

$$\mathcal{H} \rightarrow \frac{-2\sqrt{\kappa R[\varphi]} + \kappa^4 (2\pi_{ab}\pi^{ab} - \pi^2)}{2\kappa^2\sqrt{\kappa}}$$