

Wave operator and propagator

| | $1^+ \mathcal{A}_5^+ \uparrow_{a\beta}$ | $1^+ h^+_{\alpha}$ | $1^+ \mathcal{A}_5^+ \uparrow_{\alpha}$ | $1^+ \mathcal{A}_5^+ h^+_{\alpha}$ | $1^+ \mathcal{A}_5^+ h^+_{\alpha}$ | $1^+ \mathcal{A}_5^+ h^+_{\alpha}$ | Spin-parity |
|---------------------------------------------|---------------------------------------------|-------------------------------------------|---------------------------------------------------------------|----------------------------------------------------------------------------|----------------------------------------------------------------------------|--------------------------------------------------------------------|----------------------------------------|
| $1^+ \mathcal{A}_5^+ \uparrow^{a\beta}$ | $\frac{1}{4} (a_0 + k^2 (h_{10} - h_{-9}))$ | 0 | 0 | 0 | 0 | 0 | $k^0 1^+ \mathcal{W}_5^+ \uparrow + 2$ |
| $1^+ h^+ \uparrow^{\alpha}$ | 0 | 0 | $-\frac{i a_0 k}{4 \sqrt{6}}$ | $\frac{1}{4} i \sqrt{\frac{5}{6}} a_0 k$ | $\frac{i a_0 k}{8 \sqrt{3}}$ | $-\frac{i a_0 k}{4 \sqrt{6}}$ | $2 k^1 1^+ \mathcal{W}_5^+ h^{\alpha}$ |
| $1^+ \mathcal{A}_5^+ \uparrow^{\alpha}$ | 0 | $\frac{i a_0 k}{4 \sqrt{6}}$ | $\frac{1}{6} (-2 a_0 - k^2 (h_{11} + h_{+7} + h_{+9}))$ | $\frac{1}{6} \sqrt{5} (a_0 + k^2 (h_{10} + h_{+7} + h_{+8}))$ | $\frac{a_0 + 2 k^2 (h_{11} + h_{+7} + h_{+9})}{12 \sqrt{2}}$ | $\frac{1}{12} (a_0 + k^2 (4 h_{10} + h_{+7} - 2 h_{+8}))$ | Total expectation value |
| $1^+ \mathcal{A}_5^+ h^+ \uparrow^{\alpha}$ | 0 | $-\frac{1}{4} i \sqrt{\frac{5}{6}} a_0 k$ | $\frac{1}{6} \sqrt{5} (a_0 + k^2 (h_{10} + h_{+7} + h_{+8}))$ | $\frac{1}{6} (2 a_0 - 5 k^2 (h_{11} + h_{+7} + h_{+9}))$ | $\frac{1}{12} \sqrt{\frac{5}{2}} (a_0 - 2 k^2 (h_{10} + h_{+7} + h_{+8}))$ | $\frac{1}{12} \sqrt{5} (a_0 - k^2 (h_{11} - 2 h_{+7} + 4 h_{+9}))$ | $S = \iiint d\mathbf{r} \dots$ |
| $1^+ \mathcal{A}_5^+ h^+ \uparrow^{\alpha}$ | 0 | $-\frac{i a_0 k}{8 \sqrt{3}}$ | $\frac{a_0 + 2 k^2 (h_{11} + h_{+7} + h_{+9})}{12 \sqrt{2}}$ | $\frac{1}{12} \sqrt{\frac{5}{2}} (a_0 - 2 k^2 (h_{10} + h_{+7} + h_{+8}))$ | $\frac{1}{12} (a_0 - k^2 (h_{11} + h_{+7} + h_{+9}))$ | $\frac{-4 a_0 - k^2 (4 h_{10} + h_{+7} - 2 h_{+8})}{12 \sqrt{2}}$ | |
| $1^+ \mathcal{A}_5^+ h^+ \uparrow^{\alpha}$ | 0 | $\frac{i a_0 k}{4 \sqrt{6}}$ | $\frac{1}{12} (a_0 + k^2 (4 h_{10} + h_{+7} - 2 h_{+8}))$ | $\frac{1}{12} \sqrt{5} (a_0 - k^2 (h_{11} - 2 h_{+7} + 4 h_{+9}))$ | $\frac{-4 a_0 - k^2 (4 h_{10} + h_{+7} - 2 h_{+8})}{12 \sqrt{2}}$ | $\frac{1}{12} (-a_0 + 2 k^2 (2 h_{11} - h_{+7} - 4 h_{+9}))$ | |

| Form | Covariant form | Multiplicity |
|-------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------|
| $f^0{}_i \tau^{-1} = 0$ | $\partial_\rho \partial_\sigma \mathcal{T}^{\alpha\beta} =: \partial_\rho \partial_\sigma \mathcal{V}^{\alpha\beta\gamma}$ | 1 |
| $+k \, 1 \, \omega_s^{\perp\alpha} + 6 \, i \, 1 \, \tau^{-\alpha} = 0$ | $\partial_\chi \partial_\rho \partial^\sigma \mathcal{T}^{\alpha\beta} + \partial_\sigma \partial^2 \partial_\chi \partial_\rho \mathcal{W}^{\alpha\beta\gamma} =: 2 \, \partial_\chi \partial^\alpha \partial^\beta \mathcal{T}^{\gamma\delta} + \partial_\sigma \partial_\chi \partial_\rho \partial^\sigma \mathcal{V}^{\alpha\beta\gamma} = 0$ | 3 |
| Red gauge generators: | | 4 |

$$\begin{aligned} & \frac{1}{4}(-2a_0\mathcal{A}_{\alpha\beta}\mathcal{A}^{\alpha\beta}+2a_0\mathcal{A}^{\alpha}{}_{\beta}\mathcal{A}^{\beta}{}_{\alpha}+4\mathcal{A}^{\alpha\beta}\mathcal{W}_{\alpha\beta\chi}+4\mathcal{T}^{\alpha\beta}h_{\alpha\beta}+2a_0h^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\alpha\chi}-2a_0h^{\alpha\beta}\partial_{\chi}\mathcal{A}^{\chi}{}_{\alpha\beta}-a_0h^{\alpha}{}_{\alpha}\partial_{\chi}\mathcal{A}^{\beta}{}_{\beta\chi}+a_0h^{\alpha}{}_{\alpha}\partial_{\chi}\mathcal{A}^{\beta\chi}{}_{\beta}-2h_8\partial_{\beta}\mathcal{A}^{\chi}{}_{\chi}\partial^{\chi}\mathcal{A}^{\alpha\beta}{}_{\alpha}-2h_{12}\partial_{\beta}\mathcal{A}^{\chi}{}_{\chi}\partial^{\chi}\mathcal{A}^{\alpha}{}_{\beta}-2h_7\partial_{\chi}\mathcal{A}^{\chi}{}_{\beta}\partial^{\chi}\mathcal{A}^{\alpha}{}_{\beta}-2h_{11}\partial_{\chi}\mathcal{A}^{\chi}{}_{\beta\delta}\partial^{\chi}\mathcal{A}^{\alpha}{}_{\beta}-2h_{10}\partial_{\beta}\mathcal{A}^{\chi}{}_{\chi}\partial^{\chi}\mathcal{A}^{\alpha\beta}{}_{\alpha}-2h_9\partial_{\chi}\mathcal{A}^{\chi}{}_{\beta\delta}\partial^{\chi}\mathcal{A}^{\alpha\beta}{}_{\alpha}-2h_7\partial_{\beta}\mathcal{A}^{\alpha\beta}\partial_{\chi}\mathcal{A}^{\chi}{}_{\alpha\chi}-2h_8\partial_{\beta}\mathcal{A}^{\alpha\beta}\partial_{\chi}\mathcal{A}^{\chi}{}_{\alpha\beta}-2h_{10}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+2h_{12}\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+4h_{10}\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\alpha}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}-2h_{11}\partial_{\alpha}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}-2h_{12}\partial_{\alpha}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+4h_7\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+4h_8\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+2h_{11}\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+2h_{12}\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}-2h_9\partial_{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+2h_{11}\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi}+4h_9\partial^{\chi}\mathcal{A}^{\alpha\beta}\partial_{\beta}\mathcal{A}^{\chi}{}_{\beta\chi})[t,x,y,z]dzdzdydxdt \end{aligned}$$

$$3: \mathcal{W}_S^{\perp} + \alpha \beta x$$

$$3:\mathcal{A}_5 + \alpha\beta X \quad 3:\mathcal{A}_5 \alpha\beta X \quad \frac{4}{-2}$$

$$\begin{aligned} & a_{\alpha} \partial_x \mathcal{A}^{\beta \chi}_{\beta} - 2 h_{\beta} \partial_{\beta} \mathcal{A}^{\delta}_{\chi} \partial^{\chi} \mathcal{A}^{\alpha \beta}_{\alpha} - 2 h_{12} \partial_{\beta} \mathcal{A}^{\delta}_{\chi} \partial^{\chi} \mathcal{A}^{\alpha \beta}_{\alpha} - 2 h_7 \partial_x \mathcal{A}^{\delta}_{\beta} \partial^{\chi} \mathcal{A}^{\alpha \beta}_{\alpha} - 2 h_{11} \partial_x \mathcal{A}^{\delta}_{\beta} \partial^{\chi} \mathcal{A}^{\alpha \beta}_{\alpha} \\ & \partial_{\alpha} \mathcal{A}^{\alpha \beta \chi}_{\beta} \partial_{\delta} \mathcal{A}^{\delta}_{\beta \chi} - 2 h_{12} \partial_{\alpha} \mathcal{A}^{\alpha \beta \chi}_{\beta} \partial_{\delta} \mathcal{A}^{\delta}_{\beta \chi} + \\ & (\partial^{\chi} \mathcal{A}^{\alpha \beta}_{\alpha} \partial_{\delta} \mathcal{A}^{\delta}_{\chi \beta} + 4 h_{\beta} \partial^{\chi} \mathcal{A}^{\alpha \beta}_{\alpha} \partial_{\delta} \mathcal{A}^{\delta}_{\chi \beta})) [t, x, y, z] d z d y d x d t \end{aligned}$$

| | $0^+ \mathcal{T}^\perp$ | $0^+ \mathcal{T}^\parallel$ | $0^+ \mathcal{W}_5^{\perp t}$ | $0^+ \mathcal{W}_5$ |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------|----------------------------------------------------------|-----------------------------------------------------------------------|----------------------------|
| $0^+ \mathcal{T}^\perp \uparrow$ | $\frac{4k^2(-a_0+2k^2(7h_0+3(h_0+h_1+h_2+h_3)+7h_9))}{3a_0^2(4+k^2)^2}$ | $\frac{8k^2(2h_0+h_1+h_2+2h_9)}{\sqrt{3}a_0^2(4+k^2)^2}$ | $\frac{8lk(a_0-2k^2(7h_0+3(h_0+h_1+h_2+h_3)+7h_9))}{3a_0^2(4+k^2)^2}$ | $\frac{10lk}{3a_0(4+k^2)}$ |
| $0^+ \mathcal{T}^\parallel \uparrow$ | $\frac{8k^2(2h_0+h_1+h_2+2h_9)}{\sqrt{3}a_0^2(4+k^2)^2}$ | $\frac{4(a_0+2k^2(h_0+h_1+h_2+h_3+h_9))}{a_0^2k^2}$ | $\frac{16lk(2h_0+h_1+h_2+2h_9)}{\sqrt{3}a_0^2(4+k^2)^2}$ | $\frac{2l}{\sqrt{3}a_0}$ |
| $0^+ \mathcal{W}_5^{\perp t} \uparrow$ | $\frac{8lk(a_0-2k^2(7h_0+3(h_0+h_1+h_2+h_3)+7h_9))}{3a_0^2(4+k^2)^2}$ | $\frac{16lk(2h_0+h_1+h_2+2h_9)}{\sqrt{3}a_0^2(4+k^2)^2}$ | $\frac{16(a_0+2k^2(7h_0+3(h_0+h_1+h_2+h_3)+7h_9))}{3a_0^2(4+k^2)^2}$ | $\frac{20}{3a_0(4+k^2)}$ |
| $\delta_{\beta\delta}\partial^\alpha\mathcal{A}^\beta_\alpha-2h_{10}\delta_{\beta\alpha}\mathcal{A}^\delta_\chi\partial^\chi\mathcal{A}^{ab}_\alpha-2h_9\partial_\chi\mathcal{A}^\delta_{\beta\delta}\partial^\chi\mathcal{A}^{ab}_\alpha-2$ | | | | |
| $0^+ \mathcal{W}_5^\perp \downarrow$ | $-\frac{10lk}{12a_0+3a_0k^2}$ | $\frac{2l}{\sqrt{3}a_0k}$ | $-\frac{20}{12a_0+3a_0k^2}$ | 0 |
| $0^+ \mathcal{W}_5^{\perp h} \downarrow$ | $-\frac{4l\sqrt{2}k}{12a_0+3a_0k^2}$ | $-\frac{4l\sqrt{\frac{2}{3}}}{a_0k}$ | $-\frac{8\sqrt{2}}{12a_0+3a_0k^2}$ | 0 |

| \parallel | $0^+ \mathcal{W}_S^{\pm h}$ | $0^+ h^+$ | $0^+ h^0$ | $0^+ \mathcal{A}_S^{\pm t}$ | $0^+ \mathcal{A}_S^{\parallel}$ |
|----------------|-----------------------------------|-----------------------------|---------------------------------|-----------------------------|---------------------------------|
| $\binom{+}{-}$ | $\frac{4i\sqrt{2}k}{3a_0(4+k^2)}$ | 0 | 0 | 0 | $\frac{i a_k}{4}$ |
| $-k$ | $\frac{4i\sqrt{2}}{a_0 k}$ | 0 | 0 | 0 | $-\frac{i a_k}{4\sqrt{3}}$ |
| $\binom{-}{+}$ | $\frac{8\sqrt{2}}{3a_0(4+k^2)}$ | 0 | 0 | 0 | $\frac{a_0}{2}$ |
| 0 | 0 | $0^+ \mathcal{A}_S^{\pm t}$ | $0^+ \mathcal{A}_S^{\parallel}$ | $0^+ \mathcal{A}_S^{\pm t}$ | $0^+ \mathcal{A}_S^{\parallel}$ |
| 0 | 0 | $0^+ \mathcal{W}_S^{\pm h}$ | $0^+ \mathcal{W}_S^{\pm h}$ | $0^+ \mathcal{W}_S^{\pm h}$ | $0^+ \mathcal{W}_S^{\pm h}$ |

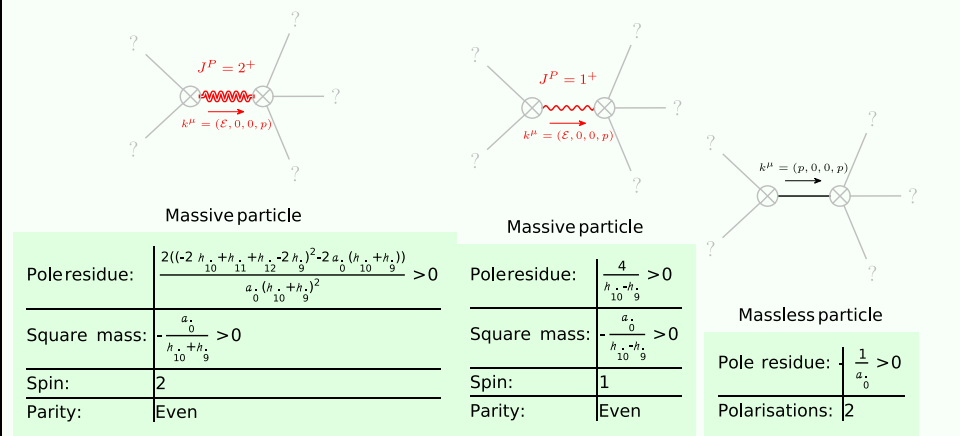
| | | |
|-------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------|----------------------------------------------------------------------------|
| $0^+ \mathcal{A}_s^{i,h}$ | $2^+ \mathcal{T}^1 \uparrow^{a\beta}$ | $-8 \frac{a_-^2}{0} + 8 \frac{a_+^2}{0} k^2 \left(\phi_1, \phi_2 \right)$ |
| $\frac{i \, a_+ \, k}{8 \sqrt{2}}$ | $2^+ \mathcal{W}_s^1 \uparrow^{a\beta}$ | . |
| $\frac{5 \, i \, a_+ \, k}{8 \sqrt{6}}$ | $2^+ \mathcal{W}_s^1 \uparrow^{a\beta}$ | $2 \, i \sqrt{}$ |
| $\frac{a_-}{4 \sqrt{2}}$ | $2^+ \mathcal{W}_s^1 \uparrow^{a\beta}$ | |
| $\frac{3 a_+ + 2 k^2 (-5 \frac{h_-}{10} - 2 \frac{h_-}{11} - 2 \frac{h_-}{12} + \frac{h_+}{7} + \frac{h_+}{8} - 5 \frac{h_+}{9})}{12 \sqrt{2}}$ | $2^+ \mathcal{W}_s^1 \uparrow^{a\beta X}$ | |
| $\frac{1}{12} (-3 a_+ - k^2 (13 \frac{h_-}{10} - 8 \frac{h_-}{11} - 8 \frac{h_-}{12} + 7 (h_+ + \frac{h_+}{7} + 13 \frac{h_+}{8})))$ | | |

| $2^i \mathcal{T}_{a\bar{b}}^i$ | $2^i \mathcal{W}_{S^1 a\bar{b}}^i$ | $2^i \mathcal{W}_{S^1 a\bar{b}}^i$ |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------|
| $\frac{-\frac{1}{2}(h_1+h_2+h_3)-2k^2(\frac{h_1+h_2}{10}+\frac{h_3}{9})^2-4(h_1+h_2)(\frac{h_1}{10}+\frac{h_2}{9})}{a_0^2 k^2(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ | $\frac{4i(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}+\frac{h_3}{12}+\frac{h_3}{9}))}{\sqrt{3}a_0k(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ | $\frac{2i\sqrt{\frac{2}{3}}(4a_0+k^2(2h_1+h_2+\frac{h_3}{10}))}{a_0k(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ |
| $\frac{4i(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}+\frac{h_3}{12}+\frac{h_3}{9}))}{\sqrt{3}a_0k(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ | $-\frac{8}{3(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ | $\frac{4\sqrt{2}}{3(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ |
| $\frac{\frac{\sqrt{2}}{3}(4a_0+k^2(2h_1+h_2+\frac{h_3}{10}+\frac{h_3}{12}+\frac{h_3}{9}))}{a_0k(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ | $\frac{4\sqrt{2}}{3(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ | $-\frac{4}{3(a_0+k^2(\frac{h_1}{10}+\frac{h_2}{9}))}$ |
| 0 | 0 | 0 |

| | | | |
|--------------------------------------------------------------------------------|-----------------------------------------------------------|-------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $2^+ \mathcal{W}_s^{\perp}{}_{a\beta\chi}$ | | $2^+ h^{\perp}{}_{a\beta}$ | $2^+ \mathcal{I}_s^{\perp}{}_{a\beta}$ |
| $\left(\begin{smallmatrix} h_{12}^+ + 2n_{12}^+ \\ \end{smallmatrix} \right)$ | 0 | 0 | $-\frac{i a_0 k}{4 \sqrt{3}}$ |
| $\left(\begin{smallmatrix} \end{smallmatrix} \right)$ | 0 | $2^+ \mathcal{I}_s^{\perp}{}_{11}^{\perp}{}_{a\beta}$ | $\frac{i a_0 k}{4 \sqrt{3}} \frac{1}{6} (-3 a_0 - k^2 \left(\begin{smallmatrix} h_{10}^+ + h_{11}^+ + h_{12}^+ + h_{78}^+ + h_{89}^+ \end{smallmatrix} \right))$ |
| $\left(\begin{smallmatrix} \end{smallmatrix} \right)$ | 0 | $2^+ \mathcal{I}_s^{\perp}{}_{11}^{\perp}{}_{a\beta}$ | $\frac{i a_0 k}{2 \sqrt{6}} \frac{k^2 (2 n_{10}^+ + n_{11}^+ + n_{12}^+ - 4 (h_{10}^+ + h_{89}^+) + 2 n_{89}^+)}{12 \sqrt{2}}$ |
| $\frac{4}{a_0}$ | $2^+ \mathcal{I}_s^{\perp}{}_{11}^{\perp}{}_{a\beta\chi}$ | 0 | 0 |

| | |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------|
| $2^{\cdot} \mathcal{A}_{\alpha\beta}^{\cdot}$ | $2^{\cdot} \mathcal{A}_{\alpha\beta}^{\cdot}$ |
| $\frac{i \frac{0}{\alpha}}{2 \sqrt{6}}$ | 0 |
| $\frac{k^2 (2 \, h_{\frac{10}{10}} \, h_{\frac{11}{11}} \, h_{\frac{12}{12}} \, 4 (h_{\frac{7}{7}} + h_{\frac{8}{8}}) + 2 \, h_{\frac{9}{9}})}{12 \sqrt{2}}$ | 0 |
| $\frac{1}{12} (3 a_{\frac{0}{0}} \cdot k^2 (h_{\frac{10}{10}} \cdot -2 \, h_{\frac{11}{11}} \cdot -2 \, h_{\frac{12}{12}} + 4 (h_{\frac{7}{7}} + h_{\frac{8}{8}}) + h_{\frac{9}{9}}))$ | 0 |
| 0 | $\frac{0}{4}$ |

Massive and massless spectra



Unitarity conditions

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