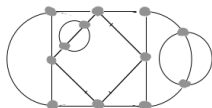


# Fishing nets

- The Euler–Poincaré theorem for *any* convex 3d polyhedron with  $C$  corners,  $E$  edges and  $F$  faces is  $C - E + F = 2$ .



A random 2d fishing net is made from  $R$  identical ropes joined by  $K$  identical knots, such that there are  $H$  holes. The *total* underwater weight  $W$  (in Newtons) of the net containing one dead fish is  $W = 4H - 2R$ . What are the submerged weights of any rope, any knot, and the fish?



$$\begin{aligned} R &= 12 \\ K &= 14 \\ H &= 1 \end{aligned}$$

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- ▶ You just obtained the formula  $W = 2R - 4K + 4$ . Now you discover that each knot connects  $k$  ropes. The net is positioned by  $G$  guide ropes with free ends, whose weights are neglected. Find  $k$  such that for given  $G$ , a sufficiently complicated net always sinks with the fish.

