

Massive particle	
Pole residue:	$\frac{6t_1t_3(t_1+t_3)-3r_5(t_1^2+2t_3^2)}{2r_5(t_1+t_3)-(3t_1t_3+r_5(t_1+t_3))} > 0$
Polarisations:	3
Square mass:	$-\frac{3t_1t_3}{2r_5t_1+2r_5t_3} > 0$
Spin:	1
Parity:	Odd

Unitarity conditions

$r_2 < 0 \&\& r_5 < 0 \&\& t_1 < 0 \&\& 0 < t_3 < -t_1$

(No massless particles)

Lagrangian density

$$\begin{aligned}
 &-\frac{1}{3}t_1\omega_{\kappa}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_3\omega_{\kappa}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa}^{\lambda'}-r_5\partial_{\lambda'}\omega_{\kappa}^{\kappa\lambda}\partial^{\lambda}\omega_{\lambda}^{\alpha}+ \\
 &\frac{2}{3}r_2\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}-\frac{2}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}- \\
 &r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}+ \\
 &2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\omega^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}\partial^{\kappa}f_{\alpha}^{\theta}- \\
 &\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\alpha\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\lambda}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}- \\
 &\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\lambda}^{\lambda}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\lambda}^{\lambda}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}+ \\
 &\frac{2}{3}t_3\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}+2t_1\omega_{\lambda\kappa\theta}\partial^{\kappa}f_{\lambda}^{\theta}-\frac{1}{3}t_1\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{2}{3}t_3\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\lambda}- \\
 &\frac{1}{3}t_1\omega_{\lambda\alpha}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{2}{3}t_3\omega_{\lambda\alpha}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\lambda}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+ \\
 &\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}-\frac{1}{3}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda\kappa}^{\lambda}+\frac{2}{3}t_3\partial^{\alpha}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda\kappa}^{\lambda}+ \\
 &\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}+ \\
 &\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}+r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}
 \end{aligned}$$

Added source term:

$f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

Source constraints	
SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1}-2\,i\,k\,\sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha}+2\,i\,k\,\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta}+i\,k\,\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta}-2\,i\,k\,\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	16

$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\frac{1}{(1+2\,k^2)^2\,t_3}$	$-\frac{i\,\sqrt{2}\,k}{(1+2\,k^2)^2\,t_3}$	0	0
$\frac{i\,\sqrt{2}\,k}{(1+2\,k^2)^2\,t_3}$	$\frac{2\,k^2}{(1+2\,k^2)^2\,t_3}$	0	0
0	0	0	0
0	0	0	$\frac{1}{k^2\,r_2-t_1}$

$\sigma_{2+}^{\#1}$	$\tau_{2+}^{\#1}$	$\sigma_{2-}^{\#1}$	$\alpha\beta\chi$
$\frac{2}{(1+2\,k^2)^2\,t_1}$	$-\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2\,t_1}$	0	0
$\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2\,t_1}$	$\frac{4\,k^2}{(1+2\,k^2)^2\,t_1}$	0	0
0	0	0	$\frac{2}{t_1}$

$\omega_{2+}^{\#1}$	$f_{2+}^{\#1}$	$\omega_{2-}^{\#1}$	$\alpha\beta\chi$
$\omega_{2+}^{\#1}\dagger^{\alpha\beta}$	$\frac{t_1}{2}$	$-\frac{i\,k\,t_1}{\sqrt{2}}$	0
$f_{2+}^{\#1}\dagger^{\alpha\beta}$	$\frac{i\,k\,t_1}{\sqrt{2}}$	$k^2\,t_1$	0
$\omega_{2-}^{\#1}\dagger^{\alpha\beta\chi}$	0	0	$\frac{t_1}{2}$

$\sigma_{1+}^{\#1}$	$\sigma_{1+}^{\#2}$	$\tau_{1+}^{\#1}$	$\sigma_{1-}^{\#1}$	$\sigma_{1-}^{\#2}$	$\tau_{1-}^{\#1}$	$\tau_{1-}^{\#2}$
$\sigma_{1+}^{\#1}\dagger^{\alpha\beta}$	0	$-\frac{\sqrt{2}}{t_1+k^2\,t_1}$	0	0	0	0
$\sigma_{1+}^{\#2}\dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{t_1+k^2\,t_1}$	$-\frac{2\,k^2\,r_5+t_1}{(1+k^2)^2\,t_1^2}$	0	0	0	0
$\tau_{1+}^{\#1}\dagger^{\alpha\beta}$	$\frac{i\,\sqrt{2}\,k}{t_1+k^2\,t_1}$	$\frac{i\,(2\,k^3\,r_5-k\,t_1)}{(1+k^2)^2\,t_1^2}$	0	0	0	0
$\sigma_{1-}^{\#1}\dagger^{\alpha}$	0	0	$\frac{2\,(t_1+t_3)}{3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3)}$	$-\frac{\sqrt{2}\,(t_1-2\,t_3)}{(1+2\,k^2)\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$	$-\frac{2\,i\,k\,(t_1-2\,t_3)}{(1+2\,k^2)\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$	$-\frac{2\,i\,k\,(6\,k^2\,r_5+t_1+4\,t_3)}{(1+2\,k^2)^2\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$
$\sigma_{1-}^{\#2}\dagger^{\alpha}$	0	0	$-\frac{\sqrt{2}\,(t_1-2\,t_3)}{(1+2\,k^2)\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$	$\frac{6\,k^2\,r_5+t_1+4\,t_3}{(1+2\,k^2)^2\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$	0	$\frac{i\,\sqrt{2}\,k\,(6\,k^2\,r_5+t_1+4\,t_3)}{(1+2\,k^2)^2\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$
$\tau_{1-}^{\#1}\dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#2}\dagger^{\alpha}$	0	0	$\frac{2\,i\,k\,(t_1-2\,t_3)}{(1+2\,k^2)\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$	$-\frac{i\,\sqrt{2}\,k\,(6\,k^2\,r_5+t_1+4\,t_3)}{(1+2\,k^2)^2\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$	0	$\frac{2\,k^2\,(6\,k^2\,r_5+t_1+4\,t_3)}{(1+2\,k^2)^2\,(3\,t_1\,t_3+2\,k^2\,r_5\,(t_1+t_3))}$

$\omega_{1+}^{\#1}$	$\omega_{1+}^{\#2}$	$f_{1+}^{\#1}$	$\omega_{1-}^{\#1}$	$\omega_{1-}^{\#2}$	$f_{1-}^{\#1}$	$f_{1-}^{\#2}$
$\omega_{1+}^{\#1}\dagger^{\alpha\beta}$	$k^2\,r_5-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{i\,k\,t_1}{\sqrt{2}}$	0	0	0
$\omega_{1+}^{\#2}\dagger^{\alpha\beta}$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$f_{1+}^{\#1}\dagger^{\alpha\beta}$	$\frac{i\,k\,t_1}{\sqrt{2}}$	0	0	0	0	0
$\omega_{1-}^{\#1}\dagger^{\alpha}$	0	0	0	$\frac{1}{6}\,(6\,k^2\,r_5+t_1+4\,t_3)$	$\frac{t_1-2\,t_3}{3\,\sqrt{2}}$	0
$\omega_{1-}^{\#2}\dagger^{\alpha}$	0	0	0	$\frac{t_1-2\,t_3}{3\,\sqrt{2}}$	$\frac{t_1+t_3}{3}$	0
$f_{1-}^{\#1}\dagger^{\alpha}$	0	0	0	0	0	$\frac{1}{3}\,i\,k\,(t_1-2\,t_3)$
$f_{1-}^{\#2}\dagger^{\alpha}$	0	0	0	$-\frac{1}{3}\,i\,k\,(t_1-2\,t_3)$	$-\frac{1}{3}\,i\,\sqrt{2}\,k\,(t_1+t_3)$	0
						$\frac{2}{3}\,k^2\,(t_1+t_3)$

$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1}\dagger$	$t_3$	$-i\,\sqrt{2}\,k\,t_3$	0
$f_{0+}^{\#1}\dagger$	$i\,\sqrt{2}\,k\,t_3$	$2\,k^2\,t_3$	0
$f_{0+}^{\#2}\dagger$	0	0	0
$\omega_{0-}^{\#1}\dagger$	0	0	$k^2\,r_2-t_1$