$$\mathcal{H} \to -\frac{-2\,\pi_{ab}\,\pi^{ab} + 2\,\alpha^2\,\tilde{h}\,R[\nabla] + \pi^2}{2\,\alpha\,\sqrt{\tilde{h}}}$$