

# Particle spectrograph

## Wave operator and propagator

$$S = \int \int \int \int (h^{\alpha\beta} \tau_{\alpha\beta} + \beta \partial_\alpha h^{\alpha\beta} \partial_\beta h^{\alpha\beta} + \frac{1}{2} \alpha (\partial_\beta h^{\alpha\beta} \partial_\alpha h^{\alpha\beta} - 2 \partial_\beta h^{\alpha\beta} \partial_\alpha h^{\alpha\beta} - \partial_\alpha h^{\alpha\beta} \partial_\beta h^{\alpha\beta})) [t, x, y, z] dx dy dz dt$$

Propagator tables:

	$\begin{smallmatrix} \#1 \\ 0^+ h \end{smallmatrix}$	$\begin{smallmatrix} \#2 \\ 0^+ h \end{smallmatrix}$
$\begin{smallmatrix} \#1 \\ 0^+ h \end{smallmatrix}$	$\alpha k^2$	0
$\begin{smallmatrix} \#2 \\ 0^+ h \end{smallmatrix}$	0	$(-\alpha + \beta) k^2$

(No source constraints)

	$\begin{smallmatrix} \#1 \\ 0^+ \tau \end{smallmatrix}$	$\begin{smallmatrix} \#2 \\ 0^+ \tau \end{smallmatrix}$
$\begin{smallmatrix} \#1 \\ 0^+ \tau \end{smallmatrix}$	$\frac{1}{\alpha k^2}$	0
$\begin{smallmatrix} \#2 \\ 0^+ \tau \end{smallmatrix}$	0	$\frac{1}{(-\alpha + \beta) k^2}$

(No source constraints)

	$\begin{smallmatrix} \#1 \\ 1^- h_\alpha \end{smallmatrix}$
$\begin{smallmatrix} \#1 \\ 1^- h_\alpha \end{smallmatrix}$	$\frac{1}{2} (-\alpha + \beta) k^2$

(No source constraints)

	$\begin{smallmatrix} \#1 \\ 2^+ h_{\alpha\beta} \end{smallmatrix}$
$\begin{smallmatrix} \#1 \\ 2^+ h_{\alpha\beta} \end{smallmatrix}$	$\frac{1}{2} (-\alpha + \beta) k^2$

(No source constraints)

	$\begin{smallmatrix} \#1 \\ 2^+ \tau_{\alpha\beta} \end{smallmatrix}$
$\begin{smallmatrix} \#1 \\ 2^+ \tau_{\alpha\beta} \end{smallmatrix}$	$\frac{1}{2} (-\alpha + \beta) k^2$

(No source constraints)

## Massive and massless spectra

(No particles)

Quartic pole

Pole residue:  $0 < \frac{6\alpha + 3\beta + \sqrt{3} \sqrt{12\alpha^2 + 12\alpha\beta - 19\beta^2 + 64(\alpha\beta)^2}}{\alpha(\alpha\beta)} \&\& \frac{6\alpha + 3\beta + \sqrt{3} \sqrt{12\alpha^2 + 12\alpha\beta - 19\beta^2 + 64(\alpha\beta)^2}}{\alpha(\alpha\beta)} > 0$

Polarisations: 1

Quartic pole

Pole residue:  $0 < \frac{6\alpha + 3\beta + \sqrt{3} \sqrt{12\alpha^2 + 12\alpha\beta - 19\beta^2 + 64(\alpha\beta)^2}}{\alpha(\alpha\beta)} \&\& \frac{6\alpha + 3\beta + \sqrt{3} \sqrt{12\alpha^2 + 12\alpha\beta - 19\beta^2 + 64(\alpha\beta)^2}}{\alpha(\alpha\beta)} > 0$

Polarisations: 1

Massless particle

Pole residue:  $\frac{-2\alpha + \beta + \sqrt{20\alpha^2 - 36\alpha\beta - 17\beta^2}}{\alpha(\alpha\beta)} > 0$

Polarisations: 1

Massless particle

Pole residue:  $\frac{2\alpha\beta + \sqrt{20\alpha^2 - 36\alpha\beta - 17\beta^2}}{\alpha^2 - \alpha\beta} > 0$

Polarisations: 1

Hexic pole

Pole residue:  $0 < \frac{2\alpha + \beta}{\alpha^2 - \alpha\beta} \&\& \frac{2\alpha + \beta}{\alpha^2 - \alpha\beta} > 0$

Polarisations: 1

Quartic pole

Pole residue:  $0 < \frac{\beta}{\alpha^2 - \alpha\beta} \&\& \frac{\beta}{\alpha^2 - \alpha\beta} > 0$

Polarisations: 2

Massless particle

Pole residue:  $\frac{1}{\alpha} + \frac{1}{-\alpha + \beta} > 0$

Polarisations: 2

Massless particle

Pole residue:  $\frac{1}{\alpha} + \frac{5}{\alpha - \beta} > 0$

Polarisations: 1

Massless particle

Pole residue:  $\frac{1}{\alpha} + \frac{1}{-\alpha + \beta} > 0$

Polarisations: 2

## Unitarity conditions