

Source constraints	
SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2\,i\,k\,\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i\,k\,\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2\,i\,k\,\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	16

$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1} +$	$6\,k^2\,r_3$	0	0
$f_{0+}^{\#1} +$	0	0	0
$f_{0+}^{\#2} +$	0	0	0
$\omega_{0-}^{\#1} +$	0	0	$k^2\,r_2 - t_1$

$\sigma_{2+}^{\#1} + \alpha\beta$	$\tau_{2+}^{\#1} + \alpha\beta$	$\sigma_{2-}^{\#1} + \alpha\beta\chi$
$\sigma_{2+}^{\#1} + \alpha\beta$	$\frac{2}{(1+2\,k^2)^2\,t_1}$	$-\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2\,t_1}$
$\tau_{2+}^{\#1} + \alpha\beta$	$\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2\,t_1}$	$\frac{4\,k^2}{(1+2\,k^2)^2\,t_1}$
$\sigma_{2-}^{\#1} + \alpha\beta\chi$	0	$\frac{2}{t_1}$

$\sigma_{0+}^{\#1}$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\sigma_{0+}^{\#1} +$	$\frac{1}{6\,k^2\,r_3}$	0	0
$\tau_{0+}^{\#1} +$	0	0	0
$\tau_{0+}^{\#2} +$	0	0	0
$\sigma_{0-}^{\#1} +$	0	0	$\frac{1}{k^2\,r_2 - t_1}$

$\omega_{2+}^{\#1}$	$f_{2+}^{\#1}$	$\omega_{2-}^{\#1}$
$\omega_{2+}^{\#1} + \alpha\beta$	$\frac{t_1}{2}$	$-\frac{i\,k\,t_1}{\sqrt{2}}$
$f_{2+}^{\#1} + \alpha\beta$	$\frac{i\,k\,t_1}{\sqrt{2}}$	$k^2\,t_1$
$\omega_{2-}^{\#1} + \alpha\beta\chi$	0	$\frac{t_1}{2}$

Lagrangian density

$$\begin{aligned}
 &-\frac{1}{3}t_1\,\omega_{,\alpha'}\,\omega_{\kappa\alpha}{}^\kappa-t_1\,\omega_{,\kappa\lambda}{}^\lambda\,\omega_{\kappa\lambda}{}^{'-} - 2\,r_3\,\partial_{,\omega}\omega_{\kappa}{}^\lambda\,\partial'\omega_{\lambda}{}^\alpha- \\
 &r_5\,\partial_{,\omega}\omega_{\kappa}{}^\lambda\,\partial'\omega_{\lambda}{}^\alpha + \frac{2}{3}r_2\,\partial^\beta\omega_{\kappa}{}^\theta\partial_\theta\omega_{\alpha\beta}{}^\kappa - \frac{1}{3}r_2\,\partial_\theta\omega_{\alpha\beta}{}^\kappa\,\partial_\kappa\omega^{\theta\alpha} - r_5\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\theta\kappa\lambda}- \\
 &\frac{2}{3}r_2\,\partial_\theta\omega_{\alpha\beta}{}^\kappa\,\partial_\kappa\omega^{\theta\alpha\beta} + 2\,r_3\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\theta\kappa\lambda} - r_5\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial_\theta\omega^{\theta\kappa\lambda}- \\
 &2\,r_3\,\partial_\theta\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\theta\kappa\lambda} + r_5\,\partial_\theta\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\theta\kappa\lambda} - 2\,r_3\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\kappa\lambda\theta}- \\
 &r_5\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\kappa\lambda\theta} + 4\,r_3\,\partial_\theta\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\kappa\lambda\theta} + 2\,r_5\,\partial_\theta\omega_{\lambda}{}^\alpha\,\partial_\kappa\omega^{\kappa\lambda\theta}- \\
 &\frac{1}{2}t_1\,\partial^\alpha f_{\theta\kappa}{}^\alpha\,\partial^\kappa f_{\alpha}{}^\theta - \frac{1}{2}t_1\,\partial^\alpha f_{\kappa\theta}{}^\alpha\,\partial^\kappa f_{\alpha}{}^\theta - \frac{1}{2}t_1\,\partial^\alpha f_{\lambda}{}^\kappa\,\partial^\kappa f_{\alpha\lambda}{}^\lambda + \\
 &\frac{1}{3}t_1\,\omega_{\kappa\alpha}{}^\alpha\,\partial^\kappa f_{,\lambda}{}^\lambda + \frac{1}{3}t_1\,\omega_{\kappa\lambda}{}^\lambda\,\partial^\kappa f_{,\lambda}{}^\lambda + \frac{2}{3}t_1\,\partial^\alpha f_{\kappa\alpha}{}^\lambda\,\partial^\kappa f_{,\lambda}{}^\lambda - \frac{1}{3}t_1\,\partial_\kappa f_{\lambda}{}^\lambda\,\partial^\kappa f_{,\lambda}{}^\lambda + \\
 &2\,t_1\,\omega_{\kappa\theta}{}^\theta\,\partial^\kappa f_{,\theta}{}^\lambda - \frac{1}{3}t_1\,\omega_{,\alpha}{}^\alpha\,\partial^\kappa f_{\kappa}{}^\lambda - \frac{1}{3}t_1\,\omega_{\lambda}{}^\lambda\,\partial^\kappa f_{\kappa}{}^\lambda + \frac{1}{2}t_1\,\partial^\alpha f_{\lambda}{}^\lambda\,\partial^\kappa f_{\lambda\alpha}{}^\lambda + \\
 &\frac{1}{2}t_1\,\partial_\kappa f_{\theta}{}^\lambda\,\partial^\kappa f_{\lambda}{}^\theta + \frac{1}{2}t_1\,\partial_\kappa f_{\lambda}{}^\theta\,\partial^\kappa f_{\theta}{}^\lambda - \frac{1}{3}t_1\,\partial^\alpha f_{\lambda}{}^\alpha\,\partial^\kappa f_{\lambda\kappa}{}^\kappa + \\
 &\frac{1}{3}r_2\,\partial_\kappa\omega^{\alpha\beta\theta}\,\partial^\kappa\omega_{\alpha\beta\theta} + \frac{2}{3}r_2\,\partial_\kappa\omega^{\theta\alpha\beta}\,\partial^\kappa\omega_{\alpha\beta\theta} - \frac{2}{3}r_2\,\partial^\beta\omega_{,\lambda}{}^\alpha\partial_\lambda\omega_{\alpha\beta}{}^{'-} + \\
 &\frac{2}{3}r_2\,\partial^\beta\omega_{,\lambda}{}^\alpha\partial_\lambda\omega_{\alpha\beta}{}^{'-} - 4\,r_3\,\partial^\beta\omega_{,\lambda}{}^\alpha\partial_\lambda\omega_{\alpha\beta}{}^{'-} - 2\,r_3\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial_\theta\omega^{\theta\lambda\kappa}{}_\kappa + \\
 &r_5\,\partial_\alpha\omega_{\lambda}{}^\alpha\,\partial^\lambda\omega^{\theta\kappa}{}_\kappa + 2\,r_3\,\partial_\theta\omega_{\lambda}{}^\alpha\,\partial^\lambda\omega^{\theta\kappa}{}_\kappa - r_5\,\partial_\theta\omega_{\lambda}{}^\alpha\,\partial^\lambda\omega^{\theta\kappa}{}_\kappa
 \end{aligned}$$

Added source term: $|f^{\alpha\beta}\,\tau_{\alpha\beta} + \omega^{\alpha\beta\chi}\,\sigma_{\alpha\beta\chi}$

$\sigma_{1+}^{\#1} + \alpha\beta$	$\sigma_{1+}^{\#2} + \alpha\beta$	$\tau_{1+}^{\#1} + \alpha\beta$	$\sigma_{1-}^{\#1} + \alpha$	$\sigma_{1-}^{\#2} + \alpha$	$\tau_{1-}^{\#1} + \alpha$	$\tau_{1-}^{\#2} + \alpha$
0	$-\frac{\sqrt{2}}{t_1 + k^2\,t_1}$	$-\frac{i\,\sqrt{2}\,k}{t_1 + k^2\,t_1}$	0	0	0	0
$\sigma_{1+}^{\#2} + \alpha\beta$	$-\frac{\sqrt{2}}{t_1 + k^2\,t_1}$	$\frac{-2\,k^2\,(2\,r_3 + r_5) + t_1}{(1 + k^2)^2\,t_1^2}$	0	0	0	0
$\tau_{1+}^{\#1} + \alpha\beta$	$\frac{i\,\sqrt{2}\,k}{t_1 + k^2\,t_1}$	$\frac{i\,(2\,k^3\,(2\,r_3 + r_5) - k\,t_1)}{(1 + k^2)^2\,t_1^2}$	0	0	0	0
$\sigma_{1-}^{\#1} + \alpha$	0	0	$\frac{1}{k^2\,(2\,r_3 + r_5)}$	$-\frac{1}{\sqrt{2}\,(k^2 + 2\,k^4)\,(2\,r_3 + r_5)}$	0	0
$\sigma_{1-}^{\#2} + \alpha$	0	0	0	$\frac{6\,k^2\,(2\,r_3 + r_5) + t_1}{2\,(k + 2\,k^3)^2\,(2\,r_3 + r_5)\,t_1}$	0	0
$\tau_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2} + \alpha$	0	0	$\frac{i}{k\,(1 + 2\,k^2)\,(2\,r_3 + r_5)}$	$-\frac{i\,(6\,k^2\,(2\,r_3 + r_5) + t_1)}{\sqrt{2}\,k\,(1 + 2\,k^2)^2\,(2\,r_3 + r_5)\,t_1}$	0	$\frac{6\,k^2\,(2\,r_3 + r_5) + t_1}{(1 + 2\,k^2)^2\,(2\,r_3 + r_5)\,t_1}$

$\omega_{1+}^{\#1} + \alpha\beta$	$\omega_{1+}^{\#2} + \alpha\beta$	$f_{1+}^{\#1} + \alpha\beta$	$\omega_{1-}^{\#1} + \alpha$	$\omega_{1-}^{\#2} + \alpha$	$f_{1-}^{\#1} + \alpha$	$f_{1-}^{\#2} + \alpha$
$\omega_{1+}^{\#1} + \alpha\beta$	$k^2\,(2\,r_3 + r_5) - \frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{i\,k\,t_1}{\sqrt{2}}$	0	0	0
$\omega_{1+}^{\#2} + \alpha\beta$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$f_{1+}^{\#1} + \alpha\beta$	$\frac{i\,k\,t_1}{\sqrt{2}}$	0	0	0	0	0
$\omega_{1-}^{\#1} + \alpha$	0	0	0	$k^2\,(2\,r_3 + r_5) + \frac{t_1}{6}$	$\frac{t_1}{3\,\sqrt{2}}$	0
$\omega_{1-}^{\#2} + \alpha$	0	0	0	$\frac{t_1}{3\,\sqrt{2}}$	$\frac{t_1}{3}$	$\frac{1}{3}\,i\,\sqrt{2}\,k\,t_1$
$f_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$f_{1-}^{\#2} + \alpha$	0	0	0	$-\frac{1}{3}\,i\,k\,t_1$	$-\frac{1}{3}\,i\,\sqrt{2}\,k\,t_1$	$\frac{2\,k^2\,t_1}{3}$

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$\frac{t_1}{r_2} > 0$
Spin:	0
Parity:	Odd

Quadratic pole	
Pole residue:	$-\frac{1}{(2\,r_3 + r_5)\,t_1^2} > 0$
Polarisations:	2

Unitarity conditions

$$r_2 < 0 \ \&\& \ r_5 < -2\,r_3 \ \&\& \ t_1 < 0$$