

| Massive particle |                       |
|------------------|-----------------------|
| Pole residue:    | $-\frac{1}{r_2} > 0$  |
| Polarisations:   | 1                     |
| Square mass:     | $\frac{t_1}{r_2} > 0$ |
| Spin:            | 0                     |
| Parity:          | Odd                   |

Unitarity conditions

$r_2 < 0 \&\& r_5 < -2\,r_3 \&\& t_1 < 0$

| Quadratic pole |                                  |
|----------------|----------------------------------|
| Pole residue:  | $-\frac{1}{(2r_3+r_5)t_1^2} > 0$ |
| Polarisations: | 2                                |

Lagrangian density

$$\begin{aligned}
 &-\frac{1}{3}t_1\,\omega_{\prime}^{\alpha\prime}\,\omega_{\kappa\alpha}^{\kappa}-t_1\,\omega_{\prime}^{\kappa\lambda}\,\omega_{\kappa\lambda}^{\prime}+f^{\alpha\beta}\,\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\,\sigma_{\alpha\beta\chi}{}^{-}2\,r_3\,\partial_{\prime}\omega_{\kappa}^{\kappa\lambda}\,\partial^{\prime}\omega_{\lambda}^{\alpha}{}_{\alpha}{}^{-}\\
 &r_5\,\partial_{\prime}\omega_{\kappa}^{\kappa\lambda}\,\partial^{\prime}\omega_{\lambda}^{\alpha}{}_{\alpha}{}^{+}\frac{2}{3}\,r_2\,\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\,\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}\,r_2\,\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\,\partial_{\kappa}\omega^{\alpha\beta\theta}{}_{-}\\
 &\frac{2}{3}\,r_2\,\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\,\partial_{\kappa}\omega^{\theta\alpha\beta}{}_{+}+2\,r_3\,\partial_{\alpha}\omega_{\lambda}^{\alpha}\,\partial_{\kappa}\omega^{\theta\kappa\lambda}{}_{-}r_5\,\partial_{\alpha}\omega_{\lambda}^{\alpha}\,\partial_{\theta}\omega^{\theta\kappa\lambda}{}_{-}\\
 &2\,r_3\,\partial_{\theta}\omega_{\lambda}^{\alpha}\,\partial_{\alpha}\omega_{\lambda}^{\theta\kappa\lambda}{}_{+}+r_5\,\partial_{\theta}\omega_{\lambda}^{\alpha}\,\partial_{\alpha}\omega_{\lambda}^{\theta\kappa\lambda}{}_{-}2\,r_3\,\partial_{\alpha}\omega_{\lambda}^{\alpha}\,\partial_{\theta}\omega_{\lambda}^{\kappa\lambda\theta}{}_{-}\\
 &r_5\,\partial_{\alpha}\omega_{\lambda}^{\alpha}\,\partial_{\theta}\omega_{\lambda}^{\kappa\lambda\theta}{}_{+}+4\,r_3\,\partial_{\theta}\omega_{\lambda}^{\alpha}\,\partial_{\kappa}\omega_{\lambda}^{\kappa\lambda\theta}{}_{+}+2\,r_5\,\partial_{\theta}\omega_{\lambda}^{\alpha}\,\partial_{\kappa}\omega_{\lambda}^{\kappa\lambda\theta}{}_{-}\\
 &\frac{1}{2}\,t_1\,\partial^{\alpha}f_{\theta\kappa}{}^{\kappa}f_{\alpha}{}^{\theta}-\frac{1}{2}\,t_1\,\partial^{\alpha}f_{\kappa\theta}{}^{\theta}f_{\alpha}{}^{\kappa}-\frac{1}{2}\,t_1\,\partial^{\alpha}f_{\lambda}{}^{\lambda}\,\partial^{\kappa}f_{\alpha}{}^{\theta}-\frac{1}{2}\,t_1\,\partial^{\alpha}f_{\lambda}{}^{\lambda}\,\partial^{\kappa}f_{\alpha}{}^{\theta}{}_{+}\\
 &\frac{1}{3}\,t_1\,\omega_{\kappa\lambda}^{\lambda}\,\partial^{\kappa}f_{\prime}{}^{\prime}{}_{+}\frac{2}{3}\,t_1\,\partial^{\alpha}f_{\kappa\alpha}{}^{\theta}f_{\prime}{}^{\prime}{}_{-}\frac{1}{3}\,t_1\,\partial_{\kappa}f_{\lambda}{}^{\lambda}\,\partial^{\kappa}f_{\prime}{}^{\prime}{}_{+}+2\,t_1\,\omega_{\kappa\theta}\,\partial^{\kappa}f^{\theta}{}_{-}\\
 &\frac{1}{3}\,t_1\,\omega_{\prime\alpha}^{\alpha}\,\partial^{\kappa}f_{\kappa}{}^{\prime}{}_{-}\frac{1}{3}\,t_1\,\omega_{\prime\lambda}^{\lambda}\,\partial^{\kappa}f_{\kappa}{}^{\prime}{}_{+}\frac{1}{2}\,t_1\,\partial^{\alpha}f_{\lambda}{}^{\lambda}\,\partial^{\kappa}f_{\theta}{}^{\theta}{}_{+}+\frac{1}{2}\,t_1\,\partial_{\kappa}f_{\theta}{}^{\theta}\,\partial^{\kappa}f_{\lambda}{}^{\lambda}-\frac{1}{3}\,t_1\,\partial^{\alpha}f_{\lambda}{}^{\lambda}\,\partial^{\kappa}f_{\alpha}{}^{\theta}-\frac{1}{3}\,t_1\,\partial^{\alpha}f_{\lambda}{}^{\lambda}\,\partial^{\kappa}f_{\alpha}{}^{\theta}{}_{-}\\
 &\frac{1}{2}\,t_1\,\partial_{\kappa}f_{\theta}{}^{\lambda}\,\partial^{\kappa}f_{\lambda}{}^{\theta}-\frac{1}{3}\,t_1\,\partial^{\alpha}f_{\alpha}{}^{\theta}\,\partial^{\kappa}f_{\lambda}{}^{\lambda}+\frac{1}{3}\,r_2\,\partial_{\kappa}\omega^{\alpha\beta\theta}\,\partial^{\kappa}\omega_{\alpha\beta\theta}{}_{+}\frac{2}{3}\,r_2\,\partial_{\kappa}\omega^{\theta\alpha\beta}\,\partial^{\kappa}\omega_{\alpha\beta\theta}{}^{-}\\
 &\frac{2}{3}\,r_2\,\partial^{\beta}\omega_{\prime}^{\alpha\lambda}\,\partial_{\lambda}\omega_{\alpha\beta}^{\prime}{}_{+}+\frac{2}{3}\,r_2\,\partial^{\beta}\omega_{\prime}^{\lambda\alpha}\,\partial_{\lambda}\omega_{\alpha\beta}^{\prime}{}_{-}4\,r_3\,\partial^{\beta}\omega_{\prime}^{\lambda\alpha}\,\partial_{\lambda}\omega_{\alpha\beta}^{\prime}{}_{-}\\
 &2\,r_3\,\partial_{\alpha}\omega_{\lambda}^{\alpha}\,\partial^{\lambda}\omega_{\theta}^{\theta\kappa}{}_{\kappa}{}_{+}+r_5\,\partial_{\alpha}\omega_{\lambda}^{\alpha}\,\partial^{\lambda}\omega_{\lambda}^{\theta\kappa}{}_{\theta}{}_{+}\partial^{\lambda}\omega_{\lambda}^{\theta\kappa}{}_{\alpha}{}_{-}2\,r_3\,\partial_{\theta}\omega_{\lambda}^{\alpha}\,\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}{}_{\kappa}{}_{-}r_5\,\partial_{\theta}\omega_{\lambda}^{\alpha}\,\partial^{\lambda}\omega_{\alpha}^{\theta\kappa}{}_{\kappa}{}_{-}
 \end{aligned}$$

Source constraints

| SO(3) irreps  | #  |
|---|----|
| $\tau_{0+}^{\#2} == 0$  | 1  |
| $\tau_{0+}^{\#1} == 0$  | 1  |
| $\tau_{1-}^{\#2\alpha} + 2\,i\,k\,\sigma_{1-}^{\#2\alpha} == 0$           | 3  |
| $\tau_{1-}^{\#1\alpha} == 0$  | 3  |
| $\tau_{1+}^{\#1\alpha\beta} + i\,k\,\sigma_{1+}^{\#2\alpha\beta} == 0$    | 3  |
| $\tau_{2+}^{\#1\alpha\beta} - 2\,i\,k\,\sigma_{2+}^{\#1\alpha\beta} == 0$ | 5  |
| Total #:  | 16 |

| $\sigma_{2+}^{\#1\alpha\beta}$                | $\tau_{2+}^{\#1\alpha\beta}$                   | $\sigma_{2-}^{\#1\alpha\beta\chi}$ |
|---|--|------------------------------------|
| $\frac{2}{(1+2\,k^2)^2}\,t_1$                 | $-\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2}\,t_1$ | 0                                  |
| $\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2}\,t_1$ | $\frac{4\,k^2}{(1+2\,k^2)^2}\,t_1$             | 0                                  |
| 0   | 0  | $\frac{2}{t_1}$                    |

| $\sigma_{0+}^{\#1}$     | $\tau_{0+}^{\#1}$ | $\tau_{0+}^{\#2}$ | $\sigma_{0-}^{\#1}$       |
|-------------------------|-------------------|-------------------|---------------------------|
| $\frac{1}{6\,k^2\,r_3}$ | 0                 | 0                 | 0                         |
| 0                       | 0                 | 0                 | 0                         |
| 0                       | 0                 | 0                 | 0                         |
| 0                       | 0                 | 0                 | $\frac{1}{k^2\,r_2\,t_1}$ |

| $\omega_{2+}^{\#1\alpha\beta}$     | $f_{2+}^{\#1\alpha\beta}$     | $\omega_{2-}^{\#1\alpha\beta\chi}$ |
|------------------------------------|-------------------------------|------------------------------------|
| $\frac{t_1}{2}$                    | $-\frac{i\,k\,t_1}{\sqrt{2}}$ | 0                                  |
| $f_{2+}^{\#1\alpha\beta}$          | $\frac{i\,k\,t_1}{\sqrt{2}}$  | 0                                  |
| $\omega_{2-}^{\#1\alpha\beta\chi}$ | 0                             | $\frac{t_1}{2}$                    |

| $\omega_{0+}^{\#1}$ | $f_{0+}^{\#1}$ | $f_{0+}^{\#2}$ | $\omega_{0-}^{\#1}$ |
|---------------------|----------------|----------------|---------------------|
| $6\,k^2\,r_3$       | 0              | 0              | 0                   |
| $f_{0+}^{\#1}$      | 0              | 0              | 0                   |
| $f_{0+}^{\#2}$      | 0              | 0              | 0                   |
| $\omega_{0-}^{\#1}$ | 0              | 0              | $k^2\,r_2-t_1$      |

| $\omega_{1+}^{\#1\alpha\beta}$    | $\omega_{1+}^{\#2\alpha\beta}$ | $f_{1+}^{\#1\alpha\beta}$     | $\omega_{1-}^{\#1\alpha}$         | $\omega_{1-}^{\#2\alpha}$           | $f_{1-}^{\#1\alpha}$ | $f_{1-}^{\#2\alpha}$               |
|-----------------------------------|--------------------------------|-------------------------------|-----------------------------------|-------------------------------------|----------------------|------------------------------------|
| $k^2\,(2\,r_3+r_5)-\frac{t_1}{2}$ | $-\frac{t_1}{\sqrt{2}}$        | $-\frac{i\,k\,t_1}{\sqrt{2}}$ | 0                                 | 0                                   | 0                    | 0                                  |
| $-\frac{t_1}{\sqrt{2}}$           | 0                              | 0                             | 0                                 | 0                                   | 0                    | 0                                  |
| $\frac{i\,k\,t_1}{\sqrt{2}}$      | 0                              | 0                             | 0                                 | 0                                   | 0                    | 0                                  |
| 0                                 | 0                              | 0                             | $k^2\,(2\,r_3+r_5)+\frac{t_1}{6}$ | $\frac{t_1}{3\,\sqrt{2}}$           | 0                    | $\frac{i\,k\,t_1}{3}$              |
| 0                                 | 0                              | 0                             | $\frac{t_1}{3\,\sqrt{2}}$         | $\frac{t_1}{3}$                     | 0                    | $\frac{1}{3}\,i\,\sqrt{2}\,k\,t_1$ |
| 0                                 | 0                              | 0                             | 0                                 | 0                                   | 0                    | 0                                  |
| 0                                 | 0                              | 0                             | $-\frac{1}{3}\,i\,k\,t_1$         | $-\frac{1}{3}\,i\,\sqrt{2}\,k\,t_1$ | 0                    | $\frac{2\,k^2\,t_1}{3}$            |