

$$\begin{array}{l}
 \text{max: } x_1 + 3x_2 \\
 \text{sub to: } -x_1 - 1x_2 \leq -3 \\
 \quad \quad -x_1 + 1x_2 \leq -1 \\
 \quad \quad x_1 + 2x_2 \leq 4 \\
 \text{Primal } x_1, x_2 \geq 0
 \end{array}$$

$$\begin{array}{l}
 \text{min: } -3y_1 - 1y_2 + 4y_3 \\
 \text{sub to: } -1y_1 - 1y_2 + 1y_3 \geq 1 \\
 \quad \quad -1y_1 + 1y_2 + 2y_3 \geq 3 \\
 \text{Dual } y_1, y_2, y_3 \geq 0
 \end{array}$$

$$-z = 0 + 0 + 0$$

-2

$$-2 = 0 + 3y_1 + 1y_2 - 4y_3$$

$$w_1 = -1 + 1y_1 + 1y_2 - 1y_3$$

$$w_2 = 3 + 1y_1 - 1y_2 - 2y_3$$

$$-2 = -4 + 4y_1 - 3y_2 + 4w_3$$

$$y_3 = -1 + 1y_1 + 1y_2 - 1w_1$$

$$w_2 = -1 + 1y_1 - 3y_2 + 2w_1$$

$$-2 = (-5) + 0y_1 - 2w_1 + 1w_2$$

$$y_3 = \frac{4}{3} - \frac{2}{3}y_1 - \frac{1}{3}w_1 - \frac{1}{3}w_2$$

$$y_2 = \frac{1}{3} - \frac{1}{3}y_1 + \frac{2}{3}w_1 - \frac{1}{3}w_2$$

$$-2 = (-5) + 0y_1 - 2w_1 + 1w_2$$

$$y_1 = -2 - \frac{3}{4}y_3 + \frac{1}{2}w_1 + \frac{1}{2}w_2$$

$$y_2 = 1 + \frac{1}{2}y_3 + \frac{1}{2}w_1 - \frac{1}{2}w_2$$

$$-2 = (-5) + 0y_2 + 2w_1 + 1w_2$$

$$y_3 = 2 - 2y_2 + 1w_1 - 1w_2$$

$$y_1 = 1 - 3y_2 + 2w_1 - 1w_2$$

$$z = 5$$

$$\begin{array}{l}
 y_1 = -2, 0, 1 \\
 y_2 = 1, \frac{1}{3}, 0 \\
 y_3 = 0, \frac{1}{3}, 2
 \end{array}$$