

Frazin (Moore-Penrose) inverses of these a -matrices, which are functionally analogous to the inverse b -matrices described below Eq. (21) of arXiv:1812.02675:

Matrix for spin-0 sector:

$$\left(\begin{array}{cccccc} -\frac{36\,k^2}{a_{0}\left(16+3\,k^2\right)^2} & \frac{4\,\sqrt{3}}{16\,a_{0}+3\,a_{0}\,k^2} & \frac{2\,i\,\sqrt{6}\,k}{16\,a_{0}+3\,a_{0}\,k^2} & -\frac{72\,i\,k}{a_{0}\left(16+3\,k^2\right)^2} & \frac{8\,i\,k\left(19+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & -\frac{4\,i\,\sqrt{2}\,k\left(10+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & 0 \\ \frac{4\,\sqrt{3}}{16\,a_{0}+3\,a_{0}\,k^2} & \frac{4}{a_{0}\,k^2} & \frac{2\,i\,\sqrt{2}}{a_{0}\,k} & \frac{8\,i\,\sqrt{3}}{16\,a_{0}\,k+3\,a_{0}\,k^3} & -\frac{8\,i}{\sqrt{3}\left(16\,a_{0}\,k+3\,a_{0}\,k^3\right)} & -\frac{8\,i\,\sqrt{\frac{2}{3}}}{16\,a_{0}\,k+3\,a_{0}\,k^3} & 0 \\ -\frac{2\,i\,\sqrt{6}\,k}{16\,a_{0}+3\,a_{0}\,k^2} & -\frac{2\,i\,\sqrt{2}}{a_{0}\,k} & 0 & \frac{4\,\sqrt{6}}{16\,a_{0}+3\,a_{0}\,k^2} & -\frac{4\,\sqrt{\frac{2}{3}}}{16\,a_{0}+3\,a_{0}\,k^2} & -\frac{8}{\sqrt{3}\left(16\,a_{0}+3\,a_{0}\,k^2\right)} & 0 \\ \frac{72\,i\,k}{a_{0}\left(16+3\,k^2\right)^2} & -\frac{8\,i\,\sqrt{3}}{16\,a_{0}\,k+3\,a_{0}\,k^3} & \frac{4\,\sqrt{6}}{16\,a_{0}+3\,a_{0}\,k^2} & -\frac{144}{a_{0}\left(16+3\,k^2\right)^2} & \frac{16\left(19+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & -\frac{8\,\sqrt{2}\left(10+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & 0 \\ -\frac{8\,i\,k\left(19+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & \frac{8\,i}{\sqrt{3}\left(16\,a_{0}\,k+3\,a_{0}\,k^3\right)} & -\frac{4\,\sqrt{\frac{2}{3}}}{16\,a_{0}+3\,a_{0}\,k^2} & \frac{16\left(19+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & -\frac{16\left(35+6\,k^2\right)}{3\,a_{0}\left(16+3\,k^2\right)^2} & -\frac{8\,\sqrt{2}\left(22+3\,k^2\right)}{3\,a_{0}\left(16+3\,k^2\right)^2} & 0 \\ \frac{4\,i\,\sqrt{2}\,k\left(10+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & \frac{8\,i\,\sqrt{\frac{2}{3}}}{16\,a_{0}\,k+3\,a_{0}\,k^3} & -\frac{8}{\sqrt{3}\left(16\,a_{0}+3\,a_{0}\,k^2\right)} & -\frac{8\,\sqrt{2}\left(10+3\,k^2\right)}{a_{0}\left(16+3\,k^2\right)^2} & -\frac{8\,\sqrt{2}\left(22+3\,k^2\right)}{3\,a_{0}\left(16+3\,k^2\right)^2} & \frac{32\left(13+3\,k^2\right)}{3\,a_{0}\left(16+3\,k^2\right)^2} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\frac{2}{a_{0}}\end{array}\right)$$

Matrix for spin-1 sector:

$$\left(\begin{array}{cccccccccccc} 0 & -\frac{2\,\sqrt{2}}{a_{0}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{2\,\sqrt{2}}{a_{0}} & \frac{2}{a_{0}+2\,c_{8}\,k^2} & \frac{4\,\sqrt{2}\,c_{8}\,k^2}{a_{0}^2+2\,a_{0}\,c_{8}\,k^2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{4\,\sqrt{2}\,c_{8}\,k^2}{a_{0}^2+2\,a_{0}\,c_{8}\,k^2} & \frac{4}{a_{0}+2\,c_{8}\,k^2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{2\,k^2}{a_{0}\left(2+k^2\right)^2} & \frac{2\,i\,\sqrt{2}\,k}{2\,a_{0}+a_{0}\,k^2} & \frac{i\,k\left(4+k^2\right)}{a_{0}\left(2+k^2\right)^2} & -\frac{i\,\sqrt{\frac{2}{3}}\,k\left(4+3\,k^2\right)}{a_{0}\left(2+k^2\right)^2} & 0 & -\frac{i\,k\left(8+3\,k^2\right)}{\sqrt{3}\,a_{0}\left(2+k^2\right)^2} & 0 \\ 0 & 0 & 0 & -\frac{2\,i\,\sqrt{2}\,k}{2\,a_{0}+a_{0}\,k^2} & 0 & \frac{\sqrt{2}\left(4+k^2\right)}{a_{0}\left(2+k^2\right)} & -\frac{2\,k^2}{\sqrt{3}\left(2\,a_{0}+a_{0}\,k^2\right)} & 0 & \frac{\sqrt{\frac{2}{3}}\,k^2}{2\,a_{0}+a_{0}\,k^2} & 0 \\ 0 & 0 & 0 & -\frac{i\,k\left(4+k^2\right)}{a_{0}\left(2+k^2\right)^2} & \frac{\sqrt{2}\left(4+k^2\right)}{a_{0}\left(2+k^2\right)} & \frac{\left(4+k^2\right)^2}{2\,a_{0}\left(2+k^2\right)^2} & -\frac{8+8\,k^2+k^4}{\sqrt{6}\,a_{0}\left(2+k^2\right)^2} & -\frac{\sqrt{\frac{10}{3}}}{a_{0}} & \frac{-16-4\,k^2+k^4}{2\,\sqrt{3}\,a_{0}\left(2+k^2\right)^2} & -\frac{2\,\sqrt{\frac{2}{3}}}{a_{0}} \\ 0 & 0 & 0 & \frac{i\,\sqrt{\frac{2}{3}}\,k\left(4+3\,k^2\right)}{a_{0}\left(2+k^2\right)^2} & -\frac{2\,k^2}{\sqrt{3}\left(2\,a_{0}+a_{0}\,k^2\right)} & -\frac{8+8\,k^2+k^4}{\sqrt{6}\,a_{0}\left(2+k^2\right)^2} & \frac{1}{6}\left(\frac{1}{c_{8}\,k^2}+\frac{2\left(-16-8\,k^2+k^4\right)}{a_{0}\left(2+k^2\right)^2}\right) & \frac{\sqrt{5}\left(a_{0}+4\,c_{8}\,k^2\right)}{6\,a_{0}\,c_{8}\,k^2} & \frac{\frac{1}{c_{8}\,k^2}+\frac{-1-\frac{4}{\left(2+k^2\right)^2}}{a_{0}}}{3\,\sqrt{2}} & \frac{1}{3}\left(\frac{4}{a_{0}}+\frac{1}{c_{8}\,k^2}\right) \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{\frac{10}{3}}}{a_{0}} & \frac{\sqrt{5}\left(a_{0}+4\,c_{8}\,k^2\right)}{6\,a_{0}\,c_{8}\,k^2} & \frac{4}{3\,a_{0}}+\frac{5}{6\,c_{8}\,k^2} & \frac{\sqrt{\frac{5}{2}}\left(a_{0}-2\,c_{8}\,k^2\right)}{3\,a_{0}\,c_{8}\,k^2} & \frac{\sqrt{5}\left(a_{0}+4\,c_{8}\,k^2\right)}{3\,a_{0}\,c_{8}\,k^2} \\ 0 & 0 & 0 & \frac{i\,k\left(8+3\,k^2\right)}{\sqrt{3}\,a_{0}\left(2+k^2\right)^2} & \frac{\sqrt{\frac{2}{3}}\,k^2}{2\,a_{0}+a_{0}\,k^2} & \frac{-16-4\,k^2+k^4}{2\,\sqrt{3}\,a_{0}\left(2+k^2\right)^2} & \frac{\frac{1}{c_{8}\,k^2}+\frac{-1-\frac{4}{\left(2+k^2\right)^2}}{a_{0}}}{3\,\sqrt{2}} & \frac{\sqrt{\frac{5}{2}}\left(a_{0}-2\,c_{8}\,k^2\right)}{3\,a_{0}\,c_{8}\,k^2} & \frac{1}{6}\left(\frac{2}{c_{8}\,k^2}+\frac{32+16\,k^2+k^4}{a_{0}\left(2+k^2\right)^2}\right) & \frac{\sqrt{2}\left(a_{0}-2\,c_{8}\,k^2\right)}{3\,a_{0}\,c_{8}\,k^2} \\ 0 & 0 & 0 & 0 & 0 & -\frac{2\,\sqrt{\frac{2}{3}}}{a_{0}} & \frac{1}{3}\left(\frac{4}{a_{0}}+\frac{1}{c_{8}\,k^2}\right) & \frac{\sqrt{5}\left(a_{0}+4\,c_{8}\,k^2\right)}{3\,a_{0}\,c_{8}\,k^2} & \frac{\sqrt{2}\left(a_{0}-2\,c_{8}\,k^2\right)}{3\,a_{0}\,c_{8}\,k^2} & \frac{2}{3}\left(\frac{10}{a_{0}}+\frac{1}{c_{8}\,k^2}\right)\end{array}\right)$$

Matrix for spin-2 sector:

$$\left(\begin{array}{cccccc} -\frac{8}{a_{0}\,k^2} & -\frac{4\,i\,\sqrt{2}}{a_{0}\,k} & \frac{4\,i}{\sqrt{3}\,a_{0}\,k} & \frac{4\,i\,\sqrt{\frac{2}{3}}}{a_{0}\,k} & 0 & 0 \\ \frac{4\,i\,\sqrt{2}}{a_{0}\,k} & 0 & \frac{2\,\sqrt{\frac{2}{3}}}{a_{0}} & \frac{4}{\sqrt{3}\,a_{0}} & 0 & 0 \\ -\frac{4\,i}{\sqrt{3}\,a_{0}\,k} & \frac{2\,\sqrt{\frac{2}{3}}}{a_{0}} & -\frac{8}{3\,a_{0}} & -\frac{2\,\sqrt{2}}{3\,a_{0}} & 0 & 0 \\ -\frac{4\,i\,\sqrt{\frac{2}{3}}}{a_{0}\,k} & \frac{4}{\sqrt{3}\,a_{0}} & -\frac{2\,\sqrt{2}}{3\,a_{0}} & \frac{8}{3\,a_{0}} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{4}{a_{0}} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{4}{a_{0}}\end{array}\right)$$

Matrix for spin-3 sector:

$$\left(-\frac{2}{a_{0}}\right)$$