

Particle spectrograph

Wave operator and propagator

$\Delta_{1^+}^{\#1} \uparrow \alpha\beta$	$\Delta_{1^+}^{\#2} \uparrow \alpha\beta$	$\Delta_{1^+}^{\#3} \uparrow \alpha\beta$	$\Delta_{1^+}^{\#1} \uparrow \alpha$	$\Delta_{1^+}^{\#2} \uparrow \alpha$	$\Delta_{1^+}^{\#3} \uparrow \alpha$	$\Delta_{1^+}^{\#4} \uparrow \alpha$	$\Delta_{1^+}^{\#5} \uparrow \alpha$	$\Delta_{1^+}^{\#6} \uparrow \alpha$	$\mathcal{T}_{1^+}^{\#1} \uparrow \alpha$
0	$-\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0	0	0
$\Delta_{1^+}^{\#2} \uparrow \alpha\beta$	$-\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0	0	0
$\Delta_{1^+}^{\#3} \uparrow \alpha\beta$	0	$\frac{4}{a_0}$	0	0	0	0	0	0	0
$\Delta_{1^+}^{\#1} \uparrow \alpha$	0	0	0	$\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0
$\Delta_{1^+}^{\#2} \uparrow \alpha$	0	0	$\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0
$\Delta_{1^+}^{\#3} \uparrow \alpha$	0	0	0	0	$-\frac{19}{12a_0}$	$\frac{5\sqrt{5}}{12a_0}$	$-\frac{1}{6\sqrt{2}a_0}$	$-\frac{1}{6a_0}$	0
$\Delta_{1^+}^{\#4} \uparrow \alpha$	0	0	0	0	$\frac{5\sqrt{5}}{12a_0}$	$\frac{1}{12a_0}$	$-\frac{\sqrt{2}}{6a_0}$	$-\frac{\sqrt{5}}{6a_0}$	0
$\Delta_{1^+}^{\#5} \uparrow \alpha$	0	0	0	0	$-\frac{1}{6\sqrt{2}a_0}$	$-\frac{\sqrt{2}}{6a_0}$	$\frac{17}{6a_0}$	$-\frac{7}{3\sqrt{2}a_0}$	0
$\Delta_{1^+}^{\#6} \uparrow \alpha$	0	0	0	0	$-\frac{1}{6a_0}$	$-\frac{\sqrt{5}}{6a_0}$	$-\frac{7}{3\sqrt{2}a_0}$	$\frac{5}{3a_0}$	0
$\mathcal{T}_{1^+}^{\#1} \uparrow \alpha$	0	0	0	0	0	0	0	0	0

$\Gamma_{1^+}^{\#1} \uparrow \alpha\beta$	$\Gamma_{1^+}^{\#2} \uparrow \alpha\beta$	$\Gamma_{1^+}^{\#3} \uparrow \alpha\beta$	$\Gamma_{1^+}^{\#1} \uparrow \alpha$	$\Gamma_{1^+}^{\#2} \uparrow \alpha$	$\Gamma_{1^+}^{\#3} \uparrow \alpha$	$\Gamma_{1^+}^{\#4} \uparrow \alpha$	$\Gamma_{1^+}^{\#5} \uparrow \alpha$	$\Gamma_{1^+}^{\#6} \uparrow \alpha$	$h_{1^+}^{\#1} \uparrow \alpha$
$-\frac{a_0}{4}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0	0	0
$-\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0	0	0	0
0	0	$\frac{a_0}{4}$	0	0	0	0	0	0	0
0	0	0	$-\frac{a_0}{4}$	$\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0
0	0	0	$\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0
0	0	0	0	0	$-\frac{a_0}{3}$	$\frac{\sqrt{5}a_0}{6}$	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{a_0}{6}$	0
0	0	0	0	0	$\frac{\sqrt{5}a_0}{6}$	$\frac{a_0}{3}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}a_0$	$-\frac{\sqrt{5}a_0}{6}$	0
0	0	0	0	0	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}a_0$	$\frac{a_0}{3}$	$\frac{a_0}{6\sqrt{2}}$	0
0	0	0	0	0	$-\frac{a_0}{6}$	$-\frac{\sqrt{5}a_0}{6}$	$\frac{a_0}{6\sqrt{2}}$	$\frac{5a_0}{12}$	0
0	0	0	0	0	0	0	0	0	0

Quadratic (free) action

$$S = \int \int \int \int (\frac{1}{8} h^{\alpha\beta} \mathcal{T}_{\alpha\beta} - 4 \Gamma^{\alpha\beta\chi} (a_0 \Gamma_{\beta\chi\alpha} - 2 \Delta_{\alpha\beta\chi} + a_0 \partial_{\beta} h_{\alpha\chi}) + 2 a_0 \Gamma_{\alpha}^{\alpha\beta} \partial_{\beta} h^{\chi}_{\chi} - 2 a_0 h^{\chi}_{\chi} \partial_{\beta} \Gamma^{\alpha\beta}_{\chi} + 2 a_0 h^{\chi}_{\chi} \partial_{\beta} \Gamma^{\alpha\beta}_{\chi} - 4 a_0 h_{\alpha\chi} \partial_{\beta} \Gamma^{\alpha\beta\chi} + 4 a_0 h^{\alpha\beta} \partial_{\beta} \partial_{\alpha} h^{\chi}_{\chi} - a_0 \partial_{\beta} h^{\chi}_{\chi} \partial^{\beta} h^{\alpha}_{\alpha} - 4 a_0 \partial_{\alpha} h^{\alpha\beta} \partial_{\chi} h^{\chi}_{\beta} + 4 a_0 \partial^{\beta} h^{\alpha}_{\alpha} \partial_{\chi} h^{\chi}_{\beta} + 2 a_0 \Gamma^{\alpha}_{\alpha} \beta (2 \Gamma^{\chi}_{\beta\chi} - \partial_{\beta} h^{\chi}_{\chi} + 2 \partial_{\chi} h^{\chi}_{\beta}) - 8 a_0 h^{\alpha\beta} \partial_{\chi} \partial_{\beta} h^{\chi}_{\alpha} + 2 a_0 h^{\alpha}_{\alpha} \partial_{\chi} \partial_{\beta} h^{\beta\chi} + 4 a_0 h^{\alpha\beta} \partial_{\chi} \partial_{\alpha} h_{\alpha\beta} - 2 a_0 h^{\alpha}_{\alpha} \partial_{\chi} \partial^{\chi} h^{\beta}_{\beta} - 2 a_0 \partial_{\beta} h_{\alpha\chi} \partial^{\chi} h^{\alpha\beta} + 3 a_0 \partial_{\chi} h_{\alpha\beta} \partial^{\chi} h^{\alpha\beta} + 4 a_0 h_{\beta\chi} \partial^{\chi} (\Gamma^{\alpha}_{\alpha} \beta)) [t, x, y, z] dz dy dx dt$$

$\Delta_{0^+}^{\#1} \uparrow$	$\Delta_{0^+}^{\#2} \uparrow$	$\Delta_{0^+}^{\#3} \uparrow$	$\Delta_{0^+}^{\#4} \uparrow$	$\mathcal{T}_{0^+}^{\#1} \uparrow$	$\mathcal{T}_{0^+}^{\#2} \uparrow$	$\Delta_{0^+}^{\#1} \uparrow$
$-\frac{2}{a_0}$	0	0	0	0	0	0
0	$-\frac{3}{4a_0}$	$\frac{5}{4a_0}$	$-\frac{1}{2\sqrt{2}a_0}$	0	0	0
0	$\frac{5}{4a_0}$	$-\frac{3}{4a_0}$	$-\frac{1}{2\sqrt{2}a_0}$	0	0	0
0	$-\frac{1}{2\sqrt{2}a_0}$	$-\frac{1}{2\sqrt{2}a_0}$	$\frac{1}{2a_0}$	0	0	0
$\mathcal{T}_{0^+}^{\#1} \uparrow$	0	0	0	$\frac{4}{a_0 k^2}$	0	0
$\mathcal{T}_{0^+}^{\#2} \uparrow$	0	0	0	0	0	0
$\Delta_{0^+}^{\#1} \uparrow$	0	0	0	0	0	$-\frac{2}{a_0}$

$\Delta_{2^+}^{\#1} \uparrow \alpha\beta$	$\Delta_{2^+}^{\#2} \uparrow \alpha\beta$	$\Delta_{2^+}^{\#3} \uparrow \alpha\beta$	$\mathcal{T}_{2^+}^{\#1} \uparrow \alpha\beta$	$\Delta_{2^+}^{\#1} \uparrow \alpha\beta\chi$	$\Delta_{2^+}^{\#2} \uparrow \alpha\beta\chi$
$\frac{4}{a_0}$	0	0	0	0	0
0	$-\frac{2}{a_0}$	0	0	0	0
0	0	$\frac{4}{a_0}$	0	0	0
0	0	0	$-\frac{8}{a_0 k^2}$	0	0
0	0	0	0	$\frac{4}{a_0}$	0
0	0	0	0	0	$\frac{4}{a_0}$

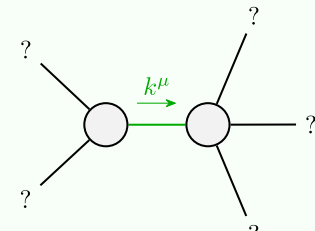
$\Gamma_{2^+}^{\#1} \uparrow \alpha\beta$	$\Gamma_{2^+}^{\#2} \uparrow \alpha\beta$	$\Gamma_{2^+}^{\#3} \uparrow \alpha\beta$	$h_{2^+}^{\#1} \uparrow \alpha\beta$	$\Gamma_{2^+}^{\#1} \uparrow \alpha\beta\chi$	$\Gamma_{2^+}^{\#2} \uparrow \alpha\beta\chi$
$\frac{a_0}{4}$	0	0	0	0	0
0	$-\frac{a_0}{2}$	0	0	0	0
0	0	$\frac{a_0}{4}$	0	0	0
0	0	0	$-\frac{a_0 k^2}{8}$	0	0
0	0	0	0	$\frac{a_0}{4}$	0
0	0	0	0	0	$\frac{a_0}{4}$

$\Gamma_{0^+}^{\#1} \uparrow$	$\Gamma_{0^+}^{\#2} \uparrow$	$\Gamma_{0^+}^{\#3} \uparrow$	$\Gamma_{0^+}^{\#4} \uparrow$	$h_{0^+}^{\#1} \uparrow$	$h_{0^+}^{\#2} \uparrow$	$\Gamma_{0^+}^{\#1} \uparrow$
$-\frac{a_0}{2}$	0	0	0	0	0	0
0	0	$\frac{a_0}{2}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
0	$\frac{a_0}{2}$	0	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
0	$-\frac{a_0}{2\sqrt{2}}$	$-\frac{a_0}{2\sqrt{2}}$	$\frac{a_0}{2}$	0	0	0
0	0	0	0	$\frac{a_0 k^2}{4}$	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	$-\frac{a_0}{2}$

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\mathcal{T}_{0^+}^{\#2} == 0$	1
$\Delta_{0^+}^{\#3} + 2 \Delta_{0^+}^{\#4} + 3 \Delta_{0^+}^{\#2} == 0$	1
$\mathcal{T}_{1^+}^{\#1\alpha} == 0$	3
$2 \Delta_{1^+}^{\#6\alpha} + \Delta_{1^+}^{\#4\alpha} + 2 \Delta_{1^+}^{\#5\alpha} + \Delta_{1^+}^{\#3\alpha} == 0$	3
Total constraints:	8

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{a_0} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$a_0 < 0$