

Lagrangian density

$$\begin{aligned}
 & \omega^{\alpha\beta\chi} \sigma_{\alpha\beta\chi} - \frac{1}{2} r_3 \partial_i \omega^{\kappa\lambda} \partial' \omega_{\lambda}^{\alpha} \partial' \omega_{\lambda}^{\kappa} - r_5 \partial_i \omega^{\kappa\lambda} \partial' \omega_{\lambda}^{\alpha} + \frac{2}{3} r_2 \partial^{\beta} \omega^{\theta\alpha} \partial_{\theta} \omega_{\alpha\beta} - \\
 & \frac{1}{3} r_2 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \partial_{\kappa} \omega^{\alpha\beta\theta} - \frac{2}{3} r_2 \partial_{\theta} \omega_{\alpha\beta}^{\kappa} \partial_{\kappa} \omega^{\theta\alpha\beta} + \frac{1}{2} r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\theta\kappa\lambda} - \\
 & r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\theta\kappa\lambda} - \frac{1}{2} r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda} + r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda} - \\
 & \frac{1}{2} r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\kappa\lambda\theta} - r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial_{\theta} \omega^{\kappa\lambda\theta} + r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda\theta} + \\
 & 2 r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial_{\kappa} \omega^{\kappa\lambda\theta} + \frac{1}{3} r_2 \partial_{\kappa} \omega^{\alpha\beta\theta} \partial^{\kappa} \omega_{\alpha\beta\theta} + \frac{2}{3} r_2 \partial_{\kappa} \omega^{\theta\alpha\beta} \partial^{\kappa} \omega_{\alpha\beta\theta} - \\
 & \frac{2}{3} r_2 \partial^{\beta} \omega_{\lambda}^{\alpha\lambda} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} + \frac{2}{3} r_2 \partial^{\beta} \omega_{\lambda}^{\lambda\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} - 4 r_3 \partial^{\beta} \omega_{\lambda}^{\lambda\alpha} \partial_{\lambda} \omega_{\alpha\beta}^{\prime} - \\
 & \frac{1}{2} r_3 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\theta}^{\theta\kappa} + r_5 \partial_{\alpha} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\theta}^{\theta\kappa} + \frac{1}{2} r_3 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\alpha}^{\theta\kappa} - r_5 \partial_{\theta} \omega_{\lambda}^{\alpha} \partial^{\lambda} \omega_{\alpha}^{\theta\kappa}
 \end{aligned}$$

| | | |
|-----------------------------|---------------------|---------------------|
| | $\omega_{0+}^{\#1}$ | $\omega_{0-}^{\#1}$ |
| $\omega_{0+}^{\#1} \dagger$ | 0 | 0 |
| $\omega_{0-}^{\#1} \dagger$ | 0 | $k^2 r_2$ |

| | | |
|-----------------------------|---------------------|---------------------|
| | $\sigma_{0+}^{\#1}$ | $\sigma_{0-}^{\#1}$ |
| $\sigma_{0+}^{\#1} \dagger$ | 0 | 0 |
| $\sigma_{0-}^{\#1} \dagger$ | 0 | $\frac{1}{k^2 r_2}$ |

| | | | | |
|---|---------------------------------|---------------------------------|------------------------------|----------------------------|
| | $\sigma_{1+}^{\#1} \alpha\beta$ | $\sigma_{1+}^{\#2} \alpha\beta$ | $\sigma_{1-}^{\#1} \alpha$ | $\sigma_{1-}^{\#2} \alpha$ |
| $\sigma_{1+}^{\#1} \dagger \alpha\beta$ | $\frac{1}{k^2 (2r_3 + r_5)}$ | 0 | 0 | 0 |
| $\sigma_{1+}^{\#2} \dagger \alpha\beta$ | 0 | 0 | 0 | 0 |
| $\sigma_{1-}^{\#1} \dagger \alpha$ | 0 | 0 | $\frac{2}{k^2 (r_3 + 2r_5)}$ | 0 |
| $\sigma_{1-}^{\#2} \dagger \alpha$ | 0 | 0 | 0 | 0 |

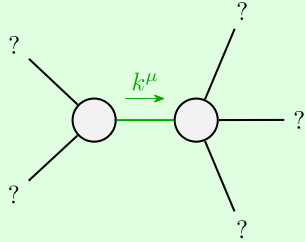
| | | | | |
|---|---------------------------------|---------------------------------|--------------------------------|----------------------------|
| | $\omega_{1+}^{\#1} \alpha\beta$ | $\omega_{1+}^{\#2} \alpha\beta$ | $\omega_{1-}^{\#1} \alpha$ | $\omega_{1-}^{\#2} \alpha$ |
| $\omega_{1+}^{\#1} \dagger \alpha\beta$ | $k^2 (2r_3 + r_5)$ | 0 | 0 | 0 |
| $\omega_{1+}^{\#2} \dagger \alpha\beta$ | 0 | 0 | 0 | 0 |
| $\omega_{1-}^{\#1} \dagger \alpha$ | 0 | 0 | $\frac{1}{2} k^2 (r_3 + 2r_5)$ | 0 |
| $\omega_{1-}^{\#2} \dagger \alpha$ | 0 | 0 | 0 | 0 |

| | | |
|---|---------------------------------|-------------------------------------|
| | $\sigma_{2+}^{\#1} \alpha\beta$ | $\sigma_{2-}^{\#1} \alpha\beta\chi$ |
| $\sigma_{2+}^{\#1} \dagger \alpha\beta$ | $-\frac{2}{3k^2 r_3}$ | 0 |
| $\sigma_{2-}^{\#1} \dagger \alpha\beta\chi$ | 0 | 0 |

| | | |
|---|---------------------------------|-------------------------------------|
| | $\omega_{2+}^{\#1} \alpha\beta$ | $\omega_{2-}^{\#1} \alpha\beta\chi$ |
| $\omega_{2+}^{\#1} \dagger \alpha\beta$ | $-\frac{3k^2 r_3}{2}$ | 0 |
| $\omega_{2-}^{\#1} \dagger \alpha\beta\chi$ | 0 | 0 |

Source constraints

| SO(3) irreps | # |
|---|----|
| $\sigma_{0+}^{\#1} == 0$ | 1 |
| $\sigma_{1-}^{\#2\alpha} == 0$ | 3 |
| $\sigma_{1+}^{\#2\alpha\beta} == 0$ | 3 |
| $\sigma_{2-}^{\#1\alpha\beta\chi} == 0$ | 5 |
| Total #: | 12 |



Quadratic pole

| | |
|---------------|--|
| Pole residue: | $-\frac{1}{r_3 (2r_3 + r_5) (r_3 + 2r_5)} > 0$ |
|---------------|--|

| | |
|----------------|---|
| Polarisations: | 2 |
|----------------|---|

(No massive particles)

Unitarity conditions

$$r_3 < 0 \&\& (r_5 < -\frac{r_3}{2} \parallel r_5 > -2r_3) \parallel r_3 > 0 \&\& -2r_3 < r_5 < -\frac{r_3}{2}$$