

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{\#1} \dagger^{\alpha}$	$\sigma_{1-}^{\#2} \dagger^{\alpha}$	$\tau_{1-}^{\#1} \dagger^{\alpha}$	$\tau_{1-}^{\#2} \dagger^{\alpha}$
$\frac{2}{3k^2r_3}$	$-\frac{2\sqrt{2}}{3k^2r_3+3k^4r_3}$	$-\frac{2i\sqrt{2}}{3kr_3+3k^3r_3}$	0	0	0	0
$-\frac{2\sqrt{2}}{3k^2r_3+3k^4r_3}$	$\frac{9k^2r_3+4t_2}{3(k+k^3)^2r_3t_2}$	$\frac{i(9k^2r_3+4t_2)}{3k(1+k^2)^2r_3t_2}$	0	0	0	0
$\frac{2i\sqrt{2}}{3kr_3+3k^3r_3}$	$-\frac{i(9k^2r_3+4t_2)}{3k(1+k^2)^2r_3t_2}$	$\frac{9k^2r_3+4t_2}{3(1+k^2)^2r_3t_2}$	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

Quadratic (free) action

S=

$$\iiint\left[\frac{1}{6}\left(6f^{\alpha\beta}\tau_{\alpha\beta}+6\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}-6r_3\partial_\beta\omega_{\beta}^{\theta}\partial'_\theta\omega_{\alpha}^{\alpha\beta}-6r_3\partial_\alpha\omega^{\alpha\beta}_\beta\partial_\theta\omega_{\beta}^{\theta}+12\right.\right.\\ \left.\left.r_3\partial'_\theta\omega_{\alpha}^{\alpha\beta}\partial_\theta\omega_{\beta}^{\theta}+4t_2\omega_{\theta\alpha}\partial^\theta f^{\alpha i}+2t_2\partial_\alpha f_{\theta}^{\theta\alpha}\partial^\theta f^{\alpha i}-t_2\partial_\alpha f_{\theta}^{\theta\alpha}\partial^\theta f^{\alpha i}-\right.\right.\\ \left.\left.t_2\partial_i f_{\alpha\theta}^{\theta\alpha}\partial^\theta f^{\alpha i}+t_2\partial_\theta f_{\alpha i}^{\alpha i}\partial^\theta f^{\alpha i}-t_2\partial_\theta f_{\alpha i}^{\alpha i}\partial^\theta f^{\alpha i}-4t_2\omega_{\alpha\theta i}\left(\omega^{\alpha i\theta}+\partial^\theta f^{\alpha i}\right)+\right.\right.\\ \left.\left.2t_2\omega_{\alpha i\theta}\left(\omega^{\alpha i\theta}+2\partial^\theta f^{\alpha i}\right)+8r_2\partial_\beta\omega_{\alpha i\theta}\partial^\theta\omega^{\alpha\beta i}-4r_2\partial_\beta\omega_{\alpha\theta i}\partial^\theta\omega^{\alpha\beta i}+\right.\right.\\ \left.\left.4r_2\partial_\beta\omega_{\theta\alpha}\partial^\theta\omega^{\alpha\beta i}-24r_3\partial_\beta\omega_{\theta\alpha}\partial^\theta\omega^{\alpha\beta i}-2r_2\partial_i\omega_{\alpha\theta\theta}\partial^\theta\omega^{\alpha\beta i}+\right.\right.\\ \left.\left.2r_2\partial_\theta\omega_{\alpha\beta i}\partial^\theta\omega^{\alpha\beta i}-4r_2\partial_\theta\omega_{\alpha i\beta}\partial^\theta\omega^{\alpha\beta i}\right)\right][t,x,y,z]dzdydxdt$$

$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1-}^{\#1} \dagger^{\alpha}$	$\omega_{1-}^{\#2} \dagger^{\alpha}$	$f_{1-}^{\#1} \dagger^{\alpha}$	$f_{1-}^{\#2} \dagger^{\alpha}$
$\frac{1}{6}(9k^2r_3+4t_2)$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0	0
$\frac{\sqrt{2}t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0	0
$-\frac{1}{3}i\sqrt{2}kt_2$	$-\frac{1}{3}ikt_2$	$\frac{k^2t_2}{3}$	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

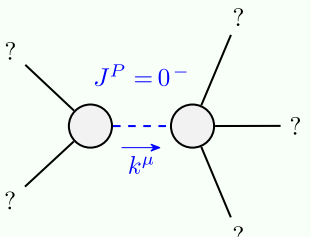
	$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$f_{2+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$		$\omega_{0+}^{\#1} \dagger$	$f_{0+}^{\#1} \dagger$	$f_{0+}^{\#2} \dagger$	$\omega_{0-}^{\#1} \dagger$
$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{3k^2r_3}{2}$	0	0	$\omega_{0+}^{\#1} \dagger$	0	0	0	0
$f_{2+}^{\#1} \dagger^{\alpha\beta}$	0	0	0	$f_{0+}^{\#1} \dagger$	0	0	0	0
$\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	0	$f_{0+}^{\#2} \dagger$	0	0	0	0
				$\omega_{0-}^{\#1} \dagger$	0	0	0	$k^2r_2+t_2$

Source constraints/gauge generators	
SO(3) irreps	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\sigma_{1-}^{\#2\alpha} == 0$	3
$\sigma_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	28

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$
$-\frac{2}{3k^2r_3}$	0	0
0	0	0
0	0	0

	$\sigma_{0+}^{\#1} \dagger$	$\tau_{0+}^{\#1} \dagger$	$\tau_{0+}^{\#2} \dagger$	$\sigma_{0-}^{\#1} \dagger$
$\sigma_{0+}^{\#1} \dagger$	0	0	0	0
$\tau_{0+}^{\#1} \dagger$	0	0	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0	0
$\sigma_{0-}^{\#1} \dagger$	0	0	0	$\frac{1}{k^2r_2+t_2}$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(no massless particles)

Unitarity conditions

$r_2 < 0 \&\& t_2 > 0$