

Wave operator and propagator

Quadratic (free) action

$$\begin{aligned} S_F = & \iiint \left(\frac{1}{3} (-6\beta_1 \omega_\alpha^{x\delta} \omega_{\chi\delta}^\alpha + 3f^{\alpha\beta} \tau_{\alpha\beta} + 3\omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 6\beta_1 \omega_\alpha^x \partial_\beta f^{\alpha\beta} - 6\beta_1 \right. \\ & \omega_\alpha^\delta \partial_\beta f^{\alpha\beta} - 12\beta_1 f^{\alpha\beta} \partial_\beta \omega_\alpha^x + 12\beta_1 \partial_\beta \omega_\alpha^{\alpha\beta} + 2\alpha_3 \partial^\alpha \omega^{\beta\zeta} \partial_\chi \omega_\zeta^x + \\ & 6\beta_1 \omega_\beta^x \partial^\beta f_\alpha^\alpha + 6\beta_1 \omega_\beta^\delta \partial^\beta f_\alpha^\alpha - 6\beta_1 \partial_\beta f_\alpha^x \partial^\beta f_\alpha^\alpha + 12\beta_1 f^{\alpha\beta} \partial_\chi \omega_\alpha^x \partial_\beta \omega_\beta^x - \\ & 12\beta_1 f_\alpha^\alpha \partial_\chi \omega_\beta^{x\chi} - 2\alpha_3 \partial_\beta \omega_\zeta^x \partial_\chi \omega_\zeta^{\beta\zeta\alpha} - \alpha_3 \partial_\beta \omega_\zeta^x \partial_\chi \omega_\zeta^{\zeta\alpha\beta} - \\ & 6\beta_1 \omega_{\alpha\chi\beta} (\omega^{\alpha\beta\chi} - 2\partial^x f_\beta^{\alpha\beta}) + 3\beta_1 \partial_\chi f_\beta^\delta \partial^x f_\delta^\beta + 3\beta_1 \partial_\chi f_\delta^\delta \partial^x f_\delta^\beta + \\ & 2\alpha_3 \partial_\chi \omega^{\beta\zeta\alpha} \partial_\alpha \omega_{\zeta\alpha\beta} + \alpha_3 \partial_\chi \omega^{\zeta\alpha\beta} \partial_\alpha \omega_{\zeta\alpha\beta} + 12\beta_1 \partial^\beta f_\alpha^\alpha \partial_\delta f_\beta^\delta - \\ & 6\beta_1 \partial_\beta f_\chi^\beta \partial_\delta f_\chi^{\alpha\delta} + 2\alpha_3 \partial^\beta \omega_\alpha^{\delta\zeta} \partial_\delta \omega_\zeta^{\alpha\delta} - 2\alpha_3 \partial^\beta \omega_\alpha^{\zeta\delta} \partial_\delta \omega_\zeta^{\alpha\delta} - 3\beta_1 \partial^x f_\zeta^\beta \partial^\zeta f_\zeta^{\beta\chi} \\ & \left. - 3\beta_1 \partial^x f_\zeta^\beta \partial^\zeta f_\chi^\beta + 3\beta_1 \partial_\chi f_{\delta\zeta}^\alpha \partial^\zeta f_\alpha^\delta - 3\beta_1 \partial_\chi f_{\zeta\delta}^\alpha \partial^\zeta f_\alpha^\delta \right) ([t, x, y, z] dz dy dx dt \end{aligned}$$

	$\omega_{2^+}^{\#1} \alpha \beta$	$f_{2^+}^{\#1} \alpha \beta$	$\omega_{2^+}^{\#1} \alpha \beta \chi$
$\omega_{2^+}^{\#1} \dagger \alpha \beta$	0	0	0
$f_{2^+}^{\#1} \dagger \alpha \beta$	0	$2 \beta_1 k^2$	0
$\omega_{2^+}^{\#1} \dagger \alpha \beta \chi$	0	0	0

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\sigma_{1-}^{\#2\alpha} == 0$	3
$\sigma_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} == 0$	3
$\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\sigma_{1+}^{\#1\alpha\beta} == 0$	3
$\sigma_{2+}^{\#1\alpha\beta} == 0$	5
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
Total constraints:	33

$\sigma_0^{#1} +$	0	0	0	0
$\tau_0^{#1} +$	0	$-\frac{1}{4\beta_1 k^2}$	0	0
$\tau_0^{#2} +$	0	0	0	0
$\sigma_0^{#1} -$	0	0	0	$\frac{1}{\alpha_3 k^2}$

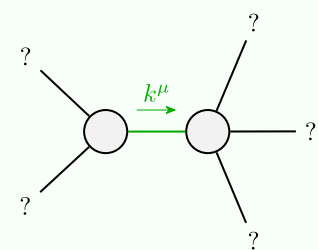
	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1} \dagger$	0	0	0	0
$f_{0+}^{\#1} \dagger$	0	$-4 \beta_1 k^2$	0	0
$f_{0+}^{\#2} \dagger$	0	0	0	0
$\omega_{0-}^{\#1} \dagger$	0	0	0	$\alpha_3 k^2$

$\sigma_2^{\#1} \dagger \alpha\beta$	$\sigma_2^{\#1} + \alpha\beta$	$\tau_2^{\#1}$	$\sigma_2^{\#1} + \alpha\beta$	$\sigma_2^{\#1} - \alpha\beta\chi$
$\tau_2^{\#1} \dagger \alpha\beta$	0	0	$\frac{1}{2\beta_1 k^2}$	0
$\sigma_2^{\#1} \dagger \alpha\beta\chi$	0	0	0	0

$\omega_1^{\#1} \dagger \alpha \beta$	0	0	$\omega_1^{\#2} \dagger \alpha \beta$	0	0	$\omega_1^{\#1} \alpha$	0	0	$\omega_1^{\#2} \alpha$	0	0	$f_1^{\#1} \alpha$	0	0	$f_1^{\#2} \alpha$
$\omega_1^{\#2} \dagger \alpha \beta$	0	0	$\omega_1^{\#1} \dagger \alpha \beta$	0	0	$\omega_1^{\#2} \alpha$	0	0	$\omega_1^{\#1} \alpha$	0	0	$f_1^{\#1} \alpha$	0	0	$f_1^{\#2} \alpha$
$f_1^{\#1} \dagger \alpha \beta$	0	0	$f_1^{\#2} \dagger \alpha \beta$	0	0	$f_1^{\#1} \alpha$	0	0	$f_1^{\#2} \alpha$	0	0	$\omega_1^{\#1} \alpha$	0	0	$\omega_1^{\#2} \alpha$
$\omega_1^{\#1} \dagger \alpha$	0	0	$\omega_1^{\#2} \dagger \alpha$	0	0	$\omega_1^{\#1} \alpha$	0	0	$\omega_1^{\#2} \alpha$	0	0	$f_1^{\#1} \alpha$	0	0	$f_1^{\#2} \alpha$
$\omega_1^{\#2} \dagger \alpha$	0	0	$\omega_1^{\#1} \dagger \alpha$	0	0	$\omega_1^{\#2} \alpha$	0	0	$\omega_1^{\#1} \alpha$	0	0	$f_1^{\#1} \alpha$	0	0	$f_1^{\#2} \alpha$
$f_1^{\#1} \dagger \alpha$	0	0	$f_1^{\#2} \dagger \alpha$	0	0	$f_1^{\#1} \alpha$	0	0	$f_1^{\#2} \alpha$	0	0	$\omega_1^{\#1} \alpha$	0	0	$\omega_1^{\#2} \alpha$
$f_1^{\#2} \dagger \alpha$	0	0	$f_1^{\#1} \dagger \alpha$	0	0	$f_1^{\#2} \alpha$	0	0	$f_1^{\#1} \alpha$	0	0	$\omega_1^{\#1} \alpha$	0	0	$\omega_1^{\#2} \alpha$

$\sigma_{1+}^{\#1} + \alpha\beta$	0	0	$\tau_{1+}^{\#1} + \alpha\beta$	0	0	$\sigma_{1-}^{\#1} + \alpha$	0	0	$\tau_{1-}^{\#1} + \alpha$	0
$\sigma_{1+}^{\#2} + \alpha\beta$	0	0	$\tau_{1+}^{\#2} + \alpha\beta$	0	0	$\sigma_{1-}^{\#2} + \alpha$	0	0	$\tau_{1-}^{\#2} + \alpha$	0
$\tau_{1+}^{\#1} + \alpha\beta$	0	0	$\tau_{1+}^{\#1} + \alpha\beta$	0	0	$\sigma_{1-}^{\#1} + \alpha$	0	0	$\tau_{1-}^{\#1} + \alpha$	0
$\sigma_{1-}^{\#1} + \alpha$	0	0	$\tau_{1-}^{\#1} + \alpha$	0	0	$\sigma_{1-}^{\#1} + \alpha$	0	0	$\tau_{1-}^{\#1} + \alpha$	0
$\sigma_{1-}^{\#2} + \alpha$	0	0	$\tau_{1-}^{\#2} + \alpha$	0	0	$\sigma_{1-}^{\#2} + \alpha$	0	0	$\tau_{1-}^{\#2} + \alpha$	0
$\tau_{1-}^{\#1} + \alpha$	0	0	$\tau_{1-}^{\#1} + \alpha$	0	0	$\sigma_{1-}^{\#1} + \alpha$	0	0	$\tau_{1-}^{\#1} + \alpha$	0
$\tau_{1-}^{\#2} + \alpha$	0	0	$\tau_{1-}^{\#2} + \alpha$	0	0	$\sigma_{1-}^{\#2} + \alpha$	0	0	$\tau_{1-}^{\#2} + \alpha$	0

Massive and massless spectra



Quadratic pole	
Pole residue:	$\frac{1}{\beta_1} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$\beta_1 > 0$$