

# Particle spectrograph

## Wave operator and propagator

Source constraints/gauge generators	
SO(3) irreps	Multiplicities
$\sigma_0^{#1-} == 0$	1
$\tau_0^{#2+} == 0$	1
$\sigma_0^{#1+} == 0$	1
$\tau_1^{#2\alpha} == 0$	3
$\tau_1^{#1\alpha} == 0$	3
$\sigma_1^{#2\alpha} == 0$	3
$\sigma_1^{#1\alpha} == 0$	3
$\tau_1^{#1\alpha\beta} == 0$	3
$\sigma_1^{#2\alpha\beta} == 0$	3
$\sigma_1^{#1\alpha\beta} == 0$	3
$\sigma_2^{#1\alpha\beta\chi} == 0$	5
$\sigma_2^{#1\alpha\beta} == 0$	5
Total constraints:	34

Quadratic (free) Lagrangian density

$$\begin{aligned} & -\lambda \omega_{\kappa\theta} \omega'^{\theta\kappa} - \lambda \omega_{\kappa\theta} \omega'^{\theta\kappa} - \lambda \omega_{\kappa\alpha} \omega'^{\alpha\kappa} - \lambda \omega_{\kappa\zeta} \omega'^{\zeta\kappa} + f^{\alpha\beta} \tau_{\alpha\beta} + \\ & \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 2\lambda f'^{\theta} \partial_{\theta} \omega_{\kappa}^{\kappa} + 2\lambda \partial_{\theta} \omega_{\kappa}^{\kappa} + 2\lambda f'^{\theta} \partial_{\kappa} \omega_{\theta}^{\kappa} - 2\lambda f'_{\theta} \partial_{\kappa} \omega^{\theta\kappa} - \\ & \frac{1}{2} \lambda \partial^{\alpha} f_{\theta\kappa} \partial^{\kappa} f_{\alpha}^{\theta} - \frac{1}{2} \lambda \partial^{\alpha} f_{\kappa\theta} \partial^{\kappa} f_{\alpha}^{\theta} - \frac{1}{2} \lambda \partial^{\alpha} f_{\zeta}^{\zeta} \partial^{\kappa} f_{\alpha}^{\kappa} + \lambda \omega_{\kappa\alpha}^{\alpha} \partial^{\kappa} f'_{\alpha} + \\ & \lambda \omega_{\kappa\zeta}^{\zeta} \partial^{\kappa} f'_{\alpha} + 2\lambda \partial^{\alpha} f_{\kappa\alpha} \partial^{\kappa} f'_{\alpha} - \lambda \partial_{\kappa} f_{\zeta}^{\zeta} \partial^{\kappa} f'_{\alpha} + 2\lambda \omega_{\kappa\theta} \partial^{\kappa} f'_{\theta} - \lambda \omega_{\alpha}^{\alpha} \partial^{\kappa} f'_{\kappa} - \\ & \lambda \omega_{\zeta}^{\zeta} \partial^{\kappa} f'_{\kappa} + \frac{1}{2} \lambda \partial^{\alpha} f_{\zeta}^{\zeta} \partial^{\kappa} f_{\alpha}^{\kappa} + \frac{1}{2} \lambda \partial_{\kappa} f_{\theta}^{\theta} \partial^{\kappa} f_{\zeta}^{\zeta} + \frac{1}{2} \lambda \partial_{\kappa} f_{\theta}^{\theta} \partial^{\kappa} f_{\zeta}^{\zeta} - \lambda \partial^{\alpha} f_{\zeta}^{\zeta} \partial^{\kappa} f_{\alpha}^{\kappa} \end{aligned}$$

	$\omega_{2+}^{#1} \dagger^{\alpha\beta}$	$f_{2+}^{#1} \dagger^{\alpha\beta}$	$\omega_{2-}^{#1} \dagger^{\alpha\beta\chi}$
$\omega_{2+}^{#1} \dagger^{\alpha\beta}$	0	0	0
$f_{2+}^{#1} \dagger^{\alpha\beta}$	0	$k^2 \lambda$	0
$\omega_{2-}^{#1} \dagger^{\alpha\beta\chi}$	0	0	0

	$\sigma_{2+}^{#1} \dagger^{\alpha\beta}$	$\tau_{2+}^{#1} \dagger^{\alpha\beta}$	$\sigma_{2-}^{#1} \dagger^{\alpha\beta\chi}$
$\sigma_{2+}^{#1} \dagger^{\alpha\beta}$	0	0	0
$\tau_{2+}^{#1} \dagger^{\alpha\beta}$	0	$\frac{1}{k^2 \lambda}$	0
$\sigma_{2-}^{#1} \dagger^{\alpha\beta\chi}$	0	0	0

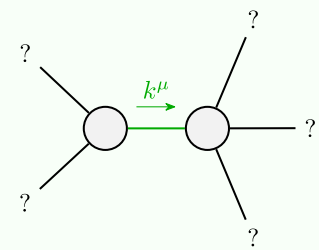
	$\omega_0^{#1} \dagger$	$f_0^{#1} \dagger$	$f_0^{#2} \dagger$	$\omega_0^{#1-} \dagger$
$\omega_0^{#1} \dagger$	0	0	0	0
$f_0^{#1} \dagger$	0	$-2 k^2 \lambda$	0	0
$f_0^{#2} \dagger$	0	0	0	0
$\omega_0^{#1-} \dagger$	0	0	0	0

	$\omega_{1+}^{#1} \dagger^{\alpha\beta}$	$\omega_{1+}^{#2} \dagger^{\alpha\beta}$	$f_{1+}^{#1} \dagger^{\alpha\beta}$	$\omega_{1-}^{#1} \dagger^{\alpha}$	$\omega_{1-}^{#2} \dagger^{\alpha}$	$f_{1-}^{#1} \dagger^{\alpha}$	$f_{1-}^{#2} \dagger^{\alpha}$
$\omega_{1+}^{#1} \dagger^{\alpha\beta}$	0	0	0	0	0	0	0
$\omega_{1+}^{#2} \dagger^{\alpha\beta}$	0	0	0	0	0	0	0
$f_{1+}^{#1} \dagger^{\alpha\beta}$	0	0	0	0	0	0	0
$\omega_{1-}^{#1} \dagger^{\alpha}$	0	0	0	0	0	0	0
$\omega_{1-}^{#2} \dagger^{\alpha}$	0	0	0	0	0	0	0
$f_{1-}^{#1} \dagger^{\alpha}$	0	0	0	0	0	0	0
$f_{1-}^{#2} \dagger^{\alpha}$	0	0	0	0	0	0	0

	$\sigma_{1+}^{#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{#2} \dagger^{\alpha\beta}$	$\tau_{1+}^{#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{#1} \dagger^{\alpha}$	$\sigma_{1-}^{#2} \dagger^{\alpha}$	$\tau_{1-}^{#1} \dagger^{\alpha}$	$\tau_{1-}^{#2} \dagger^{\alpha}$
$\sigma_{1+}^{#1} \dagger^{\alpha\beta}$	0	0	0	0	0	0	0
$\sigma_{1+}^{#2} \dagger^{\alpha\beta}$	0	0	0	0	0	0	0
$\tau_{1+}^{#1} \dagger^{\alpha\beta}$	0	0	0	0	0	0	0
$\sigma_{1-}^{#1} \dagger^{\alpha}$	0	0	0	0	0	0	0
$\sigma_{1-}^{#2} \dagger^{\alpha}$	0	0	0	0	0	0	0
$\tau_{1-}^{#1} \dagger^{\alpha}$	0	0	0	0	0	0	0
$\tau_{1-}^{#2} \dagger^{\alpha}$	0	0	0	0	0	0	0

	$\sigma_0^{#1} \dagger$	$\tau_0^{#1} \dagger$	$\tau_0^{#2} \dagger$	$\sigma_0^{#1-} \dagger$
$\sigma_0^{#1} \dagger$	0	0	0	0
$\tau_0^{#1} \dagger$	0	$-\frac{1}{2 k^2 \lambda}$	0	0
$\tau_0^{#2} \dagger$	0	0	0	0
$\sigma_0^{#1-} \dagger$	0	0	0	0

## Massive and massless spectra



Quadratic pole	
Pole residue:	$\frac{1}{\lambda} > 0$
Polarisations:	2

(No massive particles)

## Unitarity conditions

$\lambda > 0$