



Massive particle	
Pole residue:	$-\frac{1}{r_1} \succ 0$
Polarisations:	5
Square mass:	$-\frac{t_1}{2r_1} \succ 0$
Spin:	2
Parity:	Odd

Unitarity conditions

$r_1 < 0 \ \&\& \ t_1 > 0$

(No massless particles)

Lagrangian density

$$\begin{aligned} &-\frac{1}{3}t_1\omega_{\lambda'}^{\alpha i}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_3\omega_{\lambda'}^{\alpha i}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\kappa\lambda'}^{\kappa\lambda}\omega_{\lambda'}^{\prime}+r_1\partial_i\omega_{\kappa}^{\kappa\lambda}\partial^i\omega_{\lambda}^{\alpha}- \\ &\frac{2}{3}r_1\partial^\beta\omega_{\kappa}^{\theta\alpha}\partial_\theta\omega_{\alpha\beta}^{\kappa}-\frac{2}{3}r_1\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\alpha\beta\theta}+\frac{2}{3}r_1\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\theta\alpha\beta}+ \\ &r_1\partial_\alpha\omega_{\lambda\theta}^{\alpha}\partial_\kappa\omega_{\theta}^{\theta\kappa\lambda}-r_1\partial_\theta\omega_{\lambda\alpha}^{\alpha}\partial_\kappa\omega_{\theta}^{\theta\kappa\lambda}+r_1\partial_\alpha\omega_{\lambda}^{\alpha}\partial_\theta\omega_{\theta}^{\kappa\lambda\theta}- \\ &2r_1\partial_\theta\omega_{\lambda\alpha}^{\alpha}\partial_\kappa\omega_{\alpha}^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial^\alpha f_{\theta\kappa}\partial^\kappa f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^\alpha f_{\kappa\theta}\partial^\kappa f_{\alpha}^{\theta}- \\ &\frac{1}{2}t_1\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\alpha\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^\kappa f_{\lambda'}^{\prime}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^\kappa f_{\lambda'}^{\prime}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\prime}- \\ &\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\prime}+\frac{2}{3}t_1\partial^\alpha f_{\kappa\alpha}\partial^\kappa f_{\lambda'}^{\prime}-\frac{4}{3}t_3\partial^\alpha f_{\kappa\alpha}\partial^\kappa f_{\lambda'}^{\prime}-\frac{1}{3}t_1\partial_\kappa f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\prime}+ \\ &\frac{2}{3}t_3\partial_\kappa f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\prime}+2t_1\omega_{\iota\kappa\theta}\partial^\kappa f_{\iota\theta}^{\theta}-\frac{1}{3}t_1\omega_{\iota\alpha}^{\alpha}\partial^\kappa f_{\kappa}^{\prime}+\frac{2}{3}t_3\omega_{\iota\alpha}^{\alpha}\partial^\kappa f_{\kappa}^{\prime}- \\ &\frac{1}{3}t_1\omega_{\iota\lambda}^{\lambda}\partial^\kappa f_{\lambda}^{\prime}+\frac{2}{3}t_3\omega_{\iota\lambda}^{\lambda}\partial^\kappa f_{\lambda}^{\prime}+\frac{1}{2}t_1\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\lambda\alpha}^{\lambda}+\frac{1}{2}t_1\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}+ \\ &\frac{1}{2}t_1\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}-\frac{1}{3}t_1\partial^\alpha f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda\kappa}^{\kappa}+\frac{2}{3}t_3\partial^\alpha f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda\kappa}^{\kappa}+ \\ &\frac{2}{3}r_1\partial_\kappa\omega^{\alpha\beta\theta}\partial^\kappa\omega_{\alpha\beta\theta}^{\theta}-\frac{2}{3}r_1\partial_\kappa\omega^{\theta\alpha\beta}\partial^\kappa\omega_{\alpha\beta\theta}^{\theta}+\frac{2}{3}r_1\partial^\beta\omega_{\lambda'}^{\alpha\lambda}\partial_\lambda\omega_{\alpha\beta}^{\iota}- \\ &\frac{8}{3}r_1\partial^\beta\omega_{\lambda'}^{\lambda\alpha}\partial_\lambda\omega_{\alpha\beta}^{\iota}-r_1\partial_\alpha\omega_{\lambda}^{\alpha}\partial_\theta\omega_{\lambda}^{\theta\kappa}+r_1\partial_\theta\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\alpha}^{\theta\kappa} \end{aligned}$$

Added source term:

$f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

	$\sigma_{1+}^{\#1}\dagger\alpha\beta$	$\sigma_{1+}^{\#2}\alpha\beta$	$\tau_{1+}^{\#1}\alpha\beta$	$\sigma_{1-}^{\#1}\alpha$	$\sigma_{1-}^{\#2}\alpha$	$\tau_{1-}^{\#1}\alpha$	$\tau_{1-}^{\#2}\alpha$
$\sigma_{1+}^{\#1}\dagger\alpha\beta$	0	$-\frac{\sqrt{2}}{t_1+k^2}t_1$	$-\frac{i\sqrt{2}k}{t_1+k^2}t_1$	0	0	0	0
$\sigma_{1+}^{\#2}\dagger\alpha\beta$	$-\frac{\sqrt{2}}{t_1+k^2}t_1$	$\frac{-2k^2r_1+t_1}{(1+k^2)^2}t_1^2$	$-\frac{i(2k^3r_1-k t_1)}{(1+k^2)^2}t_1^2$	0	0	0	0
$\tau_{1+}^{\#1}\dagger\alpha\beta$	$\frac{i\sqrt{2}k}{t_1+k^2}t_1$	$\frac{i(2k^3r_1-k t_1)}{(1+k^2)^2}t_1^2$	$\frac{-2k^4r_1+k^2t_1}{(1+k^2)^2}t_1^2$	$\frac{2(t_1+t_3)}{3t_1t_3}$	$-\frac{\sqrt{2}(t_1-2t_3)}{3(1+2k^2)}t_1t_3$	0	$-\frac{2ik t_1-4ikt_3}{3t_1t_3+6k^2t_1t_3}$
$\sigma_{1-}^{\#1}\dagger\alpha$	0	0	0	0	0	0	0
$\sigma_{1-}^{\#2}\dagger\alpha$	0	0	0	0	0	0	0
$\tau_{1-}^{\#1}\dagger\alpha$	0	0	0	0	0	0	0
$\tau_{1-}^{\#2}\dagger\alpha$	0	0	0	$\frac{2ik(t_1-2t_3)}{3t_1t_3+6k^2t_1t_3}$	$-\frac{i\sqrt{2}k(t_1+4t_3)}{3(1+2k^2)^2}t_1t_3$	0	$\frac{2k^2(t_1+4t_3)}{3(1+2k^2)^2}t_1t_3$

	$\omega_{1+}^{\#1}\dagger\alpha\beta$	$\omega_{1+}^{\#2}\dagger\alpha\beta$	$\omega_{1-}^{\#1}\alpha$	$\omega_{1-}^{\#2}\alpha$	$f_{1-}^{\#1}\alpha$	$f_{1-}^{\#2}\alpha$
$\omega_{1+}^{\#1}\dagger\alpha\beta$	$k^2r_1-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	0	0	0
$\omega_{1+}^{\#2}\dagger\alpha\beta$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$f_{1+}^{\#1}\dagger\alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0	0
$\omega_{1-}^{\#1}\dagger\alpha$	0	0	$\frac{1}{6}(t_1+4t_3)$	$\frac{t_1-2t_3}{3\sqrt{2}}$	0	$\frac{1}{3}ik(t_1-2t_3)$
$\omega_{1-}^{\#2}\dagger\alpha$	0	0	$\frac{t_1-2t_3}{3\sqrt{2}}$	$\frac{t_1+t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}k(t_1+t_3)$
$f_{1-}^{\#1}\dagger\alpha$	0	0	0	0	0	0
$f_{1-}^{\#2}\dagger\alpha$	0	0	$-\frac{1}{3}ik(t_1-2t_3)$	$-\frac{1}{3}i\sqrt{2}k(t_1+t_3)$	0	$\frac{2}{3}k^2(t_1+t_3)$

	$\sigma_{0+}^{\#1}\dagger$	$\sigma_{0+}^{\#2}\dagger$	$\tau_{0+}^{\#1}\dagger$	$\tau_{0+}^{\#2}\dagger$	$\sigma_{0-}^{\#1}\dagger$
$\sigma_{0+}^{\#1}\dagger$	0	0	$\frac{1}{(1+2k^2)^2}t_3$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2}t_3$	0
$\tau_{0+}^{\#1}\dagger$	$\frac{i\sqrt{2}k}{(1+2k^2)^2}t_3$	$\frac{2k^2}{(1+2k^2)^2}t_3$	0	0	0
$\sigma_{0+}^{\#2}\dagger$	0	0	0	0	0
$\tau_{0-}^{\#1}\dagger$	0	0	0	0	$-\frac{1}{t_1}$

	$\sigma_{2+}^{\#1}\dagger\alpha\beta$	$\tau_{2+}^{\#1}\alpha\beta$	$\sigma_{2-}^{\#1}\alpha\beta\chi$
$\sigma_{2+}^{\#1}\dagger\alpha\beta$	$\frac{2}{(1+2k^2)^2}t_1$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2}t_1$	0
$\tau_{2+}^{\#1}\dagger\alpha\beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2}t_1$	$\frac{4k^2}{(1+2k^2)^2}t_1$	0
$\sigma_{2-}^{\#1}\dagger\alpha\beta\chi$	0	0	$\frac{2}{2k^2r_1+t_1}$

	$\omega_{0+}^{\#1}\dagger$	$f_{0+}^{\#1}\dagger$	$f_{0+}^{\#2}\dagger$	$\omega_{0-}^{\#1}\dagger$
$\omega_{0+}^{\#1}\dagger$	t_3	$-i\sqrt{2}kt_3$	0	0
$f_{0+}^{\#1}\dagger$	$i\sqrt{2}kt_3$	$2k^2t_3$	0	0
$f_{0+}^{\#2}\dagger$	0	0	0	0
$\omega_{0-}^{\#1}\dagger$	0	0	0	$-t_1$

Source constraints	#
SO(3) irreps	1
$\tau_{0+}^{\#2}==0$	1
$\tau_{0+}^{\#1}-2ik\sigma_{0+}^{\#1}==0$	3
$\tau_{1-}^{\#2\alpha}+2ik\sigma_{1-}^{\#2\alpha}==0$	3
$\tau_{1-}^{\#1\alpha}==0$	3
$\tau_{1+}^{\#1\alpha\beta}+ik\sigma_{1+}^{\#2\alpha\beta}==0$	5
$\tau_{2+}^{\#1\alpha\beta}-2ik\sigma_{2+}^{\#1\alpha\beta}==0$	16
Total #:	

	$\omega_{2+}^{\#1}\dagger\alpha\beta$	$f_{2+}^{\#1}\dagger\alpha\beta$	$\omega_{2-}^{\#1}\alpha\beta\chi$
$\omega_{2+}^{\#1}\dagger\alpha\beta$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2+}^{\#1}\dagger\alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	k^2t_1	0
$\omega_{2-}^{\#1}\dagger\alpha\beta\chi$	0	0	$k^2r_1+\frac{t_1}{2}$