$$\log\log n/\log d + O(1)$$