Math 2554 Exam 3:	$\oint 3.8 - 4.5$
Friday 3 April 2015	

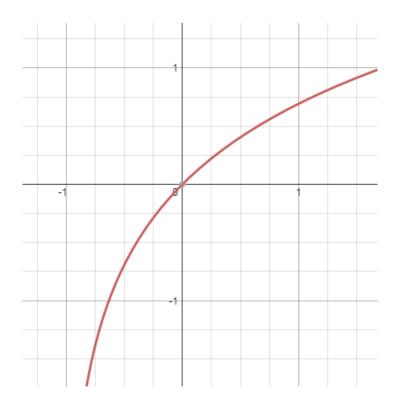
Name:			

Calculus I Exam 3: The Story Problem Exam

Please provide the following data:
Drill Instructor:
Drill Time:
Student ID or clicker #:
Exam Instructions: You have 50 minutes to complete this exam. One 3×5 inch notecard, one side only, is allowed. No graphing calculators. No programmable calculators. No electronic devices except for the approved calculators (so no phones, iDevices, computers, etc). If you finish early then you may leave, UNLESS there are less than 5 minutes of class left. To prevent disruption, if you finish with less than 5 minutes of class remaining then please stay seated and quiet.
Your signature below indicates that you have read this page and agree to follow the Academic Honesty Policies of the University of Arkansas.
Signature: (1 pt)

- 1. (3 pts ea) Let $g(x) = \ln(1+x)$.
 - (a) Write the equation for the linear approximation to g(x) at x = 0.

- (b) Use your answer to (a) to approximate g(0.9).
- (c) Below is the graph of g(x), drawn at the website desmos.com/calculator. On the same axis, draw your tangent line. Label both g(0.9) and your approximation from part (b).



2. (13 points) Your boss keeps cookies on the top shelf there but there is a hole in the bag. The cookies are spilling, accumulating in a cone-shaped pile whose radius (r) is always three times the cone's height (h). Your boss won't eat the cookies once they fall out of the bag. If the height of the pile is increasing at a rate of 2 cm/s when the pile is 12 cm high, how fast is your boss losing his eat-able cookies in that instant?

The volume of the cone is $V = \frac{1}{3}\pi r^2 h$. Round your final answer to one decimal place (if you try to tell your boss a number with π in it, he will likely get confused and angry!).

3. (2 pts ea) Evaluate. You do not need to simplify your answers. Hint: In some of these problems it is quicker if you remember the properties of logs.

(a)
$$\frac{d}{dy}\log_2\frac{8}{\sqrt{y+1}}$$

(b)
$$\frac{d}{du} \tan^{-1} \left(e^{4u} \right)$$

(c)
$$\frac{d^n}{dx^n} 2^x$$
 (n is a positive integer)

4. The goal of this problem is to produce a graph of the function

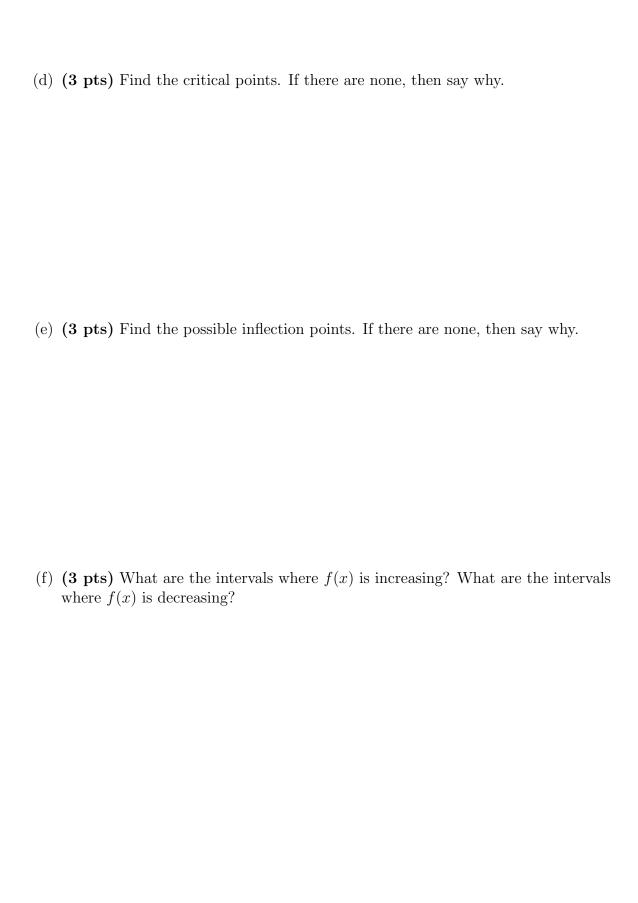
$$f(x) = xe^{-x}$$

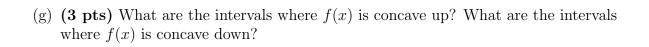
from scratch.

(a) (2 pts) Find the domain for f(x).

(b) (2pts) Is f(x) even, odd, or neither? You must justify your answer.

(c) (4 pts) Find f'(x) and f''(x). You are not required to simplify.





(h) (4 pts) Find the local extrema and inflection points. You must justify your answers. If there are no extrema or inflection points you should also say why.

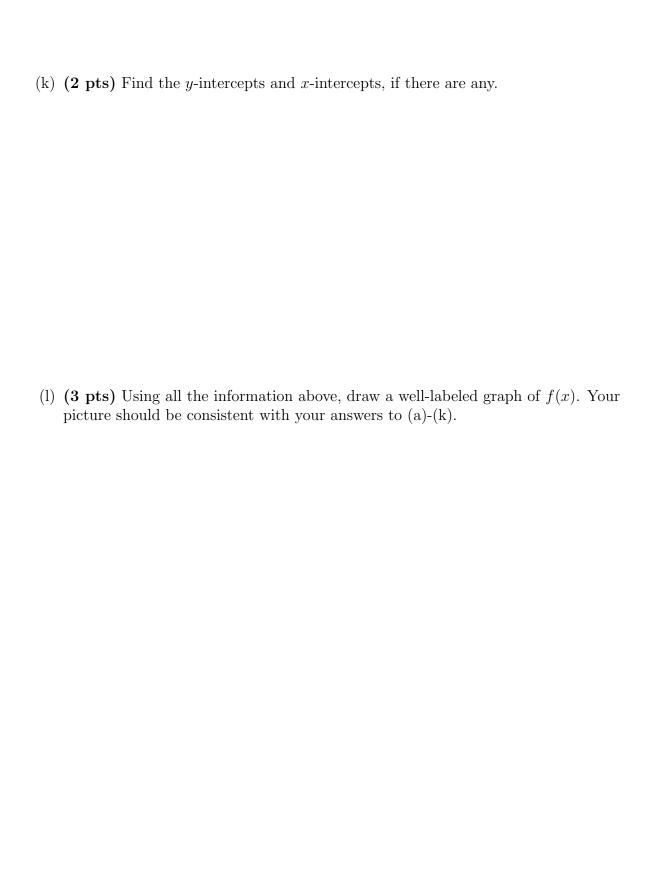
(i) (2 pts) Find the vertical asymptotes, using the limit definition of a vertical asymptote. If there are no vertical asymptotes, then say so.

(j) (2 pts) Determine the end behavior.

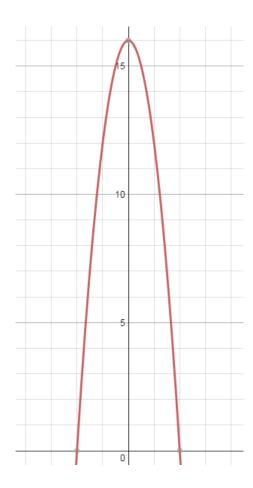
Hint: By L'ôpital's Rule ($\oint 4.7$),

$$\lim_{x \to \infty} x e^{-x} = \lim_{x \to \infty} \frac{1}{e^x}.$$

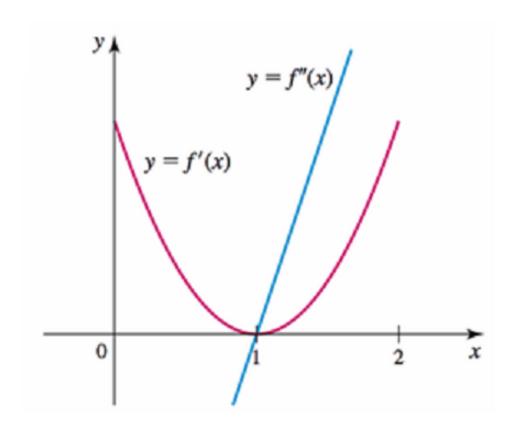
For $\lim_{x\to -\infty} f(x)$ you do not need L'ôpital's Rule.



5. (13 points) A rectangle is constructed with its base on the x-axis and two of its corners on the parabola $y = 16 - 4x^2$. What are the dimensions of the rectangle with the maximum area? Hint: The picture of the parabola is given (using desmos. com/calculator).



6. ChAlLeNgE pRoBlEm (0 pts) Using the graphs of f' and f'', draw a possible graph for f(x) on the same axes, assuming f(0) = 0. Hint: Use the picture to find intervals where f is increasing/decreasing, concave up/down, critical points, inflection points, etc.



taken from Calculus: Early Transcendentals, Briggs et al.