

Particle spectrograph

Wave operator and propagator

| $\omega_{1+}^{#1} \alpha\beta$ | $\omega_{1+}^{#2} \alpha\beta$ | $f_{1+}^{#1} \alpha\beta$ | $\omega_{1-}^{#1} \alpha$ | $\omega_{1-}^{#2} \alpha$ | $f_{1-}^{#1} \alpha$ | $f_{1-}^{#2} \alpha$ |
|----------------------------------|--------------------------------|---------------------------|----------------------------|---------------------------|----------------------|----------------------|
| $\omega_{1+}^{#1} + \alpha\beta$ | $\frac{2t_2}{3}$ | $\frac{\sqrt{2}t_2}{3}$ | $\frac{1}{3}i\sqrt{2}kt_2$ | 0 | 0 | 0 |
| $\omega_{1+}^{#2} + \alpha\beta$ | $\frac{\sqrt{2}t_2}{3}$ | $\frac{t_2}{3}$ | $\frac{ikt_2}{3}$ | 0 | 0 | 0 |
| $f_{1+}^{#1} + \alpha\beta$ | $-\frac{1}{3}i\sqrt{2}kt_2$ | $-\frac{1}{3}ikt_2$ | $\frac{k^2t_2}{3}$ | 0 | 0 | 0 |
| $\omega_{1-}^{#1} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\omega_{1-}^{#2} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{#1} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{#2} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |

| SO(3) irreps | Multiplicities |
|--|----------------|
| $\tau_{0+}^{#2} == 0$ | 1 |
| $\tau_{0+}^{#1} == 0$ | 1 |
| $\sigma_{0+}^{#1} == 0$ | 1 |
| $\tau_{1-}^{#2\alpha} == 0$ | 3 |
| $\tau_{1-}^{#1\alpha} == 0$ | 3 |
| $\sigma_{1-}^{#2\alpha} == 0$ | 3 |
| $\sigma_{1-}^{#1\alpha} == 0$ | 3 |
| $\tau_{1+}^{#1\alpha\beta} + ik\sigma_{1+}^{#1\alpha\beta} == 0$ | 3 |
| $\sigma_{1+}^{#1\alpha\beta} == \sigma_{1+}^{#2\alpha\beta}$ | 3 |
| $\sigma_2^{#1\alpha\beta\chi} == 0$ | 5 |
| $\tau_{2+}^{#1\alpha\beta} == 0$ | 5 |
| $\sigma_2^{#1\alpha\beta} == 0$ | 5 |
| Total constraints: | 36 |

| $\sigma_{1+}^{#1} + \alpha\beta$ | $\sigma_{1+}^{#2} + \alpha\beta$ | $\tau_{1+}^{#1} + \alpha\beta$ | $\sigma_{1-}^{#1} \alpha$ | $\sigma_{1-}^{#2} \alpha$ | $\tau_{1-}^{#1} \alpha$ | $\tau_{1-}^{#2} \alpha$ |
|----------------------------------|-------------------------------------|----------------------------------|------------------------------------|---------------------------|-------------------------|-------------------------|
| $\sigma_{1+}^{#1} + \alpha\beta$ | $\frac{6}{(3+k^2)^2t_2}$ | $\frac{3\sqrt{2}}{(3+k^2)^2t_2}$ | $\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$ | 0 | 0 | 0 |
| $\sigma_{1+}^{#2} + \alpha\beta$ | $\frac{3\sqrt{2}}{(3+k^2)^2t_2}$ | $\frac{3}{(3+k^2)^2t_2}$ | $\frac{3ik}{(3+k^2)^2t_2}$ | 0 | 0 | 0 |
| $\tau_{1+}^{#1} + \alpha\beta$ | $-\frac{3i\sqrt{2}k}{(3+k^2)^2t_2}$ | $-\frac{3k^2}{(3+k^2)^2t_2}$ | 0 | 0 | 0 | 0 |
| $\sigma_{1-}^{#1} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\sigma_{1-}^{#2} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1-}^{#1} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\tau_{1-}^{#2} + \alpha$ | 0 | 0 | 0 | 0 | 0 | 0 |

Quadratic (free) action

$$S_F = \int \int \int \int \left(\frac{1}{6} (4t_2\omega_{\kappa\lambda}'\omega_{\kappa\lambda}' + 2t_2\omega_{\kappa\lambda}'\omega_{\kappa\lambda}' + 6f^{\alpha\beta}\tau_{\alpha\beta} + 6\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi} + 4r_2\partial^\beta\omega_{\kappa}^{\alpha\beta}\partial_\theta\omega_{\alpha\beta}^{\kappa} - 2r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\alpha\beta\theta} - 4r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\alpha\beta\theta} + t_2\partial^\alpha f_{\theta\kappa}^{\kappa}f_{\alpha}^{\theta} - t_2\partial^\alpha f_{\kappa\theta}^{\theta}f_{\alpha}^{\kappa} + t_2\partial^\alpha f_{\alpha}^{\kappa}f_{\kappa}^{\theta} + 2t_2\omega_{\theta\kappa}^{\kappa}\partial^\kappa f_{\alpha}^{\theta} + 2t_2\omega_{\theta\kappa}^{\kappa}\partial^\kappa f_{\alpha}^{\theta} - 4t_2\omega_{\theta\kappa}^{\kappa}\partial^\kappa f_{\alpha}^{\theta} - 2t_2\omega_{\theta\kappa}^{\kappa}\partial^\kappa f_{\alpha}^{\theta} + 4t_2\omega_{\theta\kappa}^{\kappa}\partial^\kappa f_{\alpha}^{\theta} - t_2\partial^\alpha f_{\alpha}^{\kappa}f_{\kappa}^{\theta} - t_2\partial^\alpha f_{\kappa}^{\theta}f_{\alpha}^{\kappa} + 2r_2\partial_\kappa\omega^{\alpha\beta\theta}\partial^\kappa\omega_{\alpha\beta\theta} + 4r_2\partial_\kappa\omega^{\alpha\beta\theta}\partial^\kappa\omega_{\alpha\beta\theta} - 4r_2\partial^\beta\omega_{\alpha}^{\alpha\lambda}\partial_\lambda\omega_{\alpha\beta}^{\alpha} + 4r_2\partial^\beta\omega_{\alpha}^{\alpha\lambda}\partial_\lambda\omega_{\alpha\beta}^{\alpha}) [t, x, y, z] dz dy dx dt \right)$$

| $\omega_{0+}^{#1} +$ | $f_{0+}^{#1} +$ | $f_{0+}^{#2} +$ | $\omega_{0-}^{#1}$ |
|----------------------|-----------------|-----------------|--------------------|
| $\omega_{0+}^{#1} +$ | 0 | 0 | 0 |
| $f_{0+}^{#1} +$ | 0 | 0 | 0 |
| $f_{0+}^{#2} +$ | 0 | 0 | 0 |
| $\omega_{0-}^{#1} +$ | 0 | 0 | $k^2r_2 + t_2$ |

| $\sigma_{2+}^{#1} + \alpha\beta$ | $\tau_{2+}^{#1} + \alpha\beta$ | $\sigma_{2-}^{#1} + \alpha\beta\chi$ |
|--------------------------------------|--------------------------------|--------------------------------------|
| $\sigma_{2+}^{#1} + \alpha\beta$ | 0 | 0 |
| $\tau_{2+}^{#1} + \alpha\beta$ | 0 | 0 |
| $\sigma_{2-}^{#1} + \alpha\beta\chi$ | 0 | 0 |

| $\omega_{2+}^{#1} + \alpha\beta$ | $f_{2+}^{#1} + \alpha\beta$ | $\omega_{2-}^{#1} + \alpha\beta\chi$ |
|--------------------------------------|-----------------------------|--------------------------------------|
| $\omega_{2+}^{#1} + \alpha\beta$ | 0 | 0 |
| $f_{2+}^{#1} + \alpha\beta$ | 0 | 0 |
| $\omega_{2-}^{#1} + \alpha\beta\chi$ | 0 | 0 |

Massive and massless spectra

| Massive particle | |
|------------------|------------------------|
| Pole residue: | $-\frac{1}{r_2} > 0$ |
| Polarisations: | 1 |
| Square mass: | $-\frac{t_2}{r_2} > 0$ |
| Spin: | 0 |
| Parity: | Odd |

(No massless particles)

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$