

PSALTer results panel

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$$\iiint \left[ \left( \mathcal{A}^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + f^{\alpha\beta}{}_{\tau} (\Delta + \mathcal{K})_{\alpha\beta} - 2 r_{\frac{1}{3}} \left( \partial_{\beta} \mathcal{A}_{\tau}{}^{\theta}{}_{\theta} \partial^{\tau} \mathcal{A}^{\alpha\beta}{}_{\alpha} + \partial_{\tau} \mathcal{A}_{\beta}{}^{\theta}{}_{\theta} \partial^{\tau} \mathcal{A}^{\alpha\beta}{}_{\alpha} + \partial_{\alpha} \mathcal{A}^{\alpha\beta\prime}{}_{\prime} \partial_{\theta} \mathcal{A}_{\beta}{}^{\theta}{}_{\theta} - 2 \partial^{\tau} \mathcal{A}^{\alpha\beta}{}_{\alpha} \partial_{\theta} \mathcal{A}_{\beta}{}^{\theta}{}_{\theta} + \partial_{\alpha} \mathcal{A}^{\alpha\beta\prime}{}_{\prime} \partial_{\theta} \mathcal{A}_{\tau}{}^{\theta}{}_{\theta} - 2 \partial^{\tau} \mathcal{A}^{\alpha\beta}{}_{\alpha} \partial_{\theta} \mathcal{A}_{\tau}{}^{\theta}{}_{\theta} + 2 \partial_{\beta} \mathcal{A}_{\tau}{}_{\theta\alpha} \partial^{\theta} \mathcal{A}^{\alpha\beta\prime}{}_{\prime} \right) + \frac{1}{6} t_{\frac{1}{1}} \right. \\ \left. \left( 2 \mathcal{A}^{\alpha\prime}{}_{\alpha} \mathcal{A}_{\tau}{}^{\theta}{}_{\theta} - 4 \mathcal{A}_{\alpha}{}^{\theta}{}_{\theta} \partial_{\tau} f^{\alpha\prime} + 4 \mathcal{A}_{\tau}{}^{\theta}{}_{\theta} \partial^{\tau} f^{\alpha}{}_{\alpha} - 2 \partial_{\tau} f^{\theta}{}_{\theta} \partial^{\tau} f^{\alpha}{}_{\alpha} - 2 \partial_{\tau} f^{\alpha\prime}{}_{\prime} \partial_{\theta} f^{\alpha}{}_{\alpha} + 4 \partial^{\tau} f^{\alpha}{}_{\alpha} \partial_{\theta} f_{\tau}{}^{\theta}{}_{\theta} - 6 \partial_{\alpha} f_{\tau}{}_{\theta\theta} \partial^{\theta} f^{\alpha\prime} + 3 \partial_{\alpha} f_{\theta\theta} \partial^{\theta} f^{\alpha\prime} + 3 \partial_{\theta} f_{\alpha\tau} \partial^{\theta} f^{\alpha\prime} + \right. \right. \\ \left. \left. 3 \partial_{\theta} f_{\tau\alpha} \partial^{\theta} f^{\alpha\prime} + 6 \mathcal{A}_{\alpha\theta\tau} \left( \mathcal{A}^{\alpha\prime\theta} + 2 \partial^{\theta} f^{\alpha\prime\prime} \right) \right) + r_{\frac{1}{5}} \left( \partial_{\tau} \mathcal{A}_{\theta}{}^{\kappa}{}_{\kappa} \partial^{\theta} \mathcal{A}^{\alpha\prime}{}_{\alpha} - \partial_{\theta} \mathcal{A}_{\tau}{}^{\kappa}{}_{\kappa} \partial^{\theta} \mathcal{A}^{\alpha\prime}{}_{\alpha} - \left( \partial_{\alpha} \mathcal{A}^{\alpha\prime\theta} - 2 \partial^{\theta} \mathcal{A}^{\alpha\prime}{}_{\alpha} \right) \left( \partial_{\kappa} \mathcal{A}_{\tau}{}^{\kappa}{}_{\theta} - \partial_{\kappa} \mathcal{A}_{\theta}{}^{\kappa}{}_{\tau} \right) \right) \right] [t, x, y, z] dz dy dx dt$$

Wave operator

$\overset{0}{\circ}\mathcal{A}^{\parallel}$	$\overset{0}{\circ}f^{\parallel}$	$\overset{0}{\circ}f^{\perp}$	$\overset{0}{\circ}\mathcal{A}^{\parallel}$								
$\overset{0}{\circ}\mathcal{A}^{\parallel} \dagger$	$6 k^2 r_{\frac{1}{3}}$	0	0	0							
$\overset{0}{\circ}f^{\parallel} \dagger$	0	0	0	0							
$\overset{0}{\circ}f^{\perp} \dagger$	0	0	0	0							
$\overset{0}{\circ}\mathcal{A}^{\parallel} \dagger$	0	0	0	$-\frac{t_{\frac{1}{1}}}{1}$	$\overset{1}{\circ}\mathcal{A}^{\parallel}_{\alpha\beta}$	$\overset{1}{\circ}\mathcal{A}^{\perp}_{\alpha\beta}$	$\overset{1}{\circ}f^{\parallel}_{\alpha\beta}$	$\overset{1}{\circ}\mathcal{A}^{\parallel}_{\alpha}$	$\overset{1}{\circ}\mathcal{A}^{\perp}_{\alpha}$	$\overset{1}{\circ}f^{\parallel}_{\alpha}$	$\overset{1}{\circ}f^{\perp}_{\alpha}$
$\overset{1}{\circ}\mathcal{A}^{\parallel} \dagger^{\alpha\beta}$	$k^2 \left( 2 r_{\frac{1}{3}} + r_{\frac{1}{5}} \right) - \frac{t_{\frac{1}{1}}}{2}$	$-\frac{t_{\frac{1}{1}}}{\sqrt{2}}$	$-\frac{i k t_{\frac{1}{1}}}{\sqrt{2}}$	0	0	0	0	0	0	0	0
$\overset{1}{\circ}\mathcal{A}^{\perp} \dagger^{\alpha\beta}$	$-\frac{t_{\frac{1}{1}}}{\sqrt{2}}$	0	0	0	0	0	0	0	0	0	0
$\overset{1}{\circ}f^{\parallel} \dagger^{\alpha\beta}$	$\frac{i k t_{\frac{1}{1}}}{\sqrt{2}}$	0	0	0	0	0	0	0	0	0	0
$\overset{1}{\circ}\mathcal{A}^{\parallel} \dagger^{\alpha}$	0	0	0	$k^2 \left( 2 r_{\frac{1}{3}} + r_{\frac{1}{5}} \right) + \frac{t_{\frac{1}{1}}}{6}$	$\frac{t_{\frac{1}{1}}}{3 \sqrt{2}}$	0	$\frac{i k t_{\frac{1}{1}}}{3}$	0	0	0	0
$\overset{1}{\circ}\mathcal{A}^{\perp} \dagger^{\alpha}$	0	0	0	$\frac{t_{\frac{1}{1}}}{3 \sqrt{2}}$	$\frac{t_{\frac{1}{1}}}{3}$	0	$\frac{1}{3} i \sqrt{2} k t_{\frac{1}{1}}$	0	0	0	0
$\overset{1}{\circ}f^{\parallel} \dagger^{\alpha}$	0	0	0	0	0	0	0	0	0	0	0
$\overset{1}{\circ}f^{\perp} \dagger^{\alpha}$	0	0	0	$-\frac{1}{3} i k t_{\frac{1}{1}}$	$-\frac{1}{3} i \sqrt{2} k t_{\frac{1}{1}}$	0	$\frac{2 k^2 t_{\frac{1}{1}}}{3}$	$\overset{2}{\circ}\mathcal{A}^{\parallel}_{\alpha\beta}$	$\overset{2}{\circ}f^{\parallel}_{\alpha\beta}$	$\overset{2}{\circ}\mathcal{A}^{\parallel}_{\alpha\beta\chi}$	
								$\overset{2}{\circ}\mathcal{A}^{\parallel} \dagger^{\alpha\beta}$	$\frac{t_{\frac{1}{1}}}{2}$	$-\frac{i k t_{\frac{1}{1}}}{\sqrt{2}}$	0
								$\overset{2}{\circ}f^{\parallel} \dagger^{\alpha\beta}$	$\frac{i k t_{\frac{1}{1}}}{\sqrt{2}}$	$k^2 t_{\frac{1}{1}}$	0
								$\overset{2}{\circ}\mathcal{A}^{\parallel} \dagger^{\alpha\beta\chi}$	0	0	$\frac{t_{\frac{1}{1}}}{2}$

Saturated propagator

$\overset{0}{\circ}\sigma^{\parallel}$	$\overset{0}{\circ}\tau^{\parallel}$	$\overset{0}{\circ}\tau^{\perp}$	$\overset{0}{\circ}\sigma^{\parallel}$								
$\overset{0}{\circ}\sigma^{\parallel} \dagger$	$\frac{1}{6 k^2 r_{\frac{1}{3}}}$	0	0	0							
$\overset{0}{\circ}\tau^{\parallel} \dagger$	0	0	0	0							
$\overset{0}{\circ}\tau^{\perp} \dagger$	0	0	0	0							
$\overset{0}{\circ}\sigma^{\parallel} \dagger$	0	0	0	$-\frac{1}{t_{\frac{1}{1}}}$	$\overset{1}{\circ}\sigma^{\parallel}_{\alpha\beta}$	$\overset{1}{\circ}\sigma^{\perp}_{\alpha\beta}$	$\overset{1}{\circ}\tau^{\parallel}_{\alpha\beta}$	$\overset{1}{\circ}\sigma^{\parallel}_{\alpha}$	$\overset{1}{\circ}\sigma^{\perp}_{\alpha}$	$\overset{1}{\circ}\tau^{\parallel}_{\alpha}$	$\overset{1}{\circ}\tau^{\perp}_{\alpha}$
$\overset{1}{\circ}\sigma^{\parallel} \dagger^{\alpha\beta}$	0	$-\frac{\sqrt{2}}{t_{\frac{1}{1}}+k^2 t_{\frac{1}{1}}}$	$-\frac{i \sqrt{2} k}{t_{\frac{1}{1}}+k^2 t_{\frac{1}{1}}}$	0	0	0	0	0	0	0	0
$\overset{1}{\circ}\sigma^{\perp} \dagger^{\alpha\beta}$	$-\frac{\sqrt{2}}{t_{\frac{1}{1}}+k^2 t_{\frac{1}{1}}}$	$\frac{-2 k^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+t_{\frac{1}{1}}}{\left( 1+k^2 \right)^2 t_{\frac{1}{1}}^2}$	$\frac{-2 i k^3 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+i k t_{\frac{1}{1}}}{\left( 1+k^2 \right)^2 t_{\frac{1}{1}}^2}$	0	0	0	0	0	0	0	0
$\overset{1}{\circ}\tau^{\parallel} \dagger^{\alpha\beta}$	$\frac{i \sqrt{2} k}{t_{\frac{1}{1}}+k^2 t_{\frac{1}{1}}}$	$\frac{i \left( 2 k^3 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)-k t_{\frac{1}{1}} \right)}{\left( 1+k^2 \right)^2 t_{\frac{1}{1}}^2}$	$\frac{-2 k^4 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+k^2 t_{\frac{1}{1}}}{\left( 1+k^2 \right)^2 t_{\frac{1}{1}}^2}$	0	0	0	0	0	0	0	0
$\overset{1}{\circ}\sigma^{\parallel} \dagger^{\alpha}$	0	0	0	$\frac{1}{k^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)}$	$-\frac{1}{\sqrt{2} \left( k^2+2 k^4 \right) \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)}$	0	$-\frac{i}{k \left( 1+2 k^2 \right) \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)}$	0	0	0	0
$\overset{1}{\circ}\sigma^{\perp} \dagger^{\alpha}$	0	0	0	$-\frac{1}{\sqrt{2} \left( k^2+2 k^4 \right) \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)}$	$\frac{6 k^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+t_{\frac{1}{1}}}{2 \left( k+2 k^3 \right)^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right) t_{\frac{1}{1}}}$	0	$\frac{i \left( 6 k^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+t_{\frac{1}{1}} \right)}{\sqrt{2} k \left( 1+2 k^2 \right)^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right) t_{\frac{1}{1}}}$	0	0	0	0
$\overset{1}{\circ}\tau^{\parallel} \dagger^{\alpha}$	0	0	0	0	0	0	0	0	0	0	0
$\overset{1}{\circ}\tau^{\perp} \dagger^{\alpha}$	0	0	0	$\frac{i}{k \left( 1+2 k^2 \right) \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)}$	$-\frac{i \left( 6 k^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+t_{\frac{1}{1}} \right)}{\sqrt{2} k \left( 1+2 k^2 \right)^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right) t_{\frac{1}{1}}}$	0	$\frac{6 k^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right)+t_{\frac{1}{1}}}{\left( 1+2 k^2 \right)^2 \left( 2 r_{\frac{1}{3}}+r_{\frac{1}{5}} \right) t_{\frac{1}{1}}}$	$\overset{2}{\circ}\sigma^{\parallel}_{\alpha\beta}$	$\overset{2}{\circ}\tau^{\parallel}_{\alpha\beta}$	$\overset{2}{\circ}\sigma^{\parallel}_{\alpha\beta\chi}$	
								$\overset{2}{\circ}\sigma^{\parallel} \dagger^{\alpha\beta}$	$\frac{2}{\left( 1+2 k^2 \right)^2 t_{\frac{1}{1}}}-\frac{2 i \sqrt{2} k}{\left( 1+2 k^2 \right)^2 t_{\frac{1}{1}}}$	0	0
								$\overset{2}{\circ}\tau^{\parallel} \dagger^{\alpha\beta}$	$\frac{2 i \sqrt{2} k}{\left( 1+2 k^2 \right)^2 t_{\frac{1}{1}}}$	$\frac{4 k^2}{\left( 1+2 k^2 \right)^2 t_{\frac{1}{1}}}$	0
								$\overset{2}{\circ}\sigma^{\parallel} \dagger^{\alpha\beta\chi}$	0	0	$\frac{2}{t_{\frac{1}{1}}}$

Source constraints

Spin-parity form	Covariant form	Multiplicities
$\overset{0}{\circ}\tau^{\perp} == 0$	$\partial_{\beta} \partial_{\alpha \tau} (\Delta + \mathcal{K})^{\alpha\beta} == 0$	1
$\overset{0}{\circ}\tau^{\parallel} == 0$	$\partial_{\beta} \partial_{\alpha \tau} (\Delta + \mathcal{K})^{\alpha\beta} == \partial_{\beta} \partial^{\beta}{}_{\tau} (\Delta + \mathcal{K})^{\alpha}{}_{\alpha}$	1
$2 i k \overset{1}{\circ}\sigma^{\perp\alpha} + \overset{1}{\circ}\tau^{\perp\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\beta\chi} == \partial_{\chi} \partial^{\chi} \partial_{\beta \tau} (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial_{\beta} \sigma^{\beta\alpha\chi}$	3
$\overset{1}{\circ}\tau^{\parallel\alpha} == 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\beta\chi} == \partial_{\chi} \partial^{\chi} \partial_{\beta \tau} (\Delta + \mathcal{K})^{\beta\alpha}$	3
$i k \overset{1}{\circ}\sigma^{\perp\alpha\beta} + \overset{1}{\circ}\tau^{\parallel\alpha\beta} == 0$	$\partial_{\chi} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\beta\chi} + \partial_{\chi} \partial^{\beta}{}_{\tau} (\Delta + \mathcal{K})^{\chi\alpha} + \partial_{\chi} \partial^{\chi}{}_{\tau} (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\beta\delta} + 2 \partial_{\delta} \partial^{\delta} \partial_{\chi} \sigma^{\chi\alpha\beta} == \partial_{\chi} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\chi\beta} + \partial_{\chi} \partial^{\beta}{}_{\tau} (\Delta + \mathcal{K})^{\alpha\chi} + \partial_{\chi} \partial^{\chi}{}_{\tau} (\Delta + \mathcal{K})^{\beta\alpha} + 2 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\alpha\delta}$	3
$-2 i k \overset{2}{\circ}\sigma^{\parallel} + \overset{2}{\circ}\tau^{\parallel\alpha\beta} == 0$	$-i \left( 4 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\chi\delta} + 2 \partial_{\delta} \partial^{\delta} \partial^{\beta} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\chi}{}_{\chi} - 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\beta\chi} - 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha}{}_{\tau} (\Delta + \mathcal{K})^{\chi\beta} - 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta}{}_{\tau} (\Delta + \mathcal{K})^{\alpha\chi} - 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta}{}_{\tau} (\Delta + \mathcal{K})^{\chi\alpha} + \right. \\ 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi}{}_{\tau} (\Delta + \mathcal{K})^{\alpha\beta} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi}{}_{\tau} (\Delta + \mathcal{K})^{\beta\alpha} + 4 i k^{\chi} \partial_{\epsilon} \partial_{\chi} \partial^{\beta} \partial^{\alpha} \sigma^{\delta}{}_{\delta}{}^{\epsilon} - 6 i k^{\chi} \partial_{\epsilon} \partial_{\delta} \partial_{\chi} \partial^{\alpha} \sigma^{\delta\beta\epsilon} - 6 i k^{\chi} \partial_{\epsilon} \partial_{\delta} \partial_{\chi} \partial^{\beta} \sigma^{\delta\alpha\epsilon} + \\ \left. 6 i k^{\chi} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial_{\chi} \sigma^{\alpha\beta\delta} + 6 i k^{\chi} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial_{\chi} \sigma^{\beta\alpha\delta} + 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial_{\chi \tau} (\Delta + \mathcal{K})^{\chi\delta} - 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta}{}_{\tau} (\Delta + \mathcal{K})^{\chi}{}_{\chi} - 4 i \eta^{\alpha\beta} k^{\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\chi} \sigma^{\delta}{}_{\delta}{}^{\epsilon} \right) == 0$	5
Total expected gauge generators:		16

Massive spectrum

(There are no massive particles)

Massless spectrum

Massless particle

Pole residue:	$-\frac{7}{2 r_{\frac{1}{3}} + r_{\frac{1}{5}}} + \frac{-2 t_{\frac{1}{1}} p^2 - 4 \left( 2 r_{\frac{1}{3}} + r_{\frac{1}{5}} \right) p^4}{t_{\frac{1}{1}}^2} > 0$
Polarisations:	2

Gauge symmetries

(Not yet implemented in PSALTer)

Unitarity conditions

$r_{\frac{1}{3}} \in \mathbb{R} \ \&\& r_{\frac{1}{5}} < -2 r_{\frac{1}{3}} \ \&\& \left( t_{\frac{1}{1}} < 0 \parallel t_{\frac{1}{1}} > 0 \right)$

Validity assumptions

(Not yet implemented in PSALTer)