



The diagram shows a particle exchange process between two pairs of external particles. The left pair consists of a black dot (particle) and a white dot (antiparticle), and the right pair also consists of a black dot and a white dot. A dashed line with an arrow pointing from left to right represents the exchange of a particle. Above the dashed line is the label $J^P = 0^-$ and below it is the label k^μ . To the right of the diagram is a table with the following content:

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

Unitarity conditions
 $r_2 < 0 \ \&\& \ t_2 > 0$

Unitarity conditions
 $r_2 < 0 \ \&\& \ t_2 > 0$

(No massless particles)

Lagrangian density

$$\begin{aligned}
& \text{Lagrangian density} \\
& \frac{2}{3} t_3 \omega_{\kappa \alpha}^{\alpha \iota} \omega_{\kappa \alpha}^{\kappa} + \frac{2}{3} t_2 \omega_{\kappa \alpha}^{\kappa \lambda} \omega_{\kappa \lambda}^{\iota} + \frac{1}{3} t_2 \omega_{\kappa \lambda}^{\iota} \omega_{\kappa \lambda}^{\kappa \lambda} + f^{\alpha \beta} \tau_{\alpha \beta} + \\
& \omega^{\alpha \beta \chi} \sigma_{\alpha \beta \chi} - r_5 \partial_{\iota} \omega_{\kappa}^{\kappa \lambda} \partial^{\iota} \omega_{\lambda}^{\alpha} + \frac{2}{3} r_2 \partial^{\beta} \omega_{\alpha}^{\theta \alpha} \partial_{\kappa} \omega_{\alpha \beta}^{\kappa} - \frac{1}{3} r_2 \partial_{\theta} \omega_{\alpha \beta}^{\kappa} \partial_{\kappa} \omega^{\alpha \beta \theta} - \\
& \frac{2}{3} r_2 \partial_{\theta} \omega_{\alpha \beta}^{\kappa} \partial_{\kappa} \omega^{\theta \alpha \beta} - r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\theta \kappa \lambda} + r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\theta \kappa \lambda} - r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\kappa \lambda \theta} + \\
& 2 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\alpha}^{\kappa \lambda \theta} + \frac{1}{6} t_2 \partial^{\alpha} f_{\theta \kappa} \partial^{\kappa} f_{\alpha}^{\theta} - \frac{1}{6} t_2 \partial_2 \partial^{\alpha} f_{\kappa \theta} \partial^{\kappa} f_{\alpha}^{\theta} + \frac{1}{6} t_2 \partial^{\alpha} f_{\kappa}^{\lambda} \partial^{\kappa} f_{\alpha \lambda} - \\
& \frac{2}{3} t_3 \omega_{\kappa \alpha}^{\alpha} \partial^{\kappa} f_{\iota}^{\iota} - \frac{2}{3} t_3 \omega_{\kappa \lambda}^{\lambda} \partial^{\kappa} f_{\iota}^{\iota} - \frac{4}{3} t_3 \partial^{\alpha} f_{\kappa \alpha} \partial^{\kappa} f_{\iota}^{\iota} + \frac{2}{3} t_3 \partial_{\kappa} f_{\lambda}^{\lambda} \partial^{\kappa} f_{\iota}^{\iota} + \\
& \frac{1}{3} t_2 \omega_{\iota \theta \kappa} \partial^{\kappa} f^{\iota \theta} - \frac{2}{3} t_2 \omega_{\iota \kappa \theta} \partial^{\kappa} f^{\iota \theta} - \frac{1}{3} t_2 \omega_{\theta \iota \kappa} \partial^{\kappa} f^{\iota \theta} + \frac{2}{3} t_2 \omega_{\theta \kappa \iota} \partial^{\kappa} f^{\iota \theta} + \\
& \frac{2}{3} t_3 \omega_{\iota \alpha}^{\alpha} \partial^{\kappa} f_{\kappa}^{\iota} + \frac{2}{3} t_3 \omega_{\iota \lambda}^{\lambda} \partial^{\kappa} f_{\kappa}^{\iota} - \frac{1}{6} t_2 \partial^{\alpha} f_{\kappa}^{\lambda} \partial^{\kappa} f_{\lambda \alpha} - \frac{1}{6} t_2 \partial_{\kappa} f_{\theta}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} + \\
& \frac{1}{6} t_2 \partial_{\kappa} f_{\theta}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} + \frac{2}{3} t_3 \partial^{\alpha} f_{\lambda}^{\theta} \partial^{\kappa} f_{\lambda \kappa} + \frac{1}{3} r_2 \partial_{\kappa} \omega^{\alpha \beta \theta} \partial^{\kappa} \omega_{\alpha \beta \theta} + \frac{2}{3} r_2 \partial_{\kappa} \omega^{\theta \alpha \beta} \partial^{\kappa} \omega_{\alpha \beta \theta} - \\
& \frac{2}{3} r_2 \partial^{\beta} \omega_{\iota}^{\alpha \lambda} \partial_{\lambda} \omega_{\alpha \beta}^{\iota} + \frac{2}{3} r_2 \partial^{\beta} \omega_{\iota}^{\lambda \alpha} \partial_{\lambda} \omega_{\alpha \beta}^{\iota} + r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\theta}^{\theta \kappa} - r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\alpha}^{\theta \kappa}
\end{aligned}$$

$\omega_1^{\#1} + \alpha\beta$	$k^2 r_5 + \frac{2t_2}{3}$	$\frac{\sqrt{2} t_2}{3}$	$\frac{1}{3} i \sqrt{2} k t_2$	$\omega_1^{\#1} - \alpha$	$\omega_1^{\#2} - \alpha$	$f_1^{\#1} - \alpha$	$f_1^{\#2} - \alpha$
$\omega_1^{\#2} + \alpha\beta$	$\frac{\sqrt{2} t_2}{3}$	$\frac{t_2}{3}$	$\frac{i k t_2}{3}$	0	0	0	0
$f_1^{\#1} + \alpha\beta$	$-\frac{1}{3} i \sqrt{2} k t_2$	$-\frac{1}{3} i k t_2$	$\frac{k^2 t_2}{3}$	0	0	0	0
$\omega_1^{\#1} + \alpha$	0	0	0	$k^2 r_5 + \frac{2t_3}{3}$	$-\frac{\sqrt{2} t_3}{3}$	0	$-\frac{2}{3} i k t_3$
$\omega_1^{\#2} + \alpha$	0	0	0	$-\frac{\sqrt{2} t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3} i \sqrt{2} k t_3$
$f_1^{\#1} + \alpha$	0	0	0	0	0	0	0
$f_1^{\#2} + \alpha$	0	0	0	$\frac{2 i k t_3}{3}$	$-\frac{1}{3} i \sqrt{2} k t_3$	0	$\frac{2 k^2 t_3}{3}$

Source constraints	
SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} - 2 \, i \, k \, \sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2 \, i \, k \, \sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i \, k \, \sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
$\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	26

	$\omega_0^{#1}$	$f_0^{#1}$	$f_0^{#2}$	$\omega_0^{#1}$
$\omega_0^{#1} \dagger$	t_3	$-i \sqrt{2} k t_3$	0	0
$f_0^{#1} \dagger$	$i \sqrt{2} k t_3$	$2 k^2 t_3$	0	0
$f_0^{#2} \dagger$	0	0	0	0
$\omega_0^{#1} \dagger$	0	0	0	$k^2 r_2 + t_2$

$$\begin{array}{c}
 \sigma_{2^+}^{\#1} \alpha\beta \quad \tau_{2^+}^{\#1} \alpha\beta \quad \sigma_{2^-}^{\#1} \alpha\beta\chi \\
 \begin{array}{|c|c|c|}
 \hline
 \sigma_{2^+}^{\#1} \dagger^{\alpha\beta} & 0 & 0 \\
 \hline
 \tau_{2^+}^{\#1} \dagger^{\alpha\beta} & 0 & 0 \\
 \hline
 \sigma_{2^-}^{\#1} \dagger^{\alpha\beta\chi} & 0 & 0 \\
 \hline
 \end{array}
 \end{array}$$

$\sigma_0^{\#1 \dagger}$	$\frac{1}{(1+2k^2)^2 t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	0	$\sigma_0^{\#1}$
$\tau_0^{\#1 \dagger}$	$\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	$\frac{2k^2}{(1+2k^2)^2 t_3}$	0	$\tau_0^{\#2}$
$\tau_0^{\#2 \dagger}$	0	0	0	$\sigma_0^{\#2}$
$\sigma_0^{\#1 \dagger}$	0	0	0	$\frac{1}{k^2 r_2 + t_2}$

$$\begin{array}{c}
 \omega_{2+}^{\#1} \quad f_{2+}^{\#1} \quad \omega_{2-}^{\#1} \\
 \omega_{2+}^{\#1} \uparrow^{\alpha\beta} \quad \omega_{2+}^{\#1} \uparrow^{\alpha\beta} \quad \omega_{2-}^{\#1} \uparrow^{\alpha\beta\chi} \\
 \begin{array}{|c|c|c|}
 \hline
 0 & 0 & 0 \\
 \hline
 0 & 0 & 0 \\
 \hline
 0 & 0 & 0 \\
 \hline
 \end{array}
 \end{array}$$