

# Particle spectrograph

## Wave operator and propagator

Quadratic (free) action

$$S = \int \int \int \int (\beta h_{\alpha\beta} h^{\alpha\beta} - \gamma h^\alpha_\alpha h^\beta_\beta + h^{\alpha\beta} \mathcal{T}_{\alpha\beta} + \frac{1}{2} \alpha (\partial_\beta h^\chi_\chi \partial^\beta h^\alpha_\alpha + 2 \partial_\alpha h^{\alpha\beta} \partial_\chi h^\chi_\beta - 2 \partial^\beta h^\alpha_\alpha \partial_\chi h^\chi_\beta - \partial_\chi h_{\alpha\beta} \partial^\chi h^{\alpha\beta})) [t, x, y, z] dz dy dx dt$$

$\mathcal{T}^{\#1}_{0+}$ 

$\mathcal{T}^{\#1}_{0+} \dagger$	$\frac{1}{\frac{\beta(\beta-4\gamma)}{\beta-\gamma} + \alpha k^2}$	$\frac{\sqrt{3}\gamma}{\beta(\beta-4\gamma) + \alpha(\beta-\gamma)k^2}$
$\mathcal{T}^{\#2}_{0+} \dagger$	$\frac{\sqrt{3}\gamma}{\beta(\beta-4\gamma) + \alpha(\beta-\gamma)k^2}$	$\frac{1}{\beta + \gamma(-1 - \frac{3\gamma}{\beta-3\gamma + \alpha k^2})}$

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$h^{\#1}_{0+}$ 

$h^{\#1}_{0+} \dagger$	$\beta - 3\gamma + \alpha k^2$	$-\sqrt{3}\gamma$
$h^{\#2}_{0+} \dagger$	$-\sqrt{3}\gamma$	$\beta - \gamma$

$h^{\#2}_{0+}$ 

$h^{\#1}_{0+}$	$\beta - 3\gamma + \alpha k^2$	$-\sqrt{3}\gamma$
$h^{\#2}_{0+}$	$-\sqrt{3}\gamma$	$\beta - \gamma$

$\mathcal{T}^{\#1}_{2+\alpha\beta}$ 

$\mathcal{T}^{\#1}_{2+} \dagger^{\alpha\beta}$	$\frac{1}{\beta - \frac{\alpha k^2}{2}}$
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$h^{\#1}_{2+\alpha\beta}$ 

$h^{\#1}_{2+} \dagger^{\alpha\beta}$	$\beta - \frac{\alpha k^2}{2}$
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(No source constraints)

## Massive and massless spectra

Massive particle

Pole residue:	$\frac{\beta^2 - 2\beta\gamma + 4\gamma^2}{\alpha(\beta-\gamma)^2} > 0$
Polarisations:	1
Square mass:	$-\frac{\beta(\beta-4\gamma)}{\alpha(\beta-\gamma)} > 0$
Spin:	0
Parity:	Even

Massive particle

Pole residue:	$-\frac{2\beta}{\alpha} > 0$
Polarisations:	5
Square mass:	$\frac{2\beta}{\alpha} > 0$
Spin:	2
Parity:	Even

(No massless particles)

## Unitarity conditions

(Unitarity is demonstrably impossible)