

PSALTer results panel

Wave operator and propagator

[illegible]

	${}^1\mathcal{A}_{\alpha\beta}^{\parallel}$	${}^1\mathcal{A}_{\alpha\beta}^{\perp}$	${}^1\mathcal{F}_{\alpha\beta}^{\parallel}$	${}^1\mathcal{A}_{\alpha}^{\parallel}$	${}^1\mathcal{A}_{\alpha}^{\perp}$	${}^1\mathcal{F}_{\alpha}^{\parallel}$	${}^1\mathcal{F}_{\alpha}^{\perp}$
${}^1\mathcal{A}^{\parallel} + {}^{\alpha\beta}$	$\frac{1}{4}(12\beta_1 - 10\beta_2 + 2(\alpha_2 - \alpha_3 + 4\alpha_4 - 4\alpha_6)k^2 + (\mathcal{M}_{\text{Pl}})^2)$	$\frac{4\beta_1 - 6\beta_2 + (\mathcal{M}_{\text{Pl}})^2}{2\sqrt{2}}$	$\frac{i k(4\beta_1 - 6\beta_2 + (\mathcal{M}_{\text{Pl}})^2)}{2\sqrt{2}}$	0	0	0	0
${}^1\mathcal{A}^{\perp} + {}^{\alpha\beta}$	$\frac{4\beta_1 - 6\beta_2 + (\mathcal{M}_{\text{Pl}})^2}{2\sqrt{2}}$	$2\beta_1 - \beta_2$	$i(2\beta_1 - \beta_2)k$	0	0	0	0
${}^1\mathcal{F}^{\parallel} + {}^{\alpha\beta}$	$-\frac{i k(4\beta_1 - 6\beta_2 + (\mathcal{M}_{\text{Pl}})^2)}{2\sqrt{2}}$	$-i(2\beta_1 - \beta_2)k$	$(2\beta_1 - \beta_2)k^2$	0	0	0	0
${}^1\mathcal{A}^{\parallel} + {}^{\alpha}$	0	0	0	$\beta_1 + \frac{\beta_2}{2} + \beta_3 + \frac{(\mathcal{M}_{\text{Pl}})^2}{4}$	$-\frac{2\beta_1 + (\mathcal{M}_{\text{Pl}})^2}{2\sqrt{2}}$	0	$-\frac{1}{2}i k(2\beta_3 + (\mathcal{M}_{\text{Pl}})^2)$
${}^1\mathcal{A}^{\perp} + {}^{\alpha}$	0	0	0	$-\frac{2\beta_1 + (\mathcal{M}_{\text{Pl}})^2}{2\sqrt{2}}$	$\frac{1}{2}(2\beta_1 + \beta_2 + \beta_3)$	0	$\frac{i(2\beta_1 + \beta_2 + \beta_3)k}{\sqrt{2}}$
${}^1\mathcal{F}^{\parallel} + {}^{\alpha}$	0	0	0	0	0	0	0
${}^1\mathcal{F}^{\perp} + {}^{\alpha}$	0	0	0	$\frac{1}{2}i k(2\beta_3 + (\mathcal{M}_{\text{Pl}})^2)$	$-\frac{i(2\beta_1 + \beta_2 + \beta_3)k}{\sqrt{2}}$	0	$(2\beta_1 + \beta_2 + \beta_3)k^2$

Spin-parity form	Covariant form	Multiplicities
$0^+ \tau^+ = 0$	$\partial_\beta \partial_\alpha \tau (\Delta + \mathcal{K})^{\alpha\beta} = 0$	1
$2^- i \, k^+ \sigma^+ = 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau (\Delta + \mathcal{K})^{\beta\chi} = \partial_\chi \partial^\chi \partial_\beta \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \, \partial_\delta \partial^\delta \partial_\chi \partial_\beta \sigma^{\beta\alpha\chi}$	3
$1^- \tau^+ = 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau (\Delta + \mathcal{K})^{\beta\chi} = \partial_\chi \partial^\chi \partial_\beta \tau (\Delta + \mathcal{K})^{\beta\alpha}$	3
$i \, k \, 1^+ \sigma^+ = 0$	$\partial_\alpha \partial^\alpha \tau (\Delta + \mathcal{K})^{\beta\chi} + \partial_\beta \partial^\beta \tau (\Delta + \mathcal{K})^{\chi\alpha} +$ $\partial_\chi \partial^\chi \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \, \partial_\delta \partial_\chi \partial^\alpha \sigma^{\chi\beta\delta} + 2 \, \partial_\delta \partial^\delta \partial_\chi \sigma^{\chi\alpha\beta} =$ $\partial_\chi \partial^\beta \tau (\Delta + \mathcal{K})^{\chi\beta} + \partial_\chi \partial^\beta \tau (\Delta + \mathcal{K})^{\alpha\chi} + \partial_\chi \partial^\chi \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \, \partial_\delta \partial_\chi \partial^\beta \sigma^{\chi\alpha\delta}$	3
Total expected gauge generators:		10

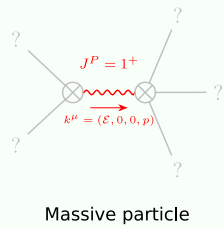
	$2^+ \mathcal{A} _{\alpha\beta}$	$2^+ f _{\alpha\beta}$	$2^- \mathcal{A} _{\alpha\beta\chi}$
$2^+ \mathcal{A} _{+}^{\alpha\beta}$	$\frac{1}{4} (4 \beta_1 + 2 \beta_2 + 2(-3 \alpha_2 + \alpha_3 - 4 \alpha_4 + 4 \alpha_6) k^2 - (\mathcal{M}_n^2))$	$-\frac{i \kappa(4 \beta_1 + 2 \beta_2 - (\mathcal{M}_n^2))}{2 \sqrt{2}}$	0
$2^+ f _{+}^{\alpha\beta}$	$\frac{i \kappa(4 \beta_1 + 2 \beta_2 - (\mathcal{M}_n^2))}{2 \sqrt{2}}$	$(2 \beta_1 + \beta_2) k^2$	0
$2^- \mathcal{A} _{+}^{\alpha\beta\chi}$	0	0	$\beta_1 + \frac{\beta_2}{2} - \alpha_2 k^2 - \frac{(\mathcal{M}_n^2)}{4}$

$$\begin{aligned}
S = & \iiint (\mathcal{A}^{\alpha\beta} \sigma_{\alpha\beta\chi} + f^{\alpha\beta} \tau(\Delta + \mathcal{K})_{\alpha\beta} - \\
& \frac{1}{2} (M_{\text{Pl}}^2) (\mathcal{A}_{\mu\theta} \mathcal{A}^{\mu\theta\kappa} + \mathcal{A}^{\mu\theta}{}_{\mu} \mathcal{A}_{\theta\kappa}{}^{\mu} + 2 f^{\mu\theta} \partial_{\theta} \mathcal{A}_{\mu\kappa}{}^{\mu} - \\
& 2 \partial_{\theta} \mathcal{A}^{\mu\theta}{}_{\mu} - 2 f^{\mu\theta} \partial_{\theta} \mathcal{A}_{\mu\kappa}{}^{\mu} + 2 f^{\mu}{}_{\mu} \partial_{\kappa} \mathcal{A}^{\theta\kappa}{}_{\theta}) + \\
& \beta_3 (-\mathcal{A}^{\mu\theta}{}_{\mu} \mathcal{A}_{\theta\kappa}{}^{\mu} + 2 \mathcal{A}_{\theta\kappa}{}^{\mu} \partial_{\theta} f^{\mu\theta} - 2 \mathcal{A}_{\theta\kappa}{}^{\mu} \partial^{\theta} f^{\mu}{}_{\mu} + \\
& \partial_{\theta} f^{\mu\kappa}{}_{\kappa} \partial^{\theta} f^{\mu}{}_{\mu} + 2 \partial_{\theta} f^{\mu\theta} \partial_{\kappa} f^{\mu\kappa}{}_{\mu} - 2 \partial^{\theta} f^{\mu}{}_{\mu} \partial_{\kappa} f^{\mu\kappa}{}_{\theta}) + \\
& 2 \alpha_4 (4 \partial_{\mu} \mathcal{A}_{\alpha\theta\kappa} - 2 \partial_{\mu} \mathcal{A}_{\alpha\theta\kappa} - \partial_{\theta} \mathcal{A}_{\alpha\mu\kappa} + \partial_{\kappa} \mathcal{A}_{\alpha\theta\mu} - 2 \partial_{\kappa} \mathcal{A}_{\alpha\theta\mu}) \\
& \partial^{\kappa} \mathcal{A}^{\alpha\mu\theta} - \alpha_2 (\partial_{\theta} \mathcal{A}_{\mu\kappa}{}^{\mu} \partial^{\kappa} \mathcal{A}^{\alpha\mu}{}_{\alpha} + \partial_{\alpha} \mathcal{A}^{\mu\theta\mu} \partial_{\kappa} \mathcal{A}_{\mu}{}^{\kappa}{}_{\theta} - \\
& 2 \partial^{\theta} \mathcal{A}^{\alpha\mu}{}_{\alpha} \partial_{\kappa} \mathcal{A}_{\mu\theta}{}^{\kappa} - 4 \partial_{\mu} \mathcal{A}_{\alpha\theta\kappa} \partial^{\kappa} \mathcal{A}^{\alpha\mu\theta} + \\
& 2 \partial_{\mu} \mathcal{A}_{\alpha\theta\kappa} \partial^{\kappa} \mathcal{A}^{\alpha\mu\theta} + 2 \partial_{\kappa} \mathcal{A}_{\alpha\theta\mu} \partial^{\kappa} \mathcal{A}^{\alpha\mu\theta}) + \\
& 2 \beta_1 (-\mathcal{A}_{\mu\theta} \mathcal{A}^{\mu\theta\kappa} + (2 \mathcal{A}_{\theta\kappa\mu} - \partial f_{\kappa\theta} + \partial_{\kappa} f_{\theta\mu}) \partial^{\kappa} f^{\mu\theta} + \\
& \mathcal{A}_{\mu\theta\kappa} (\mathcal{A}^{\mu\theta\kappa} + 2 \partial^{\kappa} f^{\mu\theta})) + \\
& \beta_2 ((-2 \partial_{\theta\kappa\mu} - 2 \partial_{\mu} f_{\theta\kappa} + \partial_{\theta} f_{\mu\kappa} + \partial_{\kappa} f_{\theta\mu}) \partial^{\kappa} f^{\mu\theta} - \\
& \mathcal{A}_{\mu\theta\kappa} (\mathcal{A}^{\mu\theta\kappa} + 2 \partial^{\kappa} f^{\mu\theta})) + \\
& \mathcal{A}_{\mu\theta\kappa} (3 \mathcal{A}^{\mu\theta\kappa} + 4 \partial^{\kappa} f^{\mu\theta})) + 4 \alpha_1 \partial_{\theta} \mathcal{A}^{\mu\theta}{}_{\mu} \partial_{\lambda} \mathcal{A}^{\kappa\lambda}{}_{\kappa} - \\
& \alpha_3 (\partial_{\kappa} \mathcal{A}_{\lambda}{}^{\zeta}{}_{\zeta} \partial^{\lambda} \mathcal{A}^{\theta\kappa}{}_{\theta} + (\partial_{\theta} \mathcal{A}^{\theta\kappa\lambda} - 2 \partial^{\lambda} \mathcal{A}^{\theta\kappa}{}_{\theta}) \partial_{\zeta} \mathcal{A}_{\lambda}{}^{\zeta}{}_{\kappa}) + \\
& 4 \alpha_6 \partial_{\lambda} \mathcal{A}_{\lambda\zeta}{}^{\alpha} \partial^{\zeta} \mathcal{A}^{\alpha\lambda}) [t, x, y, z] d z d y d x d t
\end{aligned}$$

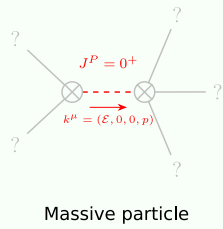
	$\mathcal{O}^{\tau} \mathcal{I}^{\dagger}$	$\mathcal{O}^{\dagger} \mathcal{I}^{\dagger}$	$\mathcal{O}^{\tau} \mathcal{I}^{\dagger}$	$\mathcal{O}^{\tau} \mathcal{I}^{\dagger}$
$\mathcal{O}^{\tau} \mathcal{I}^{\dagger} \uparrow$	$\frac{1}{2(3 \underset{3}{a} + \underset{3}{a} - \underset{6}{a} + \underset{6}{a}) k^2 + \frac{1}{2} (M_{\Pi^2})^2 (1 - \frac{(M_{\Pi^2})^2}{2\beta_1 + \beta_2 + 3\beta_3})}$	$-\frac{i \sqrt{2} (2 \beta_1 + \beta_2 + 3 \beta_3 + (M_{\Pi^2})^2)}{1 \underset{2}{\beta_1} + 2 \underset{3}{\beta_2} + 3 \underset{6}{\beta_3}}$	0	0
$\mathcal{O}^{\dagger} \mathcal{I}^{\dagger} \uparrow$	$\frac{i \sqrt{2} (2 \beta_1 + \beta_2 + 3 \beta_3 + (M_{\Pi^2})^2)}{k ((M_{\Pi^2})^2 + (2 \beta_1 + \beta_2 + 3 \beta_3) (-4(3 \underset{1}{a} + \underset{3}{a} - \underset{3}{a} + \underset{6}{a} + \underset{6}{a} + \underset{6}{a}) k^2 + (M_{\Pi^2})^2))}$	$-\frac{2 \beta_1 + \beta_2 + 3 \beta_3 + 4(3 \underset{1}{a} + \underset{2}{a} - \underset{3}{a} + \underset{4}{a} - \underset{6}{a} + \underset{6}{a}) k^2 + (M_{\Pi^2})^2}{1 \underset{2}{\beta_1} + 2 \underset{3}{\beta_2} + 3 \underset{6}{\beta_3}}$	0	0
$\mathcal{O}^{\dagger} \mathcal{I}^{\dagger} \uparrow$	0	0	0	0
$\mathcal{O}^{\tau} \mathcal{I}^{\dagger} \uparrow$	0	0	0	$\frac{2}{8 \underset{1}{\beta_1} - 8 \underset{2}{\beta_2} + 4 (\underset{3}{a} + \underset{4}{a}) k^2 + (M_{\Pi^2})^2}$

[illegible]

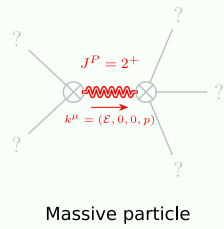
Massive and massless spectra



Massive particle



Massive particle

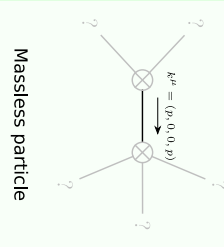


Massive particle

Pole residue:	$\left(\alpha_2 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{Pl}^2) - 12 \beta_2 (M_{Pl}^2) + (M_{Pl}^2)^2) - \right.$ $\alpha_3 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{Pl}^2) - 12 \beta_2 (M_{Pl}^2) + (M_{Pl}^2)^2) +$ $4 \alpha_4 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{Pl}^2) - 12 \beta_2 (M_{Pl}^2) + (M_{Pl}^2)^2) -$ $4 \alpha_6 (48 \beta_1^2 - 80 \beta_1 \beta_2 + 44 \beta_2^2 + 8 \beta_1 (M_{Pl}^2) - 12 \beta_2 (M_{Pl}^2) + (M_{Pl}^2)^2) -$ $2(2 \beta_1 - \beta_2)(32 \beta_1^2 - 16 \beta_1 \beta_2 + 10 \beta_2 (M_{Pl}^2) - (M_{Pl}^2)^2 - 4 \beta_1 (4 \beta_2 + (M_{Pl}^2))) \Big/$ $((\alpha_2 - \alpha_3 + 4 \alpha_4 - 4 \alpha_6)(2 \beta_1 - \beta_2)$ $(8 \alpha_2 \beta_1 - 8 \alpha_3 \beta_1 + 32 \alpha_4 \beta_1 - 32 \alpha_6 \beta_1 - 32 \beta_1^2 - 4 \alpha_2 \beta_2 + 4 \alpha_3 \beta_2 - 16 \alpha_4 \beta_2 +$ $16 \alpha_6 \beta_2 + 16 \beta_1 \beta_2 + 16 \beta_2^2 + 4 \beta_1 (M_{Pl}^2) - 10 \beta_2 (M_{Pl}^2) + (M_{Pl}^2)^2)) > 0$
Square mass:	$\frac{-32 \beta_1^2 + 16 \beta_1 \beta_2 - 10 \beta_2 (M_{Pl}^2) + (M_{Pl}^2)^2 + 4 \beta_1 (4 \beta_2 + (M_{Pl}^2))}{4(\alpha_2 - \alpha_3 + 4 \alpha_4 - 4 \alpha_6)(2 \beta_1 - \beta_2)} > 0$
Spin:	1
Parity:	Even

Pole residue:	$(-4 \frac{\alpha_1 \beta_1}{4} + 4 \frac{\alpha_1 \beta_1}{6} - 2 \frac{\alpha_1 \beta_1}{4} + 2 \frac{\alpha_1 \beta_1}{6} - 6 \frac{\alpha_1 \beta_1}{4} + 6 \frac{\alpha_1 \beta_1}{6} -$ $2 \frac{\alpha_1 (\mathcal{M}_{\text{Pl}}^2)}{4} + 2 \frac{\alpha_1 (\mathcal{M}_{\text{Pl}}^2)}{6} + 2 \frac{\beta_1 (\mathcal{M}_{\text{Pl}}^2)}{1} + \beta_2 (\mathcal{M}_{\text{Pl}}^2) + 3 \frac{\beta_3 (\mathcal{M}_{\text{Pl}}^2)}{3} +$ $6 \frac{\alpha_1 (2 \beta_1 + \beta_2 + 3 \beta_3 + (\mathcal{M}_{\text{Pl}}^2))}{1} + 2 \frac{\alpha_3 (2 \beta_1 + \beta_2 + 3 \beta_3 + (\mathcal{M}_{\text{Pl}}^2))}{3} +$ $(2(3 \frac{\alpha_1 + \alpha_3 - \alpha_4 + \alpha_6}{1} + 2 \frac{\beta_1 + \beta_2 + 3 \beta_3}{1}) (\mathcal{M}_{\text{Pl}}^2)) > 0$
Square mass:	$\frac{(\mathcal{M}_{\text{Pl}}^2)(2 \frac{\beta_1 + \beta_2 + 3 \beta_3}{1} + (\mathcal{M}_{\text{Pl}}^2))}{4(3 \frac{\alpha_1 + \alpha_3 - \alpha_4 + \alpha_6}{1} + 2 \frac{\beta_1 + \beta_2 + 3 \beta_3}{1})} > 0$
Spin:	0
Parity:	Even

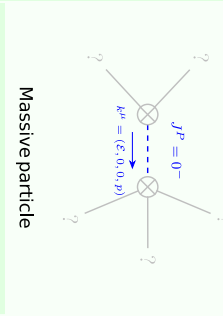
Poleresidue:	$\frac{1}{(M_{Pl}^2)} > 0$
Polarisations:	2



Massless particle

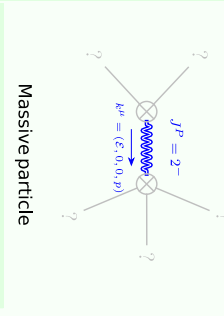
Poleresidue:	$\frac{-3\alpha_{\frac{1}{2}}(4\beta_{\frac{1}{2}}+2\beta_{\frac{1}{2}}-(M_{\Pi^2}))+\alpha_{\frac{3}{4}}(4\beta_{\frac{1}{2}}+2\beta_{\frac{1}{2}}-(M_{\Pi^2}))-2(8\alpha_{\frac{1}{4}}\beta_{\frac{1}{2}}-8\alpha_{\frac{1}{6}}\beta_{\frac{1}{2}}+4\alpha_{\frac{1}{2}}\beta_{\frac{1}{2}}-4\alpha_{\frac{3}{2}}\beta_{\frac{1}{2}}-2\alpha_{\frac{5}{2}}(M_{\Pi^2})+2\alpha_{\frac{7}{6}}(M_{\Pi^2})+2\beta_{\frac{1}{6}}(M_{\Pi^2})+\beta_{\frac{1}{2}}(M_{\Pi^2}))}{(3\alpha_{\frac{1}{2}}-\alpha_{\frac{3}{4}}+4\alpha_{\frac{1}{6}})(2\beta_{\frac{1}{2}}+\beta_{\frac{1}{2}})(M_{\Pi^2})} >$
	0
Square mass:	$\frac{(4\beta_{\frac{1}{2}}+2\beta_{\frac{1}{2}}-(M_{\Pi^2}))(M_{\Pi^2})}{4(3\alpha_{\frac{1}{2}}-\alpha_{\frac{3}{4}}+4\alpha_{\frac{1}{6}})(2\beta_{\frac{1}{2}}+\beta_{\frac{1}{2}})} > 0$
Spin:	2
Parity:	Even

Pole residue:	$-\frac{1}{2(\alpha_+ + 3\alpha_-)} > 0$
Square mass:	$-\frac{8\delta_-^2 - 8\delta_+ + (W_{12}^2)}{4(\alpha_+ + 3\alpha_-)^2} > 0$
Spin:	0
Parity:	Odd



Massive particle

Pole/residue:	$\frac{1}{\alpha_z} > 0$
Square mass:	$\frac{4B_1 + 2B_2 - (M_1 m_1^2)}{4\alpha_z} > 0$
Spin:	2
Parity:	Odd



Massive particle

Unitarity conditions

(Demonstrably impossible)