



| | |
|----------------|---|
| Quadratic pole | |
| Pole residue: | $-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$ |
| Polarisations: | 2 |

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$

(No massive particles)

| $\sigma_{1+}^{\#1} \dagger \alpha\beta$ | $\sigma_{1+}^{\#2} \alpha\beta$ | $\tau_{1+}^{\#1} \alpha\beta$ | $\sigma_{1-}^{\#1} \alpha$ | $\sigma_{1-}^{\#2} \alpha$ | $\tau_{1-}^{\#1} \alpha$ | $\tau_{1-}^{\#2} \alpha$ |
|---|---------------------------------|-------------------------------|---|--|--------------------------|---|
| $\sigma_{1+}^{\#1} \dagger \alpha\beta$ | $\frac{1}{k^2(2r_3+r_5)}$ | 0 | 0 | 0 | 0 | 0 |
| $\sigma_{1+}^{\#2} \dagger \alpha\beta$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1+}^{\#1} \dagger \alpha\beta$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\sigma_{1-}^{\#1-} \dagger \alpha$ | 0 | 0 | $\frac{2}{k^2(r_3+2r_5)}$ | $\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$ | 0 | $\frac{4i}{k(1+2k^2)(r_3+2r_5)}$ |
| $\sigma_{1-}^{\#2-} \dagger \alpha$ | 0 | 0 | $\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$ | $\frac{3k^2(r_3+2r_5)+4t_3}{(k+2k^3)^2(r_3+2r_5)t_3}$ | 0 | $\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$ |
| $\tau_{1-}^{\#1-} \dagger \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1-}^{\#2-} \dagger \alpha$ | 0 | 0 | $-\frac{4i}{k(1+2k^2)(r_3+2r_5)}$ | $-\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$ | 0 | $\frac{6k^2(r_3+2r_5)+8t_3}{(1+2k^2)^2(r_3+2r_5)t_3}$ |

Lagrangian density

$$\begin{aligned} &\frac{2}{3}t_3\omega_{\lambda\alpha}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}+f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}-\frac{1}{2}r_3\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial'_{\lambda}\omega_{\alpha}^{\alpha}-r_5\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial'_{\kappa}\omega_{\lambda}^{\alpha}+\\ &\frac{2}{3}r_2\partial^{\beta}\omega^{\theta\alpha}_{\kappa}\partial_{\theta}\omega^{\kappa}_{\alpha\beta}-\frac{1}{3}r_2\partial_{\theta}\omega^{\kappa}_{\alpha\beta}\partial_{\kappa}\omega^{\alpha\beta\theta}-\frac{2}{3}r_2\partial_{\theta}\omega^{\kappa}_{\alpha\beta}\partial_{\kappa}\omega^{\theta\alpha\beta}+\\ &\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda\theta}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda\theta}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-\frac{1}{2}r_3\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+\\ &r_5\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda\theta}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-r_5\partial_{\alpha}\omega_{\lambda\theta}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+r_3\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+\\ &2r_5\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f'_{\lambda}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f'_{\lambda}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f'_{\lambda}+\\ &\frac{2}{3}t_3\partial_{\kappa}f^{\lambda}_{\lambda}\partial^{\kappa}f'_{\lambda}+\frac{2}{3}t_3\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f'_{\kappa}+\frac{2}{3}t_3\omega_{\lambda\alpha}^{\lambda}\partial^{\kappa}f'_{\kappa}+\frac{2}{3}t_3\partial^{\alpha}f^{\lambda}_{\alpha}\partial^{\kappa}f_{\lambda\kappa}+\\ &\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial_{\kappa}\omega^{\alpha\lambda\theta}+\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda\alpha}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}+\\ &r_5\partial_{\alpha}\omega_{\lambda\theta}^{\alpha}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa}+\frac{1}{2}r_3\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial^{\lambda}\omega^{\theta\kappa}_{\alpha}-r_5\partial_{\theta}\omega_{\lambda\alpha}^{\alpha}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa} \end{aligned}$$

| $\omega_{1+}^{\#1} \dagger \alpha\beta$ | $\omega_{1+}^{\#2} \alpha\beta$ | $f_{1+}^{\#1} \alpha\beta$ | $\omega_{1-}^{\#1} \alpha$ | $\omega_{1-}^{\#2} \alpha$ | $f_{1-}^{\#1} \alpha$ | $f_{1-}^{\#2} \alpha$ |
|---|---------------------------------|----------------------------|---|-----------------------------|-----------------------|--------------------------------------|
| $\omega_{1+}^{\#1} \dagger \alpha\beta$ | $k^2(2r_3+r_5)$ | 0 | 0 | 0 | 0 | 0 |
| $\omega_{1+}^{\#2} \dagger \alpha\beta$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1+}^{\#1} \dagger \alpha\beta$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\omega_{1-}^{\#1-} \dagger \alpha$ | 0 | 0 | $k^2(\frac{r_3}{2}+r_5)+\frac{2t_3}{3}$ | $-\frac{\sqrt{2}t_3}{3}$ | 0 | $-\frac{2}{3}i\frac{kt_3}{3}$ |
| $\omega_{1-}^{\#2-} \dagger \alpha$ | 0 | 0 | $-\frac{\sqrt{2}t_3}{3}$ | $\frac{t_3}{3}$ | 0 | $\frac{1}{3}i\frac{\sqrt{2}kt_3}{3}$ |
| $f_{1-}^{\#1-} \dagger \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{\#2-} \dagger \alpha$ | 0 | 0 | $\frac{2ikt_3}{3}$ | $-\frac{1}{3}i\sqrt{2}kt_3$ | 0 | $\frac{2k^2t_3}{3}$ |

| Source constraints | |
|---|----|
| SO(3) irreps | # |
| $\tau_{0+}^{\#2} == 0$ | 1 |
| $\tau_{0+}^{\#1} - 2ik\sigma_{0+}^{\#1} == 0$ | 1 |
| $\tau_{1-}^{\#2\alpha} + 2ik\sigma_{1-}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1-}^{\#1\alpha} == 0$ | 3 |
| $\tau_{1+}^{\#1\alpha\beta} == 0$ | 3 |
| $\sigma_{1+}^{\#2\alpha\beta} == 0$ | 3 |
| $\sigma_{2-}^{\#1\alpha\beta\chi} == 0$ | 5 |
| $\tau_{2+}^{\#1\alpha\beta} == 0$ | 5 |
| Total #: | 24 |

| $\sigma_{2+}^{\#1} \dagger \alpha\beta$ | $\tau_{2+}^{\#1} \alpha\beta$ | $\sigma_{2-}^{\#1} \alpha\beta\chi$ |
|---|-------------------------------|-------------------------------------|
| $\sigma_{2+}^{\#1} \dagger \alpha\beta$ | $-\frac{2}{3k^2r_3}$ | 0 |
| $\tau_{2+}^{\#1} \dagger \alpha\beta$ | 0 | 0 |
| $\sigma_{2-}^{\#1} \dagger \alpha\beta\chi$ | 0 | 0 |

| $\sigma_{0+}^{\#1} \dagger$ | $\tau_{0+}^{\#1} \dagger$ | $\tau_{0+}^{\#2} \dagger$ | $\sigma_{0-}^{\#1} \dagger$ |
|-----------------------------|------------------------------------|-------------------------------------|-----------------------------|
| $\sigma_{0+}^{\#1} \dagger$ | $\frac{1}{(1+2k^2)^2t_3}$ | $-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$ | 0 |
| $\tau_{0+}^{\#1} \dagger$ | $\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$ | $\frac{2k^2}{(1+2k^2)^2t_3}$ | 0 |
| $\tau_{0+}^{\#2} \dagger$ | 0 | 0 | 0 |
| $\sigma_{0-}^{\#1} \dagger$ | 0 | 0 | $\frac{1}{k^2r_2}$ |

| $\omega_{2+}^{\#1} \dagger \alpha\beta$ | $f_{2+}^{\#1} \alpha\beta$ | $\omega_{2-}^{\#1} \alpha\beta\chi$ |
|---|----------------------------|-------------------------------------|
| $\omega_{2+}^{\#1} \dagger \alpha\beta$ | $-\frac{3k^2r_3}{2}$ | 0 |
| $f_{2+}^{\#1} \dagger \alpha\beta$ | 0 | 0 |
| $\omega_{2-}^{\#1} \dagger \alpha\beta\chi$ | 0 | 0 |

| $\omega_{0+}^{\#1}$ | $f_{0+}^{\#1}$ | $f_{0+}^{\#2}$ | $\omega_{0-}^{\#1}$ |
|-----------------------------|-----------------|------------------|---------------------|
| $\omega_{0+}^{\#1} \dagger$ | t_3 | $-i\sqrt{2}kt_3$ | 0 |
| $f_{0+}^{\#1} \dagger$ | $i\sqrt{2}kt_3$ | $2k^2t_3$ | 0 |
| $f_{0+}^{\#2} \dagger$ | 0 | 0 | 0 |
| $\omega_{0-}^{\#1} \dagger$ | 0 | 0 | k^2r_2 |