



Massive particle	
Pole residue:	$-\frac{1}{r_2} \gg 0$
Polarisations:	1
Square mass:	$-\frac{t_2}{r_2} \gg 0$
Spin:	0
Parity:	Odd

$$r_2 < 0 \ \& \ t_2 > 0$$

Unitarity conditions

(no massless particles)

Lagrangian density

$$\begin{aligned} &-\frac{1}{3}t_1\omega_{\kappa\alpha}^{\alpha\prime}\omega_{\kappa\alpha}^{\kappa-\frac{1}{3}t_1}\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime\prime}+\frac{2}{3}t_2\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime\prime}+\frac{1}{3}t_1\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime\prime}+\omega_{\kappa\lambda}^{\kappa\lambda\prime}\omega_{\kappa\lambda}^{\prime\prime}+ \\ &\frac{1}{3}t_2\omega_{\kappa\lambda}^{\kappa\lambda}\omega_{\kappa\lambda}^{\prime\prime}+\frac{2}{3}r_2\partial^\beta\omega_{\kappa\alpha\beta}^{\theta\alpha}\partial_\theta\omega_{\alpha\beta}^{\kappa-\frac{1}{3}}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\alpha\beta\theta}- \\ &\frac{2}{3}r_2\partial_\theta\omega_{\alpha\beta}^{\kappa}\partial_\kappa\omega^{\theta\alpha\beta}+4r_3\partial_\alpha\omega_\lambda^\alpha\partial_\kappa\omega_\lambda^{\theta\kappa\lambda}-4r_3\partial_\theta\omega_\lambda^\alpha\partial_\kappa\omega^{\theta\kappa\lambda}- \\ &\frac{1}{3}t_1\partial^\alpha f_{\theta\kappa}^\kappa\partial^\kappa f_\alpha^\theta+\frac{1}{6}t_2\partial^\alpha f_{\theta\kappa}^\kappa\partial^\kappa f_\alpha^\theta-\frac{2}{3}t_1\partial^\alpha f_{\kappa\theta}^\kappa\partial^\kappa f_\alpha^\theta- \\ &\frac{1}{6}t_2\partial^\alpha f_{\kappa\theta}^\kappa\partial^\kappa f_\alpha^\theta-\frac{1}{3}t_1\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda\partial^\kappa f_{\alpha\lambda}^\kappa+\frac{1}{6}t_2\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda\partial^\kappa f_{\alpha\lambda}^\kappa+ \\ &\frac{1}{3}t_1\omega_{\kappa\alpha}^\alpha\partial^\kappa f_{\kappa\lambda}^{\prime\prime}+\frac{1}{3}t_1\omega_{\kappa\lambda}^\lambda\partial^\kappa f_{\kappa\lambda}^{\prime\prime}+\frac{2}{3}t_1\partial^\alpha f_{\kappa\alpha}^\kappa\partial^\kappa f_{\kappa\alpha}^{\prime\prime}-\frac{1}{3}t_1\partial_\kappa f_\lambda^\lambda\partial^\kappa f_{\kappa\lambda}^{\prime\prime}+ \\ &\frac{1}{3}t_1\omega_{\kappa\theta}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}+\frac{1}{3}t_2\omega_{\kappa\theta}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}+\frac{4}{3}t_1\omega_{\kappa\theta}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}-\frac{2}{3}t_2\omega_{\kappa\theta}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}- \\ &\frac{1}{3}t_1\omega_{\theta\kappa}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}-\frac{1}{3}t_2\omega_{\theta\kappa}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}+\frac{2}{3}t_1\omega_{\theta\kappa}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}+\frac{2}{3}t_2\omega_{\theta\kappa}^\kappa\partial^\kappa f_{\kappa\theta}^{\prime\prime}- \\ &\frac{1}{3}t_1\omega_{\kappa\alpha}^\alpha\partial^\kappa f_{\kappa\lambda}^{\prime\prime}-\frac{1}{3}t_1\omega_{\kappa\lambda}^\lambda\partial^\kappa f_{\kappa\lambda}^{\prime\prime}+\frac{1}{3}t_1\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\kappa\lambda}^{\prime\prime}-\frac{1}{6}t_2\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\kappa\lambda}^{\prime\prime}+ \\ &\frac{1}{3}t_1\partial_\kappa f_\theta^\lambda\partial^\kappa f_\theta^\lambda-\frac{1}{6}t_2\partial_\kappa f_\theta^\lambda\partial^\kappa f_\theta^\lambda+\frac{2}{3}t_1\partial_\kappa f_\theta^\lambda\partial^\kappa f_\theta^\lambda \\ &\frac{1}{6}t_2\partial_\kappa f_\theta^\lambda\partial^\kappa f_\theta^\lambda-\frac{1}{3}t_1\partial^\alpha f_\lambda^\lambda\partial^\kappa f_{\alpha\lambda}^\lambda\partial^\kappa f_{\alpha\lambda}^\kappa+\frac{1}{3}r_2\partial_\kappa\omega^{\alpha\beta\theta}\partial^\kappa\omega_{\alpha\beta\theta}+ \\ &\frac{2}{3}r_2\partial_\kappa\omega^{\theta\alpha\beta}\partial^\kappa\omega_{\alpha\beta\theta}-\frac{2}{3}r_2\partial^\beta\omega_{\alpha\lambda}^{\alpha\prime}\partial_\lambda\omega_{\alpha\beta}^{\prime\prime}+\frac{2}{3}r_2\partial^\beta\omega_{\alpha\lambda}^{\lambda\prime}\partial_\lambda\omega_{\alpha\beta}^{\prime\prime}- \\ &4r_3\partial^\beta\omega_{\lambda\alpha}^{\lambda\prime}\partial_\lambda\omega_{\alpha\beta}^{\prime\prime}-4r_3\partial_\alpha\omega_\lambda^\alpha\partial^\lambda\omega_{\kappa\theta}^{\theta\kappa}+4r_3\partial_\theta\omega_\lambda^\alpha\partial^\lambda\omega_{\kappa\alpha}^{\theta\kappa} \end{aligned}$$

Added source term: $f^{\alpha\beta}\tau_{\alpha\beta}+\omega^{\alpha\beta\chi}\sigma_{\alpha\beta\chi}$

	$\sigma_{1^+}^{\#1}+\alpha\beta$	$\sigma_{1^+}^{\#2}+\alpha\beta$	$\tau_{1^+}^{\#1}+\alpha\beta$	$\sigma_{1^+}^{\#1}-\alpha$	$\sigma_{1^+}^{\#2}-\alpha$	$\tau_{1^+}^{\#1}-\alpha$	$\tau_{1^+}^{\#2}-\alpha$
$\sigma_{1^+}^{\#1}+\alpha\beta$	$\frac{2(t_1+t_2)}{3t_1t_2}$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	0	0	0	0
$\sigma_{1^+}^{\#2}+\alpha\beta$	$\frac{\sqrt{2}(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$\frac{t_1+4t_2}{3(1+k^2)^2t_1t_2}$	$\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0	0
$\tau_{1^+}^{\#1}+\alpha\beta$	$-\frac{i\sqrt{2}k(t_1-2t_2)}{3(1+k^2)t_1t_2}$	$-\frac{ik(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	$\frac{k^2(t_1+4t_2)}{3(1+k^2)^2t_1t_2}$	0	0	0	0
$\sigma_{1^+}^{\#1}-\alpha$	0	0	0	$\frac{6}{(3+4k^2)^2t_1}$	$\frac{6\sqrt{2}}{(3+4k^2)^2t_1}$	0	$\frac{12ik}{(3+4k^2)^2t_1}$
$\sigma_{1^+}^{\#2}-\alpha$	0	0	0	$\frac{6\sqrt{2}}{(3+4k^2)^2t_1}$	$\frac{12}{(3+4k^2)^2t_1}$	0	$\frac{12i\sqrt{2}k}{(3+4k^2)^2t_1}$
$\tau_{1^+}^{\#1}-\alpha$	0	0	0	0	0	0	0
$\tau_{1^+}^{\#2}-\alpha$	0	0	0	$-\frac{12ik}{(3+4k^2)^2t_1}$	$-\frac{12i\sqrt{2}k}{(3+4k^2)^2t_1}$	0	$\frac{24k^2}{(3+4k^2)^2t_1}$

	$\omega_{1^+}^{\#1}+\alpha\beta$	$\omega_{1^+}^{\#2}+\alpha\beta$	$f_{1^+}^{\#1}+\alpha\beta$	$\omega_{1^+}^{\#1}-\alpha$	$\omega_{1^+}^{\#2}-\alpha$	$f_{1^+}^{\#1}-\alpha$	$f_{1^+}^{\#2}-\alpha$
$\omega_{1^+}^{\#1}+\alpha\beta$	$\frac{1}{6}(t_1+4t_2)$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$-\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	0	0	0	0
$\omega_{1^+}^{\#2}+\alpha\beta$	$-\frac{t_1-2t_2}{3\sqrt{2}}$	$\frac{t_1+t_2}{3}$	$\frac{1}{3}ik(t_1+t_2)$	0	0	0	0
$f_{1^+}^{\#1}+\alpha\beta$	$\frac{ik(t_1-2t_2)}{3\sqrt{2}}$	$-\frac{1}{3}ik(t_1+t_2)$	$\frac{1}{3}k^2(t_1+t_2)$	0	0	0	0
$\omega_{1^+}^{\#1}-\alpha$	0	0	0	$\frac{t_1}{6}$	$\frac{t_1}{3\sqrt{2}}$	0	$\frac{ikt_1}{3}$
$\omega_{1^+}^{\#2}-\alpha$	0	0	0	$\frac{t_1}{3\sqrt{2}}$	$\frac{t_1}{3}$	0	$\frac{1}{3}i\sqrt{2}kt_1$
$f_{1^+}^{\#1}-\alpha$	0	0	0	0	0	0	0
$f_{1^+}^{\#2}-\alpha$	0	0	0	$-\frac{1}{3}ik t_1$	$-\frac{1}{3}i\sqrt{2}kt_1$	0	$\frac{2k^2t_1}{3}$

Source constraints

SO(3) irreps	#
$\tau_{0^+}^{\#2}==0$	1
$\tau_{0^+}^{\#1}==0$	1
$\tau_{1^+}^{\#2\alpha}+2ik\sigma_{1^+}^{\#1\alpha}==0$	3
$\tau_{1^+}^{\#1\alpha}==0$	3
$\sigma_{1^+}^{\#1\alpha}==\sigma_{1^+}^{\#2\alpha}$	3
$\tau_{1^+}^{\#1\alpha\beta}+ik\sigma_{1^+}^{\#2\alpha\beta}==0$	3
$\tau_{2^+}^{\#1\alpha\beta}-2ik\sigma_{2^+}^{\#1\alpha\beta}==0$	5
Total #:	19

	$q_{0^+}^{\#1}+\dagger$	$q_{0^+}^{\#1}+\dagger$	$q_{0^+}^{\#1}+\dagger$	$q_{0^+}^{\#1}+\dagger$
$q_{0^+}^{\#1}+\dagger$	0	0	0	$\frac{1}{k^2r_2+t_2}$
$q_{0^+}^{\#1}+\dagger$	0	0	0	0
$q_{0^+}^{\#1}+\dagger$	0	0	0	0
$q_{0^+}^{\#1}+\dagger$	$\frac{1}{6k^2r_3}$	0	0	0

	$\omega_{2^+}^{\#1}+\alpha\beta$	$f_{2^+}^{\#1}+\alpha\beta$	$\omega_{2^+}^{\#1}+\alpha\beta\chi$
$\omega_{2^+}^{\#1}+\alpha\beta$	$\frac{t_1}{2}$	$-\frac{ikt_1}{\sqrt{2}}$	0
$f_{2^+}^{\#1}+\alpha\beta$	$\frac{ikt_1}{\sqrt{2}}$	k^2t_1	0
$\omega_{2^+}^{\#1}+\alpha\beta\chi$	0	0	$\frac{t_1}{2}$

	$\omega_{0^+}^{\#1}+\dagger$	$f_{0^+}^{\#1}+\dagger$	$f_{0^+}^{\#2}+\dagger$	$\omega_{0^+}^{\#1}+\dagger$
$\omega_{0^+}^{\#1}+\dagger$	$6k^2r_3$	0	0	0
$f_{0^+}^{\#1}+\dagger$	0	0	0	0
$f_{0^+}^{\#2}+\dagger$	0	0	0	0
$\omega_{0^+}^{\#1}+\dagger$	0	0	0	$k^2r_2+t_2$

	$\sigma_{2^+}^{\#1}+\alpha\beta$	$\tau_{2^+}^{\#1}+\alpha\beta$	$\sigma_{2^+}^{\#1}-\alpha\beta\chi$
$\sigma_{2^+}^{\#1}+\alpha\beta$	$\frac{2}{(1+2k^2)^2t_1}$	$-\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	0
$\tau_{2^+}^{\#1}+\alpha\beta$	$\frac{2i\sqrt{2}k}{(1+2k^2)^2t_1}$	$\frac{4k^2}{(1+2k^2)^2t_1}$	0
$\sigma_{2^+}^{\#1}+\alpha\beta\chi$	0	0	$\frac{2}{t_1}$