

PSALTer results panel

Wave operator and propagator

[illegible]

	$1^+ \mathcal{A}^{\parallel}_{\alpha\beta}$	$1^+ \mathcal{A}^{\perp}_{\alpha\beta}$	$1^+ f^{\parallel}_{\alpha\beta}$	$1^- \mathcal{A}^{\parallel}_{\alpha}$	$1^- \mathcal{A}^{\perp}_{\alpha}$	$1^- f^{\parallel}_{\alpha}$	$1^- f^{\perp}_{\alpha}$
$1^+ \mathcal{A}^{\parallel} \uparrow^{\alpha\beta}$	$\frac{1}{4} (12 \beta_1 - 10 \beta_2 + 2 (\alpha_2 - \alpha_3 + 4 \alpha_4 - 4 \alpha_6) k^2 + (\mathcal{M}_{\text{Pl}})^2)$	$\frac{4 \beta_1 - 6 \beta_2 + (\mathcal{M}_{\text{Pl}})^2}{2 \sqrt{2}}$	$\frac{i k (4 \beta_1 - 6 \beta_2 + (\mathcal{M}_{\text{Pl}})^2)}{2 \sqrt{2}}$	0	0	0	0
$1^+ \mathcal{A}^{\perp} \uparrow^{\alpha\beta}$	$\frac{4 \beta_1 - 6 \beta_2 + (\mathcal{M}_{\text{Pl}})^2}{2 \sqrt{2}}$	$2 \beta_1 \cdot \beta_2$	$i (2 \beta_1 - \beta_2) k$	0	0	0	0
$1^+ f^{\parallel} \uparrow^{\alpha\beta}$	$-\frac{i k (4 \beta_1 - 6 \beta_2 + (\mathcal{M}_{\text{Pl}})^2)}{2 \sqrt{2}}$	$-i (2 \beta_1 - \beta_2) k$	$(2 \beta_1 - \beta_2) k^2$	0	0	0	0
$1^- \mathcal{A}^{\parallel} \uparrow^{\alpha}$	0	0	0	$\beta_1 + \frac{\beta_2}{2} + \beta_3 + \frac{(\mathcal{M}_{\text{Pl}})^2}{4}$	$-\frac{2 \beta_2 + (\mathcal{M}_{\text{Pl}})^2}{2 \sqrt{2}}$	0	$-\frac{1}{2} i k (2 \beta_3 + (\mathcal{M}_{\text{Pl}})^2)$
$1^- \mathcal{A}^{\perp} \uparrow^{\alpha}$	0	0	0	$-\frac{2 \beta_2 + (\mathcal{M}_{\text{Pl}})^2}{2 \sqrt{2}}$	$\frac{1}{2} (2 \beta_1 + \beta_2 + \beta_3)$	0	$\frac{i (2 \beta_1 + \beta_2 + \beta_3) k}{\sqrt{2}}$
$1^- f^{\parallel} \uparrow^{\alpha}$	0	0	0	0	0	0	0
$1^- f^{\perp} \uparrow^{\alpha}$	0	0	0	$\frac{1}{2} i k (2 \beta_3 + (\mathcal{M}_{\text{Pl}})^2)$	$-\frac{i (2 \beta_1 + \beta_2 + \beta_3) k}{\sqrt{2}}$	0	$(2 \beta_1 + \beta_2 + \beta_3) k^2$

Spin-parity form	Covariant form	Multiplicities
$0^+ \tau^i = 0$	$\partial_\beta \partial_\alpha \tau (\Delta + \mathcal{K})^{\alpha\beta} = 0$	1
$2^- i k^\perp \cdot \sigma^{\perp\alpha} + 1^- \tau^i = 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau (\Delta + \mathcal{K})^{\beta\chi} = \partial_\chi \partial^\chi \partial_\beta \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_\sigma \partial^\sigma \partial_\chi \partial_\beta \sigma^{\beta\alpha\chi}$	3
$1^- \tau^i = 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau (\Delta + \mathcal{K})^{\beta\chi} = \partial_\chi \partial^\chi \partial_\beta \tau (\Delta + \mathcal{K})^{\beta\alpha}$	3
$i k^\perp \cdot \sigma^{\perp\alpha\beta} + 1^- \tau^i = 0$	$\partial_\chi \partial^\alpha \tau (\Delta + \mathcal{K})^{\beta\chi} + \partial_\chi \partial^\beta \tau (\Delta + \mathcal{K})^{\chi\alpha} +$ $\partial_\chi \partial^\chi \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_\sigma \partial_\chi \sigma^{\chi\beta\delta} + 2 \partial_\sigma \partial^\delta \partial_\chi \sigma^{\chi\alpha\beta} =$ $\partial_\chi \partial^\alpha \tau (\Delta + \mathcal{K})^{\chi\beta} + \partial_\chi \partial^\beta \tau (\Delta + \mathcal{K})^{\alpha\chi} + \partial_\chi \partial^\chi \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \partial_\sigma \partial_\chi \partial^\beta \sigma^{\chi\alpha\delta}$	3
Total expected gauge generators:		10

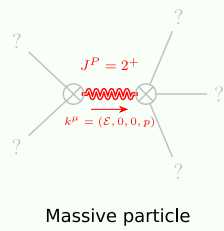
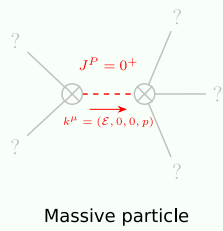
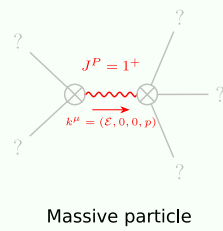
	${}^2\mathcal{A} _{\alpha\beta}$	${}^2f _{\alpha\beta}$	${}^2\mathcal{A} _{\alpha\beta\chi}$
${}^2\mathcal{A} ^{\alpha\beta}$	$\frac{1}{4}(4\beta_1+2\beta_2+2(-3\alpha_2+\alpha_3-4\alpha_4+\alpha_6)k^2-(M_{\text{Pl}}{}^2))$	$-\frac{i(4\beta_1+2\beta_2-(M_{\text{Pl}}{}^2))}{2\sqrt{2}}$	0
${}^2f ^{\alpha\beta}$	$\frac{i(4\beta_1+2\beta_2-(M_{\text{Pl}}{}^2))}{2\sqrt{2}}$	$(2\beta_1+\beta_2)k^2$	0
${}^2\mathcal{A} ^{\alpha\beta\chi}$	0	0	$\beta_1+\frac{\beta_2}{2}-\alpha_2k^2-\frac{(M_{\text{Pl}}{}^2)}{4}$

$$\begin{aligned}
S = & \iiint (\mathcal{A}^{\alpha\beta} \sigma_{\alpha\beta\chi} + \mathcal{A}^{\alpha\beta} \tau(\Delta + \mathcal{K})_{\alpha\beta} - \\
& \frac{1}{2} (M_{\mathcal{P}})^2 (\mathcal{I}_{\kappa\theta} \mathcal{I}^{\theta\kappa} + \mathcal{I}^{\theta\kappa} \mathcal{I}_{\theta}{}^{\kappa} + 2 f^{\theta} \partial_{\theta} \mathcal{I}_{\kappa}{}^{\kappa} - \\
& 2 \partial_{\theta} \mathcal{I}^{\theta}{}_{\theta} - 2 f^{\theta} \partial_{\kappa} \mathcal{I}_{\theta}{}^{\kappa} + 2 f'_{\kappa} \partial_{\kappa} \mathcal{I}^{\theta\theta}) + \\
& \beta_{\frac{3}{2}} (-\mathcal{I}_{\theta}{}^{\kappa} \mathcal{I}_{\theta}{}^{\kappa} + 2 \mathcal{I}_{\kappa}{}^{\kappa} \partial_{\theta} f^{\theta} - 2 \mathcal{I}_{\theta}{}^{\kappa} \partial^{\theta} f'_{\kappa} + \\
& \partial_{\theta} f^{\kappa}{}_{\kappa} \partial^{\theta} f'_{\kappa} + \partial_{\theta} f^{\theta}{}_{\kappa} \partial_{\kappa} f'^{\kappa} - 2 \partial^{\theta} f'_{\kappa} \partial_{\kappa} f^{\theta}{}_{\theta}) + \\
& 2 \alpha_4 (4 \partial_{\kappa} \mathcal{I}_{\alpha\theta\kappa} - 2 \partial_{\kappa} \mathcal{I}_{\alpha\kappa\theta} - \partial_{\theta} \mathcal{I}_{\alpha\kappa} + \partial_{\kappa} \mathcal{I}_{\alpha\theta} - 2 \partial_{\kappa} \mathcal{I}_{\alpha\theta}) \\
& \partial^{\kappa} \mathcal{I}^{\alpha\theta} - \alpha_{\frac{2}{2}} (\partial_{\theta} \mathcal{I}_{\kappa}{}^{\kappa} \partial^{\theta} \mathcal{I}^{\alpha}{}_{\alpha} + \partial_{\alpha} \mathcal{I}^{\alpha\theta} \partial_{\kappa} \mathcal{I}_{\theta}{}^{\kappa} - \\
& 2 \partial^{\theta} \mathcal{I}^{\alpha}{}_{\alpha} \partial_{\kappa} \mathcal{I}_{\theta}{}^{\kappa} - 4 \partial_{\kappa} \mathcal{I}_{\alpha\theta} \partial^{\kappa} \mathcal{I}^{\alpha\theta} + \\
& 2 \partial_{\kappa} \mathcal{I}_{\alpha\theta} \partial^{\kappa} \mathcal{I}^{\alpha\theta} + 2 \partial_{\kappa} \mathcal{I}_{\alpha\theta} \partial^{\kappa} \mathcal{I}^{\alpha\theta}) + \\
& 2 \beta_{\frac{1}{2}} (-\mathcal{I}_{\kappa\theta} \mathcal{I}^{\theta\kappa} + (2 \mathcal{I}_{\theta\kappa} - \partial f_{\kappa\theta} + \partial_{\kappa} f_{\theta}) \partial^{\kappa} f^{\theta} + \\
& \mathcal{I}_{\theta\kappa} (\mathcal{I}^{\theta\kappa} + 2 \partial^{\kappa} f^{\theta})) + \\
& \beta_{\frac{2}{2}} ((-2 \mathcal{I}_{\theta\kappa} - 2 \partial f_{\theta\kappa} + \partial_{\theta} f_{\kappa} + \partial_{\kappa} f_{\theta}) \partial^{\kappa} f^{\theta} - \\
& \mathcal{I}_{\theta\kappa} (\mathcal{I}^{\theta\kappa} + 2 \partial^{\kappa} f^{\theta})) + \\
& \mathcal{I}_{\kappa\theta} (3 \mathcal{I}^{\theta\kappa} + 4 \partial^{\kappa} f^{\theta})) + 4 \alpha_{\frac{1}{2}} \partial_{\theta} \mathcal{I}^{\theta}{}_{\theta} \partial_{\kappa} \mathcal{I}^{\kappa}{}_{\kappa} - \\
& \alpha_{\frac{3}{2}} (\partial_{\kappa} \mathcal{I}_{\lambda}{}^{\zeta} \partial^{\lambda} \mathcal{I}^{\theta\kappa}_{\theta} + (\partial_{\theta} \mathcal{I}^{\theta\kappa\lambda} - 2 \partial^{\lambda} \mathcal{I}^{\theta\kappa}_{\theta}) \partial_{\zeta} \mathcal{I}_{\lambda}{}^{\zeta}) + \\
& 4 \alpha_{\frac{6}{6}} \partial_{\lambda} \mathcal{I}_{\lambda}{}^{\zeta} \partial^{\zeta} \mathcal{I}^{\alpha\lambda}) [t, x, y, z] d z d y d x d t
\end{aligned}$$

	$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$
$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	$\frac{1}{2(3 \frac{1}{1} \alpha + \frac{1}{3} \alpha + \frac{1}{6} \alpha + \frac{1}{2} (M_{\text{Pl}})^2)(1 - \frac{(M_{\text{Pl}})^2}{2\beta_1 + \beta_2 + 3\beta_3})}$	$-\frac{i \sqrt{2} (2 \beta_1 + \beta_2 + 3 \beta_3 + (M_{\text{Pl}})^2)}{k (-4(3 \frac{1}{1} \alpha + \frac{1}{3} \alpha + \frac{1}{6} \alpha + \frac{1}{2} (2 \beta_1 + \beta_2 + 3 \beta_3) k^2 + (2 \beta_1 + \beta_2 + 3 \beta_3)(M_{\text{Pl}})^2 + (M_{\text{Pl}})^2)^2)}$	0	0
$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	$\frac{i \sqrt{2} (2 \beta_1 + \beta_2 + 3 \beta_3 + (M_{\text{Pl}})^2)}{k ((M_{\text{Pl}})^2)^2 + (2 \beta_1 + \beta_2 + 3 \beta_3)(-4(3 \frac{1}{1} \alpha + \frac{1}{3} \alpha + \frac{1}{6} \alpha + \frac{1}{2} (M_{\text{Pl}})^2) k^2 + (M_{\text{Pl}})^2))}$	$-\frac{2 \beta_1 + \beta_2 + 3 \beta_3 + 4(3 \frac{1}{1} \alpha + \frac{1}{3} \alpha + \frac{1}{6} \alpha + \frac{1}{2} (M_{\text{Pl}})^2) k^2 + (M_{\text{Pl}})^2}{k^2 (-4(3 \frac{1}{1} \alpha + \frac{1}{3} \alpha + \frac{1}{6} \alpha + \frac{1}{2} (2 \beta_1 + \beta_2 + 3 \beta_3) k^2 + (2 \beta_1 + \beta_2 + 3 \beta_3)(M_{\text{Pl}})^2 + (M_{\text{Pl}})^2)^2)}$	0	0
$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	0	0	0	0
$\begin{smallmatrix} 0^+ \\ \downarrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix} \begin{smallmatrix} 0^+ \\ \uparrow \end{smallmatrix}$	0	0	0	$\frac{2}{8 \beta_1 - 8 \beta_2 + 4(\frac{1}{1} \alpha + \frac{1}{3} \alpha + \frac{1}{6} \alpha) k^2 + (M_{\text{Pl}})^2}$

[illegible]

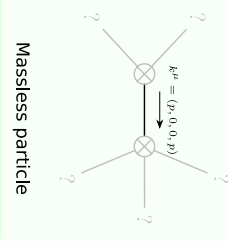
Massive and massless spectra



Pole residue:	$ \begin{aligned} & (\alpha_2 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{\text{Pl}}^2) - 12 \beta_2 (M_{\text{Pl}}^2) + (M_{\text{Pl}}^2)^2) - \\ & \alpha_3 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{\text{Pl}}^2) - 12 \beta_2 (M_{\text{Pl}}^2) + (M_{\text{Pl}}^2)^2) + \\ & 4 \alpha_4 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{\text{Pl}}^2) - 12 \beta_2 (M_{\text{Pl}}^2) + (M_{\text{Pl}}^2)^2) - \\ & 4 \alpha_6 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{\text{Pl}}^2) - 12 \beta_2 (M_{\text{Pl}}^2) + (M_{\text{Pl}}^2)^2) - \\ & 2(2 \beta_1 - \beta_2)(32 \beta_1^2 - 16 \beta_2^2 + 10 \beta_2 (M_{\text{Pl}}^2) - (M_{\text{Pl}}^2)^2 - 4 \beta_1 (4 \beta_2 + (M_{\text{Pl}}^2))))/ \\ & ((\alpha_2 - \alpha_3 + 4 \alpha_4 - 4 \alpha_6)(2 \beta_1 - \beta_2) \\ & (8 \alpha_2 \beta_1 - 8 \alpha_3 \beta_1 + 32 \alpha_4 \beta_1 - 32 \alpha_6 \beta_1 - 32 \beta_1^2 - 4 \alpha_2 \beta_2 + 4 \alpha_3 \beta_2 - 16 \alpha_4 \beta_2 + \\ & 16 \alpha_6 \beta_2 + 16 \beta_1^2 \beta_2 + 16 \beta_2^2 + 4 \beta_1 (M_{\text{Pl}}^2) - 10 \beta_2 (M_{\text{Pl}}^2) + (M_{\text{Pl}}^2)^2)) > 0 \end{aligned} $
Square mass:	$ \frac{-32 \beta_1^2 + 16 \beta_2^2 - 10 \beta_1 (M_{\text{Pl}}^2) + (M_{\text{Pl}}^2)^2 + 4 \beta_1 (4 \beta_2 + (M_{\text{Pl}}^2))}{4(\alpha_2 - \alpha_3 + 4 \alpha_4 - 4 \alpha_6)(2 \beta_1 - \beta_2)} > 0 $
Spin:	1
Parity:	Even

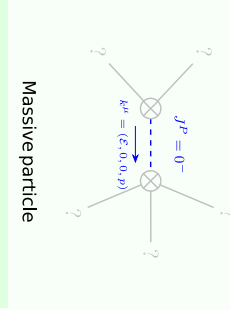
Pole residue:	$4 \alpha_4 \beta_1 + 4 \alpha_6 \beta_1 - 2 \alpha_4 \beta_2 + 2 \alpha_6 \beta_2 - 6 \alpha_4 \beta_3 + 6 \alpha_6 \beta_3 -$ $2 \alpha_4 (\mathcal{M}_{\text{Pl}}^2) + 2 \alpha_6 (\mathcal{M}_{\text{Pl}}^2) + 2 \beta_1 (\mathcal{M}_{\text{Pl}}^2) + \beta_2 (\mathcal{M}_{\text{Pl}}^2) + 3 \beta_3 (\mathcal{M}_{\text{Pl}}^2) +$ $6 \alpha_1 (2 \beta_1 + \beta_2 + 3 \beta_3 + (\mathcal{M}_{\text{Pl}}^2)) + 2 \alpha_3 (2 \beta_1 + \beta_2 + 3 \beta_3 + (\mathcal{M}_{\text{Pl}}^2)) /$ $(2(3 \alpha_1 + \alpha_3 - \alpha_4 + \alpha_6)(2 \beta_1 + \beta_2 + 3 \beta_3)(\mathcal{M}_{\text{Pl}}^2)) > 0$
Square mass:	$\frac{(\mathcal{M}_{\text{Pl}}^2)(2 \beta_1 + \beta_2 + 3 \beta_3 + (\mathcal{M}_{\text{Pl}}^2))}{4(3 \alpha_1 + \alpha_3 - \alpha_4 + \alpha_6)(2 \beta_1 + \beta_2 + 3 \beta_3)} > 0$
Spin:	0
Parity:	Even

Poleresidue:	$\frac{1}{(M_{pl}^2)} > 0$
Polarisations:	2

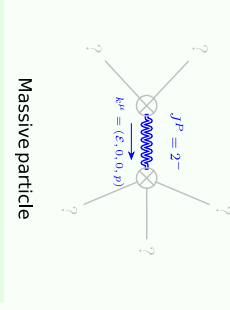


Poleresidue:	$\frac{-3\alpha_{\frac{1}{2}}(4\beta_{\frac{1}{2}}+2\beta_{\frac{1}{2}}-(M_{\Pi^2}))+\alpha_{\frac{3}{4}}(4\beta_{\frac{1}{2}}+2\beta_{\frac{1}{2}}-(M_{\Pi^2}))-2(8\alpha_{\frac{4}{6}}\beta_{\frac{1}{2}}-8\alpha_{\frac{1}{6}}\beta_{\frac{1}{2}}+4\alpha_{\frac{1}{2}}\beta_{\frac{1}{2}}-4\alpha_{\frac{1}{2}}\beta_{\frac{1}{2}}-2\alpha_{\frac{1}{6}}(M_{\Pi^2})+2\alpha_{\frac{1}{6}}(M_{\Pi^2})+2\beta_{\frac{1}{2}}(M_{\Pi^2})+\beta_{\frac{1}{2}}(M_{\Pi^2}))}{(3\alpha_{\frac{1}{2}}-\alpha_{\frac{3}{4}}+4\alpha_{\frac{4}{6}}\alpha_{\frac{1}{6}})(2\beta_{\frac{1}{2}}+\beta_{\frac{1}{2}})(M_{\Pi^2})} >$
	0
Square mass:	$\frac{(4\beta_{\frac{1}{2}}+2\beta_{\frac{1}{2}}-(M_{\Pi^2}))(M_{\Pi^2})}{4(3\alpha_{\frac{1}{2}}-\alpha_{\frac{3}{4}}+4\alpha_{\frac{4}{6}}\alpha_{\frac{1}{6}})(2\beta_{\frac{1}{2}}+\beta_{\frac{1}{2}})} > 0$
Spin:	2
Parity:	Even

Pole residue:	$\frac{1}{2(\alpha_+ + 3\alpha_-)} > 0$
Square mass:	$-\frac{8\beta_- - 8\beta_+ + (M_{\text{Pl}}^2)}{4(\alpha_+ + 3\alpha_-)} > 0$
Spin:	0
Parity:	Odd



Polesidue:	$\frac{1}{\alpha_s} > 0$
Squaremass:	$\frac{4\beta_s + 2\beta_s \cdot (M_{Pl})^2}{4\alpha_s} > 0$
Spin:	2
Parity:	Odd



Unitarity conditions

(Demonstrably impossible)