


$$r_5 < -2r_3 \ \&\& \ t_1 < 0 \ || \ t_1 > 0$$

(No massive particles)

$\#1 + \alpha\beta$ $1 +$	0	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{i\sqrt{2}k}{t_1+k^2t_1}$	0	0	0	0
$\#2 + \alpha\beta$ $1 +$	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{2k^2(2r_3+r_5)+t_1}{(1+k^2)^2t_1^2}$	$-\frac{2ik^3(2r_3+r_5)+ikt_1}{(1+k^2)^2t_1^2}$	0	0	0	0
$\#1 + \alpha\beta$ $1 +$	$\frac{i\sqrt{2}k}{t_1+k^2t_1}$	$\frac{i(2k^3(2r_3+r_5)-kt_1)}{(1+k^2)^2t_1^2}$	$-\frac{2k^4(2r_3+r_5)+k^2t_1}{(1+k^2)^2t_1^2}$	0	0	0	0
$\sigma_1^{\#1} + \alpha$	0	0	0	$\frac{1}{k^2(2r_3+r_5)}$	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	0	$-\frac{i}{k(1+2k^2)(2r_3+r_5)}$
$\sigma_1^{\#2} + \alpha$	0	0	0	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	$\frac{6k^2(2r_3+r_5)+t_1}{2(k+2k^3)^2(2r_3+r_5)t_1}$	0	$\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$
$\tau_1^{\#1} + \alpha$	0	0	0	0	0	0	0
$\tau_1^{\#2} + \alpha$	0	0	0	$\frac{i}{k(1+2k^2)(2r_3+r_5)}$	$-\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$	0	$\frac{6k^2(2r_3+r_5)+t_1}{(1+2k^2)^2(2r_3+r_5)t_1}$

## Lagrangian density

$$\begin{aligned} & -\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\kappa\alpha}^{\kappa\lambda}\omega_{\kappa\lambda}^{\lambda'}-2r_3\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial_{\lambda}\omega_{\alpha}^{\alpha}-r_5\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial_{\lambda}\omega_{\alpha}^{\alpha}+ \\ & 2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\theta}^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\theta}^{\theta\kappa\lambda}-2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\theta\kappa\lambda}+ \\ & r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\theta\kappa\lambda}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\theta}^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\theta}^{\theta\kappa\lambda}+ \\ & 4r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial_{\alpha}f_{\theta\kappa}^{\kappa}f_{\alpha}^{\theta}- \\ & \frac{1}{2}t_1\partial_{\alpha}f_{\kappa\theta}^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial_{\alpha}f_{\kappa}^{\kappa}f_{\alpha}^{\lambda}\partial_{\kappa}f_{\alpha\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial_{\kappa}f_{\alpha}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial_{\kappa}f_{\alpha}^{\lambda}+ \\ & \frac{2}{3}t_1\partial_{\alpha}f_{\kappa\alpha}^{\kappa}f_{\alpha}^{\lambda}\partial_{\kappa}f_{\lambda}^{\lambda}\partial_{\kappa}f_{\alpha}^{\lambda}+2t_1\omega_{\lambda\kappa\theta}^{\theta}\partial_{\kappa}f_{\alpha}^{\lambda}\partial_{\lambda}\omega_{\alpha}^{\theta}-\frac{1}{3}t_1\omega_{\lambda\alpha}^{\alpha}\partial_{\kappa}f_{\alpha}^{\lambda}- \\ & \frac{1}{3}t_1\omega_{\lambda\alpha}^{\lambda}\partial_{\kappa}f_{\alpha}^{\lambda}+\frac{1}{2}t_1\partial_{\alpha}f_{\kappa}^{\kappa}f_{\alpha}^{\lambda}\partial_{\kappa}f_{\theta}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial_{\kappa}f_{\alpha}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial_{\kappa}f_{\alpha}^{\theta}- \\ & \frac{1}{3}t_1\partial_{\alpha}f_{\alpha}^{\lambda}\partial_{\kappa}f_{\lambda\kappa}^{\kappa}-4r_3\partial_{\kappa}^{\beta}\omega_{\alpha\beta}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda'}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\theta}^{\theta\kappa}+ \\ & r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\theta}^{\theta\kappa}+2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\alpha}^{\theta\kappa} \end{aligned}$$

Added source term:  $f^{\alpha\beta}$

	$\omega_{1^+}^{\#1} \alpha \beta$	$\omega_{1^+}^{\#2} \alpha \beta$	$f_{1^+}^{\#1} \alpha \beta$	$\omega_{1^-}^{\#1} \alpha$	$\omega_{1^-}^{\#2} \alpha$	$f_{1^-}^{\#1} \alpha$	$f_{1^-}^{\#2} \alpha$
$\omega_{1^+}^{\#1} \dagger \alpha \beta$	$k^2 (2r_3 + r_5) - \frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2} \dagger \alpha \beta$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0	0
$f_{1^+}^{\#1} \dagger \alpha \beta$	$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0	0	0
$\omega_{1^-}^{\#1} \dagger \alpha$	0	0	0	$k^2 (2r_3 + r_5) + \frac{t_1}{6}$	$\frac{t_1}{3\sqrt{2}}$	0	$\frac{ikt_1}{3}$
$\omega_{1^-}^{\#2} \dagger \alpha$	0	0	0	$\frac{t_1}{3\sqrt{2}}$	$\frac{t_1}{3}$	0	$\frac{1}{3} i \sqrt{2} kt_1$
$f_{1^-}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$f_{1^-}^{\#2} \dagger \alpha$	0	0	0	$-\frac{1}{3} i kt_1$	$-\frac{1}{3} i \sqrt{2} kt_1$	0	$\frac{2k^2 t_1}{3}$

	$\sigma_{2^+}^{\#1} \alpha \beta$	$\tau_{2^+}^{\#1} \alpha \beta$	$\sigma_{2^-}^{\#1} \alpha \beta \chi$
$\sigma_{2^+}^{\#1} \dagger \alpha \beta$	$\frac{2}{(1+2k^2)^2 t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	0
$\tau_{2^+}^{\#1} \dagger \alpha \beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	$\frac{4k^2}{(1+2k^2)^2 t_1}$	0
$\sigma_{2^-}^{\#1} \dagger \alpha \beta \chi$	0	0	$\frac{2}{t_1}$

	$\omega_{2^+}^{\#1} \alpha_\beta$	$f_{2^+}^{\#1} \alpha_\beta$	$\omega_{2^-}^{\#1} \alpha_\beta \chi$
$\omega_{2^+}^{\#1} \dagger^{\alpha_\beta}$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2^+}^{\#1} \dagger^{\alpha_\beta}$	$\frac{ikt_1}{\sqrt{2}}$	$k^2 t_1$	0
$\omega_{2^-}^{\#1} \dagger^{\alpha_\beta \chi}$	0	0	$\frac{t_1}{2}$

	$\sigma_0^{\#1}$	$\tau_0^{\#1}$	$\tau_0^{\#2}$	$\sigma_0^{\#1}$
$\sigma_0^{\#1} \uparrow$	$\frac{1}{6k^2 r_3}$	0	0	0
$\tau_0^{\#1} \uparrow$	0	0	0	0
$\tau_0^{\#2} \uparrow$	0	0	0	0
$\sigma_0^{\#1} \downarrow$	0	0	0	$-\frac{1}{t_1}$

$\omega_0^{\#1} \uparrow$	$6k^2 r_3$	0	0	0	$\omega_0^{\#1}$
$f_0^{\#1} \uparrow$	0	0	0	0	$f_0^{\#2}$
$f_0^{\#2} \uparrow$	0	0	0	0	$\omega_0^{\#1}$
$\omega_0^{\#1} \uparrow$	0	0	0	0	$-t_1$

Source constraints	
SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2\,i\,k\,\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i\,k\,\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2\,i\,k\,\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	16