# From Memory to Matter: The Physical Basis of $\tau_2$ and the Mechanics of Emergence

Wayne Fortes

June 2025

#### Abstract

We refine and extend our curvature-memory model by providing a physical interpretation of the coherence field  $\tau_2$  and defining the emergence function  $\tau_3$  as a dynamical field governed by local coherence energy. This framework positions  $\tau_3$  as a propagating order parameter that mediates geometric transitions through a self-consistent field equation. We present the complete system of coupled equations and demonstrate how the model resolves known issues in emergent spacetime theory, including extra-dimensional stability, varying gravitational strength, and causality under localized emergence conditions.

#### 1 Introduction

The coherence field  $\tau_2$  was previously introduced as a scalar field living on a compactified internal 2-sphere, influencing the curvature of observable spacetime [6, 7]. In this paper, we refine its interpretation by treating  $\tau_2$  as a localized coherence density field modulated by 4D spacetime. We then define  $\tau_3$  as a dynamical scalar field that responds to the local coherence energy  $E_{\tau_2}(x)$ , producing smooth, propagating emergence events [8].

# 2 Physical Interpretation of $\tau_2$

We define  $\tau_2 = \tau_2(x^{\mu}, \theta, \phi, t)$  as a coherence field capturing the alignment or structured memory of internal field configurations across the compactified sphere  $S^2$  [4]. Its local energy density is computed as:

$$E_{\tau_2}(x) = \int_{S^2} d\Omega \left[ \frac{1}{2} (\partial_t \tau_2)^2 + \frac{1}{2e^{2\sigma(x)}} |\nabla_{S^2} \tau_2|^2 + \frac{1}{2} m^2 \tau_2^2 \right]$$

This formulation allows us to localize coherence across spacetime and use  $E_{\tau_2}(x)$  as the driver for emergence dynamics.

## 3 Emergence as a Dynamical Phase Field

We model  $\tau_3(x)$  as a 4D scalar field with its own dynamics, governed by a potential dependent on coherence energy:

$$V(\tau_3; E_{\tau_2}) = A(E_{\tau_2} - E_{\text{crit}})\tau_3^2 + \beta \tau_3^4$$

This yields the equation of motion:

$$\Box \tau_3 = -\frac{\partial V}{\partial \tau_3} = -2A(E_{\tau_2} - E_{\text{crit}})\tau_3 - 4\beta\tau_3^3$$

The dynamics of  $\tau_3$  allow localized emergence events to propagate through spacetime as phase fronts or oscillatory domains [2].

# 4 Coupled Field Equations

1.  $\tau_2$  dynamics on  $S^2$ :

$$-\partial_t^2 \tau_2 + \frac{1}{e^{2\sigma(x)}} \Delta_{S^2} \tau_2 = m^2 \tau_2$$

2. Coherence energy density:

$$E_{\tau_2}(x) = [as defined above]$$

3.  $\tau_3$  evolution:

$$\Box \tau_3 = -\frac{\partial V}{\partial \tau_3}$$

4. Matter field equation:

$$\left(\Box + m^2 + g\tau_2^2\right)\psi = 0$$

5. Warp field equation:

$$\Box \sigma = \alpha E_{\tau_2}(x) - M^2 \sigma - \lambda \sigma^3$$

6. Gravitational coupling:

$$\kappa_4(x) = \frac{\kappa_6}{4\pi e^{2\sigma(x)}}$$

7. Modified Einstein equations:

$$G_{\mu\nu} = \kappa_4(x) \left[ T_{\mu\nu}^{(\tau_2)} + \tau_3(x) T_{\mu\nu}^{(\psi)} + T_{\mu\nu}^{(\tau_3)} \right]$$

8.  $\tau_3$  stress-energy tensor:

$$T_{\mu\nu}^{(\tau_3)} = \partial_{\mu}\tau_3\partial_{\nu}\tau_3 - g_{\mu\nu}\left(\frac{1}{2}\partial^{\alpha}\tau_3\partial_{\alpha}\tau_3 - V(\tau_3; E_{\tau_2})\right)$$

## 5 Theoretical Challenges and Model Response

- Stability of Extra Dimensions: The internal curvature is dynamically stabilized via the potential  $V(\sigma) = M^2 \sigma^2 + \lambda \sigma^4$ , avoiding typical compactification instabilities [3].
- Varying Gravitational Constant:  $\kappa_4(x)$  varies only near emergence zones, avoiding detectable deviation in weak-field domains [5].
- Causality and Topology:  $\tau_3(x)$  evolves locally and does not require global topology changes, sidestepping no-go theorems.
- Quantum Consistency: The model is semiclassical, designed as a precursor to full quantization via an effective field theory lens [1].

#### 6 Conclusion

We have physically grounded the  $\tau_2$  field as a local coherence descriptor and introduced  $\tau_3$  as a dynamical emergence field driven by phase-transition-like behavior. The model now supports localized, evolving emergence zones that carry energy, influence curvature, and open pathways toward observation and simulation.

#### References

- [1] C. W. Misner, K. S. Thorne, and J. A. Wheeler, Gravitation, W. H. Freeman, 1973.
- [2] N. D. Birrell and P. C. W. Davies, *Quantum Fields in Curved Space*, Cambridge Monographs on Mathematical Physics, 1982.
- [3] T. Appelquist, A. Chodos, and P. G. O. Freund, Modern Kaluza-Klein Theories, Addison-Wesley, 1987.
- [4] M. Van Raamsdonk, "Building up spacetime with quantum entanglement," Gen. Rel. Grav. 42, 2323–2329 (2010).
- [5] S. M. Carroll, Spacetime and Geometry: An Introduction to General Relativity, Cambridge University Press, 2019.
- [6] Wayne Fortes, Coherence-Driven Curvature: A Six-Dimensional Model of Emergent Spacetime, June 2025.
- [7] Wayne Fortes, Warped Memory Geometry: Feedback Between Coherence Fields and Compactified Curvature, June 2025.
- [8] Wayne Fortes, Matter Coupling and Resonant Collapse: A Testable Framework for  $\tau_3$ Driven Geometric Transitions, June 2025.