Particle spectrograph

Wave operator and propagator

	$\sigma^{\#1}_{2^+\alpha\beta}$	$\tau^{\#1}_{2^+\alpha\beta}$	$\sigma^{\#1}_{2^-\alpha\beta\chi}$
$\sigma^{\#1}_{2^+}\dagger^{\alpha\beta}$	$\frac{2}{(1+2k^2)^2 t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	0
$\tau^{\#1}_{2^+}\dagger^{\alpha\beta}$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	$\frac{4k^2}{(1+2k^2)^2 t_1}$	0
$\sigma^{\#1}_{2^-}\dagger^{\alpha\beta\chi}$	0	0	$\frac{2}{t_1}$

	$\omega^{\#1}_{0^+}$	$f^{\#1}_{0^+}$	$f^{\#2}_{0^+}$	$\omega^{\#1}_{0^-}$
$\omega^{\#1}_{0^+}\dagger$	t_3	$-i\sqrt{2}\,k t_3$	0	0
$f^{\#1}_{0^+}\dagger$	$i\sqrt{2}\,k t_3$	$2k^2 t_3$	0	0
$f^{\#2}_{0^+}\dagger$	0	0	0	0
$\omega^{\#1}_{0^-}\dagger$	0	0	0	$-t_1$

$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$\frac{ikt_1}{\sqrt{2}}$	$k^2 t_1$	0
0	0	$\frac{t_1}{2}$

Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\tau^{\#2}_{0^+} == 0$	$\partial_\beta\partial_\alpha\tau^{\alpha\beta} == 0$	1
$\tau^{\#1}_{0^+} - 2ik\,\sigma^{\#1}_{0^+} == 0$	$\partial_\beta\partial_\alpha\tau^{\alpha\beta} == \partial_\beta\partial^\beta\tau^\alpha{}_\alpha + 2\partial_\chi\partial^\chi\partial_\beta\sigma^{\alpha\beta}{}_\alpha$	1
$\tau^{\#2\,\alpha}_{1^-} + 2ik\,\sigma^{\#2\,\alpha}_{1^-} == 0$	$\partial_\chi\partial_\beta\partial^\alpha\tau^{\beta\chi} == \partial_\chi\partial^\chi\partial_\beta\tau^{\alpha\beta} + 2\partial_\delta\partial^\delta\partial_\chi\partial_\beta\sigma^{\alpha\beta\chi}$	3
$\tau^{\#1\,\alpha}_{1^-} == 0$	$\partial_\chi\partial_\beta\partial^\alpha\tau^{\beta\chi} == \partial_\chi\partial^\chi\partial_\beta\tau^{\beta\alpha}$	3
$\tau^{\#1\,\alpha\beta}_{1^+} + ik\,\sigma^{\#2\,\alpha\beta}_{1^+} == 0$	$\partial_\chi\partial^\alpha\tau^{\beta\chi} + \partial_\chi\partial^\beta\tau^{\chi\alpha} + \partial_\chi\partial^\chi\tau^{\alpha\beta} +$ $2\partial_\delta\partial_\chi\partial^\alpha\sigma^{\beta\chi\delta} + 2\partial_\delta\partial^\delta\partial_\chi\sigma^{\alpha\beta\chi} ==$ $\partial_\chi\partial^\alpha\tau^{\chi\beta} + \partial_\chi\partial^\beta\tau^{\alpha\chi} +$ $\partial_\chi\partial^\chi\tau^{\beta\alpha} + 2\partial_\delta\partial_\chi\partial^\beta\sigma^{\alpha\chi\delta}$	3
$\tau^{\#1\,\alpha\beta}_{2^+} - 2ik\,\sigma^{\#1\,\alpha\beta}_{2^+} == 0$	$-i(4\partial_\delta\partial_\chi\partial^\beta\partial^\alpha\tau^{\chi\delta} + 2\partial_\delta\partial^\delta\partial^\beta\partial^\alpha\tau^\chi{}_\chi -$ $3\partial_\delta\partial^\delta\partial_\chi\partial^\alpha\tau^{\beta\chi} - 3\partial_\delta\partial^\delta\partial_\chi\partial^\alpha\tau^{\chi\beta} -$ $3\partial_\delta\partial^\delta\partial_\chi\partial^\beta\tau^{\alpha\chi} - 3\partial_\delta\partial^\delta\partial_\chi\partial^\beta\tau^{\chi\alpha} +$ $3\partial_\delta\partial^\delta\partial_\chi\partial^\chi\tau^{\alpha\beta} + 3\partial_\delta\partial^\delta\partial_\chi\partial^\chi\tau^{\beta\alpha} +$ $4ik^\chi\,\partial_\epsilon\partial_\chi\partial^\beta\partial^\alpha\sigma^{\delta\epsilon}{}_\delta -$ $6ik^\chi\,\partial_\epsilon\partial_\delta\partial_\chi\partial^\alpha\sigma^{\beta\delta\epsilon} -$ $6ik^\chi\,\partial_\epsilon\partial_\delta\partial_\chi\partial^\beta\sigma^{\alpha\delta\epsilon} +$ $2\eta^{\alpha\beta}\,\partial_\epsilon\partial^\epsilon\partial_\delta\partial_\chi\tau^{\chi\delta} +$ $6ik^\chi\,\partial_\epsilon\partial^\epsilon\partial_\delta\partial_\chi\sigma^{\alpha\delta\beta} +$ $6ik^\chi\,\partial_\epsilon\partial^\epsilon\partial_\delta\partial_\chi\sigma^{\beta\delta\alpha} -$ $2\eta^{\alpha\beta}\,\partial_\epsilon\partial^\epsilon\partial_\delta\partial^\delta\tau^\chi{}_\chi -$ $4i\eta^{\alpha\beta}\,k^\chi\,\partial_\phi\partial^\phi\partial_\epsilon\partial_\chi\sigma^{\delta\epsilon}{}_\delta) == 0$	5
Total constraints/gauge generators:		16

	$\omega^{\#1}_{1^+\alpha\beta}$	$\omega^{\#2}_{1^+\alpha\beta}$	$f^{\#1}_{1^+\alpha\beta}$	$\omega^{\#1}_{1^-\alpha}$	$\omega^{\#2}_{1^-\alpha}$	$f^{\#1}_{1^-\alpha}$	$f^{\#2}_{1^-\alpha}$
$\omega^{\#1}_{1^+}\dagger^{\alpha\beta}$	$k^2 r_5 - \frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	0	0	0	0
$\omega^{\#2}_{1^+}\dagger^{\alpha\beta}$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0	0
$f^{\#1}_{1^+}\dagger^{\alpha\beta}$	$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0	0	0
$\omega^{\#1}_{1^-}\dagger^\alpha$	0	0	0	$\frac{1}{6}(6k^2 r_5 + t_1 + 4t_3)$	$\frac{t_1 - 2t_3}{3\sqrt{2}}$	0	$\frac{1}{3}ik(t_1 - 2t_3)$
$\omega^{\#2}_{1^-}\dagger^\alpha$	0	0	0	$\frac{t_1 - 2t_3}{3\sqrt{2}}$	$\frac{t_1 + t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}\,k(t_1 + t_3)$
$f^{\#1}_{1^-}\dagger^\alpha$	0	0	0	0	0	0	0
$f^{\#2}_{1^-}\dagger^\alpha$	0	0	0	$-\frac{1}{3}ik(t_1 - 2t_3)$	$-\frac{1}{3}i\sqrt{2}\,k(t_1 + t_3)$	0	$\frac{2}{3}k^2(t_1 + t_3)$

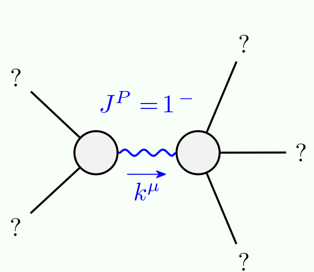
	$\sigma^{\#1}_{0^+}$	$\tau^{\#1}_{0^+}$	$\tau^{\#2}_{0^+}$	$\sigma^{\#1}_{0^-}$
$\sigma^{\#1}_{0^+}\dagger$	$\frac{1}{(1+2k^2)^2 t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	0	0
$\tau^{\#1}_{0^+}\dagger$	$\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	$\frac{2k^2}{(1+2k^2)^2 t_3}$	0	0
$\tau^{\#2}_{0^+}\dagger$	0	0	0	0
$\sigma^{\#1}_{0^-}\dagger$	0	0	0	$-\frac{1}{t_1}$

	$\sigma^{\#1}_{1^+\alpha\beta}$	$\sigma^{\#2}_{1^+\alpha\beta}$	$\tau^{\#1}_{1^+\alpha\beta}$	$\sigma^{\#1}_{1^-\alpha}$	$\sigma^{\#2}_{1^-\alpha}$	$\tau^{\#1}_{1^-\alpha}$	$\tau^{\#2}_{1^-\alpha}$
$\sigma^{\#1}_{1^+}\dagger^{\alpha\beta}$	0	$-\frac{\sqrt{2}}{t_1 + k^2 t_1}$	$-\frac{i\sqrt{2}k}{t_1 + k^2 t_1}$	0	0	0	0
$\sigma^{\#2}_{1^+}\dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{t_1 + k^2 t_1}$	$\frac{-2k^2 r_5 + t_1}{(1+k^2)^2 t_1^2}$	$-\frac{i(2k^3 r_5 - k t_1)}{(1+k^2)^2 t_1^2}$	0	0	0	0
$\tau^{\#1}_{1^+}\dagger^{\alpha\beta}$	$\frac{i\sqrt{2}k}{t_1 + k^2 t_1}$	$\frac{i(2k^3 r_5 - k t_1)}{(1+k^2)^2 t_1^2}$	$\frac{-2k^4 r_5 + k^2 t_1}{(1+k^2)^2 t_1^2}$	0	0	0	0
$\sigma^{\#1}_{1^-}\dagger^\alpha$	0	0	0	$\frac{2(t_1 + t_3)}{3t_1 t_3 + 2k^2 r_5(t_1 + t_3)}$	$-\frac{\sqrt{2}(t_1 - 2t_3)}{(1+2k^2)(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$	0	$-\frac{2ik(t_1 - 2t_3)}{(1+2k^2)(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$
$\sigma^{\#2}_{1^-}\dagger^\alpha$	0	0	0	$-\frac{\sqrt{2}(t_1 - 2t_3)}{(1+2k^2)(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$	$\frac{6k^2 r_5 + t_1 + 4t_3}{(1+2k^2)^2(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$	0	$\frac{i\sqrt{2}k(6k^2 r_5 + t_1 + 4t_3)}{(1+2k^2)^2(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$
$\tau^{\#1}_{1^-}\dagger^\alpha$	0	0	0	0	0	0	0
$\tau^{\#2}_{1^-}\dagger^\alpha$	0	0	0	$\frac{2ik(t_1 - 2t_3)}{(1+2k^2)(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$	$-\frac{i\sqrt{2}k(6k^2 r_5 + t_1 + 4t_3)}{(1+2k^2)^2(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$	0	$\frac{2k^2(6k^2 r_5 + t_1 + 4t_3)}{(1+2k^2)^2(3t_1 t_3 + 2k^2 r_5(t_1 + t_3))}$

Quadratic (free) action

$$S == \iiiint\Big(\tfrac{1}{6}\big(2\,\omega^{\alpha\iota}{}_\alpha\,(t_1\,\omega_\iota{}^\theta{}_\theta - 2t_3\,\omega_\iota{}^\kappa{}_\kappa) + 6\,f^{\alpha\beta}\,\tau_{\alpha\beta} + 6\,\omega^{\alpha\beta\chi}\,\sigma_{\alpha\beta\chi} -$$
$$4t_1\,\omega_\alpha{}^\theta{}_\theta\,\partial_\iota f^{\alpha\iota} + 8t_3\,\omega_\alpha{}^\kappa{}_\kappa\,\partial_\iota f^{\alpha\iota} + 4t_1\,\omega_\iota{}^\theta{}_\theta\,\partial^\iota f^\alpha{}_\alpha -$$
$$8t_3\,\omega_\iota{}^\kappa{}_\kappa\,\partial^\iota f^\alpha{}_\alpha - 2t_1\,\partial_\iota f^\theta{}_\theta\,\partial^\iota f^\alpha{}_\alpha + 4t_3\,\partial_\iota f^\kappa{}_\kappa\,\partial^\iota f^\alpha{}_\alpha -$$
$$2t_1\,\partial_\iota f^{\alpha\iota}\,\partial_\theta f_\alpha{}^\theta + 4t_1\,\partial^\iota f^\alpha{}_\alpha\,\partial_\theta f_\iota{}^\theta - 6t_1\,\partial_\alpha f_{\iota\theta}\,\partial^\theta f^{\alpha\iota} -$$
$$3t_1\,\partial_\alpha f_{\theta\iota}\,\partial^\theta f^{\alpha\iota} + 3t_1\,\partial_\iota f_{\alpha\theta}\,\partial^\theta f^{\alpha\iota} + 3t_1\,\partial_\theta f_{\alpha\iota}\,\partial^\theta f^{\alpha\iota} +$$
$$3t_1\,\partial_\theta f_{\iota\alpha}\,\partial^\theta f^{\alpha\iota} + 6t_1\,\omega_{\alpha\theta\iota}\,(\omega^{\alpha\iota\theta} + 2\partial^\theta f^{\alpha\iota}) +$$
$$6r_5\,\partial_\iota\omega_\theta{}^\kappa{}_\kappa\,\partial^\theta\omega^{\alpha\iota}{}_\alpha - 6r_5\,\partial_\theta\omega_\iota{}^\kappa{}_\kappa\,\partial^\theta\omega^{\alpha\iota}{}_\alpha +$$
$$4t_3\,\partial_\iota f^{\alpha\iota}\,\partial_\kappa f_\alpha{}^\kappa - 8t_3\,\partial^\iota f^\alpha{}_\alpha\,\partial_\kappa f_\iota{}^\kappa - 6r_5\,\partial_\alpha\omega^{\alpha\iota\theta}\,\partial_\kappa\omega_\iota{}^\kappa{}_\theta +$$
$$12r_5\,\partial^\theta\omega^{\alpha\iota}{}_\alpha\,\partial_\kappa\omega_\iota{}^\kappa{}_\theta + 6r_5\,\partial_\alpha\omega^{\alpha\iota\theta}\,\partial_\kappa\omega_\theta{}^\kappa{}_\iota -$$
$$12r_5\,\partial^\theta\omega^{\alpha\iota}{}_\alpha\,\partial_\kappa\omega_\theta{}^\kappa{}_\iota\big)\Big)[t, x, y, z]\,dz\,dy\,dx\,dt$$

Massive and massless spectra



Massive particle	
Pole residue:	$\frac{6t_1 t_3(t_1+t_3) - 3r_5(t_1^2 + 2t_3^2)}{2r_5(t_1+t_3)(-3t_1 t_3 + r_5(t_1+t_3))} > 0$
Polarisations:	3
Square mass:	$-\frac{3t_1 t_3}{2r_5 t_1 + 2r_5 t_3} > 0$
Spin:	1
Parity:	Odd

(No massless particles)

Unitarity conditions

$r_5 < 0 \,\&\&\, (t_1 < 0 \,\&\&\, 0 < t_3 < -t_1) \,||\, (t_1 > 0 \,\&\&\, (t_3 < -t_1 \,||\, t_3 > 0))$