

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} \quad \sigma_{1+}^{\#2} \quad \tau_{1+}^{\#1} \quad \alpha\beta$	$\sigma_{1-}^{\#1} \quad \alpha$	$\sigma_{1-}^{\#2} \quad \alpha$	$\tau_{1-}^{\#1} \quad \alpha$	$\tau_{1-}^{\#2} \quad \alpha$
$\sigma_{1+}^{\#1} \uparrow \alpha\beta$	$\frac{1}{k^2(2r_3+r_5)}$	0	0	0
$\sigma_{1+}^{\#2} \uparrow \alpha\beta$	0	0	0	0
$\tau_{1+}^{\#1} \uparrow \alpha\beta$	0	0	0	0
$\sigma_{1-}^{\#1} \uparrow \alpha$	0	0	$\frac{2}{k^2(r_3+2r_5)}$	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$
$\sigma_{1-}^{\#2} \uparrow \alpha$	0	0	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	$\frac{3k^2(r_3+2r_5)+4t_3}{(k+2k^3)^2(r_3+2r_5)t_3}$
$\tau_{1-}^{\#1} \uparrow \alpha$	0	0	0	0
$\tau_{1-}^{\#2} \uparrow \alpha$	0	$-\frac{4i}{k(1+2k^2)(r_3+2r_5)}$	0	$\frac{6k^2(r_3+2r_5)+8t_3}{(1+2k^2)^2(r_3+2r_5)t_3}$

Quadratic (free) action

$S_F ==$

$$\iiint (\frac{1}{6} (4t_3 \omega_{\lambda'}^{\alpha'} \omega_{\kappa\alpha}^{\kappa} + 6 f^{\alpha\beta} \tau_{\alpha\beta}^{\kappa} + 6 \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi}^{\kappa} - 3 r_3 \partial_{\lambda'} \omega_{\kappa}^{\kappa\lambda} \partial' \omega_{\lambda}^{\alpha} - 6 r_5 \partial_{\lambda'} \omega_{\kappa}^{\kappa\lambda} \partial' \omega_{\lambda}^{\alpha} + 4 r_2 \partial^{\beta} \omega_{\kappa}^{\theta\alpha} \partial_{\theta} \omega_{\alpha\beta}^{\kappa} - 2 r_2 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \partial_{\kappa} \omega^{\alpha\beta\theta} - 4 r_2 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \partial_{\kappa} \omega^{\theta\alpha\beta} + 3 r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\theta}^{\theta\kappa\lambda} - 6 r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega_{\lambda}^{\theta\kappa\lambda} - 3 r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\lambda}^{\alpha} \partial_{\alpha} \omega^{\theta\kappa\lambda} + 6 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\alpha} \omega^{\theta\kappa\lambda} - 6 r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega_{\lambda}^{\kappa\lambda\theta} + 6 r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\alpha} \omega_{\lambda}^{\kappa\lambda\theta} + 12 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\lambda}^{\kappa\lambda\theta} - 4 t_3 \omega_{\kappa\alpha}^{\alpha} \partial^{\kappa} f'_{\lambda} - 4 t_3 \omega_{\lambda\alpha}^{\alpha} \partial^{\kappa} f'_{\kappa} - 4 t_3 \omega_{\lambda\alpha}^{\lambda} \partial^{\kappa} f'_{\kappa} + 4 t_3 \partial^{\alpha} f'_{\alpha} \partial^{\kappa} f_{\lambda\kappa} + 2 r_2 \partial_{\kappa} \omega^{\alpha\beta\theta} \partial^{\kappa} \omega_{\alpha\beta\theta} + 4 r_2 \partial_{\kappa} \omega^{\theta\alpha\beta} \partial^{\kappa} \omega_{\alpha\beta\theta} - 4 r_2 \partial^{\beta} \omega_{\lambda'}^{\alpha\lambda} \partial_{\lambda} \omega_{\alpha\beta}^{\kappa} + 4 r_2 \partial^{\beta} \omega_{\lambda'}^{\lambda\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\kappa} - 24 r_3 \partial^{\beta} \omega_{\lambda'}^{\lambda\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\kappa} - 3 r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} + 6 r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} + 3 r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa} - 6 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\kappa}^{\theta\kappa})) [t, x, y, z] dz dy dx dt$$

$\omega_{1+}^{\#1} \uparrow \alpha\beta$	$\omega_{1+}^{\#2} \uparrow \alpha\beta$	$f_{1+}^{\#1} \uparrow \alpha\beta$	$\omega_{1-}^{\#1} \quad \alpha$	$\omega_{1-}^{\#2} \quad \alpha$	$f_{1-}^{\#1} \quad \alpha$	$f_{1-}^{\#2} \quad \alpha$
$\omega_{1+}^{\#1} \uparrow \alpha\beta$	$k^2(2r_3+r_5)$	0	0	0	0	0
$\omega_{1+}^{\#2} \uparrow \alpha\beta$	0	0	0	0	0	0
$f_{1+}^{\#1} \uparrow \alpha\beta$	0	0	0	0	0	0
$\omega_{1-}^{\#1} \uparrow \alpha$	0	0	$k^2(\frac{r_3}{2}+r_5)+\frac{2t_3}{3}$	$-\frac{\sqrt{2}t_3}{3}$	0	$-\frac{2}{3}i k t_3$
$\omega_{1-}^{\#2} \uparrow \alpha$	0	0	$-\frac{\sqrt{2}t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3}i \sqrt{2} k t_3$
$f_{1-}^{\#1} \uparrow \alpha$	0	0	0	0	0	0
$f_{1-}^{\#2} \uparrow \alpha$	0	0	$\frac{2i k t_3}{3}$	$-\frac{1}{3}i \sqrt{2} k t_3$	0	$\frac{2k^2 t_3}{3}$

$\omega_{2+}^{\#1} \uparrow \alpha\beta$	$f_{2+}^{\#1} \uparrow \alpha\beta$	$\omega_{2-}^{\#1} \alpha\beta\chi$
$\omega_{2+}^{\#1} \uparrow \alpha\beta$	$-\frac{3k^2 r_3}{2}$	0
$f_{2+}^{\#1} \uparrow \alpha\beta$	0	0
$\omega_{2-}^{\#1} \uparrow \alpha\beta\chi$	0	0

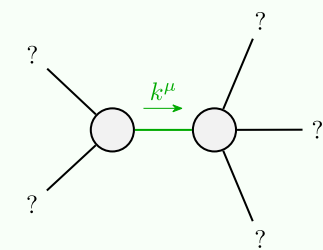
$\sigma_{2+}^{\#1} \uparrow \alpha\beta$	$\tau_{2+}^{\#1} \uparrow \alpha\beta$	$\sigma_{2-}^{\#1} \alpha\beta\chi$
$\sigma_{2+}^{\#1} \uparrow \alpha\beta$	$-\frac{2}{3k^2 r_3}$	0
$\tau_{2+}^{\#1} \uparrow \alpha\beta$	0	0
$\sigma_{2-}^{\#1} \uparrow \alpha\beta\chi$	0	0

Source constraints/gauge generators	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} - 2 i k \sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2 i k \sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} == 0$	3
$\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	24

	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1} \uparrow$	t_3	$-i \sqrt{2} k t_3$	0	0
$f_{0+}^{\#1} \uparrow$	$i \sqrt{2} k t_3$	$2 k^2 t_3$	0	0
$f_{0+}^{\#2} \uparrow$	0	0	0	0
$\omega_{0-}^{\#1} \uparrow$	0	0	0	$k^2 r_2$

	$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1} \uparrow$	$\frac{1}{(1+2k^2)^2 t_3}$	$-\frac{i \sqrt{2} k}{(1+2k^2)^2 t_3}$	0	0
$\tau_{0+}^{\#1} \uparrow$	$\frac{i \sqrt{2} k}{(1+2k^2)^2 t_3}$	$\frac{2k^2}{(1+2k^2)^2 t_3}$	0	0
$\tau_{0+}^{\#2} \uparrow$	0	0	0	0
$\sigma_{0-}^{\#1} \uparrow$	0	0	0	$\frac{1}{k^2 r_2}$

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$