

## Wave operator and propagator

	$\sigma_{1+}^{\#1} \alpha \beta$	$\sigma_{1+}^{\#2} \alpha \beta$	$\tau_{1+}^{\#1} \alpha \beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\sigma_{1+}^{\#1} \uparrow \alpha \beta$	$\frac{1}{\frac{3(a_0-4\beta_1)(a_0+8\beta_3)}{16(\beta_1+2\beta_3)}+(a_2+a_5)k^2}$	$-\frac{2\sqrt{2}(3a_0-4\beta_1+16\beta_3)}{(1+k^2)(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	$-\frac{2i\sqrt{2}(3a_0-4\beta_1+16\beta_3)k}{(1+k^2)(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	0	0	0	0
$\sigma_{1+}^{\#2} \uparrow \alpha \beta$	$-\frac{2\sqrt{2}(3a_0-4\beta_1+16\beta_3)}{(1+k^2)(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	$\frac{6a_0+8(\beta_1+8\beta_3+3(a_2+a_5)k^2)}{(1+k^2)^2(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	$\frac{2ik(3a_0+4(\beta_1+8\beta_3+3(a_2+a_5)k^2))}{(1+k^2)^2(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	0	0	0	0
$\tau_{1+}^{\#1} \uparrow \alpha \beta$	$\frac{2i\sqrt{2}(3a_0-4\beta_1+16\beta_3)k}{(1+k^2)(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	$-\frac{2ik(3a_0+4(\beta_1+8\beta_3+3(a_2+a_5)k^2))}{(1+k^2)^2(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	$\frac{2k^2(3a_0+4(\beta_1+8\beta_3+3(a_2+a_5)k^2))}{(1+k^2)^2(-3(a_0-4\beta_1)(a_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$	0	0	0	0
$\sigma_{1-}^{\#1} \uparrow \alpha$	0	0	0	$\frac{1}{\frac{3(a_0-4\beta_1)(a_0+2\beta_2)}{8(2\beta_1+\beta_2)}+(a_4+a_5)k^2}$	$\frac{2\sqrt{2}(3a_0-4\beta_1+4\beta_2)}{(1+2k^2)(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$	0	$\frac{4i(3a_0-4\beta_1+4\beta_2)k}{(1+2k^2)(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$
$\sigma_{1-}^{\#2} \uparrow \alpha$	0	0	0	$\frac{2\sqrt{2}(3a_0-4\beta_1+4\beta_2)}{(1+2k^2)(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$	$\frac{6a_0+8(\beta_1+2\beta_2+3(a_4+a_5)k^2)}{(1+2k^2)^2(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$	0	$\frac{2i\sqrt{2}k(3a_0+4(\beta_1+2\beta_2+3(a_4+a_5)k^2))}{(1+2k^2)^2(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$
$\tau_{1-}^{\#1} \uparrow \alpha$	0	0	0	0	0	0	0
$\tau_{1-}^{\#2} \uparrow \alpha$	0	0	0	$-\frac{4i(3a_0-4\beta_1+4\beta_2)k}{(1+2k^2)(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$	$-\frac{2i\sqrt{2}k(3a_0+4(\beta_1+2\beta_2+3(a_4+a_5)k^2))}{(1+2k^2)^2(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$	0	$\frac{4k^2(3a_0+4(\beta_1+2\beta_2+3(a_4+a_5)k^2))}{(1+2k^2)^2(-3(a_0-4\beta_1)(a_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$

[illegible]

	$\omega_{1^+ \alpha \beta}^{\#1}$	$\omega_{1^+ \alpha \beta}^{\#2}$	$f_{1^+ \alpha \beta}^{\#1}$	$\omega_{1^+ \alpha}^{\#1}$	$\omega_{1^+ \alpha}^{\#2}$	$f_{1^+ \alpha}^{\#1}$	$f_{1^+ \alpha}^{\#2}$
$\omega_{1^+}^{\#1} \uparrow \alpha \beta$	$\frac{\alpha_0}{4} + \frac{1}{3} (\beta_1 + 8 \beta_3) + (\alpha_2 + \alpha_5) k^2$	$\frac{3 \alpha_0 - 4 \beta_1 + 16 \beta_3}{6 \sqrt{2}}$	$\frac{i (3 \alpha_0 - 4 \beta_1 + 16 \beta_3) k}{6 \sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2} \uparrow \alpha \beta$	$\frac{3 \alpha_0 - 4 \beta_1 + 16 \beta_3}{6 \sqrt{2}}$	$\frac{2}{3} (\beta_1 + 2 \beta_3)$	$\frac{2}{3} i (\beta_1 + 2 \beta_3) k$	0	0	0	0
$f_{1^+}^{\#1} \uparrow \alpha \beta$	$-\frac{i (3 \alpha_0 - 4 \beta_1 + 16 \beta_3) k}{6 \sqrt{2}}$	$-\frac{2}{3} i (\beta_1 + 2 \beta_3) k$	$\frac{2}{3} (\beta_1 + 2 \beta_3) k^2$	0	0	0	0
$\omega_{1^+}^{\#1} \uparrow \alpha$	0	0	0	$\frac{\alpha_0}{4} + \frac{1}{3} (\beta_1 + 2 \beta_2) + (\alpha_4 + \alpha_5) k^2$	$-\frac{3 \alpha_0 - 4 \beta_1 + 4 \beta_2}{6 \sqrt{2}}$	0	$-\frac{1}{6} i (3 \alpha_0 - 4 \beta_1 + 4 \beta_2) k$
$\omega_{1^+}^{\#2} \uparrow \alpha$	0	0	0	$-\frac{3 \alpha_0 - 4 \beta_1 + 4 \beta_2}{6 \sqrt{2}}$	$\frac{1}{3} (2 \beta_1 + \beta_2)$	0	$\frac{1}{3} i \sqrt{2} (2 \beta_1 + \beta_2) k$
$f_{1^+}^{\#1} \uparrow \alpha$	0	0	0	0	0	0	0
$f_{1^+}^{\#2} \uparrow \alpha$	0	0	0	$\frac{1}{6} i (3 \alpha_0 - 4 \beta_1 + 4 \beta_2) k$	$-\frac{1}{3} i \sqrt{2} (2 \beta_1 + \beta_2) k$	0	$\frac{2}{3} (2 \beta_1 + \beta_2) k^2$

	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_0^{\#1}$
$\omega_{0+}^{\#1} \dagger$	$\frac{\alpha_0}{2} + \beta_2 + (\alpha_4 + \alpha_6) k^2$	$-\frac{i(\alpha_0 + 2\beta_2)k}{\sqrt{2}}$	0	0
$f_{0+}^{\#1} \dagger$	$\frac{i(\alpha_0 + 2\beta_2)k}{\sqrt{2}}$	$2\beta_2 k^2$	0	0
$f_{0+}^{\#2} \dagger$	0	0	0	0
$\omega_0^{\#1} \dagger$	0	0	0	$\frac{\alpha_0}{2} + 4\beta_3 + (\alpha_2 + \alpha_3) k^2$

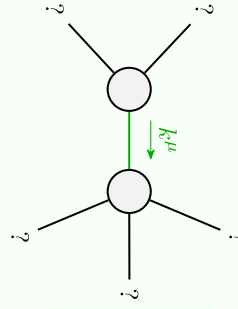
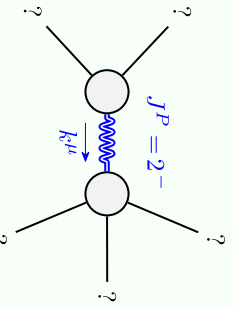
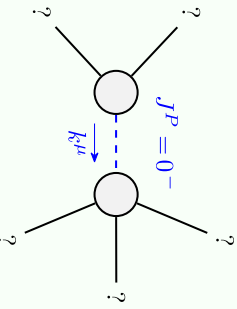
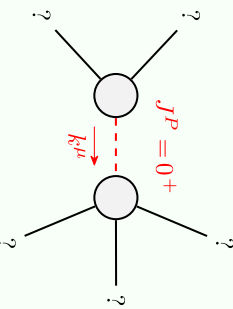
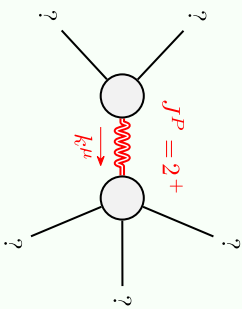
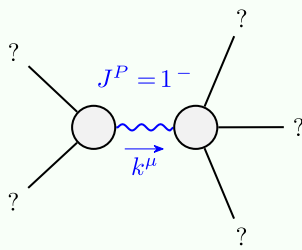
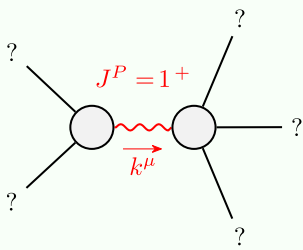
SO(3) irreps	Multiplicities
$\tau_{0+}^{\#2} = 0$	1
$\tau_1^{\#2\alpha} + 2ik\sigma_1^{\#2\alpha} = 0$	3
$\tau_1^{\#1\alpha} = 0$	3
$\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#2\alpha\beta} = 0$	3
Total constraints:	10

	$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_0^{\#1}$
$\sigma_{0+}^{\#1} \dagger$	$-\frac{4\beta_2}{\alpha_0^2 + 2\alpha_0\beta_2 - 4(\alpha_4 + \alpha_6)\beta_2 k^2}$	$\frac{i\sqrt{2}(\alpha_0 + 2\beta_2)}{-\alpha_0(\alpha_0 + 2\beta_2)k + 4(\alpha_4 + \alpha_6)\beta_2 k^3}$	0	0
$\tau_{0+}^{\#1} \dagger$	$\frac{i\sqrt{2}(\alpha_0 + 2\beta_2)}{\alpha_0(\alpha_0 + 2\beta_2)k - 4(\alpha_4 + \alpha_6)\beta_2 k^3}$	$\frac{\frac{\alpha_0}{2} + \beta_2 + (\alpha_4 + \alpha_6)k^2}{-\frac{1}{2}\alpha_0(\alpha_0 + 2\beta_2)k^2 + 2(\alpha_4 + \alpha_6)\beta_2 k^4}$	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0	0
$\sigma_0^{\#1} \dagger$	0	0	0	$\frac{2}{\alpha_0 + 8\beta_3 + 2(\alpha_2 + \alpha_3)k^2}$

	$\sigma_{2^+}^{\#1} \alpha\beta$	$\tau_{2^+}^{\#1} \alpha\beta$	$\sigma_{2^+}^{\#1} \alpha\beta\chi$
$\sigma_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{16\beta_1}{-a_0^2+4a_0\beta_1+16(a_1+a_4)\beta_1k^2}$	$\frac{2i\sqrt{2}(\alpha_0-4\beta_1)}{a_0(\alpha_0-4\beta_1)k-16(a_1+a_4)\beta_1k^3}$	0
$\tau_{2^+}^{\#1} \dagger \alpha\beta$	$-\frac{2i\sqrt{2}(\alpha_0-4\beta_1)}{a_0(\alpha_0-4\beta_1)k-16(a_1+a_4)\beta_1k^3}$	$\frac{2(\alpha_0-4(\beta_1+(a_1+a_4)k^2))}{k^2(\alpha_0^2-4a_0\beta_1-16(a_1+a_4)\beta_1k^2)}$	0
$\sigma_{2^+}^{\#1} \dagger \alpha\beta\chi$	0	0	$\frac{1}{-\frac{a_0}{4}+\beta_1+(a_1+a_2)k^2}$

	$\omega_2^{\#1} \uparrow \alpha\beta$	$f_2^{\#1} \uparrow \alpha\beta$	$\omega_2^{\#1} \uparrow \alpha\beta\chi$
$\omega_2^{\#1} \uparrow \alpha\beta$	$-\frac{\alpha_0}{4} + \beta_1 + (\alpha_1 + \alpha_4) k^2$	$\frac{i(\alpha_0 - 4\beta_1)k}{2\sqrt{2}}$	0
$f_2^{\#1} \uparrow \alpha\beta$	$-\frac{i(\alpha_0 - 4\beta_1)k}{2\sqrt{2}}$	$2\beta_1 k^2$	0
$\omega_2^{\#1} \uparrow \alpha\beta\chi$	0	0	$-\frac{\alpha_0}{4} + \beta_1 + (\alpha_1 + \alpha_2) k^2$

## Massive and massless spectra



Massive particle	
Pole residue:	$\frac{(3(\alpha_0^2(3\alpha_2+3\alpha_5+2\beta_1+4\beta_3)-8\alpha_0(\beta_1^2+\alpha_2(\beta_1-4\beta_3)+\alpha_5(\beta_1-4\beta_3)-4\beta_3^2)+16(-4\beta_1\beta_3(\beta_1+2\beta_3)+\alpha_2(\beta_1^2+8\beta_3^2)+\alpha_5(\beta_1^2+8\beta_3^2))))}{(2(\alpha_2+\alpha_5)(\beta_1+2\beta_3)(3\alpha_0^2-12\alpha_0(\beta_1-2\beta_3)+16(\alpha_5\beta_1+2\alpha_5\beta_3-6\beta_1\beta_3+\alpha_2(\beta_1+2\beta_3))))} > 0$
Polarisations:	3
Square mass:	$\frac{3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)}{16(\alpha_2+\alpha_5)(\beta_1+2\beta_3)} > 0$
Spin:	1
Parity:	Even

Massive particle	
Pole residue:	$-((3(\alpha_0^2(3\alpha_4 + 3\alpha_5 + 4\beta_1 + 2\beta_2) + 4\alpha_0(-2\alpha_4\beta_1 - 2\alpha_5\beta_1 - 4\beta_1^2 + 2\alpha_4\beta_2 + 2\alpha_5\beta_2 + \beta_2^2) + 8(-2\beta_1\beta_2(2\beta_1 + \beta_2) + \alpha_4(2\beta_1^2 + \beta_2^2) + \alpha_5(2\beta_1^2 + \beta_2^2)))))/(2(\alpha_4 + \alpha_5)(2\beta_1 + \beta_2)(3\alpha_0^2 + 6\alpha_0(-2\beta_1 + \beta_2) + 4(2\alpha_5\beta_1 + \alpha_5\beta_2 - 6\beta_1\beta_2 + \alpha_4(2\beta_1 + \beta_2)))))) > 0$
Polarisations:	3
Square mass:	$\frac{3(\alpha_0 - 4\beta_1)(\alpha_0 + 2\beta_2)}{8(\alpha_4 + \alpha_5)(2\beta_1 + \beta_2)} > 0$
Spin:	1
Parity:	Odd

Massive particle	
Pole residue:	$-\frac{2}{a_0} + \frac{(a_1 + a_2 + 2\beta_1)}{2\alpha_1\beta_1 + 2\alpha_2\beta_1} > 0$
Polarisations:	5
Square mass:	$\frac{a_0(a_0^2 - 4\beta_1)}{16(\alpha_1 + \alpha_2)\beta_1} > 0$
Spin:	2
Parity:	Even

Massive particle	
Pole residue:	$\frac{1}{a_0} > 0$ $\frac{a_4+a_6+2\beta_2}{2a_4\beta_2+2a_6\beta_2}$
Polarisations:	1
Square mass:	$a_0(a_0+2\beta_2) > 0$ $4(a_4+a_6)\beta_2$
Spin:	0
Parity:	Even

Massive particle	
Pole residue:	$-\frac{1}{a_2+a_3} > 0$
Polarisations:	1
Square mass:	$-\frac{a_0+8\beta_3}{2(a_2+a_3)} > 0$
Spin:	0
Parity:	Odd

Massive particle	
Pole residue:	$-\frac{1}{a_1+a_2} > 0$
Polarisations:	5
Square mass:	$\frac{\alpha_0^{-4} \beta_1}{4(a_1+a_2)} > 0$
Spin:	2
Parity:	Odd

Quadratic pole	
Pole residue:	$\frac{1}{\alpha_0} > 0$
Polarisations:	2

## Unitarity conditions

(Unitarity is demonstrably impossible)