

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \alpha\beta$	$\tau_{1+}^{\#1} \alpha\beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	0	$-\frac{\sqrt{2}}{t_1+k^2 t_1}$	0	0	0	0
$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{t_1+k^2 t_1}$	$\frac{-2 i k^3 (2 r_3+r_5)+t_1}{(1+k^2)^2 t_1^2}$	0	0	0	0
$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\frac{i \sqrt{2} k}{t_1+k^2 t_1}$	$\frac{-2 k^4 (2 r_3+r_5)+k^2 t_1}{(1+k^2)^2 t_1^2}$	0	0	0	0
$\sigma_{1-}^{\#1} \dagger^{\alpha}$	0	0	$\frac{1}{k^2 (2 r_3+r_5)}$	$-\frac{1}{\sqrt{2} (k^2+2 k^4) (2 r_3+r_5)}$	0	$-\frac{i}{k (1+2 k^2) (2 r_3+r_5)}$
$\sigma_{1-}^{\#2} \dagger^{\alpha}$	0	0	$-\frac{1}{\sqrt{2} (k^2+2 k^4) (2 r_3+r_5)}$	$\frac{6 k^2 (2 r_3+r_5)+t_1}{2 (k+2 k^3)^2 (2 r_3+r_5) t_1}$	0	$\frac{i (6 k^2 (2 r_3+r_5)+t_1)}{\sqrt{2} k (1+2 k^2)^2 (2 r_3+r_5) t_1}$
$\tau_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#2} \dagger^{\alpha}$	0	0	$\frac{i}{k (1+2 k^2) (2 r_3+r_5)}$	$-\frac{i (6 k^2 (2 r_3+r_5)+t_1)}{\sqrt{2} k (1+2 k^2)^2 (2 r_3+r_5) t_1}$	0	$\frac{6 k^2 (2 r_3+r_5)+t_1}{(1+2 k^2)^2 (2 r_3+r_5) t_1}$

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{2+}^{\#1} \dagger^{\alpha\beta\chi}$
$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{2}{(1+2 k^2)^2 t_1}$	$\frac{2 i \sqrt{2} k}{(1+2 k^2)^2 t_1}$
$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{2 i \sqrt{2} k}{(1+2 k^2)^2 t_1}$	$\frac{4 k^2}{(1+2 k^2)^2 t_1}$
$\sigma_{2+}^{\#1} \dagger^{\alpha\beta\chi}$	0	$\frac{2}{t_1}$

$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#2} \alpha\beta$	$f_{1+}^{\#1} \alpha\beta$	$\omega_{1-}^{\#1} \alpha$	$\omega_{1-}^{\#2} \alpha$	$f_{1-}^{\#1} \alpha$	$f_{1-}^{\#2} \alpha$
$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$k^2 (2 r_3+r_5)-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0
$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\frac{i k t_1}{\sqrt{2}}$	0	0	0	0	0
$\omega_{1-}^{\#1} \dagger^{\alpha}$	0	0	$k^2 (2 r_3+r_5)+\frac{t_1}{6}$	$\frac{t_1}{3 \sqrt{2}}$	0	$\frac{i k t_1}{3}$
$\omega_{1-}^{\#2} \dagger^{\alpha}$	0	0	$\frac{t_1}{3 \sqrt{2}}$	$\frac{t_1}{3}$	0	$\frac{1}{3} i \sqrt{2} k t_1$
$f_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#2} \dagger^{\alpha}$	0	0	$-\frac{1}{3} i k t_1$	$-\frac{1}{3} i \sqrt{2} k t_1$	0	$\frac{2 k^2 t_1}{3}$

$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$f_{2+}^{\#1} \alpha\beta$	$\omega_{2-}^{\#1} \alpha\beta\chi$
$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{t_1}{2}$	$-\frac{i k t_1}{\sqrt{2}}$
$f_{2+}^{\#1} \alpha\beta$	$\frac{i k t_1}{\sqrt{2}}$	$k^2 t_1$
$\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	0	0

$\sigma_{0+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{0+}^{\#1} \alpha\beta$	$\sigma_{0+}^{\#2} \alpha\beta$
$\sigma_{0+}^{\#1} \dagger^{\alpha\beta}$	$\frac{1}{6 k^2 r_3}$	0
$\tau_{0+}^{\#1} \dagger^{\alpha\beta}$	0	0
$\tau_{0+}^{\#2} \dagger^{\alpha\beta}$	0	0
$\sigma_{0-}^{\#1} \dagger^{\alpha\beta}$	0	$-\frac{1}{t_1}$

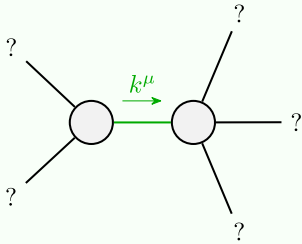
Quadratic (free) action

$$S = \iiint ((f^{\alpha\beta} \tau_{\alpha\beta} + \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + \frac{1}{6} t_1 (2 \omega^{\alpha\iota} \omega_{\alpha}{}^{\theta}{}_{,\theta} - 4 \omega_{\alpha}{}^{\theta}{}_{,\theta} \omega^{\alpha\iota} f^{\alpha}{}_{,\theta} + 4 \omega_{,\theta}{}^{\theta} \partial' f^{\alpha}{}_{,\theta} - 2 \partial_{,\theta} f^{\theta}{}_{,\alpha} \partial' f^{\alpha}{}_{,\theta} - 2 \partial_{,\theta} f^{\alpha\iota} \partial_{\theta} f^{\theta}{}_{,\alpha} + 4 \partial' f^{\alpha}{}_{,\theta} \partial_{\theta} f^{\theta}{}_{,\alpha} - 6 \partial_{\alpha} f^{\theta}{}_{,\theta} \partial^{\theta} f^{\alpha\iota} - 3 \partial_{\alpha} f^{\theta}{}_{,\theta} \partial^{\theta} f^{\alpha\iota} + 3 \partial_{\theta} f^{\alpha\iota} \partial^{\theta} f^{\alpha\iota} + 3 \partial_{\theta} f^{\alpha\iota} \partial^{\theta} f^{\alpha\iota} + 3 \partial_{\theta} f^{\alpha\iota} \partial^{\theta} f^{\alpha\iota} + 6 \omega_{\alpha\theta\iota} (\omega^{\alpha\iota\theta} + 2 \partial^{\theta} f^{\alpha\iota})) - 2 r_3 (\partial_{\beta} \omega_{,\theta} \partial' \omega_{\alpha}{}^{\beta} + \partial_{,\theta} \omega_{\beta}{}^{\theta} \partial' \omega_{\alpha}{}^{\beta} + \partial_{\alpha} \omega^{\alpha\beta} \partial_{\theta} \omega_{\beta}{}^{\theta} - 2 \partial' \omega_{\alpha}{}^{\beta} \partial_{\theta} \omega_{\beta}{}^{\theta} + \partial_{\alpha} \omega^{\alpha\beta\iota} \partial_{\theta} \omega_{,\beta}{}^{\theta} - 2 \partial' \omega_{\alpha}{}^{\beta} \partial_{\theta} \omega_{,\beta}{}^{\theta} + 2 \partial_{\beta} \omega_{,\theta\alpha} \partial^{\theta} \omega^{\alpha\beta\iota}) + r_5 (\partial_{,\iota} \omega_{\theta}{}^{\kappa} \partial^{\theta} \omega_{\alpha}{}^{\iota} - \partial_{\theta} \omega_{,\kappa}{}^{\iota} \partial^{\theta} \omega_{\alpha}{}^{\iota} - (\partial_{\alpha} \omega^{\alpha\iota\theta} - 2 \partial^{\theta} \omega_{\alpha}{}^{\iota}) (\partial_{\kappa} \omega_{,\theta}{}^{\kappa} - \partial_{\theta} \omega_{\kappa}{}^{\iota})) [t, x, y, z] dz dy dx dt$$

$\omega_{0+}^{\#1} \dagger^{\alpha\beta}$	$f_{0+}^{\#1} \alpha\beta$	$f_{0+}^{\#2} \alpha\beta$	$\omega_{0-}^{\#1} \alpha\beta$
$\omega_{0+}^{\#1} \dagger^{\alpha\beta}$	$6 k^2 r_3$	0	0
$f_{0+}^{\#1} \dagger^{\alpha\beta}$	0	0	0
$f_{0+}^{\#2} \dagger^{\alpha\beta}$	0	0	0
$\omega_{0-}^{\#1} \dagger^{\alpha\beta}$	0	0	$-t_1$

Source constraints/gauge generators	
SO(3) irreps	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2 i k \sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2 i k \sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	16

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{(2 r_3+r_5) t_1^2} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$r_5 < -2 r_3 \ \&\& \ t_1 < 0 \ || \ t_1 > 0$