

$$S = \iiint \left( \frac{1}{6} (6t_1 \mathcal{I}_{\alpha\beta}^{\alpha'} \mathcal{I}_{\theta}^{\theta} + 6 \mathcal{I}^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + 6 f^{\alpha\beta} \tau(\Delta + \mathcal{K})_{\alpha\beta} - 12t_1 \mathcal{I}_{\alpha}^{\theta} \partial_t f^{\alpha'} + 12t_1 \mathcal{I}_{\theta}^{\theta} \partial_t f^{\alpha'} - 6t_1 \partial_t f^{\theta} \partial_t f^{\alpha'} - 6t_1 \partial_t f^{\alpha'} \partial_t f_{\alpha}^{\theta} + 12t_1 \partial_t f_{\alpha}^{\theta} \partial_t f_{\theta}^{\alpha'} + 8r_2 \partial_{\beta} \mathcal{I}_{\alpha\theta} \partial^{\theta} \mathcal{I}^{\alpha\beta\iota} - 4r_2 \partial_{\beta} \mathcal{I}_{\alpha\theta} \partial^{\theta} \mathcal{I}^{\alpha\beta\iota} + 4r_2 \partial_{\beta} \mathcal{I}_{\iota\alpha} \partial^{\theta} \mathcal{I}^{\alpha\beta\iota} - 2r_2 \partial_t \mathcal{I}_{\alpha\theta} \partial^{\theta} \mathcal{I}^{\alpha\beta\iota} + 2r_2 \partial_{\beta} \mathcal{I}_{\alpha\iota} \partial^{\theta} \mathcal{I}^{\alpha\beta\theta} - 4r_2 \partial_{\beta} \mathcal{I}_{\alpha\iota} \partial^{\theta} \mathcal{I}^{\alpha\beta\theta} + 6r_5 \partial_t \mathcal{I}_{\theta}^{\kappa} \partial^{\theta} \mathcal{I}_{\alpha}^{\alpha'} - 6r_5 \partial_{\beta} \mathcal{I}_{\kappa}^{\alpha'} \partial^{\theta} \mathcal{I}_{\alpha}^{\alpha'} + 4t_1 \mathcal{I}_{\iota\alpha} \partial^{\theta} f^{\alpha'} + 4t_2 \mathcal{I}_{\iota\alpha} \partial^{\theta} f^{\alpha'} - 4t_1 \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha'} + 2t_2 \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha'} - 4t_1 \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha'} - t_2 \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha'} + 2t_1 \partial_t f_{\alpha\theta} \partial^{\theta} f^{\alpha'} - t_2 \partial_t f_{\alpha\theta} \partial^{\theta} f^{\alpha'} + 4t_1 \partial_{\theta} f_{\alpha\iota} \partial^{\theta} f^{\alpha'} + t_2 \partial_{\theta} f_{\alpha\iota} \partial^{\theta} f^{\alpha'} + 2t_1 \partial_{\theta} f_{\iota\alpha} \partial^{\theta} f^{\alpha'} - t_2 \partial_{\theta} f_{\iota\alpha} \partial^{\theta} f^{\alpha'} + 2(t_1 + t_2) \mathcal{I}_{\alpha\iota\theta} (\mathcal{I}^{\alpha\theta\iota} + 2 \partial^{\theta} f^{\alpha'}) + 2 \mathcal{I}_{\alpha\theta\iota} ((t_1 - 2t_2) \mathcal{I}^{\alpha\theta\iota} + 2(2t_1 - t_2) \partial^{\theta} f^{\alpha'}) - 6r_5 \partial_{\alpha} \mathcal{I}^{\alpha\theta\iota} \partial_{\kappa} \mathcal{I}_{\theta}^{\kappa} + 12r_5 \partial^{\theta} \mathcal{I}_{\alpha}^{\alpha'} \partial_{\kappa} \mathcal{I}_{\theta}^{\kappa} + 6r_5 \partial_{\alpha} \mathcal{I}^{\alpha\theta\iota} \partial_{\kappa} \mathcal{I}_{\theta}^{\kappa} - 12r_5 \partial^{\theta} \mathcal{I}_{\alpha}^{\alpha'} \partial_{\kappa} \mathcal{I}_{\theta}^{\kappa} ) | [t, x, y, z] dz dy dx dt \right)$$

$0^+ \mathcal{A}^\parallel \dagger$	$-t_1$	$i\sqrt{2}kt_1$	0	0
$0^+ f^\parallel \dagger$	$-i\sqrt{2}kt_1$	$-2k^2 t_1$	0	0
$0^+ f^\perp \dagger$	0	0	0	0
$0^- \mathcal{A}^\parallel \dagger$	0	0	$k^2 r_2 + t_2$	$1^+ \mathcal{A}^\parallel_{\alpha\beta}$
			$1^+ \mathcal{A}^\perp_{\alpha\beta}$	$1^+ f^\parallel_{\alpha\beta}$
			$1^- \mathcal{A}^\parallel_\alpha$	$1^- \mathcal{A}^\perp_\alpha$
			$1^- f^\parallel_\alpha$	$1^- f^\perp_\alpha$
$1^+ \mathcal{A}^\parallel \dagger^{\alpha\beta}$	$\frac{1}{6}(6k^2 r_5 + t_1 + 4t_2)$	$-\frac{t_1 - 2t_2}{3\sqrt{2}}$	$-\frac{ik(t_1 - 2t_2)}{3\sqrt{2}}$	0
$1^+ \mathcal{A}^\perp \dagger^{\alpha\beta}$	$-\frac{t_1 - 2t_2}{3\sqrt{2}}$	$\frac{t_1 + t_2}{3}$	$\frac{1}{3} ik(t_1 + t_2)$	0
$1^+ f^\parallel \dagger^{\alpha\beta}$	$\frac{ik(t_1 - 2t_2)}{3\sqrt{2}}$	$-\frac{1}{3} ik(t_1 + t_2)$	$\frac{1}{3} k^2(t_1 + t_2)$	0
$1^- \mathcal{A}^\parallel \dagger^\alpha$	0	0	0	$k^2 r_5 - \frac{t_1}{2} - \frac{t_1}{\sqrt{2}}$
$1^- \mathcal{A}^\perp \dagger^\alpha$	0	0	0	$\frac{t_1}{\sqrt{2}}$
$1^- f^\parallel \dagger^\alpha$	0	0	0	0
$1^- f^\perp \dagger^\alpha$	0	0	0	$-ikt_1$
				$2^+ \mathcal{A}^\parallel_{\alpha\beta}$
				$2^+ f^\parallel_{\alpha\beta}$
				$2^- \mathcal{A}^\parallel_{\alpha\beta X}$
				$2^- \mathcal{A}^\perp \dagger^{\alpha\beta}$
				$2^- f^\parallel \dagger^{\alpha\beta}$
				$2^- \mathcal{A}^\parallel \dagger^{\alpha\beta X}$
				$\frac{t_1}{2}$
				$-\frac{ikt_1}{\sqrt{2}}$
				0
				$\frac{ikt_1}{\sqrt{2}}$
				$k^2 t_1$
				0
				0
				$\frac{t_1}{2}$

$0^+ \sigma^\parallel \uparrow$	$0^+ \tau^\parallel$	$0^+ \tau^\perp$	$0^- \sigma^\parallel$			
$-\frac{1}{(1+2k^2)^2 t_{-1}}$	$\frac{i\sqrt{2}k}{(1+2k^2)^2 t_{-1}}$	0	0			
$-\frac{i\sqrt{2}k}{(1+2k^2)^2 t_{-1}}$	$-\frac{2k^2}{(1+2k^2)^2 t_{-1}}$	0	0			
0	0	0	0			
0	0	0	$\frac{1}{k^2 r_{-2} + t_{-2}}$			
$1^+ \sigma^\parallel \uparrow^{\alpha\beta}$	$1^+ \sigma^\perp \uparrow^{\alpha\beta}$	$1^+ \tau^\parallel \uparrow^{\alpha\beta}$	$1^- \sigma^\parallel \uparrow^\alpha$	$1^- \sigma^\perp \uparrow^\alpha$	$1^- \tau^\parallel \uparrow^\alpha$	$1^- \tau^\perp \uparrow^\alpha$
$\frac{2(t_{-1} + t_{-2})}{3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2})}$	$\frac{\sqrt{2}(t_{-1} - 2t_{-2})}{(1+k^2)(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	$\frac{i\sqrt{2}k(t_{-1} - 2t_{-2})}{(1+k^2)(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	0	0	0	0
$\frac{\sqrt{2}(t_{-1} - 2t_{-2})}{(1+k^2)(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	$\frac{6k^2 r_{-5} + t_{-1} + 4t_{-2}}{(1+k^2)^2(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	$\frac{ik(6k^2 r_{-5} + t_{-1} + 4t_{-2})}{(1+k^2)^2(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	0	0	0	0
$-\frac{i\sqrt{2}k(t_{-1} - 2t_{-2})}{(1+k^2)(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	$-\frac{ik(6k^2 r_{-5} + t_{-1} + 4t_{-2})}{(1+k^2)^2(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	$-\frac{k^2(6k^2 r_{-5} + t_{-1} + 4t_{-2})}{(1+k^2)^2(3t_{-1/2} + 2k^2 r_{-5}(t_{-1} + t_{-2}))}$	0	0	0	0
0	0	0	0	$\frac{\sqrt{2}}{t_{-1} + 2k^2 t_{-1}}$	0	$\frac{2ik}{t_{-1} + 2k^2 t_{-1}}$
0	0	0	$\frac{\sqrt{2}}{t_{-1} + 2k^2 t_{-1}}$	$\frac{-2k^2 r_{-5} + t_{-1}}{(t_{-1} + 2k^2 t_{-1})^2}$	0	$-\frac{i\sqrt{2}k(2k^2 r_{-5} t_{-1})}{(t_{-1} + 2k^2 t_{-1})^2}$
0	0	0	0	0	0	0
0	0	0	$-\frac{2ik}{t_{-1} + 2k^2 t_{-1}}$	$\frac{i\sqrt{2}k(2k^2 r_{-5} t_{-1})}{(t_{-1} + 2k^2 t_{-1})^2}$	0	$-\frac{4k^4 r_{-5} + 2k^2 t_{-1}}{(t_{-1} + 2k^2 t_{-1})^2}$
$2^+ \sigma^\parallel \uparrow^{\alpha\beta}$	$2^+ \tau^\parallel \uparrow^{\alpha\beta}$	$2^- \sigma^\parallel \uparrow^{\alpha\beta\chi}$				
$\frac{2}{(1+2k^2)^2 t_{-1}}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_{-1}}$	0				
$\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_{-1}}$	$\frac{4k^2}{(1+2k^2)^2 t_{-1}}$	0				
0	0	$\frac{2}{t_{-1}}$				

Spin-parity form	Covariant form	Multiplicities
$0^+ \tau^{\pm} = 0$	$\partial_{\beta} \partial_{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} = 0$	1
$-2 i k^0 \tau^{\pm} \sigma^{\pm} + 0^+ \tau^{\pm} = 0$	$\partial_{\beta} \partial_{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} = \partial_{\beta} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha}_{\alpha} + 2 \partial_{\chi} \partial^{\chi} \partial_{\beta} \sigma^{\alpha}_{\alpha}$	1
$2 i k^1 \tau^{\pm} \sigma^{\pm} + 1^+ \tau^{\pm} = 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} = \partial_{\chi} \partial^{\chi} \partial_{\beta} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial_{\beta} \sigma^{\beta\alpha\chi}$	3
$1^+ \tau^{\pm} = 0$	$\partial_{\chi} \partial_{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} = \partial_{\chi} \partial^{\chi} \partial_{\beta} \tau (\Delta + \mathcal{K})^{\beta\alpha}$	3
$i k^1 \tau^{\pm} \sigma^{\pm} + 1^+ \tau^{\pm} = 0$	$\partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} + \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\chi\alpha} + \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 2 \partial_{\sigma} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\beta\sigma} + 2 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \sigma^{\chi\alpha\beta} = \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\beta} + \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha\chi} + \partial_{\chi} \partial^{\chi} \tau (\Delta + \mathcal{K})^{\beta\alpha} + 2 \partial_{\sigma} \partial_{\chi} \partial^{\alpha} \sigma^{\chi\sigma\beta}$	3
$-2 i k^2 \tau^{\pm} \sigma^{\pm} + 2^+ \tau^{\pm} = 0$	$-i (4 \partial_{\sigma} \partial_{\chi} \partial^{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\sigma} + 2 \partial_{\sigma} \partial^{\sigma} \partial^{\beta} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi}_{\chi} - 3 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\chi} - 3 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\chi\beta} - 3 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\alpha\chi} - 3 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial^{\beta} \tau (\Delta + \mathcal{K})^{\chi\alpha} + 3 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\alpha\beta} + 3 \partial_{\sigma} \partial^{\sigma} \partial_{\chi} \partial^{\alpha} \tau (\Delta + \mathcal{K})^{\beta\alpha} + 4 i k^{\chi} \partial_{\chi} \partial^{\beta} \partial^{\alpha} \sigma^{\sigma}_{\sigma} - 6 i k^{\chi} \partial_{\epsilon} \partial_{\sigma} \partial_{\chi} \partial^{\alpha} \sigma^{\sigma\beta\epsilon} - 6 i k^{\chi} \partial_{\epsilon} \partial_{\sigma} \partial_{\chi} \partial^{\beta} \sigma^{\sigma\alpha\epsilon} + 6 i k^{\chi} \partial_{\epsilon} \partial^{\epsilon} \partial_{\sigma} \partial_{\chi} \sigma^{\sigma\beta\sigma} + 6 i k^{\chi} \partial_{\epsilon} \partial^{\epsilon} \partial_{\sigma} \partial_{\chi} \sigma^{\sigma\alpha\sigma} + 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\sigma} \partial_{\chi} \tau (\Delta + \mathcal{K})^{\chi\sigma} - 2 \eta^{\alpha\beta} \partial_{\epsilon} \partial^{\epsilon} \partial_{\sigma} \partial^{\sigma} \tau (\Delta + \mathcal{K})^{\chi}_{\chi} - 4 i \eta^{\alpha\beta} k^{\chi} \partial_{\phi} \partial^{\phi} \partial_{\epsilon} \partial_{\chi} \sigma^{\sigma}_{\sigma} = 0$	5
Total expected gauge generators:		16

Two Feynman diagrams illustrating meson exchange between two nucleons (represented by circles with a cross). The left diagram shows a meson with  $J^P = 0^-$  and momentum  $k^\mu = (\mathcal{E}, 0, 0, p)$  (indicated by a dashed blue line). The right diagram shows a meson with  $J^P = 1^+$  and momentum  $k^\mu = (\mathcal{E}, 0, 0, p)$  (indicated by a wavy red line). Both diagrams have question marks on the external lines, indicating unknown quantum numbers for the nucleons.

(No particles)

**Unitarity conditions**

$$r_2 < 0 \ \&\& \ t_2 > 0 \ \&\& \ r_5 > 0 \ \&\& \ -t_2 < t_1 <$$
$$r_2 < 0 \ \&\& \ t_2 > 0 \ \&\& \ r_5 > 0 \ \&\& \ -t_2 < t_1 < 0$$