



$a_0 < 0$

Unitarity conditions

(No massive particles)

$\Delta_{1^+}^{\#1} \dagger \alpha\beta$	$\Delta_{1^+}^{\#2} \dagger \alpha\beta$	$\Delta_{1^+}^{\#3} \dagger \alpha\beta$	$\Delta_{1^+}^{\#1} \dagger \alpha$	$\Delta_{1^+}^{\#2} \dagger \alpha$	$\Delta_{1^+}^{\#3} \dagger \alpha$	$\Delta_{1^+}^{\#4} \dagger \alpha$	$\Delta_{1^+}^{\#5} \dagger \alpha$	$\Delta_{1^+}^{\#6} \dagger \alpha$	$\mathcal{T}_{1^+}^{\#1} \dagger \alpha$
$\Delta_{1^+}^{\#1} \dagger \alpha\beta$	0	$-\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0	0
$\Delta_{1^+}^{\#2} \dagger \alpha\beta$	$-\frac{2\sqrt{2}}{a_0}$	$\frac{2}{a_0}$	0	0	0	0	0	0	0
$\Delta_{1^+}^{\#3} \dagger \alpha\beta$	0	0	$\frac{4}{a_0}$	0	0	0	0	0	0
$\Delta_{1^+}^{\#1} \dagger \alpha$	0	0	0	$\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0
$\Delta_{1^+}^{\#2} \dagger \alpha$	0	0	$\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0
$\Delta_{1^+}^{\#3} \dagger \alpha$	0	0	0	0	$-\frac{19}{12a_0}$	$-\frac{5\sqrt{5}}{12a_0}$	$-\frac{1}{6\sqrt{2}a_0}$	$-\frac{1}{6a_0}$	0
$\Delta_{1^+}^{\#4} \dagger \alpha$	0	0	0	0	$\frac{5\sqrt{5}}{12a_0}$	$\frac{1}{12a_0}$	$-\frac{\sqrt{5}}{6a_0}$	$-\frac{\sqrt{5}}{6a_0}$	0
$\Delta_{1^+}^{\#5} \dagger \alpha$	0	0	0	0	$-\frac{1}{6\sqrt{2}a_0}$	$-\frac{\sqrt{5}}{6a_0}$	$-\frac{17}{6a_0}$	$-\frac{7}{3\sqrt{2}a_0}$	0
$\Delta_{1^+}^{\#6} \dagger \alpha$	0	0	0	0	$-\frac{1}{6a_0}$	$-\frac{\sqrt{5}}{6a_0}$	$-\frac{7}{3\sqrt{2}a_0}$	$\frac{5}{3a_0}$	0
$\mathcal{T}_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0	0	0

$\Gamma_{1^+}^{\#1} \dagger \alpha\beta$	$\Gamma_{1^+}^{\#2} \dagger \alpha\beta$	$\Gamma_{1^+}^{\#3} \dagger \alpha\beta$	$\Gamma_{1^+}^{\#1} \dagger \alpha$	$\Gamma_{1^+}^{\#2} \dagger \alpha$	$\Gamma_{1^+}^{\#3} \dagger \alpha$	$\Gamma_{1^+}^{\#4} \dagger \alpha$	$\Gamma_{1^+}^{\#5} \dagger \alpha$	$\Gamma_{1^+}^{\#6} \dagger \alpha$	$h_{1^+}^{\#1} \dagger \alpha$
$\Gamma_{1^+}^{\#1} \dagger \alpha\beta$	$-\frac{a_0}{4}$	0	0	0	0	0	0	0	0
$\Gamma_{1^+}^{\#2} \dagger \alpha\beta$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0	0	0
$\Gamma_{1^+}^{\#3} \dagger \alpha\beta$	0	$\frac{a_0}{4}$	0	0	0	0	0	0	0
$\Gamma_{1^+}^{\#1} \dagger \alpha$	0	0	$-\frac{a_0}{4}$	$\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0
$\Gamma_{1^+}^{\#2} \dagger \alpha$	0	0	$\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0
$\Gamma_{1^+}^{\#3} \dagger \alpha$	0	0	0	0	$-\frac{a_0}{3}$	$\frac{\sqrt{5}a_0}{6}$	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{a_0}{6}$	0
$\Gamma_{1^+}^{\#4} \dagger \alpha$	0	0	0	0	$\frac{\sqrt{5}a_0}{6}$	$\frac{a_0}{3}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}a_0$	$-\frac{\sqrt{5}a_0}{6}$	0
$\Gamma_{1^+}^{\#5} \dagger \alpha$	0	0	0	0	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}a_0$	$\frac{a_0}{3}$	$\frac{a_0}{6\sqrt{2}}$	0
$\Gamma_{1^+}^{\#6} \dagger \alpha$	0	0	0	0	$-\frac{a_0}{6}$	$-\frac{\sqrt{5}a_0}{6}$	$\frac{a_0}{6\sqrt{2}}$	$\frac{5a_0}{12}$	0
$h_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0	0	0

Lagrangian density

$$\begin{aligned}
&-\frac{1}{2}a_0\,\Gamma^{\alpha\beta\chi}_{\beta\chi\alpha}+\frac{1}{2}a_0\,\Gamma^{\alpha\,\beta\,\,\,\,\,\alpha}_{\alpha\,\,\,\,\,\beta}\,\Gamma^{\chi\,\,\,\,\,\beta\chi\,\,\,\,\,\alpha}{}^-\\
&\frac{1}{2}a_0\,\Gamma^{\alpha\beta\chi}_{\beta\beta}h_{\alpha\chi}{}^--\frac{1}{4}a_0\,\Gamma^{\alpha\,\beta\,\,\,\,\,\beta}_{\alpha\,\,\,\,\,\beta}h_{\chi\,\,\,\,\,\chi}^{\chi}+\frac{1}{4}a_0\,\Gamma^{\alpha\beta}_{\alpha}\,\Gamma^{\alpha\beta}_{\beta}h_{\chi\,\,\,\,\,\chi}^{\chi}{}^-\\
&\frac{1}{4}a_0\,h_{\chi\,\,\,\,\,\chi}^{\chi}\,\partial_{\beta}\Gamma^{\alpha}_{\alpha}{}^{\beta}+\frac{1}{4}a_0\,h_{\chi\,\,\,\,\,\chi}^{\chi}\,\partial_{\beta}\Gamma^{\alpha\beta}_{\alpha}{}^{\beta}-\frac{1}{2}a_0\,h_{\alpha\chi}\,\partial_{\beta}\Gamma^{\alpha\beta\chi}_{\alpha}{}^{\beta\chi}+\\
&\frac{1}{2}a_0\,h_{\alpha\beta}^{\alpha\beta}\,\partial_{\beta}\partial_{\alpha}h_{\chi\,\,\,\,\,\chi}^{\chi}{}^--\frac{1}{8}a_0\,\partial_{\beta}h_{\chi\,\,\,\,\,\chi}^{\chi}\,\partial^{\beta}h_{\alpha}{}^{\alpha}+\frac{1}{2}a_0\,\Gamma^{\alpha}_{\alpha}\,\Gamma^{\alpha}_{\beta}h_{\chi\,\,\,\,\,\chi}^{\chi}{}^-\\
&\frac{1}{2}a_0\,\partial_{\alpha}h^{\alpha\beta}_{\chi}h_{\beta}^{\chi}+\frac{1}{2}a_0\,\partial_{\beta}h^{\alpha}_{\chi}\,\partial^{\beta}h_{\alpha}{}^{\chi}-a_0\,h^{\alpha\beta}_{\chi}\,\partial_{\chi}\partial_{\beta}h_{\alpha}{}^{\chi}+\\
&\frac{1}{4}a_0\,h_{\alpha}{}^{\alpha}\,\partial_{\chi}\partial_{\beta}h^{\beta\chi}_{\alpha}+\frac{1}{2}a_0\,h^{\alpha\beta}_{\chi}\,\partial_{\chi}\partial^{\chi}h_{\alpha\beta}{}^--\frac{1}{4}a_0\,h_{\alpha}{}^{\alpha}\,\partial_{\chi}\partial^{\chi}h_{\beta}^{\beta}{}^-\\
&\frac{1}{4}a_0\,\partial_{\beta}h_{\alpha\chi}^{\chi}\,\partial^{\chi}h^{\alpha\beta}_{\alpha}+\frac{3}{8}a_0\,\partial_{\chi}h_{\alpha\beta}^{\chi}\,\partial^{\chi}h^{\alpha\beta}_{\alpha}+\frac{1}{2}a_0\,h_{\beta\chi}\,\partial^{\chi}\Gamma^{\alpha}_{\alpha}{}^{\beta}{}^-
\end{aligned}$$

Added source term:

$h^{\alpha\beta}\,\mathcal{T}_{\alpha\beta}+\Gamma^{\alpha\beta\chi}_{\alpha\beta\chi}\,\Delta_{\alpha\beta\chi}$

	$\Delta_{2^+}^{\#1} \dagger \alpha\beta$	$\Delta_{2^+}^{\#2} \dagger \alpha\beta$	$\Delta_{2^+}^{\#3} \dagger \alpha\beta$	$\mathcal{T}_{2^+}^{\#1} \dagger \alpha\beta$	$\Delta_{2^+}^{\#1} \dagger \alpha\beta\chi$	$\Delta_{2^+}^{\#2} \dagger \alpha\beta\chi$
$\Delta_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{4}{a_0}$	0	0	0	0	0
$\Delta_{2^+}^{\#2} \dagger \alpha\beta$	0	$-\frac{2}{a_0}$	0	0	0	0
$\Delta_{2^+}^{\#3} \dagger \alpha\beta$	0	0	$\frac{4}{a_0}$	0	0	0
$\mathcal{T}_{2^+}^{\#1} \dagger \alpha\beta$	0	0	0	$-\frac{8}{a_0k^2}$	0	0
$\Delta_{2^+}^{\#1} \dagger \alpha\beta\chi$	0	0	0	0	$\frac{4}{a_0}$	0
$\Delta_{2^+}^{\#2} \dagger \alpha\beta\chi$	0	0	0	0	0	$\frac{4}{s_0}$

$\Gamma_{2^+}^{\#1} \dagger \alpha\beta$	$\Gamma_{2^+}^{\#2} \dagger \alpha\beta$	$\Gamma_{2^+}^{\#3} \dagger \alpha\beta$	$h_{2^+}^{\#1} \dagger \alpha\beta$	$\Gamma_{2^+}^{\#1} \dagger \alpha\beta\chi$	$\Gamma_{2^+}^{\#2} \dagger \alpha\beta\chi$
$\Gamma_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{a_0}{4}$	0	0	0	0
$\Gamma_{2^+}^{\#2} \dagger \alpha\beta$	0	$-\frac{a_0}{2}$	0	0	0
$\Gamma_{2^+}^{\#3} \dagger \alpha\beta$	0	0	$\frac{a_0}{4}$	0	0
$h_{2^+}^{\#1} \dagger \alpha\beta$	0	0	$-\frac{a_0k^2}{8}$	0	0
$\Gamma_{2^+}^{\#1} \dagger \alpha\beta\chi$	0	0	0	$\frac{a_0}{4}$	0
$\Gamma_{2^+}^{\#2} \dagger \alpha\beta\chi$	0	0	0	0	$\frac{a_0}{4}$

$\Gamma_{0^+}^{\#1} \dagger$	$\Gamma_{0^+}^{\#2} \dagger$	$\Gamma_{0^+}^{\#3} \dagger$	$\Gamma_{0^+}^{\#4} \dagger$	$h_{0^+}^{\#1} \dagger$	$h_{0^+}^{\#2} \dagger$	$\Gamma_{0^+}^{\#1} \dagger$
$\Gamma_{0^+}^{\#1} \dagger$	$-\frac{a_0}{2}$	0	0	0	0	0
$\Gamma_{0^+}^{\#2} \dagger$	0	$\frac{a_0}{2}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
$\Gamma_{0^+}^{\#3} \dagger$	0	$\frac{a_0}{2}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
$\Gamma_{0^+}^{\#4} \dagger$	0	$-\frac{a_0}{2\sqrt{2}}$	$\frac{a_0}{2}$	0	0	0
$h_{0^+}^{\#1} \dagger$	0	0	0	$\frac{a_0k^2}{4}$	0	0
$h_{0^+}^{\#2} \dagger$	0	0	0	0	0	0
$\Gamma_{0^+}^{\#1} \dagger$	0	0	0	0	0	$-\frac{a_0}{2}$

Source constraints

SO(3) irreps	#
$\mathcal{T}_{0^+}^{\#2} == 0$	1
$\Delta_{0^+}^{\#3} + 2\Delta_{0^+}^{\#4} + 3\Delta_{0^+}^{\#2} == 0$	1
$\mathcal{T}_{1^+}^{\#1\alpha} == 0$	3
$2\,\Delta_{1^+}^{\#6\alpha} + \Delta_{1^+}^{\#4\alpha} + 2\,\Delta_{1^+}^{\#5\alpha} + \Delta_{1^+}^{\#3\alpha} == 0$	3
Total #:	8