

PSALTer results panel

$$S = \iiint \bigg(\frac{1}{6} (6 \, \mathcal{A}^{\alpha\beta\chi} \, \sigma_{\alpha\beta\chi} + 6 \, f^{\alpha\beta} \, \tau (\Delta + \mathcal{K})_{\alpha\beta} - 3 \, r_{\frac{2}{3}} \partial_{\beta} \mathcal{A}_{\frac{1}{\theta}}^{\theta} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} - 3 \, r_{\frac{2}{3}} \partial_{\frac{1}{\theta}} \mathcal{A}_{\beta}^{\theta} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} - 3 \, r_{\frac{2}{3}} \partial_{\alpha} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} \partial_{\theta} \mathcal{A}_{\beta}^{\theta} + 6 \, r_{\frac{2}{3}} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} \partial_{\theta} \mathcal{A}_{\beta}^{\theta} - 3 \, r_{\frac{2}{3}} \partial_{\alpha} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} \partial_{\theta} \mathcal{A}_{\frac{1}{\beta}}^{\theta} + 6 \, r_{\frac{2}{3}} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} \partial_{\theta} \mathcal{A}_{\frac{1}{\beta}}^{\theta} + 8 \, r_{\frac{2}{2}} \partial_{\beta} \mathcal{A}_{\alpha\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} -$$
$$4 \, r_{\frac{2}{2}} \partial_{\beta} \mathcal{A}_{\alpha\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} + 4 \, r_{\frac{2}{2}} \partial_{\beta} \mathcal{A}_{\frac{1}{\theta\alpha}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} - 24 \, r_{\frac{2}{3}} \partial_{\beta} \mathcal{A}_{\frac{1}{\theta\alpha}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} - 2 \, r_{\frac{2}{2}} \partial_{\frac{1}{\theta}} \mathcal{A}_{\alpha\beta\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} + 2 \, r_{\frac{2}{2}} \partial_{\theta} \mathcal{A}_{\alpha\beta_{\frac{1}{\theta}}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} - 4 \, r_{\frac{2}{2}} \partial_{\theta} \mathcal{A}_{\alpha\frac{1}{\beta}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} + 6 \, r_{\frac{2}{5}} \partial_{\frac{1}{\theta}} \mathcal{A}_{\theta}^{\kappa} \partial^{\theta} \mathcal{A}^{\alpha_{\frac{1}{\theta}}} -$$
$$6 \, r_{\frac{2}{5}} \partial_{\theta} \mathcal{A}_{\frac{1}{\theta}^{\kappa}} \partial^{\theta} \mathcal{A}^{\alpha_{\frac{1}{\theta}}} + 4 \, t_{\frac{2}{2}} \mathcal{A}_{\frac{1}{\theta\alpha}} \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}} + 2 \, t_{\frac{2}{2}} \partial_{\alpha} f_{\frac{1}{\theta}} \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}} - t_{\frac{2}{2}} \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}} - t_{\frac{2}{2}} \partial_{\frac{1}{\theta}} f_{\alpha\theta} \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}} + t_{\frac{2}{2}} \partial_{\theta} f_{\alpha\frac{1}{\theta}} \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}} - t_{\frac{2}{2}} \partial_{\theta} f_{\frac{1}{\alpha}} \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}} - 4 \, t_{\frac{2}{2}} \mathcal{A}_{\alpha\theta_{\frac{1}{\theta}}} (\mathcal{A}^{\alpha_{\frac{1}{\theta}}} + \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}}) +$$
$$2 \, t_{\frac{2}{2}} \mathcal{A}_{\alpha\frac{1}{\theta}} (\mathcal{A}^{\alpha_{\frac{1}{\theta}}} + 2 \partial^{\theta} f^{\alpha_{\frac{1}{\theta}}}) - 6 \, r_{\frac{2}{5}} \partial_{\alpha} \mathcal{A}^{\alpha_{\frac{1}{\theta}}} \partial_{\kappa} \mathcal{A}_{\frac{1}{\theta}}^{\kappa} + 12 \, r_{\frac{2}{5}} \partial^{\theta} \mathcal{A}^{\alpha_{\frac{1}{\theta}}} \partial_{\kappa} \mathcal{A}_{\frac{1}{\theta}}^{\kappa} + 6 \, r_{\frac{2}{5}} \partial_{\alpha} \mathcal{A}^{\alpha_{\frac{1}{\theta}}} \partial_{\kappa} \mathcal{A}_{\theta}^{\kappa} - 12 \, r_{\frac{2}{5}} \partial^{\theta} \mathcal{A}^{\alpha_{\frac{1}{\theta}}} \partial_{\kappa} \mathcal{A}_{\theta}^{\kappa}) [t, x, y, z] dz dy dx dt$$

Wave operator

$0^+ \mathcal{A}^{\parallel}$	$0^+ f^{\parallel}$	$0^+ f^{\perp}$	$0^- \mathcal{A}^{\parallel}$										
$0^+ \mathcal{A}^{\parallel} \uparrow$	0	0	0	0									
$0^+ f^{\parallel} \uparrow$	0	0	0	0									
$0^+ f^{\perp} \uparrow$	0	0	0	0									
$0^- \mathcal{A}^{\parallel} \uparrow$	0	0	0	$k^2 r_{\frac{2}{2}} + t_{\frac{2}{2}}$	$1^+ \mathcal{A}^{\parallel}_{\alpha\beta}$	$1^+ \mathcal{A}^{\perp}_{\alpha\beta}$	$1^+ f^{\parallel}_{\alpha\beta}$	$1^- \mathcal{A}^{\parallel}_{\alpha}$	$1^- \mathcal{A}^{\perp}_{\alpha}$	$1^- f^{\parallel}_{\alpha}$	$1^- f^{\perp}_{\alpha}$		
$1^+ \mathcal{A}^{\parallel} \uparrow^{\alpha\beta}$	$k^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) + \frac{2 t_{\frac{2}{2}}}{3}$				$\frac{\sqrt{2} t_{\frac{2}{2}}}{3}$	$\frac{1}{3} i \sqrt{2} k t_{\frac{2}{2}}$							
$1^+ \mathcal{A}^{\perp} \uparrow^{\alpha\beta}$	$\frac{\sqrt{2} t_{\frac{2}{2}}}{3}$				$\frac{t_{\frac{2}{2}}}{3}$	$\frac{i k t_{\frac{2}{2}}}{3}$							
$1^+ f^{\parallel} \uparrow^{\alpha\beta}$	$-\frac{1}{3} i \sqrt{2} k t_{\frac{2}{2}}$				$-\frac{1}{3} i k t_{\frac{2}{2}}$	$\frac{k^2 t_{\frac{2}{2}}}{3}$							
$1^- \mathcal{A}^{\parallel} \uparrow^{\alpha}$	0				0	0	$\frac{1}{2} k^2 (r_{\frac{2}{3}} + 2 r_{\frac{2}{5}})$	0	0	0			
$1^- \mathcal{A}^{\perp} \uparrow^{\alpha}$	0				0	0	0	0	0	0			
$1^- f^{\parallel} \uparrow^{\alpha}$	0				0	0	0	0	0	0			
$1^- f^{\perp} \uparrow^{\alpha}$	0				0	0	0	0	0	0	$2^+ \mathcal{A}^{\parallel}_{\alpha\beta} \quad 2^+ f^{\parallel}_{\alpha\beta} \quad 2^- \mathcal{A}^{\parallel}_{\alpha\beta\chi}$		
								$2^+ \mathcal{A}^{\parallel} \uparrow^{\alpha\beta}$		$-\frac{3 k^2 r_{\frac{2}{3}}}{2}$		0	0
								$2^+ f^{\parallel} \uparrow^{\alpha\beta}$		0		0	0
								$2^- \mathcal{A}^{\parallel} \uparrow^{\alpha\beta\chi}$		0		0	0

Saturated propagator

$0^+ \sigma^{\parallel} \uparrow$	$0^+ \tau^{\parallel} \uparrow$	$0^+ \tau^{\perp} \uparrow$	$0^- \sigma^{\parallel} \uparrow$													
$0^+ \sigma^{\parallel} \uparrow$	0	0	0	0												
$0^+ \tau^{\parallel} \uparrow$	0	0	0	0												
$0^+ \tau^{\perp} \uparrow$	0	0	0	0												
$0^- \sigma^{\parallel} \uparrow$	0	0	0	$\frac{1}{k^2 r_{\frac{2}{2}} + t_{\frac{2}{2}}}$	$1^+ \sigma^{\parallel}_{\alpha\beta}$	$1^+ \sigma^{\perp}_{\alpha\beta}$	$1^+ \tau^{\parallel}_{\alpha\beta}$	$1^- \sigma^{\parallel}_{\alpha}$	$1^- \sigma^{\perp}_{\alpha}$	$1^- \tau^{\parallel}_{\alpha}$	$1^- \tau^{\perp}_{\alpha}$					
$1^+ \sigma^{\parallel} \uparrow^{\alpha\beta}$	$\frac{1}{k^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}})}$				$-\frac{\sqrt{2}}{k^2 (1 + k^2) (2 r_{\frac{2}{3}} + r_{\frac{2}{5}})}$				$-\frac{i \sqrt{2}}{k (1 + k^2) (2 r_{\frac{2}{3}} + r_{\frac{2}{5}})}$				0	0	0	0
$1^+ \sigma^{\perp} \uparrow^{\alpha\beta}$	$-\frac{\sqrt{2}}{k^2 (1 + k^2) (2 r_{\frac{2}{3}} + r_{\frac{2}{5}})}$				$\frac{3 k^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) + 2 t_{\frac{2}{2}}}{(k + k^2)^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) t_{\frac{2}{2}}}$				$\frac{i (3 k^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) + 2 t_{\frac{2}{2}})}{k (1 + k^2)^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) t_{\frac{2}{2}}}$				0	0	0	0
$1^+ \tau^{\parallel} \uparrow^{\alpha\beta}$	$\frac{i \sqrt{2}}{k (1 + k^2) (2 r_{\frac{2}{3}} + r_{\frac{2}{5}})}$				$-\frac{i (3 k^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) + 2 t_{\frac{2}{2}})}{k (1 + k^2)^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) t_{\frac{2}{2}}}$				$\frac{3 k^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) + 2 t_{\frac{2}{2}}}{(1 + k^2)^2 (2 r_{\frac{2}{3}} + r_{\frac{2}{5}}) t_{\frac{2}{2}}}$				0	0	0	0
$1^- \sigma^{\parallel} \uparrow^{\alpha}$	0				0				0				$\frac{2}{k^2 (r_{\frac{2}{3}} + 2 r_{\frac{2}{5}})}$	0	0	0
$1^- \sigma^{\perp} \uparrow^{\alpha}$	0				0				0				0	0	0	0
$1^- \tau^{\parallel} \uparrow^{\alpha}$	0				0				0				0	0	0	0
$1^- \tau^{\perp} \uparrow^{\alpha}$	0				0				0				0	0	0	0
$2^+ \sigma^{\parallel}_{\alpha\beta} \quad 2^+ \tau^{\parallel}_{\alpha\beta} \quad 2^- \sigma^{\parallel}_{\alpha\beta\chi}$																
$2^+ \sigma^{\parallel} \uparrow^{\alpha\beta}$																
														$-\frac{2}{3 k^2 r_{\frac{2}{3}}}$	0	0
$2^+ \tau^{\parallel} \uparrow^{\alpha\beta}$																
														0	0	0
$2^- \sigma^{\parallel} \uparrow^{\alpha\beta\chi}$																
														0	0	0

Source constraints

Spin-parity form	Covariant form	Multiplicities
$0^+ \tau^{\perp} == 0$	$\partial_{\beta} \partial_{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} == 0$	1
$0^+ \tau^{\parallel} == 0$	$\partial_{\beta} \partial_{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} == \partial_{\beta} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha}_{\alpha}$	1
$0^+ \sigma^{\parallel} == 0$	$\partial_{\beta} \sigma^{\alpha\beta} == 0$	1
$1^- \tau^{\perp\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} == \partial_{\chi} \partial^{\chi} \partial_{\beta} \tau (\Delta + \mathcal{K})^{\alpha\beta}$	3
$1^- \tau^{\parallel\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} == \partial_{\chi} \partial^{\chi} \partial_{\beta} \tau (\Delta + \mathcal{K})^{\beta\alpha}$	3
$1^- \sigma^{\perp\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \sigma^{\beta\alpha\chi} == 0$	3
$i k \, 1^+ \sigma^{\perp\alpha\beta} + 1^+ \tau^{\parallel\alpha\beta} == 0$	$\partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} + \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\chi\alpha} + \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \, \partial_{\delta} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\beta\delta} + 2 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \sigma^{\chi\alpha\beta} == \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\beta} + \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha\chi} + \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \, \partial_{\delta} \partial_{\chi} \partial^{\beta} \sigma^{\chi\alpha\delta}$	3
$2^- \sigma^{\parallel\alpha\beta\chi} == 0$	$3 \, \partial_{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\delta\beta\epsilon} + 3 \, \partial_{\epsilon} \partial^{\epsilon} \partial^{\chi} \sigma^{\delta\beta}_{\delta} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\chi\delta}_{\delta} + 4 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\chi\alpha\delta} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\delta\alpha\chi} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\beta\alpha\delta} + 4 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\delta\alpha\beta} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\alpha\beta\chi} +$ $3 \, \eta^{\beta\chi} \, \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\alpha} \sigma^{\delta}_{\delta}{}^{\epsilon} + 3 \, \eta^{\alpha\chi} \, \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\delta} \sigma^{\delta\beta\epsilon} + 3 \, \eta^{\beta\chi} \, \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\epsilon} \sigma^{\delta\alpha}_{\delta} == 3 \, \partial_{\epsilon} \partial_{\delta} \partial^{\chi} \partial^{\beta} \sigma^{\delta\alpha\epsilon} + 3 \, \partial_{\epsilon} \partial^{\epsilon} \partial^{\chi} \partial^{\beta} \sigma^{\delta\alpha}_{\delta} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\beta\chi\delta} + 4 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\chi\beta\delta} +$ $2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\delta\beta\chi} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\alpha\beta\delta} + 2 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\beta\alpha\chi} + 4 \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\chi\alpha\beta} + 3 \, \eta^{\alpha\chi} \, \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\beta} \sigma^{\delta}_{\delta}{}^{\epsilon} + 3 \, \eta^{\beta\chi} \, \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\delta} \sigma^{\delta\alpha\epsilon} + 3 \, \eta^{\alpha\chi} \, \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\epsilon} \sigma^{\delta\beta}_{\delta}$	5
$2^+ \tau^{\parallel\alpha\beta} == 0$	$4 \, \partial_{\delta} \partial_{\chi} \partial^{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\delta} + 2 \, \partial_{\delta} \partial^{\delta} \partial^{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi}_{\chi}{}^{\alpha} + 3 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 3 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \, \eta^{\alpha\beta} \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial_{\chi} \tau (\Delta + \mathcal{K})^{\chi\delta} ==$ $3 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} + 3 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\beta} + 3 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha\chi} + 3 \, \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\chi\alpha} + 2 \, \eta^{\alpha\beta} \, \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \tau (\Delta + \mathcal{K})^{\chi}_{\chi}{}^{\alpha}$	5
Total expected gauge generators:		25

Massive spectrum

Massive particle

Pole residue:	$-\frac{1}{r_{\frac{2}{2}}} > 0$
Square mass:	$-\frac{t_{\frac{2}{2}}}{r_{\frac{2}{2}}} > 0$
Spin:	0
Parity:	Odd

Massless spectrum

Massless particle

Pole residue:	$-\frac{2}{r_{\frac{2}{3}}} + \frac{7}{2 r_{\frac{2}{3}} + r_{\frac{2}{5}}} - \frac{24}{r_{\frac{2}{3}} + 2 r_{\frac{2}{5}}} > 0$
Polarisations:	2

Unitarity conditions

$$r_{\frac{2}{2}} < 0 \ \& \ t_{\frac{2}{2}} > 0 \ \& \ ((r_{\frac{2}{3}} < 0 \ \& \ (r_{\frac{2}{5}} < -\frac{r_{\frac{2}{3}}}{2} \ || \ r_{\frac{2}{5}} > -2 r_{\frac{2}{3}})) \ || \ (r_{\frac{2}{3}} > 0 \ \& \ -2 r_{\frac{2}{3}} < r_{\frac{2}{5}} < -\frac{r_{\frac{2}{3}}}{2}))$$