

| Massive particle | |
|------------------|-------------------------|
| Pole residue: | $-\frac{1}{r_1} > 0$ |
| Polarisations: | 5 |
| Square mass: | $-\frac{t_1}{2r_1} > 0$ |
| Spin: | 2 |
| Parity: | Odd |

| $\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{1+}^{\#2}$ | $\tau_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{1-}^{\#1}$ | $\sigma_{1-}^{\#2}$ | $\tau_{1-}^{\#1}$ | $\tau_{1-}^{\#2}$ |
|---|---------------------------------|---|--------------------------------|---|-------------------|--|
| $\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$ | 0 | $-\frac{i\sqrt{2}k}{t_1+k^2t_1}$ | 0 | 0 | 0 | 0 |
| $\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$ | $-\frac{\sqrt{2}}{t_1+k^2t_1}$ | $\frac{-2k^2(2r_1+r_5)+t_1}{(1+k^2)^2t_1^2}$ | 0 | 0 | 0 | 0 |
| $\tau_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{i\sqrt{2}k}{t_1+k^2t_1}$ | $\frac{i(2k^3(2r_1+r_5)-kt_1)}{(1+k^2)^2t_1^2}$ | 0 | 0 | 0 | 0 |
| $\sigma_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | $\frac{\sqrt{2}}{t_1+2k^2t_1}$ | 0 | $\frac{2ik}{t_1+2k^2t_1}$ |
| $\sigma_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | $\frac{\sqrt{2}}{t_1+2k^2t_1}$ | $\frac{-2k^2(r_1+r_5)+t_1}{(t_1+2k^2t_1)^2}$ | 0 | $-\frac{i\sqrt{2}k(2k^2(r_1+r_5)+t_1)}{(t_1+2k^2t_1)^2}$ |
| $\tau_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | $-\frac{2ik}{t_1+2k^2t_1}$ | $\frac{i\sqrt{2}k(2k^2(r_1+r_5)+t_1)}{(t_1+2k^2t_1)^2}$ | 0 | $\frac{-4k^4(r_1+r_5)+2k^2t_1}{(t_1+2k^2t_1)^2}$ |

Lagrangian density

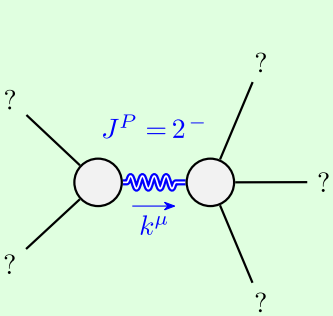
$$\begin{aligned}
 & -t_1\omega_{\lambda'}^{\alpha'}\omega_{\kappa\alpha'}^{\kappa}-t_1\omega_{\kappa\lambda'}^{\kappa\lambda}\omega_{\kappa\lambda'}^{\lambda}-r_5\partial_{\lambda'}\omega_{\kappa\lambda}^{\kappa\lambda}\partial'_{\lambda}\omega_{\lambda'}^{\alpha}-\frac{2}{3}r_1\partial^{\beta}\omega^{\theta\alpha}_{\kappa}\partial_{\theta}\omega^{\kappa}_{\lambda'}-\frac{2}{3}r_1\partial_{\theta}\omega^{\kappa}_{\alpha\beta}\partial^{\alpha}\omega^{\beta\theta}_{\kappa}+\frac{2}{3}r_1\partial_{\theta}\omega^{\kappa}_{\alpha\beta}\partial^{\alpha}\omega^{\beta\theta}_{\kappa}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}_{\lambda}+\\
 & r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}_{\alpha}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}_{\theta}+2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}_{\alpha}-\\
 & \frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial_1\partial^{\alpha}f_{\kappa\theta}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\alpha}^{\theta}\partial^{\kappa}f_{\kappa}^{\alpha}+\frac{1}{2}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda'}^{\lambda}+t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda'}^{\lambda}+2t_1\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\lambda'}^{\lambda}-t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda'}^{\lambda}+\\
 & 2t_1\omega_{\lambda\kappa\theta}\partial^{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}-t_1\omega_{\lambda\alpha}\partial^{\kappa}f_{\kappa}^{\alpha}\partial^{\kappa}f_{\lambda'}^{\lambda}-t_1\omega_{\lambda\lambda'}^{\lambda}\partial^{\kappa}f_{\theta}^{\theta}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\lambda\alpha}^{\lambda}+\\
 & \frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}-t_1\partial^{\alpha}f_{\lambda}^{\alpha}\partial^{\kappa}f_{\lambda\kappa}^{\lambda}+\frac{2}{3}r_1\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}^{\theta}-\frac{2}{3}r_1\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}^{\theta}+\frac{2}{3}r_1\partial^{\beta}\omega_{\lambda'}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda'}-\\
 & \frac{8}{3}r_1\partial^{\beta}\omega_{\lambda'}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda'}+r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\alpha}^{\theta\kappa}_{\kappa}
 \end{aligned}$$

$$\text{Added source term: } \left| f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi} \right.$$

| $\omega_{0+}^{\#1}$ | $f_{0+}^{\#1}$ | $f_{0+}^{\#2}$ | $\omega_{0-}^{\#1}$ |
|-----------------------------|------------------|-----------------|---------------------|
| $\omega_{0+}^{\#1} \dagger$ | $-t_1$ | $i\sqrt{2}kt_1$ | 0 |
| $f_{0+}^{\#1} \dagger$ | $-i\sqrt{2}kt_1$ | $-2k^2t_1$ | 0 |
| $f_{0+}^{\#2} \dagger$ | 0 | 0 | 0 |
| $\omega_{0-}^{\#1} \dagger$ | 0 | 0 | $-t_1$ |

| $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | $f_{2+}^{\#1}$ | $f_{2+}^{\#1}$ | $\omega_{2-}^{\#1}$ | $\omega_{2-}^{\#2}$ | $\alpha\beta\chi$ |
|---|--------------------------|---------------------------|------------------------|---------------------|-------------------|
| $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{t_1}{2}$ | $-\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | |
| $f_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{ikt_1}{\sqrt{2}}$ | k^2t_1 | 0 | 0 | |
| $\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | 0 | $k^2r_1+\frac{t_1}{2}$ | | |

| $\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1+}^{\#2}$ | $f_{1+}^{\#1}$ | $f_{1+}^{\#1}$ | $\omega_{1-}^{\#1}$ | $\omega_{1-}^{\#2}$ | $f_{1-}^{\#1}$ | $f_{1-}^{\#2}$ |
|---|-------------------------------|-------------------------|---------------------------|------------------------------|------------------------|----------------|----------------|
| $\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ | $k^2(2r_1+r_5)-\frac{t_1}{2}$ | $-\frac{t_1}{\sqrt{2}}$ | $-\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 |
| $\omega_{1+}^{\#2} \dagger^{\alpha\beta}$ | $-\frac{t_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\omega_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | $k^2(r_1+r_5)-\frac{t_1}{2}$ | $\frac{t_1}{\sqrt{2}}$ | 0 | ikt_1 |
| $\omega_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | $\frac{t_1}{\sqrt{2}}$ | 0 | 0 | 0 |
| $f_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | $-ikt_1$ | 0 | 0 | 0 |



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$$r_1 < 0 \&\& t_1 > 0$$

Unitarity conditions

(No massless particles)

| | $\sigma_{0+}^{\#1}$ | $\tau_{0+}^{\#1}$ | $\tau_{0+}^{\#2}$ | $\sigma_{0-}^{\#1}$ |
|-----------------------------|------------------------------------|-------------------------------------|-------------------|---------------------|
| $\sigma_{0+}^{\#1} \dagger$ | $-\frac{1}{(1+2k^2)^2t_1}$ | $-\frac{i\sqrt{2}k}{(1+2k^2)^2t_1}$ | 0 | 0 |
| $\tau_{0+}^{\#1} \dagger$ | $\frac{i\sqrt{2}k}{(1+2k^2)^2t_1}$ | $-\frac{2k^2}{(1+2k^2)^2t_1}$ | 0 | 0 |
| $\tau_{0+}^{\#2} \dagger$ | 0 | 0 | 0 | 0 |
| $\sigma_{0-}^{\#1} \dagger$ | 0 | 0 | 0 | $-\frac{1}{t_1}$ |

Source constraints

| SO(3) irreps | # |
|---|----|
| $\tau_{0+}^{\#2} == 0$ | 1 |
| $\tau_{0+}^{\#1} - 2ik\sigma_{0+}^{\#1} == 0$ | 1 |
| $\tau_{1-}^{\#2\alpha} + 2ik\sigma_{1-}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1-}^{\#1\alpha} == 0$ | 3 |
| $\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#2\alpha\beta} == 0$ | 3 |
| $\tau_{2+}^{\#1\alpha\beta} - 2ik\sigma_{2+}^{\#1\alpha\beta} == 0$ | 5 |
| Total #: | 16 |

| | $\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ |
|---|---|---|---|
| $\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{2}{(1+2k^2)^2t_1}$ | $-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$ | 0 |
| $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$ | $\frac{4k^2}{(1+2k^2)^2t_1}$ | 0 |
| $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | 0 | $\frac{2}{2k^2r_1+t_1}$ |