



Massive particle	
Pole residue:	$\frac{6t_1t_3(t_1+t_3)-3r_5(t_1^2+2t_3^2)}{2r_5(t_1+t_3)(-3t_1t_3+r_5(t_1+t_3))} > 0$
Polarisations:	3
Square mass:	$-\frac{3t_1t_3}{2r_5t_1+2r_5t_3} > 0$
Spin:	1
Parity:	Odd

Unitarity conditions

$r_5 < 0 \ \&\& \ (t_1 < 0 \ \&\& \ 0 < t_3 < -t_1) \ || \ (t_1 > 0 \ \&\& \ (t_3 < -t_1 \ || \ t_3 > 0))$

(No massless particles)

### Lagrangian density

$$\begin{aligned}
 &-\frac{1}{3}t_1\omega_{\prime}^{\alpha\prime}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_3\omega_{\prime}^{\alpha\prime}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\prime}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+ \\
 &2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}\partial^{\kappa}f_{\alpha}^{\theta}- \\
 &\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\alpha\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\prime}^{\prime}-\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\prime}^{\prime}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\prime}^{\prime}- \\
 &\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\prime}^{\prime}+\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\prime}^{\prime}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\prime}^{\prime}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\prime}^{\prime}+ \\
 &\frac{2}{3}t_3\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\prime}^{\prime}+2t_1\omega_{\prime\kappa\theta}\partial^{\kappa}f^{\prime\theta}-\frac{1}{3}t_1\omega_{\prime\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{2}{3}t_3\omega_{\prime\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\prime}- \\
 &\frac{1}{3}t_1\omega_{\prime\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{2}{3}t_3\omega_{\prime\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{\prime}+\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\lambda\alpha}+ \\
 &\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}-\frac{1}{3}t_1\partial^{\alpha}f_{\alpha}^{\lambda}\partial^{\kappa}f_{\lambda\kappa}+ \\
 &\frac{2}{3}t_3\partial^{\alpha}f_{\alpha}^{\lambda}\partial^{\kappa}f_{\lambda\kappa}+r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega^{\theta\kappa}_{\kappa}
 \end{aligned}$$

Added source term:

$f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

$\omega_{1+}^{\#1}+\alpha\beta$	$\omega_{1+}^{\#2}+\alpha\beta$	$f_{1+}^{\#1}+\alpha\beta$	$\omega_{1-}^{\#1}\alpha$	$\omega_{1-}^{\#2}\alpha$	$f_{1-}^{\#2}\alpha$
$\omega_{1+}^{\#1}+\alpha\beta$	$k^2r_5-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	0	0	0
$\omega_{1+}^{\#2}+\alpha\beta$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0
$f_{1+}^{\#1}+\alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0
$\omega_{1-}^{\#1}+\alpha$	0	0	$\frac{1}{6}(6k^2r_5+t_1+4t_3)$	$\frac{t_1-2t_3}{3\sqrt{2}}$	$\frac{1}{3}\bar{ik}(t_1-2t_3)$
$\omega_{1-}^{\#2}+\alpha$	0	0	$\frac{t_1-2t_3}{3\sqrt{2}}$	$\frac{t_1+t_3}{3}$	$\frac{1}{3}\bar{i}\sqrt{2}k(t_1+t_3)$
$f_{1-}^{\#1}+\alpha$	0	0	0	0	0
$f_{1-}^{\#2}+\alpha$	0	0	$-\frac{1}{3}\bar{ik}(t_1-2t_3)$	$-\frac{1}{3}\bar{i}\sqrt{2}k(t_1+t_3)$	$\frac{2}{3}k^2(t_1+t_3)$

$\sigma_{0+}^{\#1}+$	$\tau_{0+}^{\#1}+$	$\tau_{0+}^{\#2}+$	$\sigma_{0-}^{\#1}+$
$\sigma_{0+}^{\#1}+$	$\frac{1}{(1+2k^2)^2t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0
$\tau_{0+}^{\#1}+$	$\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0
$\tau_{0+}^{\#2}+$	0	0	0
$\sigma_{0-}^{\#1}+$	0	0	$\frac{1}{t_1}$

#### Source constraints

SO(3) irreps	#
$\tau_{0+}^{\#2}==0$	1
$\tau_{0+}^{\#1}-2\bar{ik}\sigma_{0+}^{\#1}==0$	1
$\tau_{1-}^{\#2\alpha}+2\bar{ik}\sigma_{1-}^{\#2\alpha}==0$	3
$\tau_{1-}^{\#1\alpha}==0$	3
$\tau_{1+}^{\#1\alpha\beta}+\bar{ik}\sigma_{1+}^{\#2\alpha\beta}==0$	3
$\tau_{2+}^{\#1\alpha\beta}-2\bar{ik}\sigma_{2+}^{\#1\alpha\beta}==0$	5
Total #:	16

$\omega_{2+}^{\#1}+\alpha\beta$	$f_{2+}^{\#1}+\alpha\beta$	$\omega_{2-}^{\#1}\alpha\beta\chi$
$\omega_{2+}^{\#1}+\alpha\beta$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$
$f_{2+}^{\#1}+\alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	$k^2t_1$
$\omega_{2-}^{\#1}+\alpha\beta\chi$	0	$\frac{t_1}{2}$

$\sigma_{1+}^{\#1}+\alpha\beta$	$\sigma_{1+}^{\#2}+\alpha\beta$	$\tau_{1+}^{\#1}+\alpha\beta$	$\sigma_{1-}^{\#1}\alpha$	$\sigma_{1-}^{\#2}\alpha$	$\tau_{1-}^{\#1}\alpha$	$\tau_{1-}^{\#2}\alpha$
$\sigma_{1+}^{\#1}+\alpha\beta$	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{i\sqrt{2}k}{t_1+k^2t_1}$	0	0	0	0
$\sigma_{1+}^{\#2}+\alpha\beta$	$-\frac{2k^2r_5+t_1}{(1+k^2)^2t_1^2}$	$-\frac{i(2k^3r_5-kt_1)}{(1+k^2)^2t_1^2}$	0	0	0	0
$\tau_{1+}^{\#1}+\alpha\beta$	$\frac{i(2k^3r_5-kt_1)}{(1+k^2)^2t_1^2}$	$\frac{-2k^4r_5+k^2t_1}{(1+k^2)^2t_1^2}$	0	0	0	0
$\sigma_{1-}^{\#1}+\alpha$	0	0	$\frac{2(t_1+t_3)}{3t_1t_3+2k^2r_5(t_1+t_3)}$	$-\frac{\sqrt{2}(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$	0	$-\frac{2ik(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$
$\sigma_{1-}^{\#2}+\alpha$	0	0	$-\frac{\sqrt{2}(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$	$\frac{6k^2r_5+t_1+4t_3}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$	0	$\frac{i\sqrt{2}k(6k^2r_5+t_1+4t_3)}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$
$\tau_{1-}^{\#1}+\alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2}+\alpha$	0	0	$\frac{2ik(t_1-2t_3)}{(1+2k^2)(3t_1t_3+2k^2r_5(t_1+t_3))}$	$-\frac{i\sqrt{2}k(6k^2r_5+t_1+4t_3)}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$	0	$\frac{2k^2(6k^2r_5+t_1+4t_3)}{(1+2k^2)^2(3t_1t_3+2k^2r_5(t_1+t_3))}$

$\sigma_{2+}^{\#1}+\alpha\beta$	$\tau_{2+}^{\#1}+\alpha\beta$	$\sigma_{2-}^{\#1}\alpha\beta\chi$
$\sigma_{2+}^{\#1}+\alpha\beta$	$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$
$\tau_{2+}^{\#1}+\alpha\beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$
$\sigma_{2-}^{\#1}+\alpha\beta\chi$	0	$\frac{2}{t_1}$

$\omega_{0+}^{\#1}+$	$f_{0+}^{\#1}+$	$f_{0+}^{\#2}+$	$\omega_{0-}^{\#1}+$
$\omega_{0+}^{\#1}+$	$t_3$	$-i\sqrt{2}kt_3$	0
$f_{0+}^{\#1}+$	$i\sqrt{2}kt_3$	$2k^2t_3$	0
$f_{0+}^{\#2}+$	0	0	0
$\omega_{0-}^{\#1}+$	0	0	$-t_1$