with the Lagrangian, as defined below Eq. (18) of arXiv:1812.02675: Matrix for spin-0 sector:  $\left(\left(\alpha_1+\alpha_2\right)k^2\right)$ 

Matrix for spin-1 sector: 
$$\left(\frac{\alpha_1}{2}k^2\right)$$

Matrix for spin-0 sector:

Matrix for spin-1 sector:

Massless eigenvalues:

 $\left(\frac{1}{\left(\alpha_{1}+\alpha_{2}\right)k^{2}}\right)$ 

The (possibly singular) a-matrices associated

Gauge constraints on source currents:

The Drazin (Moore-Penrose) inverses of these *a*-matrices, which are functionally

analogous to the inverse *b*-matrices described below Eq. (21) of arXiv:1812.02675:

$$\left\{ \frac{-2\frac{\alpha_{1}-\alpha_{2}}{2\alpha_{1}(\alpha_{1}+\alpha_{2})}, -\frac{1}{\alpha_{1}}, -\frac{1}{\alpha_{1}}, -\frac{1}{\alpha_{1}}, \frac{2\frac{\alpha_{1}+\alpha_{2}}{2\alpha_{1}(\alpha_{1}+\alpha_{2})} \right\}$$
Overall particle spectrum:

Massless particle Massless particle Massless particle Pole residue: 
$$-\frac{S}{\alpha P} - \frac{S}{\alpha P \ln \alpha P} > 0$$
Polarisations: 1 Polarisations: 2 Polarisations: 1

Overall unitarity conditions:
False