| α | | | | | | | | | | |
|--|--|-------------------------------------|---------------------------------|-------------------------------------|--------------------------------------|--------------------------------------|------------------------------------|------------------------------------|-------------------------------|------------------------------------|
| ${\mathcal T}_{1^{	ext{-}}}^{\#1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1^{-}\alpha}^{\#6}$ | 0 | 0 | 0 | 0 | 0 | $-\frac{1}{6a_0}$ | $-\frac{\sqrt{5}}{6a_0}$ | $-\frac{7}{3\sqrt{2}a_0}$ | 3 a 0 | 0 |
| $\Delta_{1^{^{-}}\alpha}^{\#5}$ | 0 | 0 | 0 | 0 | 0 | $-\frac{1}{6\sqrt{2}}a_0$ | $-\frac{\sqrt{\frac{5}{2}}}{6a_0}$ | $\frac{17}{6a_0}$ | $-\frac{7}{3\sqrt{2}}a_0$ | 0 |
| $\Delta_{1^{^{-}}\alpha}^{\#4}$ | 0 | 0 | 0 | 0 | 0 | $\frac{5\sqrt{5}}{12a_0}$ | $\frac{1}{12a_0}$ | $-\frac{\sqrt{\frac{5}{2}}}{6a_0}$ | $-\frac{\sqrt{5}}{6a_0}$ | 0 |
| $\Delta_{1^{^{-}}\alpha}^{\#3}$ | 0 | 0 | 0 | 0 | 0 | $-\frac{19}{12 a_0}$ | $\frac{5\sqrt{5}}{12a_0}$ | $-\frac{1}{6\sqrt{2}a_0}$ | $-\frac{1}{6a_0}$ | 0 |
| $\Delta_{1}^{\#2}{}_{\alpha}$ | 0 | 0 | 0 | $\frac{2\sqrt{2}}{a_0}$ | $\frac{2}{a_0}$ | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1^{\text{-}}}^{\#1}{}_{\alpha}$ | 0 | 0 | 0 | 0 | $\frac{2\sqrt{2}}{a_0}$ | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1}^{\#1}_{\alpha\beta} \; \Delta_{1}^{\#2}_{+\alpha\beta} \; \Delta_{1}^{\#3}_{+\alpha\beta}$ | 0 | 0 | $\frac{4}{a_0}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1}^{\#2}{}_{+}\alpha\beta$ | $-\frac{2\sqrt{2}}{a_0}$ | 2 40 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1}^{\#1}{}_{+}\alpha\beta$ | 0 | $\frac{2\sqrt{2}}{a_0}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| · | $\Delta_{1}^{\#1} \dagger^{\alpha\beta}$ | $\Delta_{1}^{\#2} + \alpha^{\beta}$ | $\Delta_{1}^{\#3} + ^{lphaeta}$ | $\Delta_{1}^{\#1} \dagger^{\alpha}$ | $\Delta_{1}^{\#2} \uparrow^{\alpha}$ | $\Delta_{1}^{\#3} \dagger^{\alpha}$ | $\Delta_{1}^{\#4} +^{lpha}$ | $\Delta_{1}^{\#5} +^{\alpha}$ | $\Delta_{1}^{\#6} +^{\alpha}$ | $\mathcal{T}_{1}^{\#1} +^{\alpha}$ |

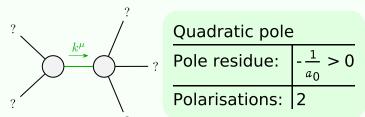
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | α | | | | | | | | | | |
|---|------------------------------|----------------------------------|--------------------------------|-----------------------------------|-----------------------------|-----------------------------|-------------------------------|---------------------------------|-------------------------------|-------------------------------|-------------------------|
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $h_{1^-}^{\#1}$ | 0 | 0 | 0 | 0 | 0 | 0 | | 0 | 0 | 0 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1^{-}\alpha}^{\#6}$ | 0 | 0 | 0 | 0 | 0 | 9 0 0 | ı | $\frac{a_0}{6\sqrt{2}}$ | $\frac{5a_0}{12}$ | 0 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1}^{\#5}$ | 0 | 0 | 0 | 0 | 0 | $\frac{a_0}{6\sqrt{2}}$ | $\frac{1}{6}\sqrt{\frac{5}{2}}$ | | $\frac{a_0}{6\sqrt{2}}$ | 0 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1^{-}}^{\#4}$ | 0 | 0 | 0 | 0 | 0 | $\frac{\sqrt{5} a_0}{6}$ | $\frac{a_0}{3}$ | $\sqrt{\frac{5}{2}}$ | $-\frac{\sqrt{5} a_0}{6}$ | 0 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1}^{\#3}$ | 0 | 0 | 0 | 0 | 0 | $-\frac{a_0}{3}$ | $\frac{\sqrt{5} \ a_0}{6}$ | $-\frac{a_0}{6\sqrt{2}}$ | $\frac{9}{0v}$ | 0 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1^{-}\alpha}^{#2}$ | 0 | 0 | 0 | $\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1^-}^{\#1}$ | 0 | 0 | 0 | $-\frac{a_0}{4}$ | $\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1}^{#3}$ | 0 | 0 | <u>a</u> 0 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $+\alpha$ $+\alpha$ $+\alpha$ $+\alpha$ $+\alpha$ $+\alpha$ $+\alpha$ $+\alpha$ | $\Gamma_{1}^{#2}$ | $-\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | $\Gamma_{1}^{\#1}$ | • | 1 | | | | | | | | |
| | | $\Gamma_1^{\#_1} + \alpha \beta$ | $\Gamma_1^{#2} + \alpha \beta$ | $\Gamma_1^{\#3} + ^{\alpha\beta}$ | $\Gamma_1^{\#1} +^{\alpha}$ | $\Gamma_1^{\#2} +^{\alpha}$ | $\Gamma_{1}^{\#3} +^{\alpha}$ | $\Gamma_1^{\#4} + ^{\alpha}$ | $\Gamma_{1}^{#5} + ^{\alpha}$ | $\Gamma_{1}^{\#6} +^{\alpha}$ | $h_{1}^{#1} +^{\alpha}$ |

| | $-\chi g \chi$ | 10 h ^X (| $a_0 \partial_{\beta} h'$ | , hab d | | | | $\Delta_{3}^{\#1}$ | | # 1.1 | <u>უ</u> | |
|--------------------|---|--|---|---|---|---|-------------------------------|----------------------|---------------------------|---------------------------|---------------------------|-----------------------------------|
| | $\alpha eta \chi \nabla^{c}$ | , X - 1 | h^{χ}_{χ} - $\frac{1}{8}$ | h_{β}^{χ} -a | $- \frac{\beta}{\beta} \mu_{\beta} -$ | $\Gamma^{\alpha}_{\alpha}^{\beta}$ | $\Delta_{0^{\text{-}}}^{\#1}$ | 0 | 0 | 0 | 0 | 0 |
| | _ + Ε | $^{8}_{\alpha}$ 0 | 3 $\partial_{eta}\partial_{lpha}$ | $^{1a}_{\alpha}\partial_{\chi}$ | $^{1a}_{\alpha}\partial_{\chi}$ | $^{\prime}^{eta_{\chi}}$ | $\mathcal{T}_{0}^{\#2}$ | 0 | 0 | 0 | 0 | 0 |
| | $^{lphaeta} {\cal T}_{_{\cal C}}$ | α ₀ Γα | a0 h ^α ! | $a_0 \partial^{\beta}$ | $\frac{1}{4}a_0$ | $\frac{1}{2}a_0h$ | $\mathcal{T}_{0}^{\#1}$ | 0 | 0 | 0 | 0 | $\frac{4}{a_0 k^2}$ |
| | $\Gamma^{X}_{\beta X} + h^{'}$ | $\beta h^{\chi}_{\chi} + \frac{1}{4}$ | $\Gamma^{\alpha\beta\chi} + \frac{1}{2}$ | $_{\chi}h_{\beta}^{\ \ \chi} + \frac{1}{2}$ | $\partial_{\chi}\partial^{\chi}h_{\alpha\beta}$ - | $+ g_{\alpha} \nu_{\alpha\beta} +$ | $\Delta_{0}^{\#4}$ | 0 | $-\frac{1}{2\sqrt{2}a_0}$ | $-\frac{1}{2\sqrt{2}a_0}$ | $\frac{1}{2a_0}$ | 0 |
| ý | $a_0 \Gamma^{\alpha \beta}_{\alpha}$ | $\iota_0 \mathrel{\Gamma^{lpha}}^{eta} \vartheta$ | $\iota_0 \; h_{\alpha\chi} \; \partial_{\beta}$ | ιο θαμ ^{αβ} ε | $\frac{1}{2}a_0h^{\alpha\beta}$ | $a_0 \partial_{\chi} h_{\alpha\beta}$ | $\Delta_{0}^{\#3}$ | 0 | 4 a 0 | $-\frac{3}{4 a_0}$ | $-\frac{1}{2\sqrt{2}a_0}$ | 0 |
| Lagrangian density | $-\frac{1}{2} a_0 \Gamma^{\alpha\beta\chi} \Gamma_{\beta\chi\alpha} + \frac{1}{2} a_0 \Gamma^{\alpha}_{\alpha}^{\beta} \Gamma^{\chi}_{\beta\chi} + h^{\alpha\beta} \mathcal{T}_{\alpha\beta} + \Gamma^{\alpha\beta\chi} \Delta_{\alpha\beta\chi} -$ | $\frac{1}{2} a_0 \Gamma^{\alpha\beta\chi} \partial_\beta h_{\alpha\chi} - \frac{1}{4} a_0 \Gamma^\alpha_{\ \alpha} \partial_\beta h_{\chi}^{\chi} + \frac{1}{4} a_0 \Gamma^{\alpha\beta}_{\ \alpha} \partial_\beta h_{\chi}^{\chi} - \frac{1}{4} a_0 h_{\chi}^{\chi} \partial_\beta h_{\chi}^{\chi} + \frac{1}{4} \partial_\gamma h_{\chi}^{\chi} \partial_\gamma h_{\chi}^$ | $\frac{1}{4} a_0 \ h_X^X \ \partial_\beta \Gamma^{\alpha\beta}_{\ \alpha} - \frac{1}{2} a_0 \ h_{\alpha\chi} \ \partial_\beta \Gamma^{\alpha\beta\chi} + \frac{1}{2} a_0 \ h^{\alpha\beta} \ \partial_\beta \partial_\alpha h^\chi_{\ X} - \frac{1}{8} a_0 \ \partial_\beta h^\chi_{\ X} + 1$ | $\frac{1}{2} a_0 \Gamma^{\alpha}_{\alpha}{}^{\beta} \partial_{\chi} h_{\beta}^{\ X} - \frac{1}{2} a_0 \partial_{\alpha} h^{\alpha\beta} \partial_{\chi} h_{\beta}^{\ X} + \frac{1}{2} a_0 \partial^{\beta} h_{\alpha}^{\alpha} \partial_{\chi} h_{\beta}^{\ X} - a_0 h^{\alpha\beta} \partial_{\beta} \partial_{\beta}^{\alpha} \partial_{\gamma} h_{\beta}^{\ X} + a_0 \partial_{\gamma} h_{\beta}^{\alpha} \partial_{\gamma} h_{\beta}^{\ X} + a_0 \partial_{\gamma} h_{\beta}^{\alpha} \partial_{\gamma} h_{\beta}^{\alpha} \partial_{\gamma} h_{\beta}^{\alpha} + a_0 \partial_{\gamma} h_{\beta}^{\alpha} \partial_{\gamma} h_{\gamma}^{\alpha} \partial_{\gamma} h_{\gamma}^{\alpha$ | $\frac{1}{4} a_0 h^{\alpha}_{\alpha} \partial_{\chi} \partial_{\beta} h^{\beta \chi} + \frac{1}{2} a_0 h^{\alpha \beta} \partial_{\chi} \partial^{\chi} h_{\alpha \beta} - \frac{1}{4} a_0 h^{\alpha}_{\alpha} \partial_{\chi} \partial^{\chi} h^{\beta}_{\beta}$ | $\frac{1}{4} a_0 \partial_{\beta} h_{\alpha\chi} \partial^{\chi} h^{\alpha\beta} + \frac{3}{8} a_0 \partial_{\chi} h_{\alpha\beta} \partial^{\chi} h^{\alpha\beta} + \frac{1}{2} a_0 h_{\beta\chi} \partial^{\chi} \Gamma^{\alpha}_{\alpha} \beta$ | $\Delta_{0}^{\#2}$ | 0 | $-\frac{3}{4 a_0}$ | $\frac{5}{4 a_0}$ | $-\frac{1}{2\sqrt{2}}a_0$ | 0 |
| ıngia | $L_{\alpha \beta \chi}$ | -αβχ ; | A_{χ}^{χ} | $-\alpha \beta \beta$ | $\lambda^{\alpha}_{\alpha} \partial_{\dot{\beta}}$ | $\beta h_{\alpha X}$ | $\Delta_0^{\#1}$ | $-\frac{2}{a_0}$ | 0 | 0 | 0 | 0 |
| Lagra | $-\frac{1}{2}a_0$ | $\frac{1}{2}a_0$ | $\frac{1}{4} a_0 /$ | $\frac{1}{2} a_0 I$ | $\frac{1}{4} a_0 /$ | $\frac{1}{4} a_0 \hat{o}$ | | $\Delta_{0}^{\#1}$ † | $\Delta_{0}^{#2} +$ | $\Delta_{0}^{#3}$ † | $\Delta_{0}^{#4}$ † | $\mathcal{T}_{0}^{\#1}$ \dagger |
| | | | | | | | | | | | | |

| | | | | | | | | | | | | _ |
|------------------------------|--------------------------|--------------------------|---------------------------------|---|---------------|-----------------------------|---------------------------------------|--|-----------------------------------|-------------------------------------|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | $-\frac{2}{a_0}$ | $\Delta_{2}^{\#2}$ $\alpha eta \chi$ | 0 | 0 | 0 | 0 | |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\alpha eta_{\chi} \Delta$ | | | | | |
| 0 | 0 | 0 | 0 | $\frac{4}{a_0 k^2}$ | 0 | 0 | $\Delta_{2^{^{-}}}^{\#1}$ | 0 | 0 | 0 | 0 | |
| 0 | $\frac{1}{2\sqrt{2}a_0}$ | $\frac{1}{2\sqrt{2}a_0}$ | $\frac{1}{2a_0}$ | 0 | 0 | 0 | $\mathcal{T}_{2}^{\#1}_{\alpha\beta}$ | 0 | 0 | 0 | $-\frac{8}{a_0 k^2}$ | |
| 0 | 5 4 <i>a</i> 0 | 3 4 a 0 | $\frac{1}{\sqrt{2}}a_0$ | 0 | 0 | 0 | $\Delta_2^{#3}$ | 0 | 0 | 4 <u>4</u> a ₀ | 0 | |
| | | ı | $\frac{a_0}{a_0} = \frac{1}{2}$ | | | | $\Delta_2^{\#_2^2}\alpha\beta$ | 0 | $-\frac{2}{a_0}$ | 0 | 0 | |
| 0 | - 3 4 a 0 | 4 a 0 | $-\frac{1}{2\sqrt{2}}$ | 0 | 0 | 0 | $\Delta_2^{\#1}_+$, | 4 a ₀ | 0 | 0 | 0 | |
| $-\frac{2}{a_0}$ | 0 | 0 | 0 | 0 | 0 | 0 | ۵ | βλ | βι | βι | βι | |
| $\Delta_{0}^{\#1}$ \dagger | $\Delta_{0}^{#2} +$ | $\Delta_{0}^{#3}$ † | $\Delta_{0}^{#4}$ † | $rac{7}{0} + \frac{1}{1} + \frac{1}{1}$ | $T_0^{\#2} +$ | $\Delta_{0}^{\#1} \uparrow$ | | $\Delta_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\Delta_2^{\#2} + \alpha^{\beta}$ | $\Delta_{2}^{\#3} + ^{\alpha\beta}$ | $\mathcal{T}_{2}^{\#1} \dagger^{\alpha\beta}$ | |
| | | | | | | | | | | | | |

| Source constraints | |
|--|---|
| SO(3) irreps | # |
| $\mathcal{T}_{0^{+}}^{#2} == 0$ | 1 |
| $\Delta_{0^{+}}^{\#3} + 2\Delta_{0^{+}}^{\#4} + 3\Delta_{0^{+}}^{\#2} == 0$ | 1 |
| $\mathcal{T}_{1}^{\#1\alpha} == 0$ | 3 |
| $2 \Delta_{1}^{\#6\alpha} + \Delta_{1}^{\#4\alpha} + 2 \Delta_{1}^{\#5\alpha} + \Delta_{1}^{\#3\alpha} == 0$ | 3 |
| Total #: | 8 |

| | $\Gamma_0^{\#1}$ | Γ ₀ ^{#2} | Γ ₀ ^{#3} | $\Gamma_0^{\#4}$ | $h_{0}^{\#1}$ | $h_0^{\#2}$ | Γ ₀ -1 |
|--------------------------------|-------------------|------------------------------|------------------------------|---------------------------|---------------------|-------------|-------------------|
| $\Gamma_{0}^{\#1}$ † | - <u>a_0</u> 2 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Gamma_{0}^{\#2}$ † | 0 | 0 | <u>a₀</u> 2 | $-\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 |
| Γ ₀ ^{#3} † | 0 | <u>a₀</u> 2 | 0 | $-\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 |
| Γ ₀ ^{#4} † | 0 | $-\frac{a_0}{2\sqrt{2}}$ | $-\frac{a_0}{2\sqrt{2}}$ | <u>a₀</u> 2 | 0 | 0 | 0 |
| $h_{0}^{#1}$ † | 0 | 0 | 0 | 0 | $\frac{a_0 k^2}{4}$ | 0 | 0 |
| $h_0^{\#2}$ † | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Gamma_0^{\#1}$ † | 0 | 0 | 0 | 0 | 0 | 0 | $-\frac{a_0}{2}$ |
| | | | | | | | |



(No massive particles)