

# Machine Learning.

## Non-Coding Portion.

### 4a. PROOF of two equations

$\mathcal{S} \rightarrow$  bag of words (document)

$n(w) \rightarrow$  each word  $w \in W$  appears in  $\mathcal{S}$ .

each word independent

Assume that the document was generated one word at a time.

~~it does not matter.~~

Assume that words are drawn from the same distribution  $\theta = \theta_w$  where  $w \in W$  appears with probability  $\theta_w$ .

in the dictionary

No it does not matter. Since, as long as the word  $w$  do not appear it is counted as  $n(w) = 0$ .

b.  $\frac{\partial \mathcal{L}}{\partial \mu} = 0$  } to derive  $\mu$

Training Loss.  $\rightarrow \mathcal{L}_n(\mu, \sigma^2) = \frac{d}{2} \log(2\pi\sigma^2) + \frac{1}{2n\sigma^2} \sum_{i=1}^n x_i \|x_i - \mu\|^2$

$$0 = \frac{d}{2n\sigma^2} + \frac{1}{2n\sigma^2} \sum_{i=1}^n x_i \|x_i - \mu\|^2$$

$$0 = \sum_{i=1}^n x_i - n\mu$$

$$\mu = \frac{1}{n} \sum_{i=1}^n x_i \quad \#$$

$\frac{\partial \mathcal{L}}{\partial \sigma} = 0$  } to derive  $\sigma$   $\log_e = \ln$

$$0 = \frac{d}{2} \left( \frac{1}{\sigma^2} \right) + \frac{-2}{2n\sigma^3} \sum_{i=1}^n \|x_i - \mu\|^2$$

$$\frac{1}{nd} \sum_{i=1}^n \|x_i - \mu\|^2 = \sigma^2$$

$$\sigma = \sqrt{\frac{1}{nd} \sum_{i=1}^n \|x_i - \mu\|^2} \quad \#$$