

Quiz 11: Antiderivatives (§4.8, 5.2, 5.3)

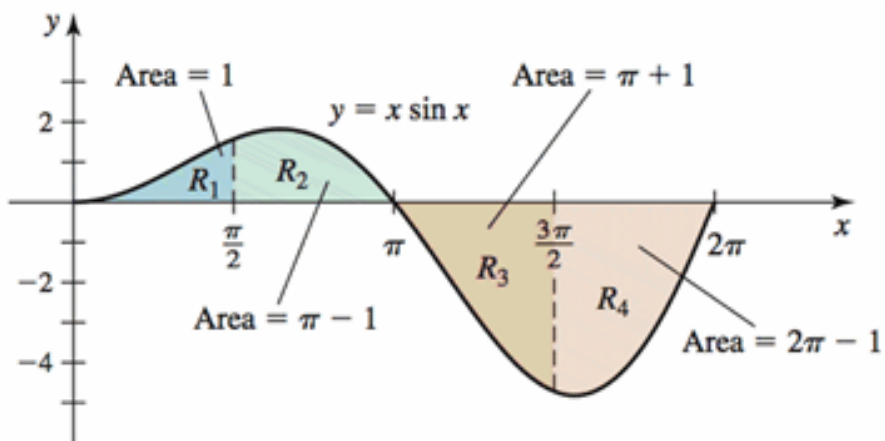
Directions: You have 30 minutes to complete this quiz. Collaborative and open book.

1. A mass oscillates up and down on the end of a spring. Find its position s relative to the equilibrium position if its acceleration is

$$a(t) = \sin(\pi t),$$

and its initial velocity and position are $v(0) = 3$ and $s(0) = 0$, respectively.

2. Use the picture to evaluate:



(a) $\int_0^{\frac{3\pi}{2}} x \sin x \, dx$

(b) $\int_{\frac{\pi}{2}}^{2\pi} x \sin x \, dx$

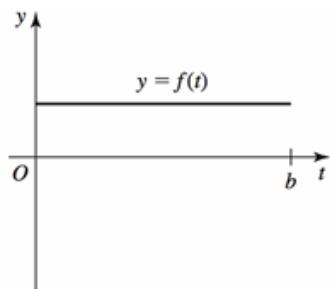
3. Use the Fundamental Theorem of Calculus to simplify the following expressions:

(a) $\frac{d}{dy} \int_{y^2}^{100} \frac{dw}{w^2 + 1}$

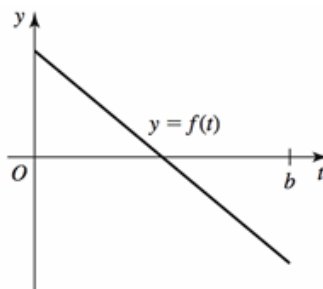
(b) $\frac{d}{dx} \int_1^x e^t \, dt$

4. Match the functions f whose graphs are given in (a)-(d) with the area functions

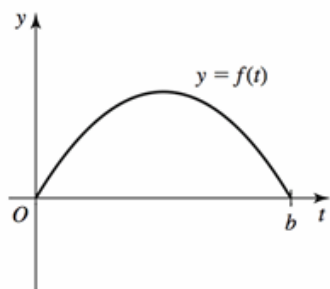
$$A(x) = \int_0^x f(t) \, dt, \quad \text{whose graphs are given in (A)-(D).}$$



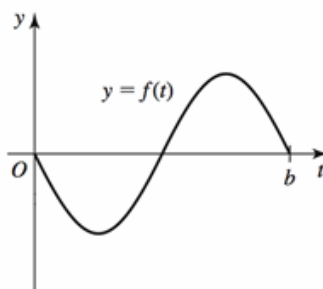
(a)



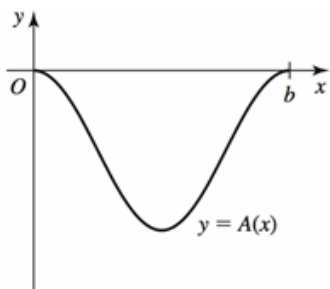
(b)



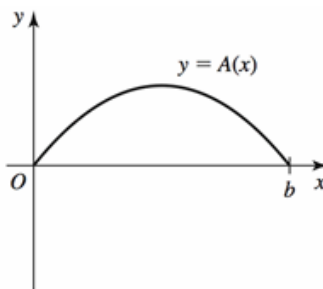
(c)



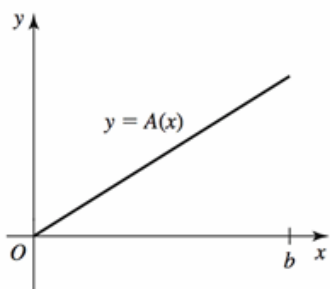
(d)



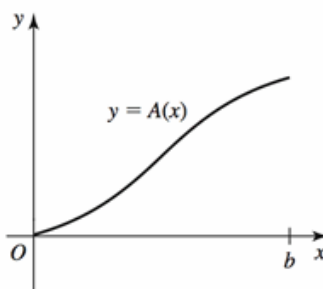
(A)



(B)



(C)



(D)