

Massive particle	
Pole residue:	$\frac{-3t_1t_2(t_1+t_2)+3r_5(t_1^2+2t_2^2)}{r_5(t_1+t_2)(-3t_1t_2+2r_5(t_1+t_2))} > 0$
Polarisations:	3
Square mass:	$-\frac{3t_1t_2}{2r_5t_1+2r_5t_2} > 0$
Spin:	1
Parity:	Even

Unitarity conditions

$r_2 < 0 \ \&\& \ r_5 > 0 \ \&\& \ t_1 < 0 \ \&\& \ t_2 > -t_1$

(No massless particles)

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

$\sigma_{1^+}^{\#1+\alpha\beta}$	$\sigma_{1^+}^{\#2}$	$\tau_{1^+}^{\#1+\alpha\beta}$	$\sigma_{1^+}^{\#2}$	$\tau_{1^+}^{\#1}$	$\tau_{1^+}^{\#2}$
$\frac{2(t_1+t_2)}{3t_1t_2+2k^2r_5(t_1+t_2)}$	$\frac{\sqrt{2}(t_1-2t_2)}{(1+k^2)(3t_1t_2+2k^2r_5(t_1+t_2))}$	$\frac{i\sqrt{2}k(t_1-2t_2)}{(1+k^2)(3t_1t_2+2k^2r_5(t_1+t_2))}$	0	0	0
$\frac{\sqrt{2}(t_1-2t_2)}{(1+k^2)(3t_1t_2+2k^2r_5(t_1+t_2))}$	$\frac{6k^2r_5+t_1+4t_2}{(1+k^2)^2(3t_1t_2+2k^2r_5(t_1+t_2))}$	$\frac{ik(6k^2r_5+t_1+4t_2)}{(1+k^2)^2(3t_1t_2+2k^2r_5(t_1+t_2))}$	0	0	0
$-\frac{i\sqrt{2}k(t_1-2t_2)}{(1+k^2)(3t_1t_2+2k^2r_5(t_1+t_2))}$	$-\frac{ik(6k^2r_5+t_1+4t_2)}{(1+k^2)^2(3t_1t_2+2k^2r_5(t_1+t_2))}$	$\frac{k^2(6k^2r_5+t_1+4t_2)}{(1+k^2)^2(3t_1t_2+2k^2r_5(t_1+t_2))}$	0	0	0
0	0	0	$\frac{\sqrt{2}}{t_1+2k^2t_1}$	0	$\frac{2ik}{t_1+2k^2t_1}$
0	0	0	$\frac{\sqrt{2}}{t_1+2k^2t_1}$	0	$-\frac{i\sqrt{2}k(2k^2r_5+t_1)}{(t_1+2k^2t_1)^2}$
0	0	0	0	0	0
0	0	0	$-\frac{2ik}{t_1+2k^2t_1}$	0	$\frac{-4k^4r_5+2k^2t_1}{(t_1+2k^2t_1)^2}$

Lagrangian density

$$\begin{aligned}
 &-t_1\omega_{\kappa\alpha}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-\frac{1}{3}t_1\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}+\frac{2}{3}t_2\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}+ \\
 &\frac{1}{3}t_2\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\kappa\lambda}+\frac{2}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega_{\alpha\beta}^{\kappa}+\frac{2}{3}r_5\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega_{\alpha\beta}^{\kappa}+ \\
 &r_5\partial_\theta\omega_{\lambda\alpha}^{\alpha}\partial_\kappa\omega_{\alpha\beta}^{\theta\kappa\lambda}-r_5\partial_\alpha\omega_{\lambda\theta}^{\alpha}\partial_\kappa\omega_{\alpha\beta}^{\kappa\lambda\theta}+2r_5\partial_\theta\omega_{\lambda\alpha}^{\alpha}\partial_\kappa\omega_{\alpha\beta}^{\kappa\lambda\theta}- \\
 &\frac{1}{3}t_1\partial^\alpha f_{\theta\kappa}\partial^\kappa f_\alpha^\theta+\frac{1}{6}t_2\partial^\alpha f_{\theta\kappa}\partial^\kappa f_\alpha^\theta-\frac{2}{3}t_1\partial^\alpha f_{\kappa\theta}\partial^\kappa f_\alpha^\theta- \\
 &\frac{1}{6}t_2\partial^\alpha f_{\kappa\theta}\partial^\kappa f_\alpha^\theta-\frac{1}{3}t_1\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{1}{6}t_2\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+t_1\omega_{\kappa\alpha}^\alpha\partial^\kappa f_{\alpha\lambda}^\lambda+ \\
 &t_1\omega_{\kappa\lambda}^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+2t_1\partial^\alpha f_{\kappa\alpha}\partial^\kappa f_{\alpha\lambda}^\lambda-t_1\partial_\kappa f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{1}{3}t_1\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda+ \\
 &\frac{1}{3}t_2\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{4}{3}t_1\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda-\frac{2}{3}t_2\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda-\frac{1}{3}t_1\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda- \\
 &\frac{1}{3}t_2\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{2}{3}t_1\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{2}{3}t_2\omega_{\theta\kappa}\partial^\kappa f_{\alpha\lambda}^\lambda-t_1\omega_{\alpha\lambda}^\alpha\partial^\kappa f_{\alpha\lambda}^\lambda- \\
 &t_1\omega_{\lambda\alpha}^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{1}{3}t_1\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda-\frac{1}{6}t_2\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{1}{3}t_1\partial_\kappa f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda- \\
 &\frac{1}{6}t_2\partial_\kappa f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{2}{3}t_1\partial_\kappa f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+\frac{1}{6}t_2\partial_\kappa f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda-t_1\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda+ \\
 &\frac{1}{3}r_2\partial_\kappa\omega_{\alpha\beta}^{\theta\theta}\partial^\kappa\omega_{\alpha\beta}^{\theta\theta}+\frac{2}{3}r_2\partial_\kappa\omega_{\alpha\beta}^{\theta\alpha\beta}\partial^\kappa\omega_{\alpha\beta}^{\theta\alpha\beta}-\frac{2}{3}r_2\partial_\theta\omega_{\lambda\alpha}^{\alpha\lambda}\partial_\lambda\omega_{\alpha\beta}^{\theta\kappa}+ \\
 &\frac{2}{3}r_2\partial^\theta\omega_{\lambda\alpha}^{\lambda\alpha}\partial_\lambda\omega_{\alpha\beta}^{\theta\kappa}+r_5\partial_\alpha\omega_{\lambda\theta}^{\alpha}\partial^\lambda\omega_{\kappa\alpha}^{\theta\kappa}-r_5\partial_\theta\omega_{\lambda\alpha}^{\alpha}\partial^\lambda\omega_{\kappa\alpha}^{\theta\kappa}
 \end{aligned}$$

Added source term:  $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

Source constraints

SO(3) irreps	#
$\tau_{0^+}^{\#2}==0$	1
$\tau_{0^+}^{\#1}-2ik\sigma_{0^+}^{\#1}==0$	1
$\tau_{1^+}^{\#2\alpha}+2ik\sigma_{1^+}^{\#2\alpha}==0$	3
$\tau_{1^+}^{\#1\alpha}==0$	3
$\tau_{1^+}^{\#1\alpha\beta}+ik\sigma_{1^+}^{\#2\alpha\beta}==0$	3
$\tau_{2^+}^{\#1\alpha\beta}-2ik\sigma_{2^+}^{\#1\alpha\beta}==0$	5
Total #:	16

	$\sigma_{0^+}^{\#1}$	$\tau_{0^+}^{\#1}$	$\tau_{0^+}^{\#2}$	$\sigma_{0^+}^{\#1}$
$\sigma_{0^+}^{\#1}+$	$-\frac{1}{(1+2k^2)^2t_1}$	$\frac{i\sqrt{2}k}{(1+2k^2)^2t_1}$	0	0
$\tau_{0^+}^{\#1}+$	$-\frac{i\sqrt{2}k}{(1+2k^2)^2t_1}$	$-\frac{2k^2}{(1+2k^2)^2t_1}$	0	0
$\tau_{0^+}^{\#2}+$	0	0	0	0
$\sigma_{0^+}^{\#1}+$	0	0	0	$\frac{1}{k^2r_2+t_2}$

	$\omega_{1^+}^{\#1\alpha\beta}$	$\omega_{1^+}^{\#2\alpha\beta}$	$f_{1^+}^{\#1\alpha\beta}$	$\omega_{1^+}^{\#1\alpha}$	$\omega_{1^+}^{\#2\alpha}$	$f_{1^+}^{\#1\alpha}$	$f_{1^+}^{\#2\alpha}$
$\omega_{1^+}^{\#1}+$	$\frac{1}{6}(6k^2r_5+t_1+4t_2)$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$-\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2}+$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$\frac{t_1+t_2}{3}$	$\frac{1}{3}ik(t_1+t_2)$	0	0	0	0
$f_{1^+}^{\#1}+$	$\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	$-\frac{1}{3}ik(t_1+t_2)$	$\frac{1}{3}k^2(t_1+t_2)$	0	0	0	0
$\omega_{1^+}^{\#1}+$	0	0	0	$k^2r_5-\frac{t_1}{2}$	$\frac{t_1}{\sqrt{2}}$	0	$ik t_1$
$\omega_{1^+}^{\#2}+$	0	0	0	$\frac{t_1}{\sqrt{2}}$	0	0	0
$f_{1^+}^{\#1}+$	0	0	0	0	0	0	0
$f_{1^+}^{\#2}+$	0	0	0	$-ik t_1$	0	0	0

	$\omega_{0^+}^{\#1}$	$f_{0^+}^{\#1}$	$f_{0^+}^{\#2}$	$\omega_{0^+}^{\#1}$
$\omega_{0^+}^{\#1}+$	$-t_1$	$i\sqrt{2}k t_1$	0	0
$f_{0^+}^{\#1}+$	$-i\sqrt{2}k t_1$	$-2k^2t_1$	0	0
$f_{0^+}^{\#2}+$	0	0	0	0
$\omega_{0^+}^{\#1}+$	0	0	0	$k^2r_2+t_2$

	$\sigma_{2^+}^{\#1\alpha\beta}$	$\tau_{2^+}^{\#1\alpha\beta}$	$\sigma_{2^+}^{\#1\alpha\beta\chi}$
$\sigma_{2^+}^{\#1}+$	$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\tau_{2^+}^{\#1}+$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\sigma_{2^+}^{\#1}+$	0	0	$\frac{2}{t_1}$

	$\omega_{2^+}^{\#1\alpha\beta}$	$f_{2^+}^{\#1\alpha\beta}$	$\omega_{2^+}^{\#1\alpha\beta\chi}$
$\omega_{2^+}^{\#1}+$	$\frac{t_1}{2}$	$-\frac{ik t_1}{\sqrt{2}}$	0
$f_{2^+}^{\#1}+$	$\frac{ik t_1}{\sqrt{2}}$	$k^2t_1$	0
$\omega_{2^+}^{\#1}+$	0	0	$\frac{t_1}{2}$