

# Particle spectrograph

## Wave operator and propagator

Quadratic (free) action

$S_F ==$

$$\iiint (\phi \rho + h^{\alpha\beta} \mathcal{T}_{\alpha\beta} + \beta \partial_\alpha \phi \partial^\alpha \phi + \frac{1}{2} \alpha \partial_\beta h^\chi{}_\chi \partial^\beta h^\alpha{}_\alpha + \alpha \partial_\alpha h^{\alpha\beta} \partial_\chi h^\chi{}_\beta - \alpha \partial^\beta h^\alpha{}_\alpha \partial_\chi h^\chi{}_\beta - \frac{1}{2} \alpha \partial_\chi h^\chi{}_\beta \partial^\chi h^{\alpha\beta}) [t, x, y, z] dz dy dx dt$$

Source constraints/gauge generators	SO(3) irreps	Multiplicities
$\mathcal{T}^{\#2}_{0+} == 0$		1
$\mathcal{T}^{\#1\alpha}_{1-} == 0$		3
Total constraints:	4	

$\mathcal{T}^{\#1}_{0+}$	$\mathcal{T}^{\#2}_{0+}$	$\rho^{\#1}_{0+}$
$\frac{1}{\alpha k^2}$	0	0
0	0	0
0	0	$\frac{1}{\beta k^2}$

$h^{\#1}_{0+}$	$h^{\#2}_{0+}$	$\phi^{\#1}_{0+}$
$\alpha k^2$	0	0
0	0	0
0	0	$\beta k^2$

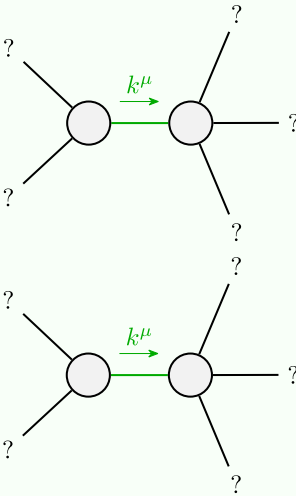
$$h^{\#1}_{1-}{}^\alpha \boxed{0}$$

$$\mathcal{T}^{\#1}_{2+}{}^{\alpha\beta} \boxed{-\frac{2}{\alpha k^2}}$$

$$h^{\#1}_{2+}{}^{\alpha\beta} \boxed{-\frac{\alpha k^2}{2}}$$

$$\mathcal{T}^{\#1}_{1-}{}^\alpha \boxed{0}$$

## Massive and massless spectra



Quadratic pole

Pole residue:  $-\frac{1}{\alpha} > 0$

Polarisations: 2

Quadratic pole

Pole residue:  $\frac{1}{\beta} > 0$

Polarisations: 1

(No massive particles)

## Unitarity conditions

$$\alpha < 0 \ \&\& \ \beta > 0$$