

|                          | $\omega_{0}^{\sharp 1}$                                    | $f_{0}^{#1}$                              | $f_{0+}^{#2}$ | $\omega_0^{\#1}$  |
|--------------------------|--|---|---------------|---|
| $\omega_{0}^{\#1}$ †     | $\frac{\alpha_0}{2} + \beta_2 + (\alpha_4 + \alpha_6) k^2$ | $-\frac{i(\alpha_0+2\beta_2)k}{\sqrt{2}}$ | 0             | 0   |
| $f_{0}^{#1}$ †           | $\frac{i(\alpha_0+2\beta_2)k}{\sqrt{2}}$                   | $2 \beta_2 k^2$                           | 0             | 0   |
| $f_{0}^{#2} \dagger$     | 0  | 0   | 0             | 0   |
| $\omega_{0^{-}}^{\#1}$ † | 0  | 0   | 0             | $\frac{\alpha_0}{2} + 4\beta_3 + (\alpha_2 + \alpha_3) k^2$ |

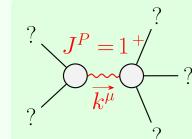
|   | $\omega_{2}^{\#1}{}_{\alpha\beta}$                   | $f_{2+\alpha\beta}^{\#1}$                 | $\omega_{2}^{\sharp 1}{}_{lphaeta\chi}$              |
|---|--|---|--|
| $\omega_{2^{+}}^{\sharp 1}\dagger^{lphaeta}$    | $-\frac{\alpha_0}{4}+\beta_1+(\alpha_1+\alpha_4)k^2$ | $\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$ | 0  |
| $f_{2+}^{\#1}\dagger^{\alpha\beta}$             | $-\frac{i(\alpha_0-4\beta_1)k}{2\sqrt{2}}$           | $2 \beta_1 k^2$                           | 0  |
| $\omega_2^{\sharp 1} \dagger^{\alpha\beta\chi}$ | 0  | 0   | $-\frac{\alpha_0}{4}+\beta_1+(\alpha_1+\alpha_2)k^2$ |

| Total #: | $\tau_{1+}^{\#1}{}^{\alpha\beta} + ik \sigma_{1+}^{\#2}{}^{\alpha\beta} == 0$ | $\tau_{1}^{\#1\alpha} == 0$ | $\tau_{1}^{\#2\alpha} + 2  i  k  \sigma_{1}^{\#2\alpha} == 0$ | $\tau_{0+}^{\#2} == 0$ | SO(3) irreps | Source constraints |
|----------|---|-----------------------------|---|------------------------|--------------|--------------------|
| 10       | 3   | 3                           | 3   | 1                      | #            |                    |

| Laglaniyani delisity  1-2 αο ω <sub>αχβ</sub> ω <sup>αβχ</sup> - 2 αο ω <sup>αβ</sup> ω <sub>δ</sub> ω <sup>χδ</sup> + 3 β1 ω <sup>αβ</sup> ω <sup>χδ</sup> α ω <sup>χδ</sup> α + 3 β2 ω <sup>αβ</sup> ω ω <sup>χδ</sup> α α α α ω <sup>χδ</sup> α ω <sup>χδ</sup> α ω <sup>χδ</sup> α α α α ω <sup>χδ</sup> α α α α α ω <sup>χδ</sup> α α α α α α α α α α α α α α α α α α α |
|--|
|--|

|  | $\omega_{1^{+}lphaeta}^{\sharp 1}$   | $\omega_{1^{+}lphaeta}^{\#2}$                       | $f_{1}^{\#1}{}_{\alpha\beta}$                        | $\omega_{1}^{\sharp 1}{}_{lpha}$   | $\omega_1^{\#2}{}_{lpha}$                                | $f_{1-\alpha}^{\#1}$ | $f_{1}^{#2}$ $\alpha$                                       |
|--|--|---|--|--|--|----------------------|---|
| $\omega_{1}^{\#1}\dagger^{lphaeta}$      | $\frac{\alpha_0}{4} + \frac{1}{3} (\beta_1 + 8 \beta_3) + (\alpha_2 + \alpha_5) k^2$ | $\frac{3\alpha_0-4\beta_1+16\beta_3}{6\sqrt{2}}$    | $\frac{i(3\alpha_0-4\beta_1+16\beta_3)k}{6\sqrt{2}}$ | 0  | 0  | 0                    | 0   |
| $\omega_{1}^{\#2} \dagger^{\alpha\beta}$ | $\frac{3 \alpha_0 - 4 \beta_1 + 16 \beta_3}{6 \sqrt{2}}$                             | $\frac{2}{3}\left(\beta_1+2\beta_3\right)$          | $\frac{2}{3}i(\beta_1+2\beta_3)k$                    | 0  | 0  | 0                    | 0   |
| $f_1^{#1} \dagger^{\alpha\beta}$         | $-\frac{i(3\alpha_0-4\beta_1+16\beta_3)k}{6\sqrt{2}}$                                | $-\frac{2}{3}\bar{i}\left(\beta_1+2\beta_3\right)k$ | $\frac{2}{3}(\beta_1 + 2\beta_3)k^2$                 | 0  | 0  | 0                    | 0   |
| $\omega_1^{\#_1} \dagger^{\alpha}$       | 0  | 0   | 0  | $\frac{\alpha_0}{4} + \frac{1}{3} (\beta_1 + 2 \beta_2) + (\alpha_4 + \alpha_5) k^2$ | $-\frac{3 \alpha_0 - 4 \beta_1 + 4 \beta_2}{6 \sqrt{2}}$ | 0                    | $-\frac{1}{6}i(3\alpha_0-4\beta_1+4\beta_2)k$               |
| $\omega_{1}^{#2} + \alpha$               | 0  | 0   | 0  | $-\frac{3 \alpha_0 - 4 \beta_1 + 4 \beta_2}{6 \sqrt{2}}$                             | $\frac{1}{3}\left(2\beta_1+\beta_2\right)$               | 0                    | $\frac{1}{3}  \bar{l}  \sqrt{2}  (2  \beta_1 + \beta_2)  k$ |
| $f_{1}^{#1} \dagger^{\alpha}$            | 0  | 0   | 0  | 0  | 0  | 0                    | 0   |
| $f_1^{#2} \dagger^{\alpha}$              | 0  | 0   | 0  | $\frac{1}{6}$ i (3 $\alpha_0$ - 4 $\beta_1$ + 4 $\beta_2$ ) k                        | $-\frac{1}{3}i\sqrt{2}(2\beta_1+\beta_2)k$               | 0                    | $\frac{2}{3} (2 \beta_1 + \beta_2) k^2$                     |

|                      | $\sigma_{0}^{\sharp 1}$  | $	au_{0}^{\#1}$  | $\tau_{0}^{\#2}$ | $\sigma_0^{\sharp 1}$                         |
|----------------------|--|--|------------------|---|
| $\sigma_{0}^{\#1}$ † | $-\frac{4 \beta_2}{{\alpha_0}^2 + 2 \alpha_0 \beta_2 - 4 (\alpha_4 + \alpha_6) \beta_2 k^2}$       | $\frac{i\sqrt{2}(\alpha_0+2\beta_2)}{-\alpha_0(\alpha_0+2\beta_2)k+4(\alpha_4+\alpha_6)\beta_2k^3}$  | 0                | 0   |
| $	au_{0^{+}}^{#1}$ † | $\frac{i\sqrt{2}(\alpha_0+2\beta_2)}{\alpha_0(\alpha_0+2\beta_2)k-4(\alpha_4+\alpha_6)\beta_2k^3}$ | $\frac{\frac{\alpha_0}{2} + \beta_2 + (\alpha_4 + \alpha_6) k^2}{\frac{1}{2} \alpha_0 (\alpha_0 + 2 \beta_2) k^2 + 2 (\alpha_4 + \alpha_6) \beta_2 k^4}$ | 0                | 0   |
| $\tau_{0}^{\#2}$ †   | 0  | 0  | 0                | 0   |
| $\sigma_{0}^{#1}$ †  | 0  | 0  | 0                | $\frac{2}{(x_0 + 8)(x_0 + 2)(x_0 + x_0) k^2}$ |



 $\frac{\frac{4}{3}}{\beta_1} \beta_1 \partial^{\chi} f_{\zeta}^{\beta} \partial^{\zeta} f_{\chi\beta} - \frac{2}{3} \beta_3 \partial^{\chi} f_{\zeta}^{\beta} \partial^{\zeta} f_{\chi\beta} +$   $\frac{2}{3} \beta_1 \partial^{\chi} f_{\zeta\delta} \partial^{\zeta} f_{\chi}^{\delta} + \frac{2}{3} \beta_3 \partial^{\chi} f_{\zeta\delta} \partial^{\zeta} f_{\chi}^{\delta}$ 

 $\chi \partial_{\zeta} \omega_{\delta}^{\zeta}{}_{\beta} + \alpha_{5} \partial^{\delta} \omega^{\beta \chi}{}_{\chi} \partial_{\zeta} \omega_{\delta}^{\zeta}{}_{\beta}$ 

## Massive particle

| Pole residue:  | $(3 (\alpha_0^2 (3 \alpha_2 + 3 \alpha_5 + 2 \beta_1 + 4 \beta_3) - 8 \alpha_0 (\beta_1^2 + \alpha_2 (\beta_1 - 4 \beta_3) + \alpha_5 (\beta_1 - 4 \beta_3) - 4 \beta_3^2) + 16 (-4 \beta_1 \beta_3 (\beta_1 + 2 \beta_3) + \alpha_2 (\beta_1^2 + 8 \beta_3^2) + \alpha_5 (\beta_1^2 + 8 \beta_3^2)))))/$ |
|----------------|---|
|                | $8 \alpha_0 (\beta_1^2 + \alpha_2 (\beta_1 - 4 \beta_3) + \alpha_5 (\beta_1 - 4 \beta_3) - 4 \beta_3^2) +$  |
|                | $16(-4\beta_1\beta_3(\beta_1+2\beta_3)+\alpha_2(\beta_1^2+8\beta_3^2)+\alpha_5(\beta_1^2+8\beta_3^2))))/$   |
|                | $(2(\alpha_2 + \alpha_5)(\beta_1 + 2\beta_3)(3\alpha_0^2 - 12\alpha_0(\beta_1 - 2\beta_3) +$  |
|                | $16 (\alpha_5 \beta_1 + 2 \alpha_5 \beta_3 - 6 \beta_1 \beta_3 + \alpha_2 (\beta_1 + 2 \beta_3)))) > 0$   |
| Polarisations: | 3   |

| Square mass: | $\frac{\frac{3(\alpha_0 - 4\beta_1)(\alpha_0 + 8\beta_3)}{16(\alpha_2 + \alpha_5)(\beta_1 + 2\beta_3)}}{16(\alpha_2 + \alpha_5)(\beta_1 + 2\beta_3)} > 0$ |
|--------------|---|
| Spin:        | 1   |
| Parity:      | Even  |

## Massive particle

Parity:

Odd

| Pole residue:  | $\begin{aligned} &-((3(\alpha_0^2(3\alpha_4 + 3\alpha_5 + 4\beta_1 + 2\beta_2) + \\ &4\alpha_0(-2\alpha_4\beta_1 - 2\alpha_5\beta_1 - 4\beta_1^2 + 2\alpha_4\beta_2 + 2\alpha_5\beta_2 + \beta_2^2) + \\ &8(-2\beta_1\beta_2(2\beta_1 + \beta_2) + \alpha_4(2\beta_1^2 + \beta_2^2) + \alpha_5(2\beta_1^2 + \beta_2^2))))/\\ &(2(\alpha_4 + \alpha_5)(2\beta_1 + \beta_2)(3\alpha_0^2 + 6\alpha_0(-2\beta_1 + \beta_2) + \\ &4(2\alpha_5\beta_1 + \alpha_5\beta_2 - 6\beta_1\beta_2 + \alpha_4(2\beta_1 + \beta_2))))) > 0 \end{aligned}$ |
|----------------|---|
| Polarisations: | 3   |
| Square mass:   | $\frac{\frac{3(\alpha_0 - 4\beta_1)(\alpha_0 + 2\beta_2)}{8(\alpha_4 + \alpha_5)(2\beta_1 + \beta_2)}}{ 8(\alpha_4 + \alpha_5)(2\beta_1 + \beta_2)} > 0$  |
| Coin           |   |

|         |       |   | 1                | +6   |                  |
|---------|-------|---|------------------|--|------------------|
|         | ·~)´  |   |                  | `.~  |                  |
| Parity: | Spin: | Square mass:  | Polarisations: 5 | Pole residue:  | Massive particle |
| Even    | 2     | $\frac{\alpha_0 (\alpha_0 - 4\beta_1)}{16 (\alpha_1 + \alpha_4) \beta_1} > 0$ | 5                | $-\frac{2}{\alpha_0} + \frac{\alpha_1 + \alpha_4 + 2\beta_1}{2\alpha_1\beta_1 + 2\alpha_4\beta_1} > 0$ | e                |

|         | .~)   |  |                             | ±   |                  |
|---------|-------|--|-----------------------------|---|------------------|
| Parity: | Spin: | Square mass:   | <sub>2</sub> Polarisations: | Pole residue:   | Massive particle |
| Even    | 0     | $\frac{\alpha_0 (\alpha_0 + 2\beta_2)}{4(\alpha_4 + \alpha_6)\beta_2} > 0$ | 1                           | $\frac{1}{\alpha_0} + \frac{\alpha_4 + \alpha_6 + 2\beta_2}{2\alpha_4\beta_2 + 2\alpha_6\beta_2}$ | le               |

|         | .~)   | $\frac{k^{\mu}}{k^{\mu}}$                           | 3              | $\frac{1}{5}$                        |                  |  |
|---------|-------|---|----------------|--------------------------------------|------------------|--|
| Parity: | Spin: | Square mass:  | Polarisations: | Pole residue:                        | Massive particle |  |
| Odd     | 0     | $-\frac{\alpha_0+8\beta_3}{2(\alpha_2+\alpha_3)}>0$ | 1              | $-\frac{1}{\alpha_2 + \alpha_3} > 0$ | e                |  |

Unitarity conditions

| Massive particle  Pole residue: $-\frac{1}{\alpha_2 + \alpha_3} > 0$ Polarisations: 1 | ? Massive Pole resi               |
|---|-----------------------------------|
| 1<br>1  | Massive Pole resi                 |
| 1<br>1<br>1   | Massive Pole resi                 |
| 1<br>1<br>1   | Massive Pole resi                 |
| 1<br>1  | Massive<br>Pole resi<br>Polarisat |
| 1<br>1<br>1   | par<br>due                        |
| $\begin{vmatrix} \alpha_2 + c \end{vmatrix}$  | S:   S:   E:                      |
|   | $\frac{1}{\alpha_2 + \epsilon}$   |

(Unitarity is demonstrably impossible)

|         | .~    |  |                |                                      |                  |
|---------|-------|--|----------------|--------------------------------------|------------------|
| Parity: | Spin: | Square mass:   | Polarisations: | Pole residue:                        | Massive particle |
| Odd     | 2     | $\frac{\alpha_0 - 4\beta_1}{4(\alpha_1 + \alpha_2)} > 0$ | 5              | $-\frac{1}{\alpha_1 + \alpha_2} > 0$ | е                |
|         |       |  |                |                                      |                  |

| .~)               |                      | $\cdot$        |
|-------------------|----------------------|----------------|
|                   | $\searrow$           |                |
|                   | $\bigvee_{i}$        | _              |
|                   |                      | 7              |
|                   | $\langle \rangle$    | _              |
| .~/               |                      | \·~            |
|                   | - ?                  |                |
| Ро                | ? Pole residue:      | Q              |
| lari              | le r                 | adı            |
| sat               | esi                  | rati           |
| ion               | du                   | C p            |
| Polarisations:  2 | Ω                    | Quadratic pole |
| 2                 | $\frac{1}{\alpha_0}$ | ,,,            |
|                   | 0 > 0                |                |
|                   | 0                    |                |

 $\sigma_{2}^{\#1} \alpha \beta \chi$ 

0