

Particle spectrograph

Wave operator and propagator

Quadratic (free) action

$$\begin{aligned} S_F = & \iiint \left(\frac{1}{6} (4t_2 \omega_{\lambda'}^{\kappa\lambda} \omega_{\kappa\lambda'}^{\prime} + 2t_2 \omega_{\kappa\lambda}^{\prime} \omega_{\lambda'}^{\kappa\lambda} + 6f^{\alpha\beta} \tau_{\alpha\beta} + 6\omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 6r_5 \partial_{\lambda'} \omega^{\kappa\lambda}_{\kappa} \right. \\ & \partial'_{\lambda} \omega^{\alpha}_{\alpha} + 4r_2 \partial^{\beta} \omega^{\theta\alpha}_{\kappa} \partial_{\theta} \omega^{\kappa}_{\alpha\beta} - 2r_2 \partial_{\theta} \omega^{\kappa}_{\alpha\beta} \partial_{\kappa} \omega^{\alpha\beta\theta} - 4r_2 \partial_{\theta} \omega^{\kappa}_{\alpha\beta} \partial_{\kappa} \omega^{\theta\alpha\beta} - \\ & 6r_5 \partial_{\alpha} \omega^{\alpha}_{\theta} \partial_{\kappa} \omega^{\theta\kappa\lambda} + 6r_5 \partial_{\theta} \omega^{\alpha}_{\lambda} \partial_{\kappa} \omega^{\theta\kappa\lambda} - 6r_5 \partial_{\alpha} \omega^{\alpha}_{\lambda} \partial_{\theta} \omega^{\kappa\lambda\theta} + \\ & 12r_5 \partial_{\theta} \omega^{\alpha}_{\lambda} \partial_{\kappa} \omega^{\kappa\lambda\theta} + t_2 \partial^{\alpha} f_{\theta\kappa} \partial^{\kappa} f_{\alpha}^{\theta} - t_2 \partial^{\alpha} f_{\kappa\theta} \partial^{\kappa} f_{\alpha}^{\theta} + t_2 \partial^{\alpha} f_{\lambda}^{\theta} \partial^{\kappa} f_{\alpha}^{\lambda} + t_2 \partial^{\alpha} f_{\lambda}^{\theta} \partial^{\kappa} f_{\alpha}^{\lambda} + \\ & 2t_2 \omega_{\theta\kappa} \partial^{\kappa} f^{\theta}_{\lambda} - 4t_2 \omega_{\lambda\theta} \partial^{\kappa} f^{\theta}_{\kappa} - 2t_2 \omega_{\theta\kappa} \partial^{\kappa} f^{\theta}_{\lambda} + 4t_2 \omega_{\theta\kappa} \partial^{\kappa} f^{\theta}_{\lambda} - \\ & t_2 \partial^{\alpha} f_{\kappa}^{\lambda} \partial^{\kappa} f_{\lambda\alpha} - t_2 \partial_{\kappa} f_{\theta}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} + t_2 \partial_{\kappa} f_{\theta}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} + 2r_2 \partial_{\kappa} \omega^{\alpha\beta\theta} \partial^{\kappa} \omega_{\alpha\beta\theta} + \\ & 4r_2 \partial_{\kappa} \omega^{\theta\alpha\beta} \partial^{\kappa} \omega_{\alpha\beta\theta} - 4r_2 \partial^{\beta} \omega_{\lambda}^{\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} + 4r_2 \partial^{\beta} \omega_{\lambda}^{\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} + \\ & \left. 6r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\theta}^{\theta\kappa} - 6r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\alpha}^{\theta\kappa} \right) [t, x, y, z] dz dy dx dt \end{aligned}$$

| | $\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$ | $\tau_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{1-}^{\#1} \dagger^{\alpha}$ | $\sigma_{1-}^{\#2} \dagger^{\alpha}$ | $\tau_{1-}^{\#1} \dagger^{\alpha}$ | $\tau_{1-}^{\#2} \dagger^{\alpha}$ |
|---|---|--|---|--------------------------------------|--------------------------------------|------------------------------------|------------------------------------|
| $\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{1}{k^2 r_5}$ | $-\frac{\sqrt{2}}{k^2 r_5 + k^4 r_5}$ | $-\frac{i\sqrt{2}}{k r_5 + k^3 r_5}$ | 0 | 0 | 0 | 0 |
| $\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$ | $-\frac{\sqrt{2}}{k^2 r_5 + k^4 r_5}$ | $\frac{3k^2 r_5 + 2t_2}{(k+k^3)^2 r_5 t_2}$ | $\frac{i(3k^2 r_5 + 2t_2)}{k(1+k^2)^2 r_5 t_2}$ | 0 | 0 | 0 | 0 |
| $\tau_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{i\sqrt{2}}{k r_5 + k^3 r_5}$ | $-\frac{i(3k^2 r_5 + 2t_2)}{k(1+k^2)^2 r_5 t_2}$ | $\frac{3k^2 r_5 + 2t_2}{(1+k^2)^2 r_5 t_2}$ | 0 | 0 | 0 | 0 |
| $\sigma_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | $\frac{1}{k^2 r_5}$ | 0 | 0 | 0 |
| $\sigma_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

| | $\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1+}^{\#2} \dagger^{\alpha\beta}$ | $f_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1-}^{\#1} \dagger^{\alpha}$ | $\omega_{1-}^{\#2} \dagger^{\alpha}$ | $f_{1-}^{\#1} \dagger^{\alpha}$ | $f_{1-}^{\#2} \dagger^{\alpha}$ |
|---|---|---|--------------------------------------|--------------------------------------|--------------------------------------|---------------------------------|---------------------------------|
| $\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ | $k^2 r_5 + \frac{2t_2}{3}$ | $\frac{\sqrt{2} t_2}{3}$ | $\frac{1}{3} i \sqrt{2} k t_2$ | 0 | 0 | 0 | 0 |
| $\omega_{1+}^{\#2} \dagger^{\alpha\beta}$ | $\frac{\sqrt{2} t_2}{3}$ | $\frac{t_2}{3}$ | $\frac{i k t_2}{3}$ | 0 | 0 | 0 | 0 |
| $f_{1+}^{\#1} \dagger^{\alpha\beta}$ | $-\frac{1}{3} i \sqrt{2} k t_2$ | $-\frac{1}{3} i k t_2$ | $\frac{k^2 t_2}{3}$ | 0 | 0 | 0 | 0 |
| $\omega_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | $k^2 r_5$ | 0 | 0 | 0 |
| $\omega_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

$\omega_{0+}^{\#1} \dagger$ $f_{0+}^{\#1} \dagger$ $f_{0+}^{\#2} \dagger$ $\omega_{0-}^{\#1} \dagger$

| | | | | |
|-----------------------------|---|---|---|-----------------|
| $\omega_{0+}^{\#1} \dagger$ | 0 | 0 | 0 | 0 |
| $f_{0+}^{\#1} \dagger$ | 0 | 0 | 0 | 0 |
| $f_{0+}^{\#2} \dagger$ | 0 | 0 | 0 | 0 |
| $\omega_{0-}^{\#1} \dagger$ | 0 | 0 | 0 | $k^2 r_2 + t_2$ |

$\sigma_{0+}^{\#1} \dagger$ $\tau_{0+}^{\#1} \dagger$ $\tau_{0+}^{\#2} \dagger$ $\sigma_{0-}^{\#1} \dagger$

| | | | | |
|-----------------------------|---|---|---|---------------------------|
| $\sigma_{0+}^{\#1} \dagger$ | 0 | 0 | 0 | 0 |
| $\tau_{0+}^{\#1} \dagger$ | 0 | 0 | 0 | 0 |
| $\tau_{0+}^{\#2} \dagger$ | 0 | 0 | 0 | 0 |
| $\sigma_{0-}^{\#1} \dagger$ | 0 | 0 | 0 | $\frac{1}{k^2 r_2 + t_2}$ |

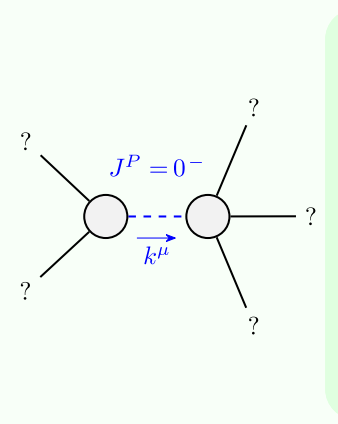
Source constraints/gauge generators

| SO(3) irreps | Multiplicities |
|--|----------------|
| $\tau_{0+}^{\#2} == 0$ | 1 |
| $\tau_{0+}^{\#1} == 0$ | 1 |
| $\sigma_{0+}^{\#1} == 0$ | 1 |
| $\tau_{1-}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1-}^{\#1\alpha} == 0$ | 3 |
| $\sigma_{1-}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#2\alpha\beta} == 0$ | 3 |
| $\sigma_{2-}^{\#1\alpha\beta\chi} == 0$ | 5 |
| $\tau_{2+}^{\#1\alpha\beta} == 0$ | 5 |
| $\sigma_{2+}^{\#1\alpha\beta} == 0$ | 5 |
| Total constraints: | 30 |

| | $\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ |
|---|---|---|---|
| $\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 | 0 | 0 |
| $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 | 0 | 0 |
| $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | 0 | 0 |

| | $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | $f_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ |
|---|---|--------------------------------------|---|
| $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 | 0 | 0 |
| $f_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 | 0 | 0 |
| $\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | 0 | 0 |

Massive and massless spectra



| Massive particle | |
|------------------|------------------------|
| Pole residue: | $-\frac{1}{r_2} > 0$ |
| Polarisations: | 1 |
| Square mass: | $-\frac{t_2}{r_2} > 0$ |
| Spin: | 0 |
| Parity: | Odd |

(No massless particles)

Unitarity conditions

$$r_2 < 0 \ \&\& \ t_2 > 0$$