

## Wave operator and propagator

	$\Delta_{0+}^{\#1}$	$\Delta_{0+}^{\#2}$	$\Delta_{0+}^{\#3}$	$\Delta_{0+}^{\#4}$	$\mathcal{T}_{0+}^{\#1}$	$\mathcal{T}_{0+}^{\#2}$	$\Delta_{0+}^{\#1}$
$\Delta_{0+}^{\#1}$	$\frac{2(a_0+25a_1k^2)}{a_0^2}$	$\frac{10\sqrt{6}a_1k^2}{a_0^2}$	$-\frac{10\sqrt{\frac{2}{3}}a_1k^2}{a_0^2}$	$-\frac{20a_1k^2}{\sqrt{3}a_0^2}$	$-\frac{50i\sqrt{2}a_1k}{a_0^2}$	0	0
$\Delta_{0+}^{\#2}$	$\frac{10\sqrt{6}a_1k^2}{a_0^2}$	$\frac{3(a_0+23a_1k^2)}{4a_0^2}$	$\frac{5a_0+23a_1k^2}{4a_0^2}$	$\frac{a_0-23a_1k^2}{2\sqrt{2}a_0^2}$	$\frac{20i\sqrt{3}a_1k}{a_0^2}$	0	0
$\Delta_{0+}^{\#3}$	$-\frac{10\sqrt{\frac{2}{3}}a_1k^2}{a_0^2}$	$\frac{5a_0+23a_1k^2}{4a_0^2}$	$-\frac{9a_0+23a_1k^2}{12a_0^2}$	$\frac{-3a_0+23a_1k^2}{6\sqrt{2}a_0^2}$	$-\frac{20a_1k}{\sqrt{3}a_0^2}$	0	0
$\Delta_{0+}^{\#4}$	$-\frac{20a_1k^2}{\sqrt{3}a_0^2}$	$-\frac{a_0-23a_1k^2}{2\sqrt{2}a_0^2}$	$-\frac{3a_0+23a_1k^2}{6\sqrt{2}a_0^2}$	$\frac{3a_0-23a_1k^2}{6a_0^2}$	$-\frac{20i\sqrt{\frac{2}{3}}a_1k}{a_0^2}$	0	0
$\mathcal{T}_{0+}^{\#1}$	$\frac{50i\sqrt{2}a_1k}{a_0^2}$	$-\frac{20i\sqrt{3}a_1k}{a_0^2}$	$\frac{20ia_1k}{\sqrt{3}a_0^2}$	$\frac{20i\sqrt{\frac{2}{3}}a_1k}{a_0^2}$	$\frac{4(a_0-25a_1k^2)}{a_0^2k^2}$	0	0
$\mathcal{T}_{0+}^{\#2}$	0	0	0	0	0	0	0
$\Delta_{0+}^{\#1}$	0	0	0	0	0	0	$-\frac{2}{a_0+a_1k^2}$

	$\Delta_{2+\alpha\beta}^{\#1}$	$\Delta_{2+\alpha\beta}^{\#2}$	$\Delta_{2+\alpha\beta}^{\#3}$	$\mathcal{T}_{2+\alpha\beta}^{\#1}$	$\Delta_{2+\alpha\beta\chi}^{\#1}$	$\Delta_{2+\alpha\beta\chi}^{\#2}$
$\Delta_{2+}^{\#1} + \alpha\beta$	$\frac{4(a_0-11a_1k^2)}{a_0^2}$	$-\frac{40\sqrt{\frac{2}{3}}a_1k^2}{a_0^2}$	$-\frac{80a_1k^2}{\sqrt{3}a_0^2}$	$-\frac{44i\sqrt{2}a_1k}{a_0^2}$	0	0
$\Delta_{2+}^{\#2} + \alpha\beta$	$-\frac{40\sqrt{\frac{2}{3}}a_1k^2}{a_0^2}$	$\frac{2(3a_0+a_1k^2)}{3a_0^2}$	$-\frac{2\sqrt{2}a_1k^2}{3a_0^2}$	$-\frac{80i a_1 k}{\sqrt{3}a_0^2}$	0	0
$\Delta_{2+}^{\#3} + \alpha\beta$	$-\frac{80a_1k^2}{\sqrt{3}a_0^2}$	$-\frac{2\sqrt{2}a_1k^2}{3a_0^2}$	$\frac{4(3a_0+a_1k^2)}{3a_0^2}$	$-\frac{80i\sqrt{\frac{2}{3}}a_1k}{a_0^2}$	0	0
$\mathcal{T}_{2+}^{\#1} + \alpha\beta$	$\frac{44i\sqrt{2}a_1k}{a_0^2}$	$\frac{80i a_1 k}{\sqrt{3}a_0^2}$	$\frac{80i\sqrt{\frac{2}{3}}a_1k}{a_0^2}$	$-\frac{8(a_0+11a_1k^2)}{a_0^2k^2}$	0	0
$\Delta_{2+}^{\#1} + \alpha\beta\chi$	0	0	0	0	$-\frac{4}{a_0+1k^2}$	0
$\Delta_{2+}^{\#2} + \alpha\beta\chi$	0	0	0	0	0	$\frac{4}{a_0-5a_1k^2}$

	$\mathcal{A}_{0+}^{\#1}$	$\mathcal{A}_{0+}^{\#2}$	$\mathcal{A}_{0+}^{\#3}$	$\mathcal{A}_{0+}^{\#4}$	$h_{0+}^{\#1}$	$h_{0+}^{\#2}$	$\mathcal{A}_{0+}^{\#1}$
$\mathcal{A}_{0+}^{\#1} \dagger$	$\frac{1}{2} (-a_0 + 25 a_1 k^2)$	0	$10 \sqrt{\frac{2}{3}} a_1 k^2$	$-\frac{10 a_1 k^2}{\sqrt{3}}$	$-\frac{25 i a_1 k^3}{2 \sqrt{2}}$	0	0
$\mathcal{A}_{0+}^{\#2} \dagger$	0	0	$\frac{a_0}{2}$	$-\frac{a_0}{2 \sqrt{2}}$	0	0	0
$\mathcal{A}_{0+}^{\#3} \dagger$	$10 \sqrt{\frac{2}{3}} a_1 k^2$	$\frac{a_0}{2}$	$\frac{23 a_1 k^2}{3}$	$-\frac{3 a_0 + 46 a_1 k^2}{6 \sqrt{2}}$	$-\frac{10 i a_1 k^3}{\sqrt{3}}$	0	0
$\mathcal{A}_{0+}^{\#4} \dagger$	$-\frac{10 a_1 k^2}{\sqrt{3}}$	$-\frac{a_0}{2 \sqrt{2}}$	$-\frac{3 a_0 + 46 a_1 k^2}{6 \sqrt{2}}$	$\frac{1}{6} (3 a_0 + 23 a_1 k^2)$	$5 i \sqrt{\frac{2}{3}} a_1 k^3$	0	0
$h_{0+}^{\#1} \dagger$	$\frac{25 i a_1 k^3}{2 \sqrt{2}}$	0	$\frac{10 i a_1 k^3}{\sqrt{3}}$	$-5 i \sqrt{\frac{2}{3}} a_1 k^3$	$\frac{1}{4} k^2 (a_0 + 25 a_1 k^2)$	0	0
$h_{0+}^{\#2} \dagger$	0	0	0	0	0	0	0
$\mathcal{A}_{0+}^{\#1} \dagger$	0	0	0	0	0	0	$\frac{1}{2} (-a_0 + a_1 k^2)$

Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\overline{\mathcal{T}}_0^{-\#2} = 0$	$\partial_\beta \partial_\alpha \mathcal{T}^{-\alpha\beta} = 0$	1
$\Delta_0^{\#3} + 2 \Delta_0^{\#4} + 3 \Delta_0^{\#6} = 0$	$\partial_\alpha \Delta^{\alpha\beta}{}_\beta = 0$	1
$\mathcal{T}_1^{-1\alpha} = 0$	$\partial_\chi \partial_\beta \partial^\alpha \mathcal{T}^{-\beta\chi} = \partial_\chi \partial^\alpha \partial_\beta \mathcal{T}^{-\alpha\beta}$	3
$2 \Delta_1^{\#6\alpha} + \Delta_1^{\#4\alpha} + 2 \Delta_1^{\#5\alpha} + \Delta_1^{\#3\alpha} = 0$	$\partial_\beta \partial^\alpha \Delta^{\beta\chi}{}_\chi = \partial_\chi \partial^\alpha \Delta^{\alpha\beta}{}_\beta$	3
Total constraints/gauge generators:		8

[illegible][illegible]

$$\mathcal{F}_3^{\#1} +^{\alpha\beta\chi} \boxed{\frac{1}{2}(-a_0 - 7a_1k^2)} \Delta_3^{\#1} +^{\alpha\beta\chi} \boxed{-\frac{2}{a_0 + 7a_1k^2}} \Delta_3^{\#1} +^{\alpha\beta\chi}$$

[illegible]

$\mathcal{I}_2^{\#1} + a\beta$	$\frac{1}{4}(a_0 + 11a_1k^2)$	$-5\sqrt{\frac{2}{3}}a_1k^2$	$\frac{5a_1k^2}{\sqrt{3}}$	$-\frac{11a_1k^2}{4\sqrt{2}}$	0	0
$\mathcal{I}_2^{\#2} + a\beta$	$-5\sqrt{\frac{2}{3}}a_1k^2$	$\frac{1}{6}(-3a_0 + a_1k^2)$	$-\frac{a_1k^2}{6\sqrt{2}}$	$\frac{5a_1k^2}{\sqrt{3}}$	0	0
$\mathcal{I}_2^{\#3} + a\beta$	$\frac{5a_1k^2}{\sqrt{3}}$	$-\frac{a_1k^2}{6\sqrt{2}}$	$\frac{1}{12}(3a_0 + a_1k^2)$	$-\frac{5a_1k^2}{\sqrt{6}}$	0	0
$\mathcal{I}_2^{\#1} + a\beta$	$\frac{11a_1k^2}{4\sqrt{2}}$	$-\frac{5a_1k^2}{\sqrt{3}}$	$\frac{5a_1k^2}{\sqrt{6}}$	$-\frac{1}{8}k^2(a_0 - 11a_1k^2)$	0	0
$\mathcal{I}_2^{\#2} + a\beta$	0	0	0	0	$\frac{1}{4}(a_0 - a_1k^2)$	0
$\mathcal{I}_2^{\#3} + a\beta$	0	0	0	0	0	$\frac{1}{4}(a_0 - 5a_1k^2)$

Figure 1 displays Feynman diagrams and corresponding mass matrices for various particle interactions. The diagrams show a central vertex with four external lines, each labeled with a particle symbol (e.g.,  $\chi$ ,  $\psi$ ,  $\phi$ ,  $\eta$ ). The mass matrices are given as 2x2 determinants of elements involving the particle symbols and their masses.

**Diagram 1 (Left):** A central vertex with four external lines labeled  $\chi$ ,  $\psi$ ,  $\phi$ , and  $\eta$ . The mass matrix is:

$$\begin{vmatrix} \frac{4}{s_{\chi 1}} & \frac{4}{s_{\psi 1}} \\ \frac{4}{s_{\phi 1}} & \frac{4}{s_{\eta 1}} \end{vmatrix} > 0$$

**Diagram 2:** A central vertex with four external lines labeled  $\chi$ ,  $\psi$ ,  $\phi$ , and  $\eta$ . The mass matrix is:

$$\begin{vmatrix} \frac{4}{s_{\chi 1}} & \frac{4}{s_{\psi 1}} \\ \frac{4}{s_{\phi 1}} & \frac{4}{s_{\eta 1}} \end{vmatrix} > 0$$

**Diagram 3:** A central vertex with four external lines labeled  $\chi$ ,  $\psi$ ,  $\phi$ , and  $\eta$ . The mass matrix is:

$$\begin{vmatrix} \frac{4}{s_{\chi 1}} & \frac{4}{s_{\psi 1}} \\ \frac{4}{s_{\phi 1}} & \frac{4}{s_{\eta 1}} \end{vmatrix} > 0$$

**Diagram 4:** A central vertex with four external lines labeled  $\chi$ ,  $\psi$ ,  $\phi$ , and  $\eta$ . The mass matrix is:

$$\begin{vmatrix} \frac{4}{s_{\chi 1}} & \frac{4}{s_{\psi 1}} \\ \frac{4}{s_{\phi 1}} & \frac{4}{s_{\eta 1}} \end{vmatrix} > 0$$

**Diagram 5:** A central vertex with four external lines labeled  $\chi$ ,  $\psi$ ,  $\phi$ , and  $\eta$ . The mass matrix is:

$$\begin{vmatrix} \frac{4}{s_{\chi 1}} & \frac{4}{s_{\psi 1}} \\ \frac{4}{s_{\phi 1}} & \frac{4}{s_{\eta 1}} \end{vmatrix} > 0$$

**Diagram 6 (Right):** A central vertex with four external lines labeled  $\chi$ ,  $\psi$ ,  $\phi$ , and  $\eta$ . The mass matrix is:

$$\begin{vmatrix} \frac{4}{s_{\chi 1}} & \frac{4}{s_{\psi 1}} \\ \frac{4}{s_{\phi 1}} & \frac{4}{s_{\eta 1}} \end{vmatrix} > 0$$

(Unitarity is demonstrably impossible)