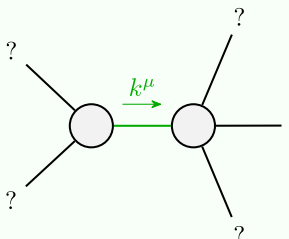


Particle spectrograph

Wave operator and propagator

Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\tau_{0+}^{\#2} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == 0$	1
$\tau_{0+}^{\#1} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == \partial_\beta \partial^\beta \tau^\alpha_\alpha$	1
$\tau_1^{\#2\alpha} + 2\,i\,k\,\sigma_1^{\#2\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\alpha\beta} + 2\,\partial_\delta \partial^\delta \partial_\chi \partial_\beta \sigma^{\alpha\beta\chi}$	3
$\tau_1^{\#1\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\beta\alpha}$	3
$\tau_{1+}^{\#1\alpha\beta} + i\,k\,\sigma_{1+}^{\#2\alpha\beta} == 0$	$\partial_\chi \partial^\alpha \tau^{\beta\chi} + \partial_\chi \partial^\beta \tau^{\chi\alpha} + \partial_\chi \partial^\chi \tau^{\alpha\beta} +$ $2\,\partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} + 2\,\partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\beta\chi} ==$ $\partial_\chi \partial^\alpha \tau^{\chi\beta} + \partial_\chi \partial^\beta \tau^{\alpha\chi} +$ $\partial_\chi \partial^\chi \tau^{\beta\alpha} + 2\,\partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta}$	3
$\tau_{2+}^{\#1\alpha\beta} - 2\,i\,k\,\sigma_{2+}^{\#1\alpha\beta} == 0$	$-i\,(4\,\partial_\delta \partial_\chi \partial^\beta \partial^\alpha \tau^{\chi\delta} + 2\,\partial_\delta \partial^\delta \partial^\beta \partial^\alpha \tau^{\chi\chi}_\chi -$ $3\,\partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\beta\chi} - 3\,\partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\chi\beta} -$ $3\,\partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\alpha\chi} - 3\,\partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\chi\alpha} +$ $3\,\partial_\delta \partial^\delta \partial_\chi \partial^\chi \tau^{\alpha\beta} + 3\,\partial_\delta \partial^\delta \partial_\chi \partial^\chi \tau^{\beta\alpha} +$ $4\,i\,k^\chi \partial_\epsilon \partial_\chi \partial^\beta \partial^\alpha \sigma^{\delta\epsilon}_\delta -$ $6\,i\,k^\chi \partial_\epsilon \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\delta\epsilon} -$ $6\,i\,k^\chi \partial_\epsilon \partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\delta\epsilon} +$ $2\,\eta^{\alpha\beta} \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\chi \tau^{\chi\delta} +$ $6\,i\,k^\chi \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\chi \sigma^{\alpha\delta\beta} +$ $6\,i\,k^\chi \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\chi \sigma^{\beta\delta\alpha} -$ $2\,\eta^{\alpha\beta} \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\delta \tau^{\chi\chi}_\chi -$ $4\,i\,\eta^{\alpha\beta} k^\chi \partial_\phi \partial^\phi \partial_\epsilon \partial_\chi \sigma^{\delta\epsilon}_\delta) == 0$	5
Total constraints/gauge generators:		16

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{(2r_3+r_5)t_1^2} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$r_5 < -2\,r_3 \,\&\& t_1 < 0 || t_1 > 0$

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \alpha\beta$	$\tau_{1+}^{\#1} \alpha\beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
0	$-\frac{\sqrt{2}}{t_1+k^2}t_1$	$-\frac{i\sqrt{2}k}{t_1+k^2}t_1$	0	0	0	0
$-\frac{\sqrt{2}}{t_1+k^2}t_1$	$\frac{-2k^2(2r_3+r_5)+t_1}{(1+k^2)^2t_1^2}$	$\frac{-2ik^3(2r_3+r_5)+ikt_1}{(1+k^2)^2t_1^2}$	$-\frac{\sqrt{2}}{t_1+k^2}t_1$	0	0	0
$\frac{i\sqrt{2}k}{t_1+k^2}t_1$	$\frac{i(2k^3(2r_3+r_5)-kt_1)}{(1+k^2)^2t_1^2}$	$\frac{-2k^4(2r_3+r_5)+k^2t_1}{(1+k^2)^2t_1^2}$	0	0	0	0
0	0	0	$\frac{1}{k^2(2r_3+r_5)}$	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	0	$-\frac{i}{k(1+2k^2)(2r_3+r_5)}$
0	0	0	0	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	0	$\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$
0	0	0	0	0	0	0
0	0	0	$\frac{i}{k(1+2k^2)(2r_3+r_5)}$	$-\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$	0	$\frac{6k^2(2r_3+r_5)+t_1}{(1+2k^2)^2(2r_3+r_5)t_1}$

Quadratic (free) action

$$S == \int \int \int \int (f^{\alpha\beta} \tau_{\alpha\beta} + \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} +$$
$$\frac{1}{6} t_1 (2 \omega_{\alpha}^{\alpha\iota} \omega_{\iota}^{\theta} \omega_{\theta}^{\theta} - 4 \omega_{\alpha}^{\theta} \omega_{\theta}^{\theta} \partial_{\iota} f^{\alpha\iota} + 4 \omega_{\iota}^{\theta} \omega_{\theta}^{\theta} \partial_{\iota} f^{\alpha\iota} - 2 \partial_{\iota} f^{\theta} \partial^{\iota} f^{\alpha} -$$
$$\partial_{\iota} f^{\alpha} - 2 \partial_{\iota} f^{\alpha\iota} \partial_{\theta} f^{\theta} + 4 \partial_{\iota} f^{\alpha} \partial_{\theta} f^{\theta} - 6 \partial_{\alpha} f^{\theta} \partial^{\theta} f^{\alpha\iota} -$$
$$3 \partial_{\alpha} f^{\theta} \partial^{\theta} f^{\alpha\iota} + 3 \partial_{\iota} f_{\alpha\theta} \partial^{\theta} f^{\alpha\iota} + 3 \partial_{\theta} f_{\alpha\iota} \partial^{\theta} f^{\alpha\iota} +$$
$$3 \partial_{\theta} f_{\iota\alpha} \partial^{\theta} f^{\alpha\iota} + 6 \omega_{\alpha\theta\iota} (\omega^{\alpha\iota\theta} + 2 \partial^{\theta} f^{\alpha\iota})) -$$
$$2 r_3 (\partial_{\beta} \omega_{\iota}^{\theta} \partial^{\iota} \omega_{\theta}^{\alpha\beta} + \partial_{\iota} \omega_{\beta}^{\theta} \partial^{\iota} \omega_{\theta}^{\alpha\beta} + \partial_{\alpha} \omega^{\alpha\beta\iota} \partial_{\theta} \omega_{\beta}^{\theta} -$$
$$2 \partial^{\iota} \omega^{\alpha\beta} \partial_{\alpha} \partial_{\theta} \omega_{\beta}^{\theta} + \partial_{\alpha} \omega^{\alpha\beta\iota} \partial_{\theta} \omega_{\iota}^{\theta} \omega_{\beta}^{\theta} -$$
$$2 \partial^{\iota} \omega^{\alpha\beta} \partial_{\alpha} \partial_{\theta} \omega_{\iota}^{\theta} + 2 \partial_{\beta} \omega_{\iota\theta\alpha} \partial^{\theta} \omega^{\alpha\beta\iota}) +$$
$$r_5 (\partial_{\iota} \omega_{\theta}^{\kappa} \partial^{\theta} \omega_{\alpha}^{\alpha\iota} - \partial_{\theta} \omega_{\iota}^{\kappa} \partial^{\theta} \omega_{\alpha}^{\alpha\iota} - (\partial_{\alpha} \omega^{\alpha\iota\theta} - 2 \partial^{\theta} \omega^{\alpha\iota} \omega_{\alpha}^{\iota})$$
$$(\partial_{\kappa} \omega_{\iota}^{\kappa} - \partial_{\kappa} \omega_{\theta}^{\kappa}))][t, x, y, z] d z d y d x d t$$

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$

$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
0	0	$\frac{2}{t_1}$

$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ $f_{2+}^{\#1} \dagger^{\alpha\beta}$ $\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$

$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$\frac{ikt_1}{\sqrt{2}}$	k^2t_1	0
0	0	$\frac{t_1}{2}$

$\sigma_{0+}^{\#1} \dagger$ $\tau_{0+}^{\#1} \dagger$ $\tau_{0+}^{\#2} \dagger$ $\sigma_{0-}^{\#1} \dagger$

$\frac{1}{6k^2r_3}$	0	0	0
0	0	0	0
0	0	0	0
0	0	0	$-\frac{1}{t_1}$

$\omega_{0+}^{\#1} \dagger$ $f_{0+}^{\#1} \dagger$ $f_{0+}^{\#2} \dagger$ $\omega_{0-}^{\#1} \dagger$

$6k^2r_3$	0	0	0
0	0	0	0
0	0	0	0
0	0	0	$-t_1$

$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ $\omega_{1+}^{\#2} \dagger^{\alpha\beta}$ $f_{1+}^{\#1} \dagger^{\alpha\beta}$ $\omega_{1-}^{\#1} \alpha$ $\omega_{1-}^{\#2} \alpha$ $f_{1-}^{\#1} \alpha$ $f_{1-}^{\#2} \alpha$

$k^2(2r_3+r_5) - \frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	0	0	0	0
$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0	0
$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0	0	0
0	0	0	$k^2(2r_3+r_5) + \frac{t_1}{6}$	$\frac{t_1}{3\sqrt{2}}$	0	$\frac{ikt_1}{3}$
0	0	0	$\frac{t_1}{3\sqrt{2}}$	$\frac{t_1}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_1$
0	0	0	0	0	0	0
0	0	0	$-\frac{1}{3}i\sqrt{2}kt_1$	$-\frac{1}{3}i\sqrt{2}kt_1$	0	$\frac{2k^2t_1}{3}$