

## Wave operator and propagator

$$S = \int \int \int \int (\mathcal{A}^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + \frac{1}{r_2} (4 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta} - 2 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta} + 2 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta} - \partial_{\rho\beta} \mathcal{A}_{\alpha\theta} + \partial_{\rho\beta} \mathcal{A}_{\alpha\theta} - 2 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}) \partial^{\rho} \mathcal{A}_{\alpha\beta}^{\theta} - \frac{1}{2} r_3 (\partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} + \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} + \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} - 2 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} + \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} - 2 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} + 8 \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} + r_5 (\partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} - \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} - (\partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha} - \partial_{\rho\beta} \mathcal{A}_{\alpha\theta}^{\theta} \partial^{\rho} \mathcal{A}_{\alpha\theta}^{\alpha})) [t, x, y, z] d x d y d z d t$$

$$\begin{array}{c}
\begin{array}{c} \#^1 \\ 0^+ \end{array} \begin{array}{c} \mathcal{A} \\ 0^+ \end{array} \begin{array}{c} \mathcal{A} \\ 0^+ \end{array} \begin{array}{c} \mathcal{A} \\ 0^+ \end{array} \\
\begin{array}{c} \#^1 \\ 0^+ \end{array} \begin{array}{c} \mathcal{A} \\ 0^+ \end{array} \begin{array}{c} \mathcal{A} \\ 0^+ \end{array} \begin{array}{c} \mathcal{A} \\ 0^+ \end{array}
\end{array}
\begin{array}{|c|c|} \hline 0 & k^2 r_2 \\ \hline 0 & 0 \\ \hline \end{array}$$

$$\begin{array}{c} \#^1 \\ 0^+ \end{array} \begin{array}{c} \sigma \\ 0^+ \end{array} \begin{array}{c} \sigma \\ 0^+ \end{array} \begin{array}{c} \sigma \\ 0^+ \end{array}
\begin{array}{|c|c|} \hline 0 & 0 \\ \hline 0 & \frac{1}{k^2 r_2} \\ \hline \end{array}$$

$$\begin{array}{c} \#^1 \\ 1^+ \end{array} \begin{array}{c} \sigma \alpha \beta \\ 1^+ \end{array} \begin{array}{c} \sigma \alpha \beta \\ 1^+ \end{array} \begin{array}{c} \sigma \alpha \\ 1^- \end{array} \begin{array}{c} \sigma \alpha \\ 1^- \end{array}
\begin{array}{|c|c|c|c|} \hline \frac{1}{k^2 (2r_3 + r_5)} & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & \frac{2}{k^2 (r_3 + 2r_5)} & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

$$\begin{array}{c} \#^1 \\ 1^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \beta \\ 1^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \beta \\ 1^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \\ 1^- \end{array} \begin{array}{c} \mathcal{A} \alpha \\ 1^- \end{array}
\begin{array}{|c|c|c|c|} \hline k^2 (2r_3 + r_5) & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & \frac{1}{2} k^2 (r_3 + 2r_5) & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

$$\begin{array}{c} \#^1 \\ 2^+ \end{array} \begin{array}{c} \sigma \alpha \beta \\ 2^+ \end{array} \begin{array}{c} \sigma \alpha \beta \\ 2^+ \end{array} \begin{array}{c} \sigma \alpha \beta \\ 2^+ \end{array} \begin{array}{c} \sigma \alpha \beta \\ 2^+ \end{array}
\begin{array}{|c|c|} \hline 0 & 0 \\ \hline -\frac{2}{3k^2 r_3} & 0 \\ \hline \end{array}$$

$$\begin{array}{c} \#^1 \\ 2^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \beta \\ 2^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \beta \\ 2^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \beta \\ 2^+ \end{array} \begin{array}{c} \mathcal{A} \alpha \beta \\ 2^+ \end{array}
\begin{array}{|c|c|} \hline 0 & 0 \\ \hline -\frac{3k^2 r_3}{2} & 0 \\ \hline \end{array}$$

## Unitarity conditions