

Massive particle

Pole residue:	$\frac{6t_1t_3(t_1+t_3)-3r_5(t_1^2+2t_3^2)}{2r_5(t_1+t_3)-(-3t_1t_3+r_5(t_1+t_3))} > 0$
Polarisations:	3
Square mass:	$-\frac{3t_1t_3}{2r_5t_1+2r_5t_3} > 0$
Spin:	1
Parity:	Odd

Unitarity conditions

$r_2 < 0 \ \&\& \ r_5 < 0 \ \&\& \ t_1 < 0 \ \&\& \ 0 < t_3 < -t_1$

Massive particle

Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$\frac{t_1}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

Lagrangian density

$$\begin{aligned}
 &-\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\lambda}+f^{\alpha\beta}\tau_{\alpha\beta}+ \\
 &\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}-r_5\partial_{\lambda}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega_{\lambda}^{\kappa\lambda}\partial_{\lambda}^{\prime}\omega_{\alpha}^{\alpha}+\frac{2}{3}r_2\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}- \\
 &\frac{2}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\kappa}^{\kappa\lambda\theta}+ \\
 &2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\alpha}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\prime}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}+ \\
 &\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\prime}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\prime}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}+\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\lambda}^{\prime}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\lambda}^{\prime}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}+\frac{2}{3}t_3\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}+ \\
 &2t_1\omega_{\lambda\kappa\theta}\partial^{\kappa}f^{\lambda\theta}-\frac{1}{3}t_1\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{2}{3}t_3\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\prime}-\frac{1}{3}t_1\omega_{\lambda\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{2}{3}t_3\omega_{\lambda\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\lambda\alpha}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}- \\
 &\frac{1}{3}t_1\partial^{\alpha}f_{\alpha}^{\kappa}f_{\lambda\kappa}^{\lambda}+\frac{2}{3}t_3\partial^{\alpha}f_{\alpha}^{\kappa}f_{\lambda\kappa}^{\lambda}\partial^{\kappa}f_{\lambda}^{\alpha}+\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}- \\
 &\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}+\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}+r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\lambda}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\lambda}^{\theta\kappa}
 \end{aligned}$$

$\sigma_{2^{+}}^{\#1} \dagger^{\alpha\beta\chi}$	$\sigma_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$\tau_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{2^{-}}^{\#1} \dagger^{\alpha\beta\chi}$
0	$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
0	$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\frac{2}{t_1}$	0	0	0

Source constraints	#
$\text{SO}(3)$ irreps	
$\tau_{0^{+}}^{\#2} == 0$	1
$\tau_{0^{+}}^{\#1} - 2i\bar{k}\sigma_{0^{+}}^{\#1} == 0$	1
$\tau_{1^{-}}^{\#2\alpha} + 2i\bar{k}\sigma_{1^{-}}^{\#2\alpha} == 0$	3
$\tau_{1^{-}}^{\#1\alpha} == 0$	3
$\tau_{1^{+}}^{\#1\alpha\beta} + i\bar{k}\sigma_{1^{+}}^{\#2\alpha\beta} == 0$	3
$\tau_{2^{+}}^{\#1\alpha\beta} - 2i\bar{k}\sigma_{2^{+}}^{\#1\alpha\beta} == 0$	5
Total #:	16

$\sigma_{0^{+}}^{\#1} \dagger$	$\tau_{0^{+}}^{\#1}$	$\tau_{0^{+}}^{\#2}$	$\sigma_{0^{-}}^{\#1}$
$\sigma_{0^{+}}^{\#1} \dagger$	$\frac{1}{(1+2k^2)^2t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0
$\tau_{0^{+}}^{\#1} \dagger$	$\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0
$\tau_{0^{+}}^{\#2} \dagger$	0	0	0
$\sigma_{0^{-}}^{\#1} \dagger$	0	0	$\frac{1}{k^2r_2-t_1}$

$\omega_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$\omega_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$f_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$\omega_{2^{-}}^{\#1} \dagger^{\alpha\beta\chi}$
$\omega_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{ikt_1}{\sqrt{2}}$	k^2t_1	0
$\omega_{2^{-}}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	$\frac{t_1}{2}$

$\omega_{0^{+}}^{\#1} \dagger$	$f_{0^{+}}^{\#1} \dagger$	$f_{0^{+}}^{\#2} \dagger$	$\omega_{0^{-}}^{\#1} \dagger$
$\omega_{0^{+}}^{\#1} \dagger$	t_3	$-i\sqrt{2}kt_3$	0
$f_{0^{+}}^{\#1} \dagger$	$i\sqrt{2}kt_3$	$2k^2t_3$	0
$f_{0^{+}}^{\#2} \dagger$	0	0	0
$\omega_{0^{-}}^{\#1} \dagger$	0	0	$k^2r_2-t_1$

$\sigma_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1^{+}}^{\#2} \dagger^{\alpha\beta}$	$\tau_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1^{-}}^{\#1} \dagger^{\alpha}$	$\sigma_{1^{-}}^{\#2} \dagger^{\alpha}$	$\tau_{1^{-}}^{\#1} \dagger^{\alpha}$	$\tau_{1^{-}}^{\#2} \dagger^{\alpha}$
$\sigma_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	0	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	0	0	0	0
$\sigma_{1^{+}}^{\#2} \dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{-2k^2r_5+t_1}{(1+k^2)^2t_1^2}$	0	0	0	0
$\tau_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{i\sqrt{2}k}{t_1+k^2t_1}$	$\frac{i(2k^3r_5-kt_1)}{(1+k^2)^2t_1^2}$	0	0	0	0
$\sigma_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	$\frac{2(t_1+t_3)}{3t_1t_3+2k^2r_5(t_1+t_3)}$	$-\frac{\sqrt{2}(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$	0	$-\frac{2ik(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$
$\sigma_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	$-\frac{\sqrt{2}(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$	$\frac{6k^2r_5+t_1+4t_3}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$	0	$\frac{i\sqrt{2}k(6k^2r_5+t_1+4t_3)}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$
$\tau_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	$\frac{2ik(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$	$-\frac{i\sqrt{2}k(6k^2r_5+t_1+4t_3)}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$	0	$\frac{2k^2(6k^2r_5+t_1+4t_3)}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$

$\omega_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1^{+}}^{\#2} \dagger^{\alpha\beta}$	$f_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1^{-}}^{\#1} \dagger^{\alpha}$	$\omega_{1^{-}}^{\#2} \dagger^{\alpha}$	$f_{1^{-}}^{\#1} \dagger^{\alpha}$	$f_{1^{-}}^{\#2} \dagger^{\alpha}$
$\omega_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$k^2r_5-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	0	0	0
$\omega_{1^{+}}^{\#2} \dagger^{\alpha\beta}$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$f_{1^{+}}^{\#1} \dagger^{\alpha\beta}$	$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0	0
$\omega_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	0	$\frac{1}{6}(6k^2r_5+t_1+4t_3)$	$\frac{t_1-2t_3}{3\sqrt{2}}$	0
$\omega_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	0	$\frac{t_1-2t_3}{3\sqrt{2}}$	$\frac{t_1+t_3}{3}$	$\frac{1}{3}ik(t_1-2t_3)$
$f_{1^{-}}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	$\frac{1}{3}i\sqrt{2}k(t_1+t_3)$
$f_{1^{-}}^{\#2} \dagger^{\alpha}$	0	0	0	$-\frac{1}{3}ik(t_1-2t_3)$	$-\frac{1}{3}i\sqrt{2}k(t_1+t_3)$	$\frac{2}{3}k^2(t_1+t_3)$