

Particle spectrograph

Wave operator and propagator

| | $\Delta_{1^{+}\alpha\beta}^{\#1}$ | $\Delta_{1^{+}\alpha\beta}^{\#2}$ | $\Delta_{1^{+}\alpha\beta}^{\#3}$ | $\Delta_{1^{-}\alpha}^{\#1}$ | $\Delta_{1^{-}\alpha}^{\#2}$ | $\Delta_{1^{-}\alpha}^{\#3}$ | $\Delta_{1^{-}\alpha}^{\#4}$ | $\Delta_{1^{-}\alpha}^{\#5}$ | $\Delta_{1^{-}\alpha}^{\#6}$ | $\mathcal{T}_{1^{-}\alpha}^{\#1}$ |
|-----------------------------------|-----------------------------------|---|--|---|---|---|---|---|---|---|
| $\Delta_{1^{+}\alpha\beta}^{\#1}$ | 0 | $-\frac{2\sqrt{2}}{a_0}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1^{+}\alpha\beta}^{\#2}$ | $-\frac{2\sqrt{2}}{a_0}$ | $\frac{2(a_0^2-14a_0a_1k^2-35a_1^2k^4)}{a_0^2(a_0-29a_1k^2)}$ | $\frac{40\sqrt{2}a_1k^2}{a_0^2-29a_0a_1k^2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1^{+}\alpha\beta}^{\#3}$ | 0 | $\frac{40\sqrt{2}a_1k^2}{a_0^2-29a_0a_1k^2}$ | $\frac{4}{a_0-29a_1k^2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Delta_{1^{+}\alpha}^{\#1}$ | 0 | 0 | 0 | 0 | $\frac{\sqrt{2}(4+k^2)}{a_0(2+k^2)}$ | $-\frac{2k^2}{\sqrt{3}a_0(2+k^2)}$ | 0 | $\frac{\sqrt{\frac{2}{3}}k^2}{a_0(2+k^2)}$ | 0 | $-\frac{2i\sqrt{2}k}{a_0(2+k^2)}$ |
| $\Delta_{1^{+}\alpha}^{\#2}$ | 0 | 0 | 0 | $\frac{\sqrt{2}(4+k^2)}{a_0(2+k^2)}$ | $\frac{a_0^2(4+k^2)^2-30a_0a_1k^2(4+k^2)(4+3k^2)+a_1^2k^4(6416+7928k^2+1901k^4)}{2a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{k^2(a_0^2(-2+k^2)+a_0a_1(560+302k^2+71k^4)-2a_1^2k^2(9440+1901k^2(4+k^2)))}{2\sqrt{6}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $-\frac{\sqrt{\frac{5}{6}}k^2(a_0+a_1(40-31k^2))}{2a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{k^2(2a_0^2(5+2k^2)-a_0a_1(880+778k^2+199k^4)+a_1^2k^2(9440+1901k^2(4+k^2)))}{2\sqrt{3}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{k^2(-a_0+a_1(200+43k^2))}{\sqrt{6}a_0(2+k^2)(a_0-33a_1k^2)}$ | $-\frac{ik(-30a_0a_1k^4+a_0^2(4+k^2)+27a_1^2k^4(-28+3k^2))}{a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ |
| $\Delta_{1^{+}\alpha}^{\#3}$ | 0 | 0 | 0 | $-\frac{2k^2}{\sqrt{3}(2a_0+a_0k^2)}$ | $\frac{k^2(a_0^2(-2+k^2)+a_0a_1(560+302k^2+71k^4)-2a_1^2k^2(9440+1901k^2(4+k^2)))}{2\sqrt{6}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{-a_0^2(76+52k^2+3k^4)+4a_0a_1k^2(472+214k^2+19k^4)+4a_1^2k^4(5120+7280k^2+1901k^4)}{12a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{\sqrt{5}(10a_0+(3a_0-328a_1)k^2-62a_1k^4)}{12a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{2a_0^2(-2+k^2)+a_0a_1k^2(472+934k^2+289k^4)-2a_1^2k^4(5120+7280k^2+1901k^4)}{6\sqrt{2}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $-\frac{2a_0+(3a_0-56a_1)k^2+86a_1k^4}{6a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{ik(54a_1^2k^4(40+3k^2)+a_0^2(6+5k^2)-3a_0a_1k^2(86+23k^2))}{\sqrt{6}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ |
| $\Delta_{1^{+}\alpha}^{\#4}$ | 0 | 0 | 0 | 0 | $-\frac{\sqrt{\frac{5}{6}}k^2(a_0+a_1(40-31k^2))}{2a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{\sqrt{5}(10a_0+k^2(3a_0-2a_1(164+31k^2)))}{12a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{1}{12a_0-396a_1k^2}$ | $\frac{\sqrt{\frac{5}{2}}(-2a_0+a_1k^2(164+31k^2))}{6a_0(2+k^2)(a_0-33a_1k^2)}$ | $-\frac{\sqrt{5}}{6(a_0-33a_1k^2)}$ | $-\frac{i\sqrt{\frac{5}{6}}k(a_0-51a_1k^2)}{a_0(2+k^2)(a_0-33a_1k^2)}$ |
| $\Delta_{1^{+}\alpha}^{\#5}$ | 0 | 0 | 0 | $\frac{\sqrt{\frac{2}{3}}k^2}{2a_0+a_0k^2}$ | $\frac{k^2(2a_0^2(5+2k^2)-a_0a_1(880+778k^2+199k^4)+a_1^2k^2(9440+1901k^2(4+k^2)))}{2\sqrt{3}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{2a_0^2(-2+k^2)+a_0a_1k^2(472+934k^2+289k^4)-2a_1^2k^4(5120+7280k^2+1901k^4)}{6\sqrt{2}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{\sqrt{\frac{5}{2}}(-2a_0+a_1k^2(164+31k^2))}{6a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{4a_0^2(17+14k^2+3k^4)-4a_0a_1k^2(236+287k^2+77k^4)+a_1^2k^4(5120+7280k^2+1901k^4)}{6a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{a_1k^2(28-43k^2)+2a_0(7+3k^2)}{3\sqrt{2}a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{ik(2a_0^2(3+k^2)-27a_1^2k^4(40+3k^2)+3a_0a_1k^2(34+7k^2))}{\sqrt{3}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ |
| $\Delta_{1^{+}\alpha}^{\#6}$ | 0 | 0 | 0 | 0 | $\frac{k^2(-a_0+a_1(200+43k^2))}{\sqrt{6}a_0(2+k^2)(a_0-33a_1k^2)}$ | $-\frac{2a_0+(3a_0-56a_1)k^2+86a_1k^4}{6a_0(2+k^2)(a_0-33a_1k^2)}$ | $-\frac{\sqrt{5}}{6(a_0-33a_1k^2)}$ | $-\frac{a_1k^2(28-43k^2)+2a_0(7+3k^2)}{3\sqrt{2}a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{5}{3(a_0-33a_1k^2)}$ | $-\frac{i\sqrt{\frac{2}{3}}k(a_0+57a_1k^2)}{a_0(2+k^2)(a_0-33a_1k^2)}$ |
| $\mathcal{T}_{1^{+}\alpha}^{\#1}$ | 0 | 0 | 0 | $\frac{2i\sqrt{2}k}{2a_0+a_0k^2}$ | $\frac{i(-30a_0a_1k^5+a_0^2k(4+k^2)+27a_1^2k^5(-28+3k^2))}{a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $-\frac{i(54a_1^2k^5(40+3k^2)+a_0^2k(6+5k^2)-3a_0a_1k^3(86+23k^2))}{\sqrt{6}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{i\sqrt{\frac{5}{6}}k(a_0-51a_1k^2)}{a_0(2+k^2)(a_0-33a_1k^2)}$ | $-\frac{i(2a_0^2k(3+k^2)-27a_1^2k^5(40+3k^2)+3a_0a_1k^3(34+7k^2))}{\sqrt{3}a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ | $\frac{i\sqrt{\frac{2}{3}}k(a_0+57a_1k^2)}{a_0(2+k^2)(a_0-33a_1k^2)}$ | $\frac{2k^2(a_0^2+30a_0a_1k^2-459a_1^2k^4)}{a_0^2(2+k^2)^2(a_0-33a_1k^2)}$ |

| | $\Gamma_{1^{+}\alpha\beta}^{\#1}$ | $\Gamma_{1^{+}\alpha\beta}^{\#2}$ | $\Gamma_{1^{+}\alpha\beta}^{\#3}$ | $\Gamma_{1^{-}\alpha}^{\#1}$ | $\Gamma_{1^{-}\alpha}^{\#2}$ | $\Gamma_{1^{-}\alpha}^{\#3}$ | $\Gamma_{1^{-}\alpha}^{\#4}$ | $\Gamma_{1^{-}\alpha}^{\#5}$ | $\Gamma_{1^{-}\alpha}^{\#6}$ | $h_{1^{-}\alpha}^{\#1}$ |
|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|--|------------------------------|------------------------------------|--|--|-------------------------------------|---------------------------------------|
| $\Gamma_{1^{+}\alpha\beta}^{\#1}$ | $\frac{1}{4}(-a_0-15a_1k^2)$ | $-\frac{a_0}{2\sqrt{2}}$ | $5a_1k^2$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Gamma_{1^{+}\alpha\beta}^{\#2}$ | $-\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Gamma_{1^{+}\alpha\beta}^{\#3}$ | $5a_1k^2$ | 0 | $\frac{1}{4}(a_0-29a_1k^2)$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Gamma_{1^{+}\alpha}^{\#1}$ | 0 | 0 | 0 | $\frac{1}{4}(-a_0-3a_1k^2)$ | $\frac{a_0}{2\sqrt{2}}$ | $\frac{5}{2}\sqrt{3}a_1k^2$ | $-\frac{5}{2}\sqrt{\frac{3}{3}}a_1k^2$ | $5\sqrt{\frac{3}{2}}a_1k^2$ | $-\frac{5a_1k^2}{\sqrt{3}}$ | $-\frac{ia_0k}{4\sqrt{2}}$ |
| $\Gamma_{1^{+}\alpha}^{\#2}$ | 0 | 0 | 0 | $-\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\Gamma_{1^{+}\alpha}^{\#3}$ | 0 | 0 | 0 | $\frac{5}{2}\sqrt{3}a_1k^2$ | 0 | $-\frac{a_0}{3}$ | $\frac{1}{6}\sqrt{5}(a_0-8a_1k^2)$ | $-\frac{a_0}{6\sqrt{2}}$ | $\frac{1}{6}(-a_0+20a_1k^2)$ | $\frac{ia_0k}{4\sqrt{6}}$ |
| $\Gamma_{1^{+}\alpha}^{\#4}$ | 0 | 0 | 0 | $-\frac{5}{2}\sqrt{\frac{3}{3}}a_1k^2$ | 0 | $\frac{1}{6}\sqrt{5}(a_0-8a_1k^2)$ | $\frac{1}{3}(a_0+7a_1k^2)$ | $-\frac{1}{6}\sqrt{\frac{5}{2}}(a_0+16a_1k^2)$ | $-\frac{1}{6}\sqrt{5}(a_0-5a_1k^2)$ | $-\frac{1}{4}i\sqrt{\frac{5}{6}}a_0k$ |
| $\Gamma_{1^{+}\alpha}^{\#5}$ | 0 | 0 | 0 | $5\sqrt{\frac{3}{2}}a_1k^2$ | 0 | $-\frac{a_0}{6\sqrt{2}}$ | $-\frac{1}{6}\sqrt{\frac{5}{2}}(a_0+16a_1k^2)$ | $\frac{a_0}{3}$ | $\frac{a_0+40a_1k^2}{6\sqrt{2}}$ | $\frac{ia_0k}{4\sqrt{3}}$ |
| $\Gamma_{1^{+}\alpha}^{\#6}$ | 0 | 0 | 0 | $-\frac{5a_1k^2}{\sqrt{3}}$ | 0 | $\frac{1}{6}(-a_0+20a_1k^2)$ | $-\frac{1}{6}\sqrt{5}(a_0-5a_1k^2)$ | $\frac{a_0+40a_1k^2}{6\sqrt{2}}$ | $\frac{5}{12}(a_0-17a_1k^2)$ | $\frac{ia_0k}{4\sqrt{6}}$ |
| $h_{1^{-}\alpha}^{\#1}$ | 0 | 0 | 0 | $\frac{ia_0k}{4\sqrt{2}}$ | 0 | $-\frac{ia_0k}{4\sqrt{6}}$ | $\frac{1}{4}i\sqrt{\frac{5}{6}}a_0k$ | $-\frac{ia_0k}{4\sqrt{3}}$ | $-\frac{ia_0k}{4\sqrt{6}}$ | 0 |

| | $\Gamma_{2^{+}\alpha\beta}^{\#1}$ | $\Gamma_{2^{+}\alpha\beta}^{\#2}$ | $\Gamma_{2^{+}\alpha\beta}^{\#3}$ | $h_{2^{+}\alpha\beta}^{\#1}$ | $\Gamma_{2^{-}\alpha\beta\chi}^{\#1}$ | $\Gamma_{2^{-}\alpha\beta\chi}^{\#2}$ |
|---------------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|------------------------------|---------------------------------------|---------------------------------------|
| $\Gamma_{2^{+}\alpha\beta}^{\#1}$ | $\frac{1}{4}(a_0+11a_1k^2)$ | $-5\sqrt{\frac{2}{3}}a_1k^2$ | $\frac{5a_1k^2}{\sqrt{3}}$ | $\frac{ia_0k}{4\sqrt{2}}$ | 0 | 0 |
| $\Gamma_{2^{+}\alpha\beta}^{\#2}$ | $-5\sqrt{\frac{2}{3}}a_1k^2$ | $\frac{1}{6}(-3a_0+a_1k^2)$ | $-\frac{a_1k^2}{6\sqrt{2}}$ | $\frac{ia_0k}{4\sqrt{3}}$ | 0 | 0 |
| $\Gamma_{2^{+}\alpha\beta}^{\#3}$ | $\frac{5a_1k^2}{\sqrt{3}}$ | $-\frac{a_1k^2}{6\sqrt{2}}$ | $\frac{1}{12}(3a_0+a_1k^2)$ | $-\frac{ia_0k}{4\sqrt{6}}$ | 0 | 0 |
| $h_{2^{+}\alpha\beta}^{\#1}$ | $-\frac{ia_0k}{4\sqrt{2}}$ | $-\frac{ia_0k}{4\sqrt{3}}$ | $\frac{ia_0k}{4\sqrt{6}}$ | 0 | 0 | 0 |
| $\Gamma_{2^{-}\alpha\beta\chi}^{\#1}$ | 0 | 0 | 0 | 0 | $\frac{1}{4}(a_0-a_1k^2)$ | 0 |
| $\Gamma_{2^{-}\alpha\beta\chi}^{\#2}$ | 0 | 0 | 0 | 0 | 0 | $\frac{1}{4}(a_0-5a_1k^2)$ |

| | $\Delta_{0^{+}}^{\#1}$ | $\Delta_{0^{+}}^{\#2}$ | $\Delta_{0^{+}}^{\#3}$ | $\Delta_{0^{+}}^{\#4}$ | $\mathcal{T}_{0^{+}}^{\#1}$ | $\mathcal{T}_{0^{+}}^{\#2}$ | $\Delta_{0^{-}}^{\#1}$ |
|-----------------------------|--|---|---|---|--|--|------------------------|
| $\Delta_{0^{+}}^{\#1}$ | 0 | $\frac{4\sqrt{6}}{16a_0+3a_0k^2}$ | $-\frac{4\sqrt{\frac{2}{3}}}{16a_0+3a_0k^2}$ | $-\frac{8}{\sqrt{3}(16a_0+3a_0k^2)}$ | $-\frac{2i\sqrt{2}}{a_0k}$ | $-\frac{2i\sqrt{6}k}{16a_0+3a_0k^2}$ | 0 |
| $\Delta_{0^{+}}^{\#2}$ | $\frac{4\sqrt{6}}{16a_0+3a_0k^2}$ | $-\frac{48(3a_0+197a_1k^2)}{a_0^2(16+3k^2)^2}$ | $\frac{16(19a_0+(3a_0+197a_1)k^2)}{a_0^2(16+3k^2)^2}$ | $-\frac{8\sqrt{2}(10a_0+(3a_0-394a_1)k^2)}{a_0^2(16+3k^2)^2}$ | $-\frac{8i\sqrt{3}(a_0-65a_1k^2)}{a_0^2k(16+3k^2)}$ | $\frac{24ik(3a_0+197a_1k^2)}{a_0^2(16+3k^2)^2}$ | 0 |
| $\Delta_{0^{+}}^{\#3}$ | $-\frac{4\sqrt{\frac{2}{3}}}{16a_0+3a_0k^2}$ | $\frac{16(19a_0+(3a_0+197a_1)k^2)}{a_0^2(16+3k^2)^2}$ | $-\frac{16(35a_0+(6a_0+197a_1)k^2)}{3a_0^2(16+3k^2)^2}$ | $-\frac{8\sqrt{2}(22a_0+(3a_0+394a_1)k^2)}{3a_0^2(16+3k^2)^2}$ | $\frac{8i(a_0-65a_1k^2)}{\sqrt{3}a_0^2k(16+3k^2)}$ | $-\frac{8ik(19a_0+(3a_0+197a_1)k^2)}{a_0^2(16+3k^2)^2}$ | 0 |
| $\Delta_{0^{+}}^{\#4}$ | $-\frac{8}{\sqrt{3}(16a_0+3a_0k^2)}$ | $-\frac{8\sqrt{2}(10a_0+(3a_0-394a_1)k^2)}{a_0^2(16+3k^2)^2}$ | $\frac{8\sqrt{2}(22a_0+(3a_0+394a_1)k^2)}{3a_0^2(16+3k^2)^2}$ | $\frac{32(13a_0+(3a_0-197a_1)k^2)}{3a_0^2(16+3k^2)^2}$ | $\frac{8i\sqrt{\frac{2}{3}}(a_0-65a_1k^2)}{a_0^2k(16+3k^2)}$ | $\frac{4i\sqrt{2}k(10a_0+(3a_0-394a_1)k^2)}{a_0^2(16+3k^2)^2}$ | 0 |
| $\mathcal{T}_{0^{+}}^{\#1}$ | $\frac{2i\sqrt{2}}{a_0k}$ | $\frac{8i\sqrt{3}(a_0-65a_1k^2)}{a_0^2k(16+3k^2)}$ | $-\frac{8i(a_0-65a_1k^2)}{\sqrt{3}a_0^2k(16+3k^2)}$ | $-\frac{8i\sqrt{\frac{2}{3}}(a_0-65a_1k^2)}{a_0^2k(16+3k^2)}$ | $\frac{4(a_0-25a_1k^2)}{a_0^2k^2}$ | $\frac{4\sqrt{3}(a_0-65a_1k^2)}{a_0^2(16+3k^2)}$ | 0 |
| $\mathcal{T}_{0^{+}}^{\#2}$ | $\frac{2i\sqrt{6}k}{16a_0+3a_0k^2}$ | $-\frac{24ik(3a_0+197a_1k^2)}{a_0^2(16+3k^2)^2}$ | $\frac{8ik(19a_0+(3a_0+197a_1)k^2)}{a_0^2(16+3k^2)^2}$ | $-\frac{4i\sqrt{2}k(10a_0+(3a_0-394a_1)k^2)}{a_0^2(16+3k^2)^2}$ | $\frac{4\sqrt{3}(a_0-65a_1k^2)}{a_0^2(16+3k^2)}$ | $-\frac{12k^2(3a_0+197a_1k^2)}{a_0^2(16+3k^2)^2}$ | 0 |
| $\Delta_{0^{-}}^{\#1}$ | 0 | 0 | 0 | 0 | 0 | 0 | $-\frac{2}{a_0a_1k^2}$ |

Quadratic (free) action

$$S = \iiint (\frac{1}{4}(2a_0\Gamma_{\alpha}^{\alpha\beta}\Gamma_{\beta\chi}^{\chi}+4h^{\alpha\beta}\mathcal{T}_{\alpha\beta}+\Gamma^{\alpha\beta\chi}(-2a_0\Gamma_{\beta\chi\alpha}+4\Delta_{\alpha\beta\chi})-a_0h_{\chi}^{\chi}\partial_{\beta}\Gamma_{\alpha}^{\alpha\beta}+a_0h_{\chi}^{\chi}\partial_{\beta}\Gamma_{\alpha}^{\alpha\beta}-2a_0h_{\alpha\chi}\partial_{\beta}\Gamma^{\alpha\beta\chi}+22a_1\partial^{\alpha}\Gamma^{\chi\delta}_{\delta}\partial_{\beta}\Gamma_{\chi\alpha}^{\alpha\beta}+2a_1\partial^{\alpha}\Gamma_{\chi\alpha}^{\beta}\partial_{\beta}\Gamma^{\chi\delta}_{\delta}-76a_1\partial^{\alpha}\Gamma^{\chi\delta}_{\chi}\partial_{\beta}\Gamma_{\delta\alpha}^{\beta}+2a_0h_{\beta\chi}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-2a_1\partial_{\beta}\Gamma_{\chi\delta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-2a_1\partial_{\beta}\Gamma_{\delta\chi}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}+2a_1\partial_{\chi}\Gamma_{\beta\delta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-2a_1\partial_{\chi}\Gamma_{\delta\beta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-22a_1\partial_{\beta}\Gamma_{\chi}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-22a_1\partial_{\chi}\Gamma_{\beta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-22a_1\partial_{\beta}\Gamma_{\chi}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}+38a_1\partial_{\beta}\Gamma_{\chi\delta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}+22a_1\partial_{\chi}\Gamma_{\beta\delta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}-2a_1\partial_{\chi}\Gamma_{\delta\beta}^{\delta}\partial^{\chi}\Gamma_{\alpha}^{\alpha\beta}+4a_1\partial_{\alpha}\Gamma_{\chi}^{\delta}\partial^{\chi}\Gamma_{\alpha\beta}^{\alpha\beta}-4a_1\partial_{\chi}\Gamma_{\alpha}^{\delta}\partial^{\chi}\Gamma^{\alpha\beta}_{\beta}-2a_1\partial_{\chi}\Gamma^{\alpha\beta\chi}\partial_{\delta}\Gamma_{\alpha\beta}^{\delta}-2a_1\partial_{\beta}\Gamma^{\alpha\beta\chi}\partial_{\delta}\Gamma_{\alpha\chi}^{\delta}-2a_1\partial_{\beta}\Gamma^{\alpha\beta\chi}\partial_{\delta}\Gamma_{\alpha}^{\delta}_{\chi}+38a_1\partial_{\chi}\Gamma^{\alpha\beta\chi}\partial_{\delta}\Gamma_{\beta\alpha}^{\delta}_{\delta}+4a_1\partial^{\chi}\Gamma_{\alpha}^{\beta}\partial_{\delta}\Gamma_{\beta\chi}^{\delta}-22a_1\partial^{\chi}\Gamma^{\alpha\beta}_{\beta}\partial_{\delta}\Gamma_{\chi\alpha}^{\delta}+2a_1\partial^{\chi}\Gamma^{\alpha\beta}_{\alpha}\partial_{\delta}\Gamma_{\chi\beta}^{\delta}-2a_1\partial_{\beta}\Gamma^{\alpha\beta\chi}\partial_{\delta}\Gamma_{\chi\alpha}^{\delta}_{\alpha}-2a_1\partial^{\chi}\Gamma^{\alpha\beta}_{\beta}\partial_{\delta}\Gamma_{\chi}^{\delta}_{\alpha}+2a_1\partial^{\chi}\Gamma_{\beta\alpha}^{\beta}\partial_{\delta}\Gamma_{\chi}^{\delta}_{\alpha}+4a_1\partial^{\chi}\Gamma_{\alpha}^{\beta}\partial_{\delta}\Gamma_{\chi}^{\delta}_{\beta}-2a_1\partial_{\beta}\Gamma_{\alpha}^{\beta}\partial_{\delta}\Gamma_{\chi}^{\delta}_{\alpha}+4a_1\partial_{\beta}\Gamma_{\alpha}^{\beta}\partial_{\delta}\Gamma_{\chi}^{\delta}_{\alpha}-2a_1\partial_{\beta}\Gamma^{\alpha\beta}_{\alpha}\partial_{\delta}\Gamma_{\chi}^{\delta}_{\chi}+2a_1\partial_{\alpha}\Gamma_{\beta\chi\delta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}+4a_1\partial_{\alpha}\Gamma_{\chi\delta\beta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}+4a_1\partial_{\alpha}\Gamma_{\chi\delta\beta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\beta}\Gamma_{\alpha\chi\delta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\beta}\Gamma_{\alpha\chi\delta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\chi}\Gamma_{\delta\alpha\delta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\chi}\Gamma_{\alpha\delta\beta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\delta}\Gamma_{\beta\alpha\delta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-4a_1\partial_{\delta}\Gamma_{\alpha\chi\beta}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\delta}\Gamma_{\beta\alpha\chi}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}-2a_1\partial_{\delta}\Gamma_{\chi\beta\alpha}^{\delta}\partial^{\delta}\Gamma^{\alpha\beta\chi}+2a_1\partial_{\beta}\Gamma_{\delta\alpha}^{\beta}\partial^{\delta}\Gamma^{\chi\alpha}_{\chi}+2a_1\partial_{\beta}\Gamma_{\delta\alpha}^{\beta}\partial^{\delta}\Gamma^{\chi}_{\chi})[t,x,y,z]dzdydxdt$$

Source constraints/gauge generators

| SO(3) irreps | Multiplicities |
|--|----------------|
| $2\mathcal{T}_{0^{+}}^{\#2}-ik\Delta_{0^{+}}^{\#2}==0$ | 1 |
| $\Delta_{0^{+}}^{\#3}+2\Delta_{0^{+}}^{\#4}+3\Delta_{0^{+}}^{\#2}==0$ | 1 |
| $6\mathcal{T}_{1^{+}}^{\#1\alpha}-i(3k\Delta_{1^{+}}^{\#2\alpha}-\Delta_1^{\#5\alpha}+\Delta_1^{\#3\alpha})==0$ | 3 |
| $2\Delta_{1^{+}}^{\#6\alpha}+\Delta_{1^{+}}^{\#4\alpha}+2\Delta_{1^{+}}^{\#5\alpha}+\Delta_{1^{+}}^{\#3\alpha}==0$ | 3 |
| Total constraints: | 8 |

$$\Delta_{3^{+}}^{\#1}\Gamma^{\alpha\beta\chi} \quad \Delta_{3^{-}}^{\#1}\alpha\beta\chi$$

| | $\Delta_{2^{+}\alpha\beta}^{\#1}$ | $\Delta_{2^{+}\alpha\beta}^{\#2}$ | $\Delta_{2^{+}\alpha\beta}^{\#3}$ | $\mathcal{T}_{2^{+}\alpha\beta}^{\#1}$ | $\Delta_{2^{-}\alpha\beta\chi}^{\#1}$ | $\Delta_{2^{-}\alpha\beta\chi}^{\#2}$ |
|--|-----------------------------------|---|---|--|---------------------------------------|---------------------------------------|
| $\Delta_{2^{+}\alpha\beta}^{\#1}$ | 0 | $\frac{2\sqrt{\frac{2}{3}}}{a_0}$ | $\frac{4}{\sqrt{3}a_0}$ | $\frac{4i\sqrt{2}}{a_0k}$ | 0 | 0 |
| $\Delta_{2^{+}\alpha\beta}^{\#2}$ | $\frac{2\sqrt{\frac{2}{3}}}{a_0}$ | $-\frac{8(a_0+13a_1k^2)}{3a_0^2}$ | $-\frac{2\sqrt{2}(a_0+52a_1k^2)}{3a_0^2}$ | $-\frac{4i(a_0+31a_1k^2)}{\sqrt{3}a_0^2k}$ | 0 | 0 |
| $\Delta_{2^{+}\alpha\beta}^{\#3}$ | $\frac{4}{\sqrt{3}a_0}$ | $-\frac{2\sqrt{2}(a_0+52a_1k^2)}{3a_0^2}$ | $\frac{8(a_0-26a_1k^2)}{3a_0^2}$ | $-\frac{4i\sqrt{\frac{2}{3}}(a_0+31a_1k^2)}{a_0^2k}$ | 0 | 0 |
| $\mathcal{T}_{2^{+}\alpha\beta}^{\#1}$ | $\frac{4i\sqrt{2}}{a_0k}$ | $\frac{4i(a_0+31a_1k^2)}{\sqrt{3}a_0^2k}$ | $\frac{4i\sqrt{\frac{2}{3}}(a_0+31a_1k^2)}{a_0^2k}$ | $-\frac{8(a_0+11a_1k^2)}{a_0^2k^2}$ | 0 | 0 |
| $\Delta_{2^{-}\alpha\beta\chi}^{\#1}$ | 0 | 0 | 0 | 0 | $\frac{4}{a_0a_1k^2}$ | 0 |
| $\Delta_{2^{-}\alpha\beta\chi}^{\#2}$ | 0 | 0 | 0 | 0 | 0 | $\frac{4}{a_0-5a_1k^2}$ |

$$\Gamma_{3^{+}\alpha\beta\chi}^{\#1} \quad \Gamma_{3^{-}\alpha\beta\chi}^{\#1}$$

| | | | | | | |
|------------------------------|--------------------------|------------------------------------|------------------------------------|------------------------------|-----------------------------|----------------------------|
| $\frac{1}{2}(-a_0+25a_1k^2)$ | 0 | $10\sqrt{\frac{2}{3}}a_1k^2$ | $-\frac{10a_1k^2}{\sqrt{3}}$ | $-\frac{t_{00}k}{2\sqrt{2}}$ | 0 | 0 |
| 0 | 0 | $\frac{a_0}{2}$ | $-\frac{a_0}{2\sqrt{2}}$ | 0 | 0 | 0 |
| $10\sqrt{\frac{2}{3}}a_1k^2$ | $\frac{a_0}{2}$ | $\frac{23a_1k^2}{4}$ | $-\frac{3a_0+46a_1k^2}{6\sqrt{2}}$ | $\frac{t_{00}k}{4\sqrt{3}}$ | $-\frac{1}{4}\tilde{f}a_0k$ | 0 |
| $-\frac{10a_1k^2}{\sqrt{3}}$ | $-\frac{a_0}{2\sqrt{2}}$ | $-\frac{3a_0+46a_1k^2}{6\sqrt{2}}$ | $\frac{1}{6}(3a_0+23a_1k^2)$ | $\frac{t_{00}k}{4\sqrt{6}}$ | $\frac{t_{00}k}{4\sqrt{2}}$ | 0 |
| $\frac{t_{00}k}{2\sqrt{2}}$ | 0 | $-\frac{t_{00}k}{4\sqrt{3}}$ | $\frac{t_{00}k}{4\sqrt{6}}$ | 0 | 0 | 0 |
| 0 | 0 | $\frac{t_{00}k}{4}$ | $-\frac{t_{00}k}{4\sqrt{2}}$ | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | $\frac{1}{2}(-a_0+a_1k^2)$ |