

Particle spectrograph

Wave operator and propagator

	$\sigma_{1+}^{\#1}{}^{\alpha\beta}$	$\sigma_{1+}^{\#2}{}^{\alpha\beta}$	$\tau_{1+}^{\#1}{}^{\alpha\beta}$	$\sigma_{1+}^{\#1}{}^{\alpha}$	$\sigma_{1+}^{\#2}{}^{\alpha}$	$\tau_{1+}^{\#1}{}^{\alpha}$	$\tau_{1+}^{\#2}{}^{\alpha}$
$\sigma_{1+}^{\#1}{}^{\alpha\beta}$	$\frac{1}{\frac{3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)}{16\left(\beta_1+2\beta_3\right)}+\left(\alpha_2+\alpha_5\right)k^2}$	$-\frac{2\sqrt{2}\left(3\alpha_0-4\beta_1+16\beta_3\right)}{\left(1+k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	$-\frac{2i\sqrt{2}\left(3\alpha_0-4\beta_1+16\beta_3\right)k}{\left(1+k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	0	0	0	0
$\sigma_{1+}^{\#2}{}^{\alpha\beta}$	$-\frac{2\sqrt{2}\left(3\alpha_0-4\beta_1+16\beta_3\right)}{\left(1+k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	$\frac{6\alpha_0+8\left(\beta_1+8\beta_3+3\left(\alpha_2+\alpha_5\right)k^2\right)}{\left(1+k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	$\frac{2ik\left(3\alpha_0+4\left(\beta_1+8\beta_3+3\left(\alpha_2+\alpha_5\right)k^2\right)\right)}{\left(1+k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	0	0	0	0
$\tau_{1+}^{\#1}{}^{\alpha\beta}$	$\frac{2i\sqrt{2}\left(3\alpha_0-4\beta_1+16\beta_3\right)k}{\left(1+k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	$-\frac{2ik\left(3\alpha_0+4\left(\beta_1+8\beta_3+3\left(\alpha_2+\alpha_5\right)k^2\right)\right)}{\left(1+k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	$\frac{2k^2\left(3\alpha_0+4\left(\beta_1+8\beta_3+3\left(\alpha_2+\alpha_5\right)k^2\right)\right)}{\left(1+k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)+16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)k^2\right)}$	0	0	0	0
$\sigma_{1+}^{\#1}{}^{\alpha}$	0	0	0	$\frac{1}{\frac{3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)}{8\left(2\beta_1+\beta_2\right)}+\left(\alpha_4+\alpha_5\right)k^2}$	$\frac{2\sqrt{2}\left(3\alpha_0-4\beta_1+4\beta_2\right)}{\left(1+2k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$	0	$\frac{4i\left(3\alpha_0-4\beta_1+4\beta_2\right)k}{\left(1+2k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$
$\sigma_{1+}^{\#2}{}^{\alpha}$	0	0	0	$\frac{2\sqrt{2}\left(3\alpha_0-4\beta_1+4\beta_2\right)}{\left(1+2k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$	$\frac{6\alpha_0+8\left(\beta_1+2\beta_2+3\left(\alpha_4+\alpha_5\right)k^2\right)}{\left(1+2k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$	0	$\frac{2i\sqrt{2}k\left(3\alpha_0+4\left(\beta_1+2\beta_2+3\left(\alpha_4+\alpha_5\right)k^2\right)\right)}{\left(1+2k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$
$\tau_{1+}^{\#1}{}^{\alpha}$	0	0	0	0	0	0	0
$\tau_{1+}^{\#2}{}^{\alpha}$	0	0	0	$-\frac{4i\left(3\alpha_0-4\beta_1+4\beta_2\right)k}{\left(1+2k^2\right)\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$	$-\frac{2i\sqrt{2}k\left(3\alpha_0+4\left(\beta_1+2\beta_2+3\left(\alpha_4+\alpha_5\right)k^2\right)\right)}{\left(1+2k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$	0	$\frac{4k^2\left(3\alpha_0+4\left(\beta_1+2\beta_2+3\left(\alpha_4+\alpha_5\right)k^2\right)\right)}{\left(1+2k^2\right)^2\left(-3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)+8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)k^2\right)}$

S==
[[[[[$\frac{1}{6}(-3\alpha_0\omega_{\alpha}^{\alpha\beta}\omega_{\beta}^{\alpha}X+4\beta_1\omega_{\alpha}^{\alpha\beta}\omega_{\beta}^{\alpha}X-4\beta_2\omega_{\alpha}^{\alpha\beta}\omega_{\beta}^{\alpha}X+6f^{\alpha\beta}\tau_{\alpha\beta}^{\alpha}+6\omega_{\alpha\beta}^{\alpha}C_{\alpha\beta X}-8\beta_1\omega_{\alpha}^{\alpha}X\partial_{\beta}f^{\alpha\beta}+8\beta_2\omega_{\alpha}^{\alpha}X\partial_{\beta}f^{\alpha\beta}-6\alpha_0f^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+6\alpha_0\partial_{\beta}\omega_{\alpha}^{\alpha\beta}\omega_{\beta}^{\alpha}X+8\beta_1\omega_{\beta}^{\alpha}X\partial_{\beta}f^{\alpha\alpha}-8\beta_2\omega_{\beta}^{\alpha}X\partial_{\beta}f^{\alpha\alpha}-4\beta_1\partial_{\beta}f^{\alpha}X\partial_{\beta}f^{\alpha\alpha}+4\beta_2\partial_{\beta}f^{\alpha}X\partial_{\beta}f^{\alpha\alpha}-4\beta_1\partial_{\beta}f^{\alpha\beta}\partial_{\alpha}f^{\alpha}X+4\beta_2\partial_{\beta}f^{\alpha\beta}\partial_{\alpha}f^{\alpha}X+8\beta_1\partial_{\beta}f^{\alpha\beta}\partial_{\alpha}f^{\alpha}X-8\beta_2\partial_{\beta}f^{\alpha\beta}\partial_{\alpha}f^{\alpha}X+6\alpha_0f^{\alpha\beta}\partial_{\alpha}f^{\alpha}X-6\alpha_0\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-6\alpha_2\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-12\alpha_1\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-12\alpha_2\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+12\alpha_4\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+12\alpha_5\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+8\alpha_1\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+8\alpha_2\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+4\alpha_1\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+4\alpha_2\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-4\alpha_1\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-4\alpha_2\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-2\alpha_3\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+2\alpha_3\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X+4\alpha_1\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X-4\alpha_3\partial_{\alpha}\omega_{\beta}^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\alpha}X)]],x,y,z]\int d\mathbf{x}d\mathbf{x}dt$

$\sigma_{0+}^{\#1}{}^{\alpha\beta}$

$\frac{-4\beta_2}{\alpha_0^2+2\alpha_0\beta_2-4\left(\alpha_4+\alpha_6\right)\beta_2k^2}$

$\frac{i\sqrt{2}\left(\alpha_0+2\beta_2\right)}{-\alpha_0\left(\alpha_0+2\beta_2\right)+4\left(\alpha_4+\alpha_6\right)\beta_2k^3}$

0

0

$\tau_{0+}^{\#1}{}^{\alpha\beta}$

$\frac{i\sqrt{2}\left(\alpha_0+2\beta_2\right)}{\alpha_0\left(\alpha_0+2\beta_2\right)+4\left(\alpha_4+\alpha_6\right)\beta_2k^3}$

$\frac{\frac{\alpha_0}{2}+\beta_2+\left(\alpha_4+\alpha_6\right)k^2}{-\frac{1}{2}\alpha_0\left(\alpha_0+2\beta_2\right)^2+2\left(\alpha_4+\alpha_6\right)\beta_2k^4}$

0

0

$\tau_{0+}^{\#2}{}^{\alpha\beta}$

0

0

0

0

$\omega_{2+}^{\#1}{}^{\alpha\beta}$

$\frac{-\frac{4}{\alpha_0}+\beta_1+\left(\alpha_1+\alpha_4\right)k^2}{2\sqrt{2}}$

$\frac{i\left(\alpha_0-4\beta_1\right)k}{2\sqrt{2}}$

0

0

$f_{2+}^{\#1}{}^{\alpha\beta}$

$-\frac{i\left(\alpha_0-4\beta_1\right)k}{2\sqrt{2}}$

$2\beta_1k^2$

0

0

$\omega_{2+}^{\#2}{}^{\alpha\beta}$

0

0

$-\frac{\alpha_0}{4}+\beta_1+\left(\alpha_1+\alpha_2\right)k^2$

k^2

$\omega_{0+}^{\#1}{}^{\alpha}$

$\frac{\alpha_0}{2}+\beta_2+\left(\alpha_4+\alpha_6\right)k^2$

$\frac{i\left(\alpha_0+2\beta_2\right)k}{\sqrt{2}}$

0

0

$f_{0+}^{\#1}{}^{\alpha}$

$\frac{i\left(\alpha_0+2\beta_2\right)k}{\sqrt{2}}$

$2\beta_2k^2$

0

0

$f_{0+}^{\#2}{}^{\alpha}$

0

0

0

0

$\omega_{0+}^{\#2}{}^{\alpha}$

0

0

$\frac{\alpha_0}{2}+4\beta_3+\left(\alpha_2+\alpha_3\right)k^2$

k^2

$\sigma_{2+}^{\#1}{}^{\alpha\beta}$

$\frac{16\beta_1}{-\alpha_0^2+4\alpha_0\beta_1+16\left(\alpha_1+\alpha_4\right)\beta_1k^2}$

$\frac{2i\sqrt{2}\left(\alpha_0-4\beta_1\right)}{\alpha_0\left(\alpha_0-4\beta_1\right)+16\left(\alpha_1+\alpha_4\right)\beta_1k^3}$

0

0

$\tau_{2+}^{\#1}{}^{\alpha\beta}$

$\frac{2i\sqrt{2}\left(\alpha_0-4\beta_1\right)}{\alpha_0\left(\alpha_0-4\beta_1\right)+16\left(\alpha_1+\alpha_4\right)\beta_1k^3}$

$\frac{2\left(\alpha_0-4\beta_1\right)+\left(\alpha_1+\alpha_4\right)k^2}{k^2\left(\alpha_0^2-4\alpha_0\beta_1-16\left(\alpha_1+\alpha_4\right)\beta_1k^2\right)}$

0

0

$\tau_{2+}^{\#2}{}^{\alpha\beta}$

0

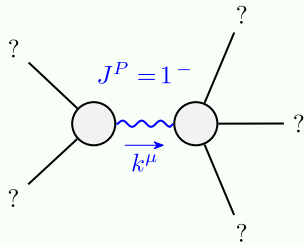
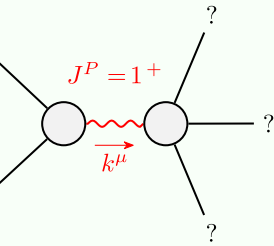
0

$\frac{-\alpha_0}{4}+\beta_1+\left(\alpha_1+\alpha_2\right)k^2$

$\frac{1}{k^2}$

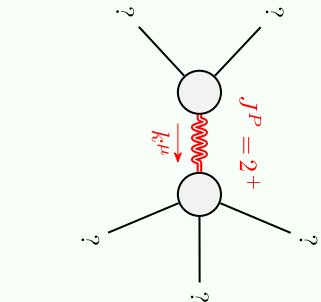
Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\tau_{0+}^{\#2} == 0$	$\partial_{\beta}\partial_{\alpha}\tau^{\alpha\beta} == 0$	1
$\tau_{1+}^{\#2\alpha} + 2i k \sigma_{1+}^{\#2\alpha} == 0$	$\partial_X\partial_{\beta}\partial^{\alpha}\tau^{\beta X} == \partial_X\partial^X\partial_{\beta}\tau^{\alpha\beta} + 2\partial_{\delta}\partial^{\delta}\partial_X\partial_{\beta}\sigma^{\alpha\beta X}$	3
$\tau_{1+}^{\#1\alpha} = 0$	$\partial_X\partial_{\beta}\partial^{\alpha}\tau^{\beta X} == \partial_X\partial^X\partial_{\beta}\tau^{\beta\alpha}$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#2\alpha\beta} == 0$	$\partial_X\partial^{\alpha}\tau^{\beta X} + \partial_X\partial^{\beta}\tau^{\alpha X} + \partial_X\partial^X\tau^{\alpha\beta} + 2\partial_{\delta}\partial_X\partial^{\alpha}\sigma^{\beta X\delta} + 2\partial_{\delta}\partial^{\delta}\partial_X\sigma^{\alpha\beta X} == \partial_X\partial^{\alpha}\tau^{\beta X} + \partial_X\partial^{\beta}\tau^{\alpha X} + \partial_X\partial^X\tau^{\alpha\beta} + 2\partial_{\delta}\partial_X\partial^{\beta}\sigma^{\alpha X\delta}$	3
Total constraints/gauge generators:		10

Massive and massless spectra

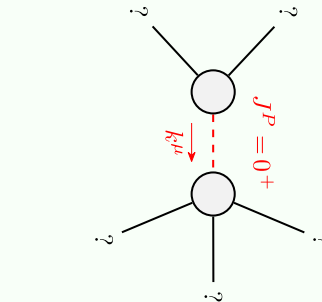


Massive particle	
Pole residue:	$\left(3\left(\alpha_0^2\left(3\alpha_2+3\alpha_5+2\beta_1+4\beta_3\right)-8\alpha_0\left(\beta_1^2+\alpha_2\left(\beta_1-4\beta_3\right)+\alpha_5\left(\beta_1-4\beta_3\right)-4\beta_3^2\right)+16\left(-4\beta_1\beta_3\left(\beta_1+2\beta_3\right)+\alpha_2\left(\beta_1^2+8\beta_3^2\right)+\alpha_5\left(\beta_1^2+8\beta_3^2\right)\right)\right)/\left(2\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)\left(3\alpha_0^2-12\alpha_0\left(\beta_1-2\beta_3\right)+16\left(\alpha_5\beta_1+2\alpha_5\beta_3-6\beta_1\beta_3+\alpha_2\left(\beta_1+2\beta_3\right)\right)\right)\right)>0$
Polarisations:	3
Square mass:	$\frac{3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+8\beta_3\right)}{16\left(\alpha_2+\alpha_5\right)\left(\beta_1+2\beta_3\right)}>0$
Spin:	1
Parity:	Even

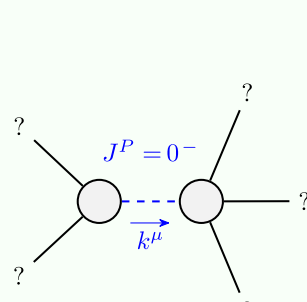
Massive particle	
Pole residue:	$\left(-\left(3\left(\alpha_0^2\left(3\alpha_4+3\alpha_5+4\beta_1+2\beta_2\right)+4\alpha_0\left(-2\alpha_4\beta_1-2\alpha_5\beta_1-4\beta_1^2+2\alpha_4\beta_2+2\alpha_5\beta_2+\beta_2^2\right)+8\left(-2\beta_1\beta_2\left(2\beta_1+\beta_2\right)+\alpha_4\left(2\beta_1^2+\beta_2^2\right)+\alpha_5\left(2\beta_1^2+\beta_2^2\right)\right)\right)/\left(2\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)\left(3\alpha_0^2+6\alpha_0\left(-2\beta_1+\beta_2\right)+4\left(2\alpha_5\beta_1+\alpha_5\beta_2-6\beta_1\beta_2+\alpha_4\left(2\beta_1+\beta_2\right)\right)\right)\right)>0$
Polarisations:	3
Square mass:	$\frac{3\left(\alpha_0-4\beta_1\right)\left(\alpha_0+2\beta_2\right)}{8\left(\alpha_4+\alpha_5\right)\left(2\beta_1+\beta_2\right)}>0$
Spin:	1
Parity:	Odd



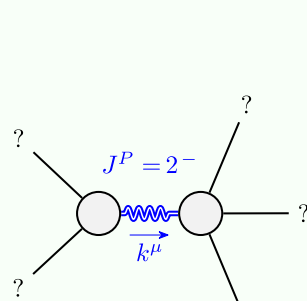
Massive particle	
Pole residue:	$-\frac{2}{\alpha_0}+\frac{\alpha_1+\alpha_4+2\beta_1}{2\alpha_1\beta_1+2\alpha_4\beta_1}>0$
Polarisations:	5
Square mass:	$\frac{\alpha_0\left(\alpha_0+2\beta_2\right)}{16\left(\alpha_1+\alpha_4\right)\beta_1}>0$
Spin:	2
Parity:	Even



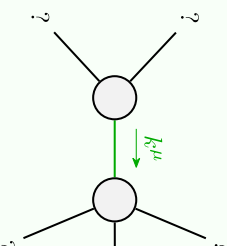
Massive particle	
Pole residue:	$\frac{1}{\alpha_0}+\frac{\alpha_4+\alpha_6+2\beta_2}{2\alpha_4\beta_2+2\alpha_6\beta_2}>0$
Polarisations:	1
Square mass:	$\frac{\alpha_0\left(\alpha_0+2\beta_2\right)}{4\left(\alpha_4+\alpha_6\right)\beta_2}>0$
Spin:	0
Parity:	Even



Massive particle	
Pole residue:	$-\frac{1}{\alpha_2+\alpha_3}>0$
Polarisations:	1
Square mass:	$-\frac{\alpha_0+8\beta_3}{2\left(\alpha_2+\alpha_3\right)}>0$
Spin:	0
Parity:	Odd



Massive particle	
Pole residue:	$-\frac{1}{\alpha_1+\alpha_2}>0$
Polarisations:	5
Square mass:	$\frac{\alpha_0-4\beta_1}{4\left(\alpha_1+\alpha_2\right)}>0$
Spin:	2
Parity:	Odd



Quadratic pole	
Pole residue:	$\frac{1}{\alpha_0}>0$
Polarisations:	2

Unitarity conditions

(Unitarity is demonstrably impossible)