

## Wave operator and propagator

	$\Delta_{1^+ \alpha \beta}^{\#1}$	$\Delta_{1^+ \alpha \beta}^{\#2}$	$\Delta_{1^+ \alpha \beta}^{\#3}$	$\Delta_{1^+ \alpha}^{\#1}$	$\Delta_{1^+ \alpha}^{\#2}$	$\Delta_{1^+ \alpha}^{\#3}$	$\Delta_{1^+ \alpha}^{\#4}$	$\Delta_{1^+ \alpha}^{\#5}$	$\Delta_{1^+ \alpha}^{\#6}$	$\mathcal{T}_{1^+ \alpha}^{\#1}$
$\Delta_{1^+ \alpha \beta}^{\#1}$	$\frac{4}{3} \left( -\frac{1}{a_0+4a_1-4a_2} + \frac{2a_1+a_2-2a_5-6a_7+2a_9}{2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9)} \right)$	$\frac{2}{3} \sqrt{2} \left( -\frac{1}{a_0+4a_1-4a_2} - \frac{2(2a_1+a_2-2a_5-6a_7+2a_9)}{2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9)} \right)$	$-\frac{4(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	0	0	0	0	0
$\Delta_{1^+ \alpha \beta}^{\#2}$	$\frac{2}{3} \sqrt{2} \left( -\frac{1}{a_0+4a_1-4a_2} - \frac{2(2a_1+a_2-2a_5-6a_7+2a_9)}{2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9)} \right)$	$-\frac{2}{3(a_0+4a_1-4a_2)} + \frac{8(2a_1+a_2-2a_5-6a_7+2a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$\frac{4\sqrt{2}(2a_1+a_2+a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	0	0	0	0	0
$\Delta_{1^+ \alpha \beta}^{\#3}$	$-\frac{4(2a_1+a_2+a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{4\sqrt{2}(2a_1+a_2+a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{4(a_0-2a_1-a_2)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	0	0	0	0	0
$\Delta_{1^+ \alpha}^{\#1}$	0	0	0	$\frac{4(2a_1+a_2-2a_5-6a_7+2a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$\frac{4\sqrt{2}(2a_1+a_2-2a_5-6a_7+2a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	$-\frac{4\sqrt{\frac{2}{3}}(2a_1+a_2+a_9)}{3\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{4(2a_1+a_2+a_9)}{3\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0
$\Delta_{1^+ \alpha}^{\#2}$	0	0	0	$\frac{4\sqrt{2}(2a_1+a_2-2a_5-6a_7+2a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$\frac{8(2a_1+a_2-2a_5-6a_7+2a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	$-\frac{4\sqrt{\frac{2}{3}}(2a_1+a_2+a_9)}{3\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{4(2a_1+a_2+a_9)}{3\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0
$\Delta_{1^+ \alpha}^{\#3}$	0	0	0	0	0	$-\frac{10}{9(a_0+2a_5-6a_7)} - \frac{1}{6(3a_0-2(a_5-8a_6+5a_7-4a_{13}k^2))}$	$\frac{1}{18} \sqrt{5} \left( -\frac{4}{a_0+2a_5-6a_7} - \frac{3}{3a_0-2(a_5-8a_6+5a_7-4a_{13}k^2)} \right)$	$-\frac{1}{\sqrt{2}(9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2))}$	$-\frac{1}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	0
$\Delta_{1^+ \alpha}^{\#4}$	0	0	0	0	0	$\frac{1}{18} \sqrt{5} \left( \frac{4}{a_0+2a_5-6a_7} - \frac{3}{3a_0-2(a_5-8a_6+5a_7-4a_{13}k^2)} \right)$	$-\frac{2}{9(a_0+2a_5-6a_7)} - \frac{5}{6(3a_0-2(a_5-8a_6+5a_7-4a_{13}k^2))}$	$-\frac{\sqrt{5}}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	$-\frac{\sqrt{5}}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	0
$\Delta_{1^+ \alpha}^{\#5}$	0	0	0	$-\frac{4\sqrt{\frac{2}{3}}(2a_1+a_2+a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{8(2a_1+a_2+a_9)}{3\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{1}{\sqrt{2}(9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2))}$	$-\frac{\sqrt{\frac{5}{2}}}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	$\frac{8(-a_0+2a_1+a_2)}{9(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))} - \frac{1}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	$(\sqrt{2}(12a_0^2-3a_9^2-a_0(30a_1+15a_2+2a_5-64a_6+22a_7+6a_9-32a_{13}k^2)+2(2a_1+a_2)(a_5-32a_6+11a_7-16a_{13}k^2)))/(9(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))(3a_0-2(a_5-8a_6+5a_7-4a_{13}k^2))))$	0
$\Delta_{1^+ \alpha}^{\#6}$	0	0	0	$\frac{4(2a_1+a_2+a_9)}{3\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$\frac{4\sqrt{\frac{2}{3}}(2a_1+a_2+a_9)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{1}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	$-\frac{\sqrt{5}}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	$(\sqrt{2}(12a_0^2-3a_9^2-a_0(30a_1+15a_2+2a_5-64a_6+22a_7+6a_9-32a_{13}k^2)+2(2a_1+a_2)(a_5-32a_6+11a_7-16a_{13}k^2)))/(9(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))(3a_0-2(a_5-8a_6+5a_7-4a_{13}k^2))))$	$\frac{-4a_0+8a_1+4a_2}{9(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))} - \frac{2}{9a_0-6(a_5-8a_6+5a_7-4a_{13}k^2)}$	0
$\mathcal{T}_{1^+ \alpha}^{\#1}$	0	0	0	0	0	0	0	0	0	0

[illegible]

	$\Delta_{2^+}^{\#1} a\beta$	$\Delta_{2^+}^{\#2} a\beta$	$\Delta_{2^+}^{\#3} a\beta$	$\mathcal{T}_{2^+}^{\#1} a\beta$	$\Delta_{2^+}^{\#1} a\beta\chi$	$\Delta_{2^+}^{\#2} a\beta\chi$
$\Delta_{2^+}^{\#1} \uparrow a\beta$	$\frac{4(2a_1+a_2-2a_5-6a_7+2a_9)}{2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9)}$	0	$-\frac{4(2a_1+a_2+a_9)}{\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	0
$\Delta_{2^+}^{\#2} \uparrow a\beta$	0	$-\frac{4}{3(a_0+2a_5-6a_7)}$	0	0	0	0
$\Delta_{2^+}^{\#3} \uparrow a\beta$	$-\frac{4(2a_1+a_2+a_9)}{\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	$-\frac{4(a_0-2a_1-a_2)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	0	0	0
$\mathcal{T}_{2^+}^{\#1} \uparrow a\beta$	0	0	0	$-\frac{8}{a_0k^2}$	0	0
$\Delta_{2^+}^{\#1} \uparrow a\beta\chi$	0	0	0	0	$-\frac{4(2a_1+a_2-2a_5-6a_7+2a_9)}{2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9)}$	$-\frac{4(2a_1+a_2+a_9)}{\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$
$\Delta_{2^+}^{\#2} \uparrow a\beta\chi$	0	0	0	0	$-\frac{4(2a_1+a_2+a_9)}{\sqrt{3}(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$	$-\frac{4(a_0-2a_1-a_2)}{3(2(2a_1+a_2)(a_5+3a_7)+a_9^2+a_0(2a_1+a_2-2a_5-6a_7+2a_9))}$

Source constraints/gauge generators	Multiplicities
$SO(3)$ irreps	
$\gamma_{0^{+}2}^{+} = 0$	1
$\Delta_{0^{+}2}^{+} + 3\Delta_{0^{+}2}^{+*} = 2\Delta_{0^{+}4}^{+}$	1
$\Delta_{0^{+}2}^{+} = 0$	1
$\gamma_{1^{+}1}^{+} = 0$	3
$2\Delta_{1^{+}2}^{+6\alpha} + \Delta_{1^{+}2}^{+5\alpha} = \Delta_{1^{+}1}^{+4\alpha} + \Delta_{1^{+}2}^{+3\alpha}$	3
$\Delta_{1^{+}2}^{+5\alpha} = \Delta_{1^{+}2}^{+4\alpha}$	3
Total constraints:	12

$$\begin{array}{c} \Gamma_{\frac{1}{3}}^{\#1} + \alpha\beta\chi \\ \frac{3}{4}(a_0 + 2a_5 - 6a_7) \end{array} \quad \begin{array}{c} \Delta_{\frac{1}{3}}^{\#1} + \alpha\beta\chi \\ \frac{4}{3(a_0 + 2a_5 - 6a_7)} \end{array}$$

[illegible]

	$\Gamma_0^{\#1}$	$\Gamma_0^{\#2}$	$\Gamma_0^{\#3}$	$\Gamma_0^{\#4}$	$h_0^{\#1}$	$h_0^{\#2}$	$\Gamma_0^{\#1}$
$\Gamma_0^{\#1} \uparrow$	0	0	0	0	0	0	0
$\Gamma_0^{\#2} \uparrow$	$\frac{1}{4}(-3a_0-2(a_5+4a_6-7a_7))$	$a_5-2a_6-a_7$	$\frac{-3a_0+2(a_5-8a_6+5a_7)}{4\sqrt{2}}$	0	0	0	0
$\Gamma_0^{\#3} \uparrow$	$a_5-2a_6-a_7$	$\frac{1}{4}(-3a_0-2(a_5+4a_6-7a_7))$	$\frac{-3a_0+2(a_5-8a_6+5a_7)}{4\sqrt{2}}$	0	0	0	0
$\Gamma_0^{\#4} \uparrow$	$\frac{-3a_0+2(a_5-8a_6+5a_7)}{4\sqrt{2}}$	$\frac{-3a_0+2(a_5-8a_6+5a_7)}{4\sqrt{2}}$	$\frac{1}{4}(-3a_0-2(a_5-8a_6+5a_7))$	0	0	0	0
$h_0^{\#1} \uparrow$	0	0	0	0	$\frac{a_0\mu^2}{4}$	0	0
$h_0^{\#2} \uparrow$	0	0	0	0	0	0	0
$\Gamma_0^{\#1} \uparrow$	0	0	0	0	0	$-\frac{a_0}{2}-2a_1+2a_2$	

	$\Delta_0^{\#1}$	$\Delta_0^{\#2}$	$\Delta_0^{\#3}$	$\Delta_0^{\#4}$	$\mathcal{T}_0^{\#1}$	$\mathcal{T}_0^{\#2}$	$\Delta_0^{\#1}$
$\Delta_0^{\#1} \dagger$	0	0	0	0	0	0	0
$\Delta_0^{\#2} \dagger$	0	$-\frac{2}{3(a_0+2a_5-6a_7)} - \frac{1}{6a_0-4(a_5-8a_6+5a_7)}$	$-\frac{2}{3(a_0+2a_5-6a_7)} - \frac{1}{6a_0-4(a_5-8a_6+5a_7)}$	$-\frac{1}{\sqrt{2}(3a_0-2(a_5-8a_6+5a_7))}$	0	0	0
$\Delta_0^{\#3} \dagger$	0	$-\frac{2}{3(a_0+2a_5-6a_7)} - \frac{1}{6a_0-4(a_5-8a_6+5a_7)}$	$-\frac{2}{3(a_0+2a_5-6a_7)} - \frac{1}{6a_0-4(a_5-8a_6+5a_7)}$	$-\frac{1}{\sqrt{2}(3a_0-2(a_5-8a_6+5a_7))}$	0	0	0
$\Delta_0^{\#4} \dagger$	0	$-\frac{1}{\sqrt{2}(3a_0-2(a_5-8a_6+5a_7))}$	$-\frac{1}{\sqrt{2}(3a_0-2(a_5-8a_6+5a_7))}$	$-\frac{1}{-3a_0+2(a_5-8a_6+5a_7)}$	0	0	0
$\mathcal{T}_0^{\#1} \dagger$	0	0	0	0	$\frac{4}{a_0 t^2}$	0	0
$\mathcal{T}_0^{\#2} \dagger$	0	0	0	0	0	0	0
$\Delta_0^{\#1} \dagger$	0	0	0	0	0	0	$-\frac{2}{a_0+4a_1-4a_2}$

	$\Gamma_{2^+ \alpha \beta}^{1^+}$	$\Gamma_{2^+ \alpha \beta}^{2^+}$	$\Gamma_{2^+ \alpha \beta}^{3^+}$	$h_{2^+ \alpha \beta}^{1^+}$	$\Gamma_{2^+ \alpha \beta \chi}^{1^+}$	$\Gamma_{2^+ \alpha \beta \chi}^{2^+}$
$\Gamma_{2^+}^{1^+ \alpha \beta}$	$\frac{1}{4} (a_0 - 2 a_1 - a_2)$	0	$-\frac{1}{4} \sqrt{3} (2 a_1 + a_2 + a_9)$	0	0	0
$\Gamma_{2^+}^{2^+ \alpha \beta}$	0	$-\frac{3}{4} (a_0 + 2 a_5 - 6 a_7)$	0	0	0	0
$\Gamma_{2^+}^{3^+ \alpha \beta}$	$\frac{1}{4} \sqrt{3} (2 a_1 + a_2 + a_9)$	0	$-\frac{3}{4} (2 a_1 + a_2 - 2 a_5 - 6 a_7 + 2 a_9)$	0	0	0
$h_{2^+}^{1^+ \alpha \beta}$	0	0	0	$-\frac{a_0 \kappa^2}{8}$	0	0
$\Gamma_{2^+}^{1^+ \alpha \beta \chi}$	0	0	0	0	$\frac{1}{4} (a_0 - 2 a_1 - a_2)$	$-\frac{1}{4} \sqrt{3} (2 a_1 + a_2 + a_9)$
$\Gamma_{2^+}^{2^+ \alpha \beta \chi}$	0	0	0	0	$-\frac{1}{4} \sqrt{3} (2 a_1 + a_2 + a_9)$	$-\frac{3}{4} (2 a_1 + a_2 - 2 a_5 - 6 a_7 + 2 a_9)$

$J^P = 1^-$   
 $K^0$

Massive particle	
Pole residue:	$\frac{1}{4a_{13}} > 0$
Polarisations:	3
Square mass:	$\frac{-3a_0 + 2(a_5 - 8a_6 + 5a_7)}{8a_{13}} > 0$
Spin:	1
Parity:	Odd

$K^0$

Quadratic pole	
Pole residue:	$-\frac{1}{a_0} > 0$
Polarisations:	2

$$a_0 < 0 \ \&\& \ a_7 > \frac{1}{10} (3a_0 - 2a_5 + 16a_6) \ \&\& \ a_{13} > 0$$
