

$\omega_{1^+}^{\#1} + \alpha\beta$	$\omega_{1^+}^{\#2} + \alpha\beta$	$f_{1^+}^{\#1} + \alpha\beta$	$\omega_{1^-}^{\#1} - \alpha$	$\omega_{1^-}^{\#2} - \alpha$	$f_{1^-}^{\#1} - \alpha$	$f_{1^-}^{\#2} - \alpha$
$k^2(2r_3+r_5)$	0	0	0	0	0	0
$\omega_{1^+}^{\#2} + \alpha\beta$	0	0	0	0	0	0
$f_{1^+}^{\#1} + \alpha\beta$	0	0	0	0	0	0
$\omega_{1^-}^{\#1} + \alpha$	0	0	$k^2(\frac{r_3}{2}+r_5)+\frac{2t_3}{3}$	$-\frac{\sqrt{2}t_3}{3}$	0	$-\frac{2}{3}i\sqrt{2}kt_3$
$\omega_{1^-}^{\#2} + \alpha$	0	0	$-\frac{\sqrt{2}t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_3$
$f_{1^-}^{\#1} + \alpha$	0	0	0	0	0	0
$f_{1^-}^{\#2} + \alpha$	0	0	$\frac{2ikt_3}{3}$	$-\frac{1}{3}i\sqrt{2}kt_3$	0	$\frac{2k^2t_3}{3}$

Lagrangian density

$$\begin{aligned} &\frac{2}{3}t_3\omega_{\kappa\alpha}^{\prime\alpha'}\omega_{\kappa\alpha}^{\prime\alpha}-\frac{1}{2}r_3\partial_l\omega_{\kappa}^{\kappa\lambda}\partial^l\omega_{\lambda\alpha}^{\alpha}-r_5\partial_l\omega_{\kappa}^{\kappa\lambda}\partial^l\omega_{\lambda\alpha}^{\alpha}+ \\ &\frac{2}{3}r_2\partial^\beta\omega_{\kappa}^{\beta\alpha}\partial_{\theta\theta}\omega_{\alpha\beta}^{\alpha\kappa}-\frac{1}{3}r_2\partial_{\theta\theta}\omega_{\alpha\beta}^{\alpha\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}-\frac{2}{3}r_2\partial_{\theta\theta}\omega_{\alpha\beta}^{\alpha\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}+ \\ &\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda\theta}^{\alpha\kappa}\partial_{\kappa}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda\theta}^{\alpha\kappa}\partial_{\kappa}\omega^{\theta\kappa\lambda}-\frac{1}{2}r_3\partial_{\theta}\omega_{\lambda}^{\alpha\kappa}\partial_{\kappa}\omega^{\theta\kappa\lambda}-\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda\theta}^{\alpha\kappa}\partial_{\kappa}\omega^{\kappa\lambda\theta}+ \\ &r_3\partial_{\theta}\omega_{\lambda\alpha}^{\alpha\kappa}\partial_{\kappa}\omega^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda\alpha}^{\alpha\kappa}\partial_{\kappa}\omega^{\kappa\lambda\theta}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha\kappa}\partial^{\kappa}f_{\prime}^{\prime}- \\ &\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda\kappa}\partial^{\kappa}f_{\prime}^{\prime}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\prime}^{\prime}+\frac{2}{3}t_3\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\prime}^{\prime}+ \\ &\frac{2}{3}t_3\omega_{\iota\alpha}^{\alpha\kappa}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{2}{3}t_3\omega_{\iota\lambda}^{\lambda\kappa}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{2}{3}t_3\partial^{\alpha}f_{\lambda\alpha}\partial^{\kappa}f_{\lambda\kappa}+ \\ &\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^{\beta}\omega_{\iota}^{\prime\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}+ \\ &\frac{2}{3}r_2\partial^{\beta}\omega_{\iota}^{\prime\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}-4r_3\partial^{\beta}\omega_{\iota}^{\prime\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}-\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda\theta}^{\alpha\kappa}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa}+ \\ &r_5\partial_{\alpha}\omega_{\lambda\theta}^{\alpha\kappa}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa}+\frac{1}{2}r_3\partial_{\theta}\omega_{\lambda\alpha}^{\alpha\kappa}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa}-r_5\partial_{\theta}\omega_{\lambda\alpha}^{\alpha\kappa}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa} \end{aligned}$$

Added source term: $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

$\sigma_{1^+}^{\#1} + \alpha\beta$	$\sigma_{1^+}^{\#2} + \alpha\beta$	$\tau_{1^+}^{\#1} + \alpha\beta$	$\sigma_{1^-}^{\#1} - \alpha$	$\sigma_{1^-}^{\#2} - \alpha$	$\tau_{1^-}^{\#1} - \alpha$	$\tau_{1^-}^{\#2} - \alpha$
$\frac{1}{k^2(2r_3+r_5)}$	0	0	0	0	0	0
$\sigma_{1^+}^{\#2} + \alpha\beta$	0	0	0	0	0	0
$\tau_{1^+}^{\#1} + \alpha\beta$	0	0	0	0	0	0
$\sigma_{1^-}^{\#1} + \alpha$	0	0	$\frac{2}{k^2(r_3+2r_5)}$	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	0	$\frac{4i}{k(1+2k^2)(r_3+2r_5)}$
$\sigma_{1^-}^{\#2} + \alpha$	0	0	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	$\frac{3k^2(r_3+2r_5)+4t_3}{(k+2k^3)^2(r_3+2r_5)t_3}$	0	$\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$
$\tau_{1^-}^{\#1} + \alpha$	0	0	0	0	0	0
$\tau_{1^-}^{\#2} + \alpha$	0	0	0	0	0	0

$\sigma_{2^+}^{\#1} + \alpha\beta$	$\tau_{2^+}^{\#1} + \alpha\beta$	$\sigma_{2^+}^{\#1} - \alpha\beta\chi$
$-\frac{2}{3k^2r_3}$	0	0
$\tau_{2^+}^{\#1} + \alpha\beta$	0	0
$\sigma_{2^+}^{\#1} + \alpha\beta\chi$	0	0

$\sigma_{0^+}^{\#1} +$	$\tau_{0^+}^{\#1} +$	$\tau_{0^+}^{\#2} +$	$\sigma_{0^+}^{\#1} -$
$\frac{1}{(1+2k^2)^2t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0	0
$\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0	0
$\tau_{0^+}^{\#2} +$	0	0	0
$\sigma_{0^+}^{\#1} +$	0	0	$\frac{1}{k^2r_2}$

$\omega_{0^+}^{\#1} +$	$f_{0^+}^{\#1} +$	$f_{0^+}^{\#2} +$	$\omega_{0^+}^{\#1} -$
t_3	$-i\sqrt{2}kt_3$	0	0
$f_{0^+}^{\#1} +$	$i\sqrt{2}kt_3$	0	0
$f_{0^+}^{\#2} +$	0	0	0
$\omega_{0^+}^{\#1} -$	0	0	k^2r_2

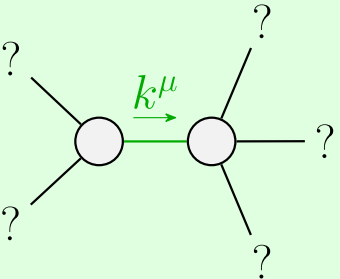
$\omega_{2^+}^{\#1} + \alpha\beta$	$f_{2^+}^{\#1} + \alpha\beta$	$\omega_{2^+}^{\#1} - \alpha\beta\chi$
$-\frac{3k^2r_3}{2}$	0	0
$f_{2^+}^{\#1} + \alpha\beta$	0	0
$\omega_{2^+}^{\#1} - \alpha\beta\chi$	0	0

Source constraints	#
SO(3) irreps	
$\tau_{0^+}^{\#2} == 0$	1
$\tau_{0^+}^{\#1} - 2i\sqrt{2}k\sigma_{0^+}^{\#1} == 0$	1
$\tau_{1^+}^{\#2} - \alpha + 2i\sqrt{2}k\sigma_{1^+}^{\#2} - \alpha == 0$	3
$\tau_{1^-}^{\#1} - \alpha == 0$	3
$\tau_{1^+}^{\#1} - \alpha\beta == 0$	3
$\sigma_{1^+}^{\#2} - \alpha\beta == 0$	3
$\sigma_{2^+}^{\#1} - \alpha\beta\chi == 0$	5
$\tau_{2^+}^{\#1} - \alpha\beta == 0$	5
Total #:	24

Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$

(No massive particles)



Quadratic pole

Pole residue: $-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$

Polarisations: 2