HW4 wgeither

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For each assignment, turn in by the due date/time. Late assignments must be arranged prior to submission. In every case, assignments are to be typed neatly using proper English in Markdown.

The last couple of weeks, we spoke about vector/matrix operations in R, discussed how the apply family of functions can assist in row/column operations, and how parallel computing in R is enabled. Combining this with previous topics, we can write functions using our Good Programming Practices style and adhere to Reproducible Research principles to create fully functional, redable and reproducible code based analysis in R. In this homework, we will put this all together and actually analyze some data. Remember to adhere to both Reproducible Research and Good Programming Practices, ie describe what you are doing and comment/indent code where necessary.

R Vector/matrix manipulations and math, speed considerations R's Apply family of functions Parallel computing in R, foreach and dopar

Problem 2: Using the dual nature to our advantage

Sometimes using a mixture of true matrix math plus component operations cleans up our code giving better readibility. Suppose we wanted to form the following computation:

•
$$while(abs(\Theta_0^i - \Theta_0^{i-1}) \text{ AND } abs(\Theta_1^i - \Theta_1^{i-1}) > tolerance)$$
 {
$$\Theta_0^i = \Theta_0^{i-1} - \alpha \frac{1}{m} \sum_{i=1}^m (h_0(x_i) - y_i)$$

$$\Theta_1^i = \Theta_1^{i-1} - \alpha \frac{1}{m} \sum_{i=1}^m ((h_0(x_i) - y_i)x_i)$$
 }

}

Where $h_0(x) = \Theta_0 + \Theta_1 x$.

Given **X** and \vec{h} below, implement the above algorithm and compare the results with $\text{lm}(h\sim0+\mathbf{X})$. State the tolerance used and the step size, α .

```
set.seed(1256)
theta <- as.matrix(c(1,2),nrow=2)
X \leftarrow cbind(1,rep(1:10,10))
h <- X%*%theta+rnorm(100,0,0.2)
```

Problem 3

The above algorithm is called Gradient Descent. This algorithm, like Newton's method, has "hyperparameters" that are determined outside the algorithm and there are no set rules for determing what settings to use. For gradient descent, you need to set a start value, a step size and tolerance.

Part a. Using a step size of $1e^{-7}$ and tolerance of $1e^{-9}$, try 10000 different combinations of start values for β_0 and β_1 across the range of possible β 's +/-1 from true determined in Problem 2, making sure to take advantages of parallel computing opportunities. In my try at this, I found starting close to true took 1.1M iterations, so set a stopping rule for 5M. Report the min and max number of iterations along with the starting values for those cases. Also report the average and stdev obtained across all 10000 β 's.

Part b. What if you were to change the stopping rule to include our knowledge of the true value? Is this a good way to run this algorithm? What is a potential problem?

Part c. What are your thoughts on this algorithm?

Problem 4: Inverting matrices

Ok, so John Cook makes some good points, but if you want to do:

$$\hat{\beta} = (X'X)^{-1}X'y$$

what are you to do?? Can you explain what is going on?

Problem 5: Need for speed challenge

In this problem, we are looking to compute the following:

$$y = p + AB^{-1}(q - r) (1)$$

Where A, B, p, q and r are formed by:

```
set.seed(12456)

G <- matrix(sample(c(0,0.5,1),size=16000,replace=T),ncol=10)
R <- cor(G) # R: 10 * 10 correlation matrix of G
C <- kronecker(R, diag(1600)) # C is a 16000 * 16000 block diagonal matrix
id <- sample(1:16000,size=932,replace=F)
q <- sample(c(0,0.5,1),size=15068,replace=T) # vector of length 15068
A <- C[id, -id] # matrix of dimension 932 * 15068
B <- C[-id, -id] # matrix of dimension 15068 * 15068
p <- runif(932,0,1)
r <- runif(15068,0,1)
C<-NULL #save some memory space</pre>
```

```
# get size of A & B
size_of_a <- object.size(A)
size_of_a <- object.size(B)

#microbenchmark(y = p + (A%*%inv(B)) %*% (q - r))
#solve(B)</pre>
```

Part a.

How large (bytes) are A and B? Without any optimization tricks, how long does the it take to calculate y?

Part b.

How would you break apart this compute, i.e., what order of operations would make sense? Are there any mathmatical simplifications you can make? Is there anything about the vectors or matrices we might take advantage of?

Part c.

Use ANY means (ANY package, ANY trick, etc) necessary to compute the above, fast. Wrap your code in "system.time({})", everything you do past assignment "C <- NULL".

Problem 3

a.)

```
# create function
prob_successes <- function(x){

# sum where x is logically equivalent to 1 meaning success and divide by length of vector
return <- sum(x == 1) / length(x)
return(return)
}</pre>
```

b.)

```
set.seed(12345)
P4b_data <- matrix(rbinom(10, 1, prob = (31:40)/100), nrow = 10, ncol = 10, byrow = FALSE)
P4b_data</pre>
```

```
##
          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
    [1,]
             1
                   1
                         1
                               1
                                     1
                                          1
                                                1
                                                            1
                                                                   1
##
   [2,]
             1
                   1
                         1
                                          1
                                                1
                                                            1
                               1
                                     1
                                                      1
                                                                   1
##
   [3,]
             1
                   1
                                    1
                                                                   1
                               1
   [4,]
##
             1
                   1
                         1
                               1
                                    1
                                          1
                                                1
                                                      1
                                                            1
                                                                   1
##
    [5,]
             0
                   0
                         0
                               0
                                    0
                                          0
                                                0
                                                                   0
                                                                   0
##
   [6,]
             0
                   0
                         0
                               0
                                    0
                                          0
                                                0
                                                            0
   [7,]
                   0
                         0
                                    0
                                          0
                                                0
                                                                   0
             0
                               0
##
    [8,]
             0
                   0
                         0
                                    0
                                          0
                                                0
                                                      0
                                                            0
                                                                   0
                               0
## [9,]
             1
                   1
                         1
                               1
                                    1
                                          1
                                                1
                                                      1
                                                            1
                                                                   1
## [10,]
             1
                   1
                               1
                                    1
                                          1
                                                            1
                                                                   1
```

```
# prob of success by columns
apply(P4b_data, 2, prob_successes)
```

```
# prob of success by rows
apply(P4b_data, 1, prob_successes)
```

```
## [1] 1 1 1 1 0 0 0 0 1 1
```

c.) the column proportions are all 0.6. And the row propotions are either 1 or 0. Which tells us that some of the row have no successes.

d.)

```
# create function for coin flips
coin_flips <- function(x){
    # input prob into rbinom and create 10 column vector
    vector <- matrix(rbinom(10, 1, prob = x), nrow = 1, ncol = 10, byrow = FALSE)
    return(vector)
}

# get probablities ready
prob_matrix <- c(rep(0.6,10))

# apply function to our prob matrix
matrix_we_want <- sapply(prob_matrix, coin_flips)

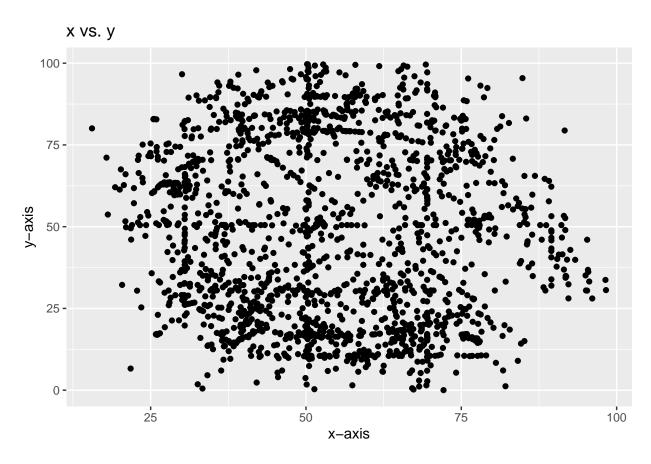
# prob of success by columns
apply(matrix_we_want, 2, prob_successes)

## [1] 0.8 0.6 0.5 0.6 0.6 0.3 0.6 0.7 0.4 0.4

# prob of success by rows
apply(matrix_we_want, 1, prob_successes)</pre>
```

Problem 4

[1] 0.3 0.7 0.5 0.4 0.6 0.8 0.2 0.6 0.7 0.7



```
# plot each one by observer
sapply(split(hw3_data_df, "Observer"), plot_function)
```

```
##
               Observer
## data
               List,3
               List,1
## layers
## scales
## mapping
               List,2
## theme
               List,0
## coordinates ?
## facet
## plot_env
## labels
               List,3
# did not get apply function to work
\#ggplot(hw3\_data\_df,\ aes(x=x,y=y))\ +\ geom\_point()\ +\ facet\_wrap(Observer^{\sim}.)
```

Problem 5

```
#read in data, looks like sql dump, blah
states <- fread(input = "us_cities_and_states/states.sql"</pre>
                 ,skip = 23
                 ,sep = "',"
                 , sep2 = ","
                 , header = F
                 , select = c(2,4))
# adjust everything to lower so we can do analysis later
states$V2 <- tolower(states$V2)</pre>
# read in cities
cities <- fread(input = "us_cities_and_states/cities.sql"</pre>
                 , skip = 23
                 ,sep = "',"
                 , sep2 = ","
                 , header = F
                 , select = c(2,4))
# get first 50 cities
cities <- cities[1:50,]
```

Part b.) Create a summary table of the number of cities included by state.

```
# number of cities by state
knitr::kable(head(dplyr::count(cities, V4)))
```

V4	r
$\overline{\mathrm{AL}}$	2
CA	1
CT	1
GA	1
ID	1
IL	1

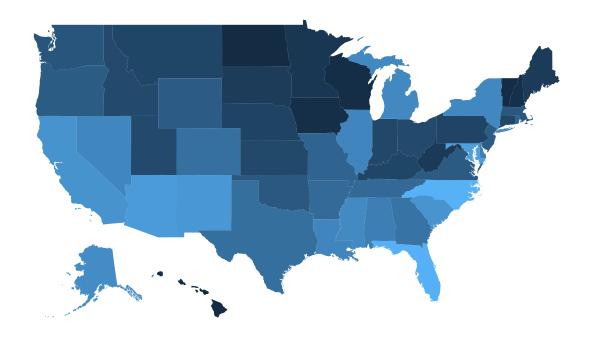
Part c.)

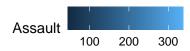
```
# create function to count occurances of letter
letter_counter <- function(letter, state_name){
    # use regex to find the matching letter in state name
    lengths(regmatches(state_name, gregexpr(letter, state_name)))
}</pre>
```

Create a for loop to loop through the state names imported in part a. Inside the for loop, use an apply family function to iterate across a vector of letters and collect the occurance count as a vector.

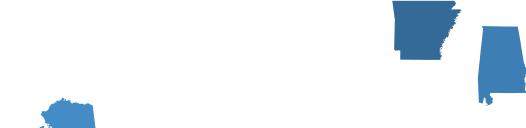
```
letter_count <- data.frame(matrix(NA, nrow=50, ncol=51))
# loop to count occurances of letters in state names
for(i in c("a")){</pre>
```

```
vector <- letter_counter(i,states$V2)</pre>
}
# print vector of counts
vector
## [39] 2 1 2 2 0 1 1 1 0 1 0 1 0
# grab states with 3 or more "a"s
a_states <- states[1:3,]</pre>
Part d.)
data("fifty_states") # this line is optional due to lazy data loading
crimes <- data.frame(state = tolower(rownames(USArrests)), USArrests)</pre>
# map_id creates the aesthetic mapping to the state name column in your data
p <- ggplot(crimes, aes(map_id = state)) +</pre>
  # map points to the fifty_states shape data
  geom_map(aes(fill = Assault), map = fifty_states) +
  expand_limits(x = fifty_states$long, y = fifty_states$lat) +
  coord_map() +
  scale_x_continuous(breaks = NULL) +
  scale_y_continuous(breaks = NULL) +
 labs(x = "", y = "") +
 theme(legend.position = "bottom",
       panel.background = element_blank())
```

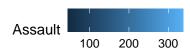




```
# grab a states found in vector
a_states_data <- fifty_states %>% filter(fifty_states$id == "alaska"
                                         | fifty_states$id == "alabama"
                                         | fifty_states$id == "arkansas")
# plot only a states
p2 <- ggplot(crimes, aes(map_id = state)) +</pre>
  # map points to the fifty_states shape data
  geom_map(aes(fill = Assault), map = a_states_data) +
  expand_limits(x = a_states_data$long, y = a_states_data$lat) +
  coord_map() +
  scale_x_continuous(breaks = NULL) +
  scale_y_continuous(breaks = NULL) +
  labs(x = "", y = "") +
  theme(legend.position = "bottom",
        panel.background = element_blank())
p2
```







Problem 2

Part a.

He forgot to name the columns in df08.

library(quantreg)

```
## Loading required package: SparseM
##
## Attaching package: 'SparseM'
## The following object is masked from 'package:base':
##
## backsolve
```

library(quantmod)

```
## Loading required package: xts
## Loading required package: zoo
```

```
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
##
## Attaching package: 'xts'
## The following objects are masked from 'package:dplyr':
##
       first, last
## The following objects are masked from 'package:data.table':
##
##
       first, last
## Loading required package: TTR
## Registered S3 method overwritten by 'quantmod':
##
     method
                       from
     as.zoo.data.frame zoo
## Version 0.4-0 included new data defaults. See ?getSymbols.
#1) fetch data from Yahoo
#AAPL prices
apple08 <- getSymbols('AAPL', auto.assign = FALSE, from = '2008-1-1', to =
"2008-12-31")[,6]
## 'getSymbols' currently uses auto.assign=TRUE by default, but will
## use auto.assign=FALSE in 0.5-0. You will still be able to use
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")
## and getOption("getSymbols.auto.assign") will still be checked for
## alternate defaults.
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.
#market proxy
rm08<-getSymbols('^ixic', auto.assign = FALSE, from = '2008-1-1', to =
"2008-12-31")[,6]
#log returns of AAPL and market
logapple08<- na.omit(ROC(apple08)*100)</pre>
logrm08<-na.omit(ROC(rm08)*100)</pre>
#OLS for beta estimation
beta_AAPL_08<-summary(lm(logapple08~logrm08))$coefficients[2,1]
```

```
#create df from AAPL returns and market returns
df08<-cbind(logapple08,logrm08)
# added this line
colnames(df08) <- c("logapple08", "logrm08")

set.seed(666)
Boot=1000
sd.boot=rep(0,Boot)
for(i in 1:Boot){
# nonparametric bootstrap
bootdata=df08[sample(nrow(df08), size = 251, replace = TRUE),]
sd.boot[i] = coef(summary(lm(logapple08~logrm08, data = bootdata)))[2,1]
}</pre>
```

Part b.

Bootstrap the analysis to get the parameter estimates using 100 bootstrapped samples. Make sure to use system.time to get total time for the analysis. You should probably make sure the samples are balanced across operators, ie each sample draws for each operator.

```
url <- "http://www2.isye.gatech.edu/~jeffwu/wuhamadabook/data/Sensory.dat"
#sensory data <- fread(url, fill=TRUE, header=TRUE)</pre>
#saveRDS(sensory_data, "sensory_data_raw.RDS")
sensory_df <- readRDS("sensory_data_raw.RDS")</pre>
# remove first row
tidyverse_sensory_df <- slice(sensory_df[2:31])</pre>
# Remove column full of na's
tidyverse_sensory_df <- select(tidyverse_sensory_df, -Operator)</pre>
# seperate values
tidyverse_sensory_df <- tidyverse_sensory_df %>%
                           separate(col=V1
                                     ,into=c("Item", "1", "2", "3", "4", "5")
                                     , sep=" "
                                     , fill="left")
# remove first column since its missing values
tidyverse_sensory_df <- select(tidyverse_sensory_df, -Item)</pre>
# add item column
tidyverse_sensory_df <- tidyverse_sensory_df %>%
                                 add_column("Item" = c(1,1,1,2,2,2,3,3,3,4,4,4
                                                        ,5,5,5,6,6,6,7,7,7,8,8,8
                                                        ,9,9,9,10,10,10)
                                             , .before = "1")
# gather all the year values into one column
tidy_tidyverse_sensory_df <- tidyverse_sensory_df %>% gather(key="Operator"
                                                                , value="Value", "1","2"
                                                                , "3", "4", "5")
```

```
# show tidy data
knitr::kable(tidy_tidyverse_sensory_df[1:5,])
```

Item	Operator	Value	
1	1	4.3	
1	1	4.3	
1	1	4.1	
2	1	6.0	
2	1	4.9	

```
# get rid of item value
test_df <- tidy_tidyverse_sensory_df[,2:3]

set.seed(54161)
Boot <- 1000
sd.boot <- rep(0,Boot)

time_results1 <- system.time(
    for(i in 1:Boot){
        # nonparametric bootstrap
        bootdata=test_df[sample(nrow(test_df), size = 150, replace = TRUE),]
        sd.boot[i] = coef(summary(lm(Operator~Value, data = bootdata)))[2,1]
    })

# store results
result_set1 <- t(data.matrix(time_results1))
rownames(result_set1) <- c("org")</pre>
```

Part c.

This can be done because each sample in the bootstrap is independent of the each other. The code runs significantly faster.

```
# set cores
cores <- detectCores() - 1

# create cluster
c1 <- makeCluster(cores)

# register cluster
registerDoParallel(c1)

# run in parallel
time_results2 <- system.time(
    foreach(i=1:Boot, combine = 'c') %dopar% {
        # nonparametric bootstrap
        bootdata=test_df[sample(nrow(test_df), size = 150, replace = TRUE),]
        sd.boot[i] = coef(summary(lm(Operator~Value, data = bootdata)))[2,1]
        })</pre>
```

```
# stopping cluster
stopCluster(c1)

# store results in a data frame and rename row
result_set2 <- t(data.matrix(time_results2))
rownames(result_set2) <- c("bootstrap")

# combine results
final_results <- rbind(result_set1, result_set2)

# print table
knitr::kable(final_results)</pre>
```

	user.self	sys.self	elapsed	user.child	sys.child
org	2.2	0.03	2.24	NA	NA
bootstrap	0.0	0.00	0.06	NA	NA

Problem 3

Part a.

```
# create function for newtons method
newtons_method_func <- function(x){

# input the equation
eq <- (3^x) - sin(x) + cos(5*x)

# store the derivative
derivative_eq <- -5*sin(5*x)-cos(x)+log(3)*3^x

# calculate the next term
x_n1 <- x - (eq/derivative_eq)

return(x_n1)
}

# create vector of values
long_vector <- seq(from = -500, to = 500, by=1)

# apply function to vector
system.time(sapply(long_vector, newtons_method_func))

## user system elapsed</pre>
```

```
## user system elapsed ## 0.01 0.00 0.02
```

Part b.

```
# set cores
cores <- detectCores() - 1

# create cluster
c1 <- makeCluster(cores)

# use Sapply
system.time(parSapply(c1,long_vector, newtons_method_func))

## user system elapsed
## 0 0 0

# stopping cluster
stopCluster(c1)</pre>
```

makeCluster(8).

Create a table summarizing the roots and timing from both parts a and b. What are your thoughts?

Problem 9

Finish this homework by pushing your changes to your repo.

Only submit the .Rmd and .pdf solution files. Names should be formatted $HW4_pid.Rmd$ and $HW4_pid.pdf$