



$a_0 < 0$

Unitarity conditions

(No massive particles)

$\Delta_{1^+}^{\#1} \Delta_{1^+}^{\#2} \Delta_{1^+}^{\#3} \Delta_{1^+}^{\#4} \Delta_{1^+}^{\#5} \Delta_{1^+}^{\#6}$	$\Delta_{1^+}^{\#1}$	$\Delta_{1^+}^{\#2}$	$\Delta_{1^+}^{\#3}$	$\Delta_{1^+}^{\#4}$	$\Delta_{1^+}^{\#5}$	$\Delta_{1^+}^{\#6}$	$\mathcal{T}_{1^+}^{\#1}$
$\Delta_{1^+}^{\#1} \dagger^{\alpha\beta}$	0	$-\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0
$\Delta_{1^+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0
$\Delta_{1^+}^{\#3} \dagger^{\alpha\beta}$	0	0	$\frac{4}{a_0}$	0	0	0	0
$\Delta_{1^+}^{\#1} \dagger^\alpha$	0	0	0	0	$-\frac{2k^2}{\sqrt{3}a_0(2+k^2)}$	0	$-\frac{2i\sqrt{2}k}{a_0(2+k^2)}$
$\Delta_{1^+}^{\#2} \dagger^\alpha$	0	0	$\frac{\sqrt{2}(4+k^2)}{a_0(2+k^2)}$	$-\frac{(4+k^2)^2}{2a_0(2+k^2)^2}$	$-\frac{k^2(5+2k^2)}{\sqrt{3}a_0(2+k^2)^2}$	$-\frac{k^2}{\sqrt{5}a_0(2+k^2)}$	$-\frac{ik(4+k^2)}{a_0(2+k^2)^2}$
$\Delta_{1^+}^{\#3} \dagger^\alpha$	0	$-\frac{2k^2}{\sqrt{3}(2a_0+a_0k^2)}$	$-\frac{k^2(2+k^2)}{2\sqrt{5}a_0(2+k^2)^2}$	$-\frac{k^2(2+k^2)}{2\sqrt{6}a_0(2+k^2)^2}$	$-\frac{76+52k^2+3k^4}{12a_0(2+k^2)^2}$	$-\frac{1}{-2a_0\frac{8a_0}{2+3k^2}}$	$-\frac{ik(6+5k^2)}{\sqrt{6}a_0(2+k^2)^2}$
$\Delta_{1^+}^{\#4} \dagger^\alpha$	0	0	$-\frac{\sqrt{5}k^2}{4a_0+2a_0k^2}$	$-\frac{\sqrt{5}k^2}{12a_0}$	$-\frac{\sqrt{5}}{6a_0+3a_0k^2}$	$-\frac{\sqrt{5}}{6a_0}$	$-\frac{i\sqrt{\frac{5}{6}}k}{a_0(2+k^2)}$
$\Delta_{1^+}^{\#5} \dagger^\alpha$	0	$\frac{\sqrt{2}k^2}{2a_0+a_0k^2}$	$-\frac{k^2(5+2k^2)}{\sqrt{3}a_0(2+k^2)^2}$	$-\frac{k^2(5+2k^2)}{3\sqrt{2}a_0(2+k^2)^2}$	$-\frac{1}{-2a_0\frac{8a_0}{2+3k^2}}$	$-\frac{\sqrt{2}(7+3k^2)}{3a_0(2+k^2)}$	$-\frac{2ik(3+k^2)}{\sqrt{3}a_0(2+k^2)^2}$
$\Delta_{1^+}^{\#6} \dagger^\alpha$	0	0	$-\frac{k^2}{\sqrt{6}(2a_0+a_0k^2)}$	$-\frac{k^2}{6a_0}$	$-\frac{\sqrt{2}(7+3k^2)}{3a_0(2+k^2)}$	$\frac{5}{3a_0}$	$-\frac{i\sqrt{\frac{2}{3}}k}{a_0(2+k^2)}$
$\mathcal{T}_{1^+}^{\#1} \dagger^\alpha$	0	$\frac{2i\sqrt{2}k}{2a_0+a_0k^2}$	$-\frac{ik(4+k^2)}{a_0(2+k^2)^2}$	$\frac{i\sqrt{\frac{5}{6}}k}{2a_0+a_0k^2}$	$-\frac{2ik(3+k^2)}{\sqrt{3}a_0(2+k^2)^2}$	$\frac{i\sqrt{\frac{2}{3}}k}{2a_0+a_0k^2}$	$\frac{2k^2}{a_0(2+k^2)^2}$

$\Delta_{0^+}^{\#1} \Delta_{0^+}^{\#2} \Delta_{0^+}^{\#3} \Delta_{0^+}^{\#4} \Delta_{0^+}^{\#5} \Delta_{0^+}^{\#6}$	$\Delta_{0^+}^{\#1}$	$\Delta_{0^+}^{\#2}$	$\Delta_{0^+}^{\#3}$	$\Delta_{0^+}^{\#4}$	$\Delta_{0^+}^{\#5}$	$\Delta_{0^+}^{\#6}$	$\mathcal{T}_{0^+}^{\#1}$
$\Delta_{0^+}^{\#1} \dagger$	0	$-\frac{2i\sqrt{2}k}{16a_0+3a_0k^2}$	$-\frac{8}{\sqrt{3}(16a_0+3a_0k^2)}$	$-\frac{2i\sqrt{2}}{a_0k}$	$-\frac{2i\sqrt{6}k}{16a_0+3a_0k^2}$	0	0
$\Delta_{0^+}^{\#2} \dagger$	$\frac{4\sqrt{6}}{16a_0+3a_0k^2}$	0	$-\frac{144}{a_0(16+3k^2)^2}$	$-\frac{8i\sqrt{3}}{16a_0k+3a_0k^3}$	$-\frac{72ik}{a_0(16+3k^2)^2}$	0	0
$\Delta_{0^+}^{\#3} \dagger$	$-\frac{4\sqrt{\frac{2}{3}}}{16a_0+3a_0k^2}$	$\frac{16(19+3k^2)}{a_0(16+3k^2)^2}$	$-\frac{16(35+6k^2)}{3a_0(16+3k^2)^2}$	$-\frac{8i\sqrt{3}}{\sqrt{3}(16a_0k+3a_0k^3)}$	$-\frac{8ik(19+3k^2)}{a_0(16+3k^2)^2}$	0	0
$\Delta_{0^+}^{\#4} \dagger$	$-\frac{8}{\sqrt{3}(16a_0+3a_0k^2)}$	$-\frac{8\sqrt{2}(10+3k^2)}{a_0(16+3k^2)^2}$	$-\frac{8\sqrt{2}(22+3k^2)}{3a_0(16+3k^2)^2}$	$-\frac{8i\sqrt{\frac{2}{3}}}{16a_0k+3a_0k^3}$	$-\frac{4i\sqrt{2}k(10+3k^2)}{a_0(16+3k^2)^2}$	0	0
$\mathcal{T}_{0^+}^{\#1} \dagger$	$\frac{2i\sqrt{2}}{a_0k}$	$-\frac{8i\sqrt{3}}{16a_0k+3a_0k^3}$	$-\frac{8i}{\sqrt{3}(16a_0k+3a_0k^3)}$	$\frac{4}{a_0k^2}$	$\frac{4\sqrt{3}}{16a_0+3a_0k^2}$	0	0
$\mathcal{T}_{0^+}^{\#2} \dagger$	$\frac{2i\sqrt{6}k}{16a_0+3a_0k^2}$	$-\frac{72ik}{a_0(16+3k^2)^2}$	$-\frac{8ik(19+3k^2)}{a_0(16+3k^2)^2}$	$-\frac{4\sqrt{3}}{16a_0+3a_0k^2}$	$-\frac{36k^2}{a_0(16+3k^2)^2}$	0	0
$\Delta_{0^+}^{\#1} \dagger$	0	0	0	0	0	$-\frac{2}{a_0}$	0

$\Delta_{3^+}^{\#1} \dagger^{\alpha\beta\chi}$

$-\frac{2}{a_0}$

$\Delta_{3^+}^{\#1} \dagger^{\alpha\beta\chi}$

$-\frac{a_0}{2}$

Source constraints	
SO(3) irreps	#
$2\mathcal{T}_{0^+}^{\#2} - ik\Delta_{0^+}^{\#2} == 0$	1
$\Delta_{0^+}^{\#3} + 2\Delta_{0^+}^{\#4} + 3\Delta_{0^+}^{\#2} == 0$	1
$6\mathcal{T}_{1^+}^{\#1\alpha} - ik(3\Delta_{1^+}^{\#2\alpha} - \Delta_{1^+}^{\#5\alpha} + \Delta_{1^+}^{\#3\alpha}) == 0$	3
$2\Delta_{1^+}^{\#6\alpha} + \Delta_{1^+}^{\#4\alpha} + 2\Delta_{1^+}^{\#5\alpha} + \Delta_{1^+}^{\#3\alpha} == 0$	3
Total #:	8

$\Gamma_{1^+}^{\#1} \Gamma_{1^+}^{\#2} \Gamma_{1^+}^{\#3} \Gamma_{1^+}^{\#4} \Gamma_{1^+}^{\#5} \Gamma_{1^+}^{\#6} h_{1^+}^{\#1}$	$\Gamma_{1^+}^{\#1}$	$\Gamma_{1^+}^{\#2}$	$\Gamma_{1^+}^{\#3}$	$\Gamma_{1^+}^{\#4}$	$\Gamma_{1^+}^{\#5}$	$\Gamma_{1^+}^{\#6}$	$h_{1^+}^{\#1}$
$\Gamma_{1^+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{a_0}{4}$	0	0	0	0	0	0
$\Gamma_{1^+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0
$\Gamma_{1^+}^{\#3} \dagger^{\alpha\beta}$	0	0	$\frac{a_0}{4}$	0	0	0	0
$\Gamma_{1^+}^{\#1} \dagger^\alpha$	0	0	0	$-\frac{a_0}{4}$	0	0	$-\frac{ia_0k}{4\sqrt{2}}$
$\Gamma_{1^+}^{\#2} \dagger^\alpha$	0	0	0	$\frac{a_0}{2\sqrt{2}}$	0	0	0
$\Gamma_{1^+}^{\#3} \dagger^\alpha$	0	0	0	0	$-\frac{a_0}{6}$	$-\frac{a_0}{6}$	$\frac{ia_0k}{4\sqrt{6}}$
$\Gamma_{1^+}^{\#4} \dagger^\alpha$	0	0	$\frac{\sqrt{5}a_0}{6}$	$-\frac{a_0}{3}$	$-\frac{\sqrt{5}a_0}{6}$	$-\frac{\sqrt{5}a_0}{6}$	$-\frac{1}{4}i\sqrt{\frac{5}{6}}a_0k$
$\Gamma_{1^+}^{\#5} \dagger^\alpha$	0	0	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}a_0$	$\frac{a_0}{3}$	$-\frac{a_0}{6\sqrt{2}}$	$\frac{ia_0k}{4\sqrt{3}}$
$\Gamma_{1^+}^{\#6} \dagger^\alpha$	0	0	$-\frac{a_0}{6}$	$-\frac{\sqrt{5}a_0}{6}$	$\frac{a_0}{6\sqrt{2}}$	$\frac{5a_0}{12}$	$\frac{ia_0k}{4\sqrt{6}}$
$h_{1^+}^{\#1} \dagger^\alpha$	0	0	$-\frac{ia_0k}{4\sqrt{2}}$	$-\frac{ia_0k}{4\sqrt{6}}$	0	0	0

Lagrangian density
$-\frac{1}{2}a_0\Gamma^{\alpha\beta\chi}_{\beta\chi\alpha}\Gamma^{\alpha\beta}_{\alpha\beta}\Gamma^{\chi}_{\beta\chi}-$
$\frac{1}{4}a_0h^{\chi}_{\chi}\partial_{\beta}\Gamma^{\alpha\beta}_{\alpha\beta}+\frac{1}{4}a_0h^{\chi}_{\chi}\partial_{\beta}\Gamma^{\alpha\beta}_{\alpha\beta}-$
$\frac{1}{2}a_0h_{\alpha\chi}\partial_{\beta}\Gamma^{\alpha\beta\chi}_{\beta\chi}+\frac{1}{2}a_0h_{\beta\chi}\partial^{\chi}\Gamma^{\alpha\beta}_{\alpha\beta}$
Added source term: $h^{\alpha\beta}\mathcal{T}_{\alpha\beta}+\Gamma^{\alpha\beta\chi}_{\alpha\beta\chi}\Delta_{\alpha\beta\chi}$

$\Gamma_{2^+}^{\#1} \Gamma_{2^+}^{\#2} \Gamma_{2^+}^{\#3} h_{2^+}^{\#1} \Gamma_{2^+}^{\#1} \Gamma_{2^+}^{\#2}$	$\Gamma_{2^+}^{\#1}$	$\Gamma_{2^+}^{\#2}$	$\Gamma_{2^+}^{\#3}$	$h_{2^+}^{\#1}$	$\Gamma_{2^+}^{\#1}$	$\Gamma_{2^+}^{\#2}$
$\Gamma_{2^+}^{\#1} \dagger^{\alpha\beta}$	$\frac{a_0}{4}$	0	0	$\frac{ia_0k}{4\sqrt{2}}$	0	0
$\Gamma_{2^+}^{\#2} \dagger^{\alpha\beta}$	0	$-\frac{a_0}{2}$	0	$\frac{ia_0k}{4\sqrt{3}}$	0	0
$\Gamma_{2^+}^{\#3} \dagger^{\alpha\beta}$	0	0	$\frac{a_0}{4}$	$-\frac{ia_0k}{4\sqrt{6}}$	0	0
$h_{2^+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{ia_0k}{4\sqrt{2}}$	$-\frac{ia_0k}{4\sqrt{3}}$	$\frac{ia_0k}{4\sqrt{6}}$	0	0	0
$\Gamma_{2^+}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	0	0	$\frac{a_0}{4}$	0
$\Gamma_{2^+}^{\#2} \dagger^{\alpha\beta\chi}$	0	0	0	0	0	$\frac{a_0}{4}$

$\Gamma_{0^+}^{\#1} \Gamma_{0^+}^{\#2} \Gamma_{0^+}^{\#3} \Gamma_{0^+}^{\#4} h_{0^+}^{\#1} h_{0^+}^{\#2} \Gamma_{0^+}^{\#1}$	$\Gamma_{0^+}^{\#1}$	$\Gamma_{0^+}^{\#2}$	$\Gamma_{0^+}^{\#3}$	$\Gamma_{0^+}^{\#4}$	$h_{0^+}^{\#1}$	$h_{0^+}^{\#2}$	$\Gamma_{0^+}^{\#1}$
$\Gamma_{0^+}^{\#1} \dagger$	$-\frac{a_0}{2}$	0	0	0	$-\frac{ia_0k}{2\sqrt{2}}$	0	0
$\Gamma_{0^+}^{\#2} \dagger$	0	0	$\frac{a_0}{2}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
$\Gamma_{0^+}^{\#3} \dagger$	0	$\frac{a_0}{2}$	0	$-\frac{a_0}{2\sqrt{2}}$	$\frac{ia_0k}{4\sqrt{3}}$	$-\frac{1}{4}ia_0k$	0
$\Gamma_{0^+}^{\#4} \dagger$	0	$-\frac{a_0}{2\sqrt{2}}$	$-\frac{a_0}{2\sqrt{2}}$	$\frac{a_0}{2}$	$-\frac{ia_0k}{4\sqrt{6}}$	$\frac{ia_0k}{4\sqrt{2}}$	0
$h_{0^+}^{\#1} \dagger$	$\frac{ia_0k}{2\sqrt{2}}$	0	$-\frac{ia_0k}{4\sqrt{3}}$	$\frac{ia_0k}{4\sqrt{6}}$	0	0	0
$h_{0^+}^{\#2} \dagger$	0	0	$\frac{ia_0k}{4}$	$-\frac{ia_0k}{4\sqrt{2}}$	0	0	0
$\Gamma_{0^+}^{\#1} \dagger$	0	0	0	0	0	0	$-\frac{a_0}{2}$

$\Delta_{2^+}^{\#1} \Delta_{2^+}^{\#2} \Delta_{2^+}^{\#3} \mathcal{T}_{2^+}^{\#1} \Delta_{2^+}^{\#1} \Delta_{2^+}^{\#2}$	$\Delta_{2^+}^{\#1}$	$\Delta_{2^+}^{\#2}$	$\Delta_{2^+}^{\#3}$	$\mathcal{T}_{2^+}^{\#1}$	$\Delta_{2^+}^{\#1}$	$\Delta_{2^+}^{\#2}$
$\Delta_{2^+}^{\#1} \dagger^{\alpha\beta}$	0	$\frac{2\sqrt{\frac{2}{3}}}{a_0}$	$\frac{4}{\sqrt{3}a_0}$	$\frac{4i\sqrt{2}}{a_0k}$	0	0
$\Delta_{2^+}^{\#2} \dagger^{\alpha\beta}$	$\frac{2\sqrt{\frac{2}{3}}}{a_0}$	$-\frac{8}{3a_0}$	$-\frac{2\sqrt{2}}{3a_0}$	$-\frac{4i}{\sqrt{3}a_0k}$	0	0
$\Delta_{2^+}^{\#3} \dagger^{\alpha\beta}$	$\frac{4}{\sqrt{3}a_0}$	$-\frac{2\sqrt{2}}{3a_0}$	$\frac{8}{3a_0}$	$-\frac{4i\sqrt{\frac{2}{3}}}{a_0k}$	0	0
$\mathcal{T}_{2^+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{4i\sqrt{2}}{a_0k}$	$\frac{4i}{\sqrt{3}a_0k}$	$\frac{4i\sqrt{\frac{2}{3}}}{a_0k}$	$-\frac{8}{a_0k^2}$	0	0
$\Delta_{2^+}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	0	0	$\frac{4}{a_0}$	0
$\Delta_{2^+}^{\#2} \dagger^{\alpha\beta\chi}$	0	0	0	0	0	$\frac{4}{a_0}$