



Quadratic pole

Pole residue:	$\frac{1}{r_1(r_1-2r_3-r_5)(2r_3+r_5)} > 0$
Polarisations:	2

(No massive particles)

## Lagrangian density

$$\begin{aligned}
 & 2r_1\partial_i\omega_{\kappa}^{\kappa\lambda}\partial'\omega_{\lambda}^{\alpha}{}_{\alpha}-2r_3\partial_i\omega_{\kappa}^{\kappa\lambda}\partial'\omega_{\lambda}^{\alpha}{}_{\alpha}- \\
 & r_5\partial_i\omega_{\kappa}^{\kappa\lambda}\partial'\omega_{\lambda}^{\alpha}{}_{\alpha}-\frac{2}{3}r_1\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{2}{3}r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\theta\theta}+ \\
 & \frac{2}{3}r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}-2r_1\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}+2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}- \\
 & r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}+2r_1\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+ \\
 & r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+2r_1\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}- \\
 & r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}-4r_1\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+4r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+ \\
 & 2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+\frac{2}{3}r_1\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}-\frac{2}{3}r_1\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}+ \\
 & \frac{2}{3}r_1\partial^{\beta}\omega_{\lambda}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}+\frac{4}{3}r_1\partial^{\beta}\omega_{\lambda}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}-4r_3\partial^{\beta}\omega_{\lambda}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}+ \\
 & 2r_1\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}+r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}- \\
 & 2r_1\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}+2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\kappa}^{\theta\kappa}
 \end{aligned}$$

Added source term:  $\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

	$\omega_{1+}^{\#1+\alpha\beta}$	$\omega_{1+}^{\#2+\alpha\beta}$	$\omega_{1-}^{\#1-\alpha}$	$\omega_{1-}^{\#2-\alpha}$
$\omega_{1+}^{\#1+}+\alpha\beta$	$k^2(2r_3+r_5)$	0	0	0
$\omega_{1+}^{\#2+}+\alpha\beta$	0	0	0	0
$\omega_{1-}^{\#1-}+\alpha$	0	0	$k^2(-r_1+2r_3+r_5)$	0
$\omega_{1-}^{\#2-}+\alpha$	0	0	0	0

	$\sigma_{2+}^{\#1+}+\alpha\beta$	$\sigma_{2-}^{\#1-}+\alpha\beta\chi$
$\sigma_{2+}^{\#1+}+\alpha\beta$	0	0
$\sigma_{2-}^{\#1-}+\alpha\beta\chi$	0	$\frac{1}{k^2r_1}$

	$\omega_{0+}^{\#1+}$	$\omega_{0-}^{\#1-}$
$\omega_{0+}^{\#1+}+\alpha\beta$	$6k^2(-r_1+r_3)$	0
$\omega_{0-}^{\#1-}+\alpha$	0	0

	$\sigma_{0+}^{\#1+}$	$\sigma_{0-}^{\#1-}$
$\sigma_{0+}^{\#1+}+\alpha$	$\frac{1}{6k^2(-r_1+r_3)}$	0
$\sigma_{0-}^{\#1-}+\alpha$	0	0

	$\omega_{2+}^{\#1+}+\alpha\beta$	$\omega_{2-}^{\#1-}+\alpha\beta\chi$
$\omega_{2+}^{\#1+}+\alpha\beta$	0	0
$\omega_{2-}^{\#1-}+\alpha\beta\chi$	0	$k^2r_1$

	$\sigma_{1+}^{\#1+}+\alpha\beta$	$\sigma_{1+}^{\#2+}+\alpha\beta$	$\sigma_{1-}^{\#1-}+\alpha$	$\sigma_{1-}^{\#2-}+\alpha$
$\sigma_{1+}^{\#1+}+\alpha\beta$	$\frac{1}{k^2(2r_3+r_5)}$	0	0	0
$\sigma_{1+}^{\#2+}+\alpha\beta$	0	0	0	0
$\sigma_{1-}^{\#1-}+\alpha$	0	0	$\frac{1}{k^2(-r_1+2r_3+r_5)}$	0
$\sigma_{1-}^{\#2-}+\alpha$	0	0	0	0

Source constraints	SO(3) irreps	#
$\sigma_{0-}^{\#1-} == 0$		1
$\sigma_{1-}^{\#2\alpha} == 0$		3
$\sigma_{1+}^{\#2\alpha\beta} == 0$		3
$\sigma_{2+}^{\#1\alpha\beta} == 0$		5
Total #:		12

## Unitarity conditions

$$r_1 < 0 \&\& (r_5 < r_1 - 2r_3 \parallel r_5 > -2r_3) \parallel r_1 > 0 \&\& -2r_3 < r_5 < r_1 - 2r_3$$