

$$\begin{aligned}
& \text{Lagrangian density} \\
& -\frac{1}{3}t_1\omega_{,\lambda}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{,\lambda}^{\lambda}\omega_{\kappa\lambda}^{\lambda}-r_5\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial^{\lambda}\omega_{\lambda}^{\alpha}-\frac{2}{3}r_1\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}- \\
& \frac{2}{3}r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}+\frac{2}{3}r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\partial_{\kappa}\omega^{\theta\lambda\theta}+ \\
& r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\partial_{\kappa}\omega^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}- \\
& \frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}^{\alpha}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}^{\alpha}\partial^{\kappa}f_{\alpha}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\alpha\lambda}^{\lambda}+ \\
& \frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{,\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{,\lambda}^{\lambda}+\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{,\lambda}^{\lambda}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{,\lambda}^{\lambda}+ \\
& 2t_1\omega_{\lambda\kappa\theta}\partial^{\kappa}f^{\lambda\theta}-\frac{1}{3}t_1\omega_{,\lambda\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{\lambda}-\frac{1}{3}t_1\omega_{\lambda\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{\lambda}+\frac{1}{2}t_1\partial^{\alpha}f_{\kappa}^{\lambda}\partial^{\kappa}f_{\lambda\alpha}^{\alpha}+ \\
& \frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}-\frac{1}{3}t_1\partial^{\alpha}f_{\alpha}^{\lambda}\partial^{\kappa}f_{\lambda\kappa}^{\kappa}+ \\
& \frac{2}{3}r_1\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_1\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_1\partial^{\beta}\omega_{,\lambda}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}- \\
& \frac{8}{3}r_1\partial^{\beta}\omega_{,\lambda}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda}+r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}
\end{aligned}$$

Added source term: $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta}\chi_{\alpha\beta}\chi$

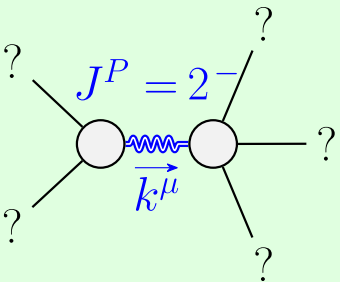
$$\begin{array}{ccc}
 \omega_{2^+}^{\#1} \alpha \beta & f_{2^+}^{\#1} \alpha \beta & \omega_{2^+}^{\#1} \alpha \beta_X \\
 \omega_{2^+}^{\#1} \dagger \alpha \beta & \frac{t_1}{2} & -\frac{i k t_1}{\sqrt{2}} & 0 \\
 f_{2^+}^{\#1} \dagger \alpha \beta & \frac{i k t_1}{\sqrt{2}} & k^2 t_1 & 0 \\
 \omega_{2^+}^{\#1} \dagger \alpha \beta_X & 0 & 0 & k^2 r_1 + \frac{t_1}{2}
 \end{array}$$

$\sigma_0^{\#1} +$	0	0	0	0
$\tau_0^{\#1} +$	0	0	0	0
$\tau_0^{\#2} +$	0	0	0	0
$\sigma_0^{\#1} +$	0	0	0	$-\frac{1}{t_1}$

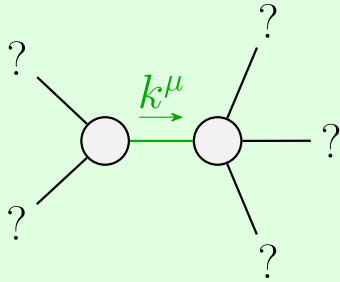
	$\omega_{0+}^{\#1}$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
$\omega_{0+}^{\#1} \dagger$	0	0	0	0
$f_{0+}^{\#1} \dagger$	0	0	0	0
$f_{0+}^{\#2} \dagger$	0	0	0	0
$\omega_{0-}^{\#1} \dagger$	0	0	0	$-t_1$

Source constraints	
SO(3) irreps	#
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{0+}^{\#2} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2 i k \sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2 i k \sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	17

	$\sigma_{2^+}^{\#1} \alpha\beta$	$\tau_{2^+}^{\#1} \alpha\beta$	$\sigma_{2^+}^{\#1} \alpha\beta\chi$
$\sigma_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{2}{(1+2k^2)^2 t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	0
$\tau_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	$\frac{4k^2}{(1+2k^2)^2 t_1}$	0
$\sigma_{2^+}^{\#1} \dagger \alpha\beta\chi$	0	0	$\frac{2}{2k^2 r_1 + t_1}$



Massive particle	
Pole residue:	$-\frac{1}{r_1} > 0$
Polarisations:	5
Square mass:	$-\frac{t_1}{2r_1} > 0$
Spin:	2
Parity:	Odd



Quadratic pole	
Pole residue:	$-\frac{1}{(r_1+r_5)t_1^2} > 0$
Polarisations:	2

Unitarity conditions

$$r_1 < 0 \ \&\& \ r_5 < -r_1 \ \&\& \ t_1 > 0$$