



$$r_2 < 0 \&\& t_2 > 0$$

### Lagrangian density

$$\begin{aligned} &-\frac{1}{3}t_1\omega_{\lambda'}^{\alpha\iota}\omega_{\kappa\alpha}^{\kappa}-\frac{1}{3}t_1\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\lambda'}+\frac{2}{3}t_2\omega_{\lambda'}^{\kappa\lambda}\omega_{\kappa\lambda}^{\lambda'}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda'}\omega_{\kappa\lambda}^{\kappa\lambda}+\\ &\frac{1}{3}t_2\omega_{\kappa\lambda}^{\lambda'}\omega_{\kappa\lambda}^{\kappa\lambda}+f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}+\frac{2}{3}r_2\partial^\beta\omega_{\kappa}^{\theta\alpha}\partial_\theta\omega_{\alpha\beta}^{\kappa}-\\ &\frac{1}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\alpha\beta\theta}-\frac{2}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\theta\alpha\beta}+4r_3\partial_\alpha\omega_{\lambda}^{\alpha}\partial_\kappa\omega^{\theta\kappa\lambda}-\\ &4r_3\partial_\theta\omega_{\lambda}^{\alpha}\partial_\kappa\omega^{\theta\kappa\lambda}-\frac{1}{3}t_1\partial^\alpha f_{\theta\kappa}\partial^\kappa f_{\alpha}^{\theta}+\frac{1}{6}t_2\partial^\alpha f_{\theta\kappa}\partial^\kappa f_{\alpha}^{\theta}-\frac{2}{3}t_1\partial^\alpha f_{\kappa\theta}\partial^\kappa f_{\alpha}^{\theta}-\\ &\frac{1}{6}t_2\partial^\alpha f_{\kappa\theta}\partial^\kappa f_{\alpha}^{\theta}-\frac{1}{3}t_1\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\alpha\lambda}^{\lambda}+\frac{1}{6}t_2\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\alpha\lambda}^{\lambda}+\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha}\partial^\kappa f_{\lambda'}^{\iota}+\\ &\frac{1}{3}t_1\omega_{\kappa\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\iota}+\frac{2}{3}t_1\partial^\alpha f_{\kappa\alpha}\partial^\kappa f_{\lambda'}^{\iota}-\frac{1}{3}t_1\partial_\kappa f_{\lambda}^{\lambda}\partial^\kappa f_{\lambda'}^{\iota}+\frac{1}{3}t_1\omega_{\iota\theta\kappa}\partial^\kappa f^{\iota\theta}+\\ &\frac{1}{3}t_2\omega_{\iota\theta\kappa}\partial^\kappa f^{\iota\theta}+\frac{4}{3}t_1\omega_{\iota\kappa\theta}\partial^\kappa f^{\iota\theta}-\frac{2}{3}t_2\omega_{\iota\kappa\theta}\partial^\kappa f^{\iota\theta}-\frac{1}{3}t_1\omega_{\theta\iota\kappa}\partial^\kappa f^{\iota\theta}-\\ &\frac{1}{3}t_2\omega_{\theta\iota\kappa}\partial^\kappa f^{\iota\theta}+\frac{2}{3}t_1\omega_{\theta\kappa\iota}\partial^\kappa f^{\iota\theta}+\frac{2}{3}t_2\omega_{\theta\kappa\iota}\partial^\kappa f^{\iota\theta}-\frac{1}{3}t_1\omega_{\lambda'\alpha}^{\alpha}\partial^\kappa f_{\kappa}^{\iota}-\\ &\frac{1}{3}t_1\omega_{\lambda'\lambda}^{\lambda}\partial^\kappa f_{\kappa}^{\iota}+\frac{1}{3}t_1\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\lambda\alpha}^{\lambda}-\frac{1}{6}t_2\partial^\alpha f_{\kappa}^{\lambda}\partial^\kappa f_{\lambda\alpha}^{\lambda}+\frac{1}{3}t_1\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}-\\ &\frac{1}{6}t_2\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}+\frac{2}{3}t_1\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}+\frac{1}{6}t_2\partial_\kappa f_{\theta}^{\lambda}\partial^\kappa f_{\lambda}^{\theta}-\frac{1}{3}t_1\partial^\alpha f_{\lambda}^{\iota}\partial^\kappa f_{\alpha}^{\iota}+\\ &\frac{1}{3}r_2\partial_\kappa\omega^{\alpha\beta\theta}\partial^\kappa\omega_{\alpha\beta\theta}+\frac{2}{3}r_2\partial_\kappa\omega^{\theta\alpha\beta}\partial^\kappa\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^\beta\omega_{\lambda'}^{\alpha\lambda}\partial_\lambda\omega_{\alpha\beta}^{\lambda'}-4r_3\partial_\alpha\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\kappa}^{\theta\kappa}+4r_3\partial_\theta\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\alpha}^{\theta\kappa}\\ &\frac{2}{3}r_2\partial^\beta\omega_{\lambda'}^{\lambda\alpha}\partial_\lambda\omega_{\alpha\beta}^{\lambda'}-4r_3\partial^\beta\omega_{\lambda'}^{\lambda\alpha}\partial_\lambda\omega_{\alpha\beta}^{\lambda'}-4r_3\partial_\alpha\omega_{\lambda}^{\alpha}\partial^\lambda\omega_{\theta}^{\theta\kappa} \end{aligned}$$

	$\sigma_{1^+}^{\#1} \dagger \alpha\beta$	$\sigma_{1^+}^{\#2} \dagger \alpha\beta$	$\tau_{1^+}^{\#1} \dagger \alpha\beta$	$\sigma_{1^+}^{\#1} \dagger \alpha$	$\sigma_{1^+}^{\#2} \dagger \alpha$	$\tau_{1^+}^{\#1} \dagger \alpha$	$\tau_{1^+}^{\#2} \dagger \alpha$
$\sigma_{1^+}^{\#1} \dagger \alpha\beta$	$\frac{2(t_1+t_2)}{3t_1t_2}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	0	0	0	0
$\sigma_{1^+}^{\#2} \dagger \alpha\beta$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{t_1+4t_2}{3(1+k^2)^2t_1t_2}$	$\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0	0
$\tau_{1^+}^{\#1} \dagger \alpha\beta$	$-\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$-\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	$\frac{k^2(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0	0
$\sigma_{1^+}^{\#1} \dagger \alpha$	0	0	0	$\frac{6}{(3+4k^2)^2t_1}$	$\frac{6\sqrt{2}}{(3+4k^2)^2t_1}$	0	$\frac{12ik}{(3+4k^2)^2t_1}$
$\sigma_{1^+}^{\#2} \dagger \alpha$	0	0	0	$\frac{6\sqrt{2}}{(3+4k^2)^2t_1}$	$\frac{12}{(3+4k^2)^2t_1}$	0	$\frac{12i\sqrt{2}k}{(3+4k^2)^2t_1}$
$\tau_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$\tau_{1^+}^{\#2} \dagger \alpha$	0	0	0	$-\frac{12ik}{(3+4k^2)^2t_1}$	$-\frac{12i\sqrt{2}k}{(3+4k^2)^2t_1}$	0	$\frac{24k^2}{(3+4k^2)^2t_1}$

	$\omega_{1^+}^{\#1} \dagger \alpha\beta$	$\omega_{1^+}^{\#2} \dagger \alpha\beta$	$f_{1^+}^{\#1} \dagger \alpha\beta$	$\omega_{1^+}^{\#1} \dagger \alpha$	$\omega_{1^+}^{\#2} \dagger \alpha$	$f_{1^+}^{\#1} \dagger \alpha$	$f_{1^+}^{\#2} \dagger \alpha$
$\omega_{1^+}^{\#1} \dagger \alpha\beta$	$\frac{1}{6}(t_1+4t_2)$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$-\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2} \dagger \alpha\beta$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$\frac{t_1+t_2}{3}$	$\frac{1}{3}ik(t_1+t_2)$	0	0	0	0
$f_{1^+}^{\#1} \dagger \alpha\beta$	$\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	$-\frac{1}{3}ik(t_1+t_2)$	$\frac{1}{3}k^2(t_1+t_2)$	0	0	0	0
$\omega_{1^+}^{\#1} \dagger \alpha$	0	0	0	$\frac{t_1}{6}$	$\frac{t_1}{3\sqrt{2}}$	0	$\frac{ikt_1}{3}$
$\omega_{1^+}^{\#2} \dagger \alpha$	0	0	0	$\frac{t_1}{3\sqrt{2}}$	$\frac{t_1}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_1$
$f_{1^+}^{\#1} \dagger \alpha$	0	0	0	0	0	0	0
$f_{1^+}^{\#2} \dagger \alpha$	0	0	0	$-\frac{1}{3}ik t_1$	$-\frac{1}{3}i\sqrt{2}kt_1$	0	$\frac{2k^2t_1}{3}$

#### Source constraints

SO(3) irreps	#
$\tau_{0^+}^{\#2} == 0$	1
$\tau_{0^+}^{\#1} == 0$	1
$\tau_{1^+}^{\#2\alpha} + 2ik\sigma_{1^+}^{\#1\alpha} == 0$	3
$\tau_{1^+}^{\#1\alpha} == 0$	3
$\sigma_{1^+}^{\#1\alpha} == \sigma_{1^+}^{\#2\alpha}$	3
$\tau_{1^+}^{\#1\alpha\beta} + ik\sigma_{1^+}^{\#2\alpha\beta} == 0$	3
$\tau_{2^+}^{\#1\alpha\beta} - 2ik\sigma_{2^+}^{\#1\alpha\beta} == 0$	5
Total #:	19

$q_{0^+}^{\#1} \dagger$	$q_{0^+}^{\#1} \dagger$	$q_{0^+}^{\#1} \dagger$	$q_{0^+}^{\#1} \dagger$	$q_{0^+}^{\#1} \dagger$
0	0	0	$\frac{1}{6k^2r_3}$	0
0	0	0	0	0
0	0	0	0	0
$\frac{1}{k^2r_2+t_2}$	0	0	0	0

$\omega_{2^+}^{\#1} \dagger \alpha\beta$	$f_{2^+}^{\#1} \dagger \alpha\beta$	$\omega_{2^+}^{\#1} \dagger \alpha\beta\chi$
$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	0
$\omega_{2^+}^{\#1} \dagger \alpha\beta\chi$	0	0
		$\frac{t_1}{2}$

$\omega_{0^+}^{\#1} \dagger$	$f_{0^+}^{\#1} \dagger$	$f_{0^+}^{\#2} \dagger$	$\omega_0^{\#1} \dagger$
$\omega_{0^+}^{\#1} \dagger$	$6k^2r_3$	0	0
$f_{0^+}^{\#1} \dagger$	0	0	0
$f_{0^+}^{\#2} \dagger$	0	0	0
$\omega_0^{\#1} \dagger$	0	0	$k^2r_2+t_2$

$\sigma_{2^+}^{\#1} \dagger \alpha\beta$	$\tau_{2^+}^{\#1} \dagger \alpha\beta$	$\sigma_{2^+}^{\#1} \dagger \alpha\beta\chi$
$\sigma_{2^+}^{\#1} \dagger \alpha\beta$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\tau_{2^+}^{\#1} \dagger \alpha\beta$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\sigma_{2^+}^{\#1} \dagger \alpha\beta\chi$	0	$\frac{2}{t_1}$