

Particle spectrograph

Wave operator and propagator

Source constraints		
SO(3) irreps	Fundamental fields	Multiplicities
$\tau_{0+}^{\#2} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == 0$	1
$\tau_{0+}^{\#1} - 2 \, i \, k \, \sigma_{0+}^{\#1} == 0$	$\partial_\beta \partial_\alpha \tau^{\alpha\beta} == \partial_\beta \partial^\beta \tau^\alpha_\alpha + 2 \, \partial_\chi \partial^\chi \partial_\beta \sigma^{\alpha\beta}_\alpha$	1
$\tau_{1-}^{\#2\alpha} + 2 \, i \, k \, \sigma_{1-}^{\#2\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\alpha\beta} + 2 \, \partial_\delta \partial^\delta \partial_\chi \partial_\beta \sigma^{\alpha\beta\chi}$	3
$\tau_{1-}^{\#1\alpha} == 0$	$\partial_\chi \partial_\beta \partial^\alpha \tau^{\beta\chi} == \partial_\chi \partial^\chi \partial_\beta \tau^{\beta\alpha}$	3
$\tau_{1+}^{\#1\alpha\beta} + i \, k \, \sigma_{1+}^{\#1\alpha\beta} == 0$	$\partial_\chi \partial^\alpha \tau^{\beta\chi} + \partial_\chi \partial^\beta \tau^{\alpha\chi} + \partial_\chi \partial^\chi \tau^{\alpha\beta} +$ $\partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\beta\chi\alpha} ==$ $\partial_\chi \partial^\alpha \tau^{\chi\beta} + \partial_\chi \partial^\beta \tau^{\alpha\chi} + \partial_\chi \partial^\chi \tau^{\beta\alpha} +$ $\partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta}$	3
$\sigma_{1+}^{\#1\alpha\beta} == \sigma_{1+}^{\#2\alpha\beta}$	$3 \, \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} +$ $2 \, \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\beta\chi} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta} ==$ $3 \, \partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\beta\chi\alpha}$	3
$\tau_{2+}^{\#1\alpha\beta} == 0$	$4 \, \partial_\delta \partial_\chi \partial^\beta \partial^\alpha \tau^{\chi\delta} + 2 \, \partial_\delta \partial^\delta \partial_\beta \partial^\alpha \tau^\chi_\chi +$ $3 \, \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\alpha\beta} + 3 \, \partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\beta\alpha} +$ $2 \, \eta^{\alpha\beta} \, \partial_\epsilon \partial^\epsilon \partial_\delta \partial_\chi \tau^{\chi\delta} ==$ $3 \, \partial_\delta \partial^\delta \partial_\chi \partial^\alpha \tau^{\beta\chi} + 3 \, \partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\alpha\chi} +$ $3 \, \partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\alpha\chi} + 3 \, \partial_\delta \partial^\delta \partial_\chi \partial^\beta \tau^{\chi\alpha} +$ $2 \, \eta^{\alpha\beta} \, \partial_\epsilon \partial^\epsilon \partial_\delta \partial^\delta \tau^\chi_\chi$	5
$\sigma_{2+}^{\#1\alpha\beta} == 0$	$3 \, \partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} + 3 \, \partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta} +$ $2 \, \eta^{\alpha\beta} \, \partial_\epsilon \partial^\epsilon \partial_\delta \sigma^{\alpha\chi\delta}_\chi == 2 \, \partial_\delta \partial^\delta \partial_\epsilon \sigma^{\alpha\chi\delta}_\chi +$ $3 \, (\partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\chi\beta} + \partial_\delta \partial^\delta \partial_\chi \sigma^{\beta\chi\alpha})$	5
Total constraints/gauge generators:		24

Quadratic (free) action

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$$\begin{aligned} & \iiint \iiint (\frac{1}{6} (-4 t_3 \mathcal{A}^{\alpha\iota}_{\iota} \mathcal{A}^{\iota\theta}_{\theta} + 6 f^{\alpha\beta} \tau_{\alpha\beta} + 6 \mathcal{A}^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} \sigma_{\alpha\beta\chi} + 8 t_3 \mathcal{A}^{\theta}_{\alpha} \partial_{\theta} \partial_{\iota} f^{\alpha\iota} - 8 t_3 \mathcal{A}^{\theta}_{\theta} \partial' f^{\alpha}_{\alpha} + 4 t_3 \partial_{\iota} f^{\theta}_{\alpha} \partial' f^{\alpha}_{\theta} - 12 r_1 \partial_{\beta} \mathcal{A}^{\theta}_{\iota} \partial_{\theta} \partial' \mathcal{A}^{\alpha\beta}_{\alpha} + 12 r_1 \partial_{\iota} \partial_{\beta} \mathcal{A}^{\theta}_{\theta} \partial' \mathcal{A}^{\alpha\beta}_{\beta} + 4 t_3 \partial_{\iota} \partial_{\beta} f^{\alpha\iota} \partial_{\theta} f^{\theta}_{\alpha} - 8 t_3 \partial_{\iota} \partial' f^{\alpha}_{\alpha} \partial_{\theta} f^{\theta}_{\theta} + 12 r_1 \partial_{\alpha} \mathcal{A}^{\alpha\beta\iota} \partial_{\theta} \mathcal{A}^{\theta}_{\beta} - 24 r_1 \partial' \mathcal{A}^{\alpha\beta}_{\alpha} \partial_{\theta} \mathcal{A}^{\theta}_{\iota} - 12 r_1 \partial_{\alpha} \mathcal{A}^{\alpha\beta\iota} \partial_{\theta} \mathcal{A}^{\theta}_{\beta} + 24 r_1 \partial_{\iota} \mathcal{A}^{\alpha\beta}_{\alpha} \partial_{\theta} \mathcal{A}^{\theta}_{\beta} + 4 t_2 \mathcal{A}_{\iota\theta\alpha} \partial^{\theta} f^{\alpha\iota} + 2 t_2 \partial_{\iota} \partial_{\theta} f^{\alpha\iota} \partial^{\theta} f^{\alpha\iota} - t_2 \partial_{\alpha} f^{\theta}_{\theta} \partial^{\theta} f^{\alpha\iota} - t_2 \partial_{\iota} f^{\alpha\iota} \partial_{\alpha\theta} \partial^{\theta} f^{\alpha\iota} + t_2 \partial_{\theta} f^{\alpha\iota} \partial_{\alpha\iota} \partial^{\theta} f^{\alpha\iota} - t_2 \partial_{\theta} f^{\alpha\iota}_{\iota} \partial^{\theta} f^{\alpha\iota} - 4 t_2 \mathcal{A}_{\alpha\theta\iota} (\mathcal{A}^{\alpha\iota\theta} + \partial^{\theta} f^{\alpha\iota}) + 2 t_2 \mathcal{A}_{\alpha\iota\theta} (\mathcal{A}^{\alpha\iota\theta} + 2 \partial^{\theta} f^{\alpha\iota}) - 8 r_1 \partial_{\beta} \mathcal{A}_{\alpha\iota\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} + 8 r_2 \partial_{\beta} \mathcal{A}_{\alpha\iota\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} + 4 r_1 \partial_{\beta} \mathcal{A}_{\alpha\theta\iota} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} - 4 r_2 \partial_{\beta} \mathcal{A}_{\alpha\theta\iota} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} - 16 r_1 \partial_{\beta} \mathcal{A}_{\iota\theta\alpha} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} + 4 r_2 \partial_{\beta} \mathcal{A}_{\iota\theta\alpha} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} - 4 r_1 \partial_{\iota} \mathcal{A}_{\alpha\beta\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} - 2 r_2 \partial_{\iota} \mathcal{A}_{\alpha\beta\theta} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} + 4 r_1 \partial_{\theta} \mathcal{A}_{\alpha\beta\iota} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} + 4 r_1 \partial_{\theta} \mathcal{A}_{\alpha\iota\beta} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota} - 4 r_2 \partial_{\theta} \mathcal{A}_{\alpha\iota\beta} \partial^{\theta} \mathcal{A}^{\alpha\beta\iota})) [t, x, y, z] d\iota dz dy dx dt \end{aligned}$$

$\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1+}^{\#2}$	$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$\sigma_{1-}^{\#1}$	$\sigma_{1-}^{\#2}$	$\tau_{1-}^{\#1}$	$\tau_{1-}^{\#2}$
$\frac{6}{(3+k^2)^2} t_2$	$\frac{3 \sqrt{2}}{(3+k^2)^2} t_2$	$\frac{3 i \sqrt{2} k}{(3+k^2)^2} t_2$	0	0	0	0
$\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{3 \sqrt{2}}{(3+k^2)^2} t_2$	$\frac{3 i k}{(3+k^2)^2} t_2$	0	0	0	0
$\tau_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{3 i \sqrt{2} k}{(3+k^2)^2} t_2$	$\frac{3 k^2}{(3+k^2)^2} t_2$	0	0	0	0
$\sigma_{1-}^{\#1} \dagger^{\alpha}$	0	0	$-\frac{1}{k^2} r_1$	$-\frac{\sqrt{2}}{k^2 r_1 + 2 k^4 r_1}$	0	$-\frac{2 i}{k r_1 + 2 k^3 r_1}$
$\sigma_{1-}^{\#2} \dagger^{\alpha}$	0	0	$-\frac{\sqrt{2}}{k^2 r_1 + 2 k^4 r_1}$	$\frac{3 k^2 r_1 - 2 t_3}{(k + 2 k^3)^2 r_1 t_3}$	0	$\frac{i \sqrt{2} (3 k^2 r_1 - 2 t_3)}{k (1 + 2 k^2)^2 r_1 t_3}$
$\tau_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$\tau_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	0	0	0

$\mathcal{A}_{1+}^{\#1} \dagger^{\alpha\beta}$	$\mathcal{A}_{1+}^{\#2}$	$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$\mathcal{A}_{1-}^{\#1}$	$\mathcal{A}_{1-}^{\#2}$	$f_{1-}^{\#1}$	$f_{1-}^{\#2}$
$\frac{2 t_2}{3}$	$\frac{\sqrt{2} t_2}{3}$	$\frac{1}{3} i \sqrt{2} k t_2$	0	0	0	0
$\mathcal{A}_{1+}^{\#2} \dagger^{\alpha\beta}$	$\frac{t_2}{3}$	$\frac{i k t_2}{3}$	0	0	0	0
$f_{1+}^{\#1} \dagger^{\alpha\beta}$	$-\frac{1}{3} i \sqrt{2} k t_2$	$\frac{k^2 t_2}{3}$	0	0	0	0
$\mathcal{A}_{1-}^{\#1} \dagger^{\alpha}$	0	0	$-k^2 r_1 + \frac{2 t_3}{3}$	$-\frac{\sqrt{2} t_3}{3}$	0	$-\frac{2}{3} i k t_3$
$\mathcal{A}_{1-}^{\#2} \dagger^{\alpha}$	0	0	0	$\frac{t_3}{3}$	0	$\frac{1}{3} i \sqrt{2} k t_3$
$f_{1-}^{\#1} \dagger^{\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#2} \dagger^{\alpha}$	0	0	$\frac{2 i k t_3}{3}$	$-\frac{1}{3} i \sqrt{2} k t_3$	0	$\frac{2 k^2 t_3}{3}$

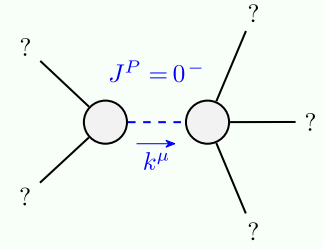
$\sigma_{0+}^{\#1} \dagger$	$\frac{1}{(1+2 k^2)^2 t_3}$	$-\frac{i \sqrt{2} k}{(1+2 k^2)^2 t_3}$	0	0
$\tau_{0+}^{\#1} \dagger$	$\frac{i \sqrt{2} k}{(1+2 k^2)^2 t_3}$	$\frac{2 k^2}{(1+2 k^2)^2 t_3}$	0	0
$\tau_{0+}^{\#2} \dagger$	0	0	0	0
$\sigma_{0-}^{\#1} \dagger$	0	0	0	$\frac{1}{k^2 r_2 + t_2}$

$\mathcal{A}_{0+}^{\#1} \dagger$	$t_3$	$-i \sqrt{2} k t_3$	0	0
$f_{0+}^{\#1} \dagger$	$i \sqrt{2} k t_3$	$2 k^2 t_3$	0	0
$f_{0+}^{\#2} \dagger$	0	0	0	0
$\mathcal{A}_{0-}^{\#1} \dagger$	0	0	$k^2 r_2 + t_2$	

$\mathcal{A}_{2+}^{\#1} \dagger^{\alpha\beta}$	0	0	0	0
$f_{2+}^{\#1} \dagger^{\alpha\beta}$	0	0	0	0
$\mathcal{A}_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	$k^2 r_1$	

$\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$	0	0	$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	0
$\tau_{2+}^{\#1} \dagger^{\alpha\beta}$	0	0	0	0
$\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$	0	0	0	$\frac{1}{k^2 r_1}$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

Unitarity conditions

$r_2 < 0 \ \&\& \ t_2 > 0$