

Particle spectrograph

Wave operator and propagator

	$\sigma_{2^+}^{\#1}{}_{\alpha\beta}$	$\tau_{2^+}^{\#1}{}_{\alpha\beta}$	$\sigma_{2^+}^{\#1}{}_{\alpha\beta\chi}$
$\sigma_{2^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\tau_{2^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\sigma_{2^+}^{\#1}{}_{\dagger\alpha\beta\chi}$	0	0	$\frac{2}{t_1}$

	$\omega_{0^+}^{\#1}$	$f_{0^+}^{\#1}$	$f_{0^+}^{\#2}$	$\omega_{0^+}^{\#1}$
$\omega_{0^+}^{\#1}{}_{\dagger}$	t_3	$-i\sqrt{2}kt_3$	0	0
$f_{0^+}^{\#1}{}_{\dagger}$	$i\sqrt{2}kt_3$	$2k^2t_3$	0	0
$f_{0^+}^{\#2}{}_{\dagger}$	0	0	0	0
$\omega_{0^+}^{\#1}{}_{\dagger}$	0	0	0	$k^2r_2+t_2$

	$\omega_{2^+}^{\#1}{}_{\alpha\beta}$	$f_{2^+}^{\#1}{}_{\alpha\beta}$	$\omega_{2^+}^{\#1}{}_{\alpha\beta\chi}$
$\omega_{2^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{ikt_1}{\sqrt{2}}$	k^2t_1	0
$\omega_{2^+}^{\#1}{}_{\dagger\alpha\beta\chi}$	0	0	$\frac{t_1}{2}$

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\tau_{0^+}^{\#2} == 0$	1
$\tau_{0^+}^{\#1} - 2ik\sigma_{0^+}^{\#1} == 0$	1
$\tau_{1^-}^{\#2\alpha} + 2ik\sigma_{1^-}^{\#2\alpha} == 0$	3
$\tau_{1^-}^{\#1\alpha} == 0$	3
$\tau_{1^+}^{\#1\alpha\beta} + ik\sigma_{1^+}^{\#2\alpha\beta} == 0$	3
$\tau_{2^+}^{\#1\alpha\beta} - 2ik\sigma_{2^+}^{\#1\alpha\beta} == 0$	5
Total constraints:	16

Quadratic (free) Lagrangian density

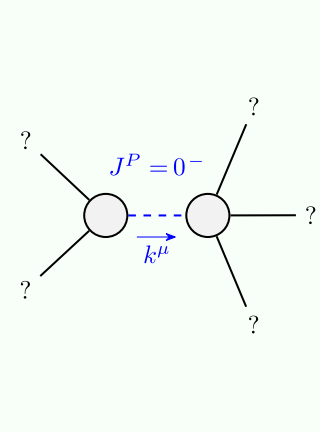
$$\begin{aligned} & -\frac{1}{3}t_1\omega_{\lambda'}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_3\omega_{\lambda'}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-\frac{1}{3}t_1\omega_{\kappa\lambda'}^{\kappa\lambda}\omega_{\lambda'}^{\lambda'}+\frac{2}{3}t_2\omega_{\lambda'}^{\kappa\lambda}\omega_{\kappa\lambda}^{\lambda'}+ \\ & \frac{1}{3}t_1\omega_{\kappa\lambda'}^{\lambda'}\omega_{\lambda'}^{\kappa\lambda}+\frac{1}{3}t_2\omega_{\kappa\lambda'}^{\lambda'}\omega_{\lambda'}^{\kappa\lambda}+f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}+ \\ & \frac{2}{3}r_2\partial^\theta\omega_{\kappa}^{\theta\alpha}\partial_\theta\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega_{\alpha\beta}^{\theta}-\frac{2}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega_{\alpha\beta}^{\theta}- \\ & \frac{1}{3}t_1\partial^\alpha f_{\theta\kappa}\partial_\kappa f_{\alpha}^{\theta}+\frac{1}{6}t_2\partial^\alpha f_{\theta\kappa}\partial_\kappa f_{\alpha}^{\theta}-\frac{2}{3}t_1\partial^\alpha f_{\kappa\theta}\partial_\theta f_{\alpha}^{\kappa}-\frac{1}{6}t_2\partial^\alpha f_{\kappa\theta}\partial_\theta f_{\alpha}^{\kappa}- \\ & \frac{1}{3}t_1\partial^\alpha f_{\lambda}^{\lambda}\partial_\kappa f_{\alpha\lambda}^{\kappa}+\frac{1}{6}t_2\partial^\alpha f_{\lambda}^{\lambda}\partial_\kappa f_{\alpha\lambda}^{\kappa}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial_\kappa f_{\lambda'}^{\lambda'}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial_\kappa f_{\lambda'}^{\lambda'}+ \\ & \frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial_\kappa f_{\lambda'}^{\lambda'}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial_\kappa f_{\lambda'}^{\lambda'}+\frac{2}{3}t_1\partial^\alpha f_{\kappa\alpha}\partial_\lambda f_{\lambda'}^{\lambda'}-\frac{4}{3}t_3\partial^\alpha f_{\kappa\alpha}\partial_\lambda f_{\lambda'}^{\lambda'}- \\ & \frac{1}{3}t_1\partial_{\kappa f_{\lambda}}^{\lambda}\partial_\kappa f_{\lambda}^{\theta}-\frac{1}{6}t_2\partial_{\kappa f_{\lambda}}^{\lambda}\partial_\kappa f_{\lambda}^{\theta}+\frac{2}{3}t_1\partial_{\kappa f_{\lambda}}^{\lambda}\partial_\kappa f_{\lambda}^{\theta}+\frac{1}{6}t_2\partial_{\kappa f_{\lambda}}^{\lambda}\partial_\kappa f_{\lambda}^{\theta}- \\ & \frac{1}{3}t_1\partial^\alpha f_{\lambda}^{\lambda}\partial_\kappa f_{\lambda\kappa}^{\kappa}+\frac{2}{3}t_3\partial^\alpha f_{\lambda}^{\lambda}\partial_\kappa f_{\lambda\kappa}^{\kappa}+\frac{1}{3}r_2\partial_\kappa\omega^{\alpha\beta\theta}\partial_\kappa\omega_{\alpha\beta\theta}+ \\ & \frac{2}{3}r_2\partial_\kappa\omega^{\theta\alpha\beta}\partial_\kappa\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^\beta\omega_{\lambda'}^{\alpha\lambda}\partial_\lambda\omega_{\alpha\beta}^{\lambda'}+\frac{2}{3}r_2\partial^\beta\omega_{\lambda'}^{\lambda\alpha}\partial_\lambda\omega_{\alpha\beta}^{\lambda'} \end{aligned}$$

	$\sigma_{0^+}^{\#1}$	$\tau_{0^+}^{\#1}$	$\tau_{0^+}^{\#2}$	$\sigma_{0^+}^{\#1}$
$\sigma_{0^+}^{\#1}{}_{\dagger}$	$\frac{1}{(1+2k^2)^2t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0	0
$\tau_{0^+}^{\#1}{}_{\dagger}$	$\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0	0
$\tau_{0^+}^{\#2}{}_{\dagger}$	0	0	0	0
$\sigma_{0^+}^{\#1}{}_{\dagger}$	0	0	0	$\frac{1}{k^2r_2+t_2}$

	$\omega_{1^+}^{\#1}{}_{\alpha\beta}$	$\omega_{1^+}^{\#2}{}_{\alpha\beta}$	$f_{1^+}^{\#1}{}_{\alpha\beta}$	$\omega_{1^+}^{\#1}{}_{\alpha}$	$\omega_{1^+}^{\#2}{}_{\alpha}$	$f_{1^+}^{\#1}{}_{\alpha}$	$f_{1^+}^{\#2}{}_{\alpha}$
$\omega_{1^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{1}{6}(t_1+4t_2)$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$-\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2}{}_{\dagger\alpha\beta}$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$\frac{t_1+t_2}{3}$	$\frac{1}{3}ik(t_1+t_2)$	0	0	0	0
$f_{1^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	$-\frac{1}{3}ik(t_1+t_2)$	$\frac{1}{3}k^2(t_1+t_2)$	0	0	0	0
$\omega_{1^+}^{\#1}{}_{\dagger\alpha}$	0	0	0	$\frac{1}{6}(t_1+4t_3)$	$\frac{t_1-2t_3}{3\sqrt{2}}$	0	$\frac{1}{3}ik(t_1-2t_3)$
$\omega_{1^+}^{\#2}{}_{\dagger\alpha}$	0	0	0	$\frac{t_1-2t_3}{3\sqrt{2}}$	$\frac{t_1+t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}k(t_1+t_3)$
$f_{1^+}^{\#1}{}_{\dagger\alpha}$	0	0	0	0	0	0	0
$f_{1^+}^{\#2}{}_{\dagger\alpha}$	0	0	0	$-\frac{1}{3}ik(t_1-2t_3)$	$-\frac{1}{3}i\sqrt{2}k(t_1+t_3)$	0	$\frac{2}{3}k^2(t_1+t_3)$

	$\sigma_{1^+}^{\#1}{}_{\alpha\beta}$	$\sigma_{1^+}^{\#2}{}_{\alpha\beta}$	$\tau_{1^+}^{\#1}{}_{\alpha\beta}$	$\sigma_{1^+}^{\#1}{}_{\alpha}$	$\sigma_{1^+}^{\#2}{}_{\alpha}$	$\tau_{1^+}^{\#1}{}_{\alpha}$	$\tau_{1^+}^{\#2}{}_{\alpha}$
$\sigma_{1^+}^{\#1}{}_{\dagger\alpha\beta}$	$\frac{2(t_1+t_2)}{3t_1t_2}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	0	$-\frac{\sqrt{2}(t_1-2t_2)}{3(1+2k^2)t_1t_3}$	0	$-\frac{2ikt_1-4ikt_3}{3t_1t_3+6k^2t_1t_3}$
$\sigma_{1^+}^{\#2}{}_{\dagger\alpha\beta}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{t_1+4t_2}{3(1+k^2)^2t_1t_2}$	$\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	$\frac{t_1+4t_3}{3(1+2k^2)^2t_1t_3}$	0	$\frac{i\sqrt{2}k(t_1+4t_3)}{3(1+2k^2)^2t_1t_3}$
$\tau_{1^+}^{\#1}{}_{\dagger\alpha\beta}$	$-\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$-\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	$\frac{k^2(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	$-\frac{\sqrt{2}(t_1-2t_3)}{3(1+2k^2)t_1t_3}$	0	$-\frac{2ikt_1-4ikt_3}{3t_1t_3+6k^2t_1t_3}$
$\sigma_{1^+}^{\#1}{}_{\dagger\alpha}$	0	0	0	$\frac{2(t_1+t_3)}{3t_1t_3}$	$-\frac{\sqrt{2}(t_1-2t_3)}{3(1+2k^2)t_1t_3}$	0	$\frac{2k^2(t_1+4t_3)}{3(1+2k^2)^2t_1t_3}$
$\sigma_{1^+}^{\#2}{}_{\dagger\alpha}$	0	0	0	0	$-\frac{\sqrt{2}(t_1-2t_3)}{3(1+2k^2)t_1t_3}$	0	$\frac{i\sqrt{2}k(t_1+4t_3)}{3(1+2k^2)^2t_1t_3}$
$\tau_{1^+}^{\#1}{}_{\dagger\alpha}$	0	0	0	0	0	0	0
$\tau_{1^+}^{\#2}{}_{\dagger\alpha}$	0	0	0	0	$-\frac{2ikt_1-4ikt_3}{3t_1t_3+6k^2t_1t_3}$	0	$\frac{2k^2(t_1+4t_3)}{3(1+2k^2)^2t_1t_3}$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

Unitarity conditions

$$r_2 < 0 \ \&\& \ t_2 > 0$$