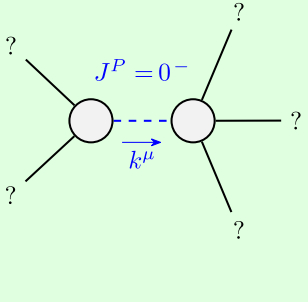


Lagrangian density

$$\begin{aligned} &-\frac{1}{3}t_1\omega_{\kappa\alpha}'\omega_{\kappa\lambda}-\frac{1}{3}t_1\omega_{\kappa\lambda}'\omega_{\kappa\lambda}'+\frac{2}{3}t_2\omega_{\kappa\lambda}'\omega_{\kappa\lambda}'+\frac{1}{3}t_1\omega_{\kappa\lambda}'\omega^{\kappa\lambda}{}_'+ \\ &\frac{1}{3}t_2\omega_{\kappa\lambda}'\omega^{\kappa\lambda}{}_'+f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}+\frac{2}{3}r_2\partial^\beta\omega^{\theta\alpha}{}_\kappa\partial_\theta\omega_{\alpha\beta}{}^\kappa- \\ &\frac{1}{3}r_2\partial_\theta\omega_{\alpha\beta}{}^\kappa\partial_\kappa\omega^{\alpha\beta\theta}-\frac{2}{3}r_2\partial_\theta\omega_{\alpha\beta}{}^\kappa\partial_\kappa\omega^{\theta\alpha\beta}+4r_3\partial_\alpha\omega_{\lambda}{}^\alpha\partial_\kappa\omega^{\theta\kappa\lambda}- \\ &4r_3\partial_\theta\omega_{\lambda}{}^\alpha\partial_\kappa\omega^{\theta\kappa\lambda}-\frac{1}{3}t_1\partial^\alpha f_{\theta\kappa}{}^\kappa\partial^\kappa f_{\alpha}{}^\theta+\frac{1}{6}t_2\partial^\alpha f_{\theta\kappa}{}^\kappa\partial^\kappa f_{\alpha}{}^\theta-\frac{2}{3}t_1\partial^\alpha f_{\kappa\theta}{}^\theta\partial^\kappa f_{\alpha}{}^\theta- \\ &\frac{1}{6}t_2\partial^\alpha f_{\kappa\theta}{}^\theta\partial^\kappa f_{\alpha}{}^\theta-\frac{1}{3}t_1\partial^\alpha f_{\kappa}{}^\alpha\partial^\kappa f_{\alpha\lambda}{}^\kappa+\frac{1}{6}t_2\partial^\alpha f_{\kappa}{}^\alpha\partial^\kappa f_{\alpha\lambda}{}^\kappa+\frac{1}{3}t_1\omega_{\kappa\alpha}{}^\alpha\partial^\kappa f_{\lambda}{}'+ \\ &\frac{1}{3}t_1\omega_{\kappa\lambda}{}^\lambda\partial^\kappa f_{\lambda}{}'+\frac{2}{3}t_1\partial^\alpha f_{\kappa\alpha}{}^\alpha\partial^\kappa f_{\lambda}{}'-\frac{1}{3}t_1\partial_\kappa f_{\lambda}{}^\lambda\partial^\kappa f_{\lambda}{}'+\frac{1}{3}t_1\omega_{\iota\theta\kappa}{}^\kappa\partial^\kappa f_{\iota}{}^\theta+ \\ &\frac{1}{3}t_2\omega_{\iota\theta\kappa}{}^\kappa\partial^\kappa f_{\iota}{}^\theta+\frac{4}{3}t_1\omega_{\iota\kappa\theta}{}^\kappa\partial^\kappa f_{\iota}{}^\theta-\frac{2}{3}t_2\omega_{\iota\kappa\theta}{}^\kappa\partial^\kappa f_{\iota}{}^\theta-\frac{1}{3}t_1\omega_{\theta\iota\kappa}{}^\kappa\partial^\kappa f_{\iota}{}^\theta- \\ &\frac{1}{3}t_2\omega_{\theta\iota\kappa}{}^\kappa\partial^\kappa f_{\iota}{}^\theta+\frac{2}{3}t_1\omega_{\theta\kappa\iota}{}^\kappa\partial^\kappa f_{\iota}{}^\theta+\frac{2}{3}t_2\omega_{\theta\kappa\iota}{}^\kappa\partial^\kappa f_{\iota}{}^\theta-\frac{1}{3}t_1\omega_{\iota\alpha}{}^\alpha\partial^\kappa f_{\kappa}{}'- \\ &\frac{1}{3}t_1\omega_{\iota\lambda}{}^\lambda\partial^\kappa f_{\kappa}{}'+\frac{1}{3}t_1\partial^\alpha f_{\kappa}{}^\alpha\partial^\kappa f_{\lambda\alpha}{}^\kappa-\frac{1}{6}t_2\partial^\alpha f_{\kappa}{}^\alpha\partial^\kappa f_{\lambda\alpha}{}^\kappa+\frac{1}{3}t_1\partial_\kappa f_{\theta}{}^\lambda\partial^\kappa f_{\lambda}{}^\theta- \\ &\frac{1}{6}t_2\partial_\kappa f_{\theta}{}^\lambda\partial^\kappa f_{\lambda}{}^\theta+\frac{2}{3}t_1\partial_\kappa f_{\theta}{}^\lambda\partial^\kappa f_{\lambda}{}^\theta+\frac{1}{6}t_2\partial_\kappa f_{\theta}{}^\lambda\partial^\kappa f_{\lambda}{}^\theta-\frac{1}{3}t_1\partial^\alpha f_{\lambda}{}^\alpha\partial^\kappa f_{\lambda\kappa}{}'+ \\ &\frac{1}{3}r_2\partial_\kappa\omega_{\alpha\beta\theta}{}^\kappa\omega_{\alpha\beta\theta}{}^\kappa+\frac{2}{3}r_2\partial_\kappa\omega^{\theta\alpha\beta}{}^\kappa\omega_{\alpha\beta\theta}{}^\kappa-\frac{2}{3}r_2\partial^\beta\omega_{\lambda}{}'\partial_\lambda\omega_{\alpha\beta}{}^\lambda\omega_{\alpha}{}^\kappa\partial^\lambda\omega_{\lambda}{}^\theta\omega_{\kappa}{}^\kappa \\ &\frac{2}{3}r_2\partial^\beta\omega_{\lambda}{}'\partial_\lambda\omega_{\alpha\beta}{}^\lambda\omega_{\alpha}{}'\partial_\lambda\omega_{\alpha\beta}{}^\lambda\omega_{\alpha}{}'\partial^\lambda\omega_{\lambda}{}^\theta\omega_{\kappa}{}^\kappa+4r_3\partial_\theta\omega_{\lambda}{}^\alpha\partial^\lambda\omega_{\alpha}{}^\theta\omega_{\kappa}{}^\kappa \end{aligned}$$



Massive particle	
Pole residue:	$-\frac{1}{\gamma_2} \succ 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{\gamma_2} \succ 0$
Spin:	0
Parity:	Odd

$r_2 < 0 \ \&\& \ t_2 > 0$

Unitarity conditions

(No massless particles)

$\sigma_{1^+}^{\#1} \dagger \alpha\beta$	$\sigma_{1^+}^{\#2} \dagger \alpha\beta$	$\tau_{1^+}^{\#1} \dagger \alpha\beta$	$\sigma_{1^+}^{\#1} \alpha$	$\sigma_{1^+}^{\#2} \alpha$	$\tau_{1^+}^{\#1} \alpha$	$\tau_{1^+}^{\#2} \alpha$
$\sigma_{1^+}^{\#1} \dagger \alpha\beta$	$\frac{2(t_1+t_2)}{3t_1t_2}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	0	0	0
$\sigma_{1^+}^{\#2} \dagger \alpha\beta$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{t_1+4t_2}{3(1+k^2)^2t_1t_2}$	$\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0
$\tau_{1^+}^{\#1} \dagger \alpha\beta$	$-\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$-\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	$\frac{k^2(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0
$\sigma_{1^-}^{\#1} \dagger \alpha$	0	0	$\frac{6}{(3+4k^2)^2t_1}$	$\frac{6\sqrt{2}}{(3+4k^2)^2t_1}$	0	$\frac{12ik}{(3+4k^2)^2t_1}$
$\sigma_{1^-}^{\#2} \dagger \alpha$	0	0	0	$\frac{6\sqrt{2}}{(3+4k^2)^2t_1}$	0	$\frac{12i\sqrt{2}k}{(3+4k^2)^2t_1}$
$\tau_{1^-}^{\#1} \dagger \alpha$	0	0	0	0	0	0
$\tau_{1^-}^{\#2} \dagger \alpha$	0	0	$-\frac{12ik}{(3+4k^2)^2t_1}$	$-\frac{12i\sqrt{2}k}{(3+4k^2)^2t_1}$	0	$\frac{24k^2}{(3+4k^2)^2t_1}$

$\omega_{1^+}^{\#1} \dagger \alpha\beta$	$\omega_{1^+}^{\#2} \dagger \alpha\beta$	$f_{1^+}^{\#1} \dagger \alpha\beta$	$\omega_{1^-}^{\#1} \alpha$	$\omega_{1^-}^{\#2} \alpha$	$f_{1^-}^{\#1} \alpha$	$f_{1^-}^{\#2} \alpha$
$\omega_{1^+}^{\#1} \dagger \alpha\beta$	$\frac{1}{6}(t_1+4t_2)$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$-\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	0	0	0
$\omega_{1^+}^{\#2} \dagger \alpha\beta$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$\frac{t_1+t_2}{3}$	$\frac{1}{3}\bar{ik}(t_1+t_2)$	0	0	0
$f_{1^+}^{\#1} \dagger \alpha\beta$	$\frac{\bar{ik}(t_1-2t_2)}{3\sqrt{2}}$	$-\frac{1}{3}\bar{ik}(t_1+t_2)$	$\frac{1}{3}k^2(t_1+t_2)$	0	0	0
$\omega_{1^-}^{\#1} \dagger \alpha$	0	0	0	$\frac{t_1}{3\sqrt{2}}$	0	$\frac{ikt_1}{3}$
$\omega_{1^-}^{\#2} \dagger \alpha$	0	0	0	$\frac{t_1}{3\sqrt{2}}$	0	$\frac{1}{3}\bar{i}\sqrt{2}kt_1$
$f_{1^-}^{\#1} \dagger \alpha$	0	0	0	0	0	0
$f_{1^-}^{\#2} \dagger \alpha$	0	0	$-\frac{1}{3}\bar{ik}kt_1$	$-\frac{1}{3}\bar{i}\sqrt{2}kt_1$	0	$\frac{2k^2t_1}{3}$

Source constraints

SO(3) irreps	#
$\tau_{0^+}^{\#2} == 0$	1
$\tau_{0^+}^{\#1} == 0$	1
$\tau_{1^-}^{\#2\alpha} + 2\bar{ik}\sigma_{1^-}^{\#1\alpha} == 0$	3
$\tau_{1^-}^{\#1\alpha} == 0$	3
$\sigma_{1^-}^{\#1\alpha} == \sigma_{1^-}^{\#2\alpha}$	3
$\tau_{1^+}^{\#1\alpha\beta} + \bar{ik}\sigma_{1^+}^{\#2\alpha\beta} == 0$	3
$\tau_{2^+}^{\#1\alpha\beta} - 2\bar{ik}\sigma_{2^+}^{\#1\alpha\beta} == 0$	5
Total #:	19

$\sigma_{0^+}^{\#1} \dagger$	$\tau_{0^+}^{\#2} \dagger$	$\tau_{0^+}^{\#1} \dagger$	$\sigma_{0^+}^{\#1} \dagger$
0	0	0	$\frac{1}{6\sqrt{2}r_3}$
0	0	0	0
0	0	0	0
$\frac{1}{k^2r_2+t_2}$	0	0	0

$\omega_{2^+}^{\#1} \dagger \alpha\beta$	$f_{2^+}^{\#1} \alpha\beta$	$\omega_{2^-}^{\#1} \alpha\beta\chi$
$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	0
$\omega_{2^-}^{\#1} \dagger \alpha\beta\chi$	0	$\frac{t_1}{2}$

$\omega_{0^+}^{\#1}$	$f_{0^+}^{\#1}$	$f_{0^+}^{\#2}$	$\omega_{0^-}^{\#1}$
$\omega_{0^+}^{\#1} \dagger$	$6k^2r_3$	0	0
$f_{0^+}^{\#1} \dagger$	0	0	0
$f_{0^+}^{\#2} \dagger$	0	0	0
$\omega_{0^-}^{\#1} \dagger$	0	0	$k^2r_2+t_2$

$\sigma_{2^+}^{\#1} \dagger \alpha\beta$	$\tau_{2^+}^{\#1} \dagger \alpha\beta$	$\sigma_{2^-}^{\#1} \alpha\beta\chi$	
$\sigma_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{2}{(1+2k^2)^2 t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	0
$\tau_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2 t_1}$	$\frac{4k^2}{(1+2k^2)^2 t_1}$	0
$\sigma_{2^-}^{\#1} \dagger \alpha\beta\chi$	0	0	$\frac{2}{t_1}$