

$\omega_{2+}^{\#1} + \alpha\beta$	$f_{2+}^{\#1} + \alpha\beta$	$\omega_{2-}^{\#1} - \alpha\beta\chi$
$-\frac{\alpha_0}{4} + \beta_1$	$\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	0
$-\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	$2\beta_1 k^2$	0
0	0	$-\frac{\alpha_0}{4} + \beta_1$

$\omega_{1+}^{\#1} + \alpha\beta$	$\omega_{1+}^{\#2} - \alpha\beta$	$f_{1+}^{\#1} - \alpha\beta$	$\omega_{1-}^{\#1} - \alpha$	$\omega_{1-}^{\#2} - \alpha$	$f_{1-}^{\#1} - \alpha$	$f_{1-}^{\#2} - \alpha$
$\frac{1}{4}(\alpha_0 - 4\beta_1)$	$\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	$\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	0	0	0	0
$\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	0	0	0	0	0	0
$-\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	0	0	$\frac{1}{4}(\alpha_0 - 4\beta_1)$	$-\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	0	$-\frac{1}{2}i(\alpha_0 - 4\beta_1)k$
0	0	0	$-\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	0	0	0
0	0	0	0	0	0	0
0	0	0	$\frac{1}{2}i(\alpha_0 - 4\beta_1)k$	0	0	0

Source constraints	
SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2ik\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#2\alpha\beta} == 0$	3
Total #:	10

$\sigma_{2+}^{\#1} + \alpha\beta$	$\tau_{2+}^{\#1} + \alpha\beta$	$\sigma_{2-}^{\#1} - \alpha\beta\chi$
$-\frac{16\beta_1}{\alpha_0^2-4\alpha_0\beta_1}$	$\frac{2i\sqrt{2}}{\alpha_0 k}$	0
$-\frac{2i\sqrt{2}}{\alpha_0 k}$	$\frac{2}{\alpha_0 k^2}$	0
0	0	$\frac{1}{-\frac{\alpha_0}{4} + \beta_1}$

$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\frac{8\beta_1}{\alpha_0^2-4\alpha_0\beta_1}$	$-\frac{i\sqrt{2}}{\alpha_0 k}$	0	0
$\frac{i\sqrt{2}}{\alpha_0 k}$	$-\frac{1}{\alpha_0 k^2}$	0	0
0	0	0	0
0	0	0	$\frac{2}{\alpha_0-4\beta_1+2\alpha_3k^2}$

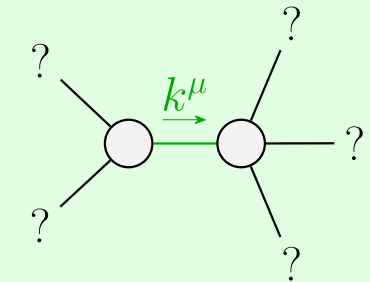
Lagrangian density

$$\begin{aligned}
&-\frac{1}{2}\alpha_0\omega_{\alpha\chi\beta}\omega^{\alpha\beta\chi}-\frac{1}{2}\alpha_0\omega_{\alpha}^{\alpha\beta}\omega_{\beta}^{\chi}+2\beta_1\omega_{\alpha}^{\alpha\beta}\omega_{\beta}^{\chi\chi}- \\
&2\beta_1\omega_{\alpha}^{\chi\delta}\omega_{\chi\delta}^{\alpha}-2\beta_1\omega_{\alpha}^{\chi}\partial_{\beta}f^{\alpha\beta}-2\beta_1\omega_{\alpha}^{\delta}\partial_{\beta}f^{\alpha\beta}-\alpha_0f^{\alpha\beta}\partial_{\beta}\omega_{\alpha}^{\chi}+ \\
&\alpha_0\partial_{\beta}\omega_{\alpha}^{\alpha\beta}+\frac{2}{3}\alpha_3\partial^{\alpha}\omega_{\chi}^{\beta\zeta}\partial_{\beta}\omega_{\zeta\alpha}^{\chi}+2\beta_1\omega_{\beta}^{\chi}\partial^{\beta}f_{\alpha}^{\alpha}+ \\
&2\beta_1\omega_{\beta}^{\delta}\partial^{\beta}f_{\alpha}^{\alpha}-2\beta_1\partial_{\beta}f^{\chi\chi}\partial^{\beta}f_{\alpha}^{\alpha}+\alpha_0f^{\alpha\beta}\partial_{\chi}\omega_{\alpha}^{\chi}- \\
&\alpha_0f_{\alpha}^{\alpha}\partial_{\chi}\omega_{\beta}^{\beta\chi}-\frac{2}{3}\alpha_3\partial_{\beta}\omega_{\zeta\alpha}^{\chi}\partial_{\chi}\omega_{\zeta\alpha}^{\beta\chi}-\frac{1}{3}\alpha_3\partial_{\beta}\omega_{\zeta\alpha}^{\chi}\partial_{\chi}\omega_{\zeta\alpha}^{\beta\chi}+ \\
&4\beta_1\omega_{\alpha\chi\beta}\partial^{\chi}f^{\alpha\beta}+\beta_1\partial_{\chi}f_{\beta}^{\delta}\partial^{\chi}f_{\delta}^{\beta}+\beta_1\partial_{\chi}f_{\beta}^{\delta}\partial^{\chi}f_{\delta}^{\beta}+ \\
&\frac{2}{3}\alpha_3\partial_{\chi}\omega_{\zeta\alpha\beta}^{\beta\zeta\alpha}\partial^{\chi}\omega_{\zeta\alpha\beta}^{\alpha}+\frac{1}{3}\alpha_3\partial_{\chi}\omega_{\zeta\alpha\beta}^{\beta\zeta\alpha}\partial^{\chi}\omega_{\zeta\alpha\beta}^{\alpha}+4\beta_1\partial^{\beta}f_{\alpha}^{\alpha}\partial_{\delta}f_{\beta}^{\delta}- \\
&2\beta_1\partial_{\beta}f_{\chi}^{\beta}\partial_{\delta}f^{\chi\delta}+\frac{2}{3}\alpha_3\partial^{\beta}\omega_{\alpha}^{\delta\zeta}\partial_{\delta}\omega_{\zeta\beta}^{\alpha}-\frac{2}{3}\alpha_3\partial^{\beta}\omega_{\alpha}^{\zeta\delta}\partial_{\delta}\omega_{\zeta\beta}^{\alpha}- \\
&\beta_1\partial^{\chi}f_{\zeta}^{\beta}\partial^{\zeta}f_{\beta\chi}^{\beta}-\beta_1\partial^{\chi}f_{\zeta}^{\beta}\partial^{\zeta}f_{\chi\beta}^{\beta}+\beta_1\partial^{\chi}f_{\delta\zeta}^{\delta}\partial^{\zeta}f_{\delta}^{\delta}-\beta_1\partial^{\chi}f_{\zeta\delta}^{\delta}\partial^{\zeta}f_{\delta}^{\delta}
\end{aligned}$$

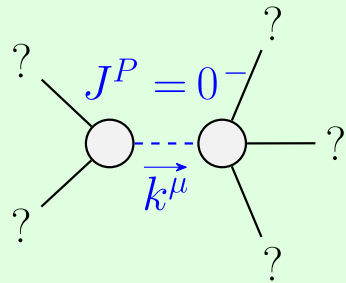
Added source term: $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\frac{1}{2}(\alpha_0-4\beta_1)$	$-\frac{i(\alpha_0-4\beta_1)k}{\sqrt{2}}$	0	0
$\frac{i(\alpha_0-4\beta_1)k}{\sqrt{2}}$	$-4\beta_1k^2$	0	0
0	0	0	0
0	0	0	$\frac{\alpha_0}{2}-2\beta_1+\alpha_3k^2$

$\sigma_{1+}^{\#1} + \alpha\beta$	$\sigma_{1+}^{\#2} - \alpha\beta$	$\tau_{1+}^{\#1} + \alpha\beta$	$\sigma_{1-}^{\#1} - \alpha$	$\sigma_{1-}^{\#2} - \alpha$	$\tau_{1-}^{\#1} - \alpha$	$\tau_{1-}^{\#2} - \alpha$
0	$\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+k^2)}$	$\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+k^2)}$	0	0	0	0
$\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+k^2)}$	$-\frac{2}{(\alpha_0-4\beta_1)(1+k^2)^2}$	$-\frac{2ik}{(\alpha_0-4\beta_1)(1+k^2)^2}$	0	0	0	0
$-\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+k^2)}$	$\frac{2ik}{(\alpha_0-4\beta_1)(1+k^2)^2}$	$-\frac{2k^2}{(\alpha_0-4\beta_1)(1+k^2)^2}$	0	0	0	0
0	0	0	0	$-\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+2k^2)}$	0	$-\frac{4ik}{(\alpha_0-4\beta_1)(1+2k^2)}$
0	0	0	$-\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+2k^2)}$	0	0	0
$\tau_{1+}^{\#1} + \alpha\beta$	$-\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+k^2)}$	$-\frac{2k^2}{(\alpha_0-4\beta_1)(1+k^2)^2}$	0	0	0	0
$\sigma_{1-}^{\#1} + \alpha$	0	0	0	$-\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+2k^2)}$	0	$-\frac{4ik}{(\alpha_0-4\beta_1)(1+2k^2)}$
$\sigma_{1-}^{\#2} + \alpha$	0	0	0	$-\frac{2}{(\alpha_0-4\beta_1)(1+2k^2)^2}$	0	$-\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+2k^2)^2}$
$\tau_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2} + \alpha$	0	0	0	0	0	$-\frac{4k^2}{(\alpha_0-4\beta_1)(1+2k^2)^2}$



Quadratic pole	
Pole residue:	$\frac{1}{\alpha_0} > 0$
Polarisations:	2



Massive particle	
Pole residue:	$-\frac{1}{\alpha_3} > 0$
Polarisations:	1
Square mass:	$-\frac{\alpha_0-4\beta_1}{2\alpha_3} > 0$
Spin:	0
Parity:	Odd

Unitarity conditions	
$\alpha_0 > 0$ && $\alpha_3 < 0$ && $\beta_1 < \frac{\alpha_0}{4}$	