## Relevant Literature

Wesley van der Lee May 31, 2017

## 1 Relevant Literature

## 1.1 Learning Regular Sets from Queries and Counterexamples

Learning Regular Sets from Queries and Counterexamples by Dana Angluin forms the basis of many modern state machine inference algorithms. Her research introduces the polynomial complex L\* algorithm for learning a regular set, a task which before was computationally intractable because it was proven to be NP-hard [1]. The basic idea of L\* is a learner whose goal is to create a valid conjecture by utilization of an expert system, the Minimally Adequate Teacher (MAT). This is achieved by posing two types of queries to the MAT: membership queries and conjectures. A membership query inquires a given string t to the MAT, who answers yes or no depending on whether t is a member of the to be hypothesized set U. The learner can also verify a conjecture to the MAT, which answers yes if the conjecture is equal to the unknown language. iF this is not the case, the MAT provides a counterexample, which is a string t in the symmetric difference of the conjecture and the unknown language.

The learner keeps track of the queried strings, classified by either a member or non-member of the unknown regular set U. This information is organized in an observation table that consists of three fields: a nonempty finite prefix-closed set S of strings, a nonempty finite suffix-closed set E of strings and a finite function T that maps  $(S \cup S \cdot A) \cdot E$  to  $\{0,1\}$ . A word U can be typically of the form  $(S \cup S \cdot A) \cdot E$  and if  $U \in U$  then U will result to 1 and 0 otherwise. Thus the observation table can be denoted as U then U t

The learner queries for the right amount of data from the MAT, by establishing an observation table that is closed and consistent. The table is closed if for every t in  $S \cdot A$ , there exists an s in S such that row(t) = row(s). If the table is not closed, there exists a  $t \in S \cdot A$  where no prefix will lead to. The learner identifies for which suffix distinguishes the rows and adds the word to the set S. When  $s_1, s_2 \in S$  such that  $row(s_1) = row(s_2)$ , then if for all a in the alphabet holds  $row(s_1 \cdot a) = row(s_2 \cdot a)$ , the table is consistent. If the table is not closed, the language would not be regular as it shows non-deterministic behavior. The learner identifies for which  $s_1, s_2 \in S$  distinguishes the result of output T and adds the word to the set E.

If (S, E, T) is closed and consistent, a acceptor M(S, E, T) can be defined which is consistent with T and has the smallest set of states. This can be proven as follows. Let  $q_0$  be the starting state  $(row(\lambda))$  and  $\delta$  be the transition function from one state to another in the acceptor, then because  $\delta(row(s), a) = row(s \cdot a)$ 

too quich explain in detail. explain in futrocy