

Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$\frac{t_1}{r_2} > 0$
Spin:	0
Parity:	Odd

Quadratic pole	
Pole residue:	$-\frac{1}{(2r_3+r_5)t_1^2} > 0$
Polarisations:	2

Unitarity conditions

$r_2 < 0$ 
&&
 $r_5 < -2r_3$ 
&&
 $t_1 < 0$

Lagrangian density

$$\begin{aligned}
&-\frac{1}{3}t_1\omega_{\lambda'}^{\alpha'}\omega_{\kappa\alpha}^{\kappa}-t_1\omega_{\lambda'}^{\kappa\lambda}\omega_{\kappa\lambda}^{'\kappa}+f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}{}^{-2}r_3\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial^{\lambda}\omega_{\lambda}^{\alpha}- \\
&r_5\partial_{\lambda}\omega_{\kappa}^{\kappa\lambda}\partial^{\lambda}\omega_{\lambda}^{\alpha}+\frac{2}{3}r_2\partial^{\beta}\omega_{\alpha}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-\frac{1}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}- \\
&\frac{2}{3}r_2\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}+2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega_{\lambda}^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\theta\kappa\lambda}- \\
&2r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\omega_{\lambda}^{\theta\kappa\lambda}+r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\omega_{\lambda}^{\theta\kappa\lambda}-2r_3\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}- \\
&r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\theta}\omega^{\kappa\lambda\theta}+4r_3\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\omega^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\alpha}\omega^{\kappa\lambda\theta}- \\
&\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}{}^{\kappa}\partial^{\kappa}f_{\alpha}{}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}{}^{\theta}\partial^{\theta}f_{\alpha}{}^{\kappa}-\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}{}^{\lambda}\partial^{\lambda}f_{\alpha}{}^{\kappa}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{'\alpha}+ \\
&\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{'\alpha}+\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}{}^{\theta}\partial^{\theta}f_{\lambda}^{'\alpha}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{'\alpha}+2t_1\omega_{\lambda\kappa\theta}^{\theta}\partial^{\kappa}f^{'\theta}- \\
&\frac{1}{3}t_1\omega_{\lambda\alpha}^{\alpha}\partial^{\kappa}f_{\kappa}^{'\alpha}-\frac{1}{3}t_1\omega_{\lambda\lambda}^{\lambda}\partial^{\kappa}f_{\kappa}^{'\alpha}+\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}^{\lambda}\partial^{\kappa}f_{\lambda\alpha}{}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}^{\theta}+ \\
&\frac{1}{2}t_1\partial_{\kappa}f_{\theta}^{\lambda}\partial^{\kappa}f_{\lambda}{}^{\theta}-\frac{1}{3}t_1\partial^{\alpha}f_{\lambda}{}^{\alpha}\partial^{\alpha}f_{\lambda\kappa}{}^{\kappa}+\frac{1}{3}r_2\partial_{\kappa}\omega^{\alpha\beta\theta}\partial^{\kappa}\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}- \\
&\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{'\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{'\theta}+\frac{2}{3}r_2\partial^{\beta}\omega_{\lambda}^{'\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{'\theta}-4r_3\partial^{\beta}\omega_{\lambda}^{'\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{'\theta}- \\
&2r_3\partial_{\alpha}\omega_{\lambda}^{'\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}{}_{\kappa}+r_5\partial_{\alpha}\omega_{\lambda}^{'\alpha}\partial_{\theta}\omega_{\lambda}^{\theta\kappa}{}_{\kappa}+2r_3\partial_{\theta}\omega_{\lambda}^{'\alpha}\partial^{\lambda}\omega_{\lambda}^{\theta\kappa}{}_{\kappa}-r_5\partial_{\theta}\omega_{\lambda}^{'\alpha}\partial^{\lambda}\omega_{\lambda}^{\theta\kappa}{}_{\kappa}
\end{aligned}$$

Source constraints

SO(3) irreps	#
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} + 2\,i\,k\,\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i\,k\,\sigma_{1+}^{\#2\alpha\beta} == 0$	3
$\tau_{2+}^{\#1\alpha\beta} - 2\,i\,k\,\sigma_{2+}^{\#1\alpha\beta} == 0$	5
Total #:	16

$\sigma_{2+}^{\#1} + ^{\alpha\beta}$	$\tau_{2+}^{\#1} + ^{\alpha\beta}$	$\sigma_{2-}^{\#1} + ^{\alpha\beta\chi}$
$\frac{2}{(1+2\,k^2)^2}t_1$	$-\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2}t_1$	0
$\frac{2\,i\,\sqrt{2}\,k}{(1+2\,k^2)^2}t_1$	$\frac{4k^2}{(1+2\,k^2)^2}t_1$	0
0	0	$\frac{2}{t_1}$

$\sigma_{0+}^{\#1} +$	$\tau_{0+}^{\#1} +$	$\sigma_{0+}^{\#2} +$
$\frac{1}{6\,k^2}r_3$	0	0
0	0	0
0	0	0
0	0	$\frac{1}{k^2}r_2-t_1$

$\omega_{2+}^{\#1} + ^{\alpha\beta}$	$f_{2+}^{\#1} + ^{\alpha\beta}$	$\omega_{2-}^{\#1} + ^{\alpha\beta\chi}$
$\frac{t_1}{2}$	$-\frac{i\,k\,t_1}{\sqrt{2}}$	0
$\frac{i\,k\,t_1}{\sqrt{2}}$	$k^2\,t_1$	0
0	0	$\frac{t_1}{2}$

$\omega_{0+}^{\#1} +$	$f_{0+}^{\#1} +$	$\omega_0^{\#1} +$
$6\,k^2\,r_3$	0	0
0	0	0
0	0	0
0	0	$k^2\,r_2-t_1$

$\omega_{1+}^{\#1} + ^{\alpha\beta}$	$\omega_{1+}^{\#2} + ^{\alpha\beta}$	$f_{1+}^{\#1} + ^{\alpha\beta}$	$\omega_{1-}^{\#1} +$	$\omega_{1-}^{\#2} +$	$f_{1-}^{\#1} + ^{\alpha}$
$k^2\,(2\,r_3+r_5)-\frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{i\,k\,t_1}{\sqrt{2}}$	0	0	0
$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$\frac{i\,k\,t_1}{\sqrt{2}}$	0	0	0	0	0
0	0	$k^2\,(2\,r_3+r_5)+\frac{t_1}{6}$	$\frac{t_1}{3\,\sqrt{2}}$	$\frac{t_1}{3\,\sqrt{2}}$	$\frac{i\,k\,t_1}{3}$
0	0	0	$\frac{t_1}{3\,\sqrt{2}}$	$\frac{t_1}{3}$	$\frac{1}{3}\,i\,\sqrt{2}\,k\,t_1$
0	0	0	0	0	0
0	0	0	$-\frac{1}{3}\,i\,k\,t_1$	$-\frac{1}{3}\,i\,\sqrt{2}\,k\,t_1$	$\frac{2\,k^2\,t_1}{3}$