## $S = \iiint \left(\frac{1}{4}\left(2\,a_{0}\,\mathcal{R}^{\alpha\beta}_{\alpha}\,\mathcal{R}^{\chi}_{\beta\chi} + \mathcal{R}^{\alpha\beta\chi}\right) + \mathcal{R}^{\alpha\beta\chi}_{\beta\chi\alpha} + 4\,\mathcal{W}_{\alpha\beta\chi}\right) + 4\,\mathcal{T}^{\alpha\beta}_{\alpha\beta}\,h_{\alpha\beta} - a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} - 2\,a_{0}\,h_{\alpha\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta\chi} + 2\,a_{0}\,h_{\beta\chi}\,\partial^{\chi}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} - 2\,a_{0}\,h_{\alpha\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta\chi} + 2\,a_{0}\,h_{\beta\chi}\,\partial^{\chi}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} - 2\,a_{0}\,h_{\alpha\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta\chi} + 2\,a_{0}\,h_{\beta\chi}\,\partial^{\chi}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{0}\,h_{\chi}^{\chi}\,\partial_{\beta}\mathcal{R}^{\alpha\beta}_{\alpha} + a_{$ $4c_{1}\partial_{\alpha}\mathcal{A}_{\mu\beta\chi}\partial^{\mu}\mathcal{A}^{\alpha\beta\chi} + 4c_{2}\partial_{\alpha}\mathcal{A}_{\mu\chi\beta}\partial^{\mu}\mathcal{A}^{\alpha\beta\chi} - 4c_{1}\partial_{\mu}\mathcal{A}_{\alpha\beta\chi}\partial^{\mu}\mathcal{A}^{\alpha\beta\chi} - 4c_{2}\partial_{\mu}\mathcal{A}_{\alpha\chi\beta}\partial^{\mu}\mathcal{A}^{\alpha\beta\chi}))[t, x, y, z]dzdydxdt$ ${}^{0^{+}}\mathcal{A}_{a}^{\parallel} + \qquad 0 \qquad {}^{ia.k}_{-\frac{0}{2}\sqrt{2}} - {}^{\frac{0}{2}}_{-\frac{0}{2}} + (-c. + c.) k^{2} \qquad 0 \qquad \qquad 0$ ${\stackrel{0^{+}}{\mathcal{A}}}_{s} {\parallel} + \left[ -\frac{1}{4} \, i \, a_{.} \, k \, \frac{i \, a_{.} \, k}{4 \, \sqrt{3}} \right] \qquad \qquad 0 \qquad \qquad {\stackrel{a}{\stackrel{0}{=}}} \quad -\frac{2}{3} \, (c_{.} + c_{.}) \, k^{2} \qquad \frac{-3 \, a_{.} + 4 \, (c_{.} + c_{.}) \, k^{2}}{6 \, \sqrt{2}}$ $\frac{1}{1}h^{\perp} + \frac{\alpha}{4} \qquad 0 \qquad 0 \qquad 0 \qquad 0 \qquad \frac{ia.k}{4\sqrt{2}} \qquad 0 \qquad -\frac{ia.k}{4\sqrt{6}} \qquad \frac{1}{4}i\sqrt{\frac{5}{6}}a.k \qquad -\frac{ia.k}{4\sqrt{3}}$ $\frac{1}{3}\mathcal{A}_{a}^{\parallel} + \alpha \qquad 0 \qquad 0 \qquad -\frac{ia.k}{4\sqrt{2}} \qquad -\frac{a.}{4} + (-c. + c.)k^{2} \qquad \frac{a.}{2\sqrt{2}} \qquad 0 \qquad 0 \qquad 0$ $\frac{1}{2}\mathcal{A}_{a}^{\perp} + \frac{\alpha}{2}$ 0 0 0 0 $\frac{a}{2}\frac{a}{\sqrt{2}}$ 0 0 0 0 $\frac{1}{3}\mathcal{A}_{s}^{1} + \alpha \qquad 0 \qquad 0 \qquad \frac{\frac{ia.k}{0}}{4\sqrt{6}} \qquad 0 \qquad 0 \qquad \frac{\frac{1}{3}(-a. -(c. + c.)k^2)}{6} \qquad \frac{\sqrt{5}a.}{\frac{0}{6}} \qquad \frac{\frac{-a. -4(c. + c.)k^2}{1-2}}{6\sqrt{2}}$ $\frac{1}{3}\mathcal{A}_{s}^{\parallel t} + \alpha \qquad 0 \qquad 0 \qquad -\frac{1}{4}i\sqrt{\frac{5}{6}}a_{0}k \qquad 0 \qquad 0 \qquad \frac{\sqrt{5}a_{0}}{6} \qquad \frac{1}{3}(a_{0}-3(c_{1}+c_{2})k^{2}) \qquad -\frac{1}{6}\sqrt{\frac{5}{2}}a_{0} \qquad -\frac{\sqrt{5}a_{0}}{6}$ $\frac{1}{3}\mathcal{A}_{s}^{\perp h} \uparrow^{\alpha} = 0 \qquad 0 \qquad 0 \qquad \frac{\frac{ia.k}{0}}{4\sqrt{3}} \qquad 0 \qquad 0 \qquad \frac{\frac{-a.-4(c.+c.)k^{2}}{0\sqrt{2}}}{6\sqrt{2}} \qquad -\frac{1}{6}\sqrt{\frac{5}{2}}a_{0} \qquad \frac{1}{3}(a_{0}-2(c_{1}+c_{2})k^{2}) \qquad \frac{a.}{6\sqrt{2}}$ ${}^{2^{+}}\mathcal{A}_{s}{}^{\perp} + {}^{\alpha\beta} \left[ -\frac{i a \cdot k}{\frac{0}{4} \sqrt{6}} \right] = 0 \qquad \qquad \frac{1}{3} \sqrt{2} \left( c_{1} + c_{2} \right) k^{2} \qquad \frac{a}{0} - \frac{1}{3} \left( c_{1} + c_{2} \right) k^{2} \qquad \qquad 0 \qquad \qquad 0$ ${}^{2}\mathcal{H}_{a}^{\parallel} \dagger^{\alpha\beta\chi} = 0 \qquad 0 \qquad 0 \qquad 0 \qquad \frac{{}^{a}}{{}^{0}} + (-c_{1} + c_{2}) k^{2} = 0$ $\frac{24ik(-3a.+2(5c.+3c.)k^2)}{a.^2(16+3k^2)^2} \qquad \frac{8ik(19a.+(3a.-10c.-6c.)k^2)}{a.^2(16+3k^2)^2} \qquad \frac{4i\sqrt{2}k(10a.+(3a.+20c.+12c.)k^2)}{a.^2(16+3k^2)^2}$ $-\frac{8i(a.+2(c.-c.)k^2)}{\sqrt{3}a.^2k(16+3k^2)}$ $-\frac{8}{\sqrt{3} (16a.+3a.k^2)}$ $\frac{304a.+16(3a.-10c.-6c.)k^{2}}{a.^{2}(16+3k^{2})^{2}} \qquad \frac{-560a.+32(-3a.+5c.+3c.)k^{2}}{3a.^{2}(16+3k^{2})^{2}} \qquad \frac{8\sqrt{2}(-22a.+(-3a.+20c.+12c.)k^{2})}{3a.^{2}(16+3k^{2})^{2}} \qquad 0$ $\frac{4i\sqrt{2}k(10a.+(3a.+20c.+12c.)k^2)}{a.\frac{2}{0}(16+3k^2)^2} \frac{8i\sqrt{\frac{2}{3}}(a.+2(c.-c.)k^2)}{a.\frac{2}{0}k(16+3k^2)} - \frac{8}{\sqrt{3}}\frac{(16a.+3a.k^2)}{(16a.+3a.k^2)} - \frac{8\sqrt{2}(10a.+(3a.+20c.+12c.)k^2)}{a.\frac{2}{0}(16+3k^2)^2} \frac{8\sqrt{2}(-22a.+(-3a.+20c.+12c.)k^2)}{3a.\frac{2}{0}(16+3k^2)^2} - \frac{416a.+32(3a.+10c.+6c.)k^2}{3a.\frac{2}{0}(16+3k^2)^2}$ $\begin{array}{c|c} \hline & \overline{a} + 2 (c - c) k^2 \\ \hline & 1 + 2 \begin{pmatrix} c - c \end{pmatrix} k^2 \\ \hline & W_a \parallel_{\alpha\beta} & 1 + W_a \parallel_{\alpha\beta} & 1 + W_s \parallel_{\alpha\beta} \\ \hline \end{array}$ $-\frac{i\,k\,(6\,a.\overset{2}{\overset{+}a.}\,(5\,a.\overset{-}{\overset{32}(c.+c.)})\,k^{2}-8\,(-4\,(c.+c.)^{2}+a.\,(c.+3\,c.))\,k^{4}-16\,(c.-2\,c.)\,(c.+c.)\,k^{6})}{\sqrt{6}\,a.\overset{2}{\overset{2}(2+k^{2})^{2}}\,(a.\overset{-}{\overset{3}(c.+c.)}\,k^{2})}$ $-\frac{2\,i\,k\,(3\,a.^{\,2}+a.\,(a.+2\,(c.+c.))\,k^{2}-(a.\,(c.-3\,c.)+8\,(c.+c.)^{\,2})\,k^{\,4}+4\,(c.-2\,c.)\,(c.+c.)\,k^{\,6})}{\sqrt{3}\,a.^{\,2}\,(2+k^{\,2})^{\,2}\,(a.-3\,(c.+c.)\,k^{\,2})}$ $\frac{2 k^{2} (a.^{2}+4 a. (c.-c.) k^{2}-8 (2 c.-c.) (c.+c.) k^{4})}{0 \quad 1 \quad 2}$ $i k (4 \underbrace{a. (c. -7 c.)}_{0} k^{2} - 2 \underbrace{a. (c. +5 c.)}_{1} k^{4} + a.^{2} (4 + k^{2}) - 8 (c. +c.) k^{4} (-2 c. (3 + k^{2}) + c. (6 + k^{2})))$ $\frac{i\sqrt{\frac{5}{6}}k(a.-4(c.+c.)k^2)}{a.(2+k^2)(a.-3(c.+c.)k^2)\atop 0}$ $\frac{i \sqrt{\frac{2}{3}} k (a.+2 (c.+c.) k^2)}{a. (2+k^2) (a.-3 (c.+c.) k^2)}$ $a.^{2}(2+k^{2})^{2}(a.-3(c.+c.)k^{2})$ $a.^{2}(2+k^{2})^{2}(a.-3(c.+c.)k^{2})$ $|W_a| \uparrow^\alpha 0$ 0 0 $\frac{1}{2} \mathcal{W}_{a}^{\perp} + \frac{\alpha}{2} \qquad 0 \qquad 0 \qquad 0 \qquad -\frac{\frac{i \, k \, (4 \, a \, \cdot \, (c \, -7 \, c \, \cdot \, ) \, k^2 - 2 \, a \, \cdot \, (c \, +5 \, c \, \cdot ) \, k^4 + a \, \cdot^2 \, (4 + k^2) - 8 \, (c \, +c \, \cdot \, ) \, k^4 \, (-2 \, c \, \cdot \, (3 + k^2) + c \, \cdot \, (6 + k^2)))}{a \, \cdot^2 \, (2 + k^2)^2 \, (a \, -3 \, (c \, +c \, \cdot \, ) \, k^2)} \qquad \frac{\sqrt{2} \, \, (4 + k^2)}{a \, \cdot^2 \, (2 + k^2)} \qquad \frac{a \, \cdot^2 \, (4 + k^2)^2 - 8 \, (c \, +c \, \cdot \, ) \, k^4 \, (2 \, c \, \cdot \, (12 + 6 \, k^2 + k^4) - c \, \cdot \, (24 + 12 \, k^2 + k^4) + a \, \cdot \, k^2 \, (c \, \cdot \, (4 + 2 \, k^2 + k^4) - c \, \cdot \, (28 + 14 \, k^2 + k^4))}{a \, \cdot^2 \, (2 + k^2)^2 \, (a \, -3 \, (c \, +c \, \cdot \, ) \, k^4 \, (2 \, c \, \cdot \, (12 + 6 \, k^2 + k^4) - c \, \cdot \, (24 + 12 \, k^2 + k^4) - c \,$ $\frac{a \cdot {}^{2} k^{2} (-2+k^{2})+16 (2 c \cdot -c \cdot ) (c \cdot +c \cdot ) k^{6} (4+k^{2})+4 a \cdot k^{4} (-10 c \cdot +6 c \cdot +(-3 c \cdot +c \cdot ) k^{2})}{2 \sqrt{6} a \cdot {}^{2} (2+k^{2})^{2} (a \cdot -3 (c \cdot +c \cdot ) k^{2})}$ $\frac{-4 \left(2 c.-c.\right) \left(c.+c.\right) k^{6} \left(4+k^{2}\right)+a.^{2} k^{2} \left(5+2 k^{2}\right)+4 a. k^{4} \left(c.-c. \left(3+k^{2}\right)\right)}{\sqrt{3} a.^{2} \left(2+k^{2}\right)^{2} \left(a.-3 \left(c.+c.\right) k^{2}\right)}$ $-\frac{\sqrt{\frac{5}{6}} k^2 (a.-4 (c.+c.) k^2)}{2 a. (2+k^2) (a.-3 (c.+c.) k^2)}$ $-\frac{k^2 (a.+2 (c.+c.) k^2)}{\sqrt{6} a.(2+k^2) (a.-3 (c.+c.) k^2)}$ $\frac{i \, k \, (6 \, a_{.0}^{\ 2} + a_{.0}^{\ } (5 \, a_{.0}^{\ -32} \, (c_{.1} + c_{.0}^{\ })) \, k^2 - 8 \, (-4 \, (c_{.} + c_{..}^{\ })^2 + a_{.0}^{\ } \, (c_{.1} + 3 \, c_{.0}^{\ })) \, k^4 - 16 \, (c_{.-2} \, c_{.0}^{\ }) \, (c_{.} + c_{.0}^{\ }) \, k^6)}{\sqrt{6} \, a_{.0}^{\ 2} \, (2 + k^2)^2 \, (a_{.0}^{\ -3} \, (c_{.1} + c_{.0}^{\ }) \, k^2)} - \frac{2 \, k^2}{\sqrt{3} \, a_{.0}^{\ } \, (2 + k^2)}$ $\frac{a.^{2} k^{2} (-2+k^{2})+16 (2 c. -c.) (c. +c.) k^{6} (4+k^{2})+4 a. k^{4} (-10 c. +6 c. +(-3 c. +c.) k^{2})}{2 \sqrt{6} a.^{2} (2+k^{2})^{2} (a. -3 (c. +c.) k^{2})}$ $-\frac{\sqrt{5}\frac{(a.-4(c.+c.)k^2)(a.(2+k^2)-2(c.+c.)k^2(2+k^2)-2(c.+c.)k^2(4+k^2))}{12a.(c.+c.)k^2(2+k^2)(a.-3(c.+c.)k^2)(2+k^2)(a.-3(c.+c.)k^2)}}{(-a.-3(c.+c.)k^2(2+k^2)(a.-3(c.+c.)k^2)(2+k^2)(a.-3(c.+c.)k^2)}(-a.-3(c.+c.)k^2)($ $-((a_{.0}^{.3}(2+k^2)^2+8a_{.0}^{.2}(c_{.1}+c_{.2})k^2(8+5k^2)-32a_{.0}(c_{.1}+c_{.2})k^4(10(c_{.1}+c_{.2})+6(c_{.1}+c_{.2})k^2+c_{.1}k^4)+32(c_{.1}+c_{.2})k^6(8(c_{.1}+c_{.2})+4(c_{.1}+c_{.2})k^2+(2c_{.1}-c_{.2})k^4))/(12a_{.0}^{.2}(c_{.1}+c_{.2})k^2(2+k^2)^2(a_{.0}-3(c_{.1}+c_{.2})k^2)))$ $-\frac{\sqrt{5} \left(a._{0}^{2} (2+k^{2})+8 (c.+c.)^{2} k^{4} (4+k^{2})-2 a. (c.+c.) k^{2} (8+3 k^{2})\right)}{12 a. (c.+c.) k^{2} (2+k^{2}) (a.-3 (c.+c.) k^{2})}$ $-\frac{\sqrt{5} (a.-2 (c.+c.) k^2)}{6 (c.+c.) k^2 (a.-3 (c.+c.) k^2)}$ $\frac{-5a.+16(c.+c.)k^2}{12(c.+c.)k^2(a.-3(c.+c.)k^2)}$ $\frac{\sqrt{\frac{5}{2}} (-a_{.0}^{2} (2+k^{2})+4 (c_{.1}+c_{.1})^{2} k^{4} (4+k^{2})+a_{.0} (c_{.1}+c_{.1}) k^{2} (4+3 k^{2}))}{6 a_{.0} (c_{.1}+c_{.1}) k^{2} (2+k^{2}) (a_{.0}-3 (c_{.1}+c_{.1}) k^{2})}$ $-\frac{\sqrt{\frac{5}{6}} k^2 (a_0 - 4 (c_1 + c_2) k^2)}{2 a_0 (2 + k^2) (a_0 - 3 (c_1 + c_2) k^2)}$ $-\frac{\sqrt{\frac{5}{2}}\frac{(a_{.}-4(c_{.}+c_{.})k^{2})(a_{.}(2+k^{2})+(c_{.}+c_{.})k^{2}(4+k^{2})}{(a_{.}-4(c_{.}+c_{.})k^{2})(a_{.}(2+k^{2})+(c_{.}+c_{.})k^{2})(a_{.}(2+k^{2})+(c_{.}+c_{.})k^{2}(4+k^{2}))}}{6a_{.}(c_{.}+c_{.})k^{2}(2+k^{2})(a_{.}-3(c_{.}+c_{.})k^{2})}} -((a_{.}-3(c_{.}+c_{.})k^{2}(4+k^{2}))(a_{.}-3(c_{.}+c_{.})k^{2})(a_{.}-3(c_{.}+c_{.$ $\frac{2ik(3a.^{2}+a.(a.+2(c.+c.))k^{2}-(a.(c.^{3}c.)+8(c.+c.)^{2})k^{4}+4(c.^{2}c.)(c.+c.)k^{6})}{\sqrt{3}a.^{2}(2+k^{2})^{2}(a.^{3}(c.+c.)k^{2})} \frac{\sqrt{\frac{2}{3}}k^{2}}{a.(2+k^{2})}$ $\frac{-4 \left(2 c.-c.\right) \left(c.+c.\right) k^{6} \left(4+k^{2}\right)+a.^{2} k^{2} \left(5+2 k^{2}\right)+4 a. k^{4} \left(c.-c. \left(3+k^{2}\right)\right)}{\sqrt{3} a.^{2} \left(2+k^{2}\right)^{2} \left(a.-3 \left(c.+c.\right) k^{2}\right)}$ $(-a.^{3}(2+k^{2})^{2}+a.^{2}(c.+c.)k^{2}(4+k^{2})(2+3k^{2})-4a.(c.+c.)k^{4}(16(c.+c.)+6(c.+c.)+6(c.+c.)k^{2}+(c.-3c.)k^{4})+16(c.+c.)+4(c.+c.)+4(c.+c.)+4(c.+c.)k^{2}+(2c.-c.)k^{4}))/(6\sqrt{2}a.^{2}(c.+c.)k^{2})(2+k^{2})^{2}(a.-3(c.+c.)k^{2}))$ $\frac{4a.(c.+c.)k^{2}-a.^{2}(2+k^{2})+4(c.+c.)^{2}k^{4}(4+k^{2})}{6a.(c.+c.)k^{2}(2+k^{2})(a.-3(c.+c.)k^{2})}$ $-\frac{(a.+2(c.+c.)k^2)(a.(2+k^2)+(c.+c.)k^2(4+k^2))}{3\sqrt{2}a.(c.+c.)k^2(2+k^2)(a.-3(c.+c.)k^2)}$ $-\frac{\sqrt{5} (a.-2 (c.+c.) k^2)}{6 (c.+c.) k^2 (a.-3 (c.+c.) k^2)}$ $-\frac{k^2 (a. + 2 (c. + c.) k^2)}{\sqrt{6} a. (2 + k^2) (a. - 3 (c. + c.) k^2)}$ $\frac{a.-8 (c.+c.) k^2}{{}_{0} {}_{1} {}_{2} k^2}$ $-3 a. (c.+c.) k^2 + 9 (c.+c.)^2 k^4$ $-\frac{i\sqrt{\frac{2}{3}}k(a.+2(c.+c.)k^2)}{a.(2+k^2)(a.-3(c.+c.)k^2)}$ ${}^{2^{+}}\!\mathcal{T} \parallel_{\alpha\beta} \qquad {}^{2^{+}}\!W_{\mathsf{a}} \parallel_{\alpha\beta} \qquad {}^{2^{+}}\!W_{\mathsf{s}} \parallel_{\alpha\beta} \qquad {}^{2^{+}}\!W_{\mathsf{s}} \parallel_{\alpha\beta} \qquad {}^{2^{-}}\!W_{\mathsf{a}} \parallel_{\alpha\beta\chi} \qquad {}^{2^{-}}\!W_{\mathsf{s}} \parallel_{\alpha\gamma\chi} \qquad {}^{2^{-}}\!W$ **Source constraints** Spin-parity form $2 \partial_{\beta} \partial_{\alpha} \mathcal{T}^{\alpha\beta} + \partial_{\chi} \partial^{\chi} \partial_{\alpha} \mathcal{W}^{\alpha\beta}{}_{\beta} = \partial_{\chi} \partial_{\beta} \partial_{\alpha} \mathcal{W}^{\alpha\beta\chi}$ $k^{0+}W_{s}^{\parallel} + 2k^{0+}W_{s}^{\perp h} - 6i^{0+}T^{\perp} == 0$ $2\,\partial_{\beta}\partial_{\alpha}\mathcal{T}^{\alpha\beta} = \partial_{\chi}\partial_{\beta}\partial_{\alpha}\mathcal{W}^{\alpha\beta\chi}$ $k^{0^{+}} \mathcal{W}_{s}^{\perp t} + 2 i^{0^{+}} \mathcal{T}^{\perp} == 0$ $k \, {}^{1}\mathcal{W}_{\mathsf{s}}{}^{\perp\mathsf{h}\alpha} - 6 \, i \, {}^{1}\mathcal{T}^{\perp\alpha} == k \, (3 \, {}^{1}\mathcal{W}_{\mathsf{a}}{}^{\perp\alpha} + \, {}^{1}\mathcal{W}_{\mathsf{s}}{}^{\perp\mathsf{t}\alpha}) \, \left[ 2 \, \partial_{\chi} \partial_{\beta} \partial^{\alpha} \mathcal{T}^{\beta\chi} + \partial_{\delta} \partial^{\delta} \partial_{\chi} \partial_{\beta} \mathcal{W}^{\beta\alpha\chi} == 2 \, \partial_{\chi} \partial^{\chi} \partial_{\beta} \mathcal{T}^{\alpha\beta} + \partial_{\delta} \partial_{\chi} \partial_{\beta} \partial^{\alpha} \mathcal{W}^{\beta\chi\delta} \, \right] \, 3$ Total expected gauge generators: $J^{P} = 1^{+}$ $k^{\mu} = \underbrace{(\mathcal{E}, 0, 0, p)}$ Massive particle Massive particle Square mass: $-\frac{a}{2(c.-c.)} > 0$ $J^P = 2^$ $k^{\mu} = (\mathcal{E}, 0, 0, p)$

**PSALTer results panel** 

Massless particle