

Particle spectrograph

Wave operator and propagator

Quadratic (free) action

$$\begin{aligned}
S = & \iiint (\omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 2r_3 (\partial_\beta \omega_{,\theta}^\theta \partial' \omega_{,\theta}^{\alpha\beta} + \partial'_\theta \omega_{,\beta}^\theta \partial' \omega_{,\theta}^{\alpha\beta} + \partial_\alpha \omega_{,\theta}^{\alpha\beta} \partial_\theta \omega_{,\beta}^\theta - \\
& 2 \partial'_\theta \omega_{,\beta}^{\alpha\beta} \partial_\theta \omega_{,\beta}^\theta + \partial_\alpha \omega_{,\beta}^{\alpha\beta} \partial_\theta \omega_{,\beta}^\theta - 2 \partial'_\theta \omega_{,\beta}^{\alpha\beta} \partial_\theta \omega_{,\theta}^\theta + 2 \partial_\beta \omega_{,\theta\alpha}^\theta \partial^\theta \omega^{\alpha\beta}) + \\
& \frac{2}{3} r_1 (3 \partial_\beta \omega_{,\theta}^\theta \partial'_\theta \omega_{,\theta}^{\alpha\beta} + 3 \partial'_\theta \omega_{,\beta}^\theta \partial'_\theta \omega_{,\theta}^{\alpha\beta} + 3 \partial_\alpha \omega_{,\beta}^{\alpha\beta} \partial_\theta \omega_{,\beta}^\theta - 6 \partial'_\theta \omega_{,\beta}^{\alpha\beta} \partial_\alpha \partial_\theta \omega_{,\beta}^\theta + \\
& 3 \partial_\alpha \omega_{,\beta}^{\alpha\beta} \partial_\theta \omega_{,\beta}^\theta - 6 \partial'_\theta \omega_{,\beta}^{\alpha\beta} \partial_\alpha \partial_\theta \omega_{,\beta}^\theta - 2 \partial_\beta \omega_{,\alpha\theta}^\theta \partial^\theta \omega^{\alpha\beta} + \partial_\beta \omega_{,\alpha\theta}^\theta \partial^\theta \omega^{\alpha\beta} + \\
& 2 \partial_\beta \omega_{,\theta\alpha}^\theta \partial^\theta \omega^{\alpha\beta} - \partial'_\theta \omega_{,\alpha\beta\theta}^\theta \partial^\theta \omega^{\alpha\beta} + \partial_\theta \omega_{,\alpha\beta}^\theta \partial^\theta \omega^{\alpha\beta} + \partial_\theta \omega_{,\alpha\beta}^\theta \partial^\theta \omega^{\alpha\beta}) + \\
& r_5 (\partial'_\theta \omega_{,\theta}^\kappa \partial^\theta \omega_{,\kappa}^{\alpha\iota} - \partial_\theta \omega_{,\kappa}^\kappa \partial^\theta \omega_{,\iota}^{\alpha\iota} - (\partial_\alpha \omega_{,\kappa}^{\alpha\iota} - 2 \partial^\theta \omega_{,\iota}^{\alpha\iota}) (\partial_\kappa \omega_{,\theta}^\kappa - \partial_\kappa \omega_{,\theta}^\kappa))) [\\
& t, x, y, z] dz dy dx dt
\end{aligned}$$

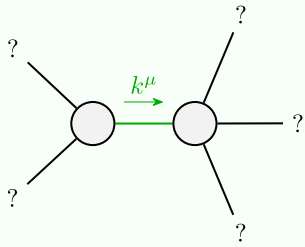
$$\begin{array}{c}
\begin{array}{cc}
\omega_{2+}^{\#1} \alpha\beta & \omega_{2-}^{\#1} \alpha\beta\chi \\
\omega_{2+}^{\#1} \dagger\alpha\beta & \omega_{2-}^{\#1} \dagger\alpha\beta\chi \\
\omega_{2+}^{\#1} \dagger\alpha\beta\chi & \omega_{2-}^{\#1} \dagger\alpha\beta\chi
\end{array}
\begin{array}{cc}
0 & 0 \\
0 & k^2 r_1
\end{array}
\end{array}
\begin{array}{c}
\begin{array}{cc}
\sigma_{2+}^{\#1} \alpha\beta & \sigma_{2-}^{\#1} \alpha\beta\chi \\
\sigma_{2+}^{\#1} \dagger\alpha\beta & \sigma_{2-}^{\#1} \dagger\alpha\beta\chi \\
\sigma_{2+}^{\#1} \dagger\alpha\beta\chi & \sigma_{2-}^{\#1} \dagger\alpha\beta\chi
\end{array}
\begin{array}{cc}
0 & 0 \\
0 & \frac{1}{k^2 r_1}
\end{array}
\end{array}
\begin{array}{c}
\begin{array}{cc}
\omega_0^{\#1} & \omega_0^{\#1} \\
\omega_0^{\#1} \dagger & \omega_0^{\#1} \dagger \\
\omega_0^{\#1} \dagger & \omega_0^{\#1} \dagger
\end{array}
\begin{array}{cc}
6k^2(-r_1+r_3) & 0 \\
0 & 0
\end{array}
\end{array}
\end{array}$$

Source constraints/gauge generators	SO(3) irreps	Multiplicities
	$\sigma_0^{\#1} == 0$	1
	$\sigma_{1-}^{\#2\alpha} == 0$	3
	$\sigma_{1+}^{\#2\alpha\beta} == 0$	3
	$\sigma_{2+}^{\#1\alpha\beta} == 0$	5
	Total constraints:	12

	$\sigma_{0+}^{\#1}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1} \uparrow$	$\frac{1}{6k^2(-r_1+r_3)}$	0
$\sigma_{0-}^{\#1} \uparrow$	0	0

	$\sigma_{1^+}^{\#1} + \alpha\beta$	$\sigma_{1^+}^{\#2}$	$\sigma_{1^+}^{\#1} + \alpha\beta$	$\sigma_{1^+}^{\#1} + \alpha$	$\sigma_{1^+}^{\#2}$
$\sigma_{1^+}^{\#1} + \alpha\beta$	$\frac{1}{k^2(2r_3+r_5)}$	0	0	0	0
$\sigma_{1^+}^{\#2} + \alpha\beta$	0	0	0	0	0
$\sigma_{1^+}^{\#1} + \alpha$	0	0	$\frac{1}{k^2(-r_1+2r_3+r_5)}$	0	0
$\sigma_{1^+}^{\#2} + \alpha$	0	0	0	0	0

Massive and massless spectra



Quadratic pole	
Pole residue:	$\frac{1}{r_1 (r_1 - 2r_3 - r_5) (2r_3 + r_5)} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$r_1 < 0 \&\& (r_5 < r_1 - 2r_3 \parallel r_5 > -2r_3) \parallel r_1 > 0 \&\& -2r_3 < r_5 < r_1 - 2r_3$$