

# Particle spectrograph

## Wave operator and propagator

Quadratic (free) Lagrangian density

$$\phi \rho + h^{\alpha\beta} \mathcal{T}_{\alpha\beta} + \beta \partial_\alpha \phi \partial^\alpha \phi + \frac{1}{2} \alpha \partial_\beta h^\chi{}_\chi \partial^\beta h^\alpha{}_\alpha +$$
$$\alpha \partial_\alpha h^{\alpha\beta} \partial_\chi h_\beta{}^\chi - \alpha \partial^\beta h^\alpha{}_\alpha \partial_\chi h_\beta{}^\chi - \frac{1}{2} \alpha \partial_\chi h_{\alpha\beta} \partial^\chi h^{\alpha\beta}$$

| Source constraints/gauge generators | Multiplicities |
|-------------------------------------|----------------|
| SO(3) irreps                        |                |
| $\mathcal{T}^{\#2}_{0+} == 0$       | 1              |
| $\mathcal{T}^{\#1\alpha}_1 == 0$    | 3              |
| Total constraints:                  | 4              |

|                            |                          |                       |
|----------------------------|--------------------------|-----------------------|
| $\mathcal{T}^{\#1}_{0+} +$ | $\mathcal{T}^{\#2}_{0+}$ | $\rho^{\#1}_{0+}$     |
| $\mathcal{T}^{\#2}_{0+} +$ |                          |                       |
| $\rho^{\#1}_{0+} +$        |                          |                       |
| 0                          | $\frac{1}{\alpha k^2}$   | 0                     |
| 0                          | 0                        | 0                     |
| 0                          | 0                        | $\frac{1}{\beta k^2}$ |

|                     |                |                |                   |
|---------------------|----------------|----------------|-------------------|
|                     | $h^{\#1}_{0+}$ | $h^{\#2}_{0+}$ | $\phi^{\#1}_{0+}$ |
| $h^{\#1}_{0+} +$    | $\alpha k^2$   | 0              | 0                 |
| $h^{\#2}_{0+} +$    | 0              | 0              | 0                 |
| $\phi^{\#1}_{0+} +$ | 0              | 0              | $\beta k^2$       |

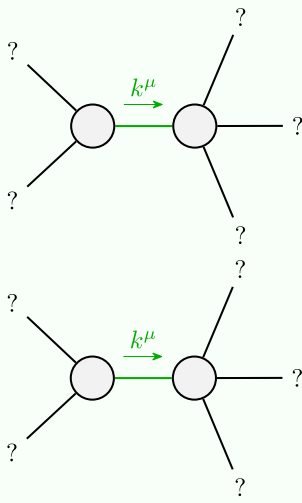
|  |                                      |
|--|--------------------------------------|
| $\mathcal{T}^{\#1}_{2+} + \alpha\beta$ | $\mathcal{T}^{\#1}_{2+} \alpha\beta$ |
|  | $-\frac{2}{\alpha k^2}$              |

|                                   |                                 |
|-----------------------------------|---------------------------------|
| $\mathcal{T}^{\#1}_{1-} + \alpha$ | $\mathcal{T}^{\#1}_{1-} \alpha$ |
|                                   | 0                               |

|                         |                       |
|-------------------------|-----------------------|
| $h^{\#1}_{1-} + \alpha$ | $h^{\#1}_{1-} \alpha$ |
|                         | 0                     |

|                              |                            |
|------------------------------|----------------------------|
| $h^{\#1}_{2+} + \alpha\beta$ | $h^{\#1}_{2+} \alpha\beta$ |
|                              | $-\frac{\alpha k^2}{2}$    |

## Massive and massless spectra



|                |                         |
|----------------|-------------------------|
| Quadratic pole |                         |
| Pole residue:  | $-\frac{1}{\alpha} > 0$ |
| Polarisations: | 2                       |

|                |                       |
|----------------|-----------------------|
| Quadratic pole |                       |
| Pole residue:  | $\frac{1}{\beta} > 0$ |
| Polarisations: | 1                     |

(No massive particles)

## Unitarity conditions

$$\alpha < 0 \ \&\& \ \beta > 0$$