

	$\sigma_{1^+}^{\#1} \dagger \alpha \beta$	$\sigma_{1^+}^{\#2} \dagger \alpha \beta$	$\tau_{1^+}^{\#1} \dagger \alpha \beta$	$\sigma_{1^-}^{\#1} \dagger \alpha$	$\sigma_{1^-}^{\#2} \dagger \alpha$	$\tau_{1^-}^{\#1} \dagger \alpha$	$\tau_{1^-}^{\#2} \dagger \alpha$
$\sigma_{1^+}^{\#1} \dagger \alpha \beta$	0	$\frac{2 \sqrt{2}}{(\alpha_0-4 \beta_1)(1+k^2)}$	$\frac{2 i \sqrt{2} k}{(\alpha_0-4 \beta_1)(1+k^2)}$	0	0	0	0
$\sigma_{1^+}^{\#2} \dagger \alpha \beta$	$\frac{2 \sqrt{2}}{(\alpha_0-4 \beta_1)(1+k^2)}$	$-\frac{2}{(\alpha_0-4 \beta_1)(1+k^2)^2}$	$-\frac{2 i k}{(\alpha_0-4 \beta_1)(1+k^2)^2}$	0	0	0	0
$\tau_{1^+}^{\#1} \dagger \alpha \beta$	$-\frac{2 i \sqrt{2} k}{(\alpha_0-4 \beta_1)(1+k^2)}$	$\frac{2 i k}{(\alpha_0-4 \beta_1)(1+k^2)^2}$	$-\frac{2 k^2}{(\alpha_0-4 \beta_1)(1+k^2)^2}$	0	0	0	0
$\sigma_{1^-}^{\#1} \dagger \alpha$	0	0	0	0	$-\frac{2 \sqrt{2}}{(\alpha_0-4 \beta_1)(1+2 k^2)}$	0	$-\frac{4 i k}{(\alpha_0-4 \beta_1)(1+2 k^2)}$
$\sigma_{1^-}^{\#2} \dagger \alpha$	0	0	0	$-\frac{2 \sqrt{2}}{(\alpha_0-4 \beta_1)(1+2 k^2)}$	$-\frac{2}{(\alpha_0-4 \beta_1)(1+2 k^2)^2}$	0	$-\frac{2 i \sqrt{2} k}{(\alpha_0-4 \beta_1)(1+2 k^2)^2}$
$\tau_{1^-}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$\tau_{1^-}^{\#2} \dagger \alpha$	0	0	0	$\frac{4 i k}{(\alpha_0-4 \beta_1)(1+2 k^2)}$	$\frac{2 i \sqrt{2} k}{(\alpha_0-4 \beta_1)(1+2 k^2)^2}$	0	$-\frac{4 k^2}{(\alpha_0-4 \beta_1)(1+2 k^2)^2}$

### Lagrangian density

$$\begin{aligned}
 &-\frac{1}{2} \alpha_0 \omega_{\alpha \chi \beta} \omega^{\alpha \beta \chi}-\frac{1}{2} \alpha_0 \omega^{\alpha \beta}{}_{\alpha} \omega_{\beta}^{\chi}{}_{\chi}+2 \beta_1 \omega^{\alpha \beta}{}_{\alpha} \omega_{\beta}^{\chi}{}_{\chi}- \\
 &2 \beta_1 \omega_{\alpha}^{\chi \delta} \omega_{\chi \delta}^{\alpha}-2 \beta_1 \omega_{\alpha}^{\chi}{}_{\chi} \partial_{\beta} f^{\alpha \beta}-2 \beta_1 \omega_{\alpha}^{\delta}{}_{\delta} \partial_{\beta} f^{\alpha \beta}- \\
 &\alpha_0 f^{\alpha \beta} \partial_{\beta} \omega_{\alpha}^{\chi}{}_{\chi}+\alpha_0 \partial_{\beta} \omega^{\alpha \beta}{}_{\alpha}+2 \beta_1 \omega_{\beta}^{\chi}{}_{\chi} \partial^{\beta} f^{\alpha}{}_{\alpha}+2 \beta_1 \omega_{\beta}^{\delta}{}_{\delta} \partial^{\beta} f^{\alpha}{}_{\alpha}- \\
 &2 \beta_1 \partial_{\beta} f^{\chi}{}_{\chi} \partial^{\beta} f^{\alpha}{}_{\alpha}+\alpha_0 f^{\alpha \beta} \partial_{\chi} \omega_{\alpha}^{\chi}{}_{\beta}-\alpha_0 f^{\alpha}{}_{\alpha} \partial_{\chi} \omega^{\beta \chi}{}_{\beta}+ \\
 &4 \beta_1 \omega_{\alpha \chi \beta} \partial^{\chi} f^{\alpha \beta}+\beta_1 \partial_{\chi} f_{\beta}^{\delta} \partial^{\chi} f_{\delta}^{\beta}+\beta_1 \partial_{\chi} f_{\beta}^{\delta} \partial^{\chi} f_{\delta}^{\beta}+ \\
 &4 \beta_1 \partial^{\beta} f^{\alpha}{}_{\alpha} \partial_{\delta} f_{\beta}^{\delta}-2 \beta_1 \partial_{\beta} f_{\chi}^{\beta} \partial_{\delta} f^{\chi \delta}+\frac{2}{3} \alpha_6 \partial_{\beta} \omega^{\alpha \beta}{}_{\alpha} \partial_{\delta} \omega^{\chi \delta}{}_{\chi}- \\
 &\beta_1 \partial^{\chi} f_{\zeta}^{\beta} \partial^{\zeta} f_{\beta \chi}-\beta_1 \partial^{\chi} f_{\zeta}^{\beta} \partial^{\zeta} f_{\chi \beta}+\beta_1 \partial^{\chi} f_{\delta \zeta} \partial^{\zeta} f^{\delta}{}_{\chi}-\beta_1 \partial^{\chi} f_{\zeta \delta} \partial^{\zeta} f^{\delta}{}_{\chi}
 \end{aligned}$$

$$\text{Added source term: } \left| f^{\alpha \beta} \tau_{\alpha \beta}+\omega^{\alpha \beta \chi} \sigma_{\alpha \beta \chi} \right.$$

	$\omega_{2^+}^{\#1} \dagger \alpha \beta$	$f_{2^+}^{\#1} \dagger \alpha \beta$	$\omega_{2^-}^{\#1} \dagger \alpha \beta \chi$
$\omega_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{\alpha_0}{4}+\beta_1$	$\frac{i\left(\alpha_0-4 \beta_1\right) k}{2 \sqrt{2}}$	0
$f_{2^+}^{\#1} \dagger \alpha \beta$	$\frac{i\left(\alpha_0-4 \beta_1\right) k}{2 \sqrt{2}}$	$2 \beta_1 k^2$	0
$\omega_{2^-}^{\#1} \dagger \alpha \beta \chi$	$-\frac{\alpha_0}{4}+\beta_1$	0	0

	$\omega_{1^+}^{\#1} \dagger \alpha \beta$	$\omega_{1^+}^{\#2} \dagger \alpha \beta$	$f_{1^+}^{\#1} \dagger \alpha \beta$	$\omega_{1^-}^{\#1} \dagger \alpha$	$\omega_{1^-}^{\#2} \dagger \alpha$	$f_{1^-}^{\#1} \dagger \alpha$	$f_{1^-}^{\#2} \dagger \alpha$
$\omega_{1^+}^{\#1} \dagger \alpha \beta$	$\frac{1}{4}\left(\alpha_0-4 \beta_1\right)$	$\frac{\alpha_0-4 \beta_1}{2 \sqrt{2}}$	$\frac{i\left(\alpha_0-4 \beta_1\right) k}{2 \sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2} \dagger \alpha \beta$	$\frac{\alpha_0-4 \beta_1}{2 \sqrt{2}}$	0	0	$-\frac{\alpha_0-4 \beta_1}{2 \sqrt{2}}$	0	0	0
$f_{1^+}^{\#1} \dagger \alpha \beta$	$-\frac{i\left(\alpha_0-4 \beta_1\right) k}{2 \sqrt{2}}$	0	0	0	0	0	0
$\omega_{1^-}^{\#1} \dagger \alpha$	0	0	0	$\frac{1}{4}\left(\alpha_0-4 \beta_1\right)$	0	0	0
$\omega_{1^-}^{\#2} \dagger \alpha$	0	0	0	$-\frac{\alpha_0-4 \beta_1}{2 \sqrt{2}}$	0	0	0
$f_{1^-}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$f_{1^-}^{\#2} \dagger \alpha$	0	0	0	$\frac{1}{2} i\left(\alpha_0-4 \beta_1\right) k$	0	0	0

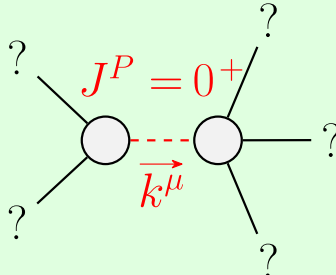
	$\sigma_{0^+}^{\#1}$	$\tau_{0^+}^{\#1}$	$\tau_{0^+}^{\#2}$	$\sigma_{0^-}^{\#1}$
$\sigma_{0^+}^{\#1} \dagger$	$\frac{8 \beta_1}{\alpha_0^2-4 \alpha_0 \beta_1+8 \alpha_6 \beta_1 k^2}$	$-\frac{i \sqrt{2}\left(\alpha_0-4 \beta_1\right)}{\alpha_0\left(\alpha_0-4 \beta_1\right) k+8 \alpha_6 \beta_1 k^3}$	0	0
$\tau_{0^+}^{\#1} \dagger$	$\frac{i \sqrt{2}\left(\alpha_0-4 \beta_1\right)}{\alpha_0\left(\alpha_0-4 \beta_1\right) k+8 \alpha_6 \beta_1 k^3}$	$-\frac{\alpha_0-4 \beta_1+2 \alpha_6 k^2}{k^2\left(\alpha_0^2-4 \alpha_0 \beta_1+8 \alpha_6 \beta_1 k^2\right)}$	0	0
$\tau_{0^+}^{\#2} \dagger$	0	0	0	0
$\sigma_{0^-}^{\#1} \dagger$	0	0	0	$\frac{2}{\alpha_0-4 \beta_1}$

	$\omega_{0^+}^{\#1} \dagger$	$f_{0^+}^{\#1} \dagger$	$f_{0^+}^{\#2} \dagger$	$\omega_{0^-}^{\#1} \dagger$
$\omega_{0^+}^{\#1} \dagger$	$\frac{\alpha_0}{2}-2 \beta_1+\alpha_6 k^2$	$-\frac{i\left(\alpha_0-4 \beta_1\right) k}{\sqrt{2}}$	0	0
$f_{0^+}^{\#1} \dagger$	$\frac{i\left(\alpha_0-4 \beta_1\right) k}{\sqrt{2}}$	$-4 \beta_1 k^2$	0	0
$f_{0^+}^{\#2} \dagger$	0	0	0	0
$\omega_{0^-}^{\#1} \dagger$	0	0	0	$\frac{1}{2}\left(\alpha_0-4 \beta_1\right)$

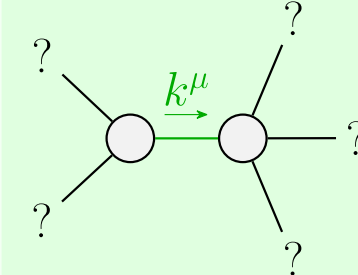
	$\sigma_{2^+}^{\#1} \dagger \alpha \beta$	$\tau_{2^+}^{\#1} \dagger \alpha \beta$	$\sigma_{2^-}^{\#1} \dagger \alpha \beta \chi$
$\sigma_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{16 \beta_1}{\alpha_0^2-4 \alpha_0 \beta_1}$	$\frac{2 i \sqrt{2}}{\alpha_0 k}$	0
$\tau_{2^+}^{\#1} \dagger \alpha \beta$	$-\frac{2 i \sqrt{2}}{\alpha_0 k}$	$\frac{2}{\alpha_0 k^2}$	0
$\sigma_{2^-}^{\#1} \dagger \alpha \beta \chi$	0	0	$\frac{1}{-\frac{\alpha_0}{4}+\beta_1}$

### Source constraints

SO(3) irreps	#
$\tau_{0^+}^{\#2}==0$	1
$\tau_{1^-}^{\#2 \alpha}+2 i k \sigma_{1^-}^{\#2 \alpha}==0$	3
$\tau_{1^-}^{\#1 \alpha}==0$	3
$\tau_{1^+}^{\#1 \alpha \beta}+i k \sigma_{1^+}^{\#2 \alpha \beta}==0$	3
Total #:	10



Massive particle	
Pole residue:	$\frac{1}{\alpha_0}+\frac{1}{\alpha_6}-\frac{1}{4 \beta_1}>0$
Polarisations:	1
Square mass:	$-\frac{\alpha_0\left(\alpha_0-4 \beta_1\right)}{8 \alpha_6 \beta_1}>0$
Spin:	0
Parity:	Even



Quadratic pole	
Pole residue:	$\frac{1}{\alpha_0}>0$
Polarisations:	2

### Unitarity conditions

$$\alpha_0>0 \ \&\& \ \alpha_6>0 \ \&\& \ \beta_1<0 \ || \ \beta_1>\frac{\alpha_0}{4}$$