

Particle spectrograph

Wave operator and propagator

$\omega_{1+}^{\#1} \alpha\beta$	$\omega_{1+}^{\#2} \alpha\beta$	$f_{1+}^{\#1} \alpha\beta$	$\omega_{1-}^{\#1} \alpha$	$\omega_{1-}^{\#2} \alpha$	$f_{1-}^{\#1} \alpha$	$f_{1-}^{\#2} \alpha$
$\omega_{1+}^{\#1} + \alpha\beta$	$\frac{2t_2}{3}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0
$\omega_{1+}^{\#2} + \alpha\beta$	$\frac{\sqrt{2}t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0
$f_{1+}^{\#1} + \alpha\beta$	$-\frac{1}{3}i\sqrt{2}kt_2$	$-\frac{1}{3}i\sqrt{2}kt_2$	$\frac{k^2t_2}{3}$	0	0	0
$\omega_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$\omega_{1-}^{\#2} + \alpha$	0	0	0	0	0	0
$f_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$f_{1-}^{\#2} + \alpha$	0	0	0	0	0	0

Source constraints/gauge generators	
SO(3) irreps	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\sigma_{1-}^{\#2\alpha} == 0$	3
$\sigma_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#1\alpha\beta} == 0$	3
$\sigma_{1+}^{\#1\alpha\beta} == \sigma_{1+}^{\#2\alpha\beta}$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
$\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	36

$\sigma_{1+}^{\#1} \alpha\beta$	$\sigma_{1+}^{\#2} \alpha\beta$	$\tau_{1+}^{\#1} \alpha\beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\sigma_{1+}^{\#1} + \alpha\beta$	$\frac{6}{(3+k^2)^2t_2}$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$	0	0	0
$\sigma_{1+}^{\#2} + \alpha\beta$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3}{(3+k^2)^2t_2}$	$\frac{3ik}{(3+k^2)^2t_2}$	0	0	0
$\tau_{1+}^{\#1} + \alpha\beta$	$-\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$	$-\frac{3k^2}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$\sigma_{1-}^{\#2} + \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2} + \alpha$	0	0	0	0	0	0

Quadratic (free) Lagrangian density

$$\frac{2}{3}t_2\omega_{\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime} + \frac{1}{3}t_2\omega_{\kappa\lambda}^{\prime}\omega_{\lambda}^{\kappa\lambda} + f^{\alpha\beta}\tau_{\alpha\beta} + \omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi} +$$
$$\frac{2}{3}r_2\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa} - \frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta} - \frac{2}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta} +$$
$$\frac{1}{6}t_2\partial^{\alpha}f_{\theta\kappa}^{\kappa}\partial_{\kappa}f_{\alpha}^{\theta} - \frac{1}{6}t_2\partial_2^{\alpha}f_{\kappa\theta}^{\theta}\partial^{\kappa}f_{\alpha}^{\theta} + \frac{1}{6}t_2\partial_2^{\alpha}f_{\alpha}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta} + \frac{1}{3}t_2\omega_{\theta\kappa}\partial^{\kappa}f^{\theta\theta} -$$
$$\frac{2}{3}t_2\omega_{\kappa\theta}\partial^{\kappa}f^{\theta\theta} - \frac{1}{3}t_2\omega_{\theta\kappa}\partial^{\kappa}f^{\theta\theta} + \frac{2}{3}t_2\omega_{\theta\kappa}\partial^{\kappa}f^{\theta\theta} - \frac{1}{6}t_2\partial_2^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta} -$$
$$\frac{1}{6}t_2\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta} + \frac{1}{6}t_2\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta} + \frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta} +$$
$$\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta} - \frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{\prime\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime} + \frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{\prime\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}$$

$\sigma_{2+}^{\#1} + \alpha\beta$

$\tau_{2+}^{\#1} + \alpha\beta$

$\sigma_{2-}^{\#1} + \alpha\beta\chi$

$\sigma_{2+}^{\#1}$ $\tau_{2+}^{\#1}$ $\tau_{0+}^{\#2}$ $\sigma_{0-}^{\#1}$

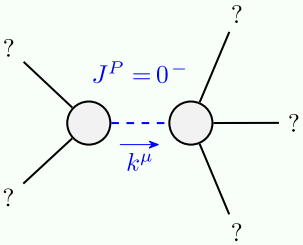
$\omega_{2+}^{\#1} + \alpha\beta$ $f_{2+}^{\#1} + \alpha\beta$ $\omega_{2-}^{\#1} + \alpha\beta\chi$

$\omega_{0+}^{\#1} +$ $f_{0+}^{\#1} +$ $f_{0+}^{\#2} +$ $\omega_{0-}^{\#1}$

$\omega_{2+}^{\#1}$ $f_{2+}^{\#1}$ $\omega_{2-}^{\#1}$

$\omega_{0+}^{\#1}$ $f_{0+}^{\#1}$ $f_{0+}^{\#2}$ $\omega_{0-}^{\#1}$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$