

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \alpha\beta$	$\tau_{1+}^{\#1} \alpha\beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\frac{1}{k^2(2r_3-r_4)}$	$-\frac{\sqrt{2}}{k^2(1+k^2)(2r_3-r_4)}$	$-\frac{i\sqrt{2}}{k(1+k^2)(2r_3-r_4)}$	0	0	0
$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{k^2(1+k^2)(2r_3-r_4)}$	$\frac{k^2(6r_3-3r_4)+2t_2}{(k+k^2)^2(2r_3-r_4)t_2}$	$\frac{i(k^2(6r_3-3r_4)+2t_2)}{k(1+k^2)^2(2r_3-r_4)t_2}$	0	0	0
$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\frac{i\sqrt{2}}{k(1+k^2)(2r_3-r_4)}$	$-\frac{i(k^2(6r_3-3r_4)+2t_2)}{k(1+k^2)^2(2r_3-r_4)t_2}$	$\frac{1}{r_3}\frac{3k^2}{2t_2}\frac{1}{(1+k^2)^2}$	0	0	0
$\sigma_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\sigma_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0

Quadratic (free) action

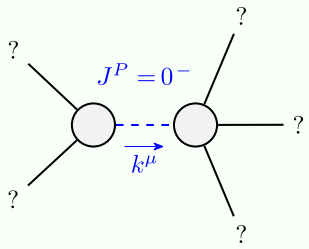
$S = \iiint (\frac{1}{6} f^{\alpha\beta} \tau_{\alpha\beta} + 6 \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + 4 t_2 \omega_{1\theta\alpha} \partial^\theta f^{\alpha i} + 2 t_2 \partial_\alpha f_{1\theta} \partial^\theta f^{\alpha i} - t_2 \partial_\alpha f_{\theta i} \partial^\theta f^{\alpha i} - \partial^\theta f^{\alpha i} - t_2 \partial_i f_{\alpha\theta} \partial^\theta f^{\alpha i} + t_2 \partial_\theta f_{\alpha i} \partial^\theta f^{\alpha i} - t_2 \partial_\theta f_{i\alpha} \partial^\theta f^{\alpha i} - 4 t_2 \omega_{\alpha\theta i} (\omega^{\alpha i\theta} + \partial^\theta f^{\alpha i}) + 2 t_2 \omega_{\alpha i\theta} (\omega^{\alpha i\theta} + 2 \partial^\theta f^{\alpha i}) + 8 r_2 \partial_2 \omega_{\alpha i\theta} \partial^\theta \omega^{\alpha\beta i} - 4 r_2 \partial_\beta \omega_{\alpha\theta i} \partial^\theta \omega^{\alpha\beta i} + 4 r_2 \partial_\beta \omega_{1\theta\alpha} \partial^\theta \omega^{\alpha\beta i} - 2 r_2 \partial_i \omega_{\alpha\beta\theta} \partial^\theta \omega^{\alpha\beta i} + 2 r_2 \partial_\theta \omega_{\alpha\beta i} \partial^\theta \omega^{\alpha\beta i} - 4 r_2 \partial_\theta \omega_{\alpha i\beta} \partial^\theta \omega^{\alpha\beta i} - 12 r_4 \partial_\theta \omega_{\kappa\lambda} \partial^\kappa \omega^{\alpha\theta} - 12 r_4 \partial_\alpha \omega^{\alpha\theta\kappa} \partial_\lambda \omega_{\kappa\theta}^\lambda + 24 r_4 \partial^\kappa \omega^{\alpha\theta} \partial_\lambda \omega_{\kappa\theta}^\lambda - 24 r_3 \partial_\beta \omega_{1\lambda\alpha} \partial^\lambda \omega^{\alpha\beta i}) [t, x, y, z] dz dy dx dt$

$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#2} \alpha\beta$	$f_{1+}^{\#1} \alpha\beta$	$\omega_{1-}^{\#1} \alpha$	$\omega_{1-}^{\#2} \alpha$	$f_{1-}^{\#1} \alpha$	$f_{1-}^{\#2} \alpha$
$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$k^2(2r_3-r_4) + \frac{2t_2}{3}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0
$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0
$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{1}{3}i\sqrt{2}kt_2$	$-\frac{1}{3}ikt_2$	$\frac{k^2t_2}{3}$	0	0	0
$\omega_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\omega_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0

Source constraints/gauge generators	Multiplicities
SO(3) irreps	
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\sigma_{1-}^{\#2\alpha} == 0$	3
$\sigma_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	27

$\sigma_{0+}^{\#1} \dagger$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1} \dagger$	$\frac{1}{-2k^2r_3+4k^2r_4}$	0	0
$\tau_{0+}^{\#1} \dagger$	0	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0
$\sigma_{0-}^{\#1} \dagger$	0	0	$\frac{1}{k^2r_2+t_2}$
$\omega_{0+}^{\#1} \dagger$	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1} \dagger$	$-2k^2(r_3-2r_4)$	0	0
$f_{0+}^{\#1} \dagger$	0	0	0
$f_{0+}^{\#2} \dagger$	0	0	0
$\omega_{0-}^{\#1} \dagger$	0	0	$k^2r_2+t_2$
$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{2+}^{\#1} \alpha\beta$	$\tau_{2+}^{\#1} \alpha\beta$	$\sigma_{2-}^{\#1} \alpha\beta\chi$
$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{1}{k^2(-2r_3+r_4)}$	0	0
$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	0	0	0
$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	0

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(no massless particles)

Unitarity conditions

$r_2 < 0 \&\& t_2 > 0$