

## 4 Symmetries in Single Diagonalization Approach

For  $J=3/2$ ,  $m=-3,0,3$ :

[illegible]

After unitary transformations:

[illegible]

$A_1$  matrix:

$D_{11} - D_{-11} + F_3$	$\frac{\sqrt{2}D_{01}}{\sqrt{2}D_{01}}$	$\rho_{13}$	$S_{12}$	$S_{11} + S_{-11}$	.	.	.	$\eta_{13}$	.	.
$D_{00} + F_3$	.	.	$-\sqrt{2}S_{02}$	$\sqrt{2}S_{10}$	.	.	.	.	.	.
.	$D_{11} + D_{-11} + F_0$	$-\sqrt{2}V$	.	.	$S_{11} - S_{-11}$	$\sqrt{2}S_{01}$	$S_{12}$	.	.	.
$\rho_{13}$	$-\sqrt{2}V$	$D_{11} + D_{-11} + F_3$	.	$\eta_{13}$	.	.	.	$S_{11} - S_{-11}$	$\sqrt{2}S_{01}$	$S_{12}$
$S_{12}$	$-\sqrt{2}S_{02}$	.	$E_{22} + F_3$	$E_{12}$	.	.	.	.	.	$\rho_{23}$
$S_{11} + S_{-11}$	$\sqrt{2}S_{10}$	$\eta_{13}$	$E_{12}$	$E_{11} + E_{-11} + F_3$	.	.	.	$\rho_{13}$	.	.
.	$S_{11} - S_{-11}$	.	.	.	$E_{11} - E_{-11} + F_0$	$\sqrt{2}E_{01}$	$E_{12}$	$-\sqrt{2}V$	.	.
.	$\sqrt{2}S_{01}$	.	.	.	$\sqrt{2}E_{01}$	$E_{00} + F_0$	$\sqrt{2}E_{02}$	.	$-\sqrt{2}V$	.
.	$S_{12}$	.	.	.	$E_{12}$	$\sqrt{2}E_{02}$	$E_{22} + F_0$	.	.	$-\sqrt{2}V$
$\eta_{13}$	.	$S_{11} - S_{-11}$	.	$\rho_{13}$	$-\sqrt{2}V$	.	.	$E_{11} - E_{-11} + F_3$	$\sqrt{2}E_{01}$	$E_{12}$
.	.	$\sqrt{2}S_{01}$	.	.	.	$-\sqrt{2}V$	.	$\sqrt{2}E_{01}$	$E_{00} + F_3$	$\sqrt{2}E_{02}$
.	.	$S_{12}$	$\rho_{23}$	.	.	.	$-\sqrt{2}V$	$E_{12}$	$\sqrt{2}E_{02}$	$E_{22} + F_3$

$A_2$  matrix:

$D_{11} + D_{-11} + F_3$	.	.	$\rho_{13}$	.	$S_{11} - S_{-11}$	$\sqrt{2}S_{01}$	$S_{12}$	.	.	.	$\eta_{13}$
.	$D_{11} - D_{-11} + F_0$	$\sqrt{2}D_{01}$	$-\sqrt{2}V$	.	.	.	.	$S_{12}$	$S_{11} + S_{-11}$	.	.
.	$\sqrt{2}D_{01}$	$D_{00} + F_0$	$-\sqrt{2}V$	.	.	.	.	$-\sqrt{2}S_{02}$	$\sqrt{2}S_{10}$	.	.
$\rho_{13}$	$-\sqrt{2}V$	.	$D_{11} - D_{-11} + F_3$	$\sqrt{2}D_{01}$	$\eta_{13}$	.	.	.	.	$S_{12}$	$S_{11} + S_{-11}$
.	$-\sqrt{2}V$	.	$\sqrt{2}D_{01}$	$D_{00} + F_3$	.	.	.	.	.	$-\sqrt{2}S_{02}$	$\sqrt{2}S_{10}$
$S_{11} - S_{-11}$	.	.	$\eta_{13}$	.	$E_{11} - E_{-11} + F_3$	$\sqrt{2}E_{01}$	$E_{12}$	.	.	.	.
$\sqrt{2}S_{01}$	.	.	.	.	$\sqrt{2}E_{01}$	$E_{00} + F_3$	$\sqrt{2}E_{02}$	.	.	.	$\rho_{13}$
$S_{12}$	.	.	.	.	$E_{12}$	$\sqrt{2}E_{02}$	$E_{22} + F_3$	.	.	.	.
.	$S_{12}$	$-\sqrt{2}S_{02}$	.	.	.	.	.	$E_{22} + F_0$	$E_{12}$	$-\sqrt{2}V$	.
.	$S_{11} + S_{-11}$	$\sqrt{2}S_{10}$	.	.	.	.	.	$E_{12}$	$E_{11} + E_{-11} + F_0$	.	$-\sqrt{2}V$
$\eta_{13}$	.	.	$S_{12}$	$-\sqrt{2}S_{02}$	.	.	$\rho_{23}$	$-\sqrt{2}V$	.	$E_{22} + F_3$	$E_{12}$
.	.	.	$S_{11} + S_{-11}$	$\sqrt{2}S_{10}$	$\rho_{13}$	.	.	.	$-\sqrt{2}V$	$E_{12}$	$E_{11} + E_{-11} + F_3$