

# Particle spectrograph

## Wave operator and propagator

	$\sigma_1^{#1} \dagger^{\alpha\beta}$	$\sigma_1^{#2} \dagger^{\alpha\beta}$	$\tau_1^{#1} \dagger^{\alpha\beta}$	$\sigma_1^{#1} \dagger^{\alpha}$	$\sigma_1^{#2} \dagger^{\alpha}$	$\tau_1^{#2} \dagger^{\alpha}$
$\sigma_1^{#1} \dagger^{\alpha\beta}$	$\frac{1}{k^2(2r_3+r_5)}$	$-\frac{\sqrt{2}}{k^2(1+k^2)(2r_3+r_5)}$	$-\frac{i\sqrt{2}}{k(1+k^2)(2r_3+r_5)}$	0	0	0
$\sigma_1^{#2} \dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{k^2(1+k^2)(2r_3+r_5)}$	$\frac{3k^2(2r_3+r_5)+2t_2}{(k+k^3)^2(2r_3+r_5)t_2}$	$\frac{i(3k^2(2r_3+r_5)+2t_2)}{k(1+k^2)^2(2r_3+r_5)t_2}$	0	0	0
$\tau_1^{#1} \dagger^{\alpha\beta}$	$\frac{i\sqrt{2}}{k(1+k^2)(2r_3+r_5)}$	$-\frac{i(3k^2(2r_3+r_5)+2t_2)}{k(1+k^2)^2(2r_3+r_5)t_2}$	$\frac{3k^2(2r_3+r_5)+2t_2}{(1+k^2)^2(2r_3+r_5)t_2}$	0	0	0
$\sigma_1^{#1} \dagger^{\alpha}$	0	0	0	$\frac{2}{k^2(r_3+2r_5)}$	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	$\frac{4i}{k(1+2k^2)(r_3+2r_5)}$
$\sigma_1^{#2} \dagger^{\alpha}$	0	0	0	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	$\frac{3k^2(r_3+2r_5)+4t_3}{(k+2k^3)^2(r_3+2r_5)t_3}$	$\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$
$\tau_1^{#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_1^{#2} \dagger^{\alpha}$	0	0	0	$-\frac{4i}{k(1+2k^2)(r_3+2r_5)}$	$-\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$	$\frac{6k^2(r_3+2r_5)+8t_3}{(1+2k^2)^2(r_3+2r_5)t_3}$

	$\omega_{1+}^{#1} \alpha\beta$	$\omega_{1+}^{#2} \alpha\beta$	$f_{1+}^{#1} \alpha\beta$	$\omega_{1-}^{#1} \alpha$	$\omega_{1-}^{#2} \alpha$	$f_{1-}^{#1} \alpha$	$f_{1-}^{#2} \alpha$
$\omega_{1+}^{#1} \dagger^{\alpha\beta}$	$k^2(2r_3+r_5)+\frac{2t_2}{3}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0	0
$\omega_{1+}^{#2} \dagger^{\alpha\beta}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0	0
$f_{1+}^{#1} \dagger^{\alpha\beta}$	$-\frac{1}{3}i\sqrt{2}kt_2$	$-\frac{1}{3}ikt_2$	$\frac{k^2t_2}{3}$	0	0	0	0
$\omega_{1-}^{#1} \dagger^{\alpha}$	0	0	0	$k^2(\frac{r_3}{2}+r_5)+\frac{2t_3}{3}$	$-\frac{\sqrt{2}t_3}{3}$	0	$-\frac{2}{3}ikt_3$
$\omega_{1-}^{#2} \dagger^{\alpha}$	0	0	0	$-\frac{\sqrt{2}t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_3$
$f_{1-}^{#1} \dagger^{\alpha}$	0	0	0	0	0	0	0
$f_{1-}^{#2} \dagger^{\alpha}$	0	0	0	$\frac{2ikt_3}{3}$	$-\frac{1}{3}i\sqrt{2}kt_3$	0	$\frac{2k^2t_3}{3}$

	$\sigma_{2+}^{#1} \alpha\beta$	$\tau_{2+}^{#1} \alpha\beta$	$\sigma_{2-}^{#1} \alpha\beta\chi$
$\sigma_{2+}^{#1} \dagger^{\alpha\beta}$	$-\frac{2}{3k^2r_3}$	0	0
$\tau_{2+}^{#1} \dagger^{\alpha\beta}$	0	0	0
$\sigma_{2-}^{#1} \dagger^{\alpha\beta\chi}$	0	0	0

	$\omega_{2+}^{#1} \alpha\beta$	$f_{2+}^{#1} \alpha\beta$	$\omega_{2-}^{#1} \alpha\beta\chi$
$\omega_{2+}^{#1} \dagger^{\alpha\beta}$	$-\frac{3k^2r_3}{2}$	0	0
$f_{2+}^{#1} \dagger^{\alpha\beta}$	0	0	0
$\omega_{2-}^{#1} \dagger^{\alpha\beta\chi}$	0	0	0

Quadratic (free) action

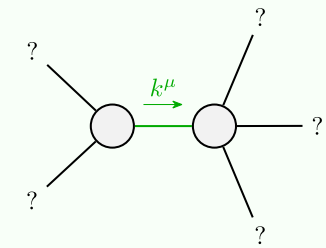
$$S_F == \iiint (\frac{1}{6} (4t_3 \omega_{\alpha}^{\alpha} \omega_{\kappa\alpha}^{\kappa} + 4t_2 \omega_{\kappa\lambda}^{\kappa\lambda} \omega_{\alpha}^{\alpha} + 2t_2 \omega_{\kappa\lambda}^{\kappa\lambda} \omega_{\alpha}^{\alpha} + 6f^{\alpha\beta} \tau_{\alpha\beta} + 6\omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 3r_3 \partial_{\lambda} \omega_{\kappa}^{\kappa\lambda} \partial' \omega_{\lambda}^{\alpha} \omega_{\alpha}^{\alpha} - 6r_5 \partial_{\lambda} \omega_{\kappa}^{\kappa\lambda} \partial' \omega_{\lambda}^{\alpha} \omega_{\alpha}^{\alpha} + 3r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega_{\lambda}^{\kappa\lambda} + 6r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\lambda}^{\kappa\lambda} + 6r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\lambda}^{\kappa\lambda\theta} + 6r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\lambda}^{\kappa\lambda\theta} + 12r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\lambda}^{\kappa\lambda\theta} + t_2 \partial^{\alpha} f_{\theta\kappa} \partial^{\kappa} f_{\alpha}^{\theta} - t_2 \partial^{\alpha} f_{\kappa\theta} \partial^{\kappa} f_{\alpha}^{\theta} + t_2 \partial^{\alpha} f_{\lambda}^{\lambda} \partial^{\kappa} f_{\kappa\alpha}^{\alpha} - 8t_3 \partial^{\alpha} f_{\kappa\alpha} \partial^{\kappa} f_{\lambda}^{\lambda} + 4t_3 \partial_{\kappa} f_{\lambda}^{\lambda} \partial^{\kappa} f_{\alpha}^{\alpha} - 4t_3 \omega_{\kappa\alpha}^{\alpha} \partial^{\kappa} f_{\alpha}^{\lambda} - 4t_2 \omega_{\lambda\kappa\theta} \partial^{\kappa} f^{\lambda\theta} - 2t_2 \omega_{\theta\lambda\kappa} \partial^{\kappa} f^{\lambda\theta} + 4t_2 \omega_{\theta\kappa\lambda} \partial^{\kappa} f^{\lambda\theta} + 4t_3 \omega_{\lambda\alpha}^{\alpha} \partial^{\kappa} f_{\lambda}^{\theta} - t_2 \partial^{\alpha} f_{\kappa}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} - t_2 \partial_{\kappa} f_{\lambda}^{\theta} \partial^{\kappa} f_{\theta}^{\lambda} + 4t_3 \partial^{\alpha} f_{\alpha}^{\lambda} \partial^{\kappa} f_{\lambda\kappa} - 24r_3 \partial^{\beta} \omega_{\lambda}^{\lambda\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\beta} - 3r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} + 6r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} + 3r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} - 6r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} )) [t, x, y, z] dz dy dx dt$$

Source constraints/gauge generators	
SO(3) irreps	Multiplicities
$\tau_{0+}^{#2} == 0$	1
$\tau_{0+}^{#1} - 2ik\sigma_{0+}^{#1} == 0$	1
$\tau_{1-}^{#2\alpha} + 2ik\sigma_{1-}^{#2\alpha} == 0$	3
$\tau_{1-}^{#1\alpha} == 0$	3
$\tau_{1+}^{#1\alpha\beta} + ik\sigma_{1+}^{#2\alpha\beta} == 0$	3
$\sigma_{2-}^{#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{#1\alpha\beta} == 0$	5
Total constraints:	
21	

	$\omega_{0+}^{#1}$	$f_{0+}^{#1}$	$f_{0+}^{#2}$	$\omega_{0-}^{#1}$
$\omega_{0+}^{#1} \dagger$	$t_3$	$-i\sqrt{2}kt_3$	0	0
$f_{0+}^{#1} \dagger$	$i\sqrt{2}kt_3$	$2k^2t_3$	0	0
$f_{0+}^{#2} \dagger$	0	0	0	0
$\omega_{0-}^{#1} \dagger$	0	0	0	$t_2$

	$\sigma_{0+}^{#1}$	$\tau_{0+}^{#2}$	$\sigma_{0-}^{#1}$
$\sigma_{0+}^{#1} \dagger$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0	0
$\tau_{0+}^{#1} \dagger$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0	0
$\tau_{0+}^{#2} \dagger$	0	0	0
$\sigma_{0-}^{#1} \dagger$	0	0	$\frac{1}{t_2}$

## Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$
Polarisations:	2

(No massive particles)

## Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$