

PSALTer results panel

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$$\iiint\!\!\!\int(\mathcal{A}^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}+f^{\alpha\beta}\tau(\Delta+\mathcal{K})_{\alpha\beta}+2\beta_1(-\mathcal{A}_{\alpha\chi\beta}\mathcal{A}^{\alpha\beta\chi}+(2\mathcal{A}_{\beta\chi\alpha}-\partial_\alpha f_{\chi\beta}+\partial_\chi f_{\alpha\beta})\partial^\chi f^{\alpha\beta}+\mathcal{A}_{\alpha\beta\chi}(\mathcal{A}^{\alpha\beta\chi}+2\partial^\chi f^{\alpha\beta}))+2\alpha_1(-\partial_\chi\mathcal{A}_{\alpha\beta\delta}+\partial_\delta\mathcal{A}_{\alpha\beta\chi})\partial^\delta\mathcal{A}^{\alpha\beta\chi})[t,\chi,y,z]$$

$$dz\,dy\,dx\,dt$$

Wave operator

$0^+\mathcal{A}^{\parallel}$	0^+f^{\parallel}	0^+f^{\perp}	$0^+\mathcal{A}^{\parallel}$								
$0^+\mathcal{A}^{\parallel}\dagger$	$\beta_1+2\alpha_1k^2-i\sqrt{2}\beta_1k$	0	0	0	$1^+\mathcal{A}^{\parallel}_{\alpha\beta}$	$1^+\mathcal{A}^{\perp}_{\alpha\beta}$	$1^+f^{\parallel}_{\alpha\beta}$	$1^+\mathcal{A}^{\parallel}_{\alpha}$	$1^+\mathcal{A}^{\perp}_{\alpha}$	$1^+f^{\parallel}_{\alpha}$	$1^+f^{\perp}_{\alpha}$
$0^+f^{\parallel}\dagger$	$i\sqrt{2}\beta_1k$	$2\beta_1k^2$	0	0	$1^+\mathcal{A}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{A}^{\perp}\dagger^{\alpha\beta}$	$1^+f^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{A}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{A}^{\perp}\dagger^{\alpha}$	$1^+f^{\parallel}\dagger^{\alpha}$	$1^+f^{\perp}\dagger^{\alpha}$
$0^+f^{\perp}\dagger$	0	0	0	0	$1^+\mathcal{A}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{A}^{\perp}\dagger^{\alpha\beta}$	$1^+f^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{A}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{A}^{\perp}\dagger^{\alpha}$	$1^+f^{\parallel}\dagger^{\alpha}$	$1^+f^{\perp}\dagger^{\alpha}$
$0^+\mathcal{A}^{\parallel}\dagger$	0	0	0	$4\beta_1+2\alpha_1k^2$	$1^+\mathcal{A}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{A}^{\perp}\dagger^{\alpha\beta}$	$1^+f^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{A}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{A}^{\perp}\dagger^{\alpha}$	$1^+f^{\parallel}\dagger^{\alpha}$	$1^+f^{\perp}\dagger^{\alpha}$
				$1^+\mathcal{A}^{\parallel}\dagger^{\alpha\beta}$	$3\beta_1+2\alpha_1k^2$	$\sqrt{2}\beta_1$	$i\sqrt{2}\beta_1k$	0	0	0	0
				$1^+\mathcal{A}^{\perp}\dagger^{\alpha\beta}$	$\sqrt{2}\beta_1$	$2\beta_1$	$2i\beta_1k$	0	0	0	0
				$1^+f^{\parallel}\dagger^{\alpha\beta}$	$-i\sqrt{2}\beta_1k$	$-2i\beta_1k$	$2\beta_1k^2$	0	0	0	0
				$1^+\mathcal{A}^{\parallel}\dagger^{\alpha}$	0	0	0	$\beta_1+2\alpha_1k^2$	0	0	0
				$1^+\mathcal{A}^{\perp}\dagger^{\alpha}$	0	0	0	0	β_1	0	$i\sqrt{2}\beta_1k$
				$1^+f^{\parallel}\dagger^{\alpha}$	0	0	0	0	0	0	0
				$1^+f^{\perp}\dagger^{\alpha}$	0	0	0	0	$-i\sqrt{2}\beta_1k$	0	$2\beta_1k^2$
						$2^+\mathcal{A}^{\parallel}_{\alpha\beta}$	$2^+f^{\parallel}_{\alpha\beta}$	$2^+\mathcal{A}^{\parallel}_{\alpha\beta\chi}$			
						$2^+\mathcal{A}^{\parallel}\dagger^{\alpha\beta}$	$\beta_1+2\alpha_1k^2-i\sqrt{2}\beta_1k$	0			
						$2^+f^{\parallel}\dagger^{\alpha\beta}$	$i\sqrt{2}\beta_1k$	$2\beta_1k^2$	0		
						$2^+\mathcal{A}^{\parallel}\dagger^{\alpha\beta\chi}$	0	0	$\beta_1+2\alpha_1k^2$		

Saturated propagator

$0^+\mathcal{O}^{\parallel}$	$0^+\mathcal{T}^{\parallel}$	$0^+\mathcal{T}^{\perp}$	$0^+\mathcal{O}^{\parallel}$								
$0^+\mathcal{O}^{\parallel}\dagger$	$\frac{1}{2\alpha_1k^2}$	$\frac{i}{2\sqrt{2}\alpha_1k^3}$	0	0	$1^+\mathcal{O}^{\parallel}_{\alpha\beta}$	$1^+\mathcal{O}^{\perp}_{\alpha\beta}$	$1^+\mathcal{T}^{\parallel}_{\alpha\beta}$	$1^+\mathcal{O}^{\parallel}_{\alpha}$	$1^+\mathcal{O}^{\perp}_{\alpha}$	$1^+\mathcal{T}^{\parallel}_{\alpha}$	$1^+\mathcal{T}^{\perp}_{\alpha}$
$0^+\mathcal{T}^{\parallel}\dagger$	$-\frac{i}{2\sqrt{2}\alpha_1k^3}$	$\frac{\beta_1+2\alpha_1k^2}{4\alpha_1\beta_1k^4}$	0	0	$1^+\mathcal{O}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{O}^{\perp}\dagger^{\alpha\beta}$	$1^+\mathcal{T}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{O}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{O}^{\perp}\dagger^{\alpha}$	$1^+\mathcal{T}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{T}^{\perp}\dagger^{\alpha}$
$0^+\mathcal{T}^{\perp}\dagger$	0	0	0	0	$1^+\mathcal{O}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{O}^{\perp}\dagger^{\alpha\beta}$	$1^+\mathcal{T}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{O}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{O}^{\perp}\dagger^{\alpha}$	$1^+\mathcal{T}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{T}^{\perp}\dagger^{\alpha}$
$0^+\mathcal{O}^{\parallel}\dagger$	0	0	0	$\frac{1}{4\beta_1+2\alpha_1k^2}$	$1^+\mathcal{O}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{O}^{\perp}\dagger^{\alpha\beta}$	$1^+\mathcal{T}^{\parallel}\dagger^{\alpha\beta}$	$1^+\mathcal{O}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{O}^{\perp}\dagger^{\alpha}$	$1^+\mathcal{T}^{\parallel}\dagger^{\alpha}$	$1^+\mathcal{T}^{\perp}\dagger^{\alpha}$
				$1^+\mathcal{O}^{\parallel}\dagger^{\alpha\beta}$	$\frac{1}{2\beta_1+2\alpha_1k^2}$	$-\frac{1}{2\sqrt{2}(1+k^2)(\beta_1+\alpha_1k^2)}$	$-\frac{ik}{2\sqrt{2}(1+k^2)(\beta_1+\alpha_1k^2)}$	0	0	0	0
				$1^+\mathcal{O}^{\perp}\dagger^{\alpha\beta}$	$-\frac{1}{2\sqrt{2}(1+k^2)(\beta_1+\alpha_1k^2)}$	$\frac{3\beta_1+2\alpha_1k^2}{4\beta_1(1+k^2)^2(\beta_1+\alpha_1k^2)}$	$\frac{ik(3\beta_1+2\alpha_1k^2)}{4\beta_1(1+k^2)^2(\beta_1+\alpha_1k^2)}$	0	0	0	0
				$1^+\mathcal{T}^{\parallel}\dagger^{\alpha\beta}$	$\frac{ik}{2\sqrt{2}(1+k^2)(\beta_1+\alpha_1k^2)}$	$-\frac{ik(3\beta_1+2\alpha_1k^2)}{4\beta_1(1+k^2)^2(\beta_1+\alpha_1k^2)}$	$\frac{k^2(3\beta_1+2\alpha_1k^2)}{4\beta_1(1+k^2)^2(\beta_1+\alpha_1k^2)}$	0	0	0	0
				$1^+\mathcal{O}^{\parallel}\dagger^{\alpha}$	0	0	0	$\frac{1}{\beta_1+2\alpha_1k^2}$	0	0	0
				$1^+\mathcal{O}^{\perp}\dagger^{\alpha}$	0	0	0	0	$\frac{1}{\beta_1(1+2k^2)^2}$	0	$\frac{i\sqrt{2}k}{\beta_1(1+2k^2)^2}$
				$1^+\mathcal{T}^{\parallel}\dagger^{\alpha}$	0	0	0	0	0	0	0
				$1^+\mathcal{T}^{\perp}\dagger^{\alpha}$	0	0	0	0	$-\frac{i\sqrt{2}k}{\beta_1(1+2k^2)^2}$	0	$\frac{2k^2}{\beta_1(1+2k^2)^2}$
						$2^+\mathcal{O}^{\parallel}_{\alpha\beta}$	$2^+\mathcal{T}^{\parallel}_{\alpha\beta}$	$2^+\mathcal{O}^{\parallel}_{\alpha\beta\chi}$			
						$2^+\mathcal{O}^{\parallel}\dagger^{\alpha\beta}$	$\frac{1}{2\alpha_1k^2}$	$\frac{i}{2\sqrt{2}\alpha_1k^3}$	0		
						$2^+\mathcal{T}^{\parallel}\dagger^{\alpha\beta}$	$-\frac{i}{2\sqrt{2}\alpha_1k^3}$	$\frac{\beta_1+2\alpha_1k^2}{4\alpha_1\beta_1k^4}$	0		
						$2^+\mathcal{O}^{\parallel}\dagger^{\alpha\beta\chi}$	0	0	$\frac{1}{\beta_1+2\alpha_1k^2}$		

Source constraints

Spin-parity form	Covariant form	Multiplicities
$0^+\mathcal{T}^{\perp}==0$	$\partial_\beta\partial_\alpha\tau(\Delta+\mathcal{K})^{\alpha\beta}==0$	1
$1^-\mathcal{T}^{\parallel\alpha}==0$	$\partial_\chi\partial_\beta\partial^\alpha\tau(\Delta+\mathcal{K})^{\beta\chi}==\partial_\chi\partial^\chi\partial_\beta\tau(\Delta+\mathcal{K})^{\beta\alpha}$	3
$2ik1^-\mathcal{O}^{\perp\alpha}+1^-\mathcal{T}^{\perp\alpha}==0$	$\partial_\chi\partial_\beta\partial^\alpha\tau(\Delta+\mathcal{K})^{\beta\chi}==\partial_\chi\partial^\chi\partial_\beta\tau(\Delta+\mathcal{K})^{\alpha\beta}+2\partial_\delta\partial^\delta\partial_\chi\partial_\beta\sigma^{\beta\alpha\chi}$	3
$ik1^-\mathcal{O}^{\perp\alpha\beta}+1^-\mathcal{T}^{\parallel\alpha\beta}==0$	$\partial_\chi\partial^\alpha\tau(\Delta+\mathcal{K})^{\beta\chi}+\partial_\chi\partial^\beta\tau(\Delta+\mathcal{K})^{\chi\alpha}+\partial_\chi\partial^\chi\tau(\Delta+\mathcal{K})^{\alpha\beta}+2\partial_\delta\partial_\chi\partial^\alpha\sigma^{\chi\beta\delta}+2\partial_\delta\partial^\delta\partial_\chi\sigma^{\chi\alpha\beta}==\partial_\chi\partial^\alpha\tau(\Delta+\mathcal{K})^{\chi\beta}+\partial_\chi\partial^\beta\tau(\Delta+\mathcal{K})^{\alpha\chi}+\partial_\chi\partial^\chi\tau(\Delta+\mathcal{K})^{\beta\alpha}+2\partial_\delta\partial_\chi\partial^\beta\sigma^{\chi\alpha\delta}$	3
Total expected gauge generators:		10

Massive spectrum

$J^P = 0^-$
 $k^\mu = (\mathcal{E}, 0, 0, p)$

$J^P = 1^+$
 $k^\mu = (\mathcal{E}, 0, 0, p)$

Massive particle

Pole residue:	$-\frac{1}{2\alpha_1} > 0$
Square mass:	$-\frac{2\beta_1}{\alpha_1} > 0$
Spin:	0
Parity:	Odd

Massive particle

Pole residue:	$\frac{3\alpha_1-2\beta_1}{4\alpha_1{}^24\alpha_1\beta_1} > 0$
Square mass:	$-\frac{\beta_1}{\alpha_1} > 0$
Spin:	1
Parity:	Even

$J^P = 1^-$
 $k^\mu = (\mathcal{E}, 0, 0, p)$

$J^P = 2^-$
 $k^\mu = (\mathcal{E}, 0, 0, p)$

Massive particle

Pole residue:	$-\frac{1}{2\alpha_1} > 0$
Square mass:	$-\frac{\beta_1}{2\alpha_1} > 0$
Spin:	1
Parity:	Odd

Massive particle

Pole residue:	$-\frac{1}{2\alpha_1} > 0$
Square mass:	$-\frac{\beta_1}{2\alpha_1} > 0$
Spin:	2
Parity:	Odd

Massless spectrum

$k^\mu = (p, 0, 0, p)$

$k^\mu = (p, 0, 0, p)$

Massless particle

Pole residue:	$\frac{7}{\alpha_1} + \frac{2p^2}{\beta_1} + \frac{4\alpha_1p^4}{\beta_1{}^2} > 0$
Polarisations:	2

Massless particle

Pole residue:	$-\frac{1}{\alpha_1\beta_1{}^2}(\beta_1{}^2+28\alpha_1\beta_1p^2+3\sqrt{(\beta_1{}^2(9\beta_1{}^2-8\alpha_1\beta_1p^2+144\alpha_1{}^2p^4)))} > 0$
Polarisations:	3

$k^\mu = (p, 0, 0, p)$

$k^\mu = (p, 0, 0, p)$
 $k^\mu = (\mathcal{E}, 0, 0, p)$

Massless particle

Pole residue:	$\frac{1}{\alpha_1\beta_1{}^2}(-\beta_1(\beta_1+28\alpha_1p^2)+3\sqrt{(\beta_1{}^2(9\beta_1{}^2-8\alpha_1\beta_1p^2+144\alpha_1{}^2p^4)))} > 0$
Polarisations:	3

Quartic pole

Pole residue:	$0 < \frac{p^2}{\alpha_1} \ \&\& \ \frac{p^2}{\alpha_1} > 0$
Polarisations:	3

Unitarity conditions

(Demonstrably impossible)