Math 115 Quiz 4: \oint 2.5-6 and Barehanded Differentiation

You have 25 minutes to complete this quiz. Calculators are OK.

1. **Definitions/Concepts.** (1 pt) Let g be the function defined by

$$g(x) = \begin{cases} 1 & \text{if } x \le 0\\ \cos x & \text{if } 0 < x < \frac{\pi}{2}\\ 0 & \text{if } x > \frac{\pi}{2} \end{cases}.$$

Which of the following statements are true? Check all that apply.

- (a) g is continuous at x = 0
- (b) g is continuous at $x = \frac{\pi}{2}$
- (c) g is differentiable at x = 0
- (d) g is differentiable at $x = \frac{\pi}{2}$
- 2. **Questions/Problems.** A Purple-Headed Uniquely Nocturnal Chartreuse And Luridly Colored wombat is sighted moving across the diag. Its position, measured in feet from the West Engineering arch, is given as a function of time (in minutes past midnight) in the following table.

- (a) (4 pts) Estimate the wombat's velocity at t = 0, t = 5, t = 10 and t = 15.
- (b) (2 pts) Estimate the wombat's acceleration at t = 5 and t = 10.
- (c) (1 pt) What do you think happened between t = 25 and t = 30?
- 3. **Computations/Algebra.** (2 pts) Use the limit definition of the derivative to compute the following. You *must* show all steps.

$$\frac{d}{dx}\left(\frac{x^2+3}{x^9}\right)$$