

Particle spectrograph

Wave operator and propagator

$\sigma_{1+}^{\#1} + \alpha\beta$	$\sigma_{1+}^{\#2}$	$\tau_{1+}^{\#1} + \alpha\beta$	$\sigma_{1-}^{\#1} \alpha$	$\sigma_{1-}^{\#2} \alpha$	$\tau_{1-}^{\#1} \alpha$	$\tau_{1-}^{\#2} \alpha$
$\frac{1}{k^2 r_5}$	$-\frac{\sqrt{2}}{k^2 r_5 + k^4 r_5}$	$-\frac{i \sqrt{2}}{k r_5 + k^3 r_5}$	0	0	0	0
$-\frac{\sqrt{2}}{k^2 r_5 + k^4 r_5}$	$\frac{3 k^2 r_5 + 2 t_2}{(k + k^3)^2 r_5 t_2}$	$\frac{i (3 k^2 r_5 + 2 t_2)}{k (1 + k^2)^2 r_5 t_2}$	0	0	0	0
$\frac{i \sqrt{2}}{k r_5 + k^3 r_5}$	$-\frac{i (3 k^2 r_5 + 2 t_2)}{k (1 + k^2)^2 r_5 t_2}$	$\frac{3 k^2 r_5 + 2 t_2}{(1 + k^2)^2 r_5 t_2}$	0	0	0	0
$\sigma_{1-}^{\#1} + \alpha$	0	0	$\frac{1}{k^2 r_5}$	$\frac{\sqrt{2}}{k^2 r_5 + 2 k^4 r_5}$	0	$\frac{2 i}{k r_5 + 2 k^3 r_5}$
$\sigma_{1-}^{\#2} + \alpha$	0	0	$\frac{\sqrt{2}}{k^2 r_5 + 2 k^4 r_5}$	$\frac{3 k^2 r_5 + 2 t_3}{(k + 2 k^3)^2 r_5 t_3}$	0	$\frac{i \sqrt{2} (3 k^2 r_5 + 2 t_3)}{k (1 + 2 k^2)^2 r_5 t_3}$
$\tau_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2} + \alpha$	0	0	$-\frac{2 i}{k r_5 + 2 k^3 r_5}$	$-\frac{i \sqrt{2} (3 k^2 r_5 + 2 t_3)}{k (1 + 2 k^2)^2 r_5 t_3}$	0	$\frac{6 k^2 r_5 + 4 t_3}{(1 + 2 k^2)^2 r_5 t_3}$

Quadratic (free) action

$$S = \iiint \left(\frac{1}{6} (-4 t_3 \omega_{\alpha}^{\alpha i} \omega_{\kappa}^{\kappa} + 6 f^{\alpha \beta} \tau_{\alpha \beta} + 6 \omega^{\alpha \beta \chi} \sigma_{\alpha \beta \chi} + 8 t_3 \omega_{\alpha}^{\kappa} \partial_{\kappa} f^{\alpha i} - 8 t_3 \omega_{\kappa}^{\alpha} \partial_{\alpha} f^{\alpha i} - \partial_{\alpha} f^{\alpha} + 4 t_3 \partial_{\alpha} f_{\kappa}^{\kappa} \partial_{\alpha} f_{\kappa}^{\alpha} + 4 t_2 \omega_{\theta \alpha} \partial^{\theta} f^{\alpha i} + 2 t_2 \partial_{\alpha} f_{\theta} \partial^{\theta} f^{\alpha i} - t_2 \partial_{\alpha} f_{\theta i} \partial^{\theta} f^{\alpha i} - t_2 \partial_{\alpha} f_{\alpha \theta} \partial^{\theta} f^{\alpha i} + 2 t_2 \omega_{\alpha i \theta} (\omega^{\alpha i \theta} + 2 \partial^{\theta} f^{\alpha i}) + 8 r_2 \partial_{\beta} \omega_{\alpha i \theta} \partial^{\theta} \omega^{\alpha \beta i} - 4 t_2 \omega_{\alpha \theta i} (\omega^{\alpha i \theta} + \partial^{\theta} f^{\alpha i}) + 4 r_2 \partial_{\beta} \omega_{\alpha i \theta} \partial^{\theta} \omega^{\alpha \beta i} - 2 r_2 \partial_{\alpha} \omega_{\alpha \beta \theta} \partial^{\theta} \omega^{\alpha \beta i} + 2 r_2 \partial_{\theta} \omega_{\alpha \beta i} \partial^{\theta} \omega^{\alpha \beta i} + 4 r_2 \partial_{\theta} \omega_{\alpha i \beta} \partial^{\theta} \omega^{\alpha \beta i} + 6 r_5 \partial_{\alpha} \omega_{\theta}^{\kappa} \partial^{\theta} \omega_{\kappa}^{\alpha i} - 6 r_5 \partial_{\theta} \omega_{\alpha}^{\kappa} \partial^{\theta} \omega_{\kappa}^{\alpha i} + 4 t_3 \partial_{\alpha} f^{\alpha i} \partial_{\kappa} f_{\alpha}^{\kappa} - 8 t_3 \partial_{\alpha} f_{\alpha}^{\kappa} \partial_{\kappa} f_{\alpha}^{\alpha} + 6 r_5 \partial_{\alpha} \omega^{\alpha i \theta} \partial_{\kappa} \omega_{\theta}^{\kappa} + 12 r_5 \partial_{\alpha} \omega^{\alpha i} \partial_{\kappa} \omega_{\theta}^{\kappa} + 6 r_5 \partial_{\alpha} \omega^{\alpha i \theta} \partial_{\kappa} \omega_{\theta}^{\kappa} - 12 r_5 \partial^{\theta} \omega^{\alpha i} \partial_{\alpha} \omega_{\theta}^{\kappa}) [t, x, y, z] dz dy dx dt$$

$\omega_{1+}^{\#1} + \alpha\beta$	$\omega_{1+}^{\#2}$	$f_{1+}^{\#1} + \alpha\beta$	$\omega_{1-}^{\#1} \alpha$	$\omega_{1-}^{\#2} \alpha$	$f_{1-}^{\#1} \alpha$	$f_{1-}^{\#2} \alpha$
$k^2 r_5 + \frac{2 t_2}{3}$	$\frac{\sqrt{2} t_2}{3}$	$\frac{1}{3} i \sqrt{2} k t_2$	0	0	0	0
$\frac{\sqrt{2} t_2}{3}$	$\frac{t_2}{3}$	$\frac{i k t_2}{3}$	0	0	0	0
$-\frac{1}{3} i \sqrt{2} k t_2$	$-\frac{1}{3} i k t_2$	$\frac{k^2 t_2}{3}$	0	0	0	0
$\omega_{1-}^{\#1} + \alpha$	0	0	$k^2 r_5 + \frac{2 t_3}{3}$	$-\frac{\sqrt{2} t_3}{3}$	0	$-\frac{2}{3} i k t_3$
$\omega_{1-}^{\#2} + \alpha$	0	0	$-\frac{\sqrt{2} t_3}{3}$	$\frac{t_3}{3}$	0	$\frac{1}{3} i \sqrt{2} k t_3$
$f_{1-}^{\#1} + \alpha$	0	0	0	0	0	0
$f_{1-}^{\#2} + \alpha$	0	0	$\frac{2 i k t_3}{3}$	$-\frac{1}{3} i \sqrt{2} k t_3$	0	$\frac{2 k^2 t_3}{3}$

Source constraints/gauge generators	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} - 2 i k \sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2 \alpha} + 2 i k \sigma_{1-}^{\#2 \alpha} == 0$	3
$\tau_{1-}^{\#1 \alpha} == 0$	3
$\tau_{1+}^{\#1 \alpha \beta} + i k \sigma_{1+}^{\#2 \alpha \beta} == 0$	3
$\sigma_{2-}^{\#1 \alpha \beta \chi} == 0$	5
$\tau_{2+}^{\#1 \alpha \beta} == 0$	5
$\sigma_{2+}^{\#1 \alpha \beta} == 0$	5
Total constraints:	26

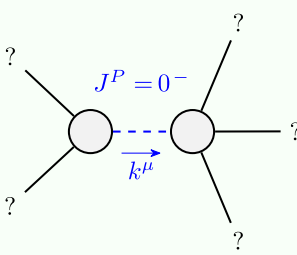
$\omega_{2+}^{\#1} + \alpha\beta\chi$	$f_{2+}^{\#1} + \alpha\beta$	$\omega_{2+}^{\#1} + \alpha\beta$
0	0	0
0	0	0
0	0	0

$\sigma_{2+}^{\#1} + \alpha\beta$	$\tau_{2+}^{\#1} + \alpha\beta$	$\sigma_{2-}^{\#1} + \alpha\beta$
0	0	0
0	0	0
0	0	0

$\sigma_{0+}^{\#1} +$	$\tau_{0+}^{\#1}$	$\tau_{0+}^{\#2}$	$\sigma_{0-}^{\#1}$
$\frac{1}{(1 + 2 k^2)^2 t_3}$	$-\frac{i \sqrt{2} k}{(1 + 2 k^2)^2 t_3}$	0	0
$\frac{i \sqrt{2} k}{(1 + 2 k^2)^2 t_3}$	$\frac{2 k^2}{(1 + 2 k^2)^2 t_3}$	0	0
0	0	0	0
0	0	0	$\frac{1}{k^2 r_2 + t_2}$

$\omega_{0+}^{\#1} +$	$f_{0+}^{\#1}$	$f_{0+}^{\#2}$	$\omega_{0-}^{\#1}$
t_3	$-i \sqrt{2} k t_3$	0	0
$i \sqrt{2} k t_3$	$2 k^2 t_3$	0	0
0	0	0	0
0	0	0	$k^2 r_2 + t_2$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(no massless particles)

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$