

Particle spectrograph

Wave operator and propagator

Quadratic (free) action

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$$\begin{aligned} & \iiint \left[\left(\frac{1}{6} f^{\alpha\beta} \tau_{\alpha\beta} + 6 \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - 15 r_3 \partial_\beta \omega_{,\theta}^\theta \partial' \omega_{,\theta}^{\alpha\beta} + 9 r_3 \partial_\beta \omega_{,\theta}^\theta \partial' \omega_{,\theta}^{\alpha\beta} + \right. \right. \\ & \quad \left. \left. 9 r_3 \partial_\alpha \omega^{\alpha\beta} \partial_\theta \omega_{\beta,\theta}^\theta - 18 r_3 \partial' \omega_{,\theta}^{\alpha\beta} \partial_\theta \omega_{\beta,\theta}^\theta - 15 r_3 \partial_\alpha \omega^{\alpha\beta} \partial_\theta \omega_{,\theta}^\theta + \right. \right. \\ & \quad \left. \left. 30 r_3 \partial' \omega_{,\theta}^{\alpha\beta} \partial_\theta \omega_{,\theta}^\theta + 4 t_2 \omega_{,\theta\alpha}^\theta \partial^\theta f^{\alpha\iota} + 2 t_2 \partial_\alpha f_{,\theta}^\theta \partial^\theta f^{\alpha\iota} - t_2 \partial_\alpha f_{,\theta\iota}^\theta \partial^\theta f^{\alpha\iota} - \right. \right. \\ & \quad \left. \left. t_2 \partial_\iota f_{,\alpha\theta}^\theta \partial^\theta f^{\alpha\iota} + t_2 \partial_\theta f_{,\alpha\iota}^\theta \partial^\theta f^{\alpha\iota} - t_2 \partial_\theta f_{,\iota\alpha}^\theta \partial^\theta f^{\alpha\iota} - 4 t_2 \omega_{\alpha\theta\iota}^{\alpha\iota\theta} (\omega^{\alpha\iota\theta} + \partial^\theta f^{\alpha\iota}) + \right. \right. \\ & \quad \left. \left. 2 t_2 \omega_{\alpha\iota\theta}^{\alpha\iota\theta} (\omega^{\alpha\iota\theta} + 2 \partial^\theta f^{\alpha\iota}) + 8 r_2 \partial_\beta \omega_{\alpha\iota\theta}^\theta \partial^\theta \omega^{\alpha\beta\iota} - 4 r_2 \partial_\beta \omega_{\alpha\theta\iota}^\theta \partial^\theta \omega^{\alpha\beta\iota} + \right. \right. \\ & \quad \left. \left. 4 r_2 \partial_\beta \omega_{,\theta\alpha}^\theta \partial^\theta \omega_{,\theta\alpha}^{\alpha\beta\iota} - 24 r_3 \partial_\beta \omega_{,\theta\alpha}^\theta \partial^\theta \omega_{,\theta\alpha}^{\alpha\beta\iota} - 2 r_2 \partial_\iota \omega_{\alpha\beta\theta}^\theta \partial^\theta \omega^{\alpha\beta\iota} + \right. \right. \\ & \quad \left. \left. 2 r_2 \partial_\theta \omega_{\alpha\beta\iota}^\theta \partial^\theta \omega_{\alpha\beta\iota}^{\alpha\beta\iota} - 4 r_2 \partial_\theta \omega_{\alpha\iota\beta}^\theta \partial^\theta \omega_{\alpha\iota\beta}^{\alpha\beta\iota} \right) \right] [t, x, y, z] dz dy dx dt \end{aligned}$$

$\omega_{1+}^{\#1+\alpha\beta}$	$\frac{2t_2}{3}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{1}{3}\bar{i}\sqrt{2}kt_2$	$\omega_{1-}^{\#1}\omega_{1-}^{\#2}$	$\omega_{1-}^{\#1}\omega_{1-}^{\#2}$	$f_{1-}^{\#1}f_{1-}^{\#2}$
$\omega_{1+}^{\#2+\alpha\beta}$	$\frac{\sqrt{2}t_2}{3}$	$\frac{t_2}{3}$	$\frac{ikt_2}{3}$	0	0	0
$f_{1+}^{\#1+\alpha\beta}$	$-\frac{1}{3}\bar{i}\sqrt{2}kt_2$	$-\frac{1}{3}\bar{i}kt_2$	$\frac{k^2t_2}{3}$	0	0	0
$\omega_{1-}^{\#1+\alpha}$	0	0	0	$-\frac{3k^2r_3}{2}$	0	0
$\omega_{1-}^{\#2+\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#1+\alpha}$	0	0	0	0	0	0
$f_{1-}^{\#2+\alpha}$	0	0	0	0	0	0

	$\omega_{2+}^{\#1} \alpha \beta$	$f_{2+}^{\#1} \alpha \beta$	$\omega_{2-}^{\#1} \alpha \beta \chi$
$\omega_{2+}^{\#1} \dagger \alpha \beta$	$-\frac{3k^2 r_3}{2}$	0	0
$f_{2+}^{\#1} \dagger \alpha \beta$	0	0	0
$\omega_{2-}^{\#1} \dagger \alpha \beta \chi$	0	0	0

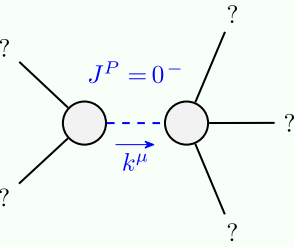
	$\sigma_{2+}^{\#1} \alpha\beta$	$\tau_{2+}^{\#1} \alpha\beta$	$\sigma_{2-}^{\#1} \alpha\beta\chi$
$\sigma_{2+}^{\#1} \dagger \alpha\beta$	$-\frac{2}{3k^2 r_3}$	0	0
$\tau_{2+}^{\#1} \dagger \alpha\beta$	0	0	0
$\sigma_{2-}^{\#1} \dagger \alpha\beta\chi$	0	0	0

	ω_0^{1+}	f_0^{1+}	f_0^{2+}	ω_0^{1-}
$\omega_0^{1+} \uparrow$	0	0	0	0
$f_0^{1+} \uparrow$	0	0	0	0
$f_0^{2+} \uparrow$	0	0	0	0
$\omega_0^{1-} \uparrow$	0	0	0	$k^2 r_2 + t_2$

SO(3) irreps	Multiplicities
$\tau_{0+}^{\#2} == 0$	1
$\tau_{0+}^{\#1} == 0$	1
$\sigma_{0+}^{\#1} == 0$	1
$\tau_{1-}^{\#2\alpha} == 0$	3
$\tau_{1-}^{\#1\alpha} == 0$	3
$\sigma_{1-}^{\#2\alpha} == 0$	3
$\tau_{1+}^{\#1\alpha\beta} + i k \sigma_{1+}^{\#1\alpha\beta} == 0$	3
$\sigma_{1+}^{\#1\alpha\beta} == \sigma_{1+}^{\#2\alpha\beta}$	3
$\sigma_{2-}^{\#1\alpha\beta\chi} == 0$	5
$\tau_{2+}^{\#1\alpha\beta} == 0$	5
Total constraints:	28

	$\sigma_{0^+}^{\#1}$	$\tau_{0^+}^{\#1}$	$\tau_{0^+}^{\#2}$	$\sigma_{0^-}^{\#1}$
$\sigma_{0^+}^{\#1} \dagger$	0	0	0	0
$\tau_{0^+}^{\#1} \dagger$	0	0	0	0
$\tau_{0^+}^{\#2} \dagger$	0	0	0	0
$\sigma_{0^-}^{\#1} \dagger$	0	0	0	$\frac{1}{k^2 r_2 + t_2}$

Massive and massless spectra



Massive particle	
Pole residue:	$-\frac{1}{r_2} > 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} > 0$
Spin:	0
Parity:	Odd

(No massless particles)

Unitarity conditions

$$r_2 < 0 \ \&\& \ t_2 > 0$$