

PSALTer results panel

$$S = \iiint \bigg(\frac{1}{6} (6 \mathcal{A}^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + 6 f^{\alpha\beta} \tau (\Delta + \mathcal{K})_{\alpha\beta} - 18 r_{\frac{1}{3}} \partial_{\beta} \mathcal{A}_{\frac{1}{\theta}}^{\theta} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} - 6 r_{\frac{1}{3}} \partial_{\frac{1}{\beta}} \mathcal{A}_{\theta}^{\theta} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} - 6 r_{\frac{1}{3}} \partial_{\alpha} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} \partial_{\theta} \mathcal{A}_{\beta}^{\theta} + 12 r_{\frac{1}{3}} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} \partial_{\theta} \mathcal{A}_{\beta}^{\theta} -$$
$$18 r_{\frac{1}{3}} \partial_{\alpha} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} \partial_{\theta} \mathcal{A}_{\frac{1}{\beta}}^{\theta} + 36 r_{\frac{1}{3}} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} \partial_{\theta} \mathcal{A}_{\frac{1}{\beta}}^{\theta} + 8 r_{\frac{1}{2}} \partial_{\beta} \mathcal{A}_{\alpha\frac{1}{\theta}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} - 4 r_{\frac{1}{2}} \partial_{\beta} \mathcal{A}_{\alpha\theta_{\frac{1}{\theta}}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} + 4 r_{\frac{1}{2}} \partial_{\beta} \mathcal{A}_{\frac{1}{\theta}\alpha} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} - 24 r_{\frac{1}{3}} \partial_{\beta} \mathcal{A}_{\frac{1}{\theta}\alpha} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} -$$
$$2 r_{\frac{1}{2}} \partial_{\frac{1}{\beta}} \mathcal{A}_{\alpha\beta\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} + 2 r_{\frac{1}{2}} \partial_{\theta} \mathcal{A}_{\alpha\beta_{\frac{1}{\theta}}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} - 4 r_{\frac{1}{2}} \partial_{\theta} \mathcal{A}_{\alpha\frac{1}{\beta}} \partial^{\theta} \mathcal{A}^{\alpha\beta_{\frac{1}{\theta}}} + 4 t_{\frac{1}{2}} \mathcal{A}_{\frac{1}{\theta}\alpha} \partial^{\theta} f^{\alpha\frac{1}{\theta}} + 2 t_{\frac{1}{2}} \partial_{\alpha} f_{\frac{1}{\theta}} \partial^{\theta} f^{\alpha\frac{1}{\theta}} - t_{\frac{1}{2}} \partial_{\alpha} f_{\theta_{\frac{1}{\theta}}} \partial^{\theta} f^{\alpha\frac{1}{\theta}} -$$
$$t_{\frac{1}{2}} \partial_{\frac{1}{\beta}} f_{\alpha\theta} \partial^{\theta} f^{\alpha\frac{1}{\theta}} + t_{\frac{1}{2}} \partial_{\theta} f_{\alpha_{\frac{1}{\theta}}} \partial^{\theta} f^{\alpha\frac{1}{\theta}} - t_{\frac{1}{2}} \partial_{\theta} f_{\frac{1}{\alpha}} \partial^{\theta} f^{\alpha\frac{1}{\theta}} - 4 t_{\frac{1}{2}} \mathcal{A}_{\alpha\theta_{\frac{1}{\theta}}} (\mathcal{A}^{\alpha\frac{1}{\theta}} + \partial^{\theta} f^{\alpha\frac{1}{\theta}}) + 2 t_{\frac{1}{2}} \mathcal{A}_{\alpha\theta} (\mathcal{A}^{\alpha\frac{1}{\theta}} + 2 \partial^{\theta} f^{\alpha\frac{1}{\theta}})) \bigg) [t, x, y, z] dz dy dx dt$$

Wave operator

$0^+ \mathcal{A}^{\parallel}$	$0^+ f^{\parallel}$	$0^+ f^{\perp}$	$0^- \mathcal{A}^{\parallel}$											
$0^+ \mathcal{A}^{\parallel} \uparrow$	$6 k^2 r_3$	0	0	0										
$0^+ f^{\parallel} \uparrow$	0	0	0	0										
$0^+ f^{\perp} \uparrow$	0	0	0	0										
$0^- \mathcal{A}^{\parallel} \uparrow$	0	0	0	$k^2 r_2 + \frac{t_2}{2}$	$1^+ \mathcal{A}^{\parallel}_{\alpha\beta}$	$1^+ \mathcal{A}^{\perp}_{\alpha\beta}$	$1^+ f^{\parallel}_{\alpha\beta}$	$1^- \mathcal{A}^{\parallel}_{\alpha}$	$1^- \mathcal{A}^{\perp}_{\alpha}$	$1^- f^{\parallel}_{\alpha}$	$1^- f^{\perp}_{\alpha}$			
	$1^+ \mathcal{A}^{\parallel} \uparrow^{\alpha\beta}$	$k^2 r_3 + \frac{2 t_2}{3}$	$\frac{\sqrt{2} t_2}{3}$	$\frac{1}{3} i \sqrt{2} k t_2$	0	0	0	0						
	$1^+ \mathcal{A}^{\perp} \uparrow^{\alpha\beta}$	$\frac{\sqrt{2} t_2}{3}$	$\frac{t_2}{3}$	$\frac{i k t_2}{3}$	0	0	0	0						
	$1^+ f^{\parallel} \uparrow^{\alpha\beta}$	$-\frac{1}{3} i \sqrt{2} k t_2$	$-\frac{1}{3} i k t_2$	$\frac{k^2 t_2}{3}$	0	0	0	0						
	$1^- \mathcal{A}^{\parallel} \uparrow^{\alpha}$	0	0	0	$k^2 r_3$	0	0	0						
	$1^- \mathcal{A}^{\perp} \uparrow^{\alpha}$	0	0	0	0	0	0	0						
	$1^- f^{\parallel} \uparrow^{\alpha}$	0	0	0	0	0	0	0						
	$1^- f^{\perp} \uparrow^{\alpha}$	0	0	0	0	0	0	0	$2^+ \mathcal{A}^{\parallel}_{\alpha\beta}$	$2^+ f^{\parallel}_{\alpha\beta}$	$2^- \mathcal{A}^{\parallel}_{\alpha\beta\chi}$			
					$2^+ \mathcal{A}^{\parallel} \uparrow^{\alpha\beta}$	0	0		0					
					$2^+ f^{\parallel} \uparrow^{\alpha\beta}$	0	0		0					
					$2^- \mathcal{A}^{\parallel} \uparrow^{\alpha\beta\chi}$	0	0		0					

Saturated propagator

$0^+ \sigma^{\parallel}$	$0^+ \tau^{\parallel}$	$0^+ \tau^{\perp}$	$0^- \sigma^{\parallel}$										
$0^+ \sigma^{\parallel} \uparrow$	$\frac{1}{6 k^2 r_{\frac{1}{3}}}$	0	0	0									
$0^+ \tau^{\parallel} \uparrow$	0	0	0	0									
$0^+ \tau^{\perp} \uparrow$	0	0	0	0									
$0^- \sigma^{\parallel} \uparrow$	0	0	0	$\frac{1}{k^2 r_{\frac{1}{2}} + t_{\frac{1}{2}}}$	$1^+ \sigma^{\parallel}_{\alpha\beta}$	$1^+ \sigma^{\perp}_{\alpha\beta}$	$1^+ \tau^{\parallel}_{\alpha\beta}$	$1^- \sigma^{\parallel}_{\alpha}$	$1^- \sigma^{\perp}_{\alpha}$	$1^- \tau^{\parallel}_{\alpha}$	$1^- \tau^{\perp}_{\alpha}$		
	$1^+ \sigma^{\parallel} \uparrow^{\alpha\beta}$	$\frac{1}{k^2 r_{\frac{1}{3}}}$	$-\frac{\sqrt{2}}{k^2 r_{\frac{1}{3}} + k^4 r_{\frac{1}{3}}}$	$-\frac{i \sqrt{2}}{k r_{\frac{1}{3}} + k^3 r_{\frac{1}{3}}}$	0	0	0	0					
	$1^+ \sigma^{\perp} \uparrow^{\alpha\beta}$	$-\frac{\sqrt{2}}{k^2 r_{\frac{1}{3}} + k^4 r_{\frac{1}{3}}}$	$\frac{3 k^2 r_{\frac{1}{3}} + 2 t_{\frac{1}{2}}}{(k + k^3)^2 r_{\frac{1}{3}} t_{\frac{1}{2}}}$	$\frac{i (3 k^2 r_{\frac{1}{3}} + 2 t_{\frac{1}{2}})}{k (1 + k^2)^2 r_{\frac{1}{3}} t_{\frac{1}{2}}}$	0	0	0	0					
	$1^+ \tau^{\parallel} \uparrow^{\alpha\beta}$	$\frac{i \sqrt{2}}{k r_{\frac{1}{3}} + k^3 r_{\frac{1}{3}}}$	$-\frac{i (3 k^2 r_{\frac{1}{3}} + 2 t_{\frac{1}{2}})}{k (1 + k^2)^2 r_{\frac{1}{3}} t_{\frac{1}{2}}}$	$\frac{3 k^2 r_{\frac{1}{3}} + 2 t_{\frac{1}{2}}}{(1 + k^2)^2 r_{\frac{1}{3}} t_{\frac{1}{2}}}$	0	0	0	0					
	$1^- \sigma^{\parallel} \uparrow^{\alpha}$	0	0	0	$\frac{1}{k^2 r_{\frac{1}{3}}}$	0	0	0					
	$1^- \sigma^{\perp} \uparrow^{\alpha}$	0	0	0	0	0	0	0					
	$1^- \tau^{\parallel} \uparrow^{\alpha}$	0	0	0	0	0	0	0					
	$1^- \tau^{\perp} \uparrow^{\alpha}$	0	0	0	0	0	0	0	$2^+ \sigma^{\parallel}_{\alpha\beta}$ $2^+ \tau^{\parallel}_{\alpha\beta}$ $2^- \sigma^{\parallel}_{\alpha\beta\chi}$				
									$2^+ \sigma^{\parallel} \uparrow^{\alpha\beta}$	0	0	0	
									$2^+ \tau^{\parallel} \uparrow^{\alpha\beta}$	0	0	0	
									$2^- \sigma^{\parallel} \uparrow^{\alpha\beta\chi}$	0	0	0	

Source constraints

Spin-parity form	Covariant form	Multiplicities
$0^+ \tau^{\perp} == 0$	$\partial_{\beta} \partial_{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} == 0$	1
$0^+ \tau^{\parallel} == 0$	$\partial_{\beta} \partial_{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} == \partial_{\beta} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha}_{\alpha}$	1
$1^- \tau^{\perp\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} == \partial_{\chi} \partial^{\chi} \partial_{\beta} \tau (\Delta + \mathcal{K})^{\alpha\beta}$	3
$1^- \tau^{\parallel\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} == \partial_{\chi} \partial^{\chi} \partial_{\beta} \tau (\Delta + \mathcal{K})^{\beta\alpha}$	3
$1^- \sigma^{\perp\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \sigma^{\beta\alpha\chi} == 0$	3
$i k \ 1^- \sigma^{\perp\alpha\beta} + 1^+ \tau^{\parallel\alpha\beta} == 0$	$\partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} + \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\chi\alpha} + \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_{\delta} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\beta\delta} + 2 \partial_{\delta} \partial^{\delta} \partial_{\chi} \sigma^{\chi\alpha\beta} ==$ $\partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\beta} + \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha\chi} + \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \partial_{\delta} \partial_{\chi} \partial^{\beta} \sigma^{\chi\alpha\delta}$	3
$2^- \sigma^{\parallel\alpha\beta\chi} == 0$	$3 \partial_{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\delta\beta\epsilon} + 3 \partial_{\epsilon} \partial^{\epsilon} \partial^{\chi} \partial^{\alpha} \sigma^{\delta\beta}_{\delta} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\alpha\chi\delta} + 4 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\chi\alpha\delta} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\delta\alpha\chi} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\beta\alpha\delta} +$ $4 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\delta\alpha\beta} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\alpha\beta\chi} + 3 \eta^{\beta\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\alpha} \sigma^{\delta}_{\delta}{}^{\epsilon} + 3 \eta^{\alpha\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\delta} \sigma^{\delta\beta\epsilon} + 3 \eta^{\beta\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\delta} \sigma^{\delta\alpha}_{\delta} ==$ $3 \partial_{\epsilon} \partial_{\delta} \partial^{\chi} \partial^{\beta} \sigma^{\delta\alpha\epsilon} + 3 \partial_{\epsilon} \partial^{\epsilon} \partial^{\chi} \partial^{\beta} \sigma^{\delta\alpha}_{\delta} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\beta\chi\delta} + 4 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\chi\beta\delta} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\delta\beta\chi} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\alpha\beta\delta} +$ $2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\beta\alpha\chi} + 4 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\chi\alpha\beta} + 3 \eta^{\alpha\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\delta} \sigma^{\delta}_{\delta}{}^{\epsilon} + 3 \eta^{\beta\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\delta} \sigma^{\delta\alpha\epsilon} + 3 \eta^{\alpha\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\delta} \sigma^{\delta\beta}_{\delta}$	5
$2^+ \tau^{\parallel\alpha\beta} == 0$	$4 \partial_{\delta} \partial_{\chi} \partial^{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\delta} + 2 \partial_{\delta} \partial^{\delta} \partial^{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi}_{\chi} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial_{\chi} \tau (\Delta + \mathcal{K})^{\chi\delta} ==$ $3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\beta} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha\chi} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\chi\alpha} + 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \tau (\Delta + \mathcal{K})^{\chi}_{\chi}$	5
$2^+ \sigma^{\parallel\alpha\beta} == 0$	$3 \partial_{\delta} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\beta\delta} + 3 \partial_{\delta} \partial_{\chi} \partial^{\beta} \sigma^{\chi\alpha\delta} + 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \sigma^{\chi}_{\chi}{}^{\delta} == 2 \partial_{\delta} \partial^{\delta} \partial^{\alpha} \sigma^{\chi}_{\chi}{}^{\delta} + 3 (\partial_{\delta} \partial^{\delta} \partial_{\chi} \sigma^{\alpha\beta\chi} + \partial_{\delta} \partial^{\delta} \partial_{\chi} \sigma^{\beta\alpha\chi})$	5
Total expected gauge generators:		29

Massive spectrum

Massive particle

Pole residue:	$-\frac{1}{r_2} > 0$
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

Massless spectrum

(No particles)

Unitarity conditions

$$r_{\frac{1}{2}} < 0 \ \&\& \ t_{\frac{1}{2}} > 0$$