_quantile	0.8894	0.0602	14.77	0.0000
$num\_days$	0.1229	0.0096	12.79	0.0000
nws_prec	0.4522	0.0376	12.01	0.0000

Table 11 - Summary table for of model for  $log(sediment\ yield)$  during the snowmelt period.

	Estimate	Std. Error	t value	$\Pr(> t )$
(Intercept)	-1.5140	0.0640	-23.65	0.0000
$\operatorname{tmax}$	0.0142	0.0014	9.83	0.0000
antecedent_qbase_quantile	0.9487	0.0605	15.69	0.0000
$num\_days$	0.1154	0.0096	12.06	0.0000
nws_prec	0.4447	0.0375	11.85	0.0000

Table 12 – Summary table for of model for  $log(phosphorus\ yield)$  during the snowmelt period.



 $\label{eq:figure 5-Proportion} Figure \ 5-Proportion \ of the total load contributed by rainfall events up to the size shown. Snowmelt-driven events are excluded.$ 

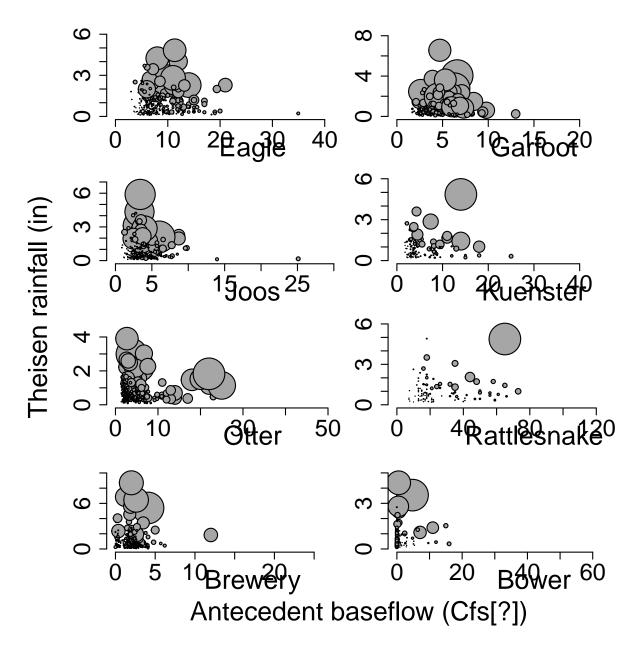


FIGURE 6 – Antecedent base flow is the horizontal axis; theisen rainfall is the vertical axis. Each dot represents one event. The size of the dot shows the total sediment load (in tons) contributed by that event.

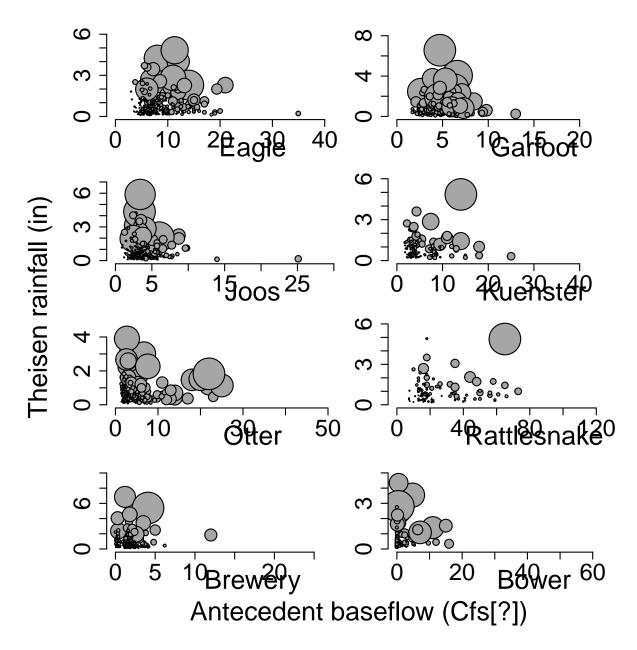


FIGURE 7 – Antecedent base flow is the horizontal axis; theisen rainfall is the vertical axis. Each dot represents one event. The size of the dot shows the total phosphorus load (in pounds) contributed by that event.