

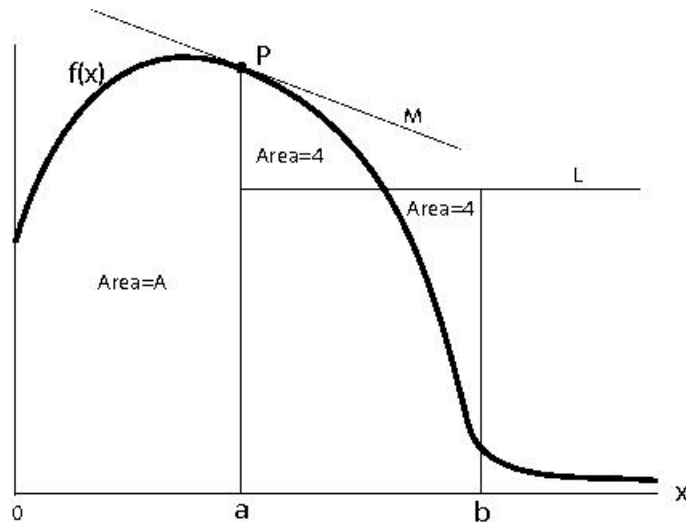
**Math 115 Quiz 10: § 5.1-3 Summing Rectangles**

**Wed 8 December 2010**

**Name:** \_\_\_\_\_

You have 30 minutes to complete this quiz. Make your variables clear and consistent (so if you want to say, for example,  $\frac{dy}{dx}$ , you should also mention  $y = f(x)$ , or “ $y$  is a function of  $x$ ”). Calculators are OK.

1. **Definitions/Concepts.** (1 pt each) True or False? No explanation necessary.
  - (a) For an increasing function, the left-hand sum on a given interval with a given number of subdivisions is always less than the right-hand sum.
  - (b) A 4-term left-hand Riemann sum approximation cannot give the exact value of a definite integral.
  - (c) The units for an integral of a function  $f(x)$  are the same as the units for  $f(x)$ .
2. **Questions/Problems.** Below you will write expressions for each of various quantities indicated on the graph of  $f(x)$ . Your expressions may involve integrals or derivatives. For example, if asked for the “ $x$ -coordinate of the point  $P$ ,” you would write “ $a$ ”.



a) (1 pt) The height (above the  $x$ -axis) of the point  $P$ .

b) (1 pt) The slope of the line  $M$ .

c) (1 pt) The size of the area A.

d) (1 pt) The height of the line L.

**3. Computations/Algebra.**

(a) (1 pt) If  $F(t) = \frac{1}{2} \sin t^2$ , find  $F'(t)$ .

(b) Find  $\int_{0.2}^{0.4} \sin t \cos t dt$  two ways:

(i) (1 pt) Numerically.

(ii) (1 pt) Using the Fundamental Theorem of Calculus.