

§ 2.3

11

$$\bullet \lim_{x \rightarrow 3} \frac{x^2 - x - 6}{x^2 - 9} = \lim_{x \rightarrow 3} \frac{(x - 3)(x + 2)}{(x - 3)(x + 3)}$$

$$= \lim_{x \rightarrow 3} \frac{x + 2}{x + 3} = \frac{3 + 2}{3 + 3} = \frac{5}{6}$$

$$\bullet \lim_{\theta \rightarrow 0} \frac{\sec \theta + \tan \theta}{\theta} = \lim_{\theta \rightarrow 0} \frac{\frac{1}{\cos \theta} \cdot \frac{\sin \theta}{\cos \theta}}{\theta}$$

$$= \lim_{\theta \rightarrow 0} \frac{1}{\cos^2 \theta} \cdot \frac{\sin \theta}{\theta}$$

$$= \left( \lim_{\theta \rightarrow 0} \frac{1}{\cos^2 \theta} \right) \left( \lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} \right)$$

$$= \frac{1}{\cos^2(0)} \cdot 1$$

$$= 1$$

§ 2.6

12

$$0 \leq x \leq 2$$

$$f(x) = \begin{cases} x^2 + k & 0 \leq x \leq 1 \\ -2kx + 4 & 1 < x \leq 2 \end{cases}$$

$f$  is a polynomial on  $[0, 1]$  and on  $(1, 2]$ , so the only point to check for continuity is  $x = 1$ :

$$f(1) = (1)^2 + k = 1 + k$$

$$\lim_{x \rightarrow 1^-} f(x) = 1 + k \text{ because}$$

$$\lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^+} -2kx + 4$$

$$= -2k(1) + 4 = -2k + 4$$

$$\lim_{x \rightarrow 1} f(x) = 1 + k = -2k + 4$$

$$3k = 3$$

$$\boxed{k = 1}$$

$$y = 3x + 2 \text{ tan to } f(x) \quad x = 1 \quad \S 3.2$$

13

$$y = -5x + 6$$

$$g(x) \quad x = 1$$

$$h(1) = f(1)g(1)$$

$$h(x) = f(x)g(x)$$

$$h'(x) = f'(x)g(x) + f(x)g'(x)$$

$$h'(1) = f'(1)g(1) + f(1)g'(1)$$

$$(3)(1) + 5(-5)$$

$$= 3 - 25 = -22$$

$$| y - 5 = -22(x - 1) |$$



$$\frac{f(x)}{f(y)} \quad \text{with a crossed-out } y$$

$$\frac{d}{dx}(\sin x = \sin y) \quad \S 3.7$$

$$\frac{d}{dx}(\cos x = \frac{dy}{dx} \cdot \cos y) \Rightarrow \frac{dy}{dx} = \frac{\cos x}{\cos y} \quad \text{with a crossed-out } y$$

$$-\sin x = \left( \frac{d^2 y}{dx^2} \right) \cdot \cos y + \frac{dy}{dx} (-\sin y) \frac{dy}{dx}$$

§ 3.4

14

$$\bullet f(x) = (1 + \sec x) \sin^3 x$$

$$f'(x) = (0 + \sec x \tan x) \sin^3 x$$

$$+ (1 + \sec x)(3 \sin^2 x \cos x)$$

$$\bullet g(x) = \frac{\sin x + \cot x}{\cos x}$$

$$= \frac{\sin x}{\cos x} + \frac{\cot x}{\cos x} = \frac{\sin x}{\cos x} + \frac{\cancel{\cos x}}{\sin x} \left( \frac{1}{\cancel{\cos x}} \right)$$

$$= \tan x + \csc x$$

$$g'(x) = \sec^2 x - \csc x \cot x$$

§3.7

Find  $\frac{dz}{dw}$  for

$$e^{2w} = \sin(wz)$$

$$\frac{d}{dw} [e^{2w} = \sin(wz)]$$

$$2e^{2w} = \cos(wz) \left[ (w) \frac{dz}{dw} + (1)z \right]$$

$$= (\cos(wz)) w \frac{dz}{dw} + (\cos(wz)) z$$

$$\Rightarrow \frac{dz}{dw} = \frac{2e^{2w} - z \cos(wz)}{w \cos(wz)}$$