

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{\#1} \dagger^{\alpha}$	$\sigma_{1-}^{\#2} \dagger^{\alpha}$	$\tau_{1-}^{\#1} \dagger^{\alpha}$	$\tau_{1-}^{\#2} \dagger^{\alpha}$
$\frac{1}{k^2(2r_3+r_5)}$	$-\frac{\sqrt{2}}{k^2(1+k^2)(2r_3+r_5)}$	$-\frac{i\sqrt{2}}{k(1+k^2)(2r_3+r_5)}$	0	0	0	0
$-\frac{\sqrt{2}}{k^2(1+k^2)(2r_3+r_5)}$	$\frac{3k^2(2r_3+r_5)+2t_2}{(k+k^2)^2(2r_3+r_5)t_2}$	$\frac{i(3k^2(2r_3+r_5)+2t_2)}{k(1+k^2)^2(2r_3+r_5)t_2}$	0	0	0	0
$\frac{i\sqrt{2}}{k(1+k^2)(2r_3+r_5)}$	$-\frac{i(3k^2(2r_3+r_5)+2t_2)}{k(1+k^2)^2(2r_3+r_5)t_2}$	$\frac{3k^2(2r_3+r_5)+2t_2}{(1+k^2)^2(2r_3+r_5)t_2}$	0	0	0	0
0	0	0	$\frac{2}{k^2(r_3+2r_5)}$	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

$\omega_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{\#2} \dagger^{\alpha\beta}$	$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{1-}^{\#1} \dagger^{\alpha}$	$\omega_{1-}^{\#2} \dagger^{\alpha}$	$f_{1-}^{\#1} \dagger^{\alpha}$	$f_{1-}^{\#2} \dagger^{\alpha}$
$k^2(2r_3+r_5)+\frac{2t_2}{3}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}i\sqrt{2}kt_2$	0	0	0	0
$\frac{\sqrt{2}t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0	0
$-\frac{1}{3}i\sqrt{2}kt_2$	$-\frac{1}{3}i\frac{kt_2}{3}$	$\frac{k^2t_2}{3}$	0	0	0	0
0	0	0	$\frac{1}{2}k^2(r_3+2r_5)$	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

Quadratic (free) Lagrangian density

$$\begin{aligned} & \frac{2}{3}t_2\omega_{\kappa\lambda}'\omega_{\kappa\lambda}' + \frac{1}{3}t_2\omega_{\kappa\lambda}'\omega_{\kappa\lambda}' + f^{\alpha\beta}\tau_{\alpha\beta} + \omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi} - \frac{1}{2}r_3\partial_\mu\omega_{\lambda}^{\kappa\lambda}\partial'_\mu\omega_{\lambda}^{\alpha} - \\ & r_5\partial_\mu\omega_{\kappa}^{\kappa\lambda}\partial'_\mu\omega_{\lambda}^{\alpha} + \frac{1}{2}r_3\partial_\alpha\omega_{\lambda}^{\alpha}\partial_{\theta\kappa}\omega_{\lambda}^{\theta\kappa\lambda} - r_5\partial_\alpha\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\lambda}^{\theta\kappa\lambda} - \frac{1}{2}r_3\partial_\theta\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\lambda}^{\theta\kappa\lambda} + \\ & r_5\partial_\theta\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\lambda}^{\theta\kappa\lambda} - \frac{1}{2}r_3\partial_\alpha\omega_{\lambda}^{\alpha}\partial_{\theta\kappa}\omega_{\lambda}^{\kappa\lambda\theta} - r_5\partial_\alpha\omega_{\lambda}^{\alpha}\partial_{\theta\kappa}\omega_{\lambda}^{\kappa\lambda\theta} + r_3\partial_\theta\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\lambda}^{\kappa\lambda\theta} + \\ & 2r_5\partial_\theta\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega_{\lambda}^{\kappa\lambda\theta} + \frac{1}{6}t_2\partial^\alpha f_{\theta\kappa}\partial^\kappa f_{\alpha}{}^\theta - \frac{1}{6}t_2\partial^\alpha f_{\kappa\theta}\partial^\kappa f_{\alpha}{}^\theta + \frac{1}{6}t_2\partial^\alpha f_{\lambda}{}^\theta\partial^\kappa f_{\alpha\lambda} + \\ & \frac{1}{3}t_2\omega_{\mu\theta\kappa}\partial^\kappa f^{\mu\theta} - \frac{2}{3}t_2\omega_{\mu\kappa\theta}\partial^\kappa f^{\mu\theta} - \frac{1}{3}t_2\omega_{\theta\mu\kappa}\partial^\kappa f^{\mu\theta} + \frac{2}{3}t_2\omega_{\theta\kappa\mu}\partial^\kappa f^{\mu\theta} - \\ & \frac{1}{6}t_2\partial^\alpha f_{\lambda}{}^\theta\partial_{\kappa}f_{\lambda\alpha} - \frac{1}{6}t_2\partial_{\kappa}f_{\lambda}{}^\theta\partial^\lambda f_{\lambda}{}^\theta + \frac{1}{6}t_2\partial_{\kappa}f_{\theta}{}^\lambda\partial^\kappa f_{\lambda}{}^\theta - 4r_3\partial^\beta\omega_{\lambda}^{\lambda\alpha}\partial_{\alpha}\omega_{\lambda}^{\beta} - \\ & \frac{1}{2}r_3\partial_\alpha\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\theta}^{\theta\kappa} + r_5\partial_\alpha\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\theta}^{\theta\kappa} + \frac{1}{2}r_3\partial_\theta\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\alpha}^{\theta\kappa} - r_5\partial_\theta\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\alpha}^{\theta\kappa} \end{aligned}$$

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{0+}^{\#2} == 0$	1
$\tau_{1-}^{2\alpha} == 0$	3
$\tau_{1-}^{1\alpha} == 0$	3
$\sigma_{1-}^{2\alpha} == 0$	3
$\tau_{1+}^{1\alpha\beta} + ik\sigma_{1+}^{2\alpha\beta} == 0$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{1\alpha\beta} == 0$	5
Total constraints:	25

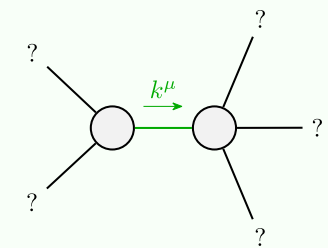
$\sigma_{0+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{0+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{0+}^{\#2} \dagger^{\alpha\beta}$	$\sigma_{0-}^{\#1} \dagger^{\alpha}$
0	0	0	0
0	0	0	0
0	0	0	0
0	0	0	$\frac{1}{t_2}$

$\omega_{0+}^{\#1} \dagger^{\alpha\beta}$	$f_{0+}^{\#1} \dagger^{\alpha\beta}$	$f_{0+}^{\#2} \dagger^{\alpha\beta}$	$\omega_{0-}^{\#1} \dagger^{\alpha}$
0	0	0	0
0	0	0	0
0	0	0	0
0	0	0	t_2

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$
$-\frac{2}{3k^2r_3}$	0	0
0	0	0
0	0	0

$\omega_{2+}^{\#1} \dagger^{\alpha\beta}$	$f_{2+}^{\#1} \dagger^{\alpha\beta}$	$\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$
$-\frac{3k^2r_3}{2}$	0	0
0	0	0
0	0	0

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$