

Massive particle	
Pole residue:	$-\frac{1}{r_1} \succ 0$
Polarisations:	5
Square mass:	$-\frac{t_1}{2r_1} \succ 0$
Spin:	2
Parity:	Odd

Unitarity conditions

$r_1 < 0$
&
 $t_1 > 0$

(No massless particles)

Lagrangian density

$$\begin{aligned}
 &-t_1 \, \omega_{\,\,\,\prime}^{\alpha\prime} \, \omega_{\kappa\alpha}^{\,\,\,\prime} \, \omega_{\kappa\lambda}^{\,\,\,\prime} \, \omega_{\kappa\lambda}^{\,\,\,\prime} + \frac{2}{3} t_2 \, \omega_{\kappa\lambda}^{\,\,\,\prime} \, \omega_{\kappa\lambda}^{\,\,\,\prime} \, \omega_{\kappa\lambda}^{\,\,\,\prime} + \frac{1}{3} t_1 \, \omega_{\kappa\lambda}^{\,\,\,\prime} \, \omega_{\kappa\lambda}^{\,\,\,\prime} + \\
 &\frac{1}{3} t_2 \, \omega_{\kappa\lambda}^{\,\,\,\prime} \, \omega_{\kappa\lambda}^{\,\,\,\prime} + 2 \, r_1 \partial_{\prime} \omega_{\kappa\lambda}^{\kappa\lambda} \, \partial^{\prime} \omega_{\lambda\,\,\,\alpha}^{\alpha} - \frac{2}{3} r_1 \partial^{\beta} \omega_{\alpha\,\,\,\kappa}^{\beta\theta} \, \partial_{\theta} \omega_{\alpha\beta}^{\kappa-} \\
 &\frac{2}{3} r_1 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \, \partial_{\kappa} \omega^{\alpha\beta\theta} + \frac{2}{3} r_1 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \, \partial_{\kappa} \omega^{\theta\alpha\beta} + 2 \, r_1 \partial_{\alpha} \omega_{\lambda\,\,\,\theta}^{\alpha} \, \partial_{\kappa} \omega^{\theta\kappa\lambda} - \\
 &2 \, r_1 \partial_{\theta} \omega_{\lambda\,\,\,\alpha}^{\alpha} \, \partial_{\kappa} \omega^{\theta\kappa\lambda} + 2 \, r_1 \partial_{\alpha} \omega_{\lambda\,\,\,\theta}^{\alpha} \, \partial_{\kappa} \omega^{\kappa\lambda\theta} - 4 \, r_1 \partial_{\theta} \omega_{\lambda\,\,\,\alpha}^{\alpha} \, \partial_{\kappa} \omega^{\kappa\lambda\theta} - \\
 &\frac{1}{3} t_1 \partial^{\alpha} f_{\theta\kappa}^{\kappa} \, \partial^{\kappa} f_{\alpha}^{\theta} + \frac{1}{6} t_2 \partial^{\alpha} f_{\theta\kappa}^{\kappa} \, \partial^{\kappa} f_{\alpha}^{\theta} - \frac{2}{3} t_1 \partial^{\alpha} f_{\kappa\theta}^{\kappa} \, \partial^{\kappa} f_{\alpha}^{\theta} - \\
 &\frac{1}{6} t_2 \partial^{\alpha} f_{\kappa\theta}^{\kappa} \, \partial^{\kappa} f_{\alpha}^{\theta} - \frac{1}{3} t_1 \partial^{\alpha} f_{\kappa}^{\lambda} \, \partial^{\kappa} f_{\alpha\lambda}^{\lambda} + \frac{1}{6} t_2 \partial^{\alpha} f_{\kappa}^{\lambda} \, \partial^{\kappa} f_{\alpha\lambda}^{\lambda} + t_1 \, \omega_{\kappa\alpha}^{\alpha} \, \partial^{\kappa} f_{\prime}^{\prime} + \\
 &t_1 \, \omega_{\kappa\lambda}^{\lambda} \, \partial^{\kappa} f_{\prime}^{\prime} + 2 \, t_1 \partial^{\alpha} f_{\kappa\alpha}^{\kappa} \, \partial^{\kappa} f_{\prime}^{\prime} - t_1 \partial_{\kappa} f_{\lambda}^{\lambda} \, \partial^{\kappa} f_{\prime}^{\prime} + \frac{1}{3} t_1 \, \omega_{\prime\theta\kappa} \, \partial^{\kappa} f_{\prime}^{\prime\theta} + \\
 &\frac{1}{3} t_2 \, \omega_{\prime\theta\kappa} \, \partial^{\kappa} f_{\prime}^{\prime\theta} + \frac{4}{3} t_1 \, \omega_{\prime\kappa\theta} \, \partial^{\kappa} f_{\prime}^{\prime\theta} - \frac{2}{3} t_2 \, \omega_{\prime\kappa\theta} \, \partial^{\kappa} f_{\prime}^{\prime\theta} - \frac{1}{3} t_1 \, \omega_{\theta\prime\kappa} \, \partial^{\kappa} f_{\prime}^{\prime\theta} - \\
 &\frac{1}{3} t_2 \, \omega_{\theta\prime\kappa} \, \partial^{\kappa} f_{\prime}^{\prime\theta} + \frac{2}{3} t_1 \, \omega_{\theta\kappa\prime} \, \partial^{\kappa} f_{\prime}^{\prime\theta} + \frac{2}{3} t_2 \, \omega_{\theta\kappa\prime} \, \partial^{\kappa} f_{\prime}^{\prime\theta} - t_1 \, \omega_{\prime\alpha}^{\alpha} \, \partial^{\kappa} f_{\kappa}^{\prime-} - \\
 &t_1 \, \omega_{\prime\lambda}^{\lambda} \, \partial^{\kappa} f_{\kappa}^{\prime} + \frac{1}{3} t_1 \partial^{\alpha} f_{\kappa}^{\lambda} \, \partial^{\kappa} f_{\lambda\alpha}^{\lambda} - \frac{1}{6} t_2 \partial^{\alpha} f_{\kappa}^{\lambda} \, \partial^{\kappa} f_{\lambda\alpha}^{\lambda} + \frac{1}{3} t_1 \partial_{\kappa} f_{\theta}^{\lambda} \, \partial^{\kappa} f_{\lambda}^{\theta} - \\
 &\frac{1}{6} t_2 \partial_{\kappa} f_{\theta}^{\lambda} \, \partial^{\kappa} f_{\lambda}^{\theta} + \frac{2}{3} t_1 \partial_{\kappa} f_{\theta}^{\lambda} \, \partial^{\kappa} f_{\lambda}^{\theta} + \frac{1}{6} t_2 \partial_{\kappa} f_{\theta}^{\lambda} \, \partial^{\kappa} f_{\lambda}^{\theta} - t_1 \partial^{\alpha} f_{\lambda}^{\alpha} \, \partial^{\kappa} f_{\lambda\kappa}^{\kappa} + \\
 &\frac{2}{3} r_1 \partial_{\kappa} \omega^{\alpha\beta\theta} \, \partial^{\kappa} \omega_{\alpha\beta\theta} - \frac{2}{3} r_1 \partial_{\kappa} \omega^{\theta\alpha\beta} \, \partial^{\kappa} \omega_{\alpha\beta\theta} + \frac{2}{3} r_1 \partial^{\beta} \omega_{\lambda\,\,\,\prime}^{\alpha\lambda} \, \partial_{\lambda} \omega_{\alpha\beta}^{\prime-} - \\
 &\frac{8}{3} r_1 \partial^{\beta} \omega_{\lambda\,\,\,\prime}^{\lambda\alpha} \, \partial_{\lambda} \omega_{\alpha\beta}^{\prime-} - 2 \, r_1 \partial_{\alpha} \omega_{\lambda\,\,\,\theta}^{\alpha} \, \partial^{\lambda} \omega_{\lambda\,\,\,\alpha}^{\theta\kappa} + 2 \, r_1 \partial_{\theta} \omega_{\lambda\,\,\,\alpha}^{\alpha} \, \partial^{\lambda} \omega_{\lambda\,\,\,\kappa}^{\theta\kappa}
 \end{aligned}$$

Added source term:

$f^{\alpha\beta} \, \tau_{\alpha\beta} + \omega^{\alpha\beta\chi} \, \sigma_{\alpha\beta\chi}$

$\sigma_{1^{+}\alpha\beta}^{\#1}$	$\sigma_{1^{+}\alpha\beta}^{\#2}$	$\tau_{1^{+}\alpha\beta}^{\#1}$	$\sigma_{1^{\alpha}}^{\#1}$	$\sigma_{1^{\alpha}}^{\#2}$	$\tau_{1^{\alpha}}^{\#1}$	$\tau_{1^{\alpha}}^{\#2}$
$\sigma_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{2(t_1+t_2)}{3t_1t_2}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	0	0	0
$\sigma_{1^{+}}^{\#2} \dagger^{\alpha\beta}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{t_1+4t_2}{3(1+k^2)^2t_1t_2}$	$\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0
$\tau_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$-\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$-\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	$\frac{k^2(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0
$\sigma_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	0	$\frac{\sqrt{2}}{t_1+2k^2t_1}$	0	$\frac{2ik}{t_1+2k^2t_1}$
$\sigma_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	0	0	$\frac{2k^2r_1+t_1}{(t_1+2k^2t_1)^2}$	$\frac{i\sqrt{2}k(2k^2r_1+t_1)}{(t_1+2k^2t_1)^2}$
$\tau_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	0	$-\frac{2ik}{t_1+2k^2t_1}$	$-\frac{i\sqrt{2}k(2k^2r_1+t_1)}{(t_1+2k^2t_1)^2}$	$\frac{2k^2(2k^2r_1+t_1)}{(t_1+2k^2t_1)^2}$

$\omega_{1^{+}\alpha\beta}^{\#1}$	$\omega_{1^{+}\alpha\beta}^{\#2}$	$f_{1^{+}\alpha\beta}^{\#1}$	$\omega_{1^{\alpha}}^{\#1}$	$\omega_{1^{\alpha}}^{\#2}$	$f_{1^{\alpha}}^{\#1}$	$f_{1^{\alpha}}^{\#2}$
$\omega_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{1}{6}(t_1+4t_2)$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	0	0	0	0
$\omega_{1^{+}}^{\#2} \dagger^{\alpha\beta}$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$\frac{t_1+t_2}{3}$	0	0	0	0
$f_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	$-\frac{1}{3}\bar{ik}(t_1+t_2)$	0	0	0	0
$\omega_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	$-k^2r_1-\frac{t_1}{2}$	$\frac{t_1}{\sqrt{2}}$	0	$\bar{ik}t_1$
$\omega_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	$\frac{t_1}{\sqrt{2}}$	0	0	0
$f_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	$-\bar{ik}t_1$	0	0	0

$q_{0^{+}\dagger}^{\#1}$	$\sigma_{0^{+}}^{\#1}$	$\tau_{0^{+}}^{\#1}$	$q_{0^{+}\dagger}^{\#2}$	$\tau_{0^{+}}^{\#2}$	$\sigma_{0^{-}}^{\#1}$
$q_{0^{+}\dagger}^{\#1} \dagger$	$-\frac{1}{(1+2k^2)^2t_1}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_1}$	0	0	0
$\tau_{0^{+}}^{\#1} \dagger$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_1}$	$-\frac{2k^2}{(1+2k^2)^2t_1}$	0	0	0
$\tau_{0^{+}}^{\#2} \dagger$	0	0	0	0	0
$q_{0^{-}}^{\#1} \dagger$	0	0	0	$\frac{1}{2}$	0

Source constraints	#
$\tau_{0^{+}}^{\#2} == 0$	1
$\tau_{0^{+}}^{\#1} - 2\bar{ik}\sigma_{0^{+}}^{\#1} == 0$	1
$\tau_{1^{-}}^{\#2\alpha} + 2\bar{ik}\sigma_{1^{-}}^{\#2\alpha} == 0$	3
$\tau_{1^{-}}^{\#1\alpha} == 0$	3
$\tau_{1^{+}}^{\#1\alpha\beta} + \bar{ik}\sigma_{1^{+}}^{\#2\alpha\beta} == 0$	3
$\tau_{2^{+}}^{\#1\alpha\beta} - 2\bar{ik}\sigma_{2^{+}}^{\#1\alpha\beta} == 0$	5
Total #:	16

	$\omega_{2^{+}}^{\#1} \alpha \beta$	$f_{2^{+}}^{\#1} \alpha \beta$	$\omega_{2^{-}}^{\#1} \alpha \beta \chi$
$\omega_{2^{+}}^{\#1} \dagger^{\alpha \beta}$	$\frac{t_1}{2}$	$-\frac{i k t_1}{\sqrt{2}}$	0
$f_{2^{+}}^{\#1} \dagger^{\alpha \beta}$	$\frac{i k t_1}{\sqrt{2}}$	$k^2 t_1$	0
$\omega_{2^{-}}^{\#1} \dagger^{\alpha \beta \chi}$	0	0	$k^2 r_1 + \frac{t_1}{2}$

$\omega_{0^{+}}^{\#1}$	$f_{0^{+}}^{\#1}$	$f_{0^{+}}^{\#2}$	$\omega_0^{\#1}$
$\omega_{0^{+}}^{\#1} \dagger$	$-t_1$	$i\sqrt{2}kt_1$	0
$f_{0^{+}}^{\#1} \dagger$	$-i\sqrt{2}kt_1$	$-2k^2t_1$	0
$f_{0^{+}}^{\#2} \dagger$	0	0	0
$\omega_0^{\#1} \dagger$	0	0	t_2

$\sigma_{2^{+}\dagger}^{\#1\alpha\beta}$	$\tau_{2^{+}\dagger}^{\#1\alpha\beta}$	$\sigma_{2^{\alpha}}^{\#1\alpha\beta\chi}$
$\sigma_{2^{+}\dagger}^{\#1\alpha\beta} \dagger^{\alpha\beta}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\tau_{2^{+}\dagger}^{\#1\alpha\beta} \dagger^{\alpha\beta}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\sigma_{2^{\alpha}}^{\#1\alpha\beta\chi} \dagger^{\alpha\beta\chi}$	0	$\frac{2}{2k^2r_1+t_1}$