

$\omega_{1+}^{\#1} + \alpha\beta$	$\omega_{1+}^{\#2} + \alpha\beta$	$f_{1+}^{\#1} + \alpha\beta$	$\omega_{1-}^{\#1} - \alpha$	$\omega_{1-}^{\#2} - \alpha$	$f_{1-}^{\#1} - \alpha$	$f_{1-}^{\#2} - \alpha$
$\omega_{1+}^{\#1} + \alpha\beta$	$k^2(2r_3+r_5) - \frac{t_1}{2}$	$-\frac{t_1}{\sqrt{2}}$	$-\frac{ikt_1}{\sqrt{2}}$	0	0	0
$\omega_{1+}^{\#2} + \alpha\beta$	$-\frac{t_1}{\sqrt{2}}$	0	0	0	0	0
$f_{1+}^{\#1} + \alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	0	0	0	0	0
$\omega_{1-}^{\#1} - \alpha$	0	0	0	$k^2(2r_3+r_5) + \frac{t_1}{6}$	$\frac{t_1}{3\sqrt{2}}$	$\frac{ikt_1}{3}$
$\omega_{1-}^{\#2} - \alpha$	0	0	0	$\frac{t_1}{3\sqrt{2}}$	$\frac{t_1}{3}$	$\frac{1}{3}i\sqrt{2}kt_1$
$f_{1-}^{\#1} - \alpha$	0	0	0	0	0	0
$f_{1-}^{\#2} - \alpha$	0	0	0	$-\frac{1}{3}ikt_1$	$-\frac{1}{3}i\sqrt{2}kt_1$	$\frac{2k^2t_1}{3}$

Lagrangian density

$$\begin{aligned}
 &-\frac{1}{3}t_1\omega_{,\prime}{}^{\alpha'}\omega_{\kappa\alpha}{}^{\kappa}-t_1\omega_{,\prime}{}^{\kappa\lambda}\omega_{\kappa\lambda}{}^{\prime}-2r_3\partial_{\prime}\omega_{\kappa}{}^{\kappa\lambda}\partial^{\prime}\omega_{\lambda}{}^{\alpha}-r_5\partial_{\prime}\omega_{\kappa}{}^{\kappa\lambda}\partial^{\prime}\omega_{\lambda}{}^{\alpha}+ \\
 &2r_3\partial_{\alpha}\omega_{\lambda}{}^{\alpha}\partial_{\theta}\partial_{\kappa}\omega^{\theta\kappa\lambda}-r_5\partial_{\alpha}\omega_{\lambda}{}^{\alpha}\partial_{\theta}\partial_{\kappa}\omega^{\theta\kappa\lambda}-2r_3\partial_{\theta}\omega_{\lambda}{}^{\alpha}\partial_{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-r_5\partial_{\alpha}\omega_{\lambda}{}^{\alpha}\partial_{\theta}\partial_{\kappa}\omega^{\kappa\lambda\theta}+ \\
 &r_5\partial_{\theta}\omega_{\lambda}{}^{\alpha}\partial_{\alpha}\partial_{\kappa}\omega^{\theta\kappa\lambda}-2r_3\partial_{\alpha}\omega_{\lambda}{}^{\alpha}\partial_{\theta}\partial_{\kappa}\omega^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}{}^{\theta}- \\
 &4r_3\partial_{\theta}\omega_{\lambda}{}^{\alpha}\partial_{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}+2r_5\partial_{\theta}\omega_{\lambda}{}^{\alpha}\partial_{\alpha}\partial_{\kappa}\omega^{\kappa\lambda\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\theta\kappa}\partial^{\kappa}f_{\alpha}{}^{\theta}- \\
 &\frac{1}{2}t_1\partial^{\alpha}f_{\kappa\theta}\partial^{\kappa}f_{\alpha}{}^{\theta}-\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}{}^{\kappa}\partial^{\kappa}f_{\alpha\lambda}{}^{\prime}+\frac{1}{3}t_1\omega_{\kappa\alpha}{}^{\alpha}\partial^{\kappa}f_{,\prime}{}^{\alpha}+\frac{1}{3}t_1\omega_{\kappa\lambda}{}^{\lambda}\partial^{\kappa}f_{,\prime}{}^{\alpha}+ \\
 &\frac{2}{3}t_1\partial^{\alpha}f_{\kappa\alpha}{}^{\prime}\partial^{\kappa}f_{,\prime}{}^{\alpha}-\frac{1}{3}t_1\partial_{\kappa}f_{\lambda}{}^{\lambda}\partial^{\kappa}f_{,\prime}{}^{\alpha}+2t_1\omega_{\prime\kappa\theta}\partial^{\kappa}f^{\prime\theta}-\frac{1}{3}t_1\omega_{\prime\alpha}{}^{\alpha}\partial^{\kappa}f_{\prime}{}^{\alpha}- \\
 &\frac{1}{3}t_1\omega_{\prime\lambda}{}^{\lambda}\partial^{\kappa}f_{\prime}{}^{\alpha}+\frac{1}{2}t_1\partial^{\alpha}f_{\lambda}{}^{\kappa}\partial^{\kappa}f_{\lambda\alpha}{}^{\prime}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}{}^{\lambda}\partial^{\kappa}f_{\lambda}{}^{\theta}+\frac{1}{2}t_1\partial_{\kappa}f_{\theta}{}^{\lambda}\partial^{\kappa}f_{\lambda}{}^{\theta}- \\
 &\frac{1}{3}t_1\partial^{\alpha}f_{\lambda}{}^{\alpha}\partial^{\kappa}f_{\lambda\kappa}{}^{\prime}-4r_3\partial^{\beta}\omega_{,\prime}{}^{\lambda\alpha}\partial_{\lambda}\omega_{\alpha\beta}{}^{\prime}-2r_3\partial_{\alpha}\omega_{\lambda}{}^{\alpha}\partial_{\theta}\partial^{\lambda}\omega^{\theta\kappa}{}_{\kappa}+ \\
 &r_5\partial_{\alpha}\omega_{\lambda}{}^{\alpha}\partial_{\theta}\partial^{\lambda}\omega^{\theta\kappa}{}_{\kappa}+2r_3\partial_{\theta}\omega_{\lambda}{}^{\alpha}\partial_{\alpha}\partial^{\lambda}\omega^{\theta\kappa}{}_{\kappa}-r_5\partial_{\theta}\omega_{\lambda}{}^{\alpha}\partial_{\alpha}\partial^{\lambda}\omega^{\theta\kappa}{}_{\kappa}
 \end{aligned}$$

$$\text{Added source term: } \left| f^{\alpha\beta}\tau_{\alpha\beta} + \omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi} \right.$$

$\sigma_{1+}^{\#1} + \alpha\beta$	$\sigma_{1+}^{\#2} + \alpha\beta$	$\tau_{1+}^{\#1} + \alpha\beta$	$\sigma_{1-}^{\#1} - \alpha$	$\sigma_{1-}^{\#2} - \alpha$	$\tau_{1-}^{\#1} - \alpha$	$\tau_{1-}^{\#2} - \alpha$
$\sigma_{1+}^{\#1} + \alpha\beta$	0	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$-\frac{i\sqrt{2}k}{t_1+k^2t_1}$	0	0	0
$\sigma_{1+}^{\#2} + \alpha\beta$	$-\frac{\sqrt{2}}{t_1+k^2t_1}$	$\frac{-2k^2(2r_3+r_5)+t_1}{(1+k^2)^2t_1^2}$	$\frac{-2ik^3(2r_3+r_5)+ikt_1}{(1+k^2)^2t_1^2}$	0	0	0
$\tau_{1+}^{\#1} + \alpha\beta$	$\frac{i\sqrt{2}k}{t_1+k^2t_1}$	$\frac{i(2k^3(2r_3+r_5)-kt_1)}{(1+k^2)^2t_1^2}$	$\frac{-2k^4(2r_3+r_5)+k^2t_1}{(1+k^2)^2t_1^2}$	0	0	0
$\sigma_{1-}^{\#1} - \alpha$	0	0	0	$\frac{1}{k^2(2r_3+r_5)}$	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	0
$\sigma_{1-}^{\#2} - \alpha$	0	0	0	$-\frac{1}{\sqrt{2}(k^2+2k^4)(2r_3+r_5)}$	$\frac{6k^2(2r_3+r_5)+t_1}{2(k+2k^3)^2(2r_3+r_5)t_1}$	0
$\tau_{1-}^{\#1} - \alpha$	0	0	0	0	0	0
$\tau_{1-}^{\#2} - \alpha$	0	0	0	$\frac{i}{k(1+2k^2)(2r_3+r_5)}$	$-\frac{i(6k^2(2r_3+r_5)+t_1)}{\sqrt{2}k(1+2k^2)^2(2r_3+r_5)t_1}$	0

$\omega_{0+}^{\#1} +$	$f_{0+}^{\#1} +$	$f_{0+}^{\#2} +$	$\omega_{0-}^{\#1} -$
$\omega_{0+}^{\#1} +$	$6k^2r_3$	0	0
$f_{0+}^{\#1} +$	0	0	0
$f_{0+}^{\#2} +$	0	0	0
$\omega_{0-}^{\#1} -$	0	0	$-t_1$

$\sigma_{0+}^{\#1} +$	$\sigma_{0+}^{\#1} +$	$\tau_{0+}^{\#1} +$	$\tau_{0+}^{\#2} +$	$\sigma_{0-}^{\#1} -$
$\sigma_{0+}^{\#1} +$	$\frac{1}{6k^2r_3}$	0	0	0
$\tau_{0+}^{\#1} +$	0	0	0	0
$\tau_{0+}^{\#2} +$	0	0	0	0
$\sigma_{0-}^{\#1} -$	0	0	0	$-\frac{1}{t_1}$

$\sigma_{2^{+}\alpha\beta}^{\#1}$	$\tau_{2^{+}\alpha\beta}^{\#1}$	$\sigma_{2^{-}\alpha\beta\chi}^{\#1}$
$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
0	0	$\frac{2}{t_1}$

$\omega_{2^+}^{\#1} \alpha\beta$	$f_{2^+}^{\#1} \alpha\beta$	$\omega_{2^-}^{\#1} \alpha\beta\chi$
$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$\frac{ikt_1}{\sqrt{2}}$	$k^2 t_1$	0
0	0	$\frac{t_1}{2}$

Quadratic pole

Pole residue:	$-\frac{1}{(2r_3+r_5)t_1^2} > 0$
Polarisations:	2

$$\text{Unitarity conditions} \\
 r_5 < -2r_3 \ \&\& \ t_1 < 0 \ || \ t_1 > 0$$

(No massive particles)