## Particle spectrograph

## Wave operator and propagator

Wave	op	per	ator	and	d b	rop	ag	ato	r																										
			$\omega_{1}^{\#1}{}_{\alpha\beta}$		$\omega_1^{\scriptscriptstyle\#}$	±2 + αβ	f	#1 1 <sup>+</sup> αβ			$\omega_{1}^{\#1}$	!		$\omega_1^{#2}$	ά	$f_1^{#1}$	α	$f_1^{#2}$	α						1 0	1				7	1				
$\omega_{1}^{\sharp 1} \dagger^{lpha eta}$	$k^2$	<sup>2</sup> (2 r	$_3 + r_5$ )	$+\frac{2t_2}{3}$		2 t <sub>2</sub> 3	$\frac{1}{3}$ $\bar{I}$	$\sqrt{2} k$	$t_2$		0			0		0		0		# <sub>1</sub>	5	o	0	0	$\frac{1}{k^2 r_2 + t_2}$	$\omega_{0^{-}}^{\#1}$	0	0	0	$k^2 r_2 + t_2$					
$\omega_{1^+}^{\#2}\dagger^{lphaeta}$	3		$\frac{\sqrt{2} t_2}{3}$		-	<u>*2</u> 3		i k t <u>2</u> 3			0			0		0		0		7#2		0	0	0	0	$f_{0}^{#2}$	0	0	0	0	agx				0
$f_{1}^{\#1} \dagger^{\alpha\beta}$	3	- <u>1</u> 3	ī √2 k	$t_2$	$-\frac{1}{3}$	īkt <sub>2</sub>	<u> </u>	k <sup>2</sup> t <sub>2</sub> 3			0			0		0		0		$I_{\perp}^{\#1}$	0 <sup>1</sup> √2 <i>k</i>	$(1+2k^2)^2t_3$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0	0		; t3	$k^2 t_3$			$\beta \omega_{2}^{#1}{}_{\alpha\beta\gamma}$				
$\omega_1^{\#1} \dagger^lpha$	2		0			0		0	k	$\frac{2}{2} \left( \frac{r_3}{2} \right)$	+ r <sub>5</sub> )	$+\frac{2t}{3}$		$-\frac{\sqrt{2}}{3}$		0		$-\frac{2}{3} \bar{l} k$				<u> </u>				# f	-ī √2 k	2 K <sup>2</sup>	0	0	$f_{2}^{\#1}_{\alpha\beta}$			>	0
$\omega_1^{\#2} \dagger^{lpha}$			0			0		0				$\frac{\sqrt{2} t}{3}$	3	<u>t</u> 3 3		0	<u>1</u> 3	<i>ī</i> √2	kt <sub>3</sub>	$\sigma_{i+1}^{\#1}$	1 0	$(1+2k^2)^2t_3$	$i \sqrt{2} k $ (1+2 $k^2$ ) <sup>2</sup> $t_3$	0	0	$\omega_{0}^{\#1}$	t <sub>3</sub>	$\frac{2}{2}kt_3$	0	0	$\omega_{2}^{\#1}{}_{\alpha B}$	3 4 2 13	2 0	<b>&gt;</b>	0
$f_{1}^{#1} \dagger^{\alpha}$			0			0		0					0 1	0		0		0						+	+	] 3		Ī	<u> </u>	<u> </u>	]	$\omega_{\perp}^{*1} + \alpha \beta$	+αβ	72+ 1	۲ ما
$f_{1}^{#2} \dagger^{\alpha}$			0			0		0				2 i kt	3 - 1	<i>ī</i> √2	kt <sub>3</sub>	0		$\frac{2k^2t}{3}$	<u>3</u>		#1	0°.÷ T	$\tau_0^{\#1}$ †	$\tau_{0}^{\#2}$ .	$\sigma_{0}^{\#1}$ .		$\omega_{0}^{\#1}$ †	$f_{0}^{\#1}$	$f_0^{#2}$ †	$\omega_{0^{\text{-}}}^{\#1}$		$\omega_{\perp}^{\#1}$	~2.	72+	$\omega_{2}^{\#_{1}} + \alpha^{\mu \chi}$
traints	SO(3) irreps Fundamental fields Multiplicities	$\tau_0^{\#2} == 0 \qquad \qquad  \partial_\beta \partial_\alpha \tau^{\alpha\beta} == 0 \qquad \qquad 1$	$\tau_0^{\#1} - 2 i k \sigma_0^{\#1} == 0$ xAct`xTensor`Private`Reconstruct[ 1 Symmetry[4, $\sqrt{3} \partial^{\bullet} \partial^$	$\{\bullet 1 \rightarrow b, \bullet 2 \rightarrow -a, \bullet 3 \rightarrow -b,$	●4 → a}, StrongGenSet[	{a, -a, b, -b}[{1, 3, 5, 2}]]}]==	$\sqrt{3} \left( \partial_{\beta} \partial^{\beta} \tau^{\alpha}_{\alpha} + 2  \partial_{\chi} \partial^{\chi} \partial_{\beta} \sigma^{\alpha\beta}_{\alpha} \right)$	$\tau_{1}^{\#2}{}^{\alpha} + 2ik \sigma_{1}^{\#2}{}^{\alpha} = 0  \partial_{\chi}\partial_{\beta}\partial^{\alpha}\tau^{\beta\chi} = \partial_{\chi}\partial^{\chi}\partial_{\beta}\tau^{\alpha\beta} + 2\partial_{\delta}\partial^{\delta}\partial_{\chi}\partial_{\beta}\sigma^{\alpha\beta\chi}  3$	$\tau_{1}^{\#1}{}^{\alpha} := 0 \qquad \qquad \partial_{\chi}\partial_{\beta}\partial^{\alpha}\tau^{\beta\chi} := \partial_{\chi}\partial^{\chi}\partial_{\beta}\tau^{\beta\alpha} \qquad 3$	$\frac{\partial}{\partial x} + i k  \sigma_{1}^{\#2} \alpha \beta = 0  \left  \frac{\partial}{\partial y} \partial^{\alpha} \tau^{\beta X} + \frac{\partial}{\partial y} \partial^{\beta} \tau^{X \alpha} + \frac{\partial}{\partial y} \partial^{X} \tau^{\alpha \beta} + $		$\partial_{\chi}\partial^{\alpha} \tau^{\chi\beta} + \partial_{\chi}\partial^{\beta} \tau^{\alpha\chi} +$	$\partial_{\chi}\partial^{\chi}\tau^{\beta\alpha} + 2\partial_{\delta}\partial_{\chi}\partial^{\beta}\sigma^{\alpha\chi\delta}$	$\sigma_{2}^{\#1}{}^{\alpha\beta\chi} == 0 \qquad 3 \partial_{\varepsilon} \partial_{\delta} \partial^{\chi} \partial^{\alpha} \sigma^{\beta\delta\varepsilon} + 3 \partial_{\varepsilon} \partial^{\varepsilon} \partial^{\chi} \partial^{\alpha} \sigma^{\beta\delta}{}_{\delta} + \qquad 5$	$2  \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\alpha \chi \delta} + 4  \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial_{\delta}$	$2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\beta} \sigma^{\chi \delta \alpha} + 4 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\alpha \beta \delta} +$	$2 \partial_{\varepsilon} \partial^{\varepsilon} \partial_{\delta} \partial^{\chi} \sigma^{\alpha \delta \beta} + 2 \partial_{\varepsilon} \partial^{\varepsilon} \partial_{\delta} \partial^{\delta} \sigma^{\beta \chi \alpha} +$	$3 \eta^{\beta \chi} \partial_{\phi} \partial^{\phi} \partial_{\varepsilon} \partial^{\alpha} \sigma^{\delta \varepsilon}_{\kappa} +$	$3 \eta^{\alpha\chi} \partial_{\phi} \partial_{\phi} \partial_{\varepsilon} \partial_{\delta} \sigma^{\beta\delta\varepsilon} +$	$3 \eta^{\beta \chi} \partial_{\phi} \partial^{\phi} \partial_{\varepsilon} \partial^{\varepsilon} \sigma^{\alpha \delta}{}_{\delta} ==$	$3 \partial_{\epsilon} \partial_{\delta} \partial^{\chi} \partial^{\beta} \sigma^{\alpha \delta \epsilon} + 3 \partial_{\epsilon} \partial^{\epsilon} \partial^{\chi} \partial^{\beta} \sigma^{\alpha \delta} \partial^{\epsilon} +$	$2 \partial_{\varepsilon} \partial^{\varepsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\beta \chi \delta} + 4 \partial_{\varepsilon} \partial^{\varepsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\beta \delta \chi} +$	$2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\alpha} \sigma^{\chi \delta \beta} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\chi} \sigma^{\beta \delta \alpha} +$	$4 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\alpha \beta \chi} + 2 \partial_{\epsilon} \partial^{\epsilon} \partial_{\delta} \partial^{\delta} \sigma^{\alpha \chi \beta} +$	$3 \eta^{\alpha\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial^{\beta} \sigma^{\delta\epsilon}{}_{\delta} +$	$3 \eta^{\beta \chi} \partial_{\phi} \partial_{\phi} \partial_{\varepsilon} \partial_{\delta} \sigma^{\alpha \delta \varepsilon} +$	$3 \eta^{\alpha\chi} \partial_{\phi} \partial^{\phi} \partial_{\varepsilon} \partial^{\varepsilon} \sigma^{\beta\delta}$	$\tau_{2+}^{\#1}{}^{\alpha\beta} == 0 \qquad 4  \partial_{\delta} \partial_{\chi} \partial^{\beta} \partial^{\alpha} \tau^{\chi \delta} + 2  \partial_{\delta} \partial^{\delta} \partial^{\alpha} \tau^{\chi}_{\chi} + \qquad 5$	$3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi} \tau^{\alpha \beta} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\chi} \tau^{\beta \alpha} +$	$2 \eta^{\alpha\beta} \partial_{\epsilon} \partial_{\delta} \partial_{\chi} \iota^{\chi\delta} ==$	$3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} t^{\beta \chi} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\alpha} t^{\chi \beta} +$	$3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta} \tau^{\alpha \chi} + 3 \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial^{\beta} \tau^{\chi \alpha} +$	$2 \eta^{\alpha\beta} \partial_{\epsilon} \partial_{\delta} \partial^{\epsilon} \chi_{\chi}$	Total constraints/gauge generators:	

Quadratic (free) action	$S == \iiint \left( \frac{1}{6} \left( -4  t_3  \omega^{\alpha \prime}_{\alpha}  \omega^{\kappa}_{\prime  \kappa} + 6  f^{\alpha \beta}  \tau_{\alpha \beta} + 6  \omega^{\alpha \beta \chi}  \sigma_{\alpha \beta \chi} + 8  t_3  \omega^{\kappa}_{\alpha  \kappa}  \partial_{\beta} f^{\alpha \prime} - \right) \right)$	$8t_3\;\omega_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{$	$3r_3\partial_i\omega_{eta}^{\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	$6 r_3 \partial' \omega^{\alpha eta}_{\alpha} \partial_{\theta} \omega^{\theta}_{eta}$ , - $3 r_3 \partial_{\alpha} \omega^{\alpha eta_l} \partial_{\theta} \omega^{\theta}_{l}$ +	$6 r_3 \partial' \omega^{\alpha \beta}_{\alpha} \partial_{\theta} \omega'_{\beta}^{\theta} + 4 t_2 \omega_{\beta \alpha} \partial^{\theta} f^{\alpha \prime} + 2 t_2 \partial_{\alpha} f_{\beta \beta} \partial^{\theta} f^{\alpha \prime} -$	$t_2  \partial_{lpha} f_{ heta_I}  \partial^{eta} f^{lpha_I} - t_2  \partial_{ec{f}} f_{lpha eta}  \partial^{eta} f^{lpha_I} + t_2  \partial_{eta} f_{lpha_I}  \partial^{eta} f^{lpha_I} -$	$t_2\partial_ heta f_{\primelpha}\partial^ heta f^{lpha\prime}$ - $4t_2\omega_{lpha heta\prime}$ ( $\omega^{lpha\prime heta}+\partial^ heta f^{lpha\prime}$ ) +	$2t_2\omega_{lpha_{eta}}(\omega^{lpha_{eta}}+2\partial^{ heta}_{eta}f^{lpha_\prime})+8r_2\partial_{eta}\omega_{lpha_{eta}}\partial^{ heta}\omega^{lphaeta_\prime}$ -	$4r_2\partial_eta \omega_{lpha  heta_I}\partial^ heta \omega^{lpha eta_I} + 4r_2\partial_eta \omega_{_I  heta lpha}\partial^ heta \omega^{lpha eta_I}$ -	$24 r_3  \partial_{\beta} \omega_{\prime eta lpha}  \partial^{\theta} \omega^{lpha eta \prime} - 2  r_2  \partial_{\prime} \omega_{lpha eta eta}  \partial^{\theta} \omega^{lpha eta \prime} +$	$2r_2\partial_ heta \omega_{lphaeta_I}\partial^ heta \omega^{lphaeta_I}$ - $4r_2\partial_ heta \omega_{lpha_Ieta}\partial^ heta \omega^{lphaeta_I}$ +	$6r_5\partial_i\omega_{eta}^{\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	$4t_3\partial_{\scriptscriptstyle I} f^{\alpha\prime}\partial_{\scriptscriptstyle K} f_{}^{ K} - 8t_3\partial^{\prime} f_{\alpha}^{}\partial_{\scriptscriptstyle K} f_{\prime}^{ K} - 6r_5\partial_{\alpha}\omega^{\alpha\prime}{}^{\theta}\partial_{\scriptscriptstyle K}\omega_{\scriptscriptstyle I}^{ K} +$	$12 r_5  \partial^{\theta} \omega^{\alpha_{\prime}}_{\alpha}  \partial_{\kappa} \omega_{\prime}^{\ \kappa}_{\ \beta} + 6 r_5  \partial_{\alpha} \omega^{\alpha_{\prime} \theta}  \partial_{\kappa} \omega_{\theta}^{\ \kappa}_{\ \prime}  -$	$12  r_5  \partial^{\theta} \omega^{lpha_{\prime}}_{$
Quadratic (free	$S == \iiint \int \left( \frac{1}{6} \left( -4 t \right) \right)$														

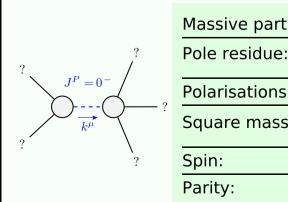
 $\tau_{1}^{\#1} \dagger^{\alpha}$ 

 $\sigma_{1}^{\#2} +^{lpha}$ 

 $\sigma_{1}^{\#_1} \! \uparrow^{\alpha}$ 

 $\tau_1^{\#1} + ^{\alpha\beta}$ 

## Massive and massless spectra



ticle									
::	$-\frac{1}{r_2} > 0$								
s:	1								
s:	$-\frac{t_2}{r_2} > 0$								
	0								
	Odd								

?	Quadratic pole	2
?	Pole residue:	$-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$
	Polarisations:	2

## Unitarity conditions

 $r_2 < 0 \& \& r_3 < 0 \& \& r_5 < -\frac{r_3}{2} \& \& t_2 > 0 \parallel r_2 < 0 \& \& r_3 < 0 \& \& r_5 > -2 r_3 \& \& t_2 > 0 \parallel r_2 < 0 \& \& r_3 > 0 \& \& -2 r_3 < r_5 < -\frac{r_3}{2} \& \& t_2 > 0$