

In-Class Quiz 3: Limits and continuity (§12.3)

Directions: This quiz is due at the end of lecture.

1. Which of the following limits exist?

(a) $\lim_{(x,y) \rightarrow (1,1)} 3x^{12}y^2$

$= 3(1)^{12}(1)^2 = 3$ exists.

(b) $\lim_{(x,y) \rightarrow (0,0)} 3x^{-2}y^2 = \lim_{(x,y) \rightarrow (0,0)} \frac{3y^2}{x^2}$. Let $(x,y) \rightarrow (0,0)$ along the line $y=mx$.

$= \lim_{(x,mx) \rightarrow (0,0)} \frac{3(mx)^2}{x^2} = \lim_{(x,y) \rightarrow (0,0)} \frac{3m^2x^2}{x^2} = 3m^2 \leftarrow$ different for different values of m

(c) $\lim_{(x,y) \rightarrow (1,2)} \underbrace{\sqrt{x-y^2}}_{\text{defined on the set } \{(x,y) \mid x \geq y^2\}}$

\Rightarrow does not exist.

Since $(1,2)$ is not an interior or boundary point of that set, the limit does not exist.