

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$

(No massless particles)

Lagrangian density

$$\begin{aligned} &\frac{2}{3}t_2\,\omega_{\,\,\,\prime}^{\kappa\lambda}\,\omega_{\kappa\lambda}^{\,\,\,\prime}+\frac{1}{3}t_2\,\omega_{\kappa\lambda}^{\,\,\,\prime}\,\omega_{\kappa\lambda}^{\,\,\,\prime\prime}+2\,r_1\,\partial_{\,\prime}\omega_{\,\,\,\kappa}^{\kappa\lambda}\,\partial_{\,\prime}\omega_{\lambda}^{\,\,\,\alpha}- \\ &\frac{2}{3}r_1\,\partial^\beta\omega_{\kappa}^{\theta\alpha}\,\partial_\theta\omega_{\alpha\beta}^{\,\,\,\kappa}+\frac{2}{3}r_2\,\partial^\beta\omega_{\kappa}^{\theta\alpha}\,\partial_\theta\omega_{\alpha\beta}^{\,\,\,\kappa}-\frac{2}{3}r_1\,\partial_\theta\omega_{\alpha\beta}^{\,\,\,\kappa}\,\partial_\kappa\omega^{\alpha\beta\theta}- \\ &\frac{1}{3}r_2\,\partial_\theta\omega_{\alpha\beta}^{\,\,\,\kappa}\,\partial_\kappa\omega^{\alpha\beta\theta}+\frac{2}{3}r_1\,\partial_\theta\omega_{\alpha\beta}^{\,\,\,\kappa}\,\partial_\kappa\omega^{\theta\alpha\beta}-\frac{2}{3}r_2\,\partial_\theta\omega_{\alpha\beta}^{\,\,\,\kappa}\,\partial_\kappa\omega^{\theta\alpha\beta}- \\ &2\,r_1\,\partial_\alpha\omega_{\lambda}^{\,\,\,\alpha}\,\partial_\kappa\omega^{\theta\kappa\lambda}+4\,r_3\,\partial_\alpha\omega_{\lambda}^{\,\,\,\alpha}\,\partial_\kappa\omega^{\kappa\lambda\theta}+ \\ &2\,r_1\,\partial_\theta\omega_{\lambda}^{\,\,\,\alpha}\,\partial_\kappa\omega^{\theta\kappa\lambda}-4\,r_3\,\partial_\theta\omega_{\lambda}^{\,\,\,\alpha}\,\partial_\kappa\omega^{\theta\kappa\lambda}+2\,r_1\,\partial_\alpha\omega_{\lambda}^{\,\,\,\alpha}\,\partial_\kappa\omega^{\kappa\lambda\theta}- \\ &4\,r_1\,\partial_\theta\omega_{\lambda}^{\,\,\,\alpha}\,\partial_\kappa\omega^{\kappa\lambda\theta}+\frac{1}{6}t_2\,\partial^\alpha f_{\theta\kappa}\,\partial^\kappa f_{\alpha}^{\,\,\,\theta}-\frac{1}{6}t_2\,\partial^\alpha f_{\kappa\theta}\,\partial^\kappa f_{\alpha}^{\,\,\,\theta}+ \\ &\frac{1}{6}t_2\,\partial^\alpha f_{\kappa}^{\,\,\,\lambda}\,\partial^\kappa f_{\alpha\lambda}^{\,\,\,\prime}+\frac{1}{3}t_2\,\omega_{\theta\kappa}\,\partial^\kappa f^{\,\,\,\prime\theta}-\frac{2}{3}t_2\,\omega_{\,\prime\kappa\theta}\,\partial^\kappa f^{\,\,\,\prime\theta}- \\ &\frac{1}{3}t_2\,\omega_{\theta\kappa}\,\partial^\kappa f^{\,\,\,\prime\theta}+\frac{2}{3}t_2\,\omega_{\theta\kappa\,\prime}\,\partial^\kappa f^{\,\,\,\prime\theta}-\frac{1}{6}t_2\,\partial^\alpha f_{\kappa}^{\,\,\,\lambda}\,\partial^\kappa f_{\lambda\alpha}^{\,\,\,\prime}- \\ &\frac{1}{6}t_2\,\partial_\kappa f_{\theta}^{\,\,\,\lambda}\,\partial^\kappa f_{\lambda}^{\,\,\,\theta}+\frac{1}{6}t_2\,\partial_\kappa f_{\theta}^{\,\,\,\lambda}\,\partial^\kappa f_{\lambda}^{\,\,\,\theta}+\frac{2}{3}r_1\,\partial_\kappa\omega^{\alpha\beta\theta}\,\partial^\kappa\omega_{\alpha\beta\theta}+ \\ &\frac{1}{3}r_2\,\partial_\kappa\omega^{\alpha\beta\theta}\,\partial^\kappa\omega_{\alpha\beta\theta}-\frac{2}{3}r_1\,\partial_\kappa\omega^{\theta\alpha\beta}\,\partial^\kappa\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\,\partial_\kappa\omega^{\theta\alpha\beta}\,\partial^\kappa\omega_{\alpha\beta\theta}+ \\ &\frac{2}{3}r_1\,\partial^\beta\omega_{\,\,\,\prime}^{\alpha\lambda}\,\partial_\lambda\omega_{\alpha\beta}^{\,\,\,\prime}-\frac{2}{3}r_2\,\partial^\beta\omega_{\,\,\,\prime}^{\alpha\lambda}\,\partial_\lambda\omega_{\alpha\beta}^{\,\,\,\prime}+\frac{4}{3}r_1\,\partial^\beta\omega_{\lambda}^{\,\,\,\prime\alpha}\,\partial_\lambda\omega_{\alpha\beta}^{\,\,\,\prime}+ \\ &\frac{2}{3}r_2\,\partial^\beta\omega_{\lambda}^{\,\,\,\prime\alpha}\,\partial_\lambda\omega_{\alpha\beta}^{\,\,\,\prime}-4\,r_3\,\partial^\beta\omega_{\lambda}^{\,\,\,\prime\alpha}\,\partial_\lambda\omega_{\alpha\beta}^{\,\,\,\prime}+2\,r_1\,\partial_\alpha\omega_{\lambda}^{\,\,\,\alpha}\,\partial^\lambda\omega_{\theta}^{\theta\kappa}- \\ &4\,r_3\,\partial_\alpha\omega_{\lambda}^{\,\,\,\alpha}\,\partial^\lambda\omega_{\theta}^{\theta\kappa}-2\,r_1\,\partial_\theta\omega_{\lambda}^{\,\,\,\alpha}\,\partial^\lambda\omega_{\kappa}^{\theta\kappa}+4\,r_3\,\partial_\theta\omega_{\lambda}^{\,\,\,\alpha}\,\partial^\lambda\omega_{\kappa}^{\theta\kappa} \end{aligned}$$

Added source term: $f^{\alpha\beta}\,\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\,\sigma_{\alpha\beta\chi}$

	$\omega_{1+}^{\#1}\,+\alpha\beta$	$\omega_{1+}^{\#2}\,+\alpha\beta$	$f_{1+}^{\#1}\,+\alpha\beta$	$\omega_{1-}^{\#1}\,+\alpha$	$\omega_{1-}^{\#2}\,+\alpha$	$f_{1-}^{\#1}\,+\alpha$	$f_{1-}^{\#2}\,+\alpha$
$\omega_{1+}^{\#1}\,+\alpha\beta$	$\frac{2t_2}{3}$	$\frac{\sqrt{2}\,t_2}{3}$	$\frac{1}{3}\,i\,\sqrt{2}\,kt_2$	0	0	0	0
$\omega_{1+}^{\#2}\,+\alpha\beta$	$\frac{\sqrt{2}\,t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0	0
$f_{1+}^{\#1}\,+\alpha\beta$	$-\frac{1}{3}\,i\,\sqrt{2}\,kt_2$	$-\frac{1}{3}\,i\,kt_2$	$\frac{k^2t_2}{3}$	0	0	0	0
$\omega_{1-}^{\#1}\,+\alpha$	0	0	0	$-k^2\,r_1$	0	0	0
$\omega_{1-}^{\#2}\,+\alpha$	0	0	0	0	0	0	0
$f_{1-}^{\#1}\,+\alpha$	0	0	0	0	0	0	0
$f_{1-}^{\#2}\,+\alpha$	0	0	0	0	0	0	0

	$\sigma_{1+}^{\#1}\,+\alpha\beta$	$\sigma_{1+}^{\#2}\,+\alpha\beta$	$\tau_{1+}^{\#1}\,+\alpha\beta$	$\sigma_{1-}^{\#1}\,+\alpha$	$\sigma_{1-}^{\#2}\,+\alpha$	$\tau_{1-}^{\#1}\,+\alpha$	$\tau_{1-}^{\#2}\,+\alpha$
$\sigma_{1+}^{\#1}\,+\alpha\beta$	$\frac{6}{(3+k^2)^2t_2}$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3i\sqrt{2}\,k}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1+}^{\#2}\,+\alpha\beta$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3}{(3+k^2)^2t_2}$	$\frac{3ik}{(3+k^2)^2t_2}$	0	0	0	0
$\tau_{1+}^{\#1}\,+\alpha\beta$	$-\frac{3i\sqrt{2}\,k}{(3+k^2)^2t_2}$	$-\frac{3ik}{(3+k^2)^2t_2}$	$\frac{3k^2}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1-}^{\#1}\,+\alpha$	0	0	0	$-\frac{1}{k^2}\,r_1$	0	0	0
$\sigma_{1-}^{\#2}\,+\alpha$	0	0	0	0	0	0	0
$\tau_{1-}^{\#1}\,+\alpha$	0	0	0	0	0	0	0
$\tau_{1-}^{\#2}\,+\alpha$	0	0	0	0	0	0	0

Source constraints

SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i\,k\,\sigma_{1+}^{\#1\alpha\beta} == 0$	3
$\sigma_{1+}^{\#1\alpha\beta} == \sigma_{1+}^{\#2\alpha\beta}$	3
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
$\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	27

	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1}\,+$	$6\,k^2\,(-r_1+r_3)$	0	0	0
$f_{0+}^{\#1}\,+$	0	0	0	0
$f_{0+}^{\#2}\,+$	0	0	0	0
$\omega_{0-}^{\#1}\,+$	0	0	0	$k^2\,r_2+t_2$

	$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1}\,+$	$\frac{1}{6\,k^2\,(-r_1+r_3)}$	0	0	0
$\tau_{0+}^{\#1}\,+$	0	0	0	0
$\tau_{0+}^{\#2}\,+$	0	0	0	0
$\sigma_{0-}^{\#1}\,+$	0	0	0	$\frac{1}{k^2\,r_2+t_2}$

	$\sigma_{2+}^{\#1}\,+\alpha\beta$	$\tau_{2+}^{\#1}\,+\alpha\beta$	$\sigma_{2-}^{\#1}\,+\alpha\beta\chi$
$\sigma_{2+}^{\#1}\,+\alpha\beta$	0	0	0
$\tau_{2+}^{\#1}\,+\alpha\beta$	0	0	0
$\sigma_{2-}^{\#1}\,+\alpha\beta\chi$	0	0	$\frac{1}{k^2}\,r_1$

	$\omega_{2+}^{\#1}\,+\alpha\beta$	$f_{2+}^{\#1}\,+\alpha\beta$	$\omega_{2-}^{\#1}\,+\alpha\beta\chi$
$\omega_{2+}^{\#1}\,+\alpha\beta$	0	0	0
$f_{2+}^{\#1}\,+\alpha\beta$	0	0	0
$\omega_{2-}^{\#1}\,+\alpha\beta\chi$	0	0	$k^2\,r_1$