

Particle spectrograph

Wave operator and propagator

Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\tau_{0+}^{\#2} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == 0$	1
$\tau_{0+}^{\#1} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == \partial_\beta \partial^\beta \tau^\alpha_\alpha$	1
$\sigma_{0+}^{\#1} == 0$	$\partial_\beta \sigma^{\alpha\beta}_\alpha == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha_\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\alpha\beta}$	3
$\tau_{1-}^{\#1\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha_\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\beta\alpha}$	3
$\sigma_{1-}^{\#2\alpha} == 0$	$\partial_\chi \partial_\beta \sigma^{\alpha\beta\chi}_\alpha == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#1\alpha\beta} == 0$	$\partial_\chi \partial^\alpha \tau^{\beta\chi}_\alpha + \partial_\chi \partial^\beta \tau^{\chi\alpha}_\alpha + \partial_\chi \partial^\chi \tau^{\alpha\beta}_\alpha ==$ $\partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta}_\alpha + \partial_\delta \partial^\delta \partial_\chi \sigma^{\beta\chi\alpha}_\alpha ==$ $\partial_\chi \partial^\alpha \tau^{\chi\beta}_\alpha + \partial_\chi \partial^\beta \tau^{\alpha\chi}_\alpha + \partial_\chi \partial^\chi \tau^{\beta\alpha}_\alpha +$ $\partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta}_\alpha + \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta}_\alpha$	3
$\sigma_{1+}^{\#1\alpha\beta} == \sigma_{1+}^{\#2\alpha\beta}$	$3 \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta}_\alpha +$ $2 \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\beta\chi}_\alpha + \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta}_\alpha ==$ $3 \partial_\delta \partial_\chi \partial^\delta \sigma^{\alpha\chi\delta}_\alpha + \partial_\delta \partial^\delta \partial_\chi \sigma^{\beta\chi\alpha}_\alpha$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	$3 \partial_\epsilon \partial_\delta \partial^\chi \partial^\alpha \sigma^{\beta\delta\epsilon}_\alpha + 3 \partial_\epsilon \partial^\epsilon \partial^\chi \partial^\alpha \sigma^{\beta\delta}_\delta +$ $2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\beta \sigma^{\alpha\chi\delta}_\delta + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\beta \sigma^{\alpha\delta\chi}_\alpha +$ $2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\beta \sigma^{\chi\delta\alpha}_\alpha + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\beta \sigma^{\alpha\beta\delta}_\delta +$ $2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\alpha \sigma^{\alpha\chi\delta}_\alpha + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\delta \sigma^{\beta\chi\alpha}_\alpha +$ $3 \eta^{\beta\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\delta\epsilon}_\delta +$ $3 \eta^{\alpha\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\beta\delta\epsilon}_\epsilon +$ $3 \eta^{\beta\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\alpha\delta}_\delta ==$ $3 \partial_\epsilon \partial_\delta \partial^\chi \partial^\beta \sigma^{\alpha\delta\epsilon}_\epsilon + 3 \partial_\epsilon \partial^\epsilon \partial^\chi \partial^\beta \sigma^{\alpha\delta}_\delta +$ $2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\alpha \sigma^{\beta\chi\delta}_\delta + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\alpha \sigma^{\beta\delta\chi}_\alpha +$ $2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\alpha \sigma^{\chi\delta\beta}_\beta + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\alpha \sigma^{\beta\delta\alpha}_\alpha +$ $4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\delta \sigma^{\alpha\beta\chi}_\alpha + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\delta \sigma^{\alpha\chi\beta}_\beta +$ $3 \eta^{\alpha\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\delta\epsilon}_\delta +$ $3 \eta^{\beta\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\alpha\delta\epsilon}_\epsilon +$ $3 \eta^{\alpha\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\beta\delta}_\delta$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	$4 \partial_\delta \partial_\chi \partial^\beta \partial^\alpha \tau^{\chi\delta}_\alpha + 2 \partial_\delta \partial^\delta \partial_\beta \partial^\alpha \tau^{\chi}_\chi +$ $3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\alpha\beta}_\alpha + 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\beta\alpha}_\alpha +$ $2 \eta^{\alpha\beta} \partial_\epsilon \partial^\epsilon \partial_\delta \tau^{\chi\delta}_\alpha ==$ $3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\beta\chi}_\alpha + 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\chi\beta}_\beta +$ $3 \partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\alpha\chi}_\alpha + 3 \partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\chi\alpha}_\alpha +$ $2 \eta^{\alpha\beta} \partial_\epsilon \partial^\epsilon \partial_\delta \tau^{\chi}_\chi$	5
Total constraints/gauge generators:		28

Quadratic (free) action

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$$\begin{aligned} & \iiint \iiint \Big(6 \, f^{\alpha\beta} \, \tau_{\alpha\beta} + 6 \, \omega^{\alpha\beta\chi} \, \sigma_{\alpha\beta\chi} - 15 \, r_3 \, \partial_\beta \omega_{\alpha\beta}^\theta \, \partial_\theta \omega^{\alpha\beta}_\alpha + 9 \, r_3 \, \partial_\theta \omega_{\beta\theta}^\theta \, \partial_\theta \omega^{\alpha\beta}_\alpha + \\ & \qquad 9 \, r_3 \, \partial_\alpha \omega^{\alpha\beta\iota} \, \partial_\theta \omega_{\beta\iota}^\theta - 18 \, r_3 \, \partial_\theta \omega_{\beta\iota}^{\alpha\beta} \, \partial_\alpha \omega_{\beta\iota}^\theta - \\ & \qquad 15 \, r_3 \, \partial_\alpha \omega^{\alpha\beta\iota} \, \partial_\theta \omega_{\beta\iota}^\theta + 30 \, r_3 \, \partial_\theta \omega^{\alpha\beta}_\alpha \, \partial_\theta \omega_{\beta\iota}^\theta + \\ & \qquad 4 \, t_2 \, \omega_{\theta\alpha} \, \partial^\theta f^{\alpha\iota} + 2 \, t_2 \, \partial_\alpha f_{\theta\alpha} \, \partial^\theta f^{\alpha\iota} - t_2 \, \partial_\alpha f_{\theta\iota} \, \partial^\theta f^{\alpha\iota} - \\ & \qquad t_2 \, \partial_\theta f_{\alpha\theta} \, \partial^\theta f^{\alpha\iota} + t_2 \, \partial_\theta f_{\alpha\iota} \, \partial^\theta f^{\alpha\iota} - t_2 \, \partial_\theta f_{\alpha\alpha} \, \partial^\theta f^{\alpha\iota} - \\ & \qquad 4 \, t_2 \, \omega_{\alpha\theta\iota} \, (\omega^{\alpha\iota\theta} + \partial^\theta f^{\alpha\iota}) + 2 \, t_2 \, \omega_{\alpha\theta\iota} \, (\omega^{\alpha\iota\theta} + 2 \, \partial^\theta f^{\alpha\iota}) + \\ & \qquad 8 \, r_2 \, \partial_\beta \omega_{\alpha\theta} \, \partial^\theta \omega^{\alpha\beta\iota}_\alpha - 4 \, r_2 \, \partial_\beta \omega_{\alpha\theta\iota} \, \partial^\theta \omega^{\alpha\beta\iota}_\alpha + \\ & \qquad 4 \, r_2 \, \partial_\beta \omega_{\theta\alpha} \, \partial^\theta \omega^{\alpha\beta\iota}_\alpha - 24 \, r_3 \, \partial_\beta \omega_{\theta\alpha} \, \partial^\theta \omega^{\alpha\beta\iota}_\alpha - \\ & \qquad 2 \, r_2 \, \partial_\theta \omega_{\alpha\beta\theta} \, \partial^\theta \omega^{\alpha\beta\iota}_\alpha + 2 \, r_2 \, \partial_\theta \omega_{\alpha\beta\iota} \, \partial^\theta \omega^{\alpha\beta\iota}_\alpha - \\ & \qquad 4 \, r_2 \, \partial_\theta \omega_{\alpha\beta} \, \partial^\theta \omega^{\alpha\beta\iota})] [t, x, y, z] d z d y d x d t \end{aligned}$$

$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1-}^{\#1} \dagger^{\alpha}$	$\omega_{1-}^{\#2} \dagger^{\alpha}$	$f_{1-}^{\#1} \dagger^{\alpha}$	$f_{1-}^{\#2} \dagger^{\alpha}$
$\frac{2 t_2}{3}$	$\frac{\sqrt{2} t_2}{3}$	$\frac{1}{3} i \sqrt{2} k t_2$	0	0	0	0
$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{t_2}{3}$	$\frac{i k t_2}{3}$	0	0	0	0
$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{1}{3} i \sqrt{2} k t_2$	$\frac{k^2 t_2}{3}$	0	0	0	0
$\omega_{1-}^{\#1} \dagger^{\alpha}$	0	0	$-\frac{3 k^2 r_3}{2}$	0	0	0
$\omega_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0

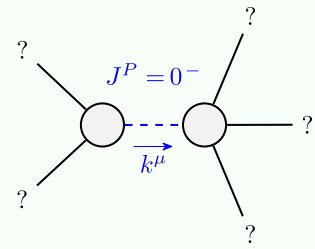
$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{\#1} \dagger^{\alpha}$	$\sigma_{1-}^{\#2} \dagger^{\alpha}$	$\tau_{1-}^{\#1} \dagger^{\alpha}$	$\tau_{1-}^{\#2} \dagger^{\alpha}$
$\frac{6}{(3+k^2)^2 t_2}$	$\frac{3 \sqrt{2}}{(3+k^2)^2 t_2}$	$\frac{3 i \sqrt{2} k}{(3+k^2)^2 t_2}$	0	0	0	0
$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{3 \sqrt{2}}{(3+k^2)^2 t_2}$	$\frac{3 i k}{(3+k^2)^2 t_2}$	0	0	0	0
$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{3 i \sqrt{2} k}{(3+k^2)^2 t_2}$	$-\frac{3 k^2}{(3+k^2)^2 t_2}$	0	0	0	0
$\sigma_{1-}^{\#1} \dagger^{\alpha}$	0	0	$-\frac{2}{3 k^2 r_3}$	0	0	0
$\sigma_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$\sigma_{0+}^{\#1} \dagger$	0	0	0	0	0	0
$\tau_{0+}^{\#1} \dagger$	0	0	0	0	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0	0	0	0
$\sigma_{0-}^{\#1} \dagger$	0	0	0	$\frac{1}{k^2 r_2 + t_2}$	0	0

$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$f_{2+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$
$-\frac{3 k^2 r_3}{2}$	0	0
0	0	0
0	0	0
$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{2}{3 k^2 r_3}$	0
0	0	0
0	0	0

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$
$-\frac{2}{3 k^2 r_3}$	0	0
0	0	0
0	0	0

$\omega_{0+}^{\#1} \dagger$	0	0	0	0
$f_{0+}^{\#1} \dagger$	0	0	0	0
$f_{0+}^{\#2} \dagger$	0	0	0	0
$\omega_{0-}^{\#1} \dagger$	0	0	0	$k^2 r_2 + t_2$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

No massless particles

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$