

## Exam 1: Intro to Multidimensional Calculus (§11.1-11.7, 12.1-12.2)

**Exam Instructions:** You have 50 minutes to complete this exam. Justification is required for all problems. No electronic devices (phones, iDevices, computers, etc) except for a **basic scientific calculator**. On story problems, round to one decimal place. If you finish early then you may leave, **UNLESS** there are less than 5 minutes of class left. To prevent disruption, if you finish with less than 5 minutes of class remaining then please stay seated and quiet.

In addition, please provide the following data:

Drill Instructor: \_\_\_\_\_

Drill Time: \_\_\_\_\_

Your signature below indicates that you have read this page and agree to follow the Academic Honesty Policies of the University of Arkansas.

Signature: (1 pt) \_\_\_\_\_

Good luck!

## Exam 1: Intro to Multidimensional Calculus

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1. Determine whether the following statements are true or false. You must justify your answer.

(a) (5 pts) The domain of the function  $u = f(w, x, y, z)$  is a region in  $\mathbb{R}^4$ .

(b) (5 pts)  $(\mathbf{u} \times \mathbf{v}) \cdot \mathbf{v} = 0$

(c) (5 pts) The domain of the function  $f(x, y) = 1 - |x - y|$  is  $\{(x, y) \mid x \geq y\}$ .

(d) (5 pts) All level curves of the plane  $z = 2x - 3y$  are lines, except for when  $z = 0$ .

2. (18 pts) Determine an equation of the line that is perpendicular to the lines

$$\mathbf{r}(t) = \langle -1 + 3t, 3t, 2t \rangle$$

$$\mathbf{R}(s) = \langle -6 + 3s, -8 + 2s, -12 + s \rangle$$

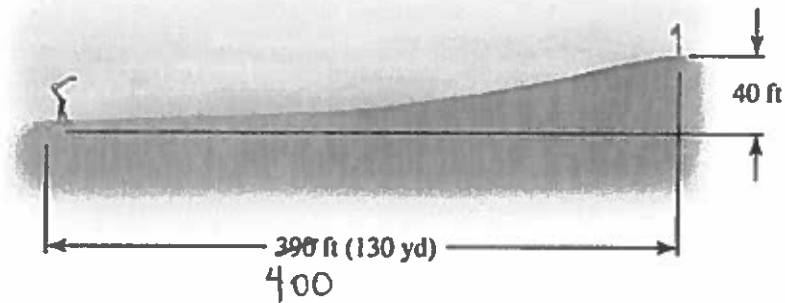
and passes through the point of intersection of the lines  $\mathbf{r}$  and  $\mathbf{R}$ .

3. Suppose  $\mathbf{u}$  and  $\mathbf{v}$  are differentiable functions at  $t = 0$  with  $\mathbf{u}(0) = \langle 1, 0, 1 \rangle$ ,  $\mathbf{u}'(0) = \langle 7, 0, 1 \rangle$ ,  $\mathbf{v}(0) = \langle 0, 1, 1 \rangle$ ,  $\mathbf{v}'(0) = \langle 1, 3, 2 \rangle$ . Evaluate the following expressions:

(a) (6 pts)  $\left. \frac{d}{dt}(\sin(t)\mathbf{u}(t)) \right|_{t=0}$

(b) (6 pts)  $\left. \frac{d}{dt}(\mathbf{u} \cdot \mathbf{v}) \right|_{t=0}$

4. A golfer stands 400 ft horizontally from the hole and 40 ft below the hole (see figure).

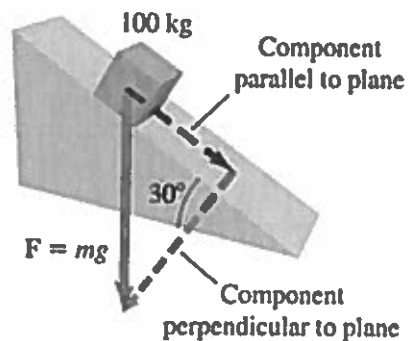


Suppose the ball is hit with an initial speed of 150 ft/s, at an angle of  $\theta$  from the ground.

- (a) **(12 pts)** Find the acceleration  $\mathbf{a}(t)$ , velocity  $\mathbf{v}(t)$ , and position  $\mathbf{r}(t) = \langle x(t), y(t) \rangle$  vectors for the trajectory of the ball. The gravitational constant is  $g = 32 \text{ ft/s}^2$ .

- (b) **(6 pts)** Write down a system of two equations to find the two unknowns: (1) time of flight and (2)  $\theta$ . **Do not** solve the system.

5. (16 pts) A 100 kg box rests on a ramp with an incline of  $30^\circ$  to the floor (see figure). Find the components of the force perpendicular to and parallel to the ramp. (The vertical component of the force exerted by an object of mass  $m$  is its weight, which is  $mg$ , where  $g = 9.8 \text{ m/s}^2$  is the acceleration due to gravity.)



6. (15 pts) Match equations (a)-(f) with the surfaces (A)-(F).

(a)  $y = |x|$

(b)  $3x - 4y - z = 5$

(c)  $y - z^2 = 0$

(d)  $4x^2 + \frac{y^2}{4} + z^2 = 1$

(e)  $x^2 + \frac{y^2}{9} = z^2$

(f)  $x^2 + \frac{y^2}{9} - z^2 = 1$

