



Quadratic pole

Pole residue:  $-\frac{1}{r_3(2r_3+r_5)(r_3+2r_5)p^2} > 0$

Polarisations: 2

Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$

(No massive particles)

$\sigma_{1+}^{\#1} \alpha\beta$	$\sigma_{1+}^{\#2} \alpha\beta$	$\tau_{1+}^{\#1} \alpha\beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\frac{1}{k^2(2r_3+r_5)}$	0	0	0	0	0	0
$\sigma_{1+}^{\#2} \alpha\beta$	0	0	0	0	0	0
$\tau_{1+}^{\#1} \alpha\beta$	0	0	0	0	0	0
$\sigma_{1-}^{\#1} \alpha$	0	0	$\frac{2}{k^2(r_3+2r_5)}$	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	0	$\frac{4i}{k(1+2k^2)(r_3+2r_5)}$
$\sigma_{1-}^{\#2} \alpha$	0	0	$\frac{2\sqrt{2}}{k^2(1+2k^2)(r_3+2r_5)}$	$\frac{3k^2(r_3+2r_5)+4t_3}{(k+2k^3)^2(r_3+2r_5)t_3}$	0	$\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$
$\tau_{1-}^{\#1} \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2} \alpha$	0	0	$-\frac{4i}{k(1+2k^2)(r_3+2r_5)}$	$-\frac{i\sqrt{2}(3k^2(r_3+2r_5)+4t_3)}{k(1+2k^2)^2(r_3+2r_5)t_3}$	0	$\frac{6k^2(r_3+2r_5)+8t_3}{(1+2k^2)^2(r_3+2r_5)t_3}$

$\omega_{1+}^{\#1} \alpha\beta$	$\omega_{1+}^{\#2} \alpha\beta$	$f_{1+}^{\#1} \alpha\beta$	$\omega_{1-}^{\#1} \alpha$	$\omega_{1-}^{\#2} \alpha$	$f_{1-}^{\#1} \alpha$	$f_{1-}^{\#2} \alpha$
$k^2(2r_3+r_5)$	0	0	0	0	0	0
$\omega_{1+}^{\#2} \alpha\beta$	0	0	0	0	0	0
$f_{1+}^{\#1} \alpha\beta$	0	0	0	0	0	0
$\omega_{1-}^{\#1} \alpha$	0	0	$k^2(\frac{r_3}{2}+r_5)+\frac{2t_3}{3}$	$-\frac{\sqrt{2}t_3}{3}$	0	$-\frac{2}{3}it_3$
$\omega_{1-}^{\#2} \alpha$	0	0	$-\frac{\sqrt{2}t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_3$
$f_{1-}^{\#1} \alpha$	0	0	0	0	0	0
$f_{1-}^{\#2} \alpha$	0	0	$\frac{2ikt_3}{3}$	$-\frac{1}{3}i\sqrt{2}kt_3$	0	$\frac{2k^2t_3}{3}$

Lagrangian density

$$\begin{aligned} &\frac{2}{3}t_3\omega_{\lambda'}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-\frac{1}{2}r_3\partial_{\lambda'}\omega_{\kappa}^{\kappa\lambda}\partial'_{\kappa}\omega_{\lambda}^{\alpha}- \\ &r_5\partial_{\lambda'}\omega_{\kappa}^{\kappa\lambda}\partial'_{\kappa}\omega_{\lambda}^{\alpha}+\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}- \\ &\frac{1}{2}r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}- \\ &r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}+r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}- \\ &\frac{2}{3}t_3\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f'_{\lambda}-\frac{2}{3}t_3\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f'_{\lambda}-\frac{4}{3}t_3\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f'_{\lambda}+ \\ &\frac{2}{3}t_3\partial_{\kappa}f'_{\lambda}\partial^{\kappa}f'_{\lambda}+\frac{2}{3}t_3\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f'_{\kappa}+\frac{2}{3}t_3\omega_{\lambda\lambda}^{\lambda}\partial^{\kappa}f'_{\kappa}+ \\ &\frac{2}{3}t_3\partial^{\alpha}f_{\lambda\kappa}\partial^{\kappa}f_{\lambda\kappa}-4r_3\partial^{\beta}\omega_{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\lambda\alpha}-\frac{1}{2}r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}+ \\ &r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\lambda\theta\kappa}+\frac{1}{2}r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\alpha}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa} \end{aligned}$$

Added source term:  $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

Source constraints

SO(3) irreps	#
$\sigma_0^{\#1} == 0$	1
$\tau_0^{\#2} == 0$	1
$\tau_0^{\#1} - 2ik\sigma_0^{\#1} == 0$	1
$\tau_1^{\#2\alpha} + 2ik\sigma_1^{\#2\alpha} == 0$	3
$\tau_1^{\#1\alpha} == 0$	3
$\tau_1^{\#1\alpha\beta} == 0$	3
$\sigma_1^{\#2\alpha\beta} == 0$	3
$\sigma_2^{\#1\alpha\beta\chi} == 0$	5
$\tau_2^{\#1\alpha\beta} == 0$	5
Total #:	25

$\omega_{2+}^{\#1} \alpha\beta$	$f_{2+}^{\#1} \alpha\beta$	$\omega_{2-}^{\#1} \alpha\beta\chi$
$\omega_{2+}^{\#1} \alpha\beta$	$-\frac{3k^2r_3}{2}$	0
$f_{2+}^{\#1} \alpha\beta$	0	0
$\omega_{2-}^{\#1} \alpha\beta\chi$	0	0

$\omega_{0+}^{\#1} \alpha\beta$	$f_{0+}^{\#1} \alpha\beta$	$f_{0+}^{\#2} \alpha\beta$	$\omega_{0-}^{\#1} \alpha\beta\chi$
$\omega_{0+}^{\#1} \alpha\beta$	$t_3$	$-i\sqrt{2}kt_3$	0
$f_{0+}^{\#1} \alpha\beta$	$i\sqrt{2}kt_3$	$2k^2t_3$	0
$f_{0+}^{\#2} \alpha\beta$	0	0	0
$\omega_{0-}^{\#1} \alpha\beta\chi$	0	0	0

$\sigma_{2+}^{\#1} \alpha\beta$	$\tau_{2+}^{\#1} \alpha\beta$	$\sigma_{2-}^{\#1} \alpha\beta\chi$
$\sigma_{2+}^{\#1} \alpha\beta$	$-\frac{2}{3k^2r_3}$	0
$\tau_{2+}^{\#1} \alpha\beta$	0	0
$\sigma_{2-}^{\#1} \alpha\beta\chi$	0	0

$\sigma_{0+}^{\#1} \alpha\beta$	$\tau_{0+}^{\#1} \alpha\beta$	$\tau_{0+}^{\#2} \alpha\beta$	$\sigma_{0-}^{\#1} \alpha\beta\chi$
$\sigma_{0+}^{\#1} \alpha\beta$	$\frac{1}{(1+2k^2)^2t_3}$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	0
$\tau_{0+}^{\#1} \alpha\beta$	$\frac{i\sqrt{2}k}{(1+2k^2)^2t_3}$	$\frac{2k^2}{(1+2k^2)^2t_3}$	0
$\tau_{0+}^{\#2} \alpha\beta$	0	0	0
$\sigma_{0-}^{\#1} \alpha\beta\chi$	0	0	0