An Introduction to HPC and Scientific Computing

Lecture six: How to multi-task on CPUs using OpenMP.

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Thanks to Ian Bush for the materials

Oxford e-Research Centre

Overview

In this lecture we will learn about:

- The Basic Idea Behind Parallelism
- What OpenMP is
- How to divide work amongst threads
- How to synchronise threads
- How to go about parallelising a simple program with OpenMP

Parallelism – How to do we split up the work?

Scenario: The application takes too long to run!

Parallel processing can shorten the run-time:

- Parallelism in the workload (in algorithms and data) and

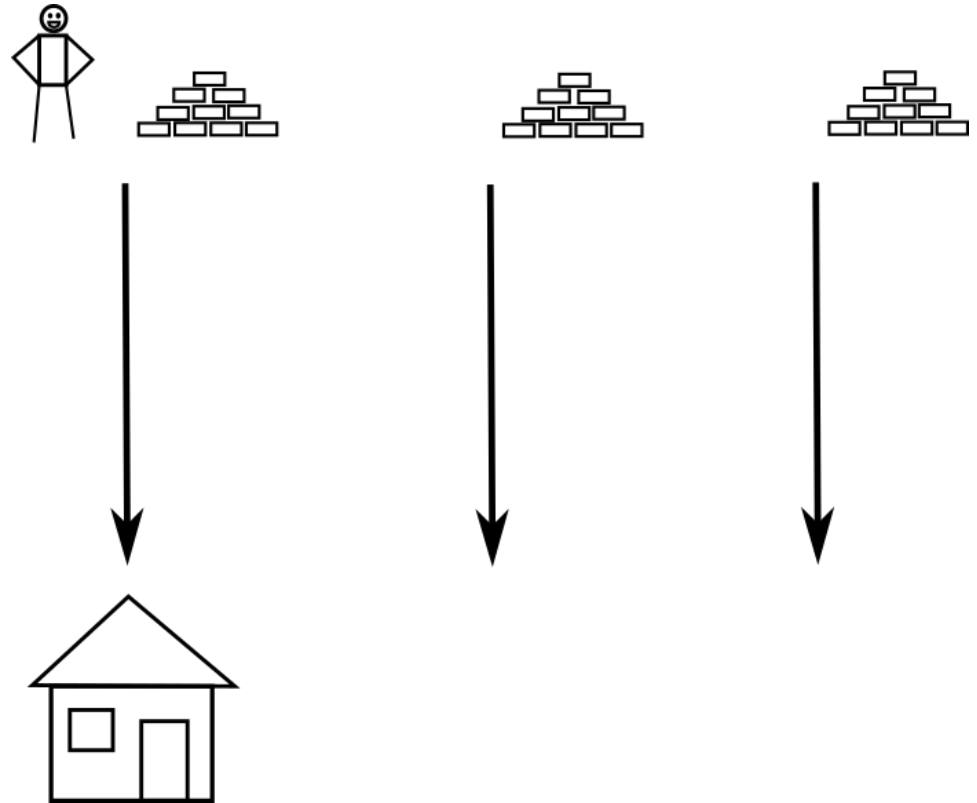- Assign portions of the workload to different workers (processors)

Parallelism – How to do we split up the work?

Analogy:
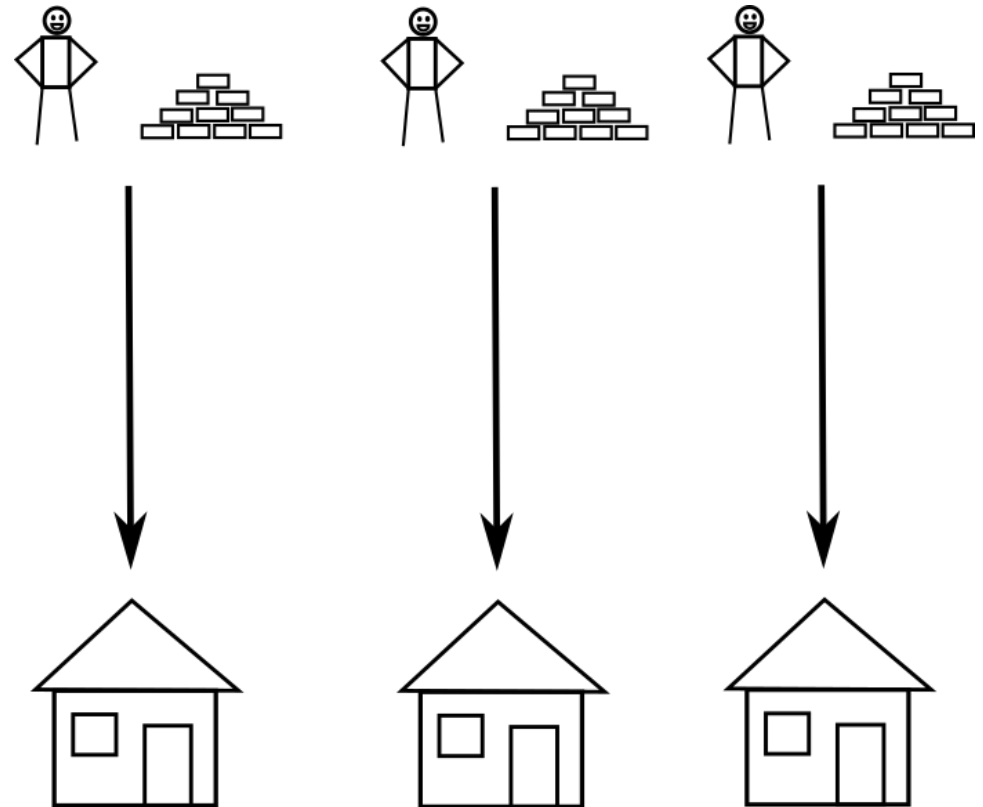Shorten the time it takes to build an entire row of houses by:

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Parallelism – How to do we split up the work?

Analogy:
Shorten the time it takes to build an entire row of houses by:

- dividing the work into parts that can be carried out in parallel and building multiple houses at the same time as one

-

Parallelism – How to do we split up the work?

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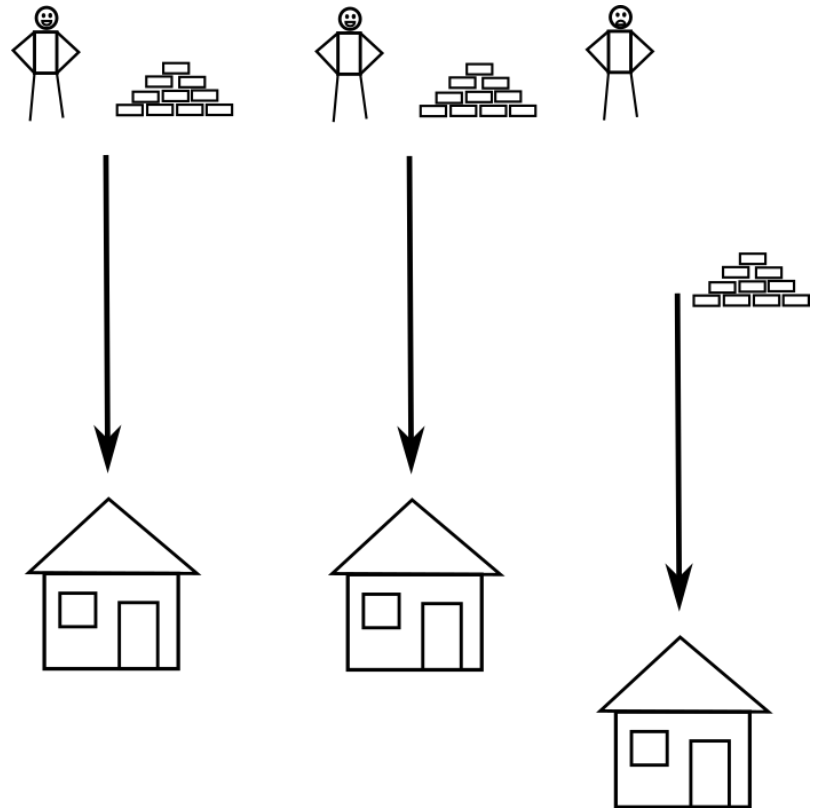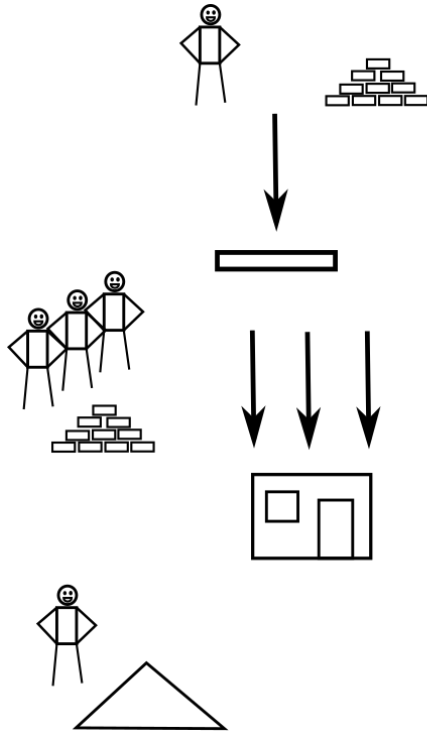
- Oh no! Supply issues!

Parallelism – How to do we split up the work?

Perfect (linear) scaling is the holy grail:

- execution time is inversely proportional with the number of processors

- by analogy: halve the time by using twice the workers

- in practice, scaling is not linear but can be close enough

Parallelism – How to do we split up the work?

Division of work for one house:

- We can divide the work on a single house between teams

- Lay the foundations (one worker)

- Build walls (three workers)
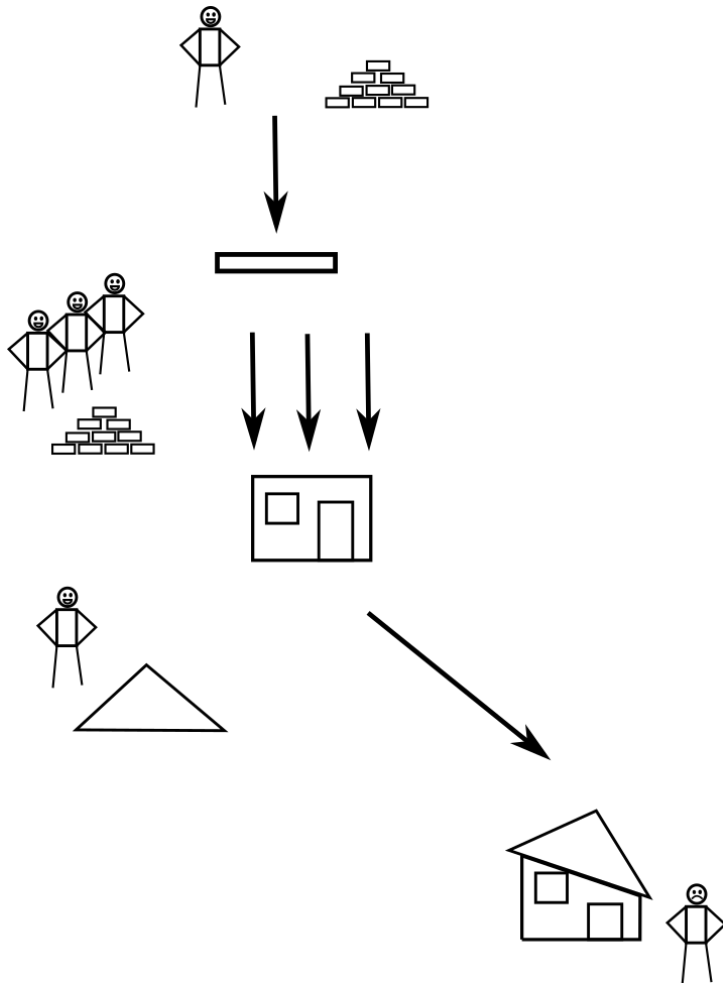
- When to build a roof?

Parallelism – How to do we split up the work?

Division of work for one house:

- We can divide the work on a single house between teams

- Lay the foundations (one worker)

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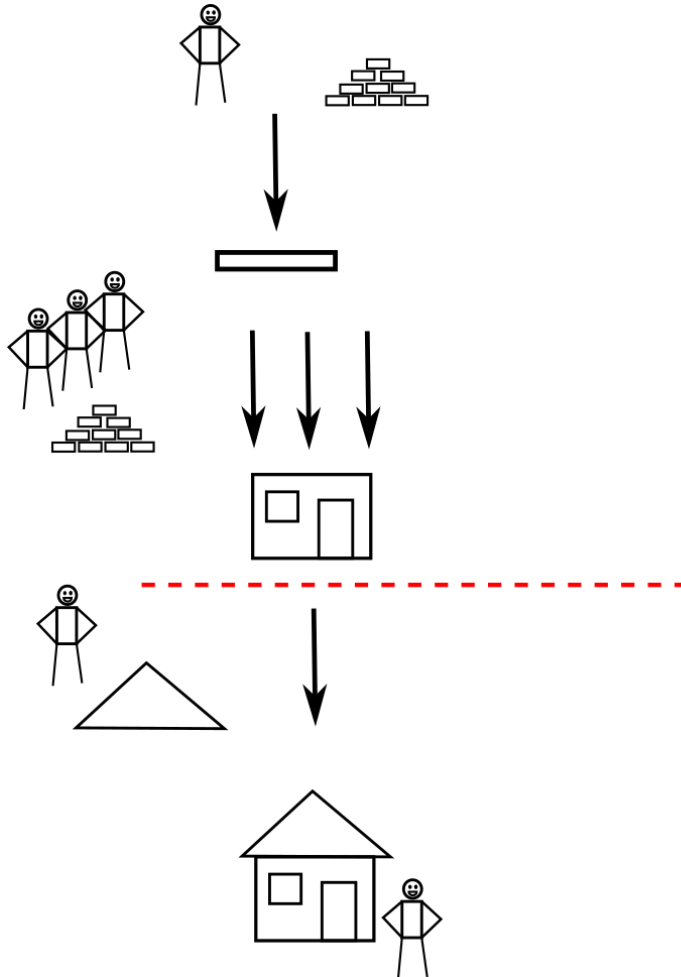- When to build a roof? Whenever we want?

Parallelism – How to do we split up the work?

Division of work for one house:

- We can divide the work on a single house between teams

- Lay the foundations (one worker)

- Build walls (three workers)

- When to build a roof? Whenever we want? NO!

- After walls are build!

Parallelism – A maths example

- Consider adding two vectors:

$$a_i = b_i + c_i$$

- The operations required for each value of *i* are independent of any other value

- Thus for parallelism we require *independent operations*

- We can perform the operations *in any order*

- We also require *independent data*
  - Consider the apparently very similar $a_i = b_i + a_{i-1}$
  - Can't calculate a_i until has been a_{i-1} calculated

Parallelism – Communication and Synchronisation

- Now consider a dot product
$$a = \sum b_i \times c_i$$

- Could give a subset of the indices to each process and form the local contribution to a

- Sum together all the local contributions for final answer

- This last phase requires the processes or threads to work together
  - i.e. they are no longer totally independent
  - They need to communicate with each other
  - If one finishes before the others it will have to wait for them
- Very typical way parallelism work inside real codes
  - Independent iterations
  - Coordinate local results into a global one

Parallel Scaling

- Consider the time to solution for our dot product.
- Vectors of order N
- P threads or processes
- The time to compute the local sum will be proportional to N/P
  - A **decreasing** function of the number of threads
- The time to synchronise is more complicated
  - But it will be an **increasing** function of the number of threads
  - and independent of N
  - A deeper analysis shows a suitable model is log(P)
- Thus our model is:
- $$t(P) = \alpha N/P + \beta \log(P)$$

- Thus parallelism is the most efficient
  - For large N
  - For small P
  - Too many threads may cause your program to slow down!

Measuring Scalability – Speed Up

$S = t(1)/t(P)$
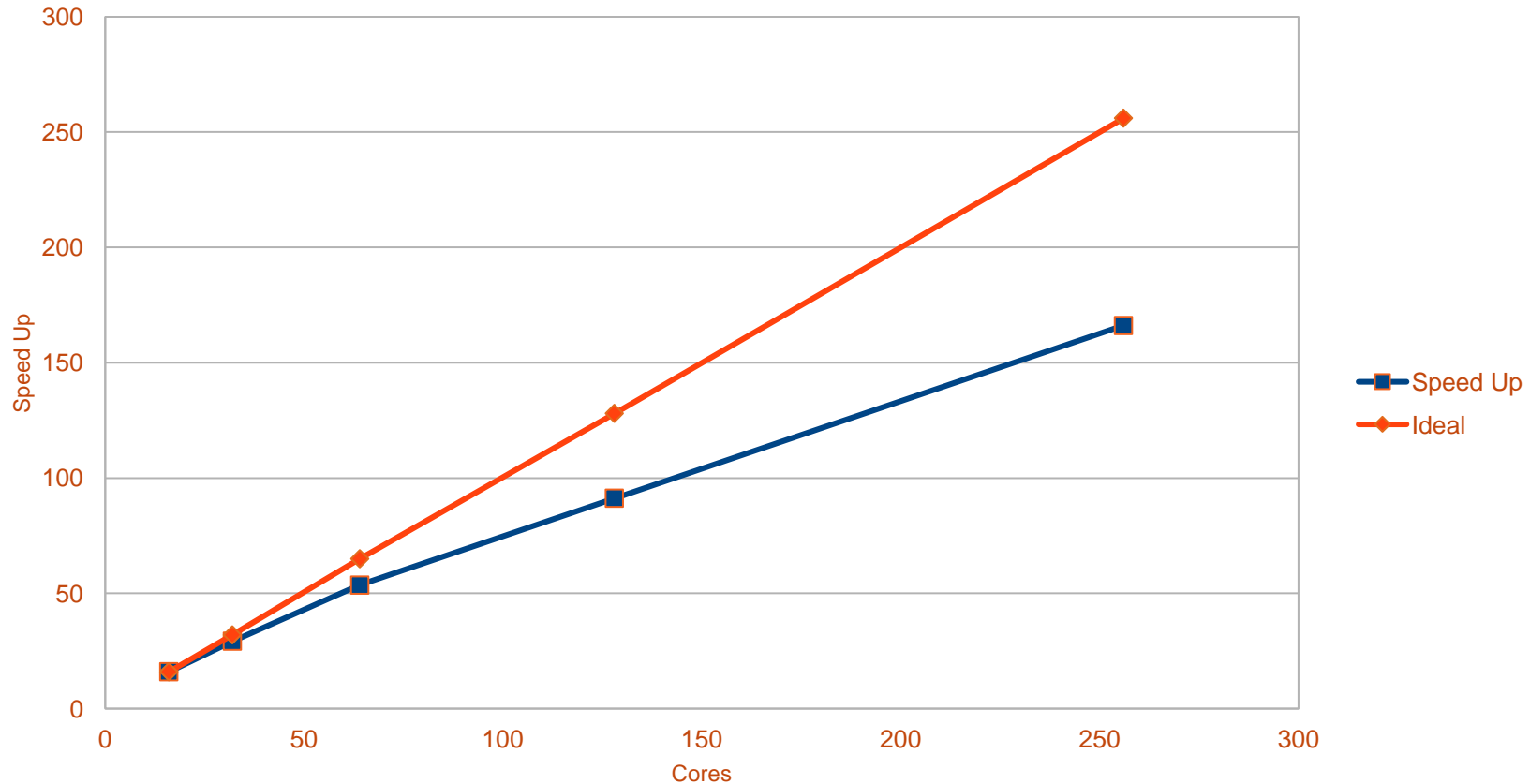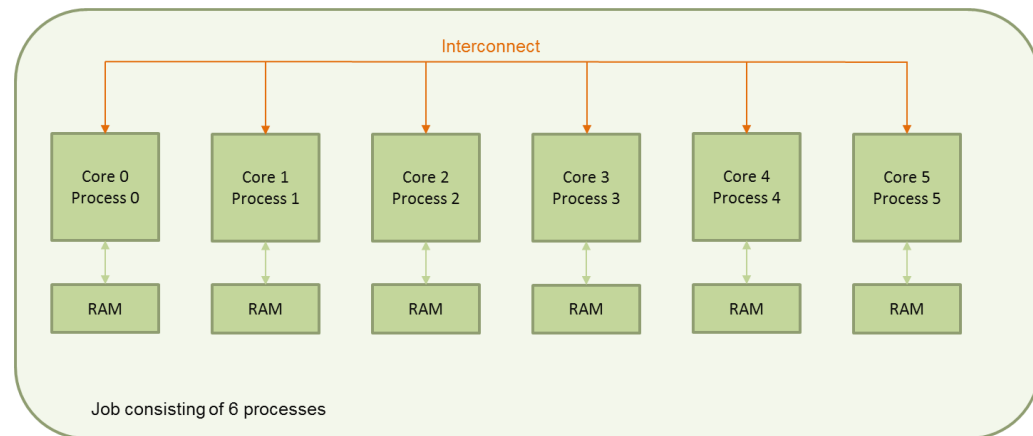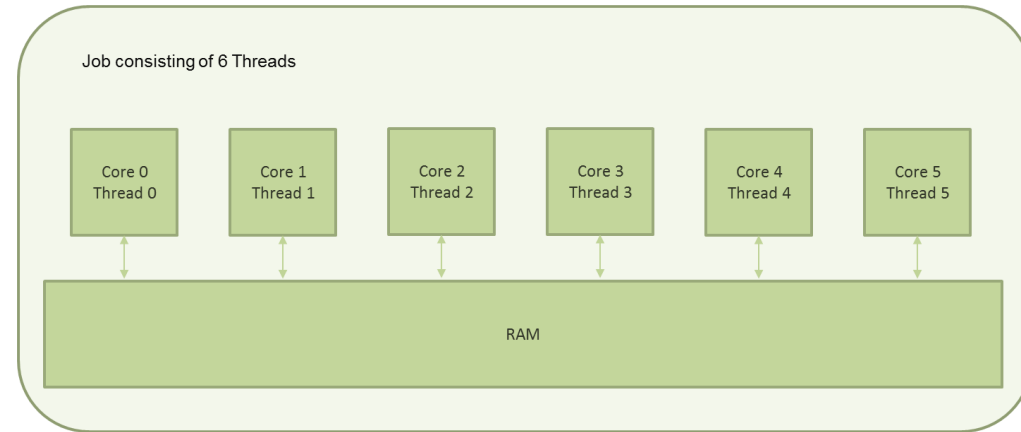
Parallelising Scientific Programs

- **Shared memory programming**
  – Each core can see all of the memory
  – This is generally done via *OpenMP*
 – Generally limited to a single node

- **Distributed memory programming**
  – Each core can only see its memory
  – Have to use the interconnect
  – Can use an unlimited number of cores
  – Generally done via *MPI*
  – We don't cover it here but there are free ARC and ARCHER courses

- Hybrids of the two are possible and are used

Job consisting of 6 Threads

| Core 0 Thread 0 | Core 1 Thread 1 | Core 2 Thread 2 | Core 3 Thread 3 | Core 4 Thread 4 | Core 5 Thread 5 |

RAM

Interconnect

| Core 0 Process 0 | Core 1 Process 1 | Core 2 Process 2 | Core 3 Process 3 | Core 4 Process 4 | Core 5 Process 5 |

| RAM | RAM | RAM | RAM | RAM | RAM |

Job consisting of 6 processes

Shared memory model

- Represents computing on a multi-processor architecture which links multiple (identical) CPUs to a single unified main memory;
- Uses a shared-memory programming model, with data that can be shared between processors
- Also called SMP, Symmetric Multi-Processor systems (for historical reasons)
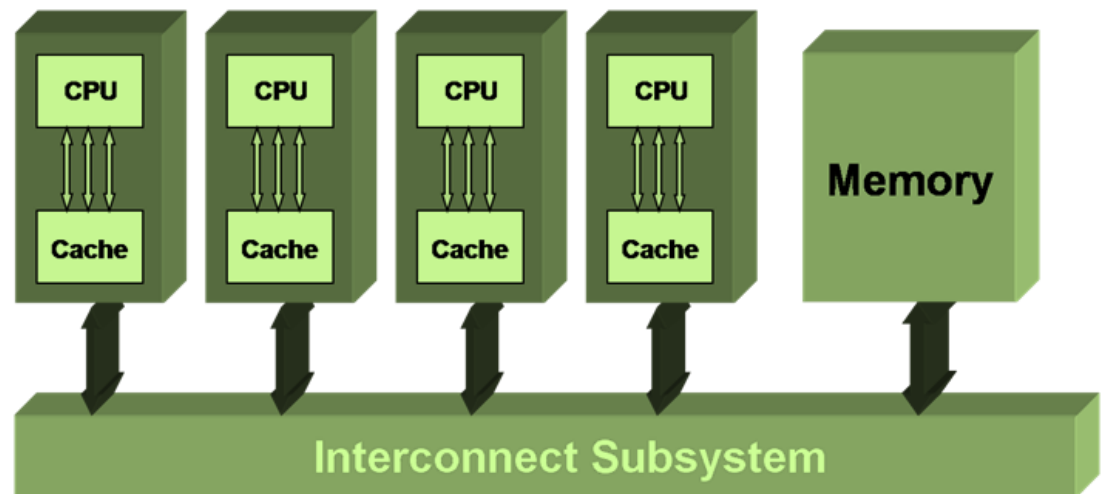
Processes and Threads

In shared-memory computing:

- An "application" is a single process – May be many threads

- The "process" is the "master thread"

- Master thread can spawn/destroy other threads (fork/join strategy)
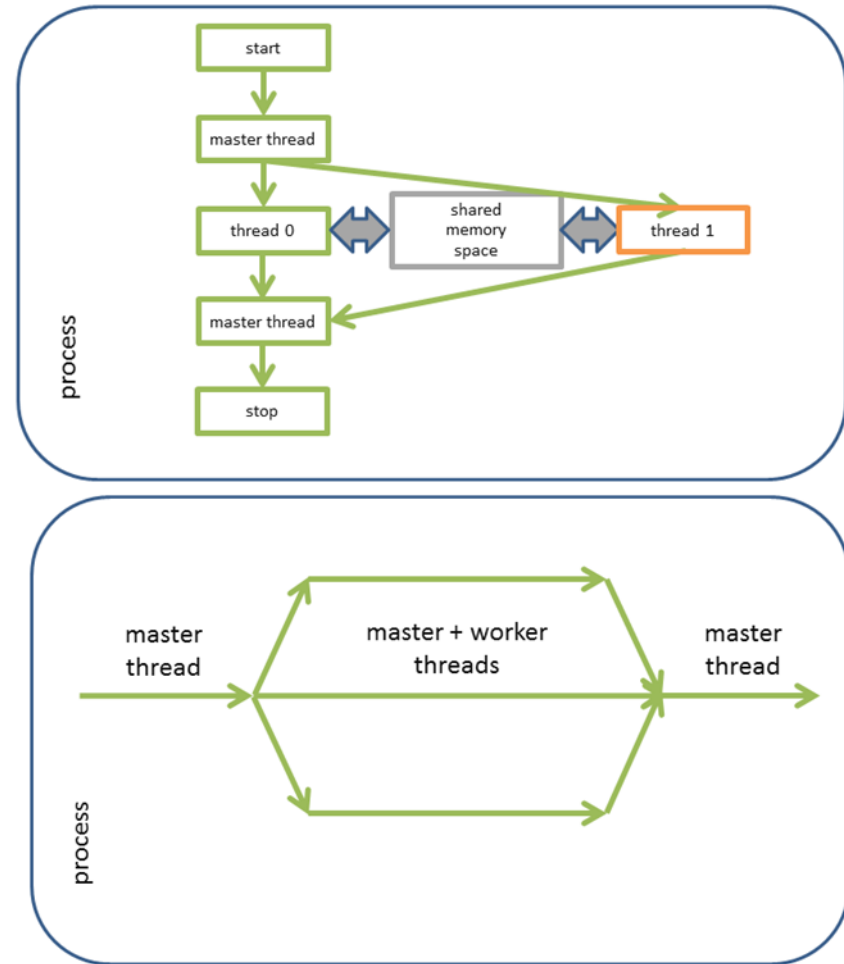
Thread programming

- Explicit, low-level thread programming:
  - start several threads and explicitly tell each what to do
  - tedious, difficult to write and difficult to maintain
  - standards not universal (POSIX pthreads, Windows threads)
  - may be suited to task parallelism

- High-level programming using the OpenMP API:
  - instruct the compiler what can be done in parallel
  - let the compiler do the tedious stuff
  - threads are generated at runtime and scheduled by the OS
  - "standard" supported by a large number of compilers and operating systems
  - by design, suited to data parallelism

OpenMP Status

- OpenMP specification is not a formal standard.

- Version 1.0 (1997)
- Version 2.0 (2002)
- Version 2.5 (2005)
- Version 3.0 (2008)
- Version 3.1 (2011)
- Version 4.0 (2013)
- Version 5.0 (2018)
- Version 5.1 (2020)

It is live and well

The OpenMP API

- OpenMP is
  - An API for portable and scalable shared memory programming
  - Defined and supported by a group of major vendors
  - Supported by most compilers for Fortran, C, C++

- OpenMP programming is
  - Standardised parallelism (fine-grained – loops, coarse-grain – regions)
  - If we're careful, usable serial code

- OpenMP API components:
  - Compiler directives
  - Runtime library routines
  - Environment variables

OpenMP "Hello World" in C

```c
#include <stdio.h>
#include <stdlib.h>
#include "omp.h"

int main( void ) {
  int my_thread;

  /* Scope the variables and create the threads */
  #pragma omp parallel default( none ) private( my_thread )
  {
    my_thread = omp_get_thread_num();
    printf( "Hello from thread %d\n", my_thread );
  }
  return EXIT_SUCCESS;

}
```

OpenMP "Hello World" in C

```
$ gcc -fopenmp -O -std=c89 -Wall -Wextra -pedantic hello.c -o
hello
$ export OMP_NUM_THREADS=5
$ ./hello
Hello from thread 2
Hello from thread 4
Hello from thread 3
Hello from thread 0
Hello from thread 1
$ export OMP_NUM_THREADS=3
$ ./hello
Hello from thread 0
Hello from thread 2
Hello from thread 1
```

Running In Batch

```bash
#!/bin/bash

# set the number of nodes, which is always 1 for OpenMP codes
#SBATCH --nodes=1

# set number of cores per node -- grab the whole node (why?)
#SBATCH --ntasks-per-node=16

# set max wallclock time
#SBATCH --time=00:10:00

# set name of job
#SBATCH --job-name hello

# Set up the software environment
module purge
module load intel-compilers

# set the number of threads we will use
export OMP_NUM_THREADS=5

# run the OpenMP program
./my_prog
```

A More Complex Example

```c
#include <stdlib.h>
#define N 50

int main( void ) {
  double a[ N ], b[ N ], c[ N ];
  int i;
  for( i = 0; i < N; i++ ) {
    b[ i ] = ( (double) rand() ) / RAND_MAX;
    c[ i ] = ( (double) rand() ) / RAND_MAX;
  }

/* Scope the variables for the parallel region and create the
threads */
#pragma omp parallel default( none ) shared( a, b, c ) private( i )
  {
    /* A work sharing directive */
    #pragma omp for
    for( i = 0; i < N; i++ ) {
      a[ i ] = b[ i ] + c [ i ];
    }
  }
  return EXIT_SUCCESS;
}
```

Scoping and Work Sharing

- So there are two main steps

1. Create the threads with a parallel directive and at that point "scope" the variables.
   - `default none` forces you to scope all the variables – USE THIS.
   - Variables can be one of
     - `Shared`   – each thread can access the variable
     - `Private`   – each thread has its own, unique copy
   - Note thread creation is *expensive.*

2. Once the threads are created you split the work up between them with a "work sharing" directive
   - Without a work sharing directive all threads will do exactly the same thing on the same data!
   - You can have as many work sharing constructs as you want within a parallel region
   - As thread creation is expensive exploit this – don't create threads every time you need to share work, reuse the threads as many times as you can!

Problems Of Sharing Data

- Shared variables makes writing parallel code easy
- But what happens if multiple threads are trying to update (the same part of) a shared variable at the same time?
    - The result is not well defined!
    - And will probably vary from run to run!
- This is called a "race condition" and OpenMP does NOTHING by default to protect you from them
- So if multiple threads need to access a shared variable you will need to synchronize the threads somehow
- Rule of thumb: **If a shared variable is on the left hand side of an = sign it is time to stop and think about thread synchronisation**
- Race conditions are very easy to write and very hard to debug! Be careful!
    - To fully cover this subject we need to have discussed the OpenMP memory model, which is well beyond what we have time to cover here.

Synchronising Threads

- So how can we synchronise threads?

- OpenMP provides a number of mechanisms. Here we will cover
  - Barrier: a given thread can only proceed once all threads have reached the barrier
    - **Important**: By default there is an implicit barrier at the end of each worksharing construct

  - Critical region: Only 1 thread can be executing codes within a critical region. All other threads must wait at the start until the thread executing the region has exited it

  - Reduction: Combining multiple private values into a single shared value

Summary: OpenMP Directives So Far

parallel region constructs	blocks of code executed by all threads (most data shared by default)	`#pragma omp parallel (C,C++)` `!$omp parallel (Fortran)` • shared data are visible to all threads • private data is local to thread and invisible outside, created on entry to scope, destroyed on exit
work-sharing constructs (within a parallel region)	parallel DO loops (distribute iterations over active threads)	`#pragma omp for` `!$omp do`
critical section	protects action on the shared variables (only one thread at a time allowed)	`#pragma omp critical` `!$omp critical`
synchronisation	barriers	`#pragma omp barrier` `!$omp barrier` Threads can proceed only after all execute the barrier; implied at end of parallel region and loop (unless overridden by nowait)

Bringing It Together – A More Complex Example

Task:

Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Serial Code

```
z = 0
for i = 1 to n
    z = z + x_i * y_i
end for

for i = 1 to n
  y_i = y_i - z * x_i
end for
```

Bringing It Together – A More Complex Example

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Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Thread 1

```
z = 0
for i = 1 to n/2
    z = z + x_i * y_i
end for


for i = 1 to n/2
  y_i = y_i - z * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for


for i = n/2+1 to n
  y_i = y_i - z * x_i
end for
```

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end for

for i = 1 to n/2
 y_i = y_i - z * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for

for i = n/2+1 to n
 y_i = y_i - z * x_i
end for
```

Problem
i and z are updated by both threads (race condition)

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```
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    z = z + x_i * y_i
end for

for i = 1 to n/2
 y_i = y_i - z * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for

for i = n/2+1 to n
 y_i = y_i - z * x_i
end for
```

Solution
make **i** and **z** private

Bringing It Together – A More Complex Example

Task:

Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Thread 1

```
z = 0
for i = 1 to n/2
    z = z + xᵢ * yᵢ
end for

for i = 1 to n/2
  yᵢ = yᵢ - z * xᵢ
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + xᵢ * yᵢ
end for

for i = n/2+1 to n
  yᵢ = yᵢ - z * xᵢ
end for
```

Problem
z has now different values in the two threads

Bringing It Together – A More Complex Example

Task:

Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Thread 1

```
z = 0
for i = 1 to n/2
    z = z + x_i * y_i
end for
w = w + z
for i = 1 to n/2
  y_i = y_i - w * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for
w = w + z
for i = n/2+1 to n
  y_i = y_i - w * x_i
end for
```

Solution
Make a global **w**
Accumulate **z** in **w**

Bringing It Together – A More Complex Example

Task:
Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Thread 1

```
z = 0
for i = 1 to n/2
    z = z + x_i * y_i
end for
w = w + z
for i = 1 to n/2
  y_i = y_i - w * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for
w = w + z
for i = n/2+1 to n
  y_i = y_i - w * x_i
end for
```

Problem
w may not have the correct value (race condition)

Bringing It Together – A More Complex Example

Task:

Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Thread 1

```
z = 0
for i = 1 to n/2
    z = z + x_i * y_i
end for
[ w = w + z ]
for i = 1 to n/2
  y_i = y_i - w * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for
[ w = w + z ]
for i = n/2+1 to n
  y_i = y_i - w * x_i
end for
```

Solution
Protect […] the update of **w**
(Only one thread at a time)

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end for
[ w = w + z ]
for i = 1 to n/2
  y_i = y_i - w * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for
[ w = w + z ]
for i = n/2+1 to n
  y_i = y_i - w * x_i
end for
```

Problem
A thread may finish before the other has updated **w**

Bringing It Together – A More Complex Example

Task:
Orthogonalise 2 NORMALIZED vectors **x** and **y** on 2 threads.

There are several problems to watch out for.

Thread 1

```
z = 0
for i = 1 to n/2
    z = z + x_i * y_i
end for
[ w = w + z ]
< barrier >
for i = 1 to n/2
 y_i = y_i - w * x_i
end for
```

Thread 2

```
z = 0
for i = n/2+1 to n
    z = z + x_i * y_i
end for
[ w = w + z ]
< barrier >
for i = n/2+1 to n
 y_i = y_i - w * x_i
end for
```

Solution
Synchronise the process (barrier)

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Thread 1

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for i = 1 to n/2
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end for
```

Thread 2

```
z = 0
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    z = z + xᵢ * yᵢ
end for
[ w = w + z ]
< barrier >
for i = n/2+1 to n
 yᵢ = yᵢ - w * xᵢ
end for
```

This now works!

OpenMP program example

Fortran

```
w = 0.0

!OMP PARALLEL SHARED(n,w,x,y), &
!OMP             PRIVATE (i,z)
   z = 0.0
!OMP DO
   DO  i = 1, n
      z = z + x(i)*y(i)
   END DO
!OMP END DO
!OMP CRITICAL
   w = w + z
!OMP END CRITICAL
!OMP BARRIER
!OMP DO
DO  i = 1, n
   y(i) = y(i) - w*x(i)
END DO
!OMP END DO
!END PARALLEL
```

C

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                  private(i,z)
{
   z = 0.0;
   #pragma omp for
   for (i=0; i<n; i++) {
      z = z + x[i]*y[i];
   }
   #pragma omp critical
   {
      w = w + z;
   }
   #pragma omp barrier
   #pragma omp for
   for (i=0; i<n; i++) {
      y(i) = y(i) - w*x(i);
   }
}
```

OpenMP program example

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   for (i=0; i<n; i++) {
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}
```

OpenMP program example

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OpenMP program example

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   {
      w = w + z;
   }

   #pragma omp barrier


   #pragma omp for
   for (i=0; i<n; i++) {
      y[i] = y[i] - w*x[i];
   }
}
```
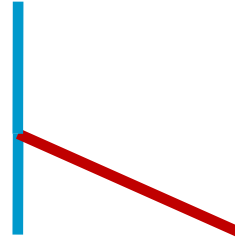
Spawn threads

OpenMP program example

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                      private(i,z)
{
   z = 0.0;

   #pragma omp for
   for (i=0; i<n; i++) {
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   }

   #pragma omp critical
   {
      w = w + z;
   }

   #pragma omp barrier


   #pragma omp for
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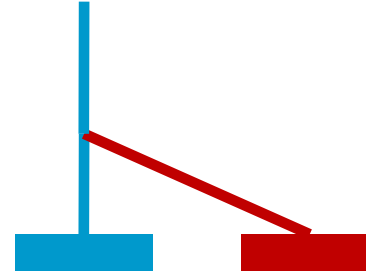
Same code

OpenMP program example

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                      private(i,z)
{
   z = 0.0;

   #pragma omp for
   for (i=0; i<n; i++) {
      z = z + x[i]*y[i];
   }

   #pragma omp critical
   {
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      y[i] = y[i] - w*x[i];
   }
}
```
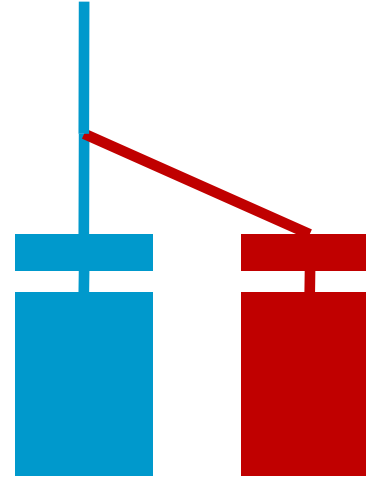
Do loop
Each thread execute a different set of loop iterations

OpenMP program example

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                      private(i,z)
{
    z = 0.0;

    #pragma omp for
    for (i=0; i<n; i++) {
        z = z + x[i]*y[i];
    }

    #pragma omp critical
    {
        w = w + z;
    }

    #pragma omp barrier


    #pragma omp for
    for (i=0; i<n; i++) {
        y[i] = y[i] - w*x[i];
    }
}
```

Barrier
All threads synchronise

OpenMP program example

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                      private(i,z)
{
   z = 0.0;

   #pragma omp for
   for (i=0; i<n; i++) {
      z = z + x[i]*y[i];
   }

   #pragma omp critical
   {
      w = w + z;
   }

   #pragma omp barrier


   #pragma omp for
   for (i=0; i<n; i++) {
      y[i] = y[i] - w*x[i];
   }
}
```
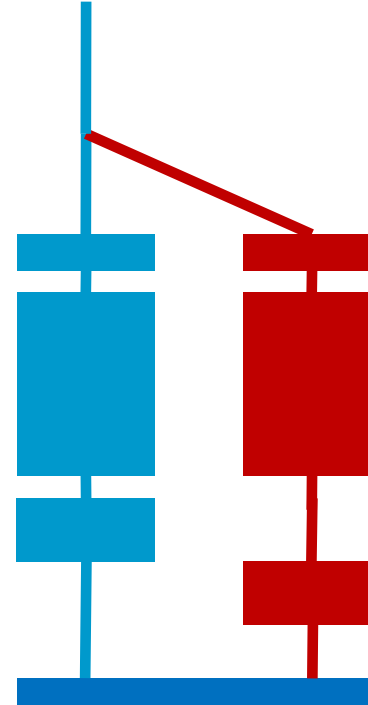
Do loop
Each thread execute a different set of loop iterations

OpenMP program example

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                      private(i,z)
{
   z = 0.0;

   #pragma omp for
   for (i=0; i<n; i++) {
      z = z + x[i]*y[i];
   }

   #pragma omp critical
   {
      w = w + z;
   }

   #pragma omp barrier


   #pragma omp for
   for (i=0; i<n; i++) {
      y[i] = y[i] – w*x[i];
   }
}
```
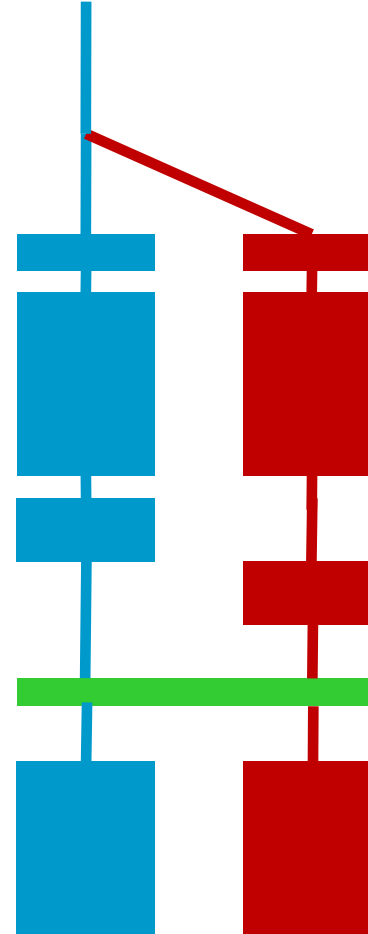
Destroy threads

OpenMP program example

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) \
                      private(i,z)
{
    z = 0.0;

    #pragma omp for
    for (i=0; i<n; i++) {
        z = z + x[i]*y[i];
    }

    #pragma omp critical
    {
        w = w + z;
    }

    #pragma omp barrier


    #pragma omp for
    for (i=0; i<n; i++) {
        y[i] = y[i] - w*x[i];
    }
}
```
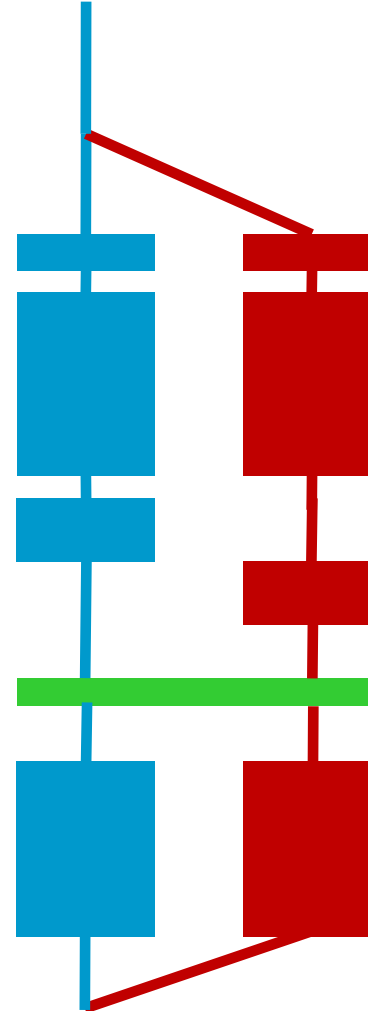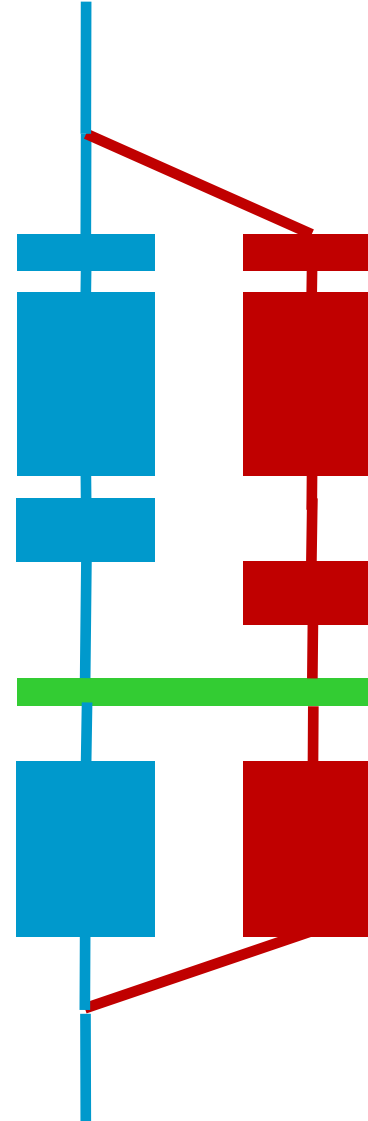
Serial code

Reductions

- In the above example we are adding up the value of the private z's across all threads to produce a shared value in w
  - So we are reducing many values to a single one via the + operator

- This is so common that reduction operations are supplied directly by OpenMP

- And if it is applicable reductions should be used rather than critical as it will be faster
  - Critical is all purpose, reduction is the precision tool

- Reductions can be applied to whole parallel regions or parallel do/for work share constructs
  - In the latter the reduction variable should be shared

```
w = 0.0;

#pragma omp parallel shared (n,w,x,y) private(i)
{

    #pragma omp for reduction(+:w)
    for (i=0; i<n; i++) {
        w = w + x[i]*y[i];
    }

    #pragma omp for
    for (i=0; i<n; i++) {
        y[i] = y[i] - w*x[i];
    }

}
```

Reduction Operators

- C/C++ Syntax:
  reduction (operator : list)

- Where
  - operator is one of: `+   *   -   &   ^  |   && ||  min max`

OpenMP: best practices

- thread creation / destruction can be expensive, so threads should be re-used
  - maximise parallel loops (large loops has more opportunities for reuse of cached data)
  - avoid parallel regions in inner loops (aim for the coarsest data parallelism)
  - minimise the number of times parallel regions are entered/exited
  - example: parallel inner loop moved to parallel outer region

```
// initial
for (n=0;n<NN;n++)
  #pragma omp parallel private(m)
  #pragma omp for
  for (m=0;m<MM;m++)
```

```
// improved
#pragma omp parallel private (n,m)
for (n=0;n<NN;n++)
  # pragma omp for
  for (m=0;m<MM;m++)
```

OpenMP: best practices

- Do not overuse synchronisation and explicit barriers
  - Remember every workshare construct by default has an implicit barrier on exit – this is normally enough

- Scope all your variables and use default(none)

- Think carefully about potential race conditions
  - Remember – a shared variable on the left hand side of an = should start alarm bells ringing
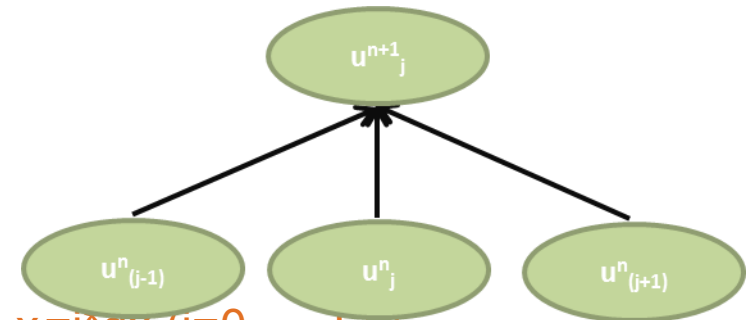
Example – The 1D Heat Equation

- The **physics**: find the time-varying distribution of temperature along a rod, starting from an initial distribution, given the fixed temperature at the ends

- The **maths** (an initial value problem): find $u(x,t)$ on the interval $[0, 1]$ given

  – $u(0, t) = u(1, t) = 0$ and $u(0, x) = u_0(x)$.

- The **numerics** (a finite difference scheme):
  – sample the interval $[0, 1]$ at equidistant points $x_j = j^*dx$ ($j=0,\ldots,J-1$) and fixed time intervals $t_n = n^*dt$, $n>0$ and find the values of all temperature samples u^n_j at the sample points
  – discretised equations give:
  $$u^{(n+1)}_j = u^n_j + nu^*(u^n_{(j+1)} - 2^*u^n_j + u^n_{(j-1)})$$
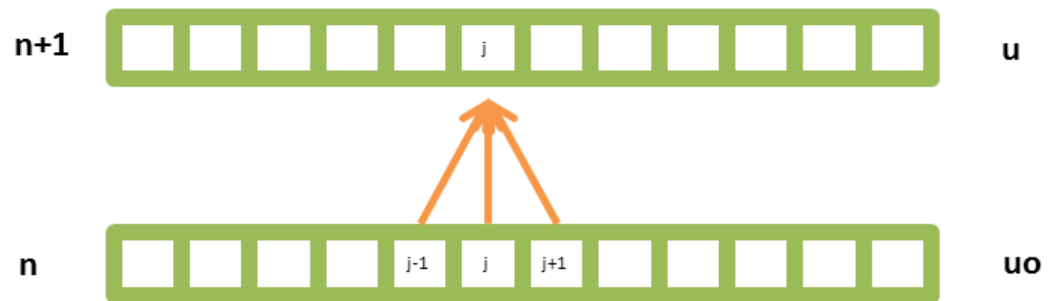 – 4 point stencil

Example: 1D Heat Equation

- The core of the program is to use two vectors u and uo (u "old").

At every time step,
- copy u into uo (not efficient but simple to understand)
- apply the finite difference scheme (the 4 point stencil)

- apply boundary conditions: $u_1 = u_J = 0$

Example – 1D Heat Equation

```
// boundary conditions
   u[0]   = 0.0; uo[0]   = 0.0;
   u[J-1] = 0.0; uo[J-1] = 0.0;

// time loop
  for (n=0; n<n_time_steps; n++) {

    // store solution
    for (j=1; j<J-1; j++) {
      uo[j] = u[j];
    }

    // finite difference scheme
    for (j=1; j<J-1; j++) {
      u[j] = uo[j] + nu*(uo[j-1]-2.0*uo[j]+uo[j+1]);
    }

}
```

Problem: 1D heat equation in Parallel – The Easy Way

```
// time loop
for (t=0; t<n_time_steps; t++) {
    // store solution


    for (j=1; j<n-1; j++) {
        uo[j] = u[j];
    }


    // finite difference scheme



    for (j=1; j<n-1; j++) {
        u[j] = uo[j] +
        nu*(uo[j-1]-2.0*uo[j]+uo[j+1]);
    }

}
```

```
// time loop
for (t=0; t<n_time_steps; t++) {
    // store solution
    #pragma omp parallel shared(n,u,uo,J) private(j)
    {
        #pragma omp for
        for (j=1; j<n-1; j++) {
            uo[j] = u[j];
        }
    }
    // finite difference scheme
    #pragma omp parallel shared(n,u,uo,nu,J) private(j)
    {
        #pragma omp for
        for (j=1; j<n-1; j++) {
            u[j] = uo[j] +
            nu*(uo[j-1]-2.0*uo[j]+uo[j+1]);
        }
    }
}
```

Problem: 1D Heat Equation in Parallel – The Better Way

```
// time loop
for (t=0; t<n_time_steps; t++) {
  // store solution
  #pragma omp parallel shared(n,u,uo,J) private(j)
  {
    #pragma omp for
    for (j=1; j<n-1; j++) {
      uo[j] = u[j];
    }
  }
  // finite difference scheme
  #pragma omp parallel shared(n,u,uo,nu,J) private(j)
  {
    #pragma omp for
    for (j=1; j<n-1; j++) {
      u[j] = uo[j] +
      nu*(uo[j-1]-2.0*uo[j]+uo[j+1]);
    }
  }
}
```

```
// time loop
  # pragma omp parallel default( none ) \
          shared(n,n_time_steps,u,uo,nu,) \
          private(t,j)
{
  for (t=0; t<n_time_steps; t++) {
    // store solution
    # pragma omp for
    for (j=1; j<n-1; j++) {
        uo[j] = u[j];
    }

    // finite difference scheme
    # pragma omp for
    for (j=1; j<n-1; j++) {
      u[j] = uo[j] +
      nu*(uo[j-1]-2.0*uo[j]+uo[j+1]);
    }
  }
}
```

What have we learnt?

We have learnt

- The basic ideas behind parallelism
- How OpenMP implements the shared memory programming model
- How to create threads with #pragma omp parallel
- How to scope variables
- How to share the work between the threads with #pragma omp for
- How to synchronise the threads with barriers, critical regions and reductions
- How to parallelise a small but realistic program

Further learning

- There is more to OpenMP

    - More run-time library routines (times, locks, execution)

    - More work-sharing directives (sections, work share, task, …)

    - More synchronization directives (atomic, flush, …)

    - More environmental variables

- The best way to learn OpenMP is to go on a longer course run by the national supercomputing service, ARCHER2
    - https://www.archer2.ac.uk/training/
    - https://www.archer2.ac.uk/training/courses/211005-advanced-openmp/

In the next lecture…

Introduction to GPUs

- Hardware architecture

- Software tools

- NVIDIA libraries