

# Particle spectrograph

## Wave operator and propagator

Quadratic (free) action

$$S_F = \int \int \int \left( \frac{1}{3} \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 3r_5 \partial_\lambda \omega^{\kappa\lambda} \partial_\lambda \omega^\alpha - 2r_1 \partial_\theta \omega^{\theta\alpha} \partial_\theta \omega_{\alpha\beta}^\kappa - 2r_1 \partial_\theta \omega_{\alpha\beta}^\kappa \partial_\kappa \omega^{\alpha\beta\theta} + 2r_1 \partial_\theta \omega_{\alpha\beta}^\kappa \partial_\kappa \omega^{\theta\alpha\beta} - 3r_5 \partial_\alpha \omega_\lambda^\alpha \partial_\theta \omega^{\kappa\lambda\theta} + 3r_5 \partial_\theta \omega_\lambda^\alpha \partial_\kappa \omega^{\theta\kappa\lambda} - 3r_5 \partial_\alpha \omega_\lambda^\alpha \partial_\kappa \omega^{\kappa\lambda\theta} + 6r_5 \partial_\theta \omega_\lambda^\alpha \partial_\kappa \omega^{\kappa\lambda\theta} + 2r_1 \partial_\kappa \omega^{\alpha\beta\theta} \partial^\kappa \omega_{\alpha\beta\theta} - 2r_1 \partial_\kappa \omega^{\theta\alpha\beta} \partial^\kappa \omega_{\alpha\beta\theta} + 2r_1 \partial_\theta \omega_{\alpha\beta}^\alpha \partial_\lambda \omega_{\alpha\beta}^\lambda - 8r_1 \partial_\theta \omega_{\alpha\beta}^\lambda \partial_\lambda \omega_{\alpha\beta}^\alpha + 3r_5 \partial_\alpha \omega_\lambda^\alpha \partial_\theta \omega^{\theta\kappa} - 3r_5 \partial_\theta \omega_\lambda^\alpha \partial_\alpha \omega^{\lambda\theta\kappa} \right) [t, x, y, z] dz dy dx dt$$

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\sigma_0^{#1} = 0$	1
$\sigma_0^{#1} = 0$	1
$\sigma_1^{#2\alpha} = 0$	3
$\sigma_1^{#2\alpha\beta} = 0$	3
$\sigma_2^{#1\alpha\beta} = 0$	5
Total constraints: 13	

	$\omega_{1+}^{#1}{}_{\alpha\beta}$	$\omega_{1+}^{#2}{}_{\alpha\beta}$	$\omega_{1-}^{#1}{}_{\alpha}$	$\omega_{1-}^{#2}{}_{\alpha}$
$\omega_{1+}^{#1}{}_{\dagger}{}^{\alpha\beta}$	$k^2 (2r_1 + r_5)$	0	0	0
$\omega_{1+}^{#2}{}_{\dagger}{}^{\alpha\beta}$	0	0	0	0
$\omega_{1-}^{#1}{}_{\dagger}{}^{\alpha}$	0	0	$k^2 (r_1 + r_5)$	0
$\omega_{1-}^{#2}{}_{\dagger}{}^{\alpha}$	0	0	0	0

$\omega_{2+}^{#1}{}_{\dagger}{}^{\alpha\beta}$	$\omega_{2-}^{#1}{}_{\dagger}{}^{\alpha\beta\chi}$
0	$k^2 r_1$
0	0

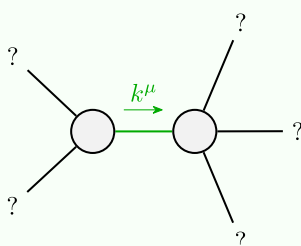
$\sigma_{0+}^{#1}{}_{\dagger}$	$\sigma_{0-}^{#1}{}_{\dagger}$
0	0
0	0

$\omega_{0+}^{#1}{}_{\dagger}$	$\omega_{0-}^{#1}{}_{\dagger}$
0	0
0	0

$\sigma_{2+}^{#1}{}_{\dagger}{}^{\alpha\beta}$	$\sigma_{2-}^{#1}{}_{\dagger}{}^{\alpha\beta\chi}$
0	0
0	$\frac{1}{k^2 r_1}$

	$\sigma_{1+}^{#1}{}_{\dagger}{}^{\alpha\beta}$	$\sigma_{1+}^{#2}{}_{\dagger}{}^{\alpha\beta}$	$\sigma_{1-}^{#1}{}_{\dagger}{}^{\alpha}$	$\sigma_{1-}^{#2}{}_{\dagger}{}^{\alpha}$
$\sigma_{1+}^{#1}{}_{\dagger}{}^{\alpha\beta}$	$\frac{1}{k^2 (2r_1 + r_5)}$	0	0	0
$\sigma_{1+}^{#2}{}_{\dagger}{}^{\alpha\beta}$	0	0	0	0
$\sigma_{1-}^{#1}{}_{\dagger}{}^{\alpha}$	0	0	$\frac{1}{k^2 (r_1 + r_5)}$	0
$\sigma_{1-}^{#2}{}_{\dagger}{}^{\alpha}$	0	0	0	0

## Massive and massless spectra



Quadratic pole

Pole residue:	$-\frac{1}{r_1 (r_1 + r_5) (2r_1 + r_5)} > 0$
Polarisations:	2

(No massive particles)

## Unitarity conditions

$$r_1 < 0 \&\& (r_5 < -r_1 \parallel r_5 > -2r_1) \parallel r_1 > 0 \&\& -2r_1 < r_5 < -r_1$$