

Particle spectrograph

Wave operator and propagator

| $\sigma_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{1+}^{\#2} \dagger^{\alpha\beta}$ | $\tau_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{1-}^{\#1} \dagger^{\alpha}$ | $\sigma_{1-}^{\#2} \dagger^{\alpha}$ | $\tau_{1-}^{\#1} \dagger^{\alpha}$ | $\tau_{1-}^{\#2} \dagger^{\alpha}$ |
|---|---|---|--------------------------------------|---|------------------------------------|--|
| 0 | $-\frac{\sqrt{2}}{t_1+k^2}t_1$ | $-\frac{i\sqrt{2}k}{t_1+k^2}t_1$ | 0 | 0 | 0 | 0 |
| $-\frac{\sqrt{2}}{t_1+k^2}t_1$ | $-\frac{2k^2(2r_1+r_5)+t_1}{(1+k^2)^2}t_1^2$ | $\frac{-2ik^3(2r_1+r_5)+ikt_1}{(1+k^2)^2}t_1^2$ | 0 | 0 | 0 | 0 |
| $\frac{i\sqrt{2}k}{t_1+k^2}t_1$ | $\frac{i(2k^3(2r_1+r_5)-kt_1)}{(1+k^2)^2}t_1^2$ | $\frac{-2k^4(2r_1+r_5)+k^2t_1}{(1+k^2)^2}t_1^2$ | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $\frac{1}{k^2(r_1+r_5)}$ | $-\frac{1}{\sqrt{2}(k^2+2k^4)(r_1+r_5)}$ | 0 | $-\frac{i}{k(1+2k^2)(r_1+r_5)}$ |
| 0 | 0 | 0 | 0 | $-\frac{1}{\sqrt{2}(k^2+2k^4)(r_1+r_5)}$ | 0 | $\frac{i(6k^2(r_1+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(r_1+r_5)t_1}$ |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $\frac{i}{k(1+2k^2)(r_1+r_5)}$ | $-\frac{i(6k^2(r_1+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(r_1+r_5)t_1}$ | 0 | $-\frac{6k^2(r_1+r_5)+t_1}{(1+2k^2)^2(r_1+r_5)t_1}$ |

| $\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ |
|---|---|---|
| $\sigma_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 |
| $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\tau_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 |
| $\sigma_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | $\frac{2}{2k^2r_1+t_1}$ |

| $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | $f_{2+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ |
|---|--------------------------------------|---|
| $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | $f_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 |
| $\omega_{2+}^{\#1} \dagger^{\alpha\beta}$ | $f_{2+}^{\#1} \dagger^{\alpha\beta}$ | 0 |
| $\omega_{2-}^{\#1} \dagger^{\alpha\beta\chi}$ | 0 | $k^2r_1+\frac{t_1}{2}$ |

| Source constraints/gauge generators | |
|---|----------------|
| SO(3) irreps | Multiplicities |
| $\sigma_{0+}^{\#1} == 0$ | 1 |
| $\tau_{0+}^{\#1} == 0$ | 1 |
| $\tau_{0+}^{\#2} == 0$ | 1 |
| $\tau_{1-}^{\#2\alpha} + 2ik\sigma_{1-}^{\#2\alpha} == 0$ | 3 |
| $\tau_{1-}^{\#1\alpha} == 0$ | 3 |
| $\tau_{1+}^{\#1\alpha\beta} + ik\sigma_{1+}^{\#2\alpha\beta} == 0$ | 3 |
| $\tau_{2+}^{\#1\alpha\beta} - 2ik\sigma_{2+}^{\#1\alpha\beta} == 0$ | 5 |
| Total constraints: | 17 |

Quadratic (free) action

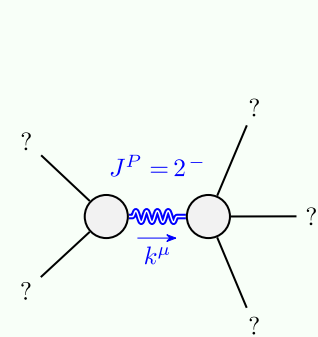
$$S_F == \iiint (\frac{1}{6}(-2t_1\omega_{\kappa\alpha}^{\alpha i}\omega_{\kappa\alpha}^{\kappa}-6t_1\omega_{\kappa\lambda}^{\kappa}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime}+6f^{\alpha\beta}\tau_{\alpha\beta}+6\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}-6r_5\partial_{\lambda}\omega^{\kappa\lambda}_{\kappa}\partial^{\kappa}f_{\alpha\lambda}+\partial^{\prime}\omega_{\lambda}^{\alpha}-4r_1\partial^{\beta}\omega_{\kappa}^{\theta\alpha}\partial_{\theta}\omega_{\alpha\beta}^{\kappa}-4r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\alpha\beta\theta}+4r_1\partial_{\theta}\omega_{\alpha\beta}^{\kappa}\partial_{\kappa}\omega^{\theta\alpha\beta}-6r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+6r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-6r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}+12r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-3t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}^{\theta}-3t_1\partial^{\alpha}f_{\kappa\theta}\partial^{\kappa}f_{\alpha}^{\theta}-3t_1\partial^{\alpha}f_{\lambda}^{\theta}\partial^{\kappa}f_{\alpha}^{\lambda}-3t_1\partial^{\alpha}f_{\lambda}^{\theta}\partial^{\kappa}f_{\alpha}^{\lambda}+2t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\prime}+2t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}+4t_1\partial^{\alpha}f_{\kappa\alpha}\partial^{\kappa}f_{\lambda}^{\prime}-2t_1\partial_{\kappa}f_{\lambda}^{\prime}\partial^{\kappa}f_{\lambda}^{\prime}+12t_1\omega_{\kappa\theta}\partial^{\kappa}f_{\lambda}^{\theta}-2t_1\omega_{\kappa\alpha}^{\alpha}\partial^{\kappa}f_{\lambda}^{\prime}-2t_1\omega_{\kappa\lambda}^{\lambda}\partial^{\kappa}f_{\lambda}^{\prime}+3t_1\partial^{\alpha}f_{\lambda}^{\theta}\partial^{\kappa}f_{\alpha}^{\lambda}+3t_1\partial_{\kappa}f_{\lambda}^{\theta}\partial^{\kappa}f_{\alpha}^{\lambda}-2t_1\partial^{\alpha}f_{\lambda}^{\theta}\partial^{\kappa}f_{\alpha}^{\lambda}+4r_1\partial_{\kappa}\omega^{\theta\alpha\beta}\partial^{\kappa}\omega_{\alpha\beta\theta}+4r_1\partial_{\theta}\omega_{\lambda}^{\alpha\lambda}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}-16r_1\partial^{\beta}\omega_{\lambda}^{\alpha}\partial_{\lambda}\omega_{\alpha\beta}^{\prime}+6r_5\partial_{\alpha}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\theta}^{\theta\kappa}-6r_5\partial_{\theta}\omega_{\lambda}^{\alpha}\partial^{\lambda}\omega_{\alpha}^{\theta\kappa})) [t, x, y, z] dz dy dx dt$$

| $\sigma_{0+}^{\#1} \dagger$ | $\tau_{0+}^{\#1} \dagger$ | $\tau_{0+}^{\#2} \dagger$ | $\sigma_{0-}^{\#1} \dagger$ |
|-----------------------------|---------------------------|---------------------------|-----------------------------|
| 0 | 0 | 0 | $\frac{1}{-t_1}$ |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

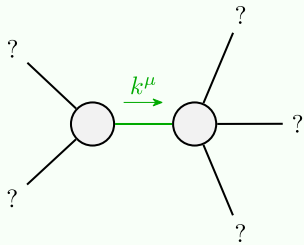
| $\omega_{0+}^{\#1} \dagger$ | $f_{0+}^{\#1} \dagger$ | $f_{0+}^{\#2} \dagger$ | $\omega_{0-}^{\#1} \dagger$ |
|-----------------------------|------------------------|------------------------|-----------------------------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | $-t_1$ |

| | $\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1+}^{\#2} \dagger^{\alpha\beta}$ | $f_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\omega_{1-}^{\#1} \dagger^{\alpha}$ | $\omega_{1-}^{\#2} \dagger^{\alpha}$ | $f_{1-}^{\#1} \dagger^{\alpha}$ | $f_{1-}^{\#2} \dagger^{\alpha}$ |
|---|---|---|--------------------------------------|--------------------------------------|--------------------------------------|---------------------------------|---------------------------------|
| $\omega_{1+}^{\#1} \dagger^{\alpha\beta}$ | $k^2(2r_1+r_5)-\frac{t_1}{2}$ | $-\frac{t_1}{\sqrt{2}}$ | $-\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 |
| $\omega_{1+}^{\#2} \dagger^{\alpha\beta}$ | $-\frac{t_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1+}^{\#1} \dagger^{\alpha\beta}$ | $\frac{ikt_1}{\sqrt{2}}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| $\omega_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | $k^2(r_1+r_5)+\frac{t_1}{6}$ | $\frac{t_1}{3\sqrt{2}}$ | 0 | $\frac{ikt_1}{3}$ |
| $\omega_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | $\frac{t_1}{3\sqrt{2}}$ | $\frac{t_1}{3}$ | 0 | $\frac{1}{3}i\sqrt{2}kt_1$ |
| $f_{1-}^{\#1} \dagger^{\alpha}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $f_{1-}^{\#2} \dagger^{\alpha}$ | 0 | 0 | 0 | $-\frac{1}{3}ikt_1$ | $-\frac{1}{3}i\sqrt{2}kt_1$ | 0 | $\frac{2k^2t_1}{3}$ |

Massive and massless spectra



| Massive particle | |
|------------------|-------------------------|
| Pole residue: | $-\frac{1}{r_1} > 0$ |
| Polarisations: | 5 |
| Square mass: | $-\frac{t_1}{2r_1} > 0$ |
| Spin: | 2 |
| Parity: | Odd |



| Quadratic pole | |
|----------------|---------------------------------|
| Pole residue: | $-\frac{1}{(r_1+r_5)t_1^2} > 0$ |
| Polarisations: | 2 |

Unitarity conditions

$$r_1 < 0 \ \&\& \ r_5 < -r_1 \ \&\& \ t_1 > 0$$