

| Massive particle | |
|------------------|-----------------------|
| Pole residue: | $-\frac{1}{r_2} > 0$ |
| Polarisations: | 1 |
| Square mass: | $\frac{t_1}{r_2} > 0$ |
| Spin: | 0 |
| Parity: | Odd |

$$\frac{r_2 < 0 \ \& \ t_1 < 0}{\text{Unitarity conditions}}$$

(No massless particles)

| $\omega_{1^+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1^+}^{\#2} \dagger^{\alpha\beta}$ | $f_{1^+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1^+}^{\#1} \dagger^{\alpha}$ | $\omega_{1^+}^{\#2} \dagger^{\alpha}$ | $f_{1^+}^{\#1} \dagger^{\alpha}$ | $f_{1^+}^{\#2} \dagger^{\alpha}$ |
|--|--|---------------------------------------|---------------------------------------|---|----------------------------------|--|
| $\omega_{1^+}^{\#1} \dagger^{\alpha\beta}$ | $-\frac{t_1}{2}$ | $-\frac{t_1}{\sqrt{2}}$ | $-\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | 0 |
| $\omega_{1^+}^{\#2} \dagger^{\alpha\beta}$ | $-\frac{t_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 |
| $f_{1^+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 |
| $\omega_{1^+}^{\#1} \dagger^{\alpha}$ | 0 | 0 | $\frac{1}{6}(t_1+4t_3)$ | $\frac{t_{1-2}t_3}{3\sqrt{2}}$ | 0 | $\frac{1}{3}\bar{i}k(t_1-2t_3)$ |
| $\omega_{1^+}^{\#2} \dagger^{\alpha}$ | 0 | 0 | $\frac{t_{1-2}t_3}{3\sqrt{2}}$ | $\frac{t_1+t_3}{3}$ | 0 | $\frac{1}{3}\bar{i}\sqrt{2}k(t_1+t_3)$ |
| $f_{1^+}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1^+}^{\#2} \dagger^{\alpha}$ | 0 | 0 | $-\frac{1}{3}\bar{i}k(t_1-2t_3)$ | $-\frac{1}{3}\bar{i}\sqrt{2}k(t_1+t_3)$ | 0 | $\frac{2}{3}k^2(t_1+t_3)$ |

Lagrangian density

$$-\frac{1}{3}t_1\omega_{\lambda'}^{\alpha\iota}\omega_{\kappa\alpha}^{\kappa}+\frac{2}{3}t_3\omega_{\lambda'}^{\alpha\iota}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\kappa\lambda'}^{\kappa}\omega_{\lambda'}^{\iota}+\frac{2}{3}r_2\partial^\beta\omega_{\kappa}^{\theta\alpha}\partial_\theta\omega_{\alpha\beta}^{\kappa}-$$

$$\frac{1}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\alpha\beta\theta}-\frac{2}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\theta\alpha\beta}-\frac{1}{2}t_1\partial^\alpha f_{\theta\kappa}^{\kappa}f_{\alpha}^{\theta}-$$

$$\frac{1}{2}t_1\partial^\alpha f_{\kappa\theta}^{\kappa}\partial^\kappa f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\alpha\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^\kappa f_{\lambda'}^{\lambda}-$$

$$\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^\kappa f_{\lambda'}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\lambda}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\lambda}+\frac{2}{3}t_1\partial^\alpha f_{\kappa\alpha}^{\kappa}\partial^\kappa f_{\lambda'}^{\lambda}-$$

$$\frac{4}{3}t_3\partial^\alpha f_{\kappa\alpha}^{\kappa}\partial^\kappa f_{\lambda'}^{\lambda}-\frac{1}{3}t_1\partial_\kappa f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\lambda}+\frac{2}{3}t_3\partial_\kappa f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\lambda}+2t_1\omega_{\iota\kappa\theta}^{\iota}\partial^\kappa f^{\iota\theta}-$$

$$\frac{1}{3}t_1\omega_{\iota\alpha}^{\alpha}\partial^\kappa f_{\kappa}^{\lambda}+\frac{2}{3}t_3\omega_{\iota\alpha}^{\alpha}\partial^\kappa f_{\kappa}^{\lambda}-\frac{1}{3}t_1\omega_{\lambda\lambda'}^{\lambda}\partial^\kappa f_{\lambda'}^{\lambda}+\frac{2}{3}t_3\omega_{\lambda\lambda'}^{\lambda}\partial^\kappa f_{\lambda'}^{\lambda}+$$

$$\frac{1}{2}t_1\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\lambda\alpha}^{\lambda}+\frac{1}{2}t_1\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}+\frac{1}{2}t_1\partial_\kappa f_{\lambda}^{\lambda}\partial^\kappa f_{\theta}^{\theta}-$$

$$\frac{1}{3}t_1\partial^\alpha f_{\alpha}^{\lambda}\partial^\kappa f_{\lambda\kappa}^{\kappa}+\frac{2}{3}t_3\partial^\alpha f_{\alpha}^{\lambda}\partial^\kappa f_{\lambda\kappa}^{\kappa}+\frac{1}{3}r_2\partial_\kappa\omega^{\alpha\beta\theta}\partial^\kappa\omega_{\alpha\beta\theta}+$$

$$\frac{2}{3}r_2\partial_\kappa\omega^{\theta\alpha\beta}\partial^\kappa\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^\beta\omega_{\alpha\beta}^{\lambda\iota}\partial_\lambda\omega_{\alpha\beta}^{\iota}+\frac{2}{3}r_2\partial^\beta\omega_{\lambda'}^{\alpha}\partial_\lambda\omega_{\alpha\beta}^{\lambda'}$$

Added source term:

$f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

| $Q_{0^+}^{\#1} \dagger$ | $Q_{0^+}^{\#1} \dagger$ | $\tau_{0^+}^{\#1} \dagger$ | $Q_{0^+}^{\#1} \dagger$ |
|----------------------------|------------------------------------|-------------------------------------|-------------------------|
| $Q_{0^+}^{\#1} \dagger$ | 0 | 0 | 0 |
| $\tau_{0^+}^{\#1} \dagger$ | $\frac{1}{(1+2k^2)^2t_3}$ | $-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$ | 0 |
| $\tau_{0^+}^{\#2} \dagger$ | $\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$ | $\frac{2k^2}{(1+2k^2)^2t_3}$ | 0 |
| $Q_{0^+}^{\#1} \dagger$ | 0 | 0 | 0 |
| $Q_{0^+}^{\#1} \dagger$ | 0 | 0 | $\frac{1}{k^2r_2-t_1}$ |

| $\sigma_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\tau_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{2^+}^{\#1} \dagger^{\alpha\beta\chi}$ |
|--|--|--|--|
| $\sigma_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{2}{(1+2k^2)^2t_1}$ | $-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$ | 0 |
| $\tau_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$ | $\frac{4k^2}{(1+2k^2)^2t_1}$ | 0 |
| $\sigma_{2^+}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | 0 | $\frac{2}{t_1}$ |

| $\omega_{0^+}^{\#1} \dagger$ | $f_{0^+}^{\#1} \dagger$ | $f_{0^+}^{\#2} \dagger$ | $\omega_{0^+}^{\#1} \dagger$ |
|------------------------------|-------------------------|-------------------------|------------------------------|
| $\omega_{0^+}^{\#1} \dagger$ | t_3 | $-i\sqrt{2}kt_3$ | 0 |
| $f_{0^+}^{\#1} \dagger$ | $i\sqrt{2}kt_3$ | $2k^2t_3$ | 0 |
| $f_{0^+}^{\#2} \dagger$ | 0 | 0 | 0 |
| $\omega_{0^+}^{\#1} \dagger$ | 0 | 0 | $k^2r_2-t_1$ |

| $\omega_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{2^+}^{\#1} \dagger^{\alpha\beta\chi}$ |
|--|--|--|
| $\omega_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{t_1}{2}$ | $-\frac{ikt_1}{\sqrt{2}}$ |
| $f_{2^+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{ikt_1}{\sqrt{2}}$ | k^2t_1 |
| $\omega_{2^+}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | $\frac{t_1}{2}$ |

| Source constraints | |
|---|----|
| SO(3) irreps | # |
| $\tau_{0^+}^{\#2} == 0$ | 1 |
| $\tau_{0^+}^{\#1}-2\bar{i}k\sigma_{0^+}^{\#1} == 0$ | 1 |
| $\tau_{1^+}^{\#2\alpha}+2\bar{i}k\sigma_{1^+}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1^+}^{\#1\alpha} == 0$ | 3 |
| $\tau_{1^+}^{\#1\alpha\beta}+\bar{i}k\sigma_{1^+}^{\#2\alpha\beta} == 0$ | 3 |
| $\tau_{2^+}^{\#1\alpha\beta}-2\bar{i}k\sigma_{2^+}^{\#1\alpha\beta} == 0$ | 5 |
| Total #: | 16 |