

Particle spectrograph

Wave operator and propagator

Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\tau_{0+}^{\#2} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == 0$	1
$\tau_{0+}^{\#1} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == \partial_\beta \partial^\beta \tau^\alpha_\alpha$	1
$\sigma_{0+}^{\#1} == 0$	$\partial_\beta \sigma^{\alpha\beta}_\alpha == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha_\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\alpha\beta}$	3
$\tau_{1-}^{\#1\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha_\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\beta\alpha}$	3
$\sigma_{1-}^{\#2\alpha} == 0$	$\partial_\chi \partial_\beta \sigma^{\alpha\beta\chi} = 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#1\alpha\beta} == 0$	$\partial_\chi \partial^\alpha \tau^{\beta\chi} + \partial_\chi \partial^\beta \tau^{\chi\alpha} + \partial_\chi \partial^\chi \tau^{\alpha\beta} + \partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\beta\chi\alpha} == \partial_\chi \partial^\alpha \tau^{\chi\beta} + \partial_\chi \partial^\beta \tau^{\alpha\chi} + \partial_\chi \partial^\chi \tau^{\beta\alpha} + \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta}$	3
$\sigma_{1+}^{\#1\alpha\beta} == \sigma_{1+}^{\#2\alpha\beta}$	$3 \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} + 2 \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\beta\chi} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta} == 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \sigma^{\alpha\chi\delta} + \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \sigma^{\beta\delta\chi} + 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \sigma^{\beta\delta\alpha}$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	$3 \partial_\epsilon \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\delta\epsilon} + 3 \partial_\epsilon \partial^\epsilon \partial_\chi \partial^\alpha \sigma^{\beta\delta}_\delta + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\chi\delta} + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\chi} + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\chi\delta\alpha} + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\beta} + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\beta} + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\beta} + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\beta} + 3 \eta^{\beta\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\delta\epsilon}_\delta + 3 \eta^{\alpha\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\beta\delta\epsilon} + 3 \eta^{\beta\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\alpha\delta}_\delta == 3 \partial_\epsilon \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\delta\epsilon} + 3 \partial_\epsilon \partial^\epsilon \partial_\chi \partial^\alpha \sigma^{\beta\delta}_\delta + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\chi\delta} + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\chi} + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\chi\delta\beta} + 2 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\beta\delta\alpha} + 4 \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\beta \sigma^{\alpha\delta\beta} + 3 \eta^{\alpha\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\delta\epsilon}_\delta + 3 \eta^{\beta\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\alpha\delta\epsilon} + 3 \eta^{\alpha\chi} \partial_\mu \partial^\mu \partial_\epsilon \partial^\epsilon \sigma^{\beta\delta}_\delta$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	$4 \partial_\delta \partial_\chi \partial^\beta \partial^\alpha \tau^{\chi\delta} + 2 \partial_\delta \partial^\delta \partial_\beta \partial^\alpha \tau^{\chi}_\chi + 3 \partial_\delta \partial^\delta \partial_\chi \tau^{\alpha\beta} + 3 \partial_\delta \partial^\delta \partial_\chi \tau^{\alpha\beta} + 3 \partial_\delta \partial^\delta \partial_\chi \tau^{\beta\alpha} + 2 \eta^{\alpha\beta} \partial_\epsilon \partial^\epsilon \partial_\delta \tau^{\chi\delta} == 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\beta\chi} + 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\chi\beta} + 3 \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\chi\alpha} + 2 \eta^{\alpha\beta} \partial_\epsilon \partial^\epsilon \partial_\delta \tau^{\chi}_\chi$	5
Total constraints/gauge generators:		28

Quadratic (free) action

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$$\begin{aligned} & \iiint \iiint \Big( 6 \, f^{\alpha\beta} \, \tau_{\alpha\beta} + 6 \, \omega^{\alpha\beta\chi} \, \sigma_{\alpha\beta\chi} - 15 \, r_3 \, \partial_\beta \omega_{\phantom{\beta} \, \theta}^{\phantom{\beta} \, \theta} \partial_\epsilon \omega^{\alpha\beta}_\alpha + 9 \, r_3 \, \partial_\epsilon \omega_{\phantom{\beta} \, \theta}^{\phantom{\beta} \, \theta} \partial_\epsilon \omega^{\alpha\beta}_\alpha + \\ & 9 \, r_3 \, \partial_\alpha \omega^{\alpha\beta\iota} \partial_\theta \omega_{\phantom{\beta} \, \beta}^{\phantom{\beta} \, \theta} - 18 \, r_3 \, \partial^\iota \omega_{\phantom{\beta} \, \beta}^{\alpha\beta} \partial_\alpha \partial_\theta \omega_{\phantom{\beta} \, \beta}^{\phantom{\beta} \, \theta} - \\ & 15 \, r_3 \, \partial_\alpha \omega^{\alpha\beta\iota} \partial_\theta \omega_{\phantom{\beta} \, \beta}^{\phantom{\beta} \, \theta} + 30 \, r_3 \, \partial^\iota \omega_{\phantom{\beta} \, \beta}^{\alpha\beta} \partial_\alpha \partial_\theta \omega_{\phantom{\beta} \, \beta}^{\phantom{\beta} \, \theta} + \\ & 4 \, t_2 \, \omega_{\phantom{\beta} \, \theta} \partial_\alpha \partial^\beta f^{\alpha\iota} + t_2 \, \partial_\epsilon \partial^\epsilon f_{\phantom{\beta} \, \alpha}^{\alpha\iota} \partial_\beta \partial^\beta f^{\alpha\iota} - t_2 \, \partial_\alpha \partial^\epsilon f_{\phantom{\beta} \, \alpha}^{\alpha\iota} \partial_\beta \partial^\beta f^{\alpha\iota} - \\ & t_2 \, \partial_\epsilon \partial^\epsilon f_{\phantom{\beta} \, \alpha}^{\alpha\iota} \partial_\beta \partial^\beta f^{\alpha\iota} + t_2 \, \partial_\epsilon \partial^\epsilon f_{\phantom{\beta} \, \alpha}^{\alpha\iota} \partial_\beta \partial^\beta f^{\alpha\iota} - t_2 \, \partial_\epsilon \partial^\epsilon f_{\phantom{\beta} \, \alpha}^{\alpha\iota} \partial_\beta \partial^\beta f^{\alpha\iota} - \\ & 4 \, t_2 \, \omega_{\alpha\theta\iota} \, (\omega^{\alpha\iota\theta} + \partial^\theta f^{\alpha\iota}) + 2 \, t_2 \, \omega_{\alpha\theta} \, (\omega^{\alpha\iota\theta} + \partial^\theta f^{\alpha\iota}) + \\ & 8 \, r_2 \, \partial_\beta \omega_{\alpha\theta} \partial^\theta \omega^{\alpha\beta\iota} - 4 \, r_2 \, \partial_\beta \omega_{\alpha\theta\iota} \partial^\theta \omega^{\alpha\beta\iota} + \\ & 4 \, r_2 \, \partial_\beta \omega_{\phantom{\beta} \, \theta} \partial^\theta \omega_{\phantom{\beta} \, \theta}^{\alpha\beta\iota} - 24 \, r_3 \, \partial_\beta \omega_{\phantom{\beta} \, \theta} \partial^\theta \omega_{\phantom{\beta} \, \theta}^{\alpha\beta\iota} - \\ & 2 \, r_2 \, \partial_\epsilon \omega_{\alpha\beta\theta} \partial^\theta \omega^{\alpha\beta\iota} + 2 \, r_2 \, \partial_\theta \omega_{\alpha\beta\iota} \partial^\theta \omega^{\alpha\beta\iota} - \\ & 4 \, r_2 \, \partial_\theta \omega_{\alpha\beta} \partial^\theta \omega^{\alpha\beta\iota}) ] [t, x, y, z] d z d y d x d t \end{aligned}$$

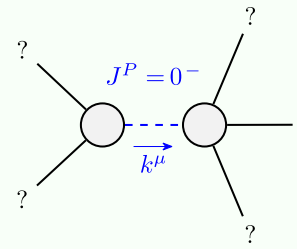
$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1-}^{\#1} \dagger^{\alpha}$	$\omega_{1-}^{\#2} \dagger^{\alpha}$	$f_{1-}^{\#1} \dagger^{\alpha}$	$f_{1-}^{\#2} \dagger^{\alpha}$
$\frac{2t_2}{3}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0	0
$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0	0
$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{1}{3}i\sqrt{2}kt_2$	$\frac{k^2t_2}{3}$	0	0	0	0
$\omega_{1-}^{\#1} \dagger^{\alpha}$	0	0	$-\frac{3k^2r_3}{2}$	0	0	0
$\omega_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{\#1} \dagger^{\alpha}$	$\sigma_{1-}^{\#2} \dagger^{\alpha}$	$\tau_{1-}^{\#1} \dagger^{\alpha}$	$\tau_{1-}^{\#2} \dagger^{\alpha}$
$\frac{6}{(3+k^2)^2t_2}$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{3\sqrt{2}}{(3+k^2)^2t_2}$	$\frac{3ik}{(3+k^2)^2t_2}$	0	0	0	0
$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$	$-\frac{3k^2}{(3+k^2)^2t_2}$	0	0	0	0
$\sigma_{1-}^{\#1} \dagger^{\alpha}$	0	0	$-\frac{2}{3k^2r_3}$	0	0	0
$\sigma_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0

$\sigma_{0+}^{\#1} \dagger$	$\tau_{0+}^{\#1} \dagger$	$\tau_{0+}^{\#2} \dagger$	$\sigma_{0-}^{\#1} \dagger$
0	0	0	0
$\tau_{0+}^{\#1} \dagger$	0	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0
$\sigma_{0-}^{\#1} \dagger$	0	0	$\frac{1}{k^2r_2+t_2}$

$\omega_{0+}^{\#1} \dagger$	$f_{0+}^{\#1} \dagger$	$f_{0+}^{\#2} \dagger$	$\omega_{0-}^{\#1} \dagger$
0	0	0	0
$f_{0+}^{\#1} \dagger$	0	0	0
$f_{0+}^{\#2} \dagger$	0	0	0
$\omega_{0-}^{\#1} \dagger$	0	0	$k^2r_2+t_2$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

No massless particles

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$