

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\frac{1}{k^2 (2r_1+r_5)}$	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	$\frac{1}{k^2 (r_1+r_5)}$	$\frac{\sqrt{2}}{k^2 (1+2k^2) (r_1+r_5)}$	0	$\frac{2i}{k (1+2k^2) (r_1+r_5)}$
0	0	$\frac{\sqrt{2}}{k^2 (1+2k^2) (r_1+r_5)}$	$\frac{3k^2 (r_1+r_5)+2t_3}{(k+2k^3)^2 (r_1+r_5) t_3}$	0	$\frac{i\sqrt{2} (3k^2 (r_1+r_5)+2t_3)}{k (1+2k^2)^2 (r_1+r_5) t_3}$
0	0	0	0	0	0
0	0	$-\frac{2i}{k (1+2k^2) (r_1+r_5)}$	$-\frac{i\sqrt{2} (3k^2 (r_1+r_5)+2t_3)}{k (1+2k^2)^2 (r_1+r_5) t_3}$	0	$\frac{6k^2 (r_1+r_5)+4t_3}{(1+2k^2)^2 (r_1+r_5) t_3}$

Quadratic (free) action

$$\begin{aligned} S_F = & \iiint \left(\frac{1}{3} (2t_3 \omega_{\lambda}^{\alpha\prime} \omega_{\kappa\alpha}^{\kappa} + 3 f^{\alpha\beta} \tau_{\alpha\beta} - 3 r_5 \partial_{\lambda} \omega_{\kappa\lambda}^{\kappa\lambda} \partial_{\lambda} \omega_{\lambda}^{\alpha} - 2 r_1 \partial^{\beta} \omega_{\kappa}^{\theta\alpha} \partial_{\theta} \omega_{\alpha\beta}^{\kappa} - 2 r_1 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \partial_{\kappa} \omega^{\alpha\beta\theta} + 2 r_1 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \partial_{\kappa} \omega^{\theta\alpha\beta} - 3 r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda\theta} - \right. \\ & \left. \partial_{\kappa} \omega^{\theta\kappa\lambda} + 3 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega_{\alpha}^{\theta\kappa\lambda} - 3 r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\kappa\lambda\theta} + 6 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda\theta} - \right. \\ & 2 t_3 \omega_{\kappa\alpha}^{\alpha} \partial^{\kappa} f_{\lambda}^{\prime} - 2 t_3 \omega_{\kappa\lambda}^{\lambda} \partial^{\kappa} f_{\lambda}^{\prime} - 4 t_3 \partial^{\alpha} f_{\kappa\alpha} \partial^{\kappa} f_{\lambda}^{\prime} + 2 t_3 \partial_{\lambda} f_{\lambda}^{\lambda} \partial^{\kappa} f_{\lambda}^{\prime} + \\ & 2 t_3 \omega_{\lambda\alpha}^{\alpha} \partial^{\kappa} f_{\kappa}^{\lambda} + 2 t_3 \omega_{\lambda\alpha}^{\lambda} \partial^{\kappa} f_{\kappa}^{\lambda} + 2 t_3 \partial^{\alpha} f_{\alpha}^{\lambda} \partial^{\kappa} f_{\lambda\kappa} + 2 r_1 \partial_{\kappa} \omega^{\alpha\beta\theta} \partial^{\kappa} \omega_{\alpha\beta\theta} - \\ & 2 r_1 \partial_{\kappa} \omega^{\theta\alpha\beta} \partial^{\kappa} \omega_{\alpha\beta\theta} + 2 r_1 \partial^{\beta} \omega_{\lambda}^{\alpha\lambda} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} - 8 r_1 \partial^{\beta} \omega_{\lambda}^{\lambda\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} + \\ & \left. 3 r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\theta}^{\theta\kappa} - 3 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\alpha}^{\theta\kappa} \right) [t, x, y, z] dz dy dx dt \end{aligned}$$

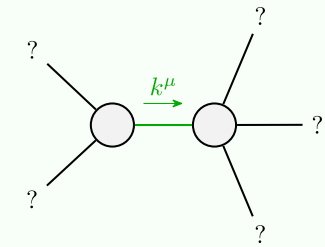
$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#1} \alpha\beta$	$\omega_{1+}^{\#2} f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1-}^{\#1} \alpha$	$\omega_{1-}^{\#2} \alpha$	$f_{1-}^{\#1} \alpha$	$f_{1-}^{\#2} \alpha$
$k^2 (2r_1+r_5)$	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	$k^2 (r_1+r_5) + \frac{2t_3}{3}$	$-\frac{\sqrt{2} t_3}{3}$	0	$-\frac{2}{3} i k t_3$
0	0	0	$-\frac{\sqrt{2} t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3} i \sqrt{2} k t_3$
0	0	0	0	0	0	0
0	0	0	$\frac{2i k t_3}{3}$	$-\frac{1}{3} i \sqrt{2} k t_3$	0	$\frac{2k^2 t_3}{3}$

Source constraints/gauge generators	
SO(3) irreps	Multiplicities
$\sigma_0^{\#1} == 0$	1
$\tau_0^{\#2} == 0$	1
$\tau_0^{\#1} - 2 i k \sigma_0^{\#1} == 0$	1
$\tau_1^{\#2\alpha} + 2 i k \sigma_1^{\#2\alpha} == 0$	3
$\tau_1^{\#1\alpha} == 0$	3
$\tau_1^{\#1\alpha\beta} == 0$	3
$\sigma_1^{\#2\alpha\beta} == 0$	3
$\tau_2^{\#1\alpha\beta} == 0$	5
$\sigma_2^{\#1\alpha\beta} == 0$	5
Total constraints:	25

$\sigma_0^{\#1} \dagger$	$\sigma_0^{\#1} \tau_0^{\#1} \dagger$	$\tau_0^{\#2} \sigma_0^{\#1} \dagger$
$\frac{1}{(1+2k^2)^2 t_3}$	$-\frac{i\sqrt{2} k}{(1+2k^2)^2 t_3}$	0
$\frac{i\sqrt{2} k}{(1+2k^2)^2 t_3}$	$\frac{2k^2}{(1+2k^2)^2 t_3}$	0
0	0	0
0	0	0
$\omega_0^{\#1} \dagger$	$f_0^{\#1} \dagger$	$f_0^{\#2} \omega_0^{\#1} \dagger$
0	t_3	$-i\sqrt{2} k t_3$
0	$i\sqrt{2} k t_3$	$2k^2 t_3$
0	0	0
0	0	0
$\sigma_2^{\#1} \dagger^{\alpha\beta}$	0	0
$\tau_2^{\#1} \dagger^{\alpha\beta}$	0	0
$\sigma_2^{\#1} \dagger^{\alpha\beta\chi}$	0	$\frac{1}{k^2 r_1}$

$\omega_2^{\#1} \dagger^{\alpha\beta}$	$f_2^{\#1} \dagger^{\alpha\beta}$	$\omega_2^{\#1} \alpha\beta\chi$
0	0	0
0	0	0
0	0	$k^2 r_1$

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{r_1 (r_1+r_5) (2r_1+r_5) p^2} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$r_1 < 0 \&\& (r_5 < -r_1 \parallel r_5 > -2r_1) \parallel r_1 > 0 \&\& -2r_1 < r_5 < -r_1$$