



$$r_2 < 0 \ \&\& \ t_2 > 0$$

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

### Lagrangian density

$$\begin{aligned} &\frac{2}{3}t_3\omega_{\lambda'}^{\alpha\lambda}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_2\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\lambda'}^{\lambda}+\frac{1}{3}t_2\omega_{\kappa\lambda}^{\lambda}\omega_{\lambda'}^{\kappa\lambda}+f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}+\\ &2r_1\partial_l\omega_{\kappa}^{\kappa\lambda}\partial_l'\omega_{\lambda}^{\alpha}-\frac{2}{3}r_1\partial^{\beta}\omega_{\alpha}^{\alpha}\partial_{\theta}\omega_{\kappa}^{\kappa}+\frac{2}{3}r_2\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha}^{\kappa}-\\ &\frac{2}{3}r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}-\frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}+\frac{2}{3}r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}-\\ &\frac{2}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}+2r_1\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\theta}^{\theta\kappa\lambda}-2r_1\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\theta\kappa\lambda}+\\ &2r_1\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\lambda}^{\kappa\lambda\theta}-4r_1\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\kappa\lambda\theta}+\frac{1}{6}t_2\partial^{\alpha}f_{\theta\kappa}^{\kappa}f_{\alpha}^{\theta}-\frac{1}{6}t_2\partial^{\alpha}f_{\kappa\theta}^{\theta}f_{\alpha}^{\kappa}+\\ &\frac{1}{6}t_2\partial^{\alpha}f_{\kappa}^{\lambda}\partial_{\alpha}^{\kappa}f_{\alpha\lambda}^{\lambda}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda'}^{\lambda}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda'}^{\lambda}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}^{\kappa}\partial^{\kappa}f_{\lambda'}^{\lambda}+\\ &\frac{2}{3}t_3\partial_{\kappa}f_{\lambda}^{\lambda}\partial_{\lambda'}^{\kappa}f_{\lambda'}^{\lambda}+\frac{1}{3}t_2\omega_{\theta\kappa}^{\kappa}\partial^{\kappa}f_{\lambda'}^{\theta}-\frac{2}{3}t_2\omega_{\kappa\theta}^{\theta}\partial^{\kappa}f_{\lambda'}^{\theta}-\frac{1}{3}t_2\omega_{\theta\kappa}^{\kappa}\partial^{\kappa}f_{\lambda'}^{\theta}+\\ &\frac{2}{3}t_2\omega_{\theta\kappa}^{\kappa}\partial^{\kappa}f_{\lambda'}^{\theta}+\frac{2}{3}t_3\omega_{\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\lambda}+\frac{2}{3}t_3\omega_{\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{\lambda}-\frac{1}{6}t_2\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\lambda}^{\alpha}-\\ &\frac{1}{6}t_2\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+\frac{1}{6}t_2\partial_2\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+\frac{2}{3}t_3\partial^{\alpha}f_{\lambda}^{\alpha}\partial^{\kappa}f_{\alpha}^{\lambda}+\frac{2}{3}r_1\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\\ &\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_1\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\\ &\frac{2}{3}r_1\partial^{\beta}\omega_{\lambda'}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}-\frac{2}{3}r_2\partial^{\beta}\omega_{\alpha\beta}^{\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}-\frac{8}{3}r_1\partial^{\beta}\omega_{\lambda'}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}+\\ &\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda'}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}-2r_1\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}^{\lambda}\omega_{\alpha}^{\theta\kappa}+2r_1\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\alpha}^{\theta\kappa}\end{aligned}$$

$\sigma_{1+}^{\#1}+\alpha\beta$	$\sigma_{1+}^{\#2}+\alpha\beta$	$\tau_{1+}^{\#1}+\alpha\beta$	$\sigma_{1-}^{\#1}\alpha$	$\sigma_{1-}^{\#2}\alpha$	$\tau_{1-}^{\#1}\alpha$	$\tau_{1-}^{\#2}\alpha$
$\sigma_{1+}^{\#1}+\alpha\beta$	$\frac{6}{(3+k^2)^2t_2}$	$\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1+}^{\#2}+\alpha\beta$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3ik}{(3+k^2)^2t_2}$	0	0	0	0
$\tau_{1+}^{\#1}+\alpha\beta$	$-\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$	$-\frac{3k^2}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1-}^{\#1}\alpha$	0	0	$-\frac{1}{k^2r_1}$	$-\frac{\sqrt{2}}{k^2r_1+2k^3r_1}$	0	$-\frac{2i}{kr_1+2k^3r_1}$
$\sigma_{1-}^{\#2}\alpha$	0	0	$-\frac{\sqrt{2}}{k^2r_1+2k^4r_1}$	$\frac{3k^2r_1-2t_3}{(k+2k^3)^2r_1t_3}$	0	$\frac{i\sqrt{2}(3k^2r_1-2t_3)}{k(1+2k^2)^2r_1t_3}$
$\tau_{1-}^{\#1}\alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2}\alpha$	0	0	$\frac{2i}{kr_1+2k^3r_1}$	$-\frac{i\sqrt{2}(3k^2r_1-2t_3)}{k(1+2k^2)^2r_1t_3}$	0	$\frac{6k^2r_1-4t_3}{(1+2k^2)^2r_1t_3}$

$\omega_{1+}^{\#1}+\alpha\beta$	$\omega_{1+}^{\#2}+\alpha\beta$	$f_{1+}^{\#1}+\alpha\beta$	$\omega_{1-}^{\#1}\alpha$	$\omega_{1-}^{\#2}\alpha$	$f_{1-}^{\#1}\alpha$	$f_{1-}^{\#2}\alpha$
$\omega_{1+}^{\#1}+\alpha\beta$	$\frac{2t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0	0
$\omega_{1+}^{\#2}+\alpha\beta$	$\frac{\sqrt{2}t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0	0
$f_{1+}^{\#1}+\alpha\beta$	$-\frac{1}{3}i\sqrt{2}kt_2$	$-\frac{1}{3}ikt_2$	0	0	0	0
$\omega_{1-}^{\#1}\alpha$	0	0	$-k^2r_1+\frac{2t_3}{3}$	$-\frac{\sqrt{2}t_3}{3}$	0	$-\frac{2}{3}ikt_3$
$\omega_{1-}^{\#2}\alpha$	0	0	0	0	0	$\frac{1}{3}i\sqrt{2}kt_3$
$f_{1-}^{\#1}\alpha$	0	0	0	0	0	0
$f_{1-}^{\#2}\alpha$	0	0	$\frac{2ikt_3}{3}$	$-\frac{1}{3}i\sqrt{2}kt_3$	0	$\frac{2k^2t_3}{3}$

### Source constraints

SO(3) irreps	#
$\tau_{0+}^{\#2}==0$	1
$\tau_{0+}^{\#1}-2ik\sigma_{0+}^{\#1}==0$	1
$\tau_{1-}^{\#2\alpha}+2ik\sigma_{1-}^{\#2\alpha}==0$	3
$\tau_{1-}^{\#1\alpha}==0$	3
$\tau_{1+}^{\#1\alpha\beta}+ik\sigma_{1+}^{\#1\alpha\beta}==0$	3
$\sigma_{1+}^{\#1\alpha\beta}==\sigma_{1+}^{\#2\alpha\beta}$	3
$\tau_{2+}^{\#1\alpha\beta}==0$	5
$\sigma_{2+}^{\#1\alpha\beta}==0$	5
Total #:	24

	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1}+$	$t_3$	$-i\sqrt{2}kt_3$	0	0
$f_{0+}^{\#1}+$	$i\sqrt{2}kt_3$	$2k^2t_3$	0	0
$f_{0+}^{\#2}+$	0	0	0	0
$\omega_{0-}^{\#1}+$	0	0	0	$k^2r_2+t_2$

	$\sigma_{2+}^{\#1}+\alpha\beta$	$\tau_{2+}^{\#1}+\alpha\beta$	$\sigma_{2-}^{\#1}\alpha\beta\chi$
$\sigma_{2+}^{\#1}+\alpha\beta$	0	0	0
$\tau_{2+}^{\#1}+\alpha\beta$	0	0	0
$\sigma_{2-}^{\#1}+\alpha\beta\chi$	0	0	$\frac{1}{k^2r_1}$

	$\omega_{2+}^{\#1}+\alpha\beta$	$f_{2+}^{\#1}+\alpha\beta$	$\omega_{2-}^{\#1}\alpha\beta\chi$
$\omega_{2+}^{\#1}+\alpha\beta$	0	0	0
$f_{2+}^{\#1}+\alpha\beta$	0	0	0
$\omega_{2-}^{\#1}+\alpha\beta\chi$	0	0	$k^2r_1$

	$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1}+$	$\frac{1}{(1+2k^2)^2t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0
$\tau_{0+}^{\#1}+$	$\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0
$\tau_{0+}^{\#2}+$	0	0	0
$\sigma_{0-}^{\#1}+$	0	0	$\frac{1}{k^2r_2+t_2}$