Particle spectrograph

Wave operator and propagator

	$\Delta^{\#1}_{1^{+}\alpha\beta}$	$\Delta^{\#2}_{1^{+}\alpha\beta}$	$\Delta^{\#3}_{1^{+}\alpha\beta}$	$\Delta^{\#1}_{1^{-}\alpha}$	$\Delta^{\#2}_{1^{-}\alpha}$	$\Delta^{\#3}_{1^{-}\alpha}$	$\Delta^{\#4}_{1^{-}\alpha}$	$\Delta^{\#5}_{1^{-}\alpha}$	$\Delta^{\#6}_{1^{-}\alpha}$	$\mathcal{T}^{\#1}_{1^{-}\alpha}$
$\Delta^{\#1}_{1^{+}}{\dagger}^{\alpha\beta}$	0	$-\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0	0	0	0
$\Delta^{\#2}_{1^{+}}{\dagger}^{\alpha\beta}$	$-\frac{2\sqrt{2}}{a_0}$	$\frac{2}{a_0}$	0	0	0	0	0	0	0	0
$\Delta^{\#3}_{1^{+}}{\dagger}^{\alpha\beta}$	0	0	$\frac{4}{a_0}$	0	0	0	0	0	0	0
$\Delta^{\#1}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	$\frac{2\sqrt{2}}{a_0}$	0	0	0	0	0
$\Delta^{\#2}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	$\frac{2\sqrt{2}}{a_0}$	$\frac{2}{a_0}$	0	0	0	0	0
$\Delta^{\#3}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$-\frac{19}{12 a_0}$	$\frac{5\sqrt{5}}{12 a_0}$	$-\frac{1}{6\sqrt{2}\,a_0}$	$-\frac{1}{6 a_0}$	0
$\Delta^{\#4}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$\frac{5\sqrt{5}}{12 a_0}$	$\frac{1}{12 a_0}$	$-\frac{\sqrt{\frac{5}{2}}}{6 a_0}$	$-\frac{\sqrt{5}}{6 a_0}$	0
$\Delta^{\#5}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$-\frac{1}{6\sqrt{2}\,a_0}$	$-\frac{\sqrt{\frac{5}{2}}}{6 a_0}$	$\frac{17}{6 a_0}$	$-\frac{7}{3\sqrt{2}\,a_0}$	0
$\Delta^{\#6}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$-\frac{1}{6 a_0}$	$-\frac{\sqrt{5}}{6 a_0}$	$-\frac{7}{3\sqrt{2}\,a_0}$	$\frac{5}{3 a_0}$	0
$\mathcal{T}^{\#1}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	0	0	0	0	0

	$\Gamma^{\#1}_{1^{+}\alpha\beta}$	$\Gamma^{\#2}_{1^{+}\alpha\beta}$	$\Gamma^{\#3}_{1^{+}\alpha\beta}$	$\Gamma^{\#1}_{1^{-}\alpha}$	$\Gamma^{\#2}_{1^{-}\alpha}$	$\Gamma^{\#3}_{1^{-}\alpha}$	$\Gamma^{\#4}_{1^{-}\alpha}$	$\Gamma^{\#5}_{1^{-}\alpha}$	$\Gamma^{\#6}_{1^{-}\alpha}$	$h^{\#1}_{1^{-}\alpha}$
$\Gamma^{\#1}_{1^{+}}{\dagger}^{\alpha\beta}$	$-\frac{a_0}{4}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0	0	0
$\Gamma^{\#2}_{1^{+}}{\dagger}^{\alpha\beta}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0	0	0	0
$\Gamma^{\#3}_{1^{+}}{\dagger}^{\alpha\beta}$	0	0	$\frac{a_0}{4}$	0	0	0	0	0	0	0
$\Gamma^{\#1}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	$-\frac{a_0}{4}$	$\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0
$\Gamma^{\#2}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	$\frac{a_0}{2\sqrt{2}}$	0	0	0	0	0	0
$\Gamma^{\#3}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$-\frac{a_0}{3}$	$\frac{\sqrt{5}\,a_0}{6}$	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{a_0}{6}$	0
$\Gamma^{\#4}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$\frac{\sqrt{5}\,a_0}{6}$	$\frac{a_0}{3}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}\,a_0$	$-\frac{\sqrt{5}\,a_0}{6}$	0
$\Gamma^{\#5}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$-\frac{a_0}{6\sqrt{2}}$	$-\frac{1}{6}\sqrt{\frac{5}{2}}\,a_0$	$\frac{a_0}{3}$	$\frac{a_0}{6\sqrt{2}}$	0
$\Gamma^{\#6}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	$-\frac{a_0}{6}$	$-\frac{\sqrt{5}\,a_0}{6}$	$\frac{a_0}{6\sqrt{2}}$	$\frac{5 a_0}{12}$	0
$h^{\#1}_{1^{-}}{\dagger}^{\alpha}$	0	0	0	0	0	0	0	0	0	0

Quadratic (free) action

$$S==\iiiint\Big(\tfrac{1}{8}\big(8\,h^{\alpha\beta}\,\mathcal{T}_{\alpha\beta}-4\,\Gamma^{\alpha\beta\chi}\,(a_0\,\Gamma_{\beta\chi\alpha}-2\,\Delta_{\alpha\beta\chi}+a_0\,\partial_{\beta}h_{\alpha\chi})+2\,a_0\,\Gamma^{\alpha\beta}{}_{\alpha}\,\partial_{\beta}h^{\chi}{}_{\chi}-$$
$$2\,a_0\,h^{\chi}{}_{\chi}\,\partial_{\beta}\Gamma^{\alpha}{}_{\alpha}{}^{\beta}+2\,a_0\,h^{\chi}{}_{\chi}\,\partial_{\beta}\Gamma^{\alpha\beta}{}_{\alpha}-4\,a_0\,h_{\alpha\chi}\,\partial_{\beta}\Gamma^{\alpha\beta\chi}+$$
$$4\,a_0\,h^{\alpha\beta}\,\partial_{\beta}\partial_{\alpha}h^{\chi}{}_{\chi}-a_0\,\partial_{\beta}h^{\chi}{}_{\chi}\,\partial^{\beta}h^{\alpha}{}_{\alpha}-4\,a_0\,\partial_{\alpha}h^{\alpha\beta}\,\partial_{\chi}h_{\beta}{}^{\chi}+$$
$$4\,a_0\,\partial^{\beta}h^{\alpha}{}_{\alpha}\,\partial_{\chi}h_{\beta}{}^{\chi}+2\,a_0\,\Gamma^{\alpha}{}_{\alpha}{}^{\beta}\,(2\,\Gamma^{\chi}{}_{\beta\chi}-\partial_{\beta}h^{\chi}{}_{\chi}+2\,\partial_{\chi}h_{\beta}{}^{\chi})-$$
$$8\,a_0\,h^{\alpha\beta}\,\partial_{\chi}\partial_{\beta}h_{\alpha}{}^{\chi}+2\,a_0\,h^{\alpha}{}_{\alpha}\,\partial_{\chi}\partial_{\beta}h^{\beta\chi}+$$
$$4\,a_0\,h^{\alpha\beta}\,\partial_{\chi}\partial^{\chi}h_{\alpha\beta}-2\,a_0\,h^{\alpha}{}_{\alpha}\,\partial_{\chi}\partial^{\chi}h^{\beta}{}_{\beta}-$$
$$2\,a_0\,\partial_{\beta}h_{\alpha\chi}\,\partial^{\chi}h^{\alpha\beta}+3\,a_0\,\partial_{\chi}h_{\alpha\beta}\,\partial^{\chi}h^{\alpha\beta}+$$
$$4\,a_0\,h_{\beta\chi}\,\partial^{\chi}\Gamma^{\alpha}{}_{\alpha}{}^{\beta}\big)\Big)[t,x,y,z]\,dz\,dy\,dx\,dt$$

Source constraints

SO(3) irreps	Fundamental fields	Multiplicities
$\mathcal{T}^{\#2}_{0^{+}}==0$	$\partial_{\beta}\partial_{\alpha}\mathcal{T}^{\alpha\beta}==0$	1
$\Delta^{\#3}_{0^{+}}+2\,\Delta^{\#4}_{0^{+}}+3\,\Delta^{\#2}_{0^{+}}==0$	$\partial_{\alpha}\Delta^{\alpha\beta}{}_{\beta}==0$	1
$\mathcal{T}^{\#1}_{1^{-}}{}^{\alpha}==0$	$\partial_{\chi}\partial_{\beta}\partial^{\alpha}\mathcal{T}^{\beta\chi}==\partial_{\chi}\partial^{\chi}\partial_{\beta}\mathcal{T}^{\alpha\beta}$	3
$2\,\Delta^{\#6}_{1^{-}}{}^{\alpha}+\Delta^{\#4}_{1^{-}}{}^{\alpha}+2\,\Delta^{\#5}_{1^{-}}{}^{\alpha}+\Delta^{\#3}_{1^{-}}{}^{\alpha}==0$	$\partial_{\beta}\partial^{\alpha}\Delta^{\beta\chi}{}_{\chi}==\partial_{\chi}\partial^{\chi}\Delta^{\alpha\beta}{}_{\beta}$	3
Total constraints/gauge generators:		8

	$\Gamma^{\#1}_{3^{-}\alpha\beta\chi}$
$\Gamma^{\#1}_{3^{-}}{\dagger}^{\alpha\beta\chi}$	$-\frac{a_0}{2}$

	$\Delta^{\#1}_{3^{-}\alpha\beta\chi}$
$\Delta^{\#1}_{3^{-}}{\dagger}^{\alpha\beta\chi}$	$-\frac{2}{a_0}$

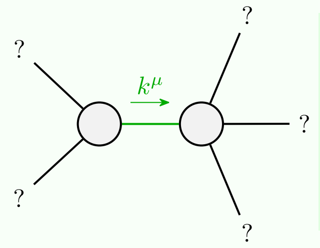
	$\Delta^{\#1}_{0^{+}}$	$\Delta^{\#2}_{0^{+}}$	$\Delta^{\#3}_{0^{+}}$	$\Delta^{\#4}_{0^{+}}$	$\mathcal{T}^{\#1}_{0^{+}}$	$\mathcal{T}^{\#2}_{0^{+}}$	$\Delta^{\#1}_{0^{-}}$
$\Delta^{\#1}_{0^{+}}{\dagger}$	$-\frac{2}{a_0}$	0	0	0	0	0	0
$\Delta^{\#2}_{0^{+}}{\dagger}$	0	$-\frac{3}{4 a_0}$	$\frac{5}{4 a_0}$	$-\frac{1}{2\sqrt{2}\,a_0}$	0	0	0
$\Delta^{\#3}_{0^{+}}{\dagger}$	0	$\frac{5}{4 a_0}$	$-\frac{3}{4 a_0}$	$-\frac{1}{2\sqrt{2}\,a_0}$	0	0	0
$\Delta^{\#4}_{0^{+}}{\dagger}$	0	$-\frac{1}{2\sqrt{2}\,a_0}$	$-\frac{1}{2\sqrt{2}\,a_0}$	$\frac{1}{2 a_0}$	0	0	0
$\mathcal{T}^{\#1}_{0^{+}}{\dagger}$	0	0	0	0	$\frac{4}{a_0 k^2}$	0	0
$\mathcal{T}^{\#2}_{0^{+}}{\dagger}$	0	0	0	0	0	0	0
$\Delta^{\#1}_{0^{-}}{\dagger}$	0	0	0	0	0	0	$-\frac{2}{a_0}$

	$\Delta^{\#1}_{2^{+}\alpha\beta}$	$\Delta^{\#2}_{2^{+}\alpha\beta}$	$\Delta^{\#3}_{2^{+}\alpha\beta}$	$\mathcal{T}^{\#1}_{2^{+}\alpha\beta}$	$\Delta^{\#1}_{2^{-}\alpha\beta\chi}$	$\Delta^{\#2}_{2^{-}\alpha\beta\chi}$
$\Delta^{\#1}_{2^{+}}{\dagger}^{\alpha\beta}$	$\frac{4}{a_0}$	0	0	0	0	0
$\Delta^{\#2}_{2^{+}}{\dagger}^{\alpha\beta}$	0	$-\frac{2}{a_0}$	0	0	0	0
$\Delta^{\#3}_{2^{+}}{\dagger}^{\alpha\beta}$	0	0	$\frac{4}{a_0}$	0	0	0
$\mathcal{T}^{\#1}_{2^{+}}{\dagger}^{\alpha\beta}$	0	0	0	$-\frac{8}{a_0 k^2}$	0	0
$\Delta^{\#1}_{2^{-}}{\dagger}^{\alpha\beta\chi}$	0	0	0	0	$\frac{4}{a_0}$	0
$\Delta^{\#2}_{2^{-}}{\dagger}^{\alpha\beta\chi}$	0	0	0	0	0	$\frac{4}{a_0}$

	$\Gamma^{\#1}_{0^{+}}$	$\Gamma^{\#2}_{0^{+}}$	$\Gamma^{\#3}_{0^{+}}$	$\Gamma^{\#4}_{0^{+}}$	$h^{\#1}_{0^{+}}$	$h^{\#2}_{0^{+}}$	$\Gamma^{\#1}_{0^{-}}$
$\Gamma^{\#1}_{0^{+}}{\dagger}$	$-\frac{a_0}{2}$	0	0	0	0	0	0
$\Gamma^{\#2}_{0^{+}}{\dagger}$	0	0	$\frac{a_0}{2}$	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
$\Gamma^{\#3}_{0^{+}}{\dagger}$	0	$\frac{a_0}{2}$	0	$-\frac{a_0}{2\sqrt{2}}$	0	0	0
$\Gamma^{\#4}_{0^{+}}{\dagger}$	0	$-\frac{a_0}{2\sqrt{2}}$	$-\frac{a_0}{2\sqrt{2}}$	$\frac{a_0}{2}$	0	0	0
$h^{\#1}_{0^{+}}{\dagger}$	0	0	0	0	$\frac{a_0 k^2}{4}$	0	0
$h^{\#2}_{0^{+}}{\dagger}$	0	0	0	0	0	0	0
$\Gamma^{\#1}_{0^{-}}{\dagger}$	0	0	0	0	0	0	$-\frac{a_0}{2}$

	$\Gamma^{\#1}_{2^{+}\alpha\beta}$	$\Gamma^{\#2}_{2^{+}\alpha\beta}$	$\Gamma^{\#3}_{2^{+}\alpha\beta}$	$h^{\#1}_{2^{+}\alpha\beta}$	$\Gamma^{\#1}_{2^{-}\alpha\beta\chi}$	$\Gamma^{\#2}_{2^{-}\alpha\beta\chi}$
$\Gamma^{\#1}_{2^{+}}{\dagger}^{\alpha\beta}$	$\frac{a_0}{4}$	0	0	0	0	0
$\Gamma^{\#2}_{2^{+}}{\dagger}^{\alpha\beta}$	0	$-\frac{a_0}{2}$	0	0	0	0
$\Gamma^{\#3}_{2^{+}}{\dagger}^{\alpha\beta}$	0	0	$\frac{a_0}{4}$	0	0	0
$h^{\#1}_{2^{+}}{\dagger}^{\alpha\beta}$	0	0	0	$-\frac{a_0 k^2}{8}$	0	0
$\Gamma^{\#1}_{2^{-}}{\dagger}^{\alpha\beta\chi}$	0	0	0	0	$\frac{a_0}{4}$	0
$\Gamma^{\#2}_{2^{-}}{\dagger}^{\alpha\beta\chi}$	0	0	0	0	0	$\frac{a_0}{4}$

Massive and massless spectra



Quadratic pole	
Pole residue:	$-\frac{1}{a_0}>0$
Polarisations:	2

(No massive particles)

Unitarity conditions

$a_0<0$