

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$\frac{t_1}{r_2} > 0$
Spin:	0
Parity:	Odd

Quadratic pole	
Pole residue:	$-\frac{1}{(2r_3+r_5)t_1^2} > 0$
Polarisations:	2

$r_2 < 0 \ \&\& \ r_5 < -2r_3 \ \&\& \ t_1 < 0$

Unitarity conditions

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2}$	$\tau_{1+}^{\#1}$	$\sigma_{1-}^{\#1}$	$\sigma_{1-}^{\#2}$	$\tau_{1-}^{\#2}$
$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$0$	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$0$	$0$	$0$
$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$\frac{-2k^2(2r_3+r_5)+t_1}{(1+k^2)^2t_1^2}$	$0$	$0$	$0$
$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\frac{i\sqrt{2}k}{t_1+k^2t_1}$	$\frac{i(2k^3(2r_3+r_5)-kt_1)}{(1+k^2)^2t_1^2}$	$0$	$0$	$0$
$\sigma_{1-}^{\#1} \dagger^{\alpha}$	$0$	$0$	$\frac{1}{k^2(2r_3+r_5)}$	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	$-\frac{i}{k(1+2k^2)(2r_3+r_5)}$
$\sigma_{1-}^{\#2} \dagger^{\alpha}$	$0$	$0$	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	$\frac{6k^2(2r_3+r_5)+t_1}{2(k+2k^3)^2(2r_3+r_5)t_1}$	$\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$
$\tau_{1-}^{\#1} \dagger^{\alpha}$	$0$	$0$	$0$	$0$	$0$
$\tau_{1-}^{\#2} \dagger^{\alpha}$	$0$	$0$	$\frac{i}{k(1+2k^2)(2r_3+r_5)}$	$-\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$	$\frac{6k^2(2r_3+r_5)+t_1}{(1+2k^2)^2(2r_3+r_5)t_1}$

Lagrangian density

$$\begin{aligned}
&-\frac{1}{3}t_1\omega_{\lambda'}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\kappa\lambda'}^{\kappa\lambda}\omega_{\lambda'}^{\lambda'}-2r_3\partial_{\lambda'}\omega_{\kappa}^{\kappa\lambda}\partial_{\lambda'}\omega_{\lambda}^{\alpha}- \\
&r_5\partial_{\lambda'}\omega_{\kappa}^{\kappa\lambda}\partial_{\lambda'}\omega_{\lambda}^{\alpha}+\frac{2}{3}r_2\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}- \\
&\frac{2}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}+2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\theta}^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}- \\
&2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}- \\
&r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}+4r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}- \\
&\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial_{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}\partial_{\theta}f_{\alpha}^{\kappa}-\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial_{\kappa}f_{\alpha\lambda}^{\kappa}+ \\
&\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial_{\kappa}f_{\lambda'}^{\lambda'}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial_{\kappa}f_{\lambda'}^{\lambda'}+\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}\partial_{\kappa}f_{\lambda'}^{\lambda'}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda'}^{\lambda'}+ \\
&2t_1\omega_{\lambda\kappa\theta}\partial^{\kappa}f_{\lambda'}^{\theta}-\frac{1}{3}t_1\omega_{\lambda'\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\lambda'}-\frac{1}{3}t_1\omega_{\lambda\lambda}^{\lambda}\partial_{\kappa}f_{\lambda'}^{\lambda'}+\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial_{\kappa}f_{\lambda\alpha}^{\kappa}+ \\
&\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial_{\theta}f_{\lambda}^{\lambda}-\frac{1}{3}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial_{\alpha}f_{\lambda\kappa}^{\kappa}+ \\
&\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda'}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda'}+ \\
&\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda'}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda'}-4r_3\partial^{\beta}\omega_{\lambda'}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda'}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}+ \\
&r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}+2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa} \\
\end{aligned}$$

Added source term:  $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{2+}^{\#1}$	$\sigma_{2-}^{\#1}$
$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$0$
$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	$0$
$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	$0$	$\frac{2}{t_1}$

$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_0^{\#1}$
$\omega_{0+}^{\#1} \dagger$	$6k^2r_3$	$0$	$0$
$f_{0+}^{\#1} \dagger$	$0$	$0$	$0$
$f_{0+}^{\#2} \dagger$	$0$	$0$	$0$
$\omega_0^{\#1} \dagger$	$0$	$0$	$k^2r_2-t_1$

Source constraints	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2i k \sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2i k \sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	16

	$\omega_{1+}^{\#1}$	$\omega_{1+}^{\#2}$	$f_{1+}^{\#1}$	$\omega_{1-}^{\#1}$	$\omega_{1-}^{\#2}$	$f_{1-}^{\#1}$	$f_{1-}^{\#2}$
$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$k^2(2r_3+r_5)-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	$0$	$0$	$0$	$0$
$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$-\frac{t_1}{\sqrt{2}}$	$0$	$0$	$0$	$0$	$0$	$0$
$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\frac{ikt_1}{\sqrt{2}}$	$0$	$0$	$0$	$0$	$0$	$0$
$\omega_{1-}^{\#1} \dagger^{\alpha}$	$0$	$0$	$0$	$k^2(2r_3+r_5)+\frac{t_1}{6}$	$\frac{t_1}{3\sqrt{2}}$	$0$	$\frac{ikt_1}{3}$
$\omega_{1-}^{\#2} \dagger^{\alpha}$	$0$	$0$	$0$	$\frac{t_1}{3\sqrt{2}}$	$\frac{t_1}{3}$	$0$	$\frac{1}{3}i\sqrt{2}kt_1$
$f_{1-}^{\#1} \dagger^{\alpha}$	$0$	$0$	$0$	$0$	$0$	$0$	$0$
$f_{1-}^{\#2} \dagger^{\alpha}$	$0$	$0$	$0$	$-\frac{1}{3}i kt_1$	$-\frac{1}{3}i\sqrt{2}kt_1$	$0$	$\frac{2k^2t_1}{3}$

	$\omega_{2+}^{\#1}$	$f_{2+}^{\#1}$	$\omega_{2-}^{\#1}$
$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	$0$
$f_{2+}^{\#1} \dagger^{\alpha\beta}$	$\frac{ikt_1}{\sqrt{2}}$	$k^2t_1$	$0$
$\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	$0$	$0$	$\frac{t_1}{2}$

	$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_0^{\#1}$
$\sigma_{0+}^{\#1} \dagger$	$\frac{1}{6k^2r_3}$	$0$	$0$	$0$
$\tau_{0+}^{\#1} \dagger$	$0$	$0$	$0$	$0$
$\tau_{0+}^{\#2} \dagger$	$0$	$0$	$0$	$0$
$\sigma_0^{\#1} \dagger$	$0$	$0$	$0$	$\frac{1}{k^2r_2-t_1}$