MATH 2554	(Calculus	I)
Spring 2016		

Name:			

Fri 8 Apr 2016

Exam 3: Applications and Story Problems (§3.10-4.6)

Exam Instructions: You have 50 minutes to complete this exam. Justification is required for all problems. Notation matters! You will also be penalized for missing units and rounding errors. calcula

No electronic devices (phones, iDevices, computers, etc) except for a basic scientificator . On story problems, round to one decimal place.
In addition, please provide the following data
Drill Instructor:
Drill Time:

Your signature below indicates that you have read this page and agree to follow the Academic Honesty Policies of the University of Arkansas.

Signature:	(1 p	t)

Good luck!

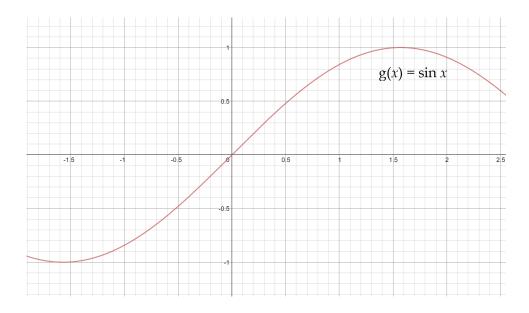
- 1. (a) (5 pts) Explain why Rolle's Theorem cannot be applied to the function f(x) = |x| on the interval [-a, a] for any a > 0.
 - (b) (3 pts) Is there any interval where Rolle's Theorem applies to f(x)? Why or why not?
 - (c) (3 pts) Is there any interval where the Mean Value Theorem applies to f(x)? Why or why not?
- 2. (12 pts) Suppose you own a tour bus and you book groups of 20 to 70 people for a day tour. The cost per person is \$30 minus 25¢ for every ticket sold. If gas and other miscellaneous costs are \$200, how many tickets should you sell to maximize your profit?

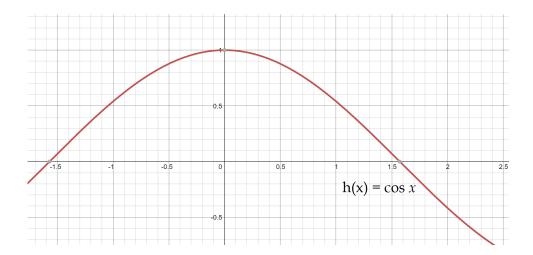
3. (a) (3 pts) Write the equations for the linear approximation to $g(x) = \sin x$ and $h(x) = \cos x$ at x = 0.

$$\sin x \approx$$

$$\cos x \approx$$

- (b) (3pts) Use your answers to (a) to approximate $\sin(0.1)$ and $\cos(0.1)$.
- (c) (5 pts) The following are the respective graphs of $\sin x$ and $\cos x$, drawn at the website desmos.com/calculator. On each graph, draw your tangent line. Label both your approximations from (b) and the exact values $\sin (0.1)$ and $\cos (0.1)$.





4. (12 pts) Two cylindrical swimming pools are being filled simultaneously at the same rate (in m³/min). The smaller pool has a radius of 5m, and the water level rises at a rate of 0.5m/min. The larger pool has a radius of 8m. How fast is the water level rising in the larger pool?

5. The goal of this problem is to produce a graph of the function

$$f(x) = \tan^{-1} x^3$$

from scratch.

(a) (2 pts) Find the domain for f(x).

(b) (2pts) Is f(x) even, odd, or neither? You must justify your answer.

(c) (4 pts) Find f'(x) and f''(x). You are not required to simplify.

(d) (3 pts) Find the critical points. If there are none, then say why.	
(e) (3 pts) Find the possible inflection points. If there are none, then say why.	
(f) (3 pts) What are the intervals where $f(x)$ is increasing? What are the intervals where $f(x)$ is decreasing?	ervals

(g)	(3 pts) What are the intervals where where $f(x)$ is concave down?	f(x)	is concave	up?	What	are th	e intervals
(h)	(4 pts) Find the local extrema and infl. If there are no extrema or inflection po						ır answers.

- (i) (4 pts) Use all the information above, plus the following facts, to draw a well-labeled graph of f(x). Your picture should be consistent with your answers to (a)-(h).
 - f(x) has no vertical asymptotes, but it has horizontal asymptotes at $y = \pm \frac{\pi}{2}$.
 - f(x) intersects the origin.