

Exam 1: Intro to Multidimensional Calculus (§11.1-11.7, 12.1-12.2)

Exam Instructions: You have 50 minutes to complete this exam. Justification is required for all problems. No electronic devices (phones, iDevices, computers, etc) except for a **basic scientific calculator**. On story problems, round to one decimal place. If you finish early then you may leave, **UNLESS** there are less than 5 minutes of class left. To prevent disruption, if you finish with less than 5 minutes of class remaining then please stay seated and quiet.

In addition, please provide the following data:

Drill Instructor: _____

Drill Time: _____

Your signature below indicates that you have read this page and agree to follow the Academic Honesty Policies of the University of Arkansas.

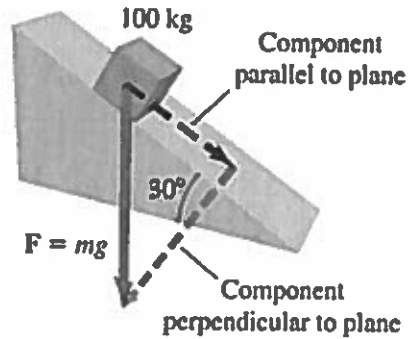
Signature: (1 pt) _____

Good luck!

Exam 1: Intro to Multidimensional Calculus

Exam 1:

1. (16 pts) A 100 kg box rests on a ramp with an incline of 30° to the floor (see figure). Find the components of the force perpendicular to and parallel to the ramp. (The vertical component of the force exerted by an object of mass m is its weight, which is mg , where $g = 9.8 \text{ m/s}^2$ is the acceleration due to gravity.)



2. Determine whether the following statements are true or false. You must justify your answer.

(a) (5 pts) The domain of the function $f(x, y) = 1 - |x - y|$ is $\{(x, y) \mid x \geq y\}$.

(b) (5 pts) $\mathbf{u} \cdot (\mathbf{u} \times \mathbf{v}) = 0$

(c) (5 pts) The domain of the function $u = f(w, x, y, z)$ is a region in \mathbb{R}^3 .

(d) (5 pts) All level curves of the plane $z = 2x - 3y$ are lines.

3. (18 pts) Determine an equation of the line that is perpendicular to the lines

$$\mathbf{r}(t) = \langle -2 + 3t, 2t, 3t \rangle$$

$$\mathbf{R}(s) = \langle -6 + s, -8 + 2s, -12 + 3s \rangle$$

and passes through the point of intersection of the lines \mathbf{r} and \mathbf{R} .

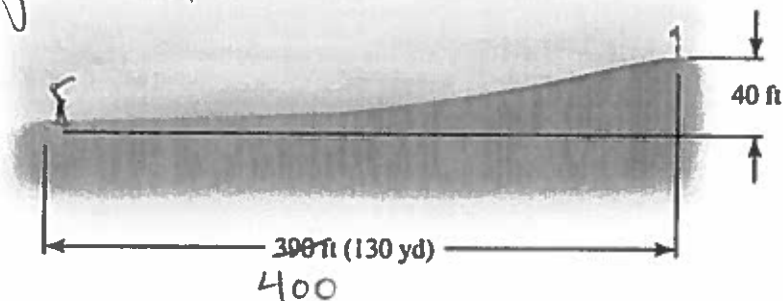
4. Suppose \mathbf{u} and \mathbf{v} are differentiable functions at $t = 0$ with $\mathbf{u}(0) = \langle 0, 1, 1 \rangle$, $\mathbf{u}'(0) = \langle 0, 7, 1 \rangle$, $\mathbf{v}(0) = \langle 0, 1, 1 \rangle$, $\mathbf{v}'(0) = \langle 1, 1, 2 \rangle$. Evaluate the following expressions:

(a) (6 pts) $\left. \frac{d}{dt}(\mathbf{u} \cdot \mathbf{v}) \right|_{t=0}$

(b) (6 pts) $\left. \frac{d}{dt}(\cos(t)\mathbf{u}(t)) \right|_{t=0}$

5. A golfer stands 400 ft horizontally from the hole and 40 ft below the hole (see figure).

$$\text{gravity} = g = 32 \text{ ft/s}^2$$



Suppose the ball is hit with an initial speed of 150 ft/s, at an angle of θ from the ground.

- (a) (12 pts) Find the acceleration $\mathbf{a}(t)$, velocity $\mathbf{v}(t)$, and position $\mathbf{r}(t) = \langle x(t), y(t) \rangle$ vectors for the trajectory of the ball.

- (b) (6 pts) Write down a system of two equations to find the two unknowns: (1) time of flight and (2) θ . Do not solve the system.

6. (15 pts) Match equations (a)-(f) with the surfaces (A)-(F).

(a) $y - z^2 = 0$

(b) $4x^2 + \frac{y^2}{9} + z^2 = 1$

(c) $x^2 + \frac{y^2}{9} = z^2$

(d) $2x - 3y - z = 5$

(e) $x^2 + \frac{y^2}{9} - z^2 = 1$

(f) $y = |x|$

