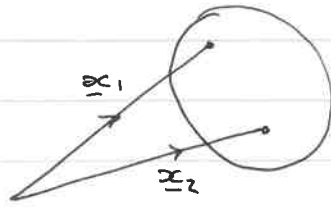


Nice solution to 3B:



$$\begin{aligned}\underline{\dot{x}} &= \underline{x}_2 - \underline{x}_1 \\ \underline{\ddot{x}} &= \underline{\ddot{x}}_2 - \underline{\ddot{x}}_1 \\ &= -(\nabla\phi|_{x_2} - \nabla\phi|_{x_1})\end{aligned}$$

$$\begin{aligned}\text{And } \nabla^2\phi &= 4\pi\rho(x) \\ \text{so } \nabla \cdot \underline{\ddot{x}} &= 0\end{aligned}$$

$$\text{Take out one time derivative: } \frac{d}{dt} \nabla \cdot \underline{u} = 0 \quad \text{where } \underline{u} = \underline{\dot{x}}$$

$$\Rightarrow \nabla \cdot \underline{u} = a \quad (a = \text{constant})$$

And stationary initial conditions, so  $a = 0$ .

$$\nabla \cdot \underline{u} = 0$$

This is the equation of motion for an incompressible fluid flow. i.e. the volume does not change.

Courtesy of C. Moore.