

# Wave operator and propagator

$$\begin{aligned}
& \text{Quadratic (free) action} \\
& S = \\
& \int \int \int \left( \frac{1}{6} (6 t_1 \omega_{\alpha}^{\alpha} \omega_{,\theta}^{\theta} + 6 f^{\alpha\beta} \tau_{\alpha\beta} + 6 \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 12 t_1 \omega_{\alpha}^{\theta} \partial_{\theta} f^{\alpha} + 12 t_1 \omega_{,\theta}^{\theta} \partial' f^{\alpha} - 6 t_1 \partial_{\theta} \omega_{,\theta}^{\theta} \partial' f^{\alpha} - 12 r_1 \partial_{\beta} \omega_{,\theta}^{\theta} \partial' \omega^{\alpha\beta} + \right. \\
& 12 r_1 \partial_{\theta} \omega_{,\beta}^{\theta} \partial' \omega^{\alpha\beta} - 6 t_1 \partial_{\theta} f^{\alpha} \partial_{\theta} f^{\theta} + \\
& 12 t_1 \partial' f^{\alpha} \partial_{\theta} f^{\theta} + 12 r_1 \partial_{\alpha} \omega^{\alpha\beta} \partial_{\theta} \omega_{,\beta}^{\theta} - \\
& 24 r_1 \partial' \omega_{\beta}^{\alpha\beta} \partial_{\theta} \omega_{,\beta}^{\theta} - 12 r_1 \partial_{\alpha} \omega^{\alpha\beta} \partial_{\theta} \omega_{,\beta}^{\theta} + \\
& 24 r_1 \partial' \omega_{\alpha}^{\alpha\beta} \partial_{\theta} \omega_{,\beta}^{\theta} + 4 t_1 \omega_{,\theta\alpha}^{\theta} \partial^{\theta} f^{\alpha} + 4 t_2 \omega_{,\theta\alpha}^{\theta} \partial^{\theta} f^{\alpha} - \\
& 4 t_1 \partial_{\alpha} f_{,\theta} \partial^{\theta} f^{\alpha} + 2 t_2 \partial_{\alpha} f_{,\theta} \partial^{\theta} f^{\alpha} - 4 t_1 \partial_{\alpha} f_{,\theta} \partial^{\theta} f^{\alpha} - \\
& t_2 \partial_{\alpha} f_{,\theta} \partial^{\theta} f^{\alpha} + 2 t_1 \partial_{\theta} f_{,\alpha\theta} \partial^{\theta} f^{\alpha} - t_2 \partial_{\theta} f_{,\alpha\theta} \partial^{\theta} f^{\alpha} + \\
& 4 t_1 \partial_{\theta} f_{,\alpha} \partial^{\theta} f^{\alpha} + t_2 \partial_{\theta} f_{,\alpha} \partial^{\theta} f^{\alpha} + 2 t_1 \partial_{\theta} f_{,\alpha} \partial^{\theta} f^{\alpha} - \\
& t_2 \partial_{\theta} f_{,\alpha} \partial^{\theta} f^{\alpha} + 2 (t_1 + t_2) \omega_{\alpha\theta}^{\alpha\theta} (\omega^{\alpha\theta} + 2 \partial^{\theta} f^{\alpha}) + \\
& 2 \omega_{\alpha\theta}^{\alpha\theta} ((t_1 - 2 t_2) \omega^{\alpha\theta} + 2 (2 t_1 - t_2) \partial^{\theta} f^{\alpha}) - \\
& 8 r_1 \partial_{\beta} \omega_{,\alpha\theta}^{\alpha\theta} \partial^{\theta} \omega^{\alpha\beta} + 4 r_1 \partial_{\beta} \omega_{,\alpha\theta}^{\alpha\theta} \partial^{\theta} \omega^{\alpha\beta} - 16 r_1 \partial_{\beta} \omega_{,\theta\alpha}^{\alpha\theta} \partial^{\theta} \omega^{\alpha\beta} - 4 r_1 \partial_{\theta} \omega_{,\alpha\beta}^{\alpha\theta} \partial^{\theta} \omega^{\alpha\beta} + \\
& 4 r_1 \partial_{\theta} \omega_{,\alpha\beta}^{\alpha\theta} \partial^{\theta} \omega^{\alpha\beta} ) ) [t, x, y, z] dz dy dx dt
\end{aligned}$$

$$\begin{array}{c}
\begin{array}{c}
\sigma_0^{\#1} + \\
\tau_0^{\#1} + \\
\tau_0^{\#2} + \\
\sigma_0^{\#1}
\end{array}
\begin{array}{c}
- \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
\frac{1}{(1+2k^2)^2 t_1} \\
\frac{i\sqrt{2}k}{(1+2k^2)^2 t_1} \\
\frac{2k^2}{(1+2k^2)^2 t_1} \\
\frac{i\sqrt{2}k}{(1+2k^2)^2 t_1}
\end{array}
\begin{array}{c}
0 \\
0 \\
0 \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
\sigma_0^{\#1} \\
\tau_0^{\#1} \\
\tau_0^{\#2} \\
\sigma_0^{\#1}
\end{array}
\begin{array}{c}
\frac{1}{t_2} \\
0 \\
0 \\
0
\end{array}$$
  

$$\begin{array}{c}
\sigma_2^{\#1} + \\
\tau_2^{\#1} + \\
\tau_2^{\#2} + \\
\sigma_2^{\#1}
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
\frac{2}{(1+2k^2)^2 t_1} \\
-\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1} \\
\frac{4k^2}{(1+2k^2)^2 t_1} \\
\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}
\end{array}
\begin{array}{c}
0 \\
0 \\
0 \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
\sigma_2^{\#1} \\
\tau_2^{\#1} \\
\tau_2^{\#2} \\
\sigma_2^{\#1}
\end{array}
\begin{array}{c}
\frac{2}{2k^2 r_1 + t_1} \\
0 \\
0 \\
0
\end{array}$$
  

$$\begin{array}{c}
\omega_0^{\#1} + \\
f_0^{\#1} + \\
f_0^{\#2} + \\
\omega_0^{\#1}
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
-t_1 \\
-i\sqrt{2}kt_1 \\
0 \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
i\sqrt{2}kt_1 \\
-2k^2 t_1 \\
0 \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
0 \\
0 \\
0 \\
t_2
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
\omega_0^{\#1} \\
f_0^{\#1} \\
f_0^{\#2} \\
\omega_0^{\#1}
\end{array}$$
  

$$\begin{array}{c}
\omega_1^{\#1} + \\
\omega_1^{\#2} + \\
f_1^{\#1} + \\
\omega_1^{\#1} + \\
\omega_1^{\#2} + \\
f_1^{\#1} + \\
f_1^{\#2} +
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
\frac{1}{6}(t_1 + 4t_2) \\
-\frac{t_1 - 2t_2}{3\sqrt{2}} \\
\frac{t_1 + t_2}{3} \\
\frac{ik(t_1 - 2t_2)}{3\sqrt{2}} \\
-\frac{1}{3}ik(t_1 + t_2) \\
\frac{1}{3}k^2(t_1 + t_2) \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
-\frac{t_1 - 2t_2}{3\sqrt{2}} \\
\frac{t_1 + t_2}{3} \\
\frac{ik(t_1 - 2t_2)}{3\sqrt{2}} \\
-\frac{1}{3}ik(t_1 + t_2) \\
\frac{1}{3}k^2(t_1 + t_2) \\
0 \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0
\end{array}
\begin{array}{c}
+ \\
+ \\
+ \\
+ \\
+ \\
+ \\
+
\end{array}
\begin{array}{c}
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0
\end{array}$$

| Massive particle |                         |
|------------------|-------------------------|
| Pole residue:    | $-\frac{1}{r_1} > 0$    |
| Polarisations:   | 5                       |
| Square mass:     | $-\frac{t_1}{2r_1} > 0$ |
| Spin:            | 2                       |
| Parity:          | Odd                     |

(No massless particles)

$$r_1 < 0 \ \&\& \ t_1 > 0$$