

## Lagrangian density

$$2\beta^2\phi^2 + \alpha^2\beta^2 h_{\alpha\mu\nu} h^{\alpha\mu\nu} - 3\alpha^2\beta^2 h^\alpha{}_\mu h^\nu{}_\nu +$$

$$\frac{1}{2}\phi\partial_\alpha\partial^\alpha\phi + \alpha\beta h^\mu{}_\alpha h^\mu{}_\mu \partial^\alpha\phi - \frac{3}{2}\alpha^2 h^\alpha{}_\mu \partial_\rho\partial^\rho h^\nu{}_\nu +$$

$$3\alpha^2 h^{\alpha\mu\nu} \partial_\rho\partial_\nu h^\rho{}_\mu + 6\alpha^2 h^\alpha{}_\mu \partial_\rho\partial^\rho h^\nu{}_\nu +$$

$$\alpha^2 h^{\alpha\mu\nu} \partial_\rho\partial^\rho h_{\alpha\mu\nu} - 3\alpha^2 h^\alpha{}_\mu \partial_\rho\partial^\rho h^\nu{}_\nu$$

Added source term:  $\phi\rho + h^{\alpha\beta\chi} \mathcal{F}_{\alpha\beta\chi}$

(No source constraints)

| $\mathcal{F}_{0+}^{\#1}$  | $\mathcal{F}_{0+}^{\#2}$  | $\rho_{0+}^{\#1}$   |
|---|---|---|
| $\mathcal{F}_{0+}^{\#1} + \frac{16\beta^4 - 39\beta^2 k^2 + 9k^4}{40\alpha^2\beta^6}$ | $\mathcal{F}_{0+}^{\#2} - \frac{24\beta^4 - 17\beta^2 k^2 + 3k^4}{40\alpha^2\beta^6}$ | $\rho_{0+}^{\#1} \frac{i k (\beta^2 + 3k^2)}{20\alpha\beta^5}$    |
| $\mathcal{F}_{0+}^{\#2} - \frac{24\beta^4 - 17\beta^2 k^2 + 3k^4}{40\alpha^2\beta^6}$ | $\mathcal{F}_{0+}^{\#2} - \frac{16\beta^4 - 7\beta^2 k^2 + k^4}{40\alpha^2\beta^6}$   | $\rho_{0+}^{\#1} \frac{i (\beta-k) k (\beta+k)}{20\alpha\beta^5}$ |
| $\rho_{0+}^{\#1} - \frac{i k (\beta^2 + 3k^2)}{20\alpha\beta^5}$                      | $\rho_{0+}^{\#1} \frac{i k (-\beta^2 + k^2)}{20\alpha\beta^5}$                        | $\rho_{0+}^{\#1} \frac{5\beta^2 + k^2}{10\beta^4}$                |

| $h_{0+}^{\#1}$  | $h_{0+}^{\#2}$                                       | $\phi_{0+}^{\#1}$                           |
|---|--|---|
| $h_{0+}^{\#1} + \frac{1}{2}\alpha^2(-4\beta^2 + k^2)$ | $h_{0+}^{\#2} \frac{3}{2}\alpha^2(-2\beta^2 + k^2)$  | $\phi_{0+}^{\#1} \frac{1}{2}i\alpha\beta k$ |
| $h_{0+}^{\#2} + \frac{3}{2}\alpha^2(-2\beta^2 + k^2)$ | $h_{0+}^{\#2} \frac{1}{2}\alpha^2(-4\beta^2 + 9k^2)$ | $\phi_{0+}^{\#1} \frac{1}{2}i\alpha\beta k$ |
| $\phi_{0+}^{\#1} - \frac{1}{2}i\alpha\beta k$         | $\phi_{0+}^{\#1} - \frac{1}{2}i\alpha\beta k$        | $\phi_{0+}^{\#1} 2\beta^2 - \frac{k^2}{2}$  |

$$\mathcal{F}_{3-}^{\#1} \alpha\beta\chi \quad \boxed{\frac{1}{\alpha^2(\beta^2 - k^2)}}$$

$$\mathcal{F}_{2+}^{\#1} + \alpha\beta \quad \boxed{\frac{1}{\alpha^2\beta^2}}$$

$$h_{2+}^{\#1} + \alpha\beta \quad \boxed{\alpha^2\beta^2}$$

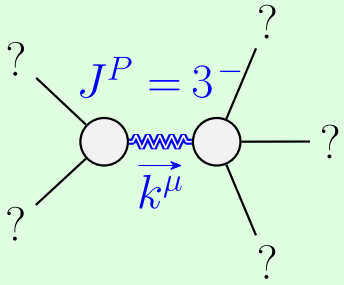
$$h_{3-}^{\#1} + \alpha\beta\chi \quad \boxed{\alpha^2(\beta - k)(\beta + k)}$$

$$h_{1-}^{\#1} + \alpha \quad \boxed{0} \quad h_{1-}^{\#2} \alpha \quad \boxed{-\sqrt{5}\alpha^2\beta^2}$$

$$h_{1-}^{\#2} + \alpha \quad \boxed{-\sqrt{5}\alpha^2\beta^2} \quad h_{1-}^{\#1} \alpha \quad \boxed{4\alpha^2(-\beta^2 + k^2)}$$

$$\mathcal{F}_{1-}^{\#1} \alpha \quad \boxed{\frac{4(\beta-k)(\beta+k)}{5\alpha^2\beta^4}} \quad \mathcal{F}_{1-}^{\#2} \alpha \quad \boxed{-\frac{1}{\sqrt{5}\alpha^2\beta^2}}$$

$$\mathcal{F}_{1-}^{\#1} + \alpha \quad \boxed{\frac{4(\beta-k)(\beta+k)}{5\alpha^2\beta^4}} \quad \mathcal{F}_{1-}^{\#2} + \alpha \quad \boxed{0}$$



| Massive particle |                          |
|------------------|--------------------------|
| Pole residue:    | $\frac{1}{\alpha^2} > 0$ |
| Polarisations:   | 7                        |
| Square mass:     | $\beta^2 > 0$            |
| Spin:            | 3                        |
| Parity:          | Odd                      |

(No massless particles)

$$\alpha < 0 \parallel \alpha > 0 \&\& \beta < 0 \parallel \beta > 0$$

Unitarity conditions