

Particle spectrograph

Wave operator and propagator

| $\sigma_{1+}^{\#1} \dagger \alpha\beta$ | $\sigma_{1+}^{\#2} \dagger \alpha\beta$ | $\tau_{1+}^{\#1} \dagger \alpha\beta$ | $\sigma_{1-}^{\#1} \alpha$ | $\sigma_{1-}^{\#2} \alpha$ | $\tau_{1-}^{\#1} \alpha$ | $\tau_{1-}^{\#2} \alpha$ |
|--|---|--|---|---|--------------------------|---|
| 0 | $\frac{2\sqrt{2}}{\alpha_0 + \alpha_0 k^2}$ | $-\frac{2i\sqrt{2}k}{\alpha_0 + \alpha_0 k^2}$ | 0 | 0 | 0 | 0 |
| $\frac{2\sqrt{2}}{\alpha_0 + \alpha_0 k^2}$ | $-\frac{2}{\alpha_0(1+k^2)^2}$ | $-\frac{2ik}{\alpha_0(1+k^2)^2}$ | 0 | 0 | 0 | 0 |
| $-\frac{2i\sqrt{2}k}{\alpha_0 + \alpha_0 k^2}$ | $\frac{2ik}{\alpha_0(1+k^2)^2}$ | $-\frac{2k^2}{\alpha_0(1+k^2)^2}$ | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $-\frac{2\sqrt{2}}{\alpha_0 + 2\alpha_0 k^2}$ | $-\frac{2\sqrt{2}}{\alpha_0 + 2\alpha_0 k^2}$ | 0 | $-\frac{4ik}{\alpha_0 + 2\alpha_0 k^2}$ |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $\frac{4ik}{\alpha_0 + 2\alpha_0 k^2}$ | $\frac{2i\sqrt{2}k}{\alpha_0(1+2k^2)^2}$ | 0 | $-\frac{4k^2}{\alpha_0(1+2k^2)^2}$ |

Quadratic (free) action

$$\mathcal{S} = \iiint (f^{\alpha\beta} \tau_{\alpha\beta} + \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + \alpha_0 (-\frac{1}{2} \omega_{\alpha\zeta\beta} \omega^{\alpha\beta\zeta} - \frac{1}{2} \omega^{\alpha\beta}_{\alpha} \omega_{\beta}^{\zeta\zeta} - f^{\alpha\beta} \partial_{\beta} \omega_{\alpha}^{\zeta\zeta} + \partial_{\beta} \omega^{\alpha\beta}_{\alpha} + f^{\alpha\beta} \partial_{\zeta} \omega_{\alpha}^{\zeta\zeta} - f^{\alpha}_{\alpha} \partial_{\zeta} \omega^{\beta\zeta}_{\beta})) [t, x, y, z] dz dy dx dt$$

| $\omega_{2+}^{\#1} \dagger \alpha\beta$ | $f_{2+}^{\#1} \dagger \alpha\beta$ | $\omega_{2-}^{\#1} \alpha\beta\chi$ |
|---|------------------------------------|-------------------------------------|
| $-\frac{\alpha_0}{4}$ | $\frac{i\alpha_0 k}{2\sqrt{2}}$ | 0 |
| $-\frac{i\alpha_0 k}{2\sqrt{2}}$ | 0 | 0 |
| 0 | 0 | $-\frac{\alpha_0}{4}$ |

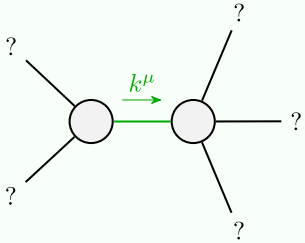
| $\omega_{1+}^{\#1} \dagger \alpha\beta$ | $\omega_{1+}^{\#2} \dagger \alpha\beta$ | $f_{1+}^{\#1} \dagger \alpha\beta$ | $\omega_{1-}^{\#1} \alpha$ | $\omega_{1-}^{\#2} \alpha$ | $f_{1-}^{\#1} \alpha$ | $f_{1-}^{\#2} \alpha$ |
|---|---|------------------------------------|-------------------------------|-------------------------------|-----------------------------|-----------------------|
| $\frac{\alpha_0}{4}$ | $\frac{\alpha_0}{2\sqrt{2}}$ | $\frac{i\alpha_0 k}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 |
| $\frac{\alpha_0}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $-\frac{i\alpha_0 k}{2\sqrt{2}}$ | 0 | 0 | $\frac{\alpha_0}{4}$ | $-\frac{\alpha_0}{2\sqrt{2}}$ | $-\frac{1}{2} i \alpha_0 k$ | 0 |
| 0 | 0 | 0 | $-\frac{\alpha_0}{2\sqrt{2}}$ | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $\frac{i\alpha_0 k}{2}$ | 0 | 0 | 0 |

| $\sigma_{0+}^{\#1} \dagger$ | $\tau_{0+}^{\#1} \dagger$ | $\tau_{0+}^{\#2} \dagger$ | $\sigma_{0-}^{\#1} \dagger$ |
|--------------------------------|---------------------------------|---------------------------|-----------------------------|
| 0 | $-\frac{i\sqrt{2}}{\alpha_0 k}$ | 0 | 0 |
| $\frac{i\sqrt{2}}{\alpha_0 k}$ | $-\frac{1}{\alpha_0 k^2}$ | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $\frac{2}{\alpha_0}$ |

| $\sigma_{2+}^{\#1} \dagger \alpha\beta$ | $\tau_{2+}^{\#1} \dagger \alpha\beta$ | $\sigma_{2-}^{\#1} \alpha\beta\chi$ |
|---|---------------------------------------|-------------------------------------|
| 0 | $\frac{2i\sqrt{2}}{\alpha_0 k}$ | 0 |
| $-\frac{2i\sqrt{2}}{\alpha_0 k}$ | $\frac{2}{\alpha_0 k^2}$ | 0 |
| 0 | 0 | $-\frac{4}{\alpha_0}$ |

| Source constraints/gauge generators | |
|---|----------------|
| SO(3) irreps | Multiplicities |
| $\tau_{0+}^{\#2} == 0$ | 1 |
| $\tau_{1-}^{\#2\alpha} + 2ik \sigma_{1-}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1-}^{\#1\alpha} == 0$ | 3 |
| $\tau_{1+}^{\#1\alpha\beta} + ik \sigma_{1+}^{\#2\alpha\beta} == 0$ | 3 |
| Total constraints: | 10 |

Massive and massless spectra



| | |
|----------------|--------------------------|
| Quadratic pole | |
| Pole residue: | $\frac{1}{\alpha_0} > 0$ |
| Polarisations: | 2 |

(No massive particles)

Unitarity conditions

$\alpha_0 > 0$