

	$\omega_{2^+}^{\#1} \alpha \beta$	$f_{2^+}^{\#1} \alpha \beta$	$\omega_{2^+}^{\#1} \alpha \beta \chi$
$\omega_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{\alpha_0}{4} + \beta_1$	$\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	0
$f_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	$2\beta_1 k^2$	0
$\omega_{2^+}^{\#1} \dagger \alpha \beta \chi$	0	0	$-\frac{\alpha_0}{4} + \beta_1$

Source constraints	
SO(3) irreps	#
$\tau_{0^+}^{\#2} == 0$	1
$\tau_{1^+}^{\#2\alpha} + 2ik \sigma_{1^+}^{\#2\alpha} == 0$	3
$\tau_{1^+}^{\#1\alpha} == 0$	3
$\tau_{1^+}^{\#1\alpha\beta} + ik \sigma_{1^+}^{\#2\alpha\beta} == 0$	3
Total #:	10

	$\sigma_{2^+}^{\#1} \alpha \beta$	$\tau_{2^+}^{\#1} \alpha \beta$	$\sigma_{2^+}^{\#1} \alpha \beta \chi$
$\sigma_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{16\beta_1}{\alpha_0^2-4\alpha_0\beta_1}$	$\frac{2i\sqrt{2}}{\alpha_0 k}$	0
$\tau_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{2i\sqrt{2}}{\alpha_0 k}$	$\frac{2}{\alpha_0 k^2}$	0
$\sigma_{2^+}^{\#1} \dagger \alpha \beta \chi$	0	0	$\frac{1}{-\frac{\alpha_0}{4} + \beta_1}$

Lagrangian density

$$-\frac{1}{2}\alpha_0\omega_{\alpha\chi\beta}\omega^{\alpha\beta\chi}-\frac{1}{2}\alpha_0\omega_{\alpha}^{\alpha\beta}\omega_{\beta\chi}^{\chi}+2\beta_1\omega_{\alpha}^{\alpha\beta}\omega_{\beta\chi}^{\chi}-2\beta_1\omega_{\chi\delta}^{\alpha}\omega_{\chi\delta}^{\alpha}-2\beta_1\omega_{\alpha\chi}^{\chi}\partial_{\beta}f^{\alpha\beta}-2\beta_1\omega_{\alpha}^{\delta}\partial_{\beta}f^{\alpha\beta}-\alpha_0f^{\alpha\beta}\partial_{\beta}\omega_{\alpha\chi}^{\chi}+\alpha_0\partial_{\beta}\omega_{\alpha}^{\alpha\beta}+2\beta_1\omega_{\beta\chi}^{\chi}\partial_{\beta}f_{\alpha}^{\alpha}+2\beta_1\omega_{\beta\delta}^{\delta}\partial^{\beta}f_{\alpha}^{\alpha}-2\beta_1\partial_{\beta}f^{\chi\chi}_{\alpha}+\alpha_0f^{\alpha\beta}\partial_{\chi}\omega_{\alpha\beta}^{\chi}-\alpha_0f_{\alpha}^{\alpha}\partial_{\chi}\omega^{\beta\chi}_{\beta}+4\beta_1\omega_{\alpha\chi\beta}\partial^{\chi}f^{\alpha\beta}+\beta_1\partial_{\chi}f_{\beta}^{\delta}\partial^{\chi}f_{\delta}^{\beta}+\beta_1\partial_{\chi}f_{\beta}^{\delta}\partial^{\chi}f_{\delta}^{\beta}+4\beta_1\partial^{\beta}f_{\alpha}^{\alpha}\partial_{\delta}f_{\beta}^{\delta}-2\beta_1\partial_{\beta}f_{\chi}^{\beta}\partial_{\delta}f^{\chi\delta}+\frac{2}{3}\alpha_6\partial_{\beta}\omega^{\alpha\beta}_{\alpha}\partial_{\delta}\omega^{\delta\delta}_{\chi}-\beta_1\partial^{\chi}f_{\zeta\delta}^{\delta}\partial^{\delta}f_{\chi}^{\delta}-\beta_1\partial^{\chi}f_{\zeta}^{\beta}\partial^{\delta}f_{\beta\chi}^{\delta}-\beta_1\partial^{\chi}f_{\chi\beta}^{\beta}+\beta_1\partial^{\chi}f_{\delta\zeta}^{\delta}\partial^{\delta}f_{\chi}^{\delta}$$

Added source term:

$$f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$$

	$\omega_{1^+}^{\#1} \alpha \beta$	$\omega_{1^+}^{\#2} \alpha \beta$	$f_{1^+}^{\#1} \alpha \beta$	$\omega_{1^+}^{\#1} \alpha$	$\omega_{1^+}^{\#2} \alpha$	$f_{1^+}^{\#1} \alpha$	$f_{1^+}^{\#2} \alpha$
$\omega_{1^+}^{\#1} \dagger \alpha \beta$	$\frac{1}{4}(\alpha_0-4\beta_1)$	$\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	$\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2} \dagger \alpha \beta$	$\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	0	0	0	0	0	0
$f_{1^+}^{\#1} \dagger \alpha \beta$	$-\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$	0	0	0	0	0	0
$\omega_{1^+}^{\#1} \dagger \alpha$	0	0	0	$\frac{1}{4}(\alpha_0-4\beta_1)$	$-\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	$-\frac{1}{2}i(\alpha_0-4\beta_1)k$	$-\frac{1}{2}i(\alpha_0-4\beta_1)k$
$\omega_{1^+}^{\#2} \dagger \alpha$	0	0	0	$-\frac{\alpha_0-4\beta_1}{2\sqrt{2}}$	0	0	0
$f_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$f_{1^+}^{\#2} \dagger \alpha$	0	0	0	$\frac{1}{2}i(\alpha_0-4\beta_1)k$	0	0	0

	$\omega_{0^+}^{\#1}$	$f_{0^+}^{\#1}$	$f_{0^+}^{\#2}$	$\omega_{0^+}^{\#1}$
$\omega_{0^+}^{\#1} \dagger$	$\frac{\alpha_0}{2}-2\beta_1+\alpha_6k^2$	$-\frac{i(\alpha_0-4\beta_1)k}{\sqrt{2}}$	0	0
$f_{0^+}^{\#1} \dagger$	$\frac{i(\alpha_0-4\beta_1)k}{\sqrt{2}}$	$-4\beta_1k^2$	0	0
$f_{0^+}^{\#2} \dagger$	0	0	0	0
$\omega_{0^+}^{\#1} \dagger$	0	0	0	$\frac{1}{2}(\alpha_0-4\beta_1)$

	$\sigma_{0^+}^{\#1}$	$\tau_{0^+}^{\#1}$	$\tau_{0^+}^{\#2}$	$\sigma_{0^+}^{\#1}$
$\sigma_{0^+}^{\#1} \dagger$	$\frac{8\beta_1}{\alpha_0^2-4\alpha_0\beta_1+8\alpha_6\beta_1k^2}$	$-\frac{i\sqrt{2}(\alpha_0-4\beta_1)}{\alpha_0(\alpha_0-4\beta_1)k+8\alpha_6\beta_1k^3}$	0	0
$\tau_{0^+}^{\#1} \dagger$	$\frac{i\sqrt{2}(\alpha_0-4\beta_1)}{\alpha_0(\alpha_0-4\beta_1)k+8\alpha_6\beta_1k^3}$	$-\frac{\alpha_0-4\beta_1+2\alpha_6k^2}{k^2(\alpha_0^2-4\alpha_0\beta_1+8\alpha_6\beta_1k^2)}$	0	0
$\tau_{0^+}^{\#2} \dagger$	0	0	0	0
$\sigma_{0^+}^{\#1} \dagger$	0	0	0	$\frac{2}{\alpha_0-4\beta_1}$

	$\sigma_{1^+}^{\#1} \alpha \beta$	$\sigma_{1^+}^{\#2} \alpha \beta$	$\tau_{1^+}^{\#1} \alpha \beta$	$\sigma_{1^+}^{\#1} \alpha$	$\sigma_{1^+}^{\#2} \alpha$	$\tau_{1^+}^{\#1} \alpha$	$\tau_{1^+}^{\#2} \alpha$
$\sigma_{1^+}^{\#1} \dagger \alpha \beta$	0	$\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+k^2)}$	$\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+k^2)}$	0	0	0	0
$\sigma_{1^+}^{\#2} \dagger \alpha \beta$	$\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+k^2)}$	$-\frac{2}{(\alpha_0-4\beta_1)(1+k^2)^2}$	$-\frac{2ik}{(\alpha_0-4\beta_1)(1+k^2)^2}$	0	0	0	0
$\tau_{1^+}^{\#1} \dagger \alpha \beta$	$-\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+k^2)}$	$\frac{2ik}{(\alpha_0-4\beta_1)(1+k^2)^2}$	$-\frac{2k^2}{(\alpha_0-4\beta_1)(1+k^2)^2}$	0	0	0	0
$\sigma_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	$-\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+2k^2)}$	0	$-\frac{4ik}{(\alpha_0-4\beta_1)(1+2k^2)}$
$\sigma_{1^+}^{\#2} \dagger \alpha$	0	0	0	$-\frac{2\sqrt{2}}{(\alpha_0-4\beta_1)(1+2k^2)}$	$-\frac{2}{(\alpha_0-4\beta_1)(1+2k^2)^2}$	0	$-\frac{2i\sqrt{2}k}{(\alpha_0-4\beta_1)(1+2k^2)^2}$
$\tau_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$\tau_{1^+}^{\#2} \dagger \alpha$	0	0	0	$-\frac{\alpha_0}{4} + \beta_1$	$\frac{1}{-\frac{\alpha_0}{4} + \beta_1}$	0	$-\frac{4k^2}{(\alpha_0-4\beta_1)(1+2k^2)^2}$

Massive particle	
Pole residue:	$\frac{1}{\alpha_0} + \frac{1}{\alpha_6} - \frac{1}{4\beta_1} > 0$
Polarisations:	1
Square mass:	$-\frac{\alpha_0(\alpha_0-4\beta_1)}{8\alpha_6\beta_1} > 0$
Spin:	0
Parity:	Even

Quadratic pole	
Pole residue:	$\frac{1}{\alpha_0} > 0$
Polarisations:	2

Unitarity conditions	
$\alpha_0 > 0 \ \&\& \ \alpha_6 > 0 \ \&\& \ \beta_1 < 0 \ \ \beta_1 > \frac{\alpha_0}{4}$	