

## Wave operator and propagator

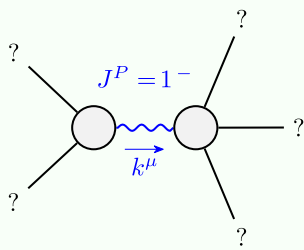
|  | $\sigma_{1^+}^{\#1} \alpha \beta$  | $\sigma_{1^+}^{\#2} \alpha \beta$  | $\tau_{1^+}^{\#1} \alpha \beta$   | $\sigma_{1^-}^{\#1} \alpha$   | $\sigma_{1^-}^{\#2} \alpha$  | $\tau_{1^-}^{\#1} \alpha$ | $\tau_{1^-}^{\#2} \alpha$   |
|--|--|--|---|---|--|---------------------------|---|
| $\sigma_{1^+}^{\#1} \uparrow \alpha \beta$ | $\frac{1}{\frac{3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)}{16(\beta_1+2\beta_3)}+(a_2+a_5)k^2}$  | $-\frac{2\sqrt{2}(3\alpha_0-4\beta_1+16\beta_3)}{(1+k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$            | $-\frac{2i\sqrt{2}(3\alpha_0-4\beta_1+16\beta_3)k}{(1+k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$           | 0   | 0  | 0                         | 0   |
| $\sigma_{1^+}^{\#2} \uparrow \alpha \beta$ | $-\frac{2\sqrt{2}(3\alpha_0-4\beta_1+16\beta_3)}{(1+k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$  | $\frac{6\alpha_0+8(\beta_1+8\beta_3+3(a_2+a_5)k^2)}{(1+k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$       | $\frac{2ik(3\alpha_0+4(\beta_1+8\beta_3+3(a_2+a_5)k^2))}{(1+k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$   | 0   | 0  | 0                         | 0   |
| $\tau_{1^+}^{\#1} \uparrow \alpha \beta$   | $\frac{2i\sqrt{2}(3\alpha_0-4\beta_1+16\beta_3)k}{(1+k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$ | $-\frac{2ik(3\alpha_0+4(\beta_1+8\beta_3+3(a_2+a_5)k^2))}{(1+k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$ | $-\frac{2k^2(3\alpha_0+4(\beta_1+8\beta_3+3(a_2+a_5)k^2))}{(1+k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+8\beta_3)+16(a_2+a_5)(\beta_1+2\beta_3)k^2)}$ | 0   | 0  | 0                         | 0   |
| $\sigma_{1^-}^{\#1} \uparrow \alpha$       | 0  | 0  | 0   | $\frac{1}{\frac{3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)}{8(2\beta_1+\beta_2)}+(a_4+a_5)k^2}$  | $\frac{2\sqrt{2}(3\alpha_0-4\beta_1+4\beta_2)}{(1+2k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$                      | 0                         | $\frac{4i(3\alpha_0-4\beta_1+4\beta_2)k}{(1+2k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$                           |
| $\sigma_{1^-}^{\#2} \uparrow \alpha$       | 0  | 0  | 0   | $\frac{2\sqrt{2}(3\alpha_0-4\beta_1+4\beta_2)}{(1+2k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$ | $\frac{6\alpha_0+8(\beta_1+2\beta_2+3(a_4+a_5)k^2)}{(1+2k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$               | 0                         | $\frac{2i\sqrt{2}k(3\alpha_0+4(\beta_1+2\beta_2+3(a_4+a_5)k^2))}{(1+2k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$ |
| $\tau_{1^-}^{\#1} \uparrow \alpha$         | 0  | 0  | 0   | 0   | 0  | 0                         | 0   |
| $\tau_{1^-}^{\#2} \uparrow \alpha$         | 0  | 0  | 0   | $-\frac{4i(3\alpha_0-4\beta_1+4\beta_2)k}{(1+2k^2)(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$      | $-\frac{2i\sqrt{2}k(3\alpha_0+4(\beta_1+2\beta_2+3(a_4+a_5)k^2))}{(1+2k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$ | 0                         | $\frac{4k^2(3\alpha_0+4(\beta_1+2\beta_2+3(a_4+a_5)k^2))}{(1+2k^2)^2(-3(\alpha_0-4\beta_1)(\alpha_0+2\beta_2)+8(a_4+a_5)(2\beta_1+\beta_2)k^2)}$        |

[illegible][illegible]

|  | $\omega_{1+\alpha\beta}^{\#1}$   | $\omega_{1+\alpha\beta}^{\#2}$                           | $f_{1+\alpha\beta}^{\#1}$                                      | $\omega_{1-\alpha}^{\#1}$  | $\omega_{1-\alpha}^{\#2}$                                | $f_{1-\alpha}^{\#1}$ | $f_{1-\alpha}^{\#2}$                                    |
|--|--|--|--|--|--|----------------------|---|
| $\omega_{1+}^{\#1} \uparrow \alpha\beta$ | $\frac{\alpha_0}{4} + \frac{1}{3} (\beta_1 + 8 \beta_3) + (\alpha_2 + \alpha_5) k^2$ | $\frac{3 \alpha_0 - 4 \beta_1 + 16 \beta_3}{6 \sqrt{2}}$ | $\frac{i (3 \alpha_0 - 4 \beta_1 + 16 \beta_3) k}{6 \sqrt{2}}$ | 0  | 0  | 0                    | 0   |
| $\omega_{1+}^{\#2} \uparrow \alpha\beta$ | $\frac{3 \alpha_0 - 4 \beta_1 + 16 \beta_3}{6 \sqrt{2}}$                             | $\frac{2}{3} (\beta_1 + 2 \beta_3)$                      | $\frac{2}{3} i (\beta_1 + 2 \beta_3) k$                        | 0  | 0  | 0                    | 0   |
| $f_{1+}^{\#1} \uparrow \alpha\beta$      | $-\frac{i (3 \alpha_0 - 4 \beta_1 + 16 \beta_3) k}{6 \sqrt{2}}$                      | $-\frac{2}{3} i (\beta_1 + 2 \beta_3) k$                 | $\frac{2}{3} (\beta_1 + 2 \beta_3) k^2$                        | 0  | 0  | 0                    | 0   |
| $\omega_{1+}^{\#1} \uparrow \alpha$      | 0  | 0  | 0  | $\frac{\alpha_0}{4} + \frac{1}{3} (\beta_1 + 2 \beta_2) + (\alpha_4 + \alpha_5) k^2$ | $-\frac{3 \alpha_0 - 4 \beta_1 + 4 \beta_2}{6 \sqrt{2}}$ | 0                    | $-\frac{1}{6} i (3 \alpha_0 - 4 \beta_1 + 4 \beta_2) k$ |
| $\omega_{1+}^{\#2} \uparrow \alpha$      | 0  | 0  | 0  | $-\frac{3 \alpha_0 - 4 \beta_1 + 4 \beta_2}{6 \sqrt{2}}$                             | $\frac{1}{3} (2 \beta_1 + \beta_2)$                      | 0                    | $\frac{1}{3} i \sqrt{2} (2 \beta_1 + \beta_2) k$        |
| $f_{1+}^{\#1} \uparrow \alpha$           | 0  | 0  | 0  | 0  | 0  | 0                    | 0   |
| $f_{1+}^{\#2} \uparrow \alpha$           | 0  | 0  | 0  | $\frac{1}{6} i (3 \alpha_0 - 4 \beta_1 + 4 \beta_2) k$                               | $-\frac{1}{3} i \sqrt{2} (2 \beta_1 + \beta_2) k$        | 0                    | $\frac{2}{3} (2 \beta_1 + \beta_2) k^2$                 |

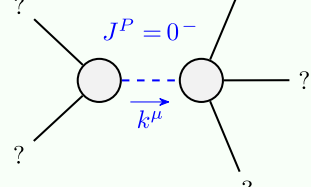
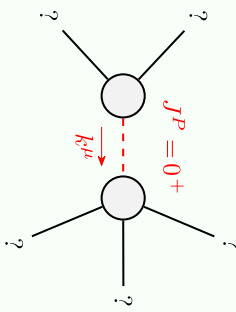
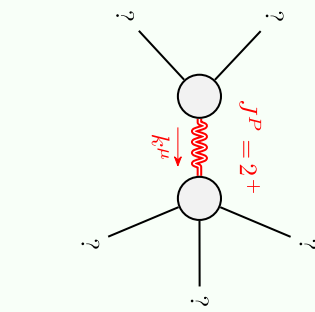
| Source constraints   | Fundamental fields  | Multiplicities |
|--|---|----------------|
| $\tau_0^{\#2} = 0$   | $\partial_\beta \partial_\alpha \tau^{\alpha\beta} = 0$   | 1              |
| $\tau_1^{\#2\alpha} + 2\,i\,k\,\sigma_1^{\#2\alpha} = 0$   | $\partial_\chi \partial_\beta \partial^\alpha \tau^{\beta\chi} = \partial_\chi \partial_\beta \partial^\alpha \tau^{\alpha\beta} + 2\,\partial_\delta \partial^\delta \partial_\chi \partial_\beta \sigma^{\alpha\beta\chi}$  | 3              |
| $\tau_1^{\#1\alpha} = 0$                                   | $\partial_\chi \partial_\beta \partial^\alpha \tau^{\beta\chi} = \partial_\chi \partial^\alpha \partial_\beta \tau^{\beta\alpha}$   | 3              |
| $\tau_1^{\#1\alpha} + i\,k\,\sigma_1^{\#2\alpha\beta} = 0$ | $\partial_\chi \partial^\alpha \tau^{\beta\chi} + \partial_\chi \partial^\beta \tau^{\alpha\chi} + \partial_\chi \partial^\alpha \tau^{\alpha\beta} +$ $2\,\partial_\delta \partial_\chi \partial^\alpha \sigma^{\beta\chi\delta} + 2\,\partial_\delta \partial^\delta \partial_\chi \sigma^{\alpha\beta\chi} =$ $\partial_\chi \partial^\alpha \tau^{\chi\beta} + \partial_\chi \partial^\beta \tau^{\alpha\chi} +$ $\partial_\chi \partial^\chi \tau^{\beta\alpha} + 2\,\partial_\delta \partial_\chi \partial^\beta \sigma^{\alpha\chi\delta}$ | 3              |
| Total constraints/gauge generators:                        |   | 10             |

A diagram showing two light-colored circles representing baryons. Each baryon has three external lines extending from it, each labeled with a question mark (?). A red wavy line connects the two baryons, labeled with  $J^P = 1+$  in red. Below the wavy line is a red arrow pointing to the right, labeled  $k^\mu$  in red.

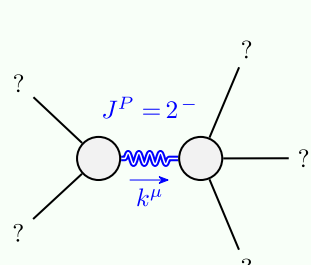


|                  |  |
|------------------|--|
| Massive particle |  |
| Pole residue:    | $\begin{aligned} & (3 (\alpha_0^2 (3 \alpha_2 + 3 \alpha_5 + 2 \beta_1 + 4 \beta_3) - \\ & 8 \alpha_0 (\beta_1^2 + \alpha_2 (\beta_1 - 4 \beta_3) + \alpha_5 (\beta_1 - 4 \beta_3) - 4 \beta_3^2) + \\ & 16 (-4 \beta_1 \beta_3 (\beta_1 + 2 \beta_3) + \alpha_2 (\beta_1^2 + 8 \beta_3^2) + \alpha_5 (\beta_1^2 + 8 \beta_3^2)))) / \\ & (2 (\alpha_2 + \alpha_5) (\beta_1 + 2 \beta_3) (3 \alpha_0^2 - 12 \alpha_0 (\beta_1 - 2 \beta_3) + \\ & 16 (\alpha_5 \beta_1 + 2 \alpha_5 \beta_3 - 6 \beta_1 \beta_3 + \alpha_2 (\beta_1 + 2 \beta_3)))) > 0 \end{aligned}$ |
| Polarisations:   | 3  |
| Square mass:     | $\frac{3 (\alpha_0 - 4 \beta_1) (\alpha_0 + 8 \beta_3)}{16 (\alpha_2 + \alpha_5) (\beta_1 + 2 \beta_3)} > 0$   |
| Spin:            | 1  |
| Parity:          | Even   |

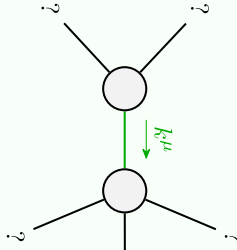
|                  |  |
|------------------|--|
| Massive particle |  |
| Pole residue:    | $-( (3 (\alpha_0^2 (3 \alpha_4 + 3 \alpha_5 + 4 \beta_1 + 2 \beta_2) + 4 \alpha_0 (-2 \alpha_4 \beta_1 - 2 \alpha_5 \beta_1 - 4 \beta_1^2 + 2 \alpha_4 \beta_2 + 2 \alpha_5 \beta_2 + \beta_2^2) + 8 (-2 \beta_1 \beta_2 (2 \beta_1 + \beta_2) + \alpha_4 (2 \beta_1^2 + \beta_2^2) + \alpha_5 (2 \beta_1^2 + \beta_2^2)))) / (2 (\alpha_4 + \alpha_5) (2 \beta_1 + \beta_2) (3 \alpha_0^2 + 6 \alpha_0 (-2 \beta_1 + \beta_2) + 4 (2 \alpha_5 \beta_1 + \alpha_5 \beta_2 - 6 \beta_1 \beta_2 + \alpha_4 (2 \beta_1 + \beta_2)))) ) > 0$ |
| Polarisations:   | 3  |
| Square mass:     | $\frac{3 (\alpha_0 - 4 \beta_1) (\alpha_0 + 2 \beta_2)}{8 (\alpha_4 + \alpha_5) (2 \beta_1 + \beta_2)} > 0$  |
| Spin:            | 1  |
| Parity:          | Odd  |



| Massive particle |   |
|------------------|---|
| Pole residue:    | $-\frac{1}{a_2+a_3} > 0$                    |
| Polarisations:   | 1   |
| Square mass:     | $-\frac{\alpha_0+8\beta_3}{2(a_2+a_3)} > 0$ |
| Spin:            | 0   |
| Parity:          | Odd   |



| Massive particle |                                       |
|------------------|---------------------------------------|
| Pole residue:    | $-\frac{1}{a_1+a_2} > 0$              |
| Polarisations:   | 5                                     |
| Square mass:     | $\frac{a_0-4\beta_1}{4(a_1+a_2)} > 0$ |
| Spin:            | 2                                     |
| Parity:          | Odd                                   |



| Quadratic pole |                     |
|----------------|---------------------|
| Pole residue:  | $\frac{1}{a_0} > 0$ |
| Polarisations: | 2                   |

(Unitarity is demonstrably impossible)