

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} + \alpha\beta$	$\sigma_{1+}^{\#2} + \alpha\beta$	$\tau_{1+}^{\#1} + \alpha\beta$	$\sigma_{1-}^{\#1} + \alpha$	$\sigma_{1-}^{\#2} + \alpha$	$\tau_{1-}^{\#1} + \alpha$	$\tau_{1-}^{\#2} + \alpha$
0	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{i\sqrt{2}k}{t_1+k^2t_1}$	0	0	0	0
$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{-2k^2r_5+t_1}{(1+k^2)^2t_1^2}$	$-\frac{i(2k^3r_5-kt_1)}{(1+k^2)^2t_1^2}$	0	0	0	0
$\frac{i\sqrt{2}k}{t_1+k^2t_1}$	$\frac{i(2k^3r_5-kt_1)}{(1+k^2)^2t_1^2}$	$\frac{-2k^4r_5+k^2t_1}{(1+k^2)^2t_1^2}$	0	0	0	0
0	0	0	$\frac{1}{k^2r_5}$	$-\frac{1}{\sqrt{2}(k^2r_5+2k^4r_5)}$	0	$-\frac{i}{kr_5+2k^3r_5}$
0	0	0	$-\frac{1}{\sqrt{2}(k^2r_5+2k^4r_5)}$	$\frac{6k^2r_5+t_1}{2(k+2k^2)^2r_5t_1}$	0	$\frac{i(6k^2r_5+t_1)}{\sqrt{2}k(1+2k^2)^2r_5t_1}$
0	0	0	0	0	0	0
0	0	0	$\frac{i}{kr_5+2k^3r_5}$	$-\frac{i(6k^2r_5+t_1)}{\sqrt{2}k(1+2k^2)^2r_5t_1}$	0	$\frac{6k^2r_5+t_1}{(1+2k^2)^2r_5t_1}$

Quadratic (free) action

$$S_F ==$$

$$\iiint (\frac{1}{6} (-2t_1 \omega_{\prime}^{\alpha\prime} \omega_{\kappa\alpha}^{\prime\kappa} - 6t_1 \omega_{\kappa\lambda}^{\prime\kappa} \omega_{\lambda\prime}^{\prime\kappa} + 6f^{\alpha\beta} \tau_{\alpha\beta} + 6\omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 6r_5 \partial_{\prime} \omega_{\kappa}^{\kappa\lambda} \partial_{\lambda} \omega_{\alpha}^{\alpha} - 6r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\theta\kappa\lambda} + 6r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\theta\kappa\lambda} - 6r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\kappa\lambda\theta} + 12r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda\theta} - 3t_1 \partial^{\alpha} f_{\theta\kappa} \partial^{\kappa} f_{\alpha}^{\theta} - 3t_1 \partial^{\alpha} f_{\kappa\theta} \partial^{\theta} f_{\alpha}^{\kappa} - 3t_1 \partial^{\alpha} f_{\alpha\lambda} \partial^{\kappa} f_{\kappa}^{\lambda} + 2t_1 \omega_{\kappa\alpha}^{\alpha} \partial^{\kappa} f_{\prime}^{\prime} + 2t_1 \omega_{\kappa\lambda}^{\lambda} \partial^{\kappa} f_{\prime}^{\prime} + 4t_1 \partial^{\alpha} f_{\kappa\alpha} \partial^{\kappa} f_{\prime}^{\prime} - 2t_1 \partial_{\kappa} f_{\lambda}^{\lambda} \partial^{\kappa} f_{\prime}^{\prime} + 12t_1 \omega_{\prime\kappa\theta} \partial^{\kappa} f_{\prime}^{\theta} - 2t_1 \omega_{\prime\alpha}^{\alpha} \partial^{\kappa} f_{\kappa}^{\prime} - 2t_1 \omega_{\prime\lambda}^{\lambda} \partial^{\kappa} f_{\kappa}^{\prime} + 3t_1 \partial^{\alpha} f_{\lambda\alpha} \partial^{\kappa} f_{\lambda}^{\theta} + 3t_1 \partial_{\kappa} f_{\theta}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} + 3t_1 \partial_{\kappa} f_{\theta}^{\lambda} \partial^{\kappa} f_{\lambda}^{\theta} - 2t_1 \partial^{\alpha} f_{\lambda}^{\theta} \partial^{\kappa} f_{\alpha}^{\lambda} + 6r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\theta}^{\theta\kappa} - 6r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\alpha}^{\theta\kappa})) [t, x, y, z] dz dy dx dt$$

	$\sigma_{2+}^{\#1} + \alpha\beta$	$\tau_{2+}^{\#1} + \alpha\beta$	$\sigma_{2-}^{\#1} + \alpha\beta\chi$
$\sigma_{2+}^{\#1} + \alpha\beta$	$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\tau_{2+}^{\#1} + \alpha\beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\sigma_{2-}^{\#1} + \alpha\beta\chi$	0	0	$\frac{2}{t_1}$

	$\omega_{2+}^{\#1} + \alpha\beta$	$f_{2+}^{\#1} + \alpha\beta$	$\omega_{2-}^{\#1} + \alpha\beta\chi$
$\omega_{2+}^{\#1} + \alpha\beta$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2+}^{\#1} + \alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	k^2t_1	0
$\omega_{2-}^{\#1} + \alpha\beta\chi$	0	0	$\frac{t_1}{2}$

	$\omega_{0+}^{\#1} +$	$f_{0+}^{\#2} +$	$\omega_{0-}^{\#1} +$
$\omega_{0+}^{\#1} +$	0	0	0
$f_{0+}^{\#1} +$	0	0	0
$f_{0+}^{\#2} +$	0	0	0
$\omega_{0-}^{\#1} +$	0	0	$-t_1$

	$\sigma_{0+}^{\#1} +$	$\tau_{0+}^{\#1} +$	$\tau_{0+}^{\#2} +$	$\sigma_{0-}^{\#1} +$
$\sigma_{0+}^{\#1} +$	0	0	0	0
$\tau_{0+}^{\#1} +$	0	0	0	0
$\tau_{0+}^{\#2} +$	0	0	0	0
$\sigma_{0-}^{\#1} +$	0	0	0	$-\frac{1}{t_1}$

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{0+}^{\#2} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2ik\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2ik\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	17

Massive and massless spectra

Quadratic pole

Pole residue:	$-\frac{1}{r_5t_1^2} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$r_5 < 0 \ \&\& \ t_1 < 0 \ || \ t_1 > 0$$