

Particle spectrograph

Wave operator and propagator

Quadratic (free) action

$$\begin{aligned} S_F = & \iiint \left(\frac{1}{6} \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 3(r_3 + 2r_5) \partial_\lambda \omega_\alpha^\lambda \partial_\lambda \omega_\alpha^\alpha + 4r_2 \partial^\beta \omega_\alpha^\beta \partial_\theta \omega_\alpha^\alpha - 2r_2 \partial_\theta \omega_\alpha^\alpha \partial_\kappa \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha - 4r_2 \partial_\theta \omega_\alpha^\alpha \partial_\kappa \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha + 3r_3 \partial_\alpha \omega_\lambda^\alpha \partial_\theta \omega_\lambda^\alpha \partial^\beta \omega_\lambda^\beta - 6r_5 \partial_\alpha \omega_\lambda^\alpha \partial_\theta \omega_\lambda^\alpha \partial^\beta \omega_\lambda^\beta - \right. \\ & 3r_3 \partial_\theta \omega_\lambda^\alpha \partial_\alpha \omega_\lambda^\beta \partial^\beta \omega_\lambda^\alpha + 6r_5 \partial_\theta \omega_\lambda^\alpha \partial_\alpha \omega_\lambda^\beta \partial^\beta \omega_\lambda^\alpha - 3r_3 \partial_\alpha \omega_\lambda^\alpha \partial_\theta \omega_\lambda^\alpha \partial^\beta \omega_\lambda^\beta + 6r_5 \partial_\alpha \omega_\lambda^\alpha \partial_\theta \omega_\lambda^\alpha \partial^\beta \omega_\lambda^\beta + 12r_5 \partial_\theta \omega_\lambda^\alpha \partial_\alpha \omega_\lambda^\beta \partial^\beta \omega_\lambda^\alpha + \\ & 2r_2 \partial_\kappa \omega_\alpha^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha + 4r_2 \partial_\kappa \omega_\alpha^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha - 4r_2 \partial_\kappa \omega_\alpha^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha + 4r_2 \partial_\kappa \omega_\alpha^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha + \\ & \partial_\lambda \omega_\alpha^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha - 24r_3 \partial_\alpha \omega_\lambda^\alpha \partial_\lambda \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha - 3r_3 \partial_\alpha \omega_\lambda^\alpha \partial_\lambda \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha + 6r_5 \partial_\alpha \omega_\lambda^\alpha \partial_\lambda \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha + \\ & \left. 3r_3 \partial_\theta \omega_\lambda^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha - 6r_5 \partial_\theta \omega_\lambda^\alpha \partial^\beta \omega_\alpha^\beta \partial^\beta \omega_\alpha^\alpha \right) [t, x, y, z] dz dy dx dt \end{aligned}$$

	$\sigma_{1^+ \alpha\beta}^{\#1}$	$\sigma_{1^+ \alpha\beta}^{\#2}$	$\sigma_{1^- \alpha}^{\#1}$	$\sigma_{1^- \alpha}^{\#2}$
$\sigma_{1^+ \alpha\beta}^{\#1}$	$\frac{1}{k^2(2r_3+r_5)}$	0	0	0
$\sigma_{1^+ \alpha\beta}^{\#2}$	0	0	0	0
$\sigma_{1^- \alpha}^{\#1}$	0	0	$\frac{2}{k^2(r_3+2r_5)}$	0
$\sigma_{1^- \alpha}^{\#2}$	0	0	0	0

	$\omega_{1^+ \alpha\beta}^{\#1}$	$\omega_{1^+ \alpha\beta}^{\#2}$	$\omega_{1^- \alpha}^{\#1}$	$\omega_{1^- \alpha}^{\#2}$
$\omega_{1^+ \alpha\beta}^{\#1}$	$k^2(2r_3+r_5)$	0	0	0
$\omega_{1^+ \alpha\beta}^{\#2}$	0	0	0	0
$\omega_{1^- \alpha}^{\#1}$	0	$\frac{1}{2} k^2(r_3+2r_5)$	0	0
$\omega_{1^- \alpha}^{\#2}$	0	0	0	0

Source constraints/gauge generators

SO(3) irreps	Multiplicities
$\sigma_0^{\#1} == 0$	1
$\sigma_1^{\#2\alpha} == 0$	3
$\sigma_1^{\#2\alpha\beta} == 0$	3
$\sigma_2^{\#1\alpha\beta\chi} == 0$	5
Total constraints: 12	

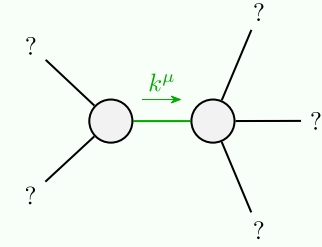
$\omega_{2^+ \alpha\beta}^{\#1}$	$\omega_{2^+ \alpha\beta}^{\#2}$	$\omega_{2^- \alpha\beta\chi}^{\#1}$	$\omega_{2^- \alpha\beta\chi}^{\#2}$
$\frac{3k^2 r_3}{2}$	0	0	0

$\omega_{0^+}^{\#1}$	$\omega_{0^+}^{\#2}$	$\omega_{0^-}^{\#1}$	$\omega_{0^-}^{\#2}$
0	0	0	$k^2 r_2$

$\sigma_0^{\#1}$	$\sigma_0^{\#2}$	$\sigma_0^{\#1}$	$\sigma_0^{\#2}$
0	0	0	$\frac{1}{k^2 r_2}$

$\sigma_{2^+ \alpha\beta}^{\#1}$	$\sigma_{2^+ \alpha\beta\chi}^{\#1}$	$\sigma_{2^- \alpha\beta\chi}^{\#1}$	$\sigma_{2^- \alpha\beta\chi}^{\#2}$
$-\frac{2}{3k^2 r_3}$	0	0	0

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)} > 0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$