# maeve long-form overview

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#### Abstract

This document contains lots of working commands with real data sets, but with minimal explanation. There is a companion manuscript in preparation to discuss the problems we address in translational oncology and theoretical aspects of the models and summary measures employed.

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#### 1 Introduction

The R package maeve coordinates fitting of linear and generalized additive mixed models for normally distributed longitudinal data from multi-group studies with multiple subjects per group, then computes one statistical summary per group and compares the resulting summary statistics across groups. The motivating application is to tumor volume growth data from mouse studies in translational oncology. Below are a number of detailed maeve code examples with real data. This vignette is light on conceptual motivation or explanation, for which readers should see the companion manuscript.

```
## This is a vignette for `maeve`. Here are `R` packages used in the analysis:
##
suppressPackageStartupMessages( library( magrittr ) )
suppressPackageStartupMessages( library( maeve ) ) # in GRAN
suppressPackageStartupMessages( library( ggplot2 ) )
##
options( width = 110 )
##
ggplot2::theme_set( switch( 2, theme_grey(), theme_bw() ) )
##
```

# Option management with maeve\_options(), maeve\_reset(), and maeve\_defaults()

The package settings is used to establish a local version of an options list that can be incorporated into package functions and locally over-ruled as needed. These options are managed by the functions maeve\_options(), maeve\_reset(), and maeve\_defaults().

```
###
### script with commands for maeve demonstration

### maeve_options(), maeve_reset()
###
### Options will persist and provide a shared set of
### arguments to maeve functions. They can be inpected
### or reset individually with the function `maeve_options()`.
###
### The function 'maeve_reset()` will reset all options to
### their default values.
###
### The function `maeve_defaults()` will list the package
### default values for the argument given (e.g.,
### 'maeve_defaults("endpoint_name")'), or all the default
### values if called with no arguments: 'maeve_defaults()'.
maeve_options('group_name')
```

```
## [1] "group_name"
maeve_options('subject_ID')
```

```
## [1] "animalID"
maeve_options('x_name')
## [1] "DAY_OF_STUDY"
maeve_options('endpoint_name')
## [1] "TUMOR_VOLUME"
maeve_options('reference_Dunnett')
## NULL
### reset names of variables in the maeve_options() list so that package functions can access them:
maeve_options( group_name = 'assay_rep',
               subject_ID = 'cell_line',
                 'x_name' = 'log_concentration', # option names (left-hand side) can be quoted or unquoted.
            endpoint_name = 'OD',
       reference_Dunnett = 'my favorite reference'
## See that they're changed:
maeve_options( 'group_name' , 'subject_ID', 'x_name', 'endpoint_name', 'reference_Dunnett' )
## $group_name
## [1] "assay_rep"
##
## $subject_ID
## [1] "cell_line"
##
## $x_name
## [1] "log_concentration"
## $endpoint_name
## [1] "OD"
## $reference_Dunnett
## [1] "my favorite reference"
## But information on original values is always available from maeve_defaults(), which
## will not change anything:
maeve_defaults( 'group_name' , 'subject_ID', 'x_name', 'endpoint_name', 'reference_Dunnett' )
## $group_name
## [1] "group_name"
##
## $subject_ID
## [1] "animalID"
##
## $x_name
## [1] "DAY_OF_STUDY"
##
## $endpoint_name
## [1] "TUMOR_VOLUME"
## $reference_Dunnett
## NULL
## Return all the options to package defaults with the maeve_reset() function:
maeve_reset()
## See that they've returned to the original values:
```

```
maeve_options( 'group_name' , 'subject_ID', 'x_name', 'endpoint_name', 'reference_Dunnett' )
## $group_name
## [1] "group_name"
## $subject_ID
## [1] "animalID"
##
## $x_name
## [1] "DAY_OF_STUDY"
##
## $endpoint_name
## [1] "TUMOR_VOLUME"
##
## $reference_Dunnett
## NULL
 ## Here are all the option names:
names( maeve_options( ) )
   [1] "group_name"
                                   "subject_ID"
                                                              "trace_ID"
                                                                                         "x_name"
                                   "EOS_CR_minval"
   [5] "endpoint_name"
                                                              "PR_threshold"
                                                                                         "summary_first_day"
## [9] "full_study_data_frame"
                                   "modeling_data_frame"
                                                              "autoset_full_study_data"
                                                                                         "autoset_modeling_data"
## [13] "truncate_fit"
                                   "truncation_return_type"
                                                              "truncated_group_levels"
                                                                                         "min_n_in_group"
## [17] "min_frac_in_group"
                                   "min_frac_in_study"
                                                              "overall_x_min"
                                                                                         "overall_x_max"
## [21] "abbreviate_n"
                                   "reference_Dunnett"
                                                              "add_to_endpoint"
                                                                                         "restrict_x"
## [25] "number_basis_vecs"
                                   "min_basis_vecs"
                                                              "max_basis_vecs"
                                                                                         "trans_func_char"
## [29] "inv_func_char"
                                   "test_func_x"
                                                                                         "metric"
                                                              "weight_lmer_option"
## [33] "metrics_supported"
                                   "N_integration_grid"
                                                              "contrast"
                                                                                         "xrange_norm_method"
## [37] "progress"
                                   "number_break_points"
                                                              "break_points"
                                                                                         "adjust_break_points"
## [41] "poly_degree"
                                                                                         "x_pred_type"
                                   "poly_object"
                                                              "mismatch_action"
## [45] "x_pred_vec"
                                   "x_pred_spacing"
                                                              "x_pred_interior_grid"
                                                                                         "include_newdata_ID"
## [49] "title_label"
                                   "y_label"
                                                              "x_label"
                                                                                         "legend_position_char"
                                                              "axis_text_x_hjust"
                                                                                         "axis_text_x_vjust"
## [53] "axis_text_x_angle"
                                   "axis_text_x_size"
                                   "legend_text_size"
## [57] "axis_text_y_size"
                                                              "strip_text_size"
                                                                                         "linear_predictor"
## [61] "linear_color"
                                   "linear_lwd"
                                                              "spline_predictor"
                                                                                         "spline_color"
## [65] "spline_lwd"
                                   "piecewise_predictor"
                                                              "piecewise_color"
                                                                                         "piecewise_lwd"
## [69] "poly_predictor"
                                   "poly_color"
                                                              "poly_lwd"
                                                                                         "geom_na_rm"
## [73] "geom_point_size"
                                   "nrow_value"
                                                              "ncol_value"
                                                                                         "alpha_value"
```

### 3 Data sets in maeve, real and simulated.

Three real data sets are included in the package /data directory: vismodegib, palb\_temo\_01, and gdc0084\_temo\_01.

```
data_set_names <- data( package = 'maeve' )
data_set_names <- data_set_names$results[,'Item']
print( data_set_names )</pre>
```

```
## [1] "gdc0084_temo_01" "palb_temo_01" "vismodegib"
```

Several simulated data sets are in the /inst/extdata directory.

### 4 Optional QC with check\_study\_data\_frame()

The function check\_study\_data\_frame() takes a data frame intended for analysis in maeve and does a number of checks on columns designated by group\_name, subject\_ID, x\_name, and endpoint\_name. This step is optional (e.g., check that levels of subject\_ID are nested within levels of group\_name). You do not need to run the data frame through check\_study\_data\_frame(), but it encapsulates many QC checks for sometimes subtle but common formatting issues that would then crop up down the road in harder-to-trace guises.

```
### check_study_data_frame() basics
### `check_study_data_frame()` takes a data frame and
### returns another data.frame after doing some QC checks.
### In brief:
### It looks at maeve_options() and finds the four columns
### matching 'group_name', 'subject_ID', 'x_name', and 'endpoint_name'
###
### (1) 'group_name' and 'subject_ID' must be factors.
### (2) 'subject_ID' must be nested within 'group_name'.
### (3) 'xname' must be numeric.
### (4) 'endpoint_name' must be numeric.
### By default it returns just these four columns.
maeve_reset()
data( vismodegib, package = 'maeve' ) # cleanly formatted version of "hedgehog" data
### Make a mis-formatted version of the vismodegib data by converting 'animalID' to character
### and 'DAY_OF_STUDY' to integer:
vismo_bad_format <-</pre>
     vismodegib %>%
     dplyr::mutate( animalID = as.character( animalID ), # started as a factor
                    DAY_OF_STUDY = as.integer( DAY_OF_STUDY ) # started as a numeric
### maeve::check_study_data_frame() will return warnings about these
### mis-formatted fields and by default convert the 'animalID' field
### to a factor and the 'DAY_OF_STUDY' field to a numeric:
vismo_fixed_format <- maeve::check_study_data_frame( vismo_bad_format )</pre>
## Warning in maeve::check_study_data_frame(vismo_bad_format): Converting animalID to factor in
## maeve::check_study_data_frame().
## Warning in maeve::check_study_data_frame(vismo_bad_format): Converting DAY_OF_STUDY from integer to numeric in
## maeve::check_study_data_frame().
### If we run the original data frame through 'check study data frame()',
### it returns the four needed columns with no warnings:
vismo_already_OK <- maeve::check_study_data_frame( vismodegib )</pre>
### Check that 'check_study_data_frame()' has fixed the "problems":
identical( vismo_fixed_format, vismo_already_OK )
```

```
## [1] TRUE
### See the output:
vismodegib %>% check_study_data_frame() %>% head( 5 )
     group_name animalID DAY_OF_STUDY TUMOR_VOLUME
## 1
       dose_0.0
                 3810580
                                    0
                                           212.7522
## 2
       dose_0.0
                 3810580
                                    3
                                           283.0926
## 3
                 3810580
                                    6
                                           337.0389
       dose_0.0
## 4
       dose 0.0
                 3810580
                                   10
                                           479.5100
## 5
       dose_0.0 3810580
                                   14
                                           429.2777
### See the output with in-line changes in the
### requested columns (here, e.g., switch from
### "TUMOR_VOLUME" to "BODY_WEIGHT":
###
vismodegib %>% check_study_data_frame( endpoint_name = 'BODY_WEIGHT' ) %>% head( 5 )
     group_name animalID DAY_OF_STUDY BODY_WEIGHT
##
## 1
       dose_0.0 3810580
                                    0
                                    3
                                              29.2
## 2
       dose_0.0
                 3810580
                                    6
## 3
       dose_0.0 3810580
                                              28.8
## 4
       dose_0.0 3810580
                                   10
                                              30.1
       dose_0.0 3810580
                                   14
### You can re-set variable names in maeve_options() and then
### use off-the-shelf tidyverse tools to rename covariates and / or
### define new variables on the fly:
maeve_options( x_name = 'day', endpoint_name = 'log_TUMOR_VOLUME' )
vismodegib %>%
     dplyr::rename( day = DAY_OF_STUDY ) %>%
     dplyr::mutate( log_TUMOR_VOLUME = log( 1 + TUMOR_VOLUME ) ) %>%
     check_study_data_frame() %>%
     head( 10 )
##
      group_name animalID day log_TUMOR_VOLUME
## 1
        dose_0.0 3810580
                            0
                                      5.364818
## 2
       dose 0.0
                  3810580
                            3
                                      5.649300
## 3
       dose_0.0
                  3810580
                            6
                                      5.823161
        dose_0.0 3810580
## 4
                           10
                                      6.174848
## 5
       dose_0.0 3810580
                           14
                                      6.064431
## 6
        dose_0.0 3810580
                           17
                                      6.386843
## 7
        dose_0.0
                 3810580
                                      6.288881
## 8
        dose_0.0
                  3810587
                                      5.415381
## 9
        dose_0.0
                  3810587
                                      5.450238
## 10
       dose_0.0
                  3810587
                                      5.833105
maeve_reset()
```

### 5 Pre-modeling group-level summaries with tally\_study()

The function tally\_study() takes a study data frame and returns one row per group, with a number of summary values that can be computed without longitudinal statistical modeling. By default, it tells the number of subjects per group, the first and last time point with observations from each group, and whether all subjects' observations started or ended on the first or last time point, respectively. Optionally, it can provide simple response rate counts (e.g., partial response, end-of-study complete response) by group, as shown in the examples. These counts also include log odds ratios and asymptotic standard errors relative to

a reference group (by default, the first group in the study). More detail on how these are calculated is in the section End of Study Complete Response and Partial Response later in this document.

```
### tally study(), basics
maeve_reset()
head( vismodegib, 15 )
      study_id group_name cohort_id animalID DAY_OF_STUDY BODY_WEIGHT TUMOR_VOLUME
## 1
         22384
                 dose_0.0
                                 02 3810580
                                                         0
                                                                  28.5
                                                                           212.7522
## 2
         22384
                                                         3
                                                                  29.2
                                                                           283.0926
                 dose_0.0
                                 02
                                     3810580
## 3
         22384
                 dose_0.0
                                 02
                                     3810580
                                                         6
                                                                  28.8
                                                                           337.0389
## 4
         22384
                 dose_0.0
                                 02
                                     3810580
                                                                  30.1
                                                                           479.5100
                                                        10
## 5
         22384
                 dose_0.0
                                 02
                                     3810580
                                                        14
                                                                  29.6
                                                                           429.2777
## 6
         22384
                 dose_0.0
                                 02 3810580
                                                        17
                                                                  30.2
                                                                           592.9786
                 dose_0.0
## 7
         22384
                                 02
                                     3810580
                                                        21
                                                                  29.2
                                                                           537.5505
## 8
         22384
                 dose_0.0
                                 05
                                     3810587
                                                         0
                                                                  24.5
                                                                           223.8383
## 9
         22384
                 dose_0.0
                                 05
                                     3810587
                                                        3
                                                                  23.5
                                                                           231.8135
                                                        7
## 10
         22384
                 dose_0.0
                                 05 3810587
                                                                  25.1
                                                                           340.4171
## 11
         22384
                 dose_0.0
                                 05 3810587
                                                        11
                                                                  24.9
                                                                           401.2144
## 12
         22384
                 dose_0.0
                                 05
                                     3810587
                                                        14
                                                                  25.2
                                                                           389.1488
## 13
         22384
                 dose_0.0
                                 05
                                     3810587
                                                        18
                                                                  25.2
                                                                           390.5655
## 14
         22384
                 dose_0.0
                                 05
                                     3810587
                                                        21
                                                                  25.5
                                                                           483.5132
         22384
                                                                           213.5640
## 15
                 dose_0.0
                                     3810601
                                                                  26.6
### Which maeve options will get used in tallying the study?
maeve_options() %>%
with( print( c( group_name, subject_ID, x_name, endpoint_name ) ) )
                      "animalID"
                                     "DAY_OF_STUDY" "TUMOR_VOLUME"
## [1] "group_name"
### Here is the data frame tally_study() will use:
maeve_options() %>%
with( vismodegib %>%
       dplyr::select(dplyr::one_of(group_name, subject_ID, x_name, endpoint_name)) %>%
      head(15)
##
      group_name animalID DAY_OF_STUDY TUMOR_VOLUME
## 1
       dose_0.0 3810580
                                           212.7522
## 2
       dose_0.0
                 3810580
                                     3
                                           283,0926
                                           337.0389
## 3
       dose_0.0
                  3810580
                                     6
## 4
       dose_0.0 3810580
                                    10
                                           479.5100
## 5
       dose_0.0 3810580
                                    14
                                           429,2777
       dose_0.0 3810580
## 6
                                    17
                                           592.9786
## 7
       dose_0.0 3810580
                                    21
                                           537.5505
## 8
       dose_0.0
                  3810587
                                     0
                                           223.8383
## 9
       dose_0.0
                  3810587
                                     3
                                           231.8135
## 10
       dose 0.0 3810587
                                     7
                                           340.4171
## 11
       dose_0.0 3810587
                                    11
                                           401.2144
## 12
       dose_0.0
                 3810587
                                    14
                                           389,1488
## 13
       dose_0.0
                  3810587
                                    18
                                           390.5655
## 14
       dose_0.0
                  3810587
                                    21
                                           483.5132
## 15
       dose_0.0 3810601
                                           213.5640
vismodegib %>% tally_study()
##
      group_name N_in_group first_day common_start last_day common_end
## 1
        dose_0.0
                          6
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
## 2
        dose_0.3
                                    0
                                               TRUE
                                                          21
                          5
                                                                  FALSE
## 3
       dose_1.0
                          5
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
## 4
        dose_3.0
                          5
                                    0
                                              TRUE
                                                          21
                                                                   TRUE
## 5
                                              TRUE
                                                          21
                                                                   TRUE
       dose 6.0
                          4
                                    0
## 6
         dose_10
                          4
                                    0
                                              TRUE
                                                          21
                                                                   TRUE
## 7
                          4
                                    0
                                              TRUE
                                                          21
                                                                   TRUE.
         dose_25
## 8
                                    0
                                                          21
         dose_50
                          4
                                               TRUE
                                                                   TRUE
## 9
        dose_75
                          4
                                    0
                                              TRUE
                                                          21
                                                                   TRUE
## 10
       dose_100
                                              TRUE
                                                                  FALSE
```

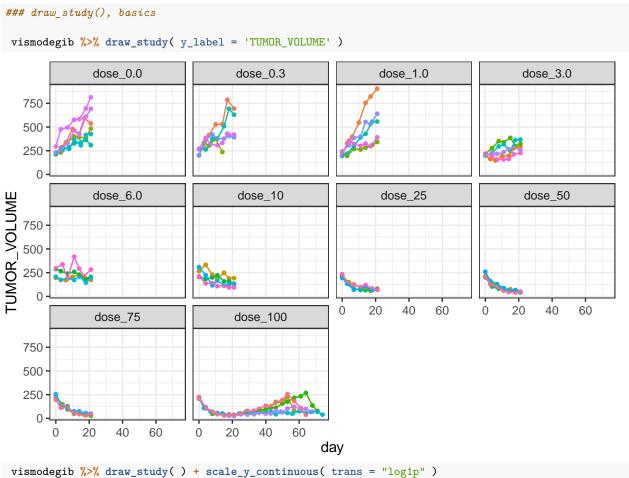
```
### Partial responses:
vismodegib %>% tally_study( response = 'PR' )
      group_name N_in_group first_day common_start last_day common_end PR PR_log_OR PR_SE_log_OR
## 1
        dose 0.0
                          6
                                    0
                                               TRUE
                                                          21
                                                                   TRUE 0 0.0000000
                                                                                          0.000000
## 2
        dose_0.3
                          5
                                    0
                                               TRUE
                                                          21
                                                                  FALSE 0 0.1670541
                                                                                          2.082226
        dose_1.0
## 3
                                    0
                                               TRUE
                                                          21
                                                                   TRUE 0 0.1670541
                                                                                          2.082226
                          5
## 4
        dose_3.0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         0 0.1670541
                                                                                          2.082226
                          5
                                    0
## 5
                                              TRUE
                                                          21
                                                                   TRUE 0 0.3677248
                                                                                          2.091905
        dose 6.0
                          4
                                    0
## 6
        dose_10
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         2 2.5649494
                                                                                          1.718676
## 7
         dose_25
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         4 4.7621739
                                                                                          2.091905
## 8
         dose_50
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         4 4.7621739
                                                                                          2.091905
## 9
         dose 75
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         4 4.7621739
                                                                                          2.091905
## 10
                                                          74
                                                                  FALSE 5 4.9628446
                                                                                          2.082226
        dose_100
                          5
                                    0
                                               TRUE
vismodegib %>% tally_study( response = 'PR', PR_threshold = 0.90 )
      group_name N_in_group first_day common_start last_day common_end PR PR_log_OR PR_SE_log_OR
## 1
        dose 0.0
                          6
                                    0
                                               TRUE
                                                          21
                                                                   TRUE 0 0.0000000
                                                                                          0.000000
## 2
        dose_0.3
                          5
                                    0
                                               TRUE
                                                          21
                                                                  FALSE 0 0.1670541
                                                                                          2.082226
## 3
        dose_1.0
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                        1 1.4663371
                                                                                          1.744344
                          5
## 4
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         2 2.2284771
                                                                                          1.685100
        dose_3.0
                          5
                                    0
## 5
        dose 6.0
                          4
                                    0
                                              TRUE
                                                          21
                                                                   TRUE
                                                                         4 4.7621739
                                                                                          2.091905
## 6
        dose_10
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE 4 4.7621739
                                                                                          2.091905
                                                                   TRUE
## 7
         dose_25
                          4
                                    0
                                               TRUE
                                                          21
                                                                        4 4.7621739
                                                                                          2.091905
## 8
         dose_50
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                         4 4.7621739
                                                                                          2.091905
         dose_75
## 9
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE 4 4.7621739
                                                                                          2.091905
## 10
                                                          74
                                                                  FALSE 5 4.9628446
        dose_100
                          5
                                    0
                                               TRUE
                                                                                          2.082226
vismodegib %>%
tally_study( response = 'PR', PR_threshold = 0.90, reference = 'dose_25' ) %>%
dplyr::select( group_name, N_in_group, PR, PR_log_OR, PR_SE_log_OR )
      group_name N_in_group PR PR_log_OR PR_SE_log_OR
## 1
                         6 0 -4.7621739
                                               2.091905
        dose 0.0
## 2
        dose_0.3
                          5 0 -4.5951199
                                               2.098581
                          5 1 -3.2958369
## 3
        dose 1.0
                                               1.763834
## 4
        dose_3.0
                          5 2 -2.5336968
                                               1.705267
## 5
        dose_6.0
                          4 4 0.0000000
                                               2.108185
## 6
        dose_10
                          4 4
                                0.0000000
                                               2.108185
         dose_25
## 7
                          4 4
                                0.0000000
                                               0.000000
## 8
         dose_50
                          4 4 0.0000000
                                               2.108185
## 9
         dose_75
                          4 4 0.0000000
                                               2.108185
## 10
        dose_100
                          5 5 0.2006707
                                               2.098581
### Both end-of-study complete responses:
vismodegib %>% tally_study( response = 'EOS_CR' )
##
      group_name N_in_group first_day common_start last_day common_end EOS_CR EOS_CR_log_OR EOS_CR_SE_log_OR
## 1
                                              TRUE
                                                                   TRUE
                                                                                    0.0000000
                                                                                                      0.000000
        dose_0.0
                                                          21
                                                                             0
                          6
                                    0
## 2
        dose_0.3
                                               TRUE
                                                          21
                                                                  FALSE
                                                                                    0.1670541
                                                                                                      2.082226
                                    0
        dose_1.0
                                               TRUE
                                                                   TRUE
                                                                                                      2 082226
## 3
                                    0
                                                          21
                                                                                    0.1670541
                          5
                                                                             Ω
## 4
        dose_3.0
                          5
                                    0
                                               TRUE
                                                          21
                                                                   TRUE.
                                                                             0
                                                                                    0.1670541
                                                                                                      2.082226
## 5
        dose_6.0
                          4
                                    0
                                              TRUE
                                                          21
                                                                   TRUE
                                                                             0
                                                                                    0.3677248
                                                                                                      2.091905
## 6
        dose_10
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                             0
                                                                                    0.3677248
                                                                                                      2.091905
## 7
         dose_25
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                              0
                                                                                    0.3677248
                                                                                                      2.091905
## 8
         dose_50
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                             0
                                                                                    0.3677248
                                                                                                      2.091905
## 9
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                                                                                    0.3677248
                                                                                                      2.091905
         dose_{75}
                          4
                                                                              0
## 10
        dose_100
                          5
                                    0
                                               TRUE
                                                                  FALSE
                                                                              0
                                                                                    0.1670541
                                                                                                      2.082226
vismodegib %>%
tally_study( response = 'EOS_CR', EOS_CR_minval = 50 ) %>%
dplyr::select( group_name, N_in_group, EOS_CR, EOS_CR_log_OR, EOS_CR_SE_log_OR )
      group_name N_in_group EOS_CR EOS_CR_log_OR EOS_CR_SE_log_OR
## 1
                                 0
                                        0.0000000
                                                          0.000000
        dose_0.0
                          6
## 2
        dose_0.3
                          5
                                 0
                                        0.1670541
                                                          2.082226
## 3
        dose_1.0
                          5
                                 0
                                        0.1670541
                                                          2.082226
```

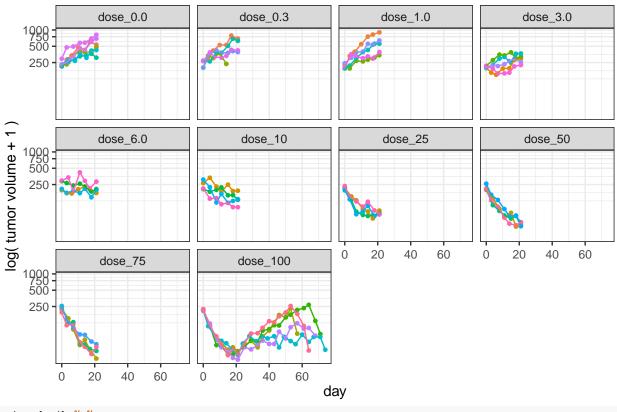
```
## 4
        dose 3.0
                           5
                                  0
                                        0.1670541
                                                           2.082226
## 5
        dose_6.0
                           4
                                  0
                                        0.3677248
                                                           2.091905
## 6
         dose_10
                                        0.3677248
                                                           2.091905
                           4
                                  0
## 7
         dose_25
                           4
                                  0
                                        0.3677248
                                                           2.091905
                           4
                                  4
                                        4.7621739
                                                           2.091905
## 8
         dose_50
## 9
         dose_75
                           4
                                  4
                                        4.7621739
                                                           2.091905
## 10
                                                           1.685100
        dose_100
                           5
                                  2
                                        2.2284771
### Both partial and complete responses combined:
vismodegib %>% tally_study( response = 'PR_or_EOS_CR' )
##
      group_name N_in_group first_day common_start last_day common_end PR_or_EOS_CR PR_or_EOS_CR_log_OR
## 1
        dose_0.0
                                               TRUE
                                                           21
                                                                    TRUE
                                                                                     0
                                                                                                  0.0000000
                           6
                                     0
## 2
        dose_0.3
                           5
                                     0
                                               TRUE
                                                           21
                                                                   FALSE
                                                                                     0
                                                                                                  0.1670541
## 3
                                               TRUE
                                                           21
                                                                    TRUE.
                                                                                                  0.1670541
        dose 1.0
                           5
                                     0
                                                                                     0
## 4
        dose_3.0
                           5
                                     0
                                               TRUE
                                                           21
                                                                     TRUE
                                                                                     0
                                                                                                  0.1670541
                                                                    TRUE
## 5
        dose_6.0
                           4
                                     0
                                               TRUE
                                                           21
                                                                                     0
                                                                                                  0.3677248
## 6
                           4
                                     0
                                               TRUE
                                                           21
                                                                     TRUE
                                                                                     2
                                                                                                  2.5649494
         dose_10
## 7
         dose_25
                           4
                                     0
                                               TRUE
                                                           21
                                                                    TRUE
                                                                                     4
                                                                                                  4.7621739
## 8
         dose_50
                           4
                                     0
                                               TRUE
                                                           21
                                                                    TRUE
                                                                                     4
                                                                                                  4.7621739
## 9
         dose_75
                           4
                                     0
                                               TRUE
                                                           21
                                                                    TRUE
                                                                                                  4.7621739
                                                                                     4
## 10
                           5
                                     0
                                               TRUE
                                                           74
                                                                   FALSE
                                                                                     5
        dose_100
                                                                                                  4.9628446
      PR_or_EOS_CR_SE_log_OR
##
## 1
                    0.000000
## 2
                    2.082226
## 3
                    2.082226
## 4
                    2.082226
                    2.091905
## 5
## 6
                    1.718676
## 7
                    2.091905
## 8
                    2.091905
## 9
                    2.091905
## 10
                    2.082226
vismodegib %>%
tally_study( response = 'PR_or_EOS_CR', PR_threshold = 0.80, EOS_CR_minval = 50, reference = 'dose_6.0' ) %>%
dplyr::select( group_name, N_in_group, PR_or_EOS_CR, PR_or_EOS_CR_log_OR, PR_or_EOS_CR_SE_log_OR )
##
      group_name N_in_group PR_or_EOS_CR PR_or_EOS_CR_log_OR PR_or_EOS_CR_SE_log_OR
## 1
                           6
                                                     -3.412247
                                                                              1.762449
        dose_0.0
                                        0
## 2
                                        0
                                                                              1.770367
        dose_0.3
                           5
                                                     -3.245193
## 3
        dose_1.0
                           5
                                        0
                                                     -3.245193
                                                                              1.770367
## 4
        dose_3.0
                           5
                                        2
                                                     -1.183770
                                                                              1.279881
## 5
                                                      0.000000
        dose_6.0
                           4
                                        3
                                                                              0.000000
## 6
         dose_10
                           4
                                        4
                                                      1.349927
                                                                              1.781742
## 7
                           4
                                        4
         dose_25
                                                      1.349927
                                                                              1.781742
## 8
         dose_50
                           4
                                        4
                                                      1.349927
                                                                              1.781742
         dose_75
## 9
                           4
                                        4
                                                      1.349927
                                                                              1.781742
## 10
        dose 100
                           5
                                                      1.550597
                                                                              1.770367
\verb|### Multiple response options can be requested at once:
vismodegib %>% tally_study( response = c('PR', 'EOS_CR') )
      group_name N_in_group first_day common_start last_day common_end PR PR_log_OR PR_SE_log_OR EOS_CR
##
## 1
        dose_0.0
                           6
                                     0
                                               TRUE
                                                           21
                                                                    TRUE 0 0.0000000
                                                                                            0.000000
                                                                                                          0
## 2
                                                                          0.0.1670541
                                                                                           2.082226
        dose_0.3
                           5
                                     0
                                               TRUE
                                                           21
                                                                   FALSE
                                                                                                          0
                                                                    TRUE 0 0.1670541
## 3
        dose_1.0
                           5
                                     0
                                               TRUE
                                                           21
                                                                                           2.082226
                                                                                                          0
## 4
        dose_3.0
                           5
                                     0
                                               TRUE
                                                           21
                                                                    TRUE 0 0.1670541
                                                                                           2.082226
                                                                                                          0
## 5
        dose_6.0
                           4
                                     0
                                               TRUE
                                                           21
                                                                    TRUE
                                                                          0 0.3677248
                                                                                           2.091905
                                                                                                          0
## 6
         dose_10
                           4
                                     0
                                               TRUE
                                                           21
                                                                     TRUE
                                                                          2 2.5649494
                                                                                            1.718676
                                                                                                          0
## 7
         dose_25
                           4
                                     0
                                               TRUE
                                                           21
                                                                    TRUE 4 4.7621739
                                                                                           2.091905
                                                                                                          0
## 8
         dose_50
                                     0
                                               TRUE
                                                           21
                                                                     TRUE 4 4.7621739
                                                                                            2.091905
                                                                                                          0
                           4
## 9
         dose_{75}
                           4
                                     0
                                               TRUE
                                                           21
                                                                    TRUE 4 4.7621739
                                                                                           2.091905
                                                                                                          0
                                                                   FALSE 5 4.9628446
## 10
        dose_100
                           5
                                     0
                                               TRUE
                                                           74
                                                                                           2.082226
                                                                                                          0
##
      EOS_CR_log_OR EOS_CR_SE_log_OR
## 1
          0.0000000
                             0.000000
## 2
          0.1670541
                             2.082226
## 3
                             2.082226
          0.1670541
```

```
## 4
                 0.1670541
                                                  2.082226
## 5
                  0.3677248
                                                  2.091905
## 6
                 0.3677248
                                                  2.091905
## 7
                  0.3677248
                                                  2.091905
## 8
                  0.3677248
                                                  2.091905
## 9
                  0.3677248
                                                   2.091905
## 10
                 0.1670541
                                                  2.082226
 vismodegib %>%
   tally_study(
                                  response = c( 'PR', 'EOS_CR', 'PR_or_EOS_CR' ),
                           PR_threshold = 0.80,
                         EOS_CR_minval = 50,
                                reference = 'dose_6.0'
                         ) %>%
   dplyr::select( group_name,
                              N_in_group,
                              PR.
                                                               PR_log_OR,
                                                                                                     PR_SE_log_OR,
                              EOS_CR,
                                                       EOS_CR_log_OR,
                                                                                              EOS_CR_SE_log_OR,
                    PR_or_EOS_CR, PR_or_EOS_CR_log_OR, PR_or_EOS_CR_SE_log_OR
##
           group_name N_in_group PR PR_log_OR PR_SE_log_OR EOS_CR EOS_CR_log_OR EOS_CR_SE_log_OR PR_or_EOS_CR
## 1
                                             6 0 -3.4122472
                                                                                   1.762449
                                                                                                            0
                                                                                                                      -0.3677248
                                                                                                                                                        2.091905
              dose_0.0
## 2
                                              5 0 -3.2451931
                                                                                                                      -0.2006707
                                                                                                                                                        2.098581
                                                                                   1.770367
              dose 0.3
                                                                                                            0
                                                                                                                                                                                            0
                                             5 0 -3.2451931
                                                                                   1.770367
                                                                                                                      -0.2006707
                                                                                                                                                        2.098581
## 3
              dose_1.0
                                                                                   1.279881
                                                                                                                     -0.2006707
                                                                                                                                                        2.098581
## 4
              dose_3.0
                                           5 2 -1.1837701
                                                                                                                                                                                            2
## 5
              dose_6.0
                                             4 3 0.0000000
                                                                                   0.000000
                                                                                                            0
                                                                                                                      0.0000000
                                                                                                                                                        0.000000
                                                                                                                                                                                            3
## 6
               dose_10
                                             4 4 1.3499267
                                                                                   1.781742
                                                                                                            0
                                                                                                                       0.0000000
                                                                                                                                                        2.108185
                                                                                                                                                                                            4
## 7
                                             4 4 1.3499267
               dose_25
                                                                                   1.781742
                                                                                                                      0.0000000
                                                                                                                                                        2.108185
                                                                                                          0
                                                                                                                                                                                            4
                                             4 0 -3.0445224
                                                                                                                     4.3944492
## 8
               dose_50
                                                                                  1.781742
                                                                                                                                                        2.108185
## 9
               dose_75
                                             4 0 -3.0445224
                                                                                  1.781742
                                                                                                          4
                                                                                                                     4.3944492
                                                                                                                                                        2.108185
                                                                                                                                                                                            4
## 10 dose_100
                                              5 3 -0.5108256
                                                                                   1.279881
                                                                                                                      1.8607523
                                                                                                                                                        1.705267
##
          PR_or_EOS_CR_log_OR PR_or_EOS_CR_SE_log_OR
## 1
                            -3.412247
                                                                       1.762449
## 2
                            -3.245193
                                                                       1.770367
## 3
                            -3.245193
                                                                       1.770367
                             -1.183770
## 4
                                                                        1.279881
## 5
                              0.000000
                                                                        0.000000
## 6
                              1.349927
                                                                        1.781742
## 7
                              1.349927
                                                                        1.781742
## 8
                              1 349927
                                                                        1.781742
                              1.349927
                                                                        1.781742
## 9
## 10
                              1.550597
                                                                        1.770367
### Alternate endpoints:
### A different endpoint can be provided, but the onus of interpretation & good
### sense is on the user:
 vismodegib %>%
 tally_study( endpoint_name = 'BODY_WEIGHT', PR_threshold = 0.90, response = 'PR')
          \verb|group_name N_in_group first_day common_start last_day common_end PR PR_log_OR PR_SE_log_OR | PR_SE_log_OR |
                                                                                   TRUE
                                                                                                                       TRUE 0 0.0000000
                                                                                                                                                               0.000000
## 1
              dose_0.0
                                             6
                                                                 0
                                                                                                       21
## 2
              dose 0.3
                                              5
                                                                 0
                                                                                   TRUE
                                                                                                       21
                                                                                                                     FALSE 1 1.4663371
                                                                                                                                                               1.744344
## 3
              dose_1.0
                                               5
                                                                 0
                                                                                   TRUE
                                                                                                       21
                                                                                                                       TRUE 1 1.4663371
                                                                                                                                                               1.744344
                                                                                                                       TRUE 0 0.1670541
## 4
                                                                                   TRUE
                                                                                                       21
              dose_3.0
                                              5
                                                                0
                                                                                                                                                               2.082226
## 5
                                                                                   TRUE
                                                                                                       21
                                                                                                                       TRUE 0 0.3677248
              dose_6.0
                                                                0
                                                                                                                                                               2.091905
                                             4
                dose_10
                                                                                   TRUE
                                                                                                                       TRUE 0 0.3677248
## 6
                                                                0
                                                                                                       21
                                                                                                                                                               2.091905
                                                                                                       21
## 7
               dose_25
                                              4
                                                                0
                                                                                   TRUE
                                                                                                                       TRUE 0 0.3677248
                                                                                                                                                               2.091905
## 8
                dose_50
                                              4
                                                                0
                                                                                   TRUE
                                                                                                       21
                                                                                                                       TRUE 0 0.3677248
                                                                                                                                                               2.091905
## 9
               dose_75
                                              4
                                                                0
                                                                                   TRUE
                                                                                                       21
                                                                                                                       TRUE 2 2.5649494
                                                                                                                                                               1.718676
## 10
              dose_100
                                               5
                                                                0
                                                                                   TRUE
                                                                                                       74
                                                                                                                     FALSE 5 4.9628446
                                                                                                                                                               2.082226
```

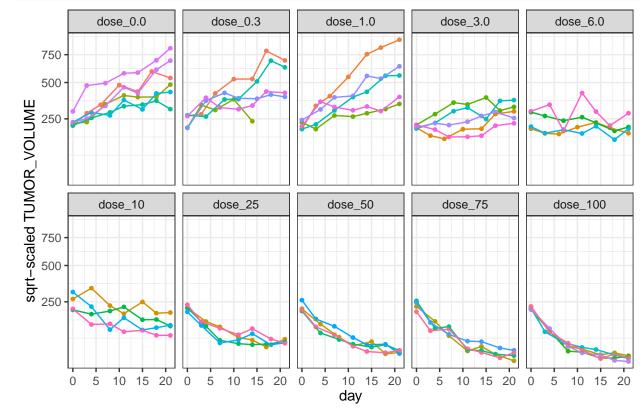
# 6 Pre-modeling pictures with draw\_study() and draw\_waterfall()

The functions maeve::draw\_study() and maeve::draw\_waterfall() generate pictures that do not require any statistical modeling (though a waterfall plot does display some ad hoc summary statistics). The draw\_study() function will be revisited later to include modeling fits with the raw data. Both produce ggplot objects, and so can be augmented with additional layers in the usual ways.

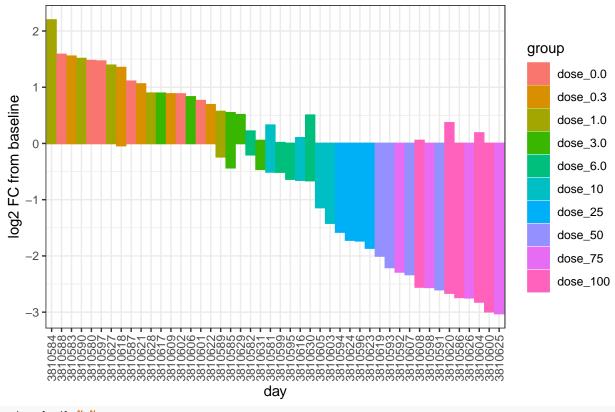




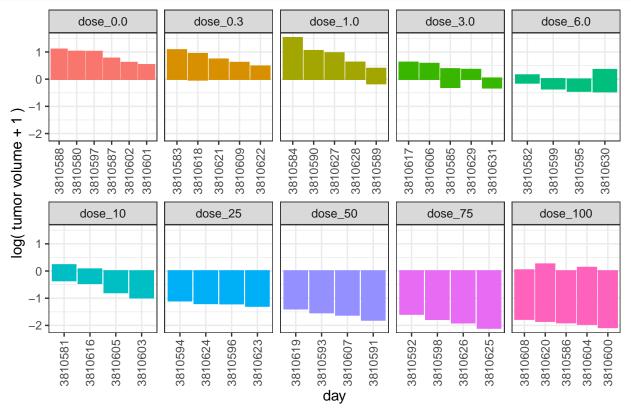








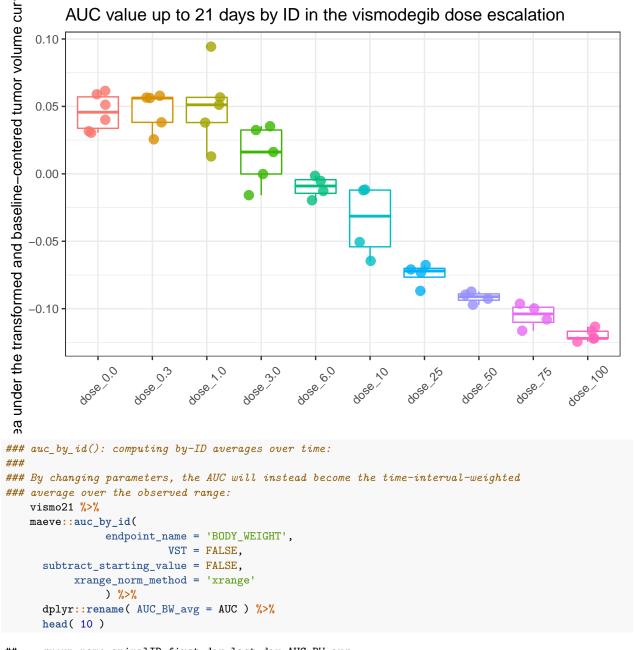




#### 7 auc\_by\_id(): pre-modeling by-ID summaries

The function maeve::auc\_by\_id() will compute an area-under-curve (AUC) statistic to distill the (x,y) data on each separate subject identifier into a single value without any explicit modeling. By default, values are variance-stabilized and centered for each subject prior to summarization.

```
maeve_reset()
 ## restrict vismodegib dose escalation to to first 21 days:
 vismo21 <- vismodegib %>% dplyr::filter( DAY_OF_STUDY <= 21 ) %>% droplevels()
 ## auc_by_id(), basics
 vismo21_AUC_TV <- vismo21 %>% auc_by_id() %>% dplyr::rename( AUC_TV = AUC )
 head( vismo21_AUC_TV, 7 )
##
    group_name animalID first_day last_day
                                             AUC_TV
## 1 dose_0.0 3810580 0 21 0.06154936
     dose_0.0 3810587
                              0
                                     21 0.04013998
## 2
## 3 dose_0.0 3810601
                             0
                                     21 0.03163079
## 4 dose_0.0 3810602
                             0
                                     21 0.03048146
                           0
     dose_0.0 3810588
                                     21 0.05127813
     dose_0.0 3810597
                                     21 0.05903663
## 7
      dose_0.3 3810583
                                      21 0.05618604
 fig_AUC_by_group <-</pre>
 vismo21_AUC_TV %>%
 ggplot( aes( x = group_name, y = AUC_TV, colour = group_name ) ) +
 geom_boxplot( outlier.size = 0 ) +
 geom_point( position = position_jitter( width = 0.25 ), size = 3, alpha = 0.80 ) +
 labs( x = '',
       y = 'Area under the transformed and baseline-centered tumor volume curves, by ID',
       title = 'AUC value up to 21 days by ID in the vismodegib dose escalation'
 theme( legend.position = 'none', axis.text.x = element_text( angle = 45, vjust = 0.5 ) )
 print( fig_AUC_by_group )
```



```
##
      group_name animalID first_day last_day AUC_BW_avg
## 1
       dose_0.0 3810580
                                  0
                                          21
                                               29.48810
       dose_0.0 3810587
                                  0
## 2
                                          21
                                               24.81905
## 3
       dose_0.0 3810601
                                  0
                                          21
                                               26.11190
## 4
       dose_0.0 3810602
                                  0
                                          21
                                               25.52381
## 5
       dose_0.0 3810588
                                  0
                                          21
                                               25.51667
## 6
        dose_0.0 3810597
                                  0
                                               30.84048
       dose_0.3 3810583
                                  0
                                               24.83571
        dose_0.3 3810609
## 8
                                  0
                                               27.21786
                                          14
## 9
        dose_0.3 3810618
                                  0
                                          21
                                               28.26905
                                  0
## 10
       dose_0.3 3810621
                                          21
                                               27.24524
```

```
### auc_by_id(): Bivariate changes to tumor volume and body weight, by ID:
## Get the approximate slope (in grams per day) of body weight change
```

```
vismo21_AUC_BW_slope <-
    vismo21 %>%
    maeve::auc_by_id(endpoint_name = 'BODY_WEIGHT') %>%
    dplyr::rename( AUC_BW_slope = AUC )

merge_cols <- c("group_name", "animalID", "first_day", "last_day")

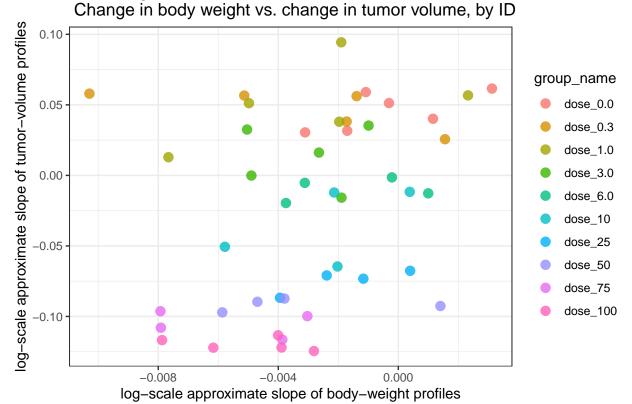
vismo21_TV_BW <- dplyr::full_join( vismo21_AUC_TV, vismo21_AUC_BW_slope, by = merge_cols )

maeve_reset()

fig_TV_vs_BW_by_ID <-
    vismo21_TV_BW %>%
    ggplot( aes( x = AUC_BW_slope, y = AUC_TV, colour = group_name ) ) +
    geom_point( size = 3, alpha = 0.80 ) +
    labs( x = 'log-scale approximate slope of body-weight profiles',
        y = 'log-scale approximate slope of tumor-volume profiles',
        title = ' vismodegib data:\n Change in body weight vs. change in tumor volume, by ID'
    )

print( fig_TV_vs_BW_by_ID )
```

# vismodegib data:



# 8 window\_by\_id(): Interpolate-by-ID on an interval.

The function maeve::window\_by\_id() accepts a data.frame with columns for group\_name, subject\_ID, x\_name, and endpoint\_name. By default, it uses the names for these four columns from the current values in

maeve\_options(). It also accepts parameters xmin and xmax, with defaults of -Inf and Inf. The function will:

- 1. filter out x-values that do not fall within this range.
- 2. add x-values and interpolated y-values for longitudinal traces that span either endpoint. The method for interpolation is one of
- a. 'trapezoid' / 'linear' (these are synonyms in this function) uses a linear approximation from stats::approxfun( ..., method = 'linear', ...).
- b. 'step' uses a left-continuous step-function from stats::approxfun( ..., method = 'constant', f
  = 0, ...).
- c. 'spline' uses a spline from stats::splinefun( ..., method = "fmm", ...).
- 3. return only the 4 columns named by group\_name, subject\_ID, x\_name, and endpoint\_name. If additional columns are returned (i.e., return\_all\_columns = TRUE), then the function sets numeric fields that are not the x\_name or endpoint\_name to NA for any rows with interpolated values.

The default behavior of window\_by\_id() is to transform the endpoint (i.e., using maeve\_options("trans\_func\_char") and maeve\_options("add\_to\_endpoint")) then do any interpolation at the endpoints for (xmin,xmax) on the transformed scale, then back-transform the window-ed and any interpolated values. See this example:

```
maeve_reset()
 print( maeve_options('trans_func_char') )
## [1] "log"
 print( maeve_options('add_to_endpoint') )
## [1] 1
### restrict vismodeqib dose escalation to days in the interval [5, 15]
### in two different ways.
### Method #1:
 vismo_5_to_15_V01 <-
 vismodegib %>%
 dplyr::mutate( y = log( 1 + TUMOR_VOLUME ) ) %>%
  ## window [5, 15]:
  \#\# 'VST = FALSE' below, so no variance-stabilizing transform is applied.
  ## Instead, we take the already-variance-stabilized 'y' just created,
  ## interpolate it at 'x = 5' and 'x = 15', then back-transform to get
  ## the 'TUMOR_VOLUME' values at the interval endpoints.
 maeve::window_by_id( xmin = 5, xmax = 15, endpoint_name = 'y', VST = FALSE ) %>%
  dplyr::mutate( TUMOR_VOLUME = exp( y ) - 1 ) %>%
  dplyr::select( group_name, animalID, DAY_OF_STUDY, TUMOR_VOLUME, y )
 head( vismo_5_to_15_V01, 7 )
     group_name animalID DAY_OF_STUDY TUMOR_VOLUME
## 1
      dose_0.0 3810580
                                    5
                                          318.0052 5.765207
## 2
       dose 0.0 3810580
                                    6
                                          337.0389 5.823161
## 3
       dose_0.0 3810580
                                   10
                                          479.5100 6.174848
## 4
      dose_0.0 3810580
                                          429.2777 6.064431
                                   14
## 5
      dose_0.0 3810580
                                   15
                                          478.0963 6.171902
## 6
      dose_0.0 3810587
                                    5
                                          280.9335 5.641671
## 7
      dose_0.0 3810587
                                    7
                                          340.4171 5.833105
### Method #2:
 ## A shorter way is to just send 'TUMOR_VOLUME' to 'window_by_id()' and
```

```
## then pipe the output through dplyr::mutate() and create 'y' there.
vismo_5_to_15_V02 <-
vismodegib %>%
maeve::window_by_id( xmin = 5, xmax = 15 ) %>%
dplyr::mutate( y = log( 1 + TUMOR_VOLUME ) )
head( vismo_5_to_15_V02, 7 )
```

```
group_name animalID DAY_OF_STUDY TUMOR_VOLUME
##
## 1
      dose_0.0 3810580
                                    5
                                          318.0052 5.765207
## 2
       dose_0.0 3810580
                                    6
                                          337.0389 5.823161
       dose_0.0 3810580
## 3
                                   10
                                          479.5100 6.174848
## 4
       dose_0.0 3810580
                                   14
                                          429.2777 6.064431
## 5
       dose_0.0 3810580
                                   15
                                          478.0963 6.171902
## 6
       dose_0.0 3810587
                                    5
                                          280.9335 5.641671
## 7
       dose_0.0 3810587
                                    7
                                          340.4171 5.833105
```

Observe that the interpolated values at the interval end points match. This is *not* guaranteed to be true if the "spline" method is set for interpolation (which is arguably a better approach), but it should be close.

The advantage of the window\_by\_id() function over simply filtering / subsetting the data is that it will automatically interpolate the endpoint values onto a common x-range. It will never extrapolate longitudinal traces out to interval endpoints, however.

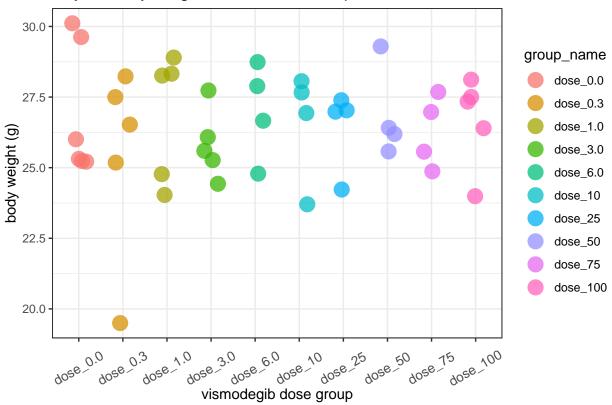
If we want an endpoint evaluated at a given time for all subjects, we can get a value by restricting the data to a very narrow window (perhaps with interpolation at the window endpoints), then calculating the AUC over that interval and dividing by the x-range. This is true even if the subject does not have a value within that interval, so long as there are values bracketing the interval on either side and the interpolation method is adjudged acceptable.

As an example, suppose we want to assess body weight for each animal in the vismodegib study at day 14 (this is the last day at which all animals are still on study). Note that only 30 of the 46 animals have body weight recorded on day 14, but those *without* readings on that day all have bracketing measurements. If we are willing to interpolate these bracketing weights for an animal in order to estimate its body weight on day 14, then we can get an observation for each animal at a common time as follows:

```
group_name animalID BW_common_day
##
## 1
        dose_0.0 3810580
                                   29.6
                                   25.2
## 2
        dose_0.0 3810587
        dose_0.0 3810601
                                   26.0
## 3
## 4
        dose_0.0 3810602
                                   25.2
        dose_0.0 3810588
                                   25.3
## 5
## 6
        dose_0.0 3810597
                                   30.1
```

```
dose_0.3 3810583
                                   25.2
## 7
                                   19.5
## 8
        dose 0.3
                  3810609
## 9
        dose_0.3
                  3810618
                                   28.2
## 10
        dose_0.3 3810621
                                   26.5
  fig_title <- paste( 'Day', common_day, 'body weight, observed or interpolated' )
 fig_common_day <-
 BW_common_day %>%
  ggplot() +
  aes( x = group_name, y = BW_common_day, colour = group_name ) +
  geom_point( size = 5, alpha = 0.75, position = position_jitter( width = 0.2 ) ) +
  labs( title = eval( fig_title ), y = 'body weight (g)', x = 'vismodegib dose group') +
  theme( axis.text.x = element_text( angle = 30, size = 10, vjust = .4 ) )
 print( fig_common_day )
```

#### Day 14 body weight, observed or interpolated



In short, the window\_by\_id() function paired with auc\_by\_id() can be used for a number of common requests, with minimal statistical modeling assumptions.

# 9 grid\_by\_trace(): Interpolate-by-trace on a grid.

The <code>grid\_by\_trace()</code> function allows for interpolation of one or more longitudinal series per subject onto a common set of grid points. This function uses the <code>maeve\_options('trace\_ID')</code> parameter to track longitudinal series nested within subject.

For some applications (e.g., biomedical imaging, a.k.a. BMI), multiple longitudinal data sets can be collected for each of several subjects. We term each such data set nested wwithin a subject identifier a *trace*. Two quick

#### examples:

- 1. A mouse is treated with vehicle, then image intensity recorded for an organ at finely-spaced time points over an hour. After a washout period, the mouse is treated with an active molecule and the same kind of image intensity is recorded for the same organ for another hour. The two sets of time points from the two scans are not necessarily identical. The two scans are two *traces* on the same mouse, but with different treatments.
- 2. A mouse is simultaneously scanned on five different body tissues (e.g., blood, liver, brain, spleen, lung) on a fine grid of time points (not necessarily the same points, but they usually are). The five collections of longitudinal data are five *traces* on one mouse.

Often, then, scientists want to align and compare the BMI traces to derive some efficacy statistic, e.g., the "spleen-to-blood signal ratio". The function maeve::grid\_by\_trace() accepts a data.frame with columns for group\_name, trace\_ID, x\_name, and endpoint\_name. By default, it uses the names for these four columns from the current values in maeve\_options(). It also accepts parameters xmin and xmax, with defaults of -Inf and Inf. The function will:

- 1. Identify a range of x-values that includes all the traces in the data set.
- 2. Define a grid on the full x-range that is the union of the observed x-values and a finely spaced grid.
- 3. Interpolate y-values for each longitudinal trace separately at the x-values for which that trace does not already have a value. The method for interpolation is one of
  - a. 'trapezoid' / 'linear' (these are synonyms in this function) uses a linear approximation from stats::approxfun( ..., method = 'linear', ...).
  - b. 'step' uses a left-continuous step-function from stats::approxfun(..., method = 'constant', f = 0, ...).
  - c. 'spline' uses a spline from stats::splinefun( ..., method = "fmm", ...).
- 4. Return only the 4 columns named by group\_name, trace\_ID, x\_name, and endpoint\_name. If additional columns are returned (i.e., return\_all\_columns = TRUE), then the function sets numeric fields that are not the x\_name or endpoint\_name to NA for any rows with interpolated values.

The default behavior of window\_by\_id() is to transform the endpoint (i.e., using maeve\_options("trans\_func\_char") and maeve\_options("add\_to\_endpoint")) then do any interpolation at the endpoints for (xmin,xmax) on the transformed scale, then back-transform the window-ed and any interpolated values. See this example:

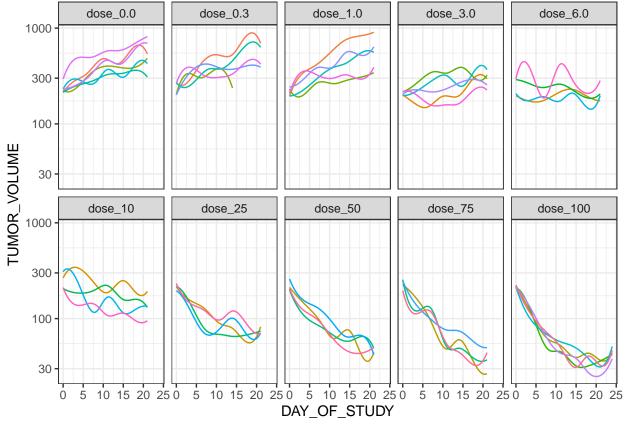
```
maeve_reset()
maeve_options( trace_ID = 'animalID', endpoint_name = 'TUMOR_VOLUME' )

vismo_trace <-
    vismodegib %>%
    maeve::window_by_id( xmin = 0, xmax = 24 ) %>%
    maeve::grid_by_trace( method = 'spline' )

head( vismo_trace, 15 ) # a few lines
```

```
type TUMOR_VOLUME
##
      group name animalID DAY OF STUDY
## 1
       dose 0.0 3810580
                                  0.00
                                           observed
                                                         212.7522
## 2
        dose 0.0 3810580
                                                         219,9040
                                  0.24 interpolated
       dose_0.0 3810580
## 3
                                  0.48 interpolated
                                                         226.8233
        dose_0.0 3810580
                                  0.72 interpolated
                                                         233.4942
## 4
## 5
        dose_0.0 3810580
                                  0.96 interpolated
                                                         239.9035
## 6
        dose_0.0 3810580
                                  1.20 interpolated
                                                         246.0406
## 7
        dose 0.0 3810580
                                  1.44 interpolated
                                                         251.8982
## 8
        dose 0.0 3810580
                                  1.68 interpolated
                                                         257.4714
## 9
       dose_0.0 3810580
                                  1.92 interpolated
                                                         262.7586
## 10
       dose_0.0 3810580
                                  2.16 interpolated
                                                         267.7604
       dose_0.0 3810580
                                  2.40 interpolated
## 11
                                                         272.4804
```

```
dose_0.0 3810580
                                  2.64 interpolated
                                                        276.9246
## 12
## 13
       dose_0.0 3810580
                                  2.88 interpolated
                                                        281.1013
## 14
       dose_0.0 3810580
                                  3.00
                                           observed
                                                        283.0926
## 15
       dose_0.0 3810580
                                  3.12 interpolated
                                                        285.0222
  vismo_trace_fig <-</pre>
      vismo_trace %>%
      dplyr::filter( !is.na( TUMOR_VOLUME ) ) %>%
      dplyr::mutate( color_order = maeve::splice_color_order( group_name, animalID ) ) %>%
      ggplot() +
      aes( x = DAY_OF_STUDY, y = TUMOR_VOLUME, group = animalID, colour = color_order ) +
      geom_line() +
      facet_wrap( ~ group_name, nrow = 2 ) +
      scale_y_log10() +
      guides( colour = FALSE ) # do not show a legend coloured by animalID
 print( vismo_trace_fig )
```



This first example has only one trace for each animal, though two or more are possible by redefining trace\_ID. Note that grid\_by\_trace() will *create* the traces on a common grid, but will not do anything to sort or compare them. This is intentional. Downstream steps are potentially wide-ranging right now, so the current function's scope is limited.

# 10 Truncating study range with truncate\_study()

(This section is optional and can be skipped on a first reading)

Truncation in maeve refers to excluding data from certain x-values before modeling is performed. For example, if a group of ten subjects has repeated measures over time, with nine subjects stopping on day 20, then the tenth subject's data continuing out to, say, day 50, we might choose to model the group's average response only out to day 20. The truncated data is not by default removed from the data set. Rather, it remains in the data, but is excluded from the data passed internally to model.

Truncation is performed through the function truncate\_study(), which is called internally in model\_study() (below), but can also be called separately if desired. Behavior of the truncation is performed through a number of package-level parameters available in maeve\_options():

- 1. min\_n\_in\_group: Data for a group are truncated from model fitting at x-values beyond which the number of subjects drops below min\_n\_in\_group. E.g., when min\_n\_in\_group = 3 for a longitudinal study data are used only until last time point with three subjects.
- 2. min\_frac\_in\_group and min\_frac\_in\_study: These two parameters work in tandem.
  - a. Data for a group are truncated when the fraction of subjects left in the group is below min\_frac\_in\_group and the fraction of subjects left in the entire study is below min\_frac\_in\_study.
  - b. Example: If min\_frac\_in\_group = 0.50 and min\_frac\_in\_study = 0.30, then data from the group will be used until over 50% of the subjects from the group have dropped out and over 70% of the subjects from the entire study have dropped out.
- 3. overall\_x\_min: This sets a numeric lower bound below which x-values are not used in modelling. By default it is -Inf, so that no truncation occurs
- 4. overall\_x\_max: This sets a numeric upper bound above which x-values are not used in modelling. By default it is Inf, so that no truncation occurs.

The values of overall\_x\_min & overall\_x\_max are applied last, and so further extend any truncation done by earlier parameters. They will not "undo" truncation implemented by min\_n\_in\_group, min\_frac\_in\_group, and min\_frac\_in\_study.

The function maeve::truncate\_study() takes as input a data.frame with the study data, and has three distinct options for what is returned, depending on what the user wants to do with the output. These options are determined by maeve\_options("truncation\_return\_type"), which can take one of the values "data.frame", "logical", or "list". The "data.frame" option returns the subset of the input data frame that is not truncated. The "logical" option returns the logical vector with length equal to the number of rows in the input data.frame and TRUE for rows that are not truncated. The "list" option returns these two in addition to much more information.

```
### truncate_study() examples
maeve_reset()

## maeve package defaults:
vismo_all <- vismodegib %>% truncate_study()
identical( vismodegib, vismo_all ) %>% print # By default, there is no truncation.

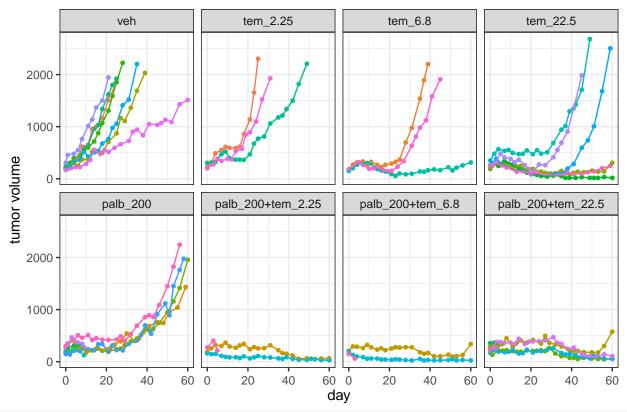
## [1] TRUE

## gRED TO defaults:
vismo_trunc_v01 <-
    vismodegib %>% truncate_study( min_n_in_group = 3, min_frac_in_group = 0.50, min_frac_in_study = 0.30 )
identical( vismodegib, vismo_trunc_v01 ) %>% print # gRED default settings will truncate some data rows

## [1] FALSE
vismodegib    %>% nrow %>% print

## [1] 385
```

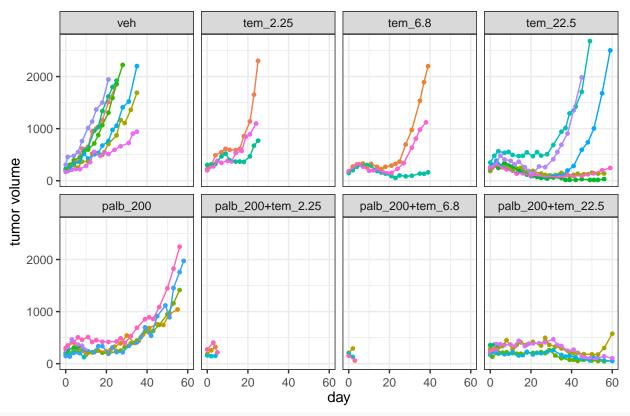
```
vismo_trunc_v01 %>% nrow %>% print
## [1] 381
vismo_trunc_v01 %>% tally_study()
      group_name N_in_group first_day common_start last_day common_end
                                                          21
## 1
       dose_0.0
                          6
                                    0
                                               TRUE
                                                                   TRUE
## 2
       dose_0.3
                          5
                                    0
                                               TRUE
                                                          21
                                                                  FALSE
                                                                   TRUE
## 3
       dose_1.0
                                               TRUE
                                                          21
                          5
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
## 4
       dose_3.0
                          5
                                    0
                                               TRUE
                                                                   TRUE
## 5
       dose_6.0
                          4
                                    0
                                                          21
## 6
        dose 10
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
## 7
        dose_25
                          4
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                          4
## 8
        dose_50
                                    0
                                               TRUE
                                                          21
                                                                   TRUE
                          4
                                               TRUE
                                                                   TRUE
## 9
         dose_75
                                    0
                                                          21
                                    0
                                               TRUE
                                                                  FALSE
## 10 dose_100
                                                          68
## gRED TO defaults:
maeve_reset()
maeve_options( min_n_in_group
                                = 3,
               min_frac_in_group = 0.50,
               min_frac_in_study = 0.30,
               truncation_return_type = 'data.frame' # one of 'data.frame', 'logical', or 'list'.
data( palb_temo_01, package = 'maeve')
maeve_options( ncol_value = 4, y_label = 'tumor volume' ) # just for these palb+temo 01 plots.
# palbociclib + temozolomide study 01 with no truncation at all
palb_temo_01 %>% tally_study()
##
            group_name N_in_group first_day common_start last_day common_end
## 1
                   veh
                                7
                                           0
                                                     TRUE
                                                                60
                                                                        FALSE
## 2
              {\tt tem\_2.25}
                                3
                                           0
                                                     TRUE
                                                                49
                                                                        FALSE
## 3
               tem_6.8
                                3
                                           0
                                                     TRUE
                                                                60
                                                                        FALSE
## 4
              tem_22.5
                                7
                                           0
                                                     TRUE
                                                                60
                                                                        FALSE
                                           0
## 5
              palb_200
                                7
                                                     TRUE
                                                                60
                                                                        FALSE
## 6 palb_200+tem_2.25
                                3
                                           0
                                                     TRUE
                                                                60
                                                                        FALSE
## 7 palb_200+tem_6.8
                                3
                                           0
                                                     TRUE
                                                                60
                                                                        FALSE
                                           0
                                                     TRUE
                                                                        FALSE
## 8 palb_200+tem_22.5
                                7
                                                                60
palb_temo_01 %>% draw_study()
```



# palbociclib + temozolomide study 01 with gRED default truncation
palb\_temo\_01 %>% truncate\_study() %>% tally\_study()

##		<pre>group_name</pre>	N_in_group	first_day	common_start	last_day	common_end
##	1	veh	7	0	TRUE	35	FALSE
##	2	tem_2.25	3	0	TRUE	25	FALSE
##	3	tem_6.8	3	0	TRUE	39	FALSE
##	4	tem_22.5	7	0	TRUE	59	FALSE
##	5	palb_200	7	0	TRUE	58	FALSE
##	6	palb_200+tem_2.25	3	0	TRUE	5	FALSE
##	7	palb_200+tem_6.8	3	0	TRUE	3	FALSE
##	8	palb_200+tem_22.5	7	0	TRUE	60	FALSE

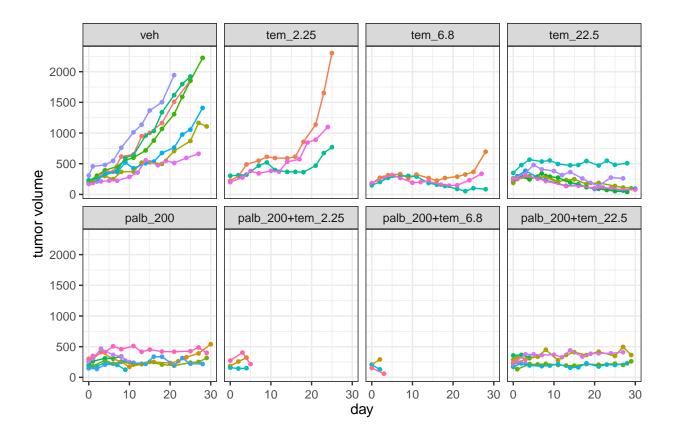
palb\_temo\_01 %>% truncate\_study() %>% draw\_study()



# palbociclib + temozolomide study 01 with gRED default truncation + hard truncation at 30 days:
palb\_temo\_01 %>% truncate\_study(overall\_x\_max = 30) %>% tally\_study()

##		<pre>group_name</pre>	N_in_group	first_day	common_start	last_day	common_end
##	1	veh	7	0	TRUE	29	FALSE
##	2	tem_2.25	3	0	TRUE	25	FALSE
##	3	tem_6.8	3	0	TRUE	28	FALSE
##	4	tem_22.5	7	0	TRUE	30	FALSE
##	5	palb_200	7	0	TRUE	30	FALSE
##	6	palb_200+tem_2.25	3	0	TRUE	5	FALSE
##	7	palb_200+tem_6.8	3	0	TRUE	3	FALSE
##	8	palb_200+tem_22.5	7	0	TRUE	29	FALSE

palb\_temo\_01 %>% truncate\_study(overall\_x\_max = 30) %>% draw\_study()



#### 11 Fitting models with model\_study()

The model\_study() function takes as input a study data frame, then fits from one to four different mixed models. Which models are fit is automatically determined by the maeve\_options('metric') values chose to summarize the groups. Supported metric values are

```
maeve_options('metrics_supported')
## [1] "linear" "ITGR" "AUC" "ITGR_pwl" "AUC_pwl" "ITGR_poly" "AUC_poly"
```

For each mixed model, each subject has a random intercept and slope term, while the group-level curve is parameterized by fixed effects. The model(s) fit will be:

- 1. A linear mixed model (LMM) if metric contains "linear".
- 2. A generalized additive mixed model (GAMM) if metric contains "AUC" and / or "ITGR". With default settings, which are to to subtract out the starting value and then scale by half the squared study range (for "AUC") or the study range (for "ITGR"), the metrics returned for "AUC" and "ITGR" are termed eGaIT and eDOT, respectively, and are described in a companion manuscript to this package.
- 3. A piecewise linear mixed model if metric contains "AUC\_pwl" and / or "ITGR\_pwl". The piecewise linear fit depends on setting parameters such as maeve\_options('number\_break\_points') and maeve\_options('break\_points'). This is mostly intended for cases with very few (e.g., three) time points. See examples.
- 4. A polynomial linear mixed model if metric contains "AUC\_poly" and / or "ITGR\_poly". The polynomial linear fit depends on setting parameters such as maeve\_options('poly\_degree'), and makes a naive polynomial basis with the stats::poly(). This is mostly intended for cases with very few (e.g., three) time points. When more time points are available, a GAMM will generally outperform this approach. See examples.

By default, the LMM and GAMM are fit. The output from model\_study() is usually sent on to another function (e.g., predict\_study(), compare\_groups()) for visualizing and summarizing results.

```
### model_study() examples
vismo21 <- vismodegib %>% dplyr::filter( DAY_OF_STUDY <= 21 )</pre>
### Fit a GAMM by specifying "metric = 'AUC'" or "metric = 'ITGR'",
### the two metrics that derive from a GAMM:
maeve_reset()
### We can return a larger list of results if needed with 'return_all = TRUE':
modeling_list = maeve::model_study( vismo21, metric = 'AUC', return_all = TRUE )
### Here are the contents of the 'return_all = TRUE' option.
modeling_list %>% names
## [1] "models" "data"
                        "extra"
modeling_list %>% with( models ) %>% names # these are what you get with 'return_all = FALSE'
## [1] "md4_lmer"
                       "md4_gamm4"
                                        "md4_lmer_pwl" "md4_lmer_poly"
modeling_list %>% with( data ) %>% names
## [1] "clean_DF_full_xrange" "clean_DF_restricted" "study_data_frame"
modeling_list %>% with( extra ) %>% names
## [1] "metric"
                            "xrange"
                                                 "reference_Dunnett" "group_name"
                                                                                          "subject_ID"
## [6] "x_name"
                            "endpoint_name"
                                                 "func_list"
                                                                     "trans\_func\_char"
                                                                                         "inv_func_char"
### Usually, we just need the list of models:
models_vismo21 = maeve::model_study( vismo21, metric = 'AUC' ) # return_all = FALSE by default.
names( models_vismo21 )
## [1] "md4_lmer"
                       "md4_gamm4"
                                       "md4_lmer_pwl" "md4_lmer_poly"
lapply( models_vismo21, class ) # metric = 'AUC', so 3 of the 4 models (all but 'md4_gamm4') will be NULL.
## $md4_lmer
## [1] "NULL"
##
## $md4 gamm4
## [1] "list"
##
## $md4_lmer_pwl
## [1] "NULL"
## $md4_lmer_poly
## [1] "NULL"
### The gamm4 results are in two distinct parts, returned in a list:
names( models_vismo21[['md4_gamm4']] )
## [1] "mer" "gam"
### names of 'gam' object in gamm4 results:
models_vismo21 %>% with( md4_gamm4 ) %>% with( gam ) %>% names
## [1] "model"
                            "formula"
                                                 "smooth"
                                                                     "nsdf"
                                                                                          "family"
## [6] "df.null"
                            "y"
                                                 "terms"
                                                                     "pterms"
                                                                                          "xlevels"
## [11] "contrasts"
                            "assign"
                                                                     "cmX"
                                                 "na.action"
                                                                                          "var.summary"
```

```
## [16] "pred.formula"
                            "coefficients"
                                                 "scale.estimated"
                                                                     "prior.weights"
                                                                                         "weights"
## [21] "R"
                            "sp"
                                                 "edf"
                                                                     "df.residual"
                                                                                         "sig2"
## [26] "method"
                            "qV"
                                                 "Ve"
                                                                     "linear.predictors" "fitted.values"
## [31] "residuals"
                            "gcv.ubre"
### names of attributes of 'mer' object in gamm4 results:
models_vismo21 %>% with( md4_gamm4 ) %>% with( mer ) %>% attributes %>% names
## [1] "resp"
                  "Gp"
                            "call"
                                      "frame"
                                                 "flist"
                                                           "cnms"
                                                                     "lower"
                                                                               "theta"
                                                                                         "beta"
                                                                                                    "u"
## [11] "devcomp" "pp"
                            "optinfo" "class"
### Fit a simple linear mixed model by specifying "metric = 'linear'":
models_vismo21 = maeve::model_study( vismo21, metric = 'linear' )
names( models_vismo21 )
## [1] "md4_lmer"
                                       "md4_lmer_pwl" "md4_lmer_poly"
                       "md4_gamm4"
lapply( models_vismo21, class )
## $md4_lmer
## [1] "lmerMod"
## attr(,"package")
## [1] "lme4"
##
## $md4_gamm4
## [1] "NULL"
##
## $md4_lmer_pwl
## [1] "NULL"
##
## $md4_lmer_poly
## [1] "NULL"
summary( models_vismo21[['md4_lmer']] )
## Linear mixed model fit by REML ['lmerMod']
## Formula: y ~ group + group:x + (1 + x | ID)
      Data: data.frame(clean_DF, weight_lmer = weight_lmer)
## Weights: weight_lmer
##
## REML criterion at convergence: 21.4
##
## Scaled residuals:
                      Median
                                    3Q
                1Q
## -2.68265 -0.66596 -0.03618 0.67780 2.42072
##
## Random effects:
   Groups
                         Variance Std.Dev. Corr
##
             (Intercept) 7.710e-03 0.087805
##
                         6.592e-05 0.008119 0.88
                         3.439e-02 0.185433
## Residual
## Number of obs: 320, groups: ID, 46
##
## Fixed effects:
                    Estimate Std. Error t value
##
## (Intercept)
                    5.534860
                               0.062818 88.110
## groupdose_0.3
                    0.055251
                               0.093837
                                         0.589
## groupdose_1.0
                   -0.081847
                               0.093063
                                         -0.879
## groupdose_3.0
                   -0.235127
                               0.093636 -2.511
                                        -0.732
## groupdose_6.0
                   -0.072489
                               0.098985
                               0.100624 -0.926
## groupdose_10
                   -0.093209
## groupdose_25
                   -0.401343 0.099484 -4.034
```

```
## groupdose 50
                  -0.344168 0.099750 -3.450
                  -0.280963
                             0.099484 -2.824
## groupdose_75
## groupdose_100 -0.466673 0.093979 -4.966
## groupdose_0.0:x 0.036672 0.005221
                                       7.024
## groupdose_0.3:x 0.032185 0.006089 5.285
## groupdose_1.0:x 0.041710 0.005754 7.249
## groupdose_3.0:x 0.017354
                            0.005781
                                       3.002
## groupdose_6.0:x -0.006018
                             0.006412 -0.939
## groupdose_10:x -0.028033 0.006440 -4.353
                             0.006442 -7.458
## groupdose_25:x -0.048045
                              0.006401 -10.902
## groupdose_50:x -0.069783
## groupdose_75:x -0.084307
                              0.006442 -13.088
## groupdose_100:x -0.085720
                            0.005746 -14.919
## Correlation matrix not shown by default, as p = 20 > 12.
## Use print(x, correlation=TRUE) or
##
      vcov(x)
                     if you need it
### Fit a piecewise linear model by specifying "metric = 'AUC_pwl'"
### (or 'ITGR_pwl') and also the break_points spanning the time range:
maeve_reset()
maeve_options( break_points = c( 0, 7, 14, 21 ) )
models_vismo21 = maeve::model_study( vismo21, metric = 'AUC_pwl' )
### Fit a simple polynomial model by specifying "metric = 'AUC_poly'"
### (or 'ITGR_poly') and also the degree.
maeve_reset()
maeve_options( poly_degree = 3 )
models_vismo21 = maeve::model_study( vismo21, metric = 'AUC_poly' )
### Fit all the endpoints at once:
maeve_reset()
maeve_options(
               metric = maeve_options('metrics_supported'), # all available summary metrics
               break_points = c(0, 7, 14, 21),
               poly_degree = 3
              )
models_vismo21 = maeve::model_study( vismo21 )
lapply( models_vismo21, class ) # see that all four models are now non-NULL
## $md4_lmer
## [1] "lmerMod"
## attr(,"package")
## [1] "lme4"
## $md4_gamm4
## [1] "list"
##
## $md4_lmer_pwl
## [1] "lmerMod"
## attr(,"package")
## [1] "lme4"
##
## $md4_lmer_poly
## [1] "lmerMod"
## attr(,"package")
## [1] "lme4"
```

#### 12 Predicting from models with predict\_study()

The predict\_study() function can be used to predict conditional and unconditional values (i.e., with & without random effects, respectively) for up to four models fit in model\_study(). By default, this is at observed x-values, but use various options (e.g., maeve\_options('x\_pred\_type'), etc.) for predicting at non-observed times. See examples.

```
### predict_study()

### Get a data.frame with predicted responses at a desired set of x-values.
###

### NB: Predicted values are retained in the data.frame even if you do NOT

### want them. Get rid of them if desired by filtering on 'in_pred_x_set'

### Predictions over an evenly-spaced grid spanning observed x-values, with grid points 0.5 apart:

pred_data_frame <-
    predict_study( models_vismo21, x_pred_type = 'grid', x_pred_spacing = 0.5 )

### Provide a user-specified x-grid over which to make predictions.

pred_data_frame <-
    predict_study( models_vismo21, x_pred_type = 'custom', x_pred_vec = seq( 0, 20, by = 2) )

### By default, "predict_study()" makes predictions only at observed x-values:

pred_data_frame <- predict_study( models_vismo21 )
head( pred_data_frame, 4 )</pre>
```

```
group_name animalID DAY_OF_STUDY TUMOR_VOLUME
                                                       group
##
                                                                   ID
                                                                           y_orig
                                                                                          y model_x_value
## 1
       dose_0.0 3810580
                                     0
                                           212.7522 dose_0.0 3810580
                                                                      0 212.7522 5.364818
                                                                                                     TRUE
## 2
       dose_0.0 3810580
                                     3
                                           283.0926 dose_0.0 3810580 3 283.0926 5.649300
                                                                                                     TRUE
## 3
       dose 0.0 3810580
                                     6
                                           337.0389 dose 0.0 3810580 6 337.0389 5.823161
                                                                                                     TRUE
## 4
       dose_0.0 3810580
                                           479.5100 dose_0.0 3810580 10 479.5100 6.174848
                                                                                                     TRUE
                                    10
##
     in_pred_x_set in_model_x_range intercept_re_lmer slope_re_lmer intercept_re_gamm4 slope_re_gamm4
## 1
              TRUE.
                                TRUE
                                            0.02831629
                                                         0.003034573
                                                                             0.008323168
                                                                                             0.004904741
## 2
              TRUE
                                TRUE
                                            0.02831629
                                                         0.003034573
                                                                             0.008323168
                                                                                             0.004904741
## 3
              TRUE
                                TRUE
                                            0.02831629
                                                         0.003034573
                                                                             0.008323168
                                                                                             0.004904741
## 4
                                TRUE
                                            0.02831629
                                                         0.003034573
                                                                             0.008323168
                                                                                             0.004904741
##
     intercept_re_lmer_pwl slope_re_lmer_pwl intercept_re_lmer_poly slope_re_lmer_poly pred_lin pred_lin_ID
## 1
                0.01034241
                                  0.004785803
                                                         0.008717379
                                                                             0.004802489 5.534860
                                                                                                      5.563176
## 2
                0.01034241
                                  0.004785803
                                                         0.008717379
                                                                             0.004802489 5.644875
                                                                                                      5.682295
## 3
                0.01034241
                                  0.004785803
                                                         0.008717379
                                                                             0.004802489 5.754891
                                                                                                      5.801414
## 4
                0.01034241
                                  0.004785803
                                                         0.008717379
                                                                             0.004802489 5.901578
                                                                                                      5.960240
    pred_gam pred_gam_ID pred_pwl pred_pwl_ID pred_poly pred_poly_ID
                                                                           y_norm pred_lin_norm pred_gam_norm
## 1 5.485855
                 5.494178 5.458929
                                       5.469271 5.450738
                                                               5.459455
                                                                         0.000000
                                                                                       0.000000
                                                                                                      0.000000
## 2 5.639951
                 5.662988 5.639877
                                       5.664577
                                                 5.655722
                                                               5.678847
                                                                         5.302743
                                                                                        1.987683
                                                                                                      2.808977
## 3 5.783585
                 5.821337 5.820824
                                       5.859882 5.811013
                                                               5.848545 8.543504
                                                                                       3.975367
                                                                                                      5.427244
                 6.004372 5.956143
                                       6.014344 5.961288
                                                               6.018030 15.098936
                                                                                                      8.406109
## 4 5.947002
                                                                                       6.625612
     pred_pwl_norm pred_poly_norm pred_gam_deriv1 base_pred_lin base_pred_gam_base_pred_gam_deriv1
## 1
          0.000000
                         0.000000
                                        0.05197849
                                                        5.534860
                                                                       5.485855
                                                                                           0.05197849
## 2
          3.314711
                          3.760674
                                        0.05013869
                                                        5.644875
                                                                       5.639951
                                                                                           0.05013869
```

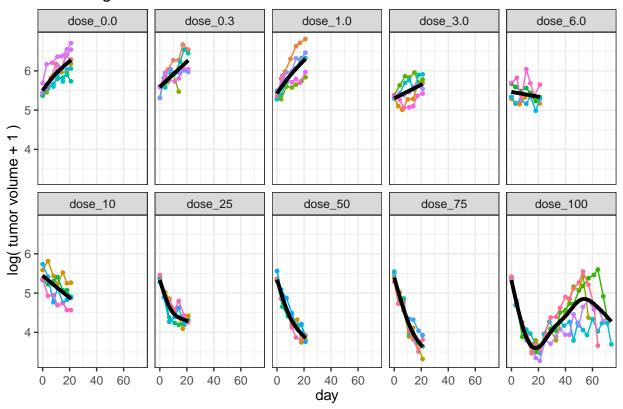
```
## 3
          6.629422
                         6.609651
                                       0.04520969
                                                       5.754891
                                                                      5.783585
                                                                                         0.04520969
          9.108274
                         9.366626
                                       0.03598394
                                                       5.901578
                                                                      5.947002
                                                                                         0.03598394
## 4
pred_data_frame %>%
     dplyr::select( group_name, animalID, DAY_OF_STUDY, in_pred_x_set, TUMOR_VOLUME, pred_gam ) %>% head( 15 )
##
      group_name animalID DAY_OF_STUDY in_pred_x_set TUMOR_VOLUME pred_gam
## 1
       dose_0.0 3810580
                                                TRUE
                                                         212.7522 5.485855
                                     0
## 2
       dose_0.0 3810580
                                     3
                                                TRUE
                                                         283.0926 5.639951
## 3
       dose_0.0 3810580
                                                TRUE
                                                         337.0389 5.783585
                                     6
## A
       dose_0.0 3810580
                                    10
                                                TRUE
                                                         479.5100 5.947002
## 5
       dose_0.0 3810580
                                                TRUE
                                                         429.2777 6.072502
                                    14
## 6
                                                         592.9786 6.157073
       dose_0.0 3810580
                                    17
                                                TRUE
## 7
       dose_0.0 3810580
                                    21
                                                TRUE
                                                         537.5505 6.264261
## 8
       dose 0.0 3810587
                                     0
                                                TRUE
                                                         223.8383 5.485855
## 9
       dose_0.0 3810587
                                     3
                                                TRUE
                                                         231.8135 5.639951
## 10
       dose_0.0 3810587
                                                         340.4171 5.827764
                                     7
                                                TRUE
## 11
       dose_0.0 3810587
                                    11
                                                TRUE
                                                         401.2144 5.981587
                                                         389.1488 6.072502
## 12
       dose_0.0
                 3810587
                                    14
                                                TRUE
## 13
        dose_0.0
                  3810587
                                    18
                                                TRUE
                                                         390.5655 6.184431
## 14
        dose_0.0
                  3810587
                                                TRUE
                                                         483.5132 6.264261
                                    21
## 15
       dose_0.0 3810601
                                                TRUE
                                                         213.5640 5.485855
### More examples:
pred_data_frame <- predict_study( models_vismo21, x_pred_type = 'union_observed_and_grid', x_pred_spacing = 2 )</pre>
pred_data_frame %>%
     dplyr::select( group_name, animalID, DAY_OF_STUDY, in_pred_x_set, TUMOR_VOLUME, pred_gam ) %>% head( 20 )
      group_name animalID DAY_OF_STUDY in_pred_x_set TUMOR_VOLUME pred_gam
## 1
       dose_0.0 3810580
                                                TRUE
                                                         212.7522 5.485855
                                     0
       dose_0.0 3810580
                                                TRUE
                                                               NA 5.589267
## 2
                                     2
## 3
       dose_0.0 3810580
                                                TRUE
                                                         283.0926 5.639951
                                     3
## 4
       dose_0.0 3810580
                                                TRUE
                                                               NA 5.689428
                                     4
## 5
       dose_0.0 3810580
                                     6
                                                TRUE
                                                         337.0389 5.783585
## 6
       dose_0.0 3810580
                                     7
                                                               NA 5.827764
                                                TRUE
## 7
       dose_0.0 3810580
                                     8
                                                TRUE
                                                               NA 5.869828
## 8
       dose_0.0 3810580
                                    10
                                                TRUE
                                                         479.5100 5.947002
## 9
       dose_0.0 3810580
                                                TRUE
                                                               NA 5.981587
                                    11
## 10
       dose_0.0 3810580
                                    12
                                                TRUE
                                                               NA 6.013561
                                                         429.2777 6.072502
## 11
       dose_0.0 3810580
                                    14
                                                TRUE
## 12
       dose_0.0
                 3810580
                                    15
                                                TRUE
                                                               NA 6.100959
       dose_0.0
                 3810580
                                                TRUE
## 13
                                    16
                                                               NA 6.129196
## 14
       dose_0.0 3810580
                                    17
                                                TRUE
                                                         592.9786 6.157073
       dose_0.0 3810580
## 15
                                    18
                                                TRUE
                                                               NA 6.184431
       dose_0.0 3810580
                                    20
                                                TRUE
## 16
                                                               NA 6.237869
## 17
       dose_0.0 3810580
                                    21
                                                TRUE
                                                         537.5505 6.264261
## 18
       dose_0.0
                 3810587
                                     0
                                                TRUE
                                                         223.8383 5.485855
## 19
       dose_0.0
                 3810587
                                     2
                                                TRUE
                                                               NA 5.589267
## 20
       dose_0.0 3810587
                                     3
                                                TRUE
                                                         231.8135 5.639951
pred_data_frame %>%
 dplyr::select( group_name, animalID, DAY_OF_STUDY, TUMOR_VOLUME,
                y, pred_lin, pred_gam, pred_pwl, pred_poly
                ) %>%
 head( 10 )
      group_name animalID DAY_OF_STUDY TUMOR_VOLUME
                                                           y pred_lin pred_gam pred_pwl pred_poly
## 1
       dose_0.0 3810580
                                     0
                                           212.7522 5.364818 5.534860 5.485855 5.458929 5.450738
## 2
       dose 0.0 3810580
                                     2
                                                          NA 5.608203 5.589267 5.579561 5.593502
## 3
       dose_0.0 3810580
                                           283.0926 5.649300 5.644875 5.639951 5.639877 5.655722
                                     3
```

```
dose 0.0 3810580
                                    4
                                                          NA 5.681547 5.689428 5.700193 5.712421
## 4
                                                 NA
## 5
       dose_0.0
                 3810580
                                    6
                                           337.0389 5.823161 5.754891 5.783585 5.820824
                                                                                         5.811013
## 6
        dose_0.0 3810580
                                    7
                                                          NA 5.791562 5.827764 5.881140
                                                                                         5.853785
                                                 NA
## 7
        dose_0.0 3810580
                                    8
                                                 NΑ
                                                          NA 5.828234 5.869828 5.906141
                                                                                         5.892796
## 8
        dose_0.0 3810580
                                    10
                                           479.5100 6.174848 5.901578 5.947002 5.956143
                                                                                         5.961288
## 9
        dose_0.0 3810580
                                    11
                                                 NA
                                                          NA 5.938250 5.981587 5.981144 5.991650
## 10
        dose_0.0 3810580
                                    12
                                                 NA
                                                          NA 5.974921 6.013561 6.006145 6.020009
```

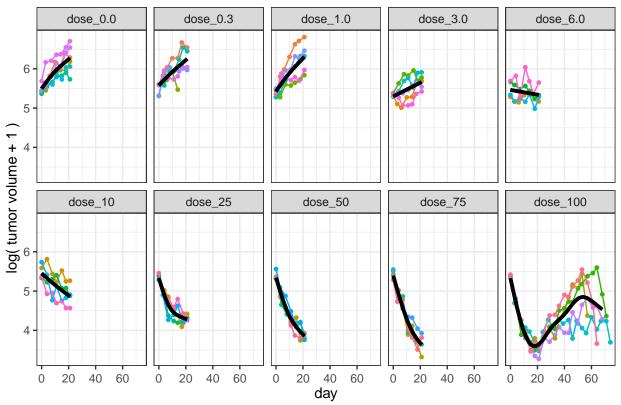
### 13 Truncation with model\_study() and predict\_study()

While study truncation can be called explicitly via maeve::truncate\_study(), a better approach is simply to set the truncation parameters in maeve\_options(), then run model\_study(). This will yield models that are fit on only the non-truncated data while (by default) keeping track of all the data (both truncated and untruncated) in maeve\_options("full\_study\_data\_frame"). The results of model\_study() can be passed directly to predict\_study() in order to return a data frame that tracks both the full original data and the predicted values, at whatever grid of predicted x-locations was requested.

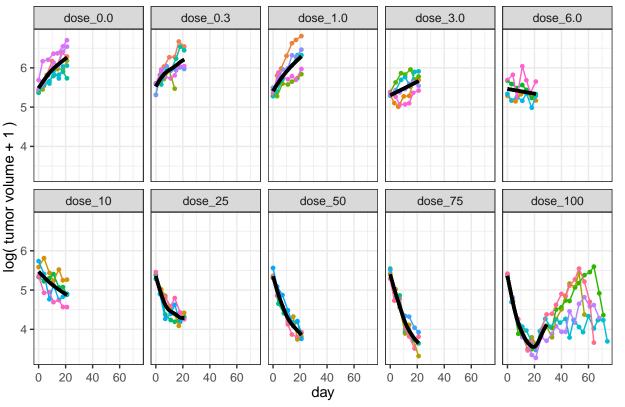
# vismodegib with no truncation



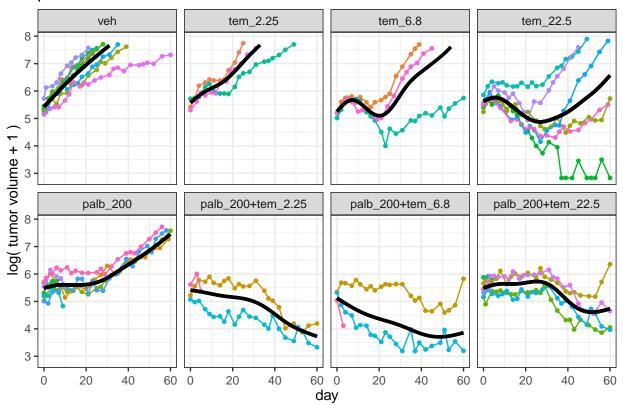
# vismodegib with gRED truncation



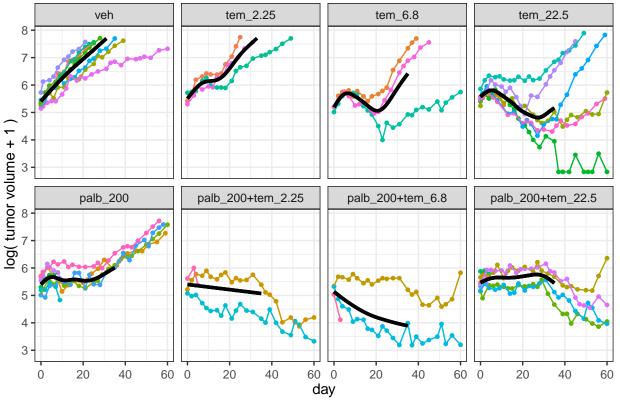
### vismodegib with gRED truncation, curtailed at day 35

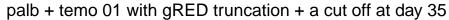


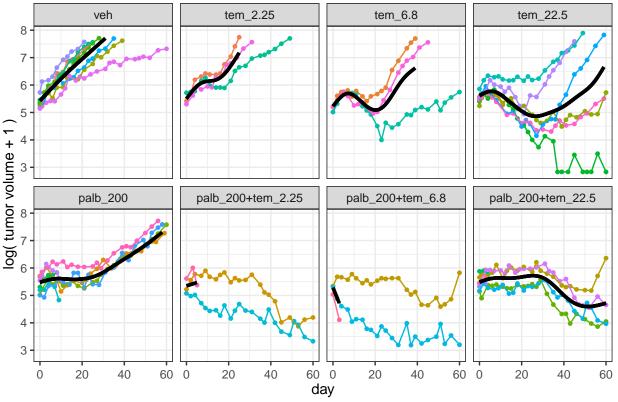
### palb + temo 01 with no truncation

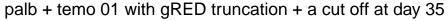


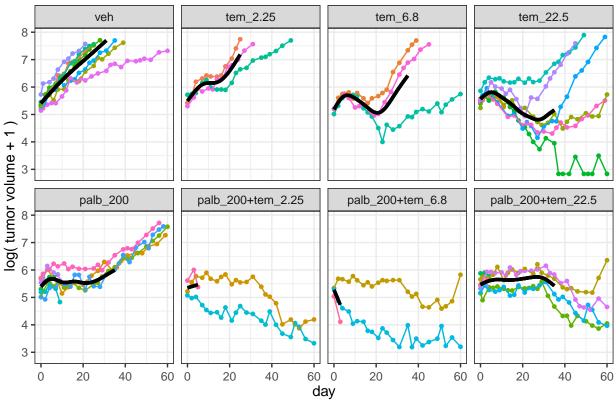
## palb + temo 01 with cut off at day 35







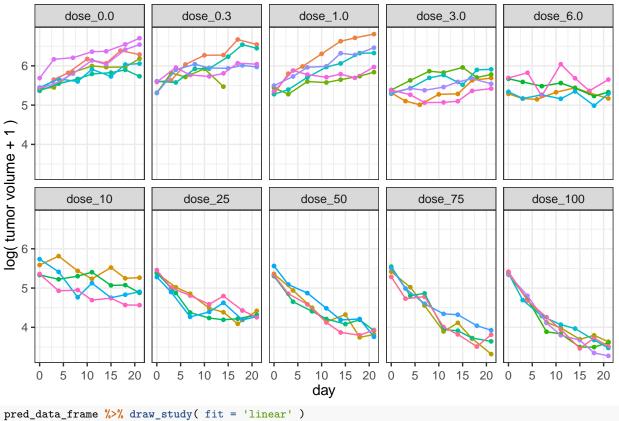




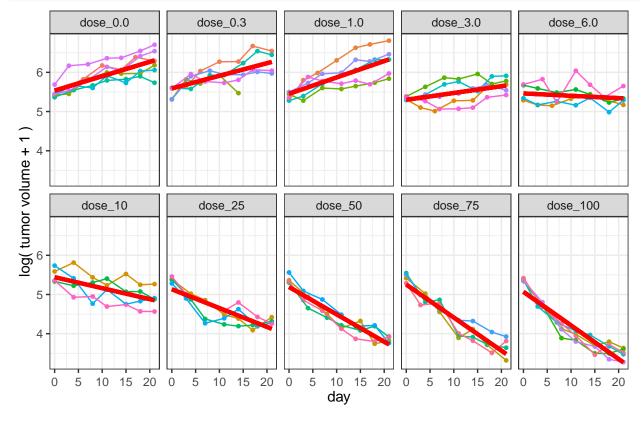
# 14 Using the predicted data frame from predict\_study() in figures: draw\_study(), draw\_waterfall(), draw\_overlay(), draw\_noise().

The functions draw\_study(), draw\_waterfall(), draw\_overlay(), and draw\_noise() allow for simple visualizations of commonly queried features in a study. Examples below show how to use them to see results captured in the output from the predict\_study() function.

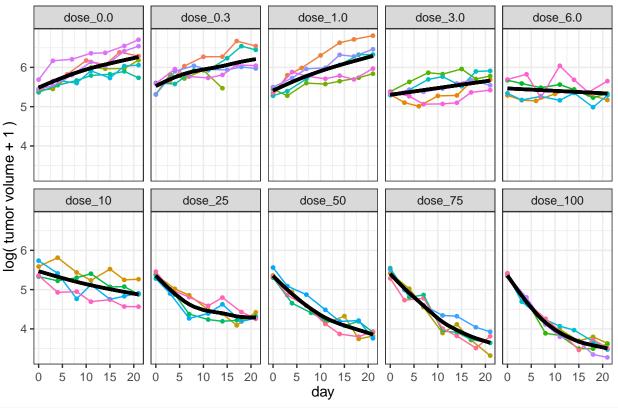
```
### 6. draw_study(), draw_overlay(), draw_noise(), draw_waterfa() using results of predict_study().
### A bunch of plots with fixed effects curves from different models.
maeve_reset()
maeve_options( endpoint_name = 'y', ncol_value = 5 )
pred_data_frame %>% draw_study( )
```

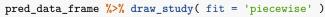


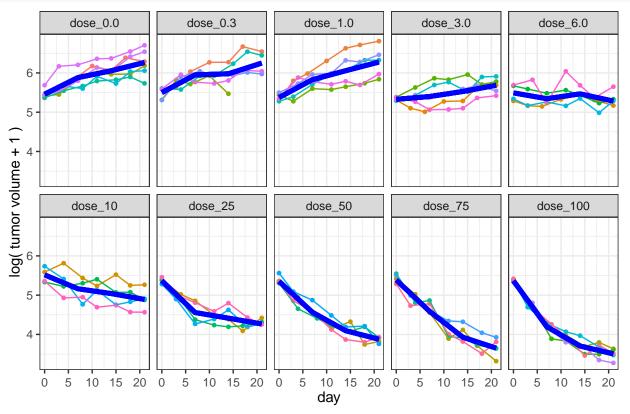


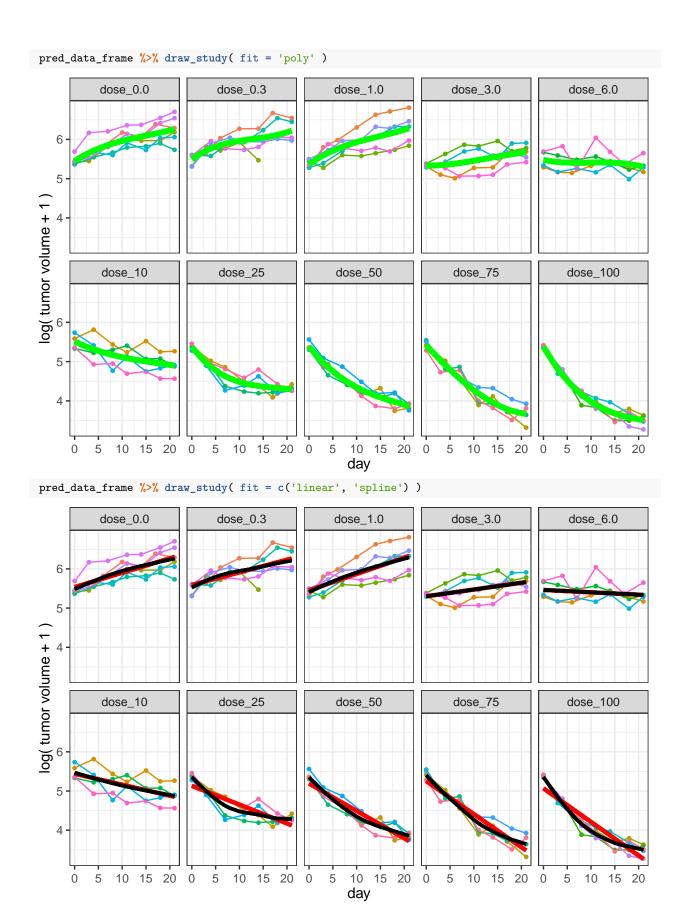




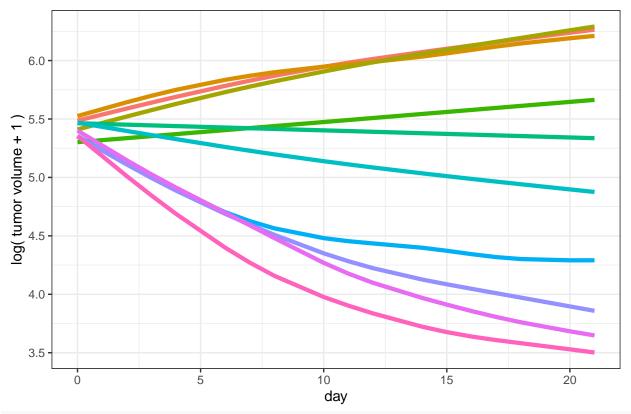




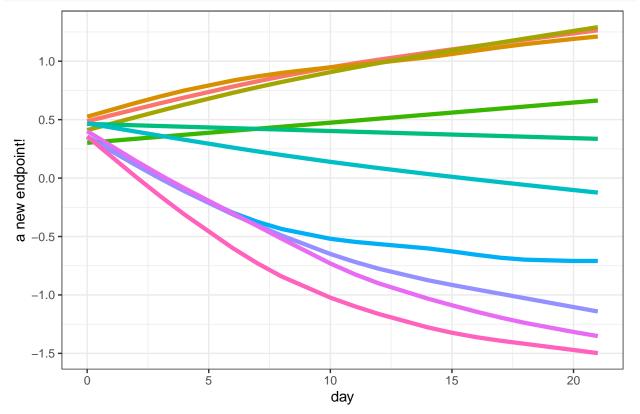




```
###
 pred_data_frame %>%
   draw_waterfall( endpoint_name = 'y', facet_char = 'group_name', ncol_value = 5 )
                    dose_0.0
                                                    dose_0.3
                                                                                     dose_1.0
                                                                                                                     dose_3.0
                                                                                                                                                     dose_6.0
        0
 log(tumor volume + 1)
                 3810580 -
                           3810587 -
                                3810602 -
                                                                                                              3810617 -
                                                                                                                    3810606
                                                                                                                                                3810582 -
                                     3810601
                                                                     3810622
             3810588
                      3810597
                                              3810583
                                                    3810618
                                                         3810621
                                                                                          3810627
                                                                                                3810628
                                                                                                     3810589
                                                                                                                          3810585
                                                                                                                                3810629
                                                                                                                                      3810631
                                                                                                                                                              3810595
                                                                                                                                                                     3810630
                                                               3810609
                                                                              3810584
                                                                                    3810590
                                                                                                                                                       3810599
                    dose_10
                                                     dose_25
                                                                                     dose_50
                                                                                                                      dose_75
                                                                                                                                                     dose_100
      -1
      -2
                                    3810603-
                                               3810594 -
                                                                                                               3810592 -
                                                                                                                                     3810625-
                     3810616
                                                                               3810619-
                                                                                                                                                                3810604
                             3810605
                                                                    3810623
                                                                                      3810593
                                                                                                     3810591
                                                                                                                       3810598
                                                                                                                              3810626
                                                                                                                                               3810608
                                                             3810596
                                                                                                                                                           3810586
                                                                                                                                                                      3810600
                                                      3810624
                                                                                             3810607
                                                                                                                                                     3810620
              3810581
                                                                                        day
### draw_overlay()
 pred_data_frame %>% draw_overlay( fit = 'spline' )
```

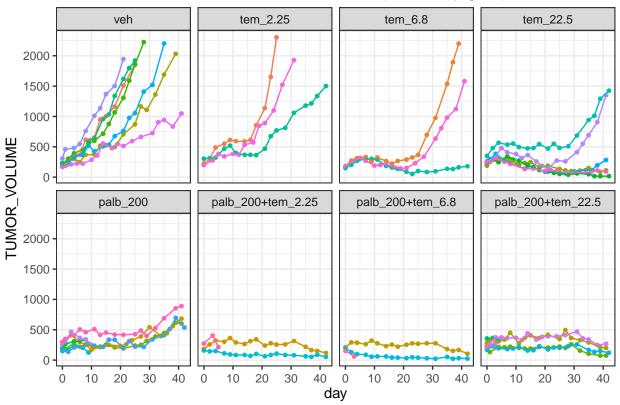


pred\_data\_frame %>% # make up another predictor from an exisiting predictor as we go:
 dplyr::mutate( pred\_gam\_minus\_5 = pred\_gam - 5 ) %>%
 draw\_overlay( fit = 'spline', spline\_predictor = 'pred\_gam\_minus\_5', y\_label = 'a new endpoint!')

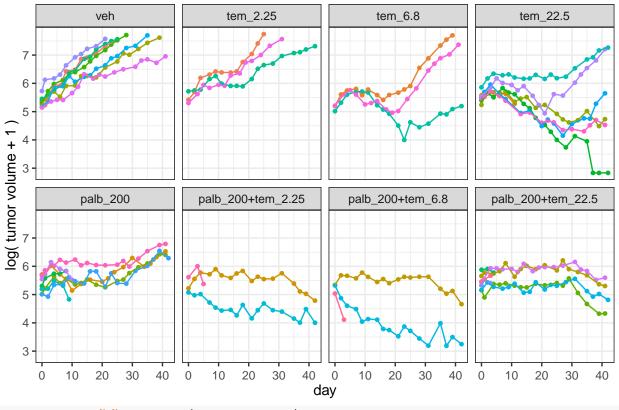


```
pred_data_frame %>% draw_overlay( fit = 'piecewise' )
    6.0
log( tumor volume + 1 )
    5.0
    4.0
    3.5
                                                      10
                                                                                                 20
            0
                                 5
                                                                            15
                                                       day
### Look at a second data set:
 data( palb_temo_01, package = 'maeve' )
 maeve_reset()
 maeve_options( break_points = c( 0, 7, 21, 42 ),
                 metric = c( 'linear', 'ITGR', 'AUC', 'ITGR_pwl', 'AUC_pwl', 'ITGR_poly', 'AUC_poly' ),
x_pred_type = 'grid', x_pred_spacing = 1,
                 ncol_value = 4 # 8 groups total
 pred_palb_temo_list <-</pre>
     palb_temo_01 %>%
     dplyr::filter( DAY_OF_STUDY <= 42 ) %>%
     model_study %>%
     predict_study( return_list = TRUE ) # return extra components (used below) in a list
 pred_palb_temo <- pred_palb_temo_list[["clean_DF_pred"]]</pre>
 palb_temo_01 %>%
  dplyr::group_by( group_name ) %>%
  dplyr::summarise( first_day = min(DAY_OF_STUDY), last_day = max(DAY_OF_STUDY) )
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 8 x 3
     group_name
                         first_day last_day
##
     <fct>
                             <dbl>
                                       <dbl>
                                          60
## 1 veh
                                  0
## 2 tem_2.25
                                  0
                                          49
```

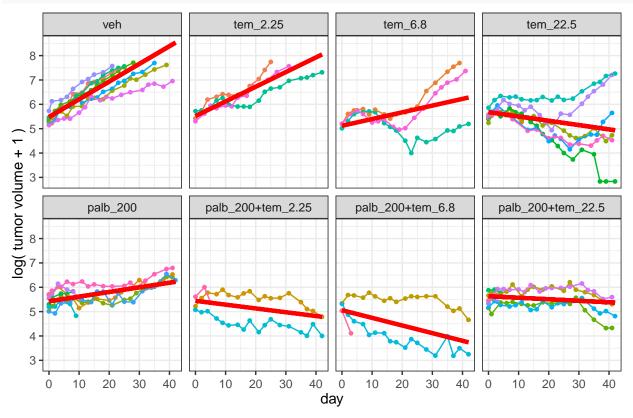
# palbociclib + temozolomide: tumor volume profiles by group



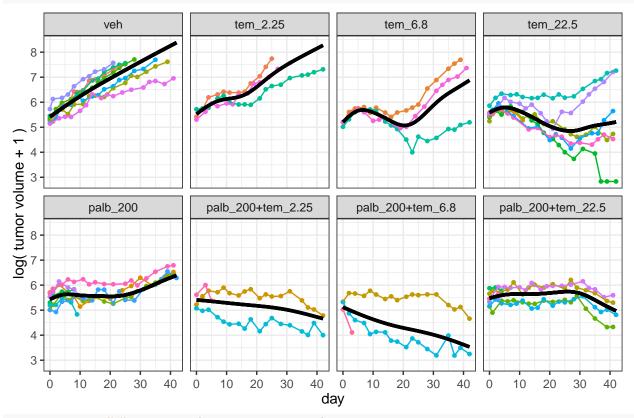
```
maeve_options( endpoint_name = 'y' ) # figures below will be on transformed endpoint.
pred_palb_temo %>% draw_study( )
```



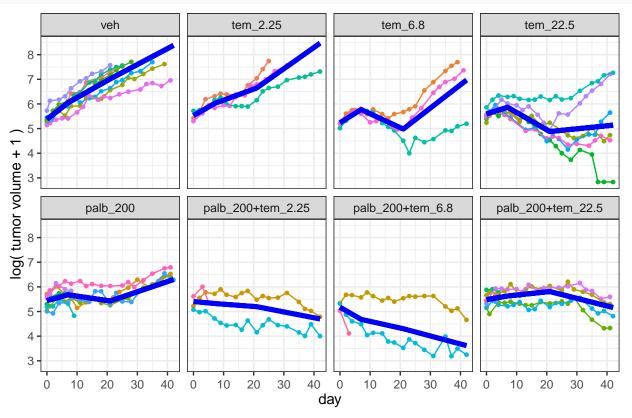
pred\_palb\_temo %>% draw\_study( fit = 'linear' )



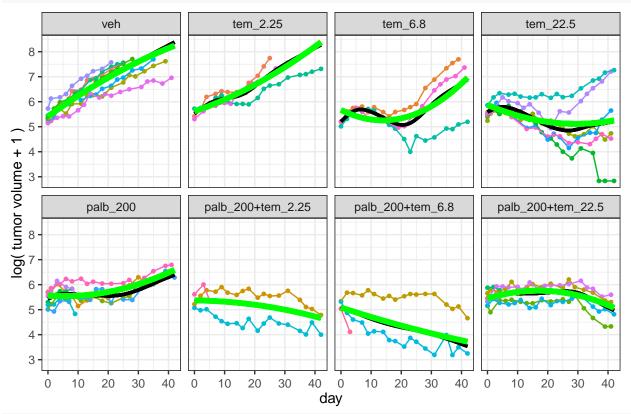




pred\_palb\_temo %>% draw\_study( fit = 'piecewise' )



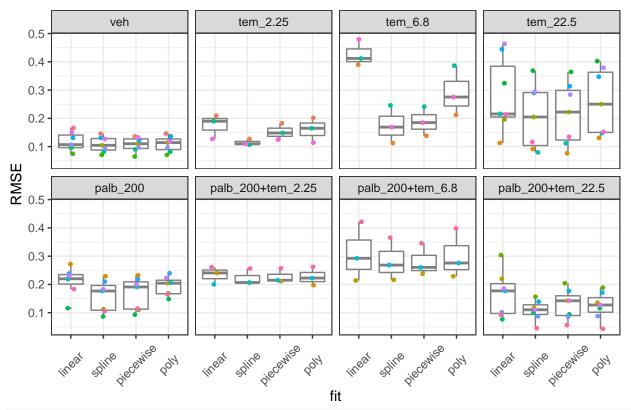
```
### overlay polynomial fits with spline fits on raw data:
pred_palb_temo %>% draw_study( fit = c( 'poly', 'spline') )
```



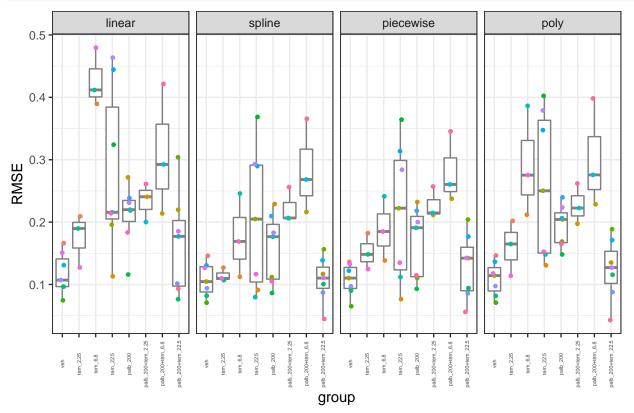
```
### draw_noise()

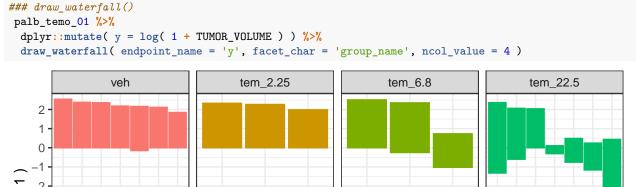
### For each animal and model, Show the RMS prediction error of the conditional fits to the data:
### ("conditional" = "predictions including BLUPs for each animal")

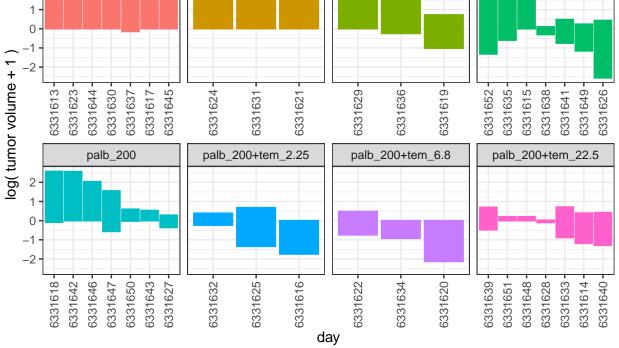
pred_palb_temo_list[['RMSE_by_ID']] %>%
    draw_noise() + theme( axis.text.x = element_text( angle = 45, vjust = 0.5 ) )
```











maeve\_reset()

# 15 Use compare\_groups() to summarize longitudinal model fits with error estimates and estimate requested contrasts.

The compare\_groups() function takes fitted models and summarizes each metric (e.g., linear, AUC, AUC\_pwl, etc.) into one number per requested comparison. Which comparisons are produced depends on the parameter maeve\_options('contrast'), which can either be set globally or just passed explicitly to compare\_groups().

By default, the contrast is "Identity", causing each group to be summarized to a single number, but with no inter-group comparison:

```
maeve_options('contrast')
```

#### ## [1] "Identity"

The supported contrast types are:

- 1. "Identity": Summarize each metric into one number per group. No inter-group comparisons are performed, so the function name compare\_groups() is arguably a misnomer in this case.
- 2. "Dunnett": Summarize each metric into one number per group, then compare each "active" group to a common control, which is determined by maeve\_options("reference\_Dunnett"). By default, the common control is just the group named as the first factor level of group\_name.

- 3. "Tukey": Summarize each metric into one number per group, then make all pairwise comparisons.
- 4. "Sequen": Summarize each metric into one number per group, then compare each group to the factor level just before it in the factor levels of group\_name. This is mostly useful in dose escalation studies.
- 5. "custom": Summarize each metric into one number per group, then compare each groups as specified by a user-provided custom contrast matrix to perform a Wald test for each row of the custom contrast matrix. See examples.

The LME slope can be obtained by setting maeve options ( metric = "linear" ).

The group summaries eGaIT and eDOT described in the manuscript are derived by setting maeve\_options(
"metric" ) to maeve\_options( "metric" = "AUC") or maeve\_options( "metric" = "ITGR"), respectively, while leaving maeve\_options( "xrange\_norm\_method" = "slope\_equivalent" ) (its default) and the parameter ..., subtract\_starting\_value = TRUE, ... in compare\_groups() (also its default). Hence, eGaIT and eDOT are special — albeit default — cases of the metrics available from compare\_groups() by toggling between metric = "AUC" and metric = "ITGR" in maeve\_options().

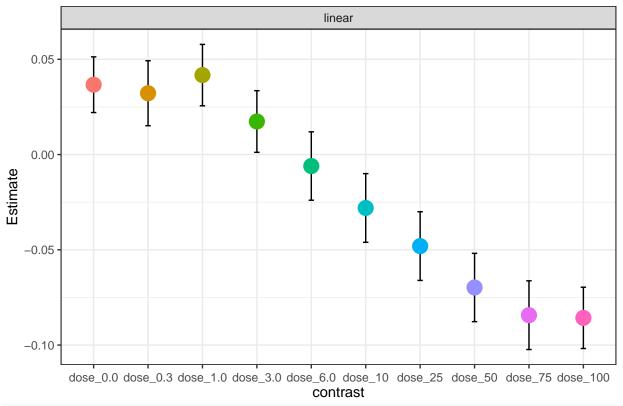
The metrics "AUC\_pwl" and "ITGR\_pwl" are the analogs of those for "AUC" and "ITGR", but derived from a piecewise linear mixed model fit instead of from a spline. Similarly, The metrics "AUC\_poly" and "ITGR\_poly" are the analogs of those for "AUC" and "ITGR", but derived from a simple polynomial basis linear mixed model fit instead of from a spline. These are intended to be used mainly when there are very few (e.g., 3-5) distinct time points in a study, so that fitting a spline may be difficult or undefined.

By default, each group is assigned a summary statistic with a 95% confidence interval. Setting ..., extended\_output = TRUE, ... in compare\_groups() will further include in the comparison table output columns with standard errors, t-statistics, and p-values of the null hypothesis that the numeric contrast considered is zero, with p-values adjusted by the method in adjustment\_method (for which none results in no adjustment).

Below are a number of worked examples summarizing estimated response curves. Note that when maeve\_options("contrast") is "Identity", there are not any actual comparisons per se, just reporting of the summary metric for each group (in which case compare\_groups() is something of a misnomer). Various comparisons are performed when "contrast" is set to, e.g., "Dunnett" or "Tukey". A "custom" option is also available for customized linear contrasts – see the example below.

```
### 7. compare_groups().
### (Recall that "models_vismo21" is from the vismo21 analysis above.)
### linear summary:
cg <- models_vismo21 %>% compare_groups( metric = 'linear' )
cg %>% with( data ) %>% with( effectDF ) %>% format( digits = 3 )
```

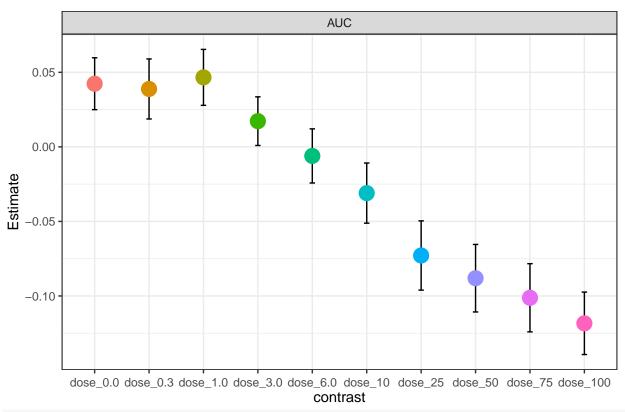
```
metric contrast Estimate
                                   lwr
                                          upr
## 1 linear dose_0.0 0.03667 0.02205
                                       0.0513
## 2 linear dose_0.3 0.03219 0.01514
## 3 linear dose_1.0 0.04171 0.02560
                                       0.0578
     linear dose_3.0 0.01735 0.00117
                                       0.0335
     linear dose_6.0 -0.00602 -0.02397
     linear dose_10 -0.02803 -0.04606 -0.0100
     linear dose_25 -0.04804 -0.06608 -0.0300
## 8 linear dose_50 -0.06978 -0.08770 -0.0519
## 9 linear dose_75 -0.08431 -0.10234 -0.0663
## 10 linear dose_100 -0.08572 -0.10181 -0.0696
cg %>% with( figures ) %>% with( figCI ) %>% print
```



```
### spline summary:
cg <- models_vismo21 %>% compare_groups( metric = 'AUC' )

cg %>% with( data ) %>% with( effectDF ) %>% format( digits = 3 )
```

```
##
     metric contrast Estimate
                                    lwr
                                            upr
## 1
        AUC dose_0.0 0.04235 0.024958
                                         0.0597
## 2
        AUC dose_0.3 0.03884 0.018709 0.0590
## 3
        AUC dose_1.0 0.04661 0.027850 0.0654
## 4
        AUC dose_3.0 0.01724 0.000918 0.0336
## 5
        AUC dose_6.0 -0.00608 -0.024239 0.0121
## 6
        AUC dose_10 -0.03102 -0.051192 -0.0109
## 7
        AUC dose_25 -0.07286 -0.096089 -0.0496
## 8
        AUC dose_50 -0.08809 -0.110728 -0.0655
## 9
        AUC dose_75 -0.10121 -0.124081 -0.0783
        AUC dose_100 -0.11835 -0.139282 -0.0974
cg %>% with( figures ) %>% with( figCI ) %>% print
```



```
metric contrast Estimate
                                    lwr
## 1
        linear dose_0.0 0.03667 0.022055 0.05129
## 2
        linear dose_0.3  0.03219  0.015137  0.04923
## 3
        ## 4
        linear dose_3.0 0.01735 0.001168 0.03354
## 5
        linear dose_6.0 -0.00602 -0.023969 0.01193
## 6
        linear dose_10 -0.02803 -0.046062 -0.01000
## 7
        linear dose_25 -0.04804 -0.066079 -0.03001
## 8
        linear dose_50 -0.06978 -0.087703 -0.05186
## 9
        linear dose_75 -0.08431 -0.102341 -0.06627
## 10
        linear dose_100 -0.08572 -0.101805 -0.06963
## 11
          ITGR dose_0.0 0.03707 0.021969 0.05216
## 12
          ITGR dose_0.3 0.03266 0.014899 0.05042
## 13
          ITGR dose_1.0 0.04195 0.025420 0.05849
## 14
         ITGR dose_3.0 0.01724 0.000918 0.03356
## 15
         ITGR dose_6.0 -0.00608 -0.024239 0.01207
```

```
ITGR dose 10 -0.02822 -0.046556 -0.00987
## 16
## 17
          ITGR dose_25 -0.05062 -0.069975 -0.03126
## 18
          ITGR dose_50 -0.07102 -0.090018 -0.05202
## 19
          ITGR dose_75 -0.08348 -0.102661 -0.06430
## 20
          ITGR dose_100 -0.08830 -0.105662 -0.07093
## 21
           AUC dose_0.0 0.04235 0.024958 0.05974
## 22
           AUC dose_0.3 0.03884 0.018709 0.05897
## 23
           AUC dose 1.0 0.04661 0.027850 0.06537
## 24
           AUC dose_3.0 0.01724 0.000918 0.03356
## 25
           AUC dose_6.0 -0.00608 -0.024239 0.01207
## 26
           AUC dose_10 -0.03102 -0.051192 -0.01085
## 27
           AUC dose_25 -0.07286 -0.096089 -0.04963
## 28
           AUC dose_50 -0.08809 -0.110728 -0.06546
## 29
           AUC dose_75 -0.10121 -0.124081 -0.07834
## 30
           AUC dose_100 -0.11835 -0.139282 -0.09741
## 31
      ITGR_pwl dose_0.0 0.02844 0.015815 0.04106
## 32
      ITGR_pwl dose_0.3  0.02273  0.008744  0.03671
## 33 ITGR_pwl dose_1.0 0.03246 0.018821 0.04610
## 34 ITGR_pwl dose_3.0 0.00952 -0.004382 0.02343
## 35 ITGR_pwl dose_6.0 -0.00119 -0.016422 0.01405
      ITGR_pwl dose_10 -0.02266 -0.038754 -0.00656
      ITGR_pwl dose_25 -0.04535 -0.060617 -0.03009
## 38
      ITGR_pwl dose_50 -0.05987 -0.075479 -0.04427
## 39
      ITGR_pwl dose_75 -0.06937 -0.084628 -0.05410
## 40
       ITGR_pwl dose_100 -0.07912 -0.093322 -0.06491
       AUC_pwl dose_0.0 0.03906 0.020994 0.05713
## 41
## 42
       AUC_pwl dose_0.3 0.03657 0.016405 0.05674
## 43
       AUC_pwl dose_1.0 0.04325 0.023539 0.06295
## 44
       AUC_pwl dose_3.0 0.00971 -0.010331 0.02975
## 45
       AUC_pwl dose_6.0 -0.00784 -0.029862 0.01418
## 46
       AUC_pwl dose_10 -0.03197 -0.054567 -0.00938
## 47
       AUC_pwl dose_25 -0.06881 -0.090703 -0.04692
## 48
       AUC_pwl dose_50 -0.07741 -0.099526 -0.05530
## 49
       AUC_pwl dose_75 -0.08424 -0.106128 -0.06235
       AUC_pwl dose_100 -0.10840 -0.128428 -0.08837
## 51 ITGR_poly dose_0.0 0.03842 0.022155 0.05468
## 52 ITGR_poly dose_0.3 0.03449 0.015651 0.05333
## 53 ITGR_poly dose_1.0 0.04375 0.025911 0.06159
## 54 ITGR_poly dose_3.0 0.01614 -0.001737 0.03401
## 55 ITGR_poly dose_6.0 -0.00836 -0.028290 0.01157
## 56 ITGR_poly dose_10 -0.02915 -0.049113 -0.00919
## 57 ITGR_poly dose_25 -0.05171 -0.071660 -0.03177
## 58 ITGR_poly dose_50 -0.07231 -0.092229 -0.05239
## 59 ITGR_poly dose_75 -0.08313 -0.103079 -0.06319
## 60 ITGR_poly dose_100 -0.08902 -0.106856 -0.07118
## 61 AUC_poly dose_0.0 0.04621 0.026700 0.06571
## 62 AUC_poly dose_0.3 0.04170 0.020203 0.06320
## 63 AUC_poly dose_1.0 0.05142 0.030034 0.07280
## 64 AUC_poly dose_3.0 0.01371 -0.007705 0.03512
## 65 AUC_poly dose_6.0 -0.00712 -0.031023 0.01678
## 66 AUC_poly dose_10 -0.03583 -0.059754 -0.01191
## 67
      AUC_poly dose_25 -0.07519 -0.099088 -0.05129
## 68
      AUC_poly dose_50 -0.09197 -0.115855 -0.06809
      AUC_poly dose_75 -0.10295 -0.126847 -0.07905
## 70 AUC_poly dose_100 -0.12125 -0.142625 -0.09987
cg %>%
     with(figures) %>%
    with( figCI +
```

```
facet_wrap( ~ metric, ncol = 7 ) +
                          theme(axis.text.x = element_text(angle = 90, size = 4)) # rotate & shrink axis text labels
                        ) %>%
            print
                                                           ITGR
                                                                                          AUC
                                                                                                                    ITGR_pwl
                                                                                                                                                   AUC_pwl
                                                                                                                                                                               ITGR_poly
                                                                                                                                                                                                              AUC_poly
                             linear
         0.05
         0.00
∃stimate
       -0.05
       -0.10
       -0.15
                                                  asop — esop — es
                                                                                                                contrast
### Change the contrast and / or testing parameters:
  cg <- models_vismo21 %>% compare_groups( metric = 'AUC', contrast = 'Dunnett' )
  cg %>% with( data ) %>% with( effectDF ) %>% format( digits = 3 )
            metric
                                                      contrast Estimate
                   AUC dose_0.3 - dose_0.0 -0.00351 -0.0293 0.02226
## 1
                   AUC dose_1.0 - dose_0.0 0.00426 -0.0205 0.02903
## 2
## 3
                   AUC dose_3.0 - dose_0.0 -0.02511 -0.0482 -0.00201
                   AUC dose_6.0 - dose_0.0 -0.04843 -0.0728 -0.02409
## 4
## 5
                   AUC dose_10 - dose_0.0 -0.07337 -0.0992 -0.04758
## 6
                   AUC dose_25 - dose_0.0 -0.11521 -0.1433 -0.08711
## 7
                   AUC dose_50 - dose_0.0 -0.13044 -0.1581 -0.10279
## 8
                   AUC dose_75 - dose_0.0 -0.14356 -0.1714 -0.11574
## 9
                   AUC dose_100 - dose_0.0 -0.16070 -0.1871 -0.13434
  cg <- models_vismo21 %>% compare_groups( metric = 'AUC', contrast = 'Dunnett', adjustment_method = 'none')
  cg %>% with( data ) %>% with( effectDF ) %>% format( digits = 3 )
##
            metric
                                                      contrast Estimate
## 1
                   AUC dose_0.3 - dose_0.0 -0.00351 -0.0221 0.01511
                   AUC dose 1.0 - dose 0.0 0.00426 -0.0136 0.02217
## 3
                   AUC dose_3.0 - dose_0.0 -0.02511 -0.0418 -0.00842
## 4
                   AUC dose_6.0 - dose_0.0 -0.04843 -0.0660 -0.03083
## 5
                  AUC dose_10 - dose_0.0 -0.07337 -0.0920 -0.05473
```

AUC dose\_25 - dose\_0.0 -0.11521 -0.1355 -0.09490

## 6

```
AUC dose_50 - dose_0.0 -0.13044 -0.1504 -0.11046
## 7
## 8
       AUC dose_75 - dose_0.0 -0.14356 -0.1637 -0.12345
## 9
       AUC dose_100 - dose_0.0 -0.16070 -0.1798 -0.14164
###
cg <-
   models_vismo21 %>%
   compare_groups( metric = 'AUC', contrast = 'Dunnett', adjustment_method = 'holm', extended_output = TRUE)
cg \%% with( data ) \%% with( effectDF ) \%% format( digits = 3 )
##
                                                                  tstat adj_method pvalues
    metric
                      contrast Estimate
                                          sigma
                                                    lwr
                                                             upr
## 1
       AUC dose_0.3 - dose_0.0 -0.00351 0.00950 -0.0293 0.02224 -0.369
                                                                               holm 1.00e+00
## 2
       AUC dose_1.0 - dose_0.0 0.00426 0.00914 -0.0205 0.02902
                                                                  0.466
                                                                               holm 1.00e+00
       AUC dose_3.0 - dose_0.0 -0.02511 0.00852 -0.0482 -0.00203 -2.948
                                                                               holm 9.60e-03
       AUC dose_6.0 - dose_0.0 -0.04843 0.00898 -0.0728 -0.02410 -5.394
                                                                               holm 2.76e-07
## 5
       AUC dose_10 - dose_0.0 -0.07337 0.00951 -0.0992 -0.04759 -7.713
                                                                               holm 0.00e+00
## 6
       AUC dose_25 - dose_0.0 -0.11521 0.01036 -0.1433 -0.08712 -11.116
                                                                               holm 0.00e+00
                                                                               holm 0.00e+00
## 7
       AUC dose_50 - dose_0.0 -0.13044 0.01020 -0.1581 -0.10281 -12.793
       AUC dose_75 - dose_0.0 -0.14356 0.01026 -0.1714 -0.11575 -13.990
                                                                               holm 0.00e+00
## 8
## 9
       AUC dose_100 - dose_0.0 -0.16070 0.00972 -0.1870 -0.13435 -16.531
                                                                               holm 0.00e+00
### Create a "custom" contrast matrix to summarize arbitrary linear combinations:
vismo21_custom_contrast <-</pre>
 rbind(
                           0,
                                 Ο,
                                        Ο,
                                             0,
                                                                          0 ), ncol = 10 ),
        matrix( c( -1,
                                                   1,
                                                          0, 0,
                                                                    Ο,
                                                         0, 1/3, 1/3, 1/3), ncol = 10),
                                       0,
                                             0,
        matrix( c(-1/3, -1/3, -1/3,
                                                   Ο,
                                 0, -1/4, -1/4, -1/4, -1/4, 1/3, 1/3, 1/3), ncol = 10)
                     Ο,
                           0,
 colnames( vismo21_custom_contrast ) <- levels( vismo21$group_name )</pre>
 rownames( vismo21_custom_contrast ) <- c('ten_minus_zero', 'high_minus_low', 'high_minus_middle')</pre>
 print( t( vismo21_custom_contrast ) )
            ten_minus_zero high_minus_low high_minus_middle
## dose_0.0
                       -1
                              -0.3333333
                                                 0.0000000
                                                 0.0000000
## dose_0.3
                        0
                              -0.3333333
                              -0.3333333
## dose_1.0
                                                 0.0000000
                        0
## dose_3.0
                        0
                               0.0000000
                                                -0.2500000
## dose_6.0
                        0
                               0.0000000
                                                -0.2500000
## dose_10
                        1
                               0.0000000
                                                -0.2500000
## dose_25
                        0
                               0.0000000
                                                -0.2500000
                        0
                                                 0.3333333
## dose_50
                               0.3333333
                        0
                                                 0.3333333
## dose_75
                               0.3333333
## dose_100
                        0
                               0.3333333
                                                 0.3333333
### Pass the customized contrast matrix to the compare groups() function:
 cg <-
  models_vismo21 %>%
  compare_groups( metric = 'AUC',
                  contrast = 'custom',
                  custom_contrast = vismo21_custom_contrast,
                  extended_output = TRUE
 cg %>% with( data ) %>% with( effectDF ) %>% format( digits = 3 )
```

lwr

upr tstat adj\_method pvalues

contrast Estimate sigma

## metric

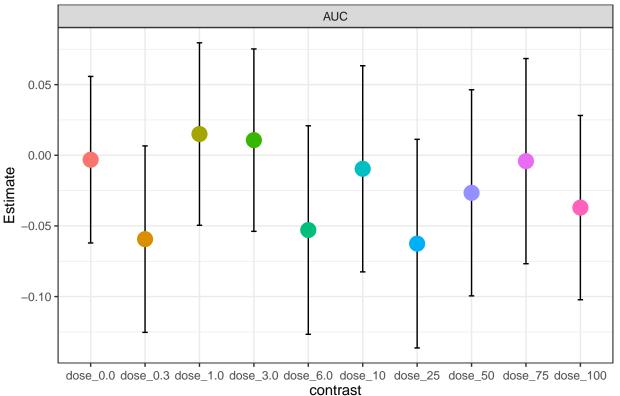
```
## 1 AUC ten_minus_zero -0.0734 0.00951 -0.0959 -0.0509 -7.71 single-step 0
## 2 AUC high_minus_low -0.1451 0.00599 -0.1593 -0.1310 -24.22 single-step 0
## 3 AUC high_minus_middle -0.0794 0.00576 -0.0930 -0.0658 -13.78 single-step 0
```

# 16 In-line permutation tests with permute\_study()

The function permute\_study() takes a study data.frame with group\_name and subject\_ID identifiers and randomly permutes the group membership of each subject, then returns the data frame. A random\_seed parameter is included to facilitate reproducibility.

```
### 8. permute_study()
### Run simple permutation tests.
maeve_reset( )
RS <- 20180830 # random.seed value (optional)
vismo21 %>%
 permute_study( random_seed = RS ) %>%
 model_study
                                     %>%
 predict_study
                                     %>%
 draw_study( fit = 'spline', endpoint_name = 'y', ncol_value = 5 )
           dose_0.0
                                                 dose_1.0
                              dose_0.3
                                                                     dose_3.0
                                                                                        dose_6.0
   6
   5
log(tumor volume + 1)
           dose_10
                              dose_25
                                                 dose_50
                                                                     dose_75
                                                                                       dose_100
   4
             10 15 20
                        0
                                10 15 20
                                            0
                                                    10 15 20 0
                                                                       10 15 20
                                                                                  0
                             5
                                                                   5
                                                                                          10 15 20
                                                    day
vismo21 %>%
 permute_study( random_seed = RS ) %>%
 model_study
 compare_groups( metric = 'AUC' )
 with( data )
                                     %>%
 with( effectDF )
                                     %>%
 format( digits = 3 )
```

```
##
      metric contrast Estimate
                                   lwr
                                           upr
## 1
         AUC dose_0.0 -0.00313 -0.0621 0.05579
## 2
         AUC dose_0.3 -0.05935 -0.1253 0.00662
## 3
         AUC dose_1.0 0.01502 -0.0495 0.07958
         AUC dose 3.0 0.01070 -0.0538 0.07525
## 4
## 5
         AUC dose_6.0 -0.05291 -0.1267 0.02087
         AUC dose_10 -0.00958 -0.0825 0.06336
## 6
## 7
         AUC dose_25 -0.06253 -0.1363 0.01129
         AUC dose_50 -0.02657 -0.0995 0.04636
## 8
## 9
         AUC dose_75 -0.00415 -0.0767 0.06845
## 10
         AUC dose_100 -0.03703 -0.1022 0.02817
vismo21 %>%
 permute_study( random_seed = RS ) %>%
                                    %>%
 model_study
 compare_groups( metric = 'AUC' )
                                    %>%
 with( figures )
                                    %>%
 with( figCI )
                                    %>%
 print
```



# 17 Treatment-to-reference summaries with generate\_summary\_table().

The "summary table" is a Dunnett-themed study summary output by default as a simple study summary. It assumes a designated reference group and focuses mainly on statistics comparing each of the other group regimens to this reference group. A little more explanation of the statistics is included in this section since these measures are not discussed in a manuscript. This functionality is **not necesarily recommended**. It provides support for a number of unpublished "legacy" statistics in use in the setting in which this package was developed, and so is included for back-comparison.

```
### 9. generate_summary_table()
### Reset options for vismodegib dose-response analysis:
maeve_reset() # reset existing options to defaults.
maeve_options( ## maeve_options('metrics_supported') =
                 \begin{tabular}{ll} \begin{tabular}{ll} \#\# & c('linear', 'ITGR', 'AUC', 'ITGR_pwl', 'AUC_pwl', 'ITGR_poly', 'AUC_poly') \end{tabular} 
                metric = maeve_options('metrics_supported'),
                modeling_data_frame = modeling_data_frame_vismo21,
                break_points = c( 0, 7, 14, 21 ),
                poly_degree = 3,
                poly_object = poly_object_vismo21
### Generating a summary table is done for one chosen metric.
### Obviously it could be parallelized, but it's a slow operation (due in part to parametric bootstrapping),
### so we haven't currently done that as it's not used that way.
   summary_linear
                      <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'linear' )
                      <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'ITGR' )
   summary_ITGR
                      <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'AUC' )
   summary_AUC
   ##
                      <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'ITGR_pwl' )
   summary_ITGR_pwl
                      <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'AUC_pwl')
   summary_AUC_pwl
   summary_ITGR_poly <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'ITGR_poly' )
   summary_AUC_poly <- models_vismo21 %>% generate_summary_table( pred_data_frame, metric = 'AUC_poly' )
print( summary_AUC %>% head(4) ) # typical gRED summary table results accessed via IDA.
        group N_first_day first_day integration_first_day integration_last_day fit_last_day last_day PR EOS_CR
## 1 dose_0.0
                        6
                                  0
                                                         0
                                                                              21
                                                                                           21
                                                                                                     21 0
                                                                                                                Λ
## 2 dose_0.3
                        5
                                   0
                                                         0
                                                                              21
                                                                                           21
                                                                                                     21 0
                                                                                                                0
                                                                                                     21 0
## 3 dose_1.0
                        5
                                  Λ
                                                         Λ
                                                                              21
                                                                                           21
                                                                                                                Λ
## 4 dose_3.0
                        5
                                  0
                                                                                                     21 0
                                                         0
                                                                              21
                                                                                           21
     effect_start effect_end effect_duration TTP_2X TTP_5X metric
##
                                                                      Estimate
                                                                                   Diff_Ref
                                                               AUC 0.04234917 0.000000000 0.000000000
          21.0000
                          21
                                      0.0000
                                                17.7
                                                         NΑ
## 2
           3.9309
                          21
                                      17.0691
                                                  NA
                                                                AUC 0.03883934 -0.003509829 0.009502330
## 3
          21.0000
                          21
                                       0.0000
                                                15.3
                                                         NΑ
                                                                AUC 0.04660828 0.004259111 0.009136903
## 4
           0.0000
                          21
                                      21 0000
                                                  NA
                                                         NA
                                                                AUC 0.01723652 -0.025112647 0.008518543
##
             lwr
                          upr
                                    tstat
                                             pvalues xrange_norm_width firstDay_orig
## 1 0.0000000 0.00000000
                                       NA
                                                  NA
                                                                     21
                                                                             240.2550
## 2 -0.02927195  0.022252287 -0.3693651  0.99994595
                                                                     21
                                                                             249.9890
## 3 -0.02051228  0.029030507  0.4661439  0.99963462
                                                                     21
                                                                             222.7022
## 4 -0.04820758 -0.002017713 -2.9479981 0.02506906
                                                                             199.6556
## firstDay_mean_originalScale_reference AUC_orig AUC_originalScale_reference TV_change TV_change_reference
## 1
                                    240.255 384.4930
                                                                          384.493 144.23798
                                                                                                         144.238
## 2
                                    240.255 382.5589
                                                                          384.493 132.56985
                                                                                                         144.238
## 3
                                                                          384.493 152.67537
                                    240.255 375.3776
                                                                                                         144.238
## 4
                                    240.255 240.7940
                                                                          384.493 41.13835
                                                                                                         144.238
            TGI TGI baseline
## 1 0.0000000
                    0.000000
## 2 0.5030336
                    8.089503
## 3 2.3707679
                   -5 849632
## 4 37.3736415
                   71.478839
```

```
group N_first_day first_day integration_first_day integration_last_day fit_last_day last_day PR EOS_CR
## 1 dose_0.0
                        6
                                  0
                                                         0
                                                                              21
                                                                                           21
                                                                                                     21
                                                                                                                0
##
  2 dose_0.3
                        5
                                   0
                                                         0
                                                                              21
                                                                                            21
                                                                                                     21
                                                                                                         0
                                                                                                                0
## 3 dose_1.0
                        5
                                   0
                                                         0
                                                                              21
                                                                                           21
                                                                                                     21
                                                                                                         0
                                                                                                                0
## 4 dose_3.0
                        5
                                   0
                                                         0
                                                                              21
                                                                                            21
                                                                                                     21
                                                                                                                0
     effect_start effect_end effect_duration TTP_2X TTP_5X metric
##
                                                                                   Diff_Ref
                                                                      Estimate
                                                                                                   sigma
## 1
                          NA
                                                         NA linear 0.03667183 0.000000000 0.000000000
               NA
                                           NA
                                                18.9
## 2
               ΝA
                                                         NA linear 0.03218513 -0.004486700 0.008021288
                          NΑ
                                           NΑ
                                                  NΑ
## 3
                                                16.6
                                                         NA linear 0.04171018 0.005038348 0.007769679
               NA
                          NA
                                           NA
## 4
                                                         NA linear 0.01735387 -0.019317964 0.007789886
               NA
                          NA
                                           NA
##
             lwr
                                           pvalues xrange_norm_width firstDay_orig
                         upr
                                   tstat
## 1 0.00000000 0.000000000
                                      NA
                                                                   21
                                                                           252.3722
                                                NA
## 2 -0.02625350 0.017280101 -0.5593491 0.9985380
                                                                   21
                                                                           266.7653
## 3 -0.01604568 0.026122374 0.6484628 0.9955997
                                                                   21
                                                                           232.4604
## 4 -0.04045682 0.001820897 -2.4798777 0.0928704
                                                                   21
                                                                           199.2833
     firstDay_mean_originalScale_reference AUC_orig AUC_originalScale_reference TV_change TV_change_reference
## 1
                                   252.3722 380.7515
                                                                         380.7515 128.37935
                                                                                                        128.3794
## 2
                                   252.3722 381.6893
                                                                         380.7515 114.92392
                                                                                                        128.3794
## 3
                                   252.3722 372.5599
                                                                         380.7515 140.09950
                                                                                                        128.3794
## 4
                                   252.3722 240.6611
                                                                         380.7515 41.37774
                                                                                                        128.3794
##
            TGI TGI_baseline
                    0.000000
## 1 0.0000000
## 2 -0.2462783
                   10.480995
## 3 2.1514476
                   -9.129308
## 4 36.7931492
                   67.769166
print( summary_ITGR_pwl %>% tail(4) )
##
         group N_first_day first_day integration_first_day integration_last_day fit_last_day last_day PR EOS_CR
## 7
       dose 25
                         4
                                    0
                                                          0
                                                                               21
                                                                                             21
                                                                                                      21
## 8
       dose_50
                         4
                                    0
                                                          0
                                                                               21
                                                                                             21
                                                                                                      21
                                                                                                          4
                                                                                                                 0
## 9
                                    0
                                                          0
                                                                                                      21
                                                                                                                 0
       dose 75
                         4
                                                                               21
                                                                                             21
                                                                                                          4
                                                                                                      21
                                    0
                                                          0
                                                                               21
                                                                                             21
                                                                                                                 0
## 10 dose_100
                         5
                                                                                                          5
      effect_start effect_end effect_duration TTP_2X TTP_5X
##
                                                               metric
                                                                          Estimate
                                                                                      Diff_Ref
## 7
                NA
                           NA
                                            NA
                                                   NA
                                                          NA ITGR_pwl -0.05243975 -0.09086999 0.008792934
## 8
                NA
                           NA
                                                   NA
                                                          NA ITGR_pwl -0.07028037 -0.10871061 0.008778359
                                            NA
## 9
                                                          NA ITGR_pwl -0.08261068 -0.12104092 0.008792934
                NA
                           NA
                                            NA
                                                   NA
## 10
                NΑ
                           NA
                                            NA
                                                   NA
                                                          NA ITGR_pwl -0.08865354 -0.12708377 0.008266694
##
                                  tstat pvalues xrange_norm_width firstDay_orig
             lwr
                         upr
## 7
     -0.1147180 -0.06702200 -10.33443
                                                                21
                                              0
                                                                        213.1401
     -0.1325191 -0.08490216 -12.38393
                                              0
                                                                21
                                                                        210.0773
## 9 -0.1448889 -0.09719294 -13.76570
                                              0
                                                                21
                                                                        217.1709
## 10 -0.1495045 -0.10466305 -15.37299
                                              0
                                                                21
                                                                        212.9676
      firstDay_mean_originalScale_reference
                                              AUC_orig AUC_originalScale_reference TV_change TV_change_reference
## 7
                                    233.8458 103.25907
                                                                           385.2784 -109.8810
                                                                                                          151,4326
                                                                           385.2784 -118.6889
## 8
                                              91.38845
                                    233.8458
                                                                                                          151.4326
## 9
                                              88.08513
                                                                           385.2784 -129.0858
                                    233.8458
                                                                                                          151,4326
## 10
                                    233.8458
                                              71.13444
                                                                           385.2784 -141.8331
                                                                                                          151.4326
           TGI TGI_baseline
##
     73.19884
## 7
                   172.5610
## 8
     76.27989
                   178.3773
## 9
     77.13728
                   185.2430
## 10 81.53687
                   193.6609
print( summary_AUC_poly %>% tail(3) )
##
         group N_first_day first_day integration_first_day integration_last_day fit_last_day last_day PR EOS_CR
## 8
       dose_50
                         4
                                    0
                                                          0
                                                                               21
                                                                                             21
                                                                                                      21 4
```

```
## 9
       dose 75
                          4
                                    0
                                                           0
                                                                                21
                                                                                             21
                                                                                                       21
                                                                                                           4
                                                                                                                  0
## 10 dose_100
                          5
                                    0
                                                           0
                                                                                21
                                                                                             21
                                                                                                       21
                                                                                                           5
                                                                                                                  0
      effect_start effect_end effect_duration TTP_2X TTP_5X
##
                                                                         Estimate
                                                                                     Diff Ref
                                                                metric
                                                                                                    sigma
                                                                                                                 lwr
                            NA
                                            NA
                                                   NA
                                                           NA AUC_poly -0.0919713 -0.1381770 0.01101442 -0.1680480
## 8
                NA
## 9
                NA
                                                   NA
                                                           NA AUC_poly -0.1029460 -0.1491517 0.01101917 -0.1790356
                            ΝA
                                            NA
## 10
                NA
                            NA
                                            NA
                                                   NA
                                                           NA AUC_poly -0.1212450 -0.1674507 0.01033735 -0.1954855
##
                      tstat pvalues xrange norm width firstDay orig firstDay mean originalScale reference
             upr
## 8
      -0.1083060 -12.54510
                                  0
                                                    21
                                                            217.0043
## 9
      -0.1192678 -13.53565
                                  0
                                                    21
                                                            223.7284
                                                                                                      231.93
  10 -0.1394160 -16.19861
                                  0
                                                   21
                                                            216.1371
                                                                                                      231.93
##
      AUC_orig AUC_originalScale_reference TV_change TV_change_reference
                                                                                 TGI
                                                                                     TGI_baseline
## 8
      90.63241
                                    386.005 -126.3719
                                                                   154.075 76.52040
                                                                                         182.0197
## 9
      87.38633
                                    386.005 -136.3421
                                                                   154.075 77.36135
                                                                                         188.4907
## 10 70.62451
                                    386.005 -145.5126
                                                                   154.075 81.70373
                                                                                         194.4427
### You can also pass multiple metrics if this is desirable. It might get slow, but is handy to compare
### summary table statistics across different metrics. Here, e.g., we compare TGI_baseline computed
### using the metrics 'linear', and 'AUC':
summary_linear_and_AUC = models_vismo21 %>% generate_summary_table( pred_data_frame, metric = c('linear','AUC') )
summary_linear_and_AUC %>% dplyr::select( group, metric, TGI_baseline ) %>% tidyr::spread( key = metric, -group )
##
         group
                   linear
                                  AUC
## 1
      dose_0.0
                 0.000000
                             0.00000
## 2
      dose_0.3
                10.480995
                             8.089503
## 3
      dose_1.0
                -9.129308
                            -5.849632
## 4
      dose_3.0 67.769166
                           71.478839
## 5
      dose_6.0 111.124520 110.018841
## 6
       dose_10 143.880197 143.887731
## 7
       dose_25 148.874564 174.713311
## 8
       dose_50 166.404573 182.052168
```

#### 17.1 End of Study Complete Response and Partial Response

Two kinds of responses are assessed and recorded. Note that in both cases, the "math" of response-determination is done on the original scale of the endpoint rather than the transformed scale (e.g., on "tumor volume" rather than "log-transformed tumor volume"). These are computed from the observed values rather than model-fitted values.

#### 17.1.1 End of Study Complete Response (EOS CR)

dose\_75 179.072966 192.266437 dose\_100 166.282867 196.889486

A complete response is one for which a tumor is not detectable at the last observation. Specifically, the tumor must have a value at or below the value EOS\_CR\_minval in maeve\_options( "EOS\_CR\_minval"). By default, EOS\_CR\_minval = 0 but can be changed to account for the endpoint and measurement system (e.g., if "less than detectable" for an endpoint were coded as a common, low number). If TUMOR\_VOLUME were kept as the endpoint\_name variable, then a value of maeve\_options( EOS\_CR\_minval = 50) would cause any tumor with a final reading at or below 50 mm<sup>3</sup> to be classified as a complete response.

#### 17.1.2 Partial Response (PR)

## 9

## 10

A partial response is a tumor that is not an End of Study Complete Response, but for which at least one observation fell at or below a specified fraction of that tumor's baseline size. The "specified fraction" is controlled by the parameter PR\_threshold in maeve\_options( "PR\_threshold") and passed to the function

generate\_summary\_table(). By default, PR\_threshold = 0.5 in maeve. Note that by construction, PR and EOS CR are mutually exclusive categories.

#### 17.1.3 A demonstration of counted responses with simulated data

These two counts are next demonstrated with the simulated data set bifurcatedGrowthSim. This data set has values on the unit interval with no censoring.

```
maeve_reset() # set all options to package defaults.

maeve_options( metric = 'AUC', ncol_value = 4, truncate_fit = TRUE )

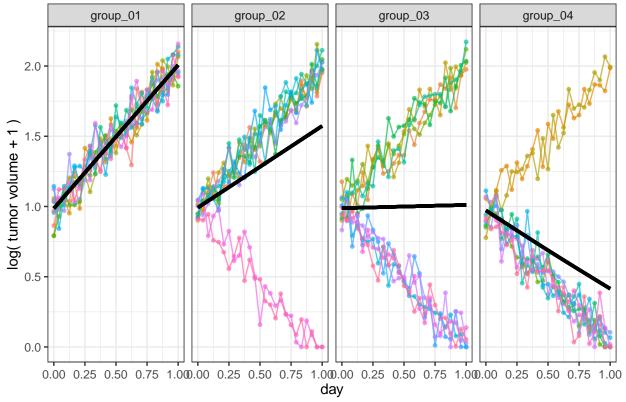
## An R data file (".rda" format) is stored in /inst/extdata/data/
load( system.file( 'extdata', 'data', 'bifurcatedGrowthSim.rda', package = 'maeve' ) )

### Fit models

model_list <- bifurcatedGrowthSim %>% model_study( number_basis_vecs = 5 )

### Set endpoint name for figures:
maeve_options( endpoint_name = 'y' ) # 'y' will be the transformed response -- usually what we want for graphics.

### Predict responses from models
model_list %>%
predict_study %>%
draw_study( fit = 'spline', endpoint_name = 'y', alpha_value = 0.67 ) %>%
print
```



```
### Set prediction grid options and store predictions in a data frame
maeve_options( x_pred_type = 'grid', x_pred_spacing = 0.025 )
pred_data_frame = predict_study( model_list )
```

Next, run the maeve::generate\_summary\_table() and select out the reported counts.

Since this simulated data set has no censoring and linear (albeit bifurcated) trends, a simple if informal check on the results is to filter out the rows at the final time point (DAY\_OF\_STUDY == 1) with small tumor volumes. Based on the picture of log tumor volume, we picked TUMOR\_VOLUME < 4. The filtered values are ordered first by group, then in descending order of TUMOR\_VOLUME within group. The observed counts should recapitulate the count table just above.

```
bifurcatedGrowthSim %>%
  dplyr::filter( DAY_OF_STUDY >= 1, TUMOR_VOLUME < 4 ) %>%
  dplyr::select( group_name, animalID, DAY_OF_STUDY, TUMOR_VOLUME ) %>%
  dplyr::arrange( group_name, desc( TUMOR_VOLUME ) ) %>%
  format( digits = 3 )
```

```
group_name animalID DAY_OF_STUDY TUMOR_VOLUME
##
## 1
                   id_019
       group_02
                                     1
                                             0.0000
## 2
       group_02
                  id_020
                                     1
## 3
       group_03
                  id_029
                                             0.1479
                                     1
## 4
       group_03
                  id_030
                                             0.0553
                                     1
## 5
       group_03
                  id_028
                                             0.0270
                                     1
## 6
       group_03
                   id_026
                                     1
                                             0.0000
## 7
       group_03
                   id_027
                                     1
                                             0.0000
## 8
                   id_037
                                             0.1093
       group_04
                                     1
## 9
       group_04
                   id_036
                                     1
                                             0.0679
                   id_038
                                             0.0167
## 10
       group_04
                                     1
## 11
                   id_034
                                             0.0035
       group_04
                                     1
## 12
       group_04
                   id_033
                                     1
                                             0.0000
                                             0.0000
## 13
       group_04
                   id_035
                                     1
## 14
       group_04
                   id_039
                                     1
                                             0.0000
                                             0.0000
## 15
       group_04
                   id_040
```

Finally, we connect this back to the tally\_study() function discussed earlier. If we want *only* the partial and complete responses, we could skip using generate\_summary\_table() and instead compute them in tally\_study():

```
maeve_reset()
tally_study(bifurcatedGrowthSim, response = c('PR', 'EOS_CR') ) %>%
## select out a subset of columns for presentation and round off the digits:
dplyr::select( group_name, N_in_group, PR:EOS_CR_SE_log_OR ) %>%
format( digits = 3 )
```

## group\_name N\_in\_group PR PR\_log\_OR PR\_SE\_log\_OR EOS\_CR EOS\_CR\_log\_OR EOS\_CR\_SE\_log\_OR

## 1	group_01	10	0	0.00	0.00	0	0.00	0.00
## 2	group_02	10	0	0.00	2.05	2	1.82	1.62
## 3	group_03	10	3	2.28	1.59	2	1.82	1.62
## 4	group_04	10	4	2.68	1.57	4	2.68	1.57

#### 17.2 Effect Duration statistics

Effect duration is a relative metric, pre-supposing a chosen control / reference group with growth curve  $g_0(t)$  against which a treatment group with growth curve  $g_1(t)$  is compared over a time interval [a, b]. On this interval, the time of effect start  $T_s$  & effect end  $T_e$  are defined. Effect duration is the time elapsed between the effect start and end.

1. Time of the start of efficacy  $T_s$  is defined as the first time in [a, b] such that the growth rate for treatment is less than that for control, i.e.,

$$T_s = \min_{t \in [a,b]} \{ t : g_1'(t) < g_0'(t) \}$$

This time can be (and often is) at an interval endpoint.

2. Time of the end of efficacy  $T_e$  is then the first time after efficacy starts such that the growth rate for treatment matches or exceeds the growth rate for control at time  $t = T_s$ , i.e.,

$$T_e = \min_{t \in [T_s, b]} \{t : g_1'(t) \ge g_0'(T_s)\}$$

This time can also be at an interval endpoint.

3. The effect duration is defined as the time elapsed time  $T_e - T_s$ .

The effect duration statistics are computed only from the spline model (not linear, piecewise linear, or simple polynomial), so they will be NA unless metric = "ITGR" or metric = "AUC".

Here is the model fitting with the default spline summary measures:

```
maeve_reset() # set all options to package defaults.
maeve_options( ncol_value = 4, truncate_fit = TRUE )
## An R data file (".rda" format) is stored in /inst/extdata/data/
load( system.file( 'extdata', 'data', 'effect_duration_trig_sim.rda', package = 'maeve' ) )
### Set working data
### data( effect_duration_trig_sim, package = 'maeve' )
## ### Presence pattern ("0" or "1") for filtered data:
  effect_duration_trig_sim %>%
##
     dplyr::select( group_name, DAY_OF_STUDY ) %>%
##
##
     unique %>%
##
     table %>%
##
     t()
            %>%
    print
### Fit models
 model_list <- effect_duration_trig_sim %>% model_study( number_basis_vecs = 8 )
```

## boundary (singular) fit: see ?isSingular

```
### Set endpoint name for figures:
 maeve_options( endpoint_name = 'y' ) # 'y' is the transformed response & usually what we want for graphics.
### Predict responses from models
 model_list %>%
  predict_study %>%
  draw_study( fit = 'spline', endpoint_name = 'y' ) %>%
             group_01
                                      group_02
                                                              group_03
                                                                                      group_04
log( tumor volume + 1 )
    3
     0.00 \ \ 0.25 \ \ 0.50 \ \ 0.75 \ \ 1.000.00 \ \ 0.25 \ \ 0.50 \ \ 0.75 \ \ 1.000.00 \ \ 0.25 \ \ 0.50 \ \ 0.75 \ \ 1.000.00
                                                    day
### run some compare_groups() analyses just to check against the later results in
### maeve::generate summary table():
 cg_Identity_AUC <-
 compare_groups( model_list, metric = 'AUC', xmin = 0, xmax = 1, contrast = 'Identity', draw_figure = FALSE )
 print( cg_Identity_AUC$data$effectDF )
     metric contrast
                         Estimate
        AUC group_01 2.54986444 2.49489499 2.60483389
        AUC group_02 2.54375340 2.48732110 2.60018569
## 3
        AUC group_03 -1.99768797 -2.05364326 -1.94173269
        AUC group_04 -0.03243146 -0.08847461 0.02361169
### Use the 'ITGR' metric over [0, 1], which gives results quite different from 'AUC':
 cg_Identity_ITGR <-
 compare_groups( model_list, metric = 'ITGR', xmin = 0, xmax = 1, contrast = 'Identity', draw_figure = FALSE )
 print( cg_Identity_ITGR$data$effectDF )
##
     metric contrast
                           Estimate
                                            lwr
       ITGR group_01 2.0072999882 1.96605813 2.048541844
## 1
## 2
       ITGR group_02  0.0001976487 -0.04300768  0.043402980
```

## 3

```
### Dunnett comparisons with 'AUC':
cg_Dunnett <-
 compare_groups( model_list, metric = 'AUC', xmin = 0, xmax = 1, contrast = 'Dunnett', draw_figure = FALSE )
print( cg_Dunnett$data$effectDF )
##
    metric
                       contrast
                                     Estimate
        AUC group_02 - group_01 -0.006111045 -0.08039672 0.06817463
## 1
        AUC group_03 - group_01 -4.547552415 -4.62151655 -4.47358828
        AUC group_04 - group_01 -2.582295899 -2.65631916 -2.50827264
Here are the estimated first derivatives of the trigonometric growth curves:
### Set prediction grid options and store predictions in a data frame
pred_data_frame = predict_study( model_list, x_pred_type = 'grid', x_pred_spacing = 0.025 )
### Draw numerically estimated first derivatives for each estimated group-level response:
deriv_norm_fig <-</pre>
pred_data_frame %>%
 dplyr::select( group, x, pred_gam_deriv1 ) %>%
 unique() %>%
 ggplot( aes( x, pred_gam_deriv1, colour = group ) ) +
 geom_line( ) # + geom_vline( xintercept = c( .4174, .5796 ), lty = 3 )
print( deriv_norm_fig )
    4
ored_gam_deriv1
                                                                                      group
                                                                                          group_01
                                                                                           group_02
                                                                                           group_03
                                                                                           group_04
```

Here are the estimates of effect duration statistics, with confidence intervals based on parametric bootstrapping.

0.75

1.00

0.50

Χ

-4

0.00

0.25

```
x_{time_spacing} = 0.01,
                          metric = 'AUC',
                          conf_int = "none"
EffectDuration_tab %>%
 dplyr::select( group, effect_start, effect_end, effect_duration ) %>%
 print
        group effect_start effect_end effect_duration
## 1 group_01
                   1.0000
                               1.0000
                                               0.0000
## 2 group_02
                    0.3644
                               1.0000
                                               0.6356
## 3 group_03
                    0.0000
                               0.5986
                                               0.5986
## 4 group_04
                    0.0841
                               0.4174
                                               0.3333
if(FALSE){ ## ERROR note (20200625):
## There is a known bug to be resolved in
## getting confidence intervals for the
## EffectDuration via the parametric bootstrap.
EffectDuration_tab_with_CI <-</pre>
 generate_summary_table( model_list,
                          pred_data_frame,
                          xmin = 0, xmax = 1,
                          x_{time_spacing} = 0.01,
                          metric = 'AUC',
                          conf_int = "Effect_Duration"
EffectDuration_tab_with_CI %>%
 dplyr::select( group, effect_start,
                                         CI_lower_Eff_Start, CI_upper_Eff_Start ) %>%
 format( digits = 4 ) %>%
 print
EffectDuration_tab_with_CI %>%
  dplyr::select( group, effect_end,
                                         CI_lower_Eff_End,
                                                              CI_upper_Eff_End ) %>%
 format( digits = 4 ) %>%
 print
EffectDuration_tab_with_CI %>%
 dplyr::select( group, effect_duration, CI_lower_Eff_Dur,
                                                              CI_upper_Eff_Dur
                                                                                 ) %>%
 format( digits = 4 ) %>%
 print
} ## end of ' if(FALSE){ ## ERROR note (20200625): ...'
```

#### 17.3 Legacy metrics TGI and TGIb

In the special case that attention is restricted to so-called Dunnett comparisons (i.e., compare the effect of each treatment to a common reference group), the gRED legacy reporting tool reports two summaries of treatment effect, which we include here. These are referred to as tumor growth inhibition (TGI) and tumor growth inhibition baseline-normalized (TGIb).

#### 17.3.1 Tumor Growth Inhibition (TGI)

Tumor growth inhibition is the ratio between treatment and control of areas under the respective growth curves on the *original* scale (i.e., any transformation of the raw measurements is inverted point-wise before numerical integration). We introduce the notation  $V_{\beta_i}(t) \equiv h^{-1}(g_{\beta_i}(t))$  for this inverted function with the mnemonic that  $V_{\beta_i}(t)$  describes the tumor *volume* over the study times  $t \in [a, b]$ . Without loss of generality, denote by i = 1 the reference group. Then for  $i \in 2, ..., I$ , define the TGI of group i relative to reference by

$$\hat{\text{TGI}}_{i} \equiv \begin{pmatrix} \int_{t=a}^{b} V_{\hat{\beta}_{i}}(t)dt \\ 1 - \frac{t=a}{b} V_{\hat{\beta}_{1}}(t)dt \end{pmatrix} \times 100\%$$

Note that even when the model holds, typically neither the dividend nor the divisor (nor their ratio) will follow a Gaussian distribution. Consequently, inference uses a parametric bootstrap.

#### 17.3.2 Tumor Growth Inhibition normalized, baseline-normalized (TGIb)

Tumor growth inhibition baseline-normalized (TGIb) extends the TGI measure by inverting the fitted curves to the original scale and also subtracting out the estimated baseline tumor burden from each group prior to numerical integration. Again letting i=1 denote the reference group, the baseline-normalized tumor growth inhibition of group i ( $i \in 2,...,I$ ) relative to reference is

$$\mathbf{T}\hat{\mathbf{G}}\mathbf{I}\mathbf{b}_{i} \equiv \begin{pmatrix} \int_{t=a}^{b} V_{\hat{\beta}_{i}}(t)dt - \left[ (b-a) \times V_{\hat{\beta}_{i}}(a) \right] \\ \int_{t-a}^{b} V_{\hat{\beta}_{1}}(t)dt - \left[ (b-a) \times V_{\hat{\beta}_{1}}(a) \right] \end{pmatrix} \times 100\%$$

The terms subtracted within the numerator and denominator can be interpreted as areas of rectangles with base lengths equal to the evaluated study period (b-a) and heights the estimated initial tumor burdens  $V_{\hat{\beta}_i}(a)$  and  $V_{\hat{\beta}_1}(a)$  for the respective groups. Like TGI, the TGIb statistic typically will not fillow a Gaussian sampling distribution but is amenable to parametric bootstrapping. Note also that by the centering and scaling, the statistic is negative for treatments inducing tumor regression, zero for the case of treatment stasis, and one for the case that treatment is exactly like the reference. It is undefined in the case of stasis for the reference group, but this was typically regarded as a failed experiment anyway, and so not of interest to analyze.

These will also be demonstrated with a simulated data set, but not yet.

```
maeve_reset() # set all options to package defaults.

maeve_options( ncol_value = 3, truncate_fit = TRUE )

## An R data file (".rda" format) is stored in /inst/extdata/data/
load( system.file( 'extdata', 'data', 'logQuadraticGrowthSim_01.rda', package = 'maeve' ) )

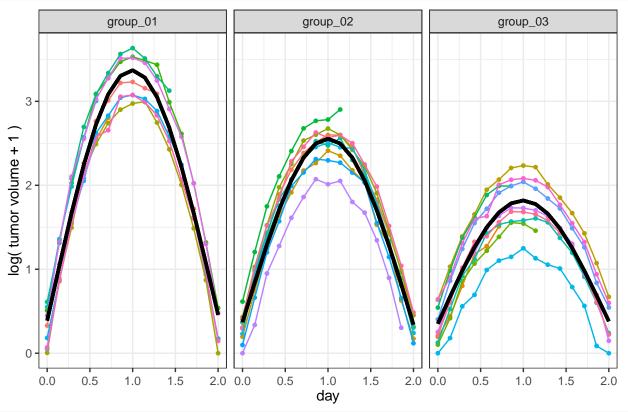
maeve_options( add_to_endpoint = 0 ) # This has been the case for log-quadratic data.

### Fit models
model_list <- logQuadraticGrowthSim_01 %>% model_study( number_basis_vecs = 4 )
```

## boundary (singular) fit: see ?isSingular

```
### Set endpoint name for figures:
maeve_options( endpoint_name = 'y' ) # 'y' is the transformed response & usually what we want for graphics.

### Plot transformed raw data along with predicted responses from models
model_list %>%
    predict_study %>%
    draw_study( fit = 'spline', endpoint_name = 'y' ) %>%
    print
```



```
### run some compare_groups() analyses just to check against the later results in
### maeve::generate_summary_table():
cg_Identity_AUC <-
compare_groups( model_list, metric = 'AUC', xmin = 0, xmax = 2, contrast = 'Identity', draw_figure = FALSE )
print( cg_Identity_AUC$data$effectDF )</pre>
```

metric contrast Estimate

```
## 1
        AUC group_01 1.8941538 1.8464886 1.9418190
        AUC group_02 1.3723123 1.3257152 1.4189095
## 3
        AUC group_03 0.9312421 0.8859001 0.9765841
pred_data_frame = predict_study( model_list, x_pred_type = 'grid', x_pred_spacing = 0.025 )
### Plot original-scale raw data along with back-transformed predicted responses from model
model_list %>%
 predict_study %>%
 dplyr::mutate( # make a "just-in-time" version of back-transformed spline fit:
            pred_gam_orig = get(maeve_options('inv_func_char'))( pred_gam ) - maeve_options('add_to_endpoint')
                ) %>%
  draw_study(
                          fit = 'spline',
                endpoint_name = 'y_orig',
                                                 # raw data in original units.
             spline_predictor = 'pred_gam_orig', # spline back-transformed to original units
```

```
y_label = 'tumor volume' # This plot is on original scale, not transformed.
) %>%
print
```

```
group_01
                                                           group_02
                                                                                                  group_03
   30
tumor volume
   10
       0.0
                0.5
                        1.0
                                 1.5
                                         2.0 0.0
                                                      0.5
                                                               1.0
                                                                       1.5
                                                                                2.0 0.0
                                                                                             0.5
                                                                                                     1.0
                                                                                                              1.5
                                                                                                                      2.0
                                                              day
```

```
##
       group firstDay_orig AUC_orig
                                           TGI CI_lower_TGI CI_upper_TGI TGI_baseline CI_lower_TGI_baseline
## 1 group_01
                   1.474535 13.756706 0.00000
                                                    0.00000
                                                                 0.00000
                                                                              0.00000
                                                                                                    0.00000
## 2 group_02
                   1.448701 6.980962 49.25412
                                                   37.23994
                                                                59.45747
                                                                             54.95698
                                                                                                   44.20848
                                                                                                   74.27090
## 3 group_03
                   1.421071 3.955257 71.24852
                                                   64.48368
                                                                77.09190
                                                                             79.36695
## CI_upper_TGI_baseline
                   0.00000
## 1
## 2
                  64.14806
## 3
                  83.63099
```

#### 17.4 Appendix: R Session Information

[56] Matrix\_1.2-18 assertthat\_0.2.1 minqa\_1.2.4 rstudioapi\_0.11 R6\_2.4.1

[61] boot\_1.3-25 nlme\_3.1-148 compiler\_4.0.0

sessionInfo() %>% print R version 4.0.0 (2020-04-24) Platform: x86\_64-pc-linux-gnu (64-bit) Running under: CentOS Linux 7 (Core) Matrix products: default BLAS: /gstore/apps/R/R\_4.0.0\_Bioc\_3.11/R-4.0.0-Bioc-3.11-tst-20200504/lib64/R/lib/libRblas.so LAPACK: /gstore/apps/R/R 4.0.0 Bioc 3.11/R-4.0.0-Bioc-3.11-tst-20200504/lib64/R/lib/libRlapack.so locale: [1] LC CTYPE=en US.UTF-8 LC NUMERIC=C LC TIME=en US.UTF-8 [4] LC\_COLLATE=en\_US.UTF-8 LC\_MONETARY=en\_US.UTF-8 LC\_MESSAGES=en\_US.UTF-8 [7] LC PAPER=en US.UTF-8 LC NAME=C LC ADDRESS=C [10] LC\_TELEPHONE=C LC\_MEASUREMENT=en\_US.UTF-8 LC\_IDENTIFICATION=C attached base packages: [1] stats graphics grDevices utils datasets methods base other attached packages: [1] ggplot2 3.3.2 maeve 0.9.9.40 magrittr 1.5 bookdown 0.20 rmarkdown 2.3 loaded via a namespace (and not attached): [1] statmod\_1.4.34 zoo\_1.8-8 settings\_0.2.4 tidyselect\_1.1.0 xfun\_0.15 [6] purrr 0.3.4 splines 4.0.0 lattice 0.20-41 colorspace 1.4-1 vctrs 0.3.1 [11] generics\_0.0.2 expm\_0.999-4 htmltools\_0.5.0 gamm4\_0.2-6 yaml\_2.2.1 [16] mgcv\_1.8-31 utf8\_1.1.4 survival\_3.2-3 rlang\_0.4.6 pillar\_1.4.4 [21] nloptr\_1.2.2.1 glue\_1.4.1 withr\_2.2.0 multcomp\_1.4-13 lifecycle\_0.2.0 [26] plyr\_1.8.6 stringr\_1.4.0 munsell\_0.5.0 gtable\_0.3.0 mvtnorm\_1.1-1 [31] codetools 0.2-16 evaluate 0.14 forcats 0.5.0 labeling 0.3 knitr 1.29 [36] fansi\_0.4.1 TH.data\_1.0-10 Rcpp\_1.0.4.6 scales\_1.1.1 farver\_2.0.3 [41] lme4\_1.1-23 digest\_0.6.25 stringi\_1.4.6 dplyr\_1.0.0 grid\_4.0.0 [46] cli 2.0.2 tools 4.0.0 sandwich 2.5-1 DescTools 0.99.36 tibble 3.0.1 [51] tidyr\_1.1.0 crayon\_1.3.4 pkgconfig\_2.0.3 ellipsis\_0.3.1 MASS\_7.3-51.6