

# Wave operator and propagator

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$$\begin{aligned}
& \text{Quadratic (free) action} \\
S = & \int \int \int \int \left( \frac{1}{6} (-4t_3 \omega_{\alpha}^{\alpha i} \omega_{\kappa}^{\kappa} + 6 f^{\alpha \beta} \tau_{\alpha \beta} + 6 \omega^{\alpha \beta X} \sigma_{\alpha \beta X} + 8 t_3 \omega_{\alpha}^{\kappa} \partial_{\kappa} f^{\alpha i} - 8 t_3 \omega_{\kappa}^{\alpha} \partial_{\alpha} f^{\kappa i} - \right. \\
& \partial_{\alpha} f^{\alpha} + 4 t_3 \partial_{\alpha} f^{\kappa} \partial_{\kappa} f^{\alpha} + 4 t_2 \omega_{\alpha \theta} \partial^{\theta} f^{\alpha i} + 2 t_2 \partial_{\alpha} f_{\theta}^{\theta} \partial^{\theta} f^{\alpha i} - t_2 \partial_{\alpha} f_{\theta i} \partial^{\theta} f^{\alpha i} - \\
& t_2 \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha i} + t_2 \partial_{\theta} f_{\alpha i} \partial^{\theta} f^{\alpha i} - t_2 \partial_{\theta} f_{\alpha} \partial^{\theta} f^{\alpha i} - 4 t_2 \omega_{\alpha \theta i} (\omega^{\alpha i \theta} + \partial^{\theta} f^{\alpha i}) + \\
& 2 t_2 \omega_{\alpha i \theta} (\omega^{\alpha i \theta} + 2 \partial^{\theta} f^{\alpha i}) + 8 r_2 \partial_{\beta} \omega_{\alpha i \theta} \partial^{\theta} \omega^{\alpha \beta i} - 4 r_2 \partial_{\beta} \omega_{\alpha \theta i} \partial^{\theta} \omega^{\alpha \beta i} + \\
& 4 r_2 \partial_{\beta} \omega_{\theta \alpha} \partial^{\theta} \omega^{\alpha \beta i} - 2 r_2 \partial_{\alpha} \omega_{\alpha \beta \theta} \partial^{\theta} \omega^{\alpha \beta i} + 2 r_2 \partial_{\theta} \omega_{\alpha \beta i} \partial^{\theta} \omega^{\alpha \beta i} - \\
& 4 r_2 \partial_{\theta} \omega_{\alpha \beta} \partial^{\theta} \omega^{\alpha \beta i} + 6 r_5 \partial_{\alpha} \omega_{\kappa}^{\kappa} \partial^{\theta} \omega^{\alpha i} - 6 r_5 \partial_{\theta} \omega_{\kappa}^{\kappa} \partial^{\theta} \omega^{\alpha i} + \\
& 4 t_3 \partial_{\alpha} f^{\alpha i} \partial_{\kappa} f^{\kappa} - 8 t_3 \partial_{\alpha} f^{\alpha} \partial_{\kappa} f^{\kappa} - 6 r_5 \partial_{\alpha} \omega^{\alpha i \theta} \partial_{\kappa} \omega_{\theta}^{\kappa} + 12 r_5 \partial^{\theta} \omega_{\theta}^{\alpha i} \partial_{\kappa} \omega_{\theta}^{\kappa} + \\
& \left. 6 r_5 \partial_{\alpha} \omega^{\alpha i \theta} \partial_{\kappa} \omega_{\theta}^{\kappa} - 12 r_5 \partial^{\theta} \omega_{\theta}^{\alpha i} \partial_{\kappa} \omega_{\theta}^{\kappa} \right) [t, x, y, z] dz dy dx dt
\end{aligned}$$

$\sigma_0^{\#1} \dagger$	$\frac{1}{(1+2k^2)^2 t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	$0$	$0$
$\tau_0^{\#1} \dagger$	$\frac{i\sqrt{2}k}{(1+2k^2)^2 t_3}$	$\frac{2k^2}{(1+2k^2)^2 t_3}$	$0$	$0$
$\tau_0^{\#2} \dagger$	$0$	$0$	$0$	$0$
$\sigma_0^{\#1} \dagger$	$0$	$0$	$0$	$\frac{1}{k^2 r_2 + t_2}$

The diagram shows two vertices, each a circle with four external lines. The left vertex has two incoming lines (bottom-left and top-left) and two outgoing lines (bottom-right and top-right). The right vertex has two incoming lines (bottom-right and top-right) and two outgoing lines (bottom-left and top-left). A dashed blue line connects the two vertices, with an arrow pointing from left to right labeled  $k^\mu$ . Above the dashed line is the text  $J^P = 0^-$ .

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

$$r_2 < 0 \ \&\& \ t_2 > 0$$