

# Particle spectrograph

# Wave operator and propagator

$\sigma_1^{\#1} + \alpha\beta$	$\frac{1}{k^2(2r_1+r_5)}$	0	0	0	0	0
$\sigma_1^{\#2} + \alpha\beta$	0	0	0	0	0	0
$\tau_1^{\#1} + \alpha\beta$	0	0	0	0	0	0
$\sigma_1^{\#1} + \alpha$	0	0	$\frac{1}{k^2(r_1+r_5)}$	$\frac{\sqrt{2}}{k^2(1+2k^2)(r_1+r_5)}$	0	$\frac{2i}{k(1+2k^2)(r_1+r_5)}$
$\sigma_1^{\#2} + \alpha$	0	0	$\frac{\sqrt{2}}{k^2(1+2k^2)(r_1+r_5)}$	$\frac{3k^2(r_1+r_5)+2t_3}{(k+2k^2)^2(r_1+r_5)t_3}$	0	$\frac{i\sqrt{2}(3k^2(r_1+r_5)+2t_3)}{k(1+2k^2)^2(r_1+r_5)t_3}$
$\tau_1^{\#1} + \alpha$	0	0	0	0	0	0
$\tau_1^{\#2} + \alpha$	0	0	$-\frac{2i}{k(1+2k^2)(r_1+r_5)}$	$-\frac{i\sqrt{2}(3k^2(r_1+r_5)+2t_3)}{k(1+2k^2)^2(r_1+r_5)t_3}$	0	$\frac{6k^2(r_1+r_5)+4t_3}{(1+2k^2)^2(r_1+r_5)t_3}$

$\omega_1^{\#1} + \alpha\beta$	$k^2(2r_1 + r_5)$	0	0	0	0	0
$\omega_1^{\#2} + \alpha\beta$	0	0	0	0	0	0
$f_1^{\#1} + \alpha\beta$	0	0	0	0	0	0
$\omega_1^{\#1} + \alpha$	0	0	$k^2(r_1 + r_5) + \frac{2t_3}{3}$	$-\frac{\sqrt{2}t_3}{3}$	0	$-\frac{2}{3}i\sqrt{2}kt_3$
$\omega_1^{\#2} + \alpha$	0	0	$-\frac{\sqrt{2}t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_3$
$f_1^{\#1} + \alpha$	0	0	0	0	0	0
$f_1^{\#2} + \alpha$	0	0	$\frac{2ikt_3}{3}$	$-\frac{1}{3}i\sqrt{2}kt_3$	0	$\frac{2k^2t_3}{3}$

## Quadratic (free) action

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$$\iiint (\frac{1}{3}(-2t_3\omega_{\alpha}^{\alpha i}\omega_{\alpha}^{\kappa}+3f^{\alpha\beta}\tau_{\alpha\beta}^{\kappa}+3\omega_{\alpha\beta}^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}^{\kappa}+4t_3\omega_{\alpha}^{\kappa}\partial_{\chi}f^{\alpha i}-4t_3\omega_{\alpha}^{\kappa}\partial_{\chi}f^{\alpha i}))$$

$$\partial' f_{\alpha}^{\alpha} + 2 t_3 \partial_{\kappa} f_{\kappa}^{\kappa} \partial' f_{\alpha}^{\alpha} - 4 r_1 \partial_{\beta} \omega_{\alpha \theta} \partial^{\theta} \omega^{\alpha \beta} + 2 r_1 \partial_{\beta} \omega_{\alpha \theta} \partial^{\theta} \omega^{\alpha \beta} -$$

$$8r_1\partial_\beta\omega_{,A\sigma}\partial^\theta\omega^{\alpha\beta_1}-2r_1\partial_1\omega_{\sigma B A}\partial^\theta\omega^{\alpha\beta_1}+2r_1\partial_\theta\omega_{\sigma B_1}\partial^\theta\omega^{\alpha\beta_1}+$$

$$2r_1\partial_\theta\omega_{\alpha\beta}\partial^\theta\omega^{\alpha\beta}+3r_5\partial_\mu\omega^\kappa_\kappa\partial^\theta\omega^{\alpha\iota}-3r_5\partial_\theta\omega^\kappa_\kappa\partial^\theta\omega^{\alpha\iota}+$$

$$2t_3\partial_{\theta'}f^{\alpha\theta}\partial_{\kappa}f^{\kappa}-4t_3\partial'f^{\alpha}\partial_{\kappa}f^{\kappa}-3r_5\partial_{\alpha}\omega^{\alpha\theta}\partial_{\kappa}\omega'_{\theta}{}^{\kappa}+6r_5\partial^{\theta}\omega^{\alpha\theta}\partial_{\kappa}\omega'_{\theta}{}^{\kappa}+$$

$$3r_5\partial_\alpha\omega^{\alpha i\theta}\partial_\kappa\omega_{\theta'}^\kappa-6r_5\partial^\theta\omega_{\alpha'}^{\alpha i}\partial_\kappa\omega_{\theta'}^\kappa)) [t,x,y,z]dzdydxdt$$

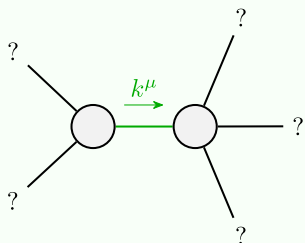
Source constraints/gauge generators	SO(3) irreps	Multiplicities
	$\sigma_0^{\#1} == 0$	1
	$\tau_{0+}^{\#2} == 0$	1
	$\tau_{0+}^{\#1} - 2ik\sigma_{0+}^{\#1} == 0$	1
	$\tau_{1-}^{\#2\alpha} + 2ik\sigma_{1-}^{\#2\alpha} == 0$	3
	$\tau_{1-}^{\#1\alpha} == 0$	3
	$\tau_{1+}^{\#1\alpha\beta} == 0$	3
	$\sigma_{1+}^{\#2\alpha\beta} == 0$	3
	$\tau_{2+}^{\#1\alpha\beta} == 0$	5
	$\sigma_{2+}^{\#1\alpha\beta} == 0$	5
	Total constraints:	25

	$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1} \dagger$	$\frac{1}{(1+2k^2)^2 t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	0	0
$\tau_{0+}^{\#1} \dagger$	$\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	$\frac{2k^2}{(1+2k^2)^2 t_3}$	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0	0
$\sigma_{0-}^{\#1} \dagger$	0	0	0	0

	$\sigma_{2^+}^{\#1} \tau_{2^+}^{\#1} \sigma_{2^+}^{\#1}$	$\tau_{2^+}^{\#1} \sigma_{2^+}^{\#1} \tau_{2^+}^{\#1}$	$\sigma_{2^+}^{\#1} \tau_{2^+}^{\#1} \sigma_{2^+}^{\#1}$
$\sigma_{2^+}^{\#1} \tau_{2^+}^{\#1} \sigma_{2^+}^{\#1}$	0	0	0
$\tau_{2^+}^{\#1} \sigma_{2^+}^{\#1} \tau_{2^+}^{\#1}$	0	0	0
$\sigma_{2^+}^{\#1} \tau_{2^+}^{\#1} \sigma_{2^+}^{\#1}$	0	0	$\frac{1}{k^2 r_1}$

	$\omega_0^{\#1} \dagger$	$f_0^{\#1}$	$f_0^{\#2}$	$\omega_0^{\#1}$
$\omega_0^{\#1} \dagger$	$t_3$	$-i\sqrt{2}kt_3$	0	0
$f_0^{\#1} \dagger$	$i\sqrt{2}kt_3$	$2k^2t_3$	0	0
$f_0^{\#2} \dagger$	0	0	0	0
$\omega_0^{\#1} \dagger$	0	0	0	0

# Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{r_1(r_1+r_5)(2r_1+r_5)p^2} > 0$
Polarisations:	2

(No massive particles)

# Unitarity conditions

$$r_1 < 0 \&\& (r_5 < -r_1 \parallel r_5 > -2r_1) \parallel r_1 > 0 \&\& -2r_1 < r_5 < -r_1$$